

# Notes on evolution of sexual reproduction

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## 1 Introduction (mostly based on Otto (2009))

Hartfield and Keightley (2012) also provides a good review.

Also see Lehtonen et al. (2012) for review on cost of sex.

We want to understand the evolution of sexual reproduction and model the freshwater snail system studied by Vergara et al. (2014). Otto (2009) provides a fairly recent review in this field.

There are a few disadvantages to sexual reproduction (Otto, 2009):

- partner searching, resource gathering, transmission of STD, and predation while mating.
- Only 50% of the parent gene is passed down to its offspring (often referred to as the cost of sex (Bell, 1982)).
- Recombination may alter favourable gene combination (Nei, 1967).

Despite such costs, sexual reproduction is a widespread phenomenon among eukaryotic organisms. One of the oldest explanation for sex is that it increases variation (Weissmann, 1889) but this is a misconception (Otto, 2009). Not only does sexual reproduction can decrease variation but variation generated through sex can also reduce fitness (segregation load). So why does sex exist?

### 1.1 Earlier models

- Focused on modifier genes but found that selection acts against sex and recombination at equilibrium (Feldman et al., 1996). This idea applies even when sexual reproduction does not have any cost. Maybe it's important to consider nonequilibrium situations!
- In an evolving population, modifiers increasing levels of recombination may be selected if "fitness surfaces were negatively curved on a multiplicative scale" (Barton, 1995; Charlesworth, 1990). However, these models are limited because negative fitness surface imposes fitness load. Moderately negative fitness curvature is necessary (Otto, 2003).
- Evidence is not consistent with this idea and the allowed curvature parameter is too narrow to be likely.

## 1.2 Recent models

### Varying selection over time (Red Queen)

- In a rapidly changing environment, segregation and recombination can increase fitness of near descendants by dissociating detrimental genetic association (Salathé et al., 2008).
- Under antagonistic interaction, species must evolve fast enough so that remain in pace with the interacting species (Red Queen) (Bell, 1982).
- Limitations: (1) selection must be quite strong in haploid populations; (2) In diploid populations, where form of selection does not cycle, genetic association built up by past selection never becomes detrimental and segregation does not provide any benefit. See Otto (2009) for more sources.
- Red queen is still beneficial when (1) parasites originate from close relatives and (2) it is "a source of ongoing selection". See Otto (2009) for more sources.

### Varying selection over space

- In a spatially heterogeneous environment, recombination can mitigate detrimental genetic association from migration. See Otto (2009) for more sources.
- See Salathe et al 2006 and Martin et al 2006

### Rates of sex vary among individuals

- Many organisms are more likely to engage in sex when they are in poor condition (e.g. *Daphnia*). See Otto (2009) for more sources.
- "Models that have investigated the evolution of condition-dependent sex have found it much easier for sex to evolve if individuals in worse condition allocate more resources to sexual reproduction than do individuals in good condition" (Otto, 2009).
- "Ineffective at selecting for recombination in diploid individuals" (Agrawal et al., 2005).

### Selection in finite population

- In an infinite population, recombination is not required to combine advantageous mutations. This is not the case in a finite population. See Otto (2009) for more sources.
- Muller's ratchet (Muller, 1964).

- In asexual populations, genome containing both advantageous mutants would occur on the order of  $1/\sqrt{N\mu^2}$  generations, whereas sexual population takes  $1/(RN\mu^2/3)^{1/3}$  order of generations (Christiansen et al., 1998).
- Hill-Robertson effect. See Hartfield and Keightley (2012) for more sources.
- (1) Results are less sensitive to epistasis; (2) population size does not need to be too small; and (3) can explain combination of selection (e.g. deleterious mutations and the Red Queen (Howard et al., 1994)).
- Not very clear whether this explanation is strong enough.

## 2 Red Queen

See Hartfield and Keightley (2012) for a review of the history of the Red Queen hypothesis.

See Gandon and Otto 2007 and Barton 2010....

Modifiers spread due to delayed short-term benefit

Recent paper by Slowinski et al. (2016) provides an experimental work on RQH. Study is based on three treatments: avirulent pathogen treatment, fixed pathogen treatment, and coevolving pathogen treatment. Asexual failed to invade the last group but managed to persist with a low frequency in some population (See (Agrawal and Lively, 2001) for the theoretical model).

Agrawal and Lively (2001) present four allele matching host-parasite models that can be used for our models. They do not include gene-for-gene interaction models (see cited papers for further detail). They assume infinite size so we should consider finite size model.

See Otto and Nuismer (2004) for broader model.

See Vergara et al 2014 for periodicity...

See Ashby and King (2015) for a stochastic model on RQH. They find that sex is more likely to persist when there is more genetic diversity in the population only if transmission rate is high enough. If transmission rate is low, high genetic diversity selects against sex. Their result may seem to contrast that of Lively (2010) because their model allows for the effects of drift but it is actually consistent. This paper also summarizes all the other model studies, which might be helpful. See supplementary materials for the code.

See Ashby and Gupta (2014) for a deterministic model. Also see May and Anderson (1983) for an old model.

## 3 Snails

There's a lot going on in the snails population. Here are some things we want to consider for the model:

- Some old papers on snails: (?)

- See Dybdahl and Lively (1998) for time-lagged selection.
- Spatial structure within/among lakes (geographic mosaic theory) (King et al., 2009). There's also fine scale spatial heterogeneous prevalence around the lake, more than one-third of which can be explained by variation in mean susceptibility (we certainly need to use a model with more than two loci) (Gibson et al., 2016). See McKone et al. (2016) for red-queen related stuff.
- Genetic diversity among different lakes - multiple loci is probably necessary to produce enough genetic diversity
- Life cycle of the parasite. Do we need to model ducks as well? We might also have to model the sexual reproduction of the parasites (HECHINGER, 2012)
- Finite population (stochastic) vs. infinite population (deterministic)
- Continuous time vs. discrete time (See Lively (2010))
- Cost of sex. A very recent paper by Gibson et al. (2017) show that snail population support two-fold cost of sex (or slightly greater based on MLE). They also found that asexual females produce more offspring than sexual females.

## 4 Model

Dybdahl and Lively (1998) provides a model for asexual snails and sexual parasite but is too simple...

Let's model sexual and asexual individuals in the absence of parasites first. We're going to use two alleles for each of the two loci. Then, there are four types of gametes that can be produced:  $AB, Ab, aB, ab$ . We will be using indices 1–4 for simplicity (Agrawal and Otto, 2006).

The number of sexual individuals with genotype  $ij$  is given by  $S_{ij}$ . Then, we can model  $S_{ij}$  in the next generation as follows:

$$\begin{aligned} S'_{ii} &= F_0(M_i F_i) W_U \\ S'_{ij} &= F_0(M_i F_j + M_j F_i) W_U, \end{aligned}$$

where  $F_0$  is the number of females  $M_i$  and  $F_i$  are proportion of male and female

gametes with allele  $i$ .

$$\begin{aligned} X_1 &= (\sum_k X_{1k} - rX_{14} + rX_{23}) / (\sum_j X_j), \\ X_2 &= (\sum_k X_{2k} - rX_{23} + rX_{14}) / (\sum_j X_j), \\ X_3 &= (\sum_k X_{3k} - rX_{23} + rX_{14}) / (\sum_j X_j), \\ X_4 &= (\sum_k X_{4k} - rX_{14} + rX_{23}) / (\sum_j X_j), \end{aligned}$$

where  $X$  refers to either male or female and  $r$  is the recombination rate. Then, number of males and females is given by

$$\begin{aligned} M'_{ij} &= sS'_{ij} \\ F'_{ij} &= (1-s)S'_{ij}, \end{aligned}$$

Asexuals are easy to model:

$$A'_{ij} = A_{ij}W_U$$

We follow Lively (2010) and define

$$W_U = \frac{b_U}{1 + (a_U N)^x}.$$

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discrete_par <- c(
  s=0.5,
  r=0.3
)
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