## Notes 2

#### June 27, 2017

Let's try to think about this more generally. We want to design and experiment for red queen hypothesis and perform power analysis.

# 1 Empirical studies

What I should be looking at:

• From Auld et al. (2016): "heritable component, rapid parasite evolution, and temporally shifting parasite-mediate selection"

### 1.1 Not Red queen?

• Michiels et al. (2001) says that their system does not match requirements of the red queen hypothesis (weak infection fitness cost). They think that there might be other factors involved.

### 2 Model

#### 2.1 Notes

Michiels et al. (2001): heterozygote triploids are hard to distinguish so di-allelic representation is used Lively (2001) suggests that prevalence is actually not a good measure. Risk of infection (probability of exposure to ifective parasite propagules) is a better measure. Near the *switch point*, asexuals can have higher

prevalence but this range is fairly narrow.

Hakoyama and Iwasa (2004) tried to model Japanese crucian carp and showed that parasitism may explain the evolution of sex. They also show that coexistence of parthnogenetic complex is more likely than that of gynogenetic complex. Read this paper later to see how we want to analyze our model!

Neiman et al. (2017) emphasizes importance of a pluralist approach and suggests directions. It's worth noting that many of pluralist studies include red queen dynamics. We are being a pluralist because we're adding ecological feedback in the model. I don't think we have to test for power yet as there aren't many appropriate systems but it might still be important and interesting to compare power for pluralist idea vs. red queen alone. See Meirmans and Neiman (2006) for testing interactive effects.

Agrawal and Lively (2002) says that dynamical qualities of matching alleles model can be observed across other continuum. We can just stick with MA for now.

Agrawal (2009) says GFG model failed to show selection for sex or recombination in diploid model. In MA and IMA models, recombination was often more favored than sex. However, they also saw cases where sex was favored but recombination was not. Using a haploid model can be misleading.

#### 2.2 Deterministic model

We simulate red queen dynamics based on matching alleles (MA) model using diploid hosts and haploid parasites. Instead of using modifier genes, we model obligate asexual and sexual population explicitly. Assuming there are two biallelic loci, there are four types of gametes that can be produced: AB, Ab, aB, ab. We will be using indices 1-4 for simplicity to refer to these gametes (Agrawal and Otto, 2006).

Let  $A_{ij}$  and  $S_{ij}$  represent density of total asexual and sexual population with genotype ij. Following Lively (2010), we can write

$$S'_{ii} = (1 - s)S_0(g_i^2)[W_I P_{ij} + W_U(1 - P_{ij})],$$
  

$$S'_{ij} = (1 - s)S_0(2g_i g_j)[W_I P_{ij} + W_U(1 - P_{ij})],$$
  

$$A'_{ij} = A_{ij}[W_I P_{ij} + W_U(1 - P_{ij})],$$

where s is the proportion of male offspring produced,  $S_0$  is the total density of the sexual population,  $g_i$  is the frequency of gamete i before recombination and  $P_{ij}$  is the probability of infection.  $W_I$  and  $W_U$  are modeled in the same way as Lively (2010). After recombination,  $\mu$  individuals enter all sexual genotypes.

Let  $\lambda_i$  be the mean number of poisson mean number of exposures for hosts with genotype ij by parasite with haplotype i, we can write

$$P_{ij} = 1 - \exp(-(\lambda_i + \lambda_j)/2).$$

By doing so, we are assuming that effects of dominance do not exist. Then, we get

$$\lambda_i = \beta \left( \sum_{p} 2_{ip}^{\delta} (S_{ip,i,I} + A_{ip,i,I}) + \kappa \right)$$

To avoid fixation, we assume that new parasites enter the population at a constant rate. Here, density of genotype ip infected with haplotype  $i - S_{ij,i,I}$  and  $A_{ij,i,I}$  is given by

$$S_{ij,i,I} = \frac{\lambda_i(t-1)}{\lambda_i(t-1) + \lambda_j(t-1)} S_{ij,I}, \dots$$

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Study	Host	Parasite	Experiment	Notes
Michiels et al.	Flatworm	Amoeboid proto-	Compare propor-	Highly hetero-
(2001) - Lab	Schmidtea  poly-	zoan (Asexual)	tion of infected in-	geneous spatial
	chroa - obligate		dividuals in mixed	distribution; need
	sexual diploid and		samples with LRT;	longer study
	parthenogenetic		rate of infection	
Kumpulainen et al.	triploid psychid moth	hymenopteran par-	test prevalence of	demonstrates cost
(2004) - Field	psychia moth	asitoids	parasitoids and	of sex; no evi-
( 2 2 )			prevalence of sex-	dence for different
			ual reproduction	reproduction mode
				preferring different
				space
Ben-Ami and	snails	trematodes	correlation for	Male frequencies
Heller (2005) - Field			males and frequency of infection	decreased bu infection levels
ricid			quency of infection	increased
Bruvo et al. (2007)	Planarian flat-	only look at asex-		
- Field	${\bf worm}  \textit{Schmidtea}$	ual; test for infec-		
	polychroa - diploid	tion rates among		
	sexuals and	the clonal lineage;		
	(mostly) triploid parthenogens	relate parasite load and fertility		
Verhoeven and	Dandelions -	Microbial commu-	Experiment +	See geographic
Biere (2013) -	diploid sexual and	nities, fungus, and	testing infection	parthenogenesis;
Field	triploid obligate	weevil	prevalence in	they address that
	apomicts		nature	they might have a
Č: 1 / 1	O:1 1 1		· · · ·	power problem
Simková et al. (2013)	Gibel carp - sexual diploid and gyno-	metazoan para- sites	Comparison of MHC genes: do	"Coexistence may be maintained by
(2013)	genetic triploid	Sites	sexual individu-	male mate choice
	genetic triploid		als have higher	or spatial and tem-
			variability + do	poral extinction
			asexual invidiauls	and recoloniza-
			suffer from higher	tion"; need longer
A 11 / 1 (001c)	D 1 : 41	D / '	parasite load	study
Auld et al. (2016) - Lab	Daphnia - partly sexual and asexual	Pasteuria ramosa	Time shift experiment (testing	Unrealistic setting in nature; their
Lab	sexual aliu asexual		for proportion	in nature; their study looks at
			of infected and	within-host factors
			spores per host)	
			with MCMCglmm	
Clawingle: -4 -1	Cae nor hab dit is	Commati ~	Introduction	paragita has to 1
Slowinski et al. (2016)	Caenorhabditis elegans -	$Serratia \ marcescens$	Introduction of mixed mating	parasite has to be coevolving
(2010)	hermaphrodite	marcescens	into outcrossing	cocvorving
	and obligate		population and	
	sexual		exposing different	
			types of parasites	
			- test selfing rates using ANOVA	
			using ANOVA	