MCMC examples

```
library(MCMCglmm) ## older, Gibbs-sampling
library(brms) ## newest, lme4-like syntax, very flexible, compiled
library(rstanarm) ## lme4-like syntax, pre-compiled
library(lme4) ## to get data
options(brms.backend = "cmdstanr")
library(broom.mixed) ## 'tidy'
library(tidybayes) ## convenience functions for getting MCMC output in 'tidy' format
library(bayesplot)
library(bayestestR) ## diagnostics
library(ggplot2); theme_set(theme_bw())
library(shinystan) ## diagnostics for Stan in a Shiny window
library(tidyverse) ## general-purpose manipulations
```

- a little more on priors:
 - parameter-expanded priors: $y_j|\mu,\xi_j\sim N(\mu+\alpha\sigma_j,\sigma_j^2),\ \sigma_j\sim N(0,\sigma_\xi^2);$ $\alpha\sim N(\alpha_0,\sigma_\alpha),\ \sigma_\alpha\sim \text{inverse-Gamma}(\nu)$

```
df(v/alpha.V, df1 = 1, df2 = nu, ncp = (alpha.mu^2)/alpha.V)
2 * dt(sqrt(v)/sqrt(alpha.V), df = nu, ncp = alpha.mu/sqrt(alpha.V))
```

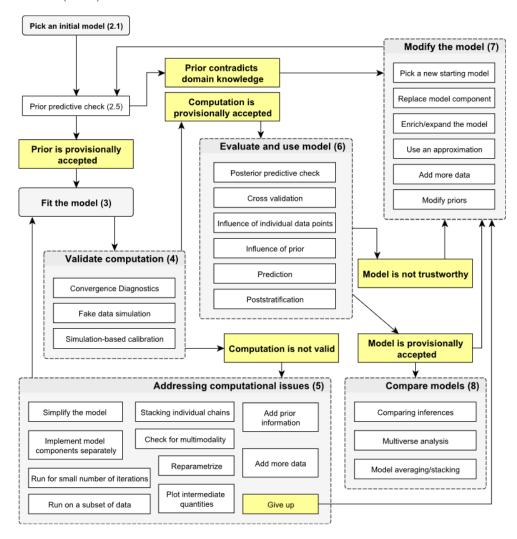
 \dots always set alpha.mu=0, can set V = 1 (or diag() in more complex cases) wlog; sqrt(alpha.V) (scale) and nu are the only relevant parameters

effective sample size

- number of samples, corrected for autocorrelation
- ESS may be > sample size! (e.g. antithetic sampling)
- efficiency of a sampler is not (samples/time), but (effective samples/time)
- effective sample size >1000 for both tail and bulk quantities (Vehtari et al. 2021)

Bayesian workflow

Gelman et al. (2020)



simulation-based calibration

Talts et al. (2020)

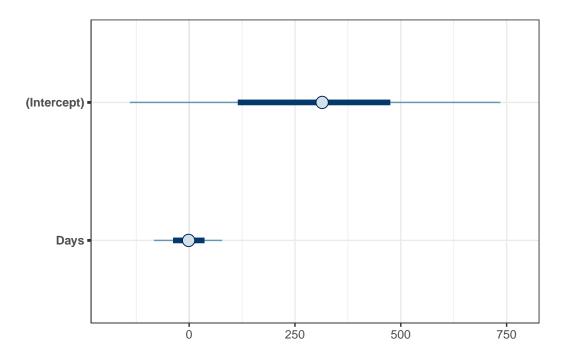
default priors/prior predictive simulations:

• rstanarm default priors

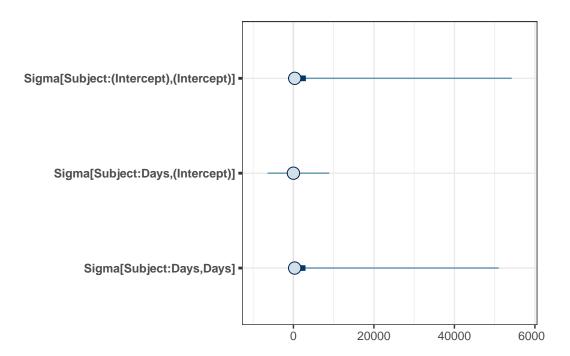
Using the good old sleepstudy example:

```
prior_summary(priorpred)
```

```
Priors for model 'priorpred'
Intercept (after predictors centered)
  Specified prior:
    ~ normal(location = 299, scale = 2.5)
  Adjusted prior:
    ~ normal(location = 299, scale = 141)
Coefficients
  Specified prior:
    ~ normal(location = 0, scale = 2.5)
  Adjusted prior:
    ~ normal(location = 0, scale = 49)
Auxiliary (sigma)
  Specified prior:
    ~ exponential(rate = 1)
  Adjusted prior:
    ~ exponential(rate = 0.018)
Covariance
 ~ decov(reg. = 1, conc. = 1, shape = 1, scale = 1)
See help('prior_summary.stanreg') for more details
plot(priorpred, pars = c("(Intercept)", "Days"))
```



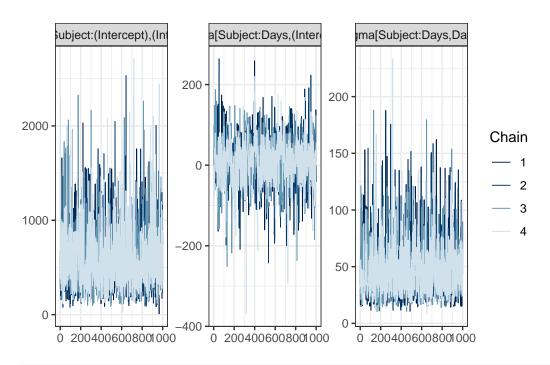
plot(priorpred, regex_pars = "Sigma")



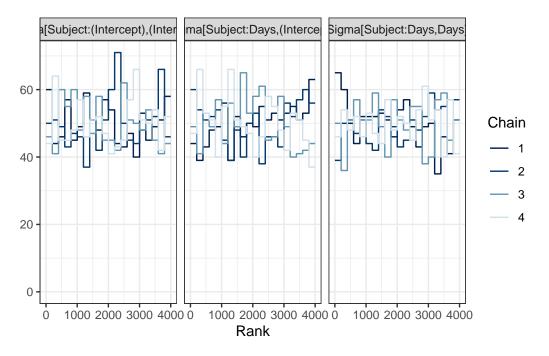
Parameter Rhat ESS MCSE 1 (Intercept) 1.001 2142 0.14337 38 Days 1.002 1353 0.04635

launch_shinystan(stanfit)

mcmc_trace(stanfit, regex_pars= "Sigma")



mcmc_rank_overlay(stanfit, regex_pars= "Sigma")



- MCMC diagnostics
 - trace plots, improved trace plots
 - R-hat Vehtari et al. (2021)
 - divergences (HMC only)

See http://bbolker.github.io/bbmisc/bayes/examples.html

doing stuff with the results

```
tidy(stanfit, effects=c("fixed", "ran_pars"), conf.int = TRUE)
```

```
# A tibble: 6 x 6
  term
                                estimate std.error conf.low conf.high group
  <chr>
                                   <dbl>
                                              <dbl>
                                                       <dbl>
                                                                  <dbl> <chr>
1 (Intercept)
                                251.
                                               6.35
                                                      240.
                                                                  262.
                                                                        <NA>
2 Days
                                 10.4
                                               1.63
                                                                   13.1 <NA>
                                                        7.48
3 sd_(Intercept).Subject
                                 24.2
                                              NA
                                                       NA
                                                                   NA
                                                                        Subject
4 sd_Days.Subject
                                  6.88
                                                                        Subject
                                              NA
                                                       NA
                                                                   NA
5 cor_(Intercept).Days.Subject
                                  0.0735
                                              NA
                                                       NA
                                                                   NA
                                                                        Subject
6 sd_Observation.Residual
                                 26.0
                                              NA
                                                       NA
                                                                   NA
                                                                        Residual
```

ii, why don't we get confidence intervals?? Do it by hand ...

```
(as_draws(stanfit)
    |> tidyr::pivot_longer(everything())
    |> group_by(name)
    |> summarise(estimate = median(value),
                 lwr = quantile(value, 0.025),
                 upr = quantile(value, 0.975))
    |> filter(!stringr::str_detect(name, "^b\\["))
)
# A tibble: 9 x 4
  name
                                          estimate
                                                       lwr
                                                              upr
  <chr>
                                              <dbl> <dbl>
                                                            <dbl>
                                              251.
1 (Intercept)
                                                    238.
                                                            264.
                                                2.5
                                                              4
2 .chain
                                                      1
3 .draw
                                             2000. 101.
                                                           3900.
4 .iteration
                                              500.
                                                     26.0
                                                            975.
5 Days
                                               10.4
                                                      6.92
                                                             13.6
6 Sigma[Subject:(Intercept),(Intercept)]
                                             515. 161.
                                                           1376.
7 Sigma[Subject:Days,(Intercept)]
                                               15.1 -99.4
                                                            109.
8 Sigma[Subject:Days,Days]
                                               42.3 18.0
                                                            107.
9 sigma
                                               25.9 23.1
                                                             29.4
form1 <- Reaction ~ Days + (Days|Subject)</pre>
get_prior(form1, sleepstudy)
```

```
prior
                               class
                                           coef
                                                  group resp dpar nlpar lb ub
                    (flat)
                                    b
                    (flat)
                                    b
                                           Days
                    lkj(1)
                                 cor
                    lkj(1)
                                                Subject
                                  cor
student_t(3, 288.7, 59.3) Intercept
    student_t(3, 0, 59.3)
                                                                           0
                                   sd
    student_t(3, 0, 59.3)
                                                                           0
                                  sd
                                                Subject
    student_t(3, 0, 59.3)
                                  sd
                                           Days Subject
                                                                           0
                                                                           0
    student_t(3, 0, 59.3)
                                   sd Intercept Subject
    student_t(3, 0, 59.3)
                                                                           0
                               sigma
      source
     default
(vectorized)
```

```
default
 (vectorized)
      default
      default
 (vectorized)
 (vectorized)
 (vectorized)
      default
b_prior <- c(set_prior("normal(200, 50)", "Intercept"),</pre>
             set_prior("normal(0, 10)", "b"),
             set_prior("normal(0, 1)", "sigma")
b <- brm(form1, sleepstudy,</pre>
         prior = b_prior,
         seed = 101,
                                  ## reproducibility
         sample_prior = 'only', ## for prior predictive sim
         chains = 1, iter = 500, ## very short sample for convenience
         silent = 2, refresh = 0 ## be vewy vewy quiet ...
p_df <- sleepstudy |> tidybayes::add_predicted_draws(b)
'spaghetti plot' of prior preds
gg0 <- ggplot(p_df,aes(Days, .prediction, group=interaction(Subject,.draw))) +
        geom_line(alpha = 0.1)
b_prior4 <- c(set_prior("normal(200, 5)", "Intercept"),</pre>
              set_prior("normal(0, 2)", "b"),
              set_prior("normal(0, 1)", "sd"),
              set_prior("normal(0, 1)", "sigma")
cc <-capture.output(</pre>
    suppressMessages(
    b_reg <- brm(form1, sleepstudy,</pre>
             prior = b_prior4,
             seed = 101,
             init = 0,
             control = list(adapt delta = 0.95)
             ))
```

I've used suppressMessages to get rid of a lot of messages like

Chain 1 Informational Message: The current Metropolis proposal is about to be rejected because of the following issue: Exception: normal_id_glm_lpdf: Scale vector is inf, but must be positive finite! (in '/tmp/RtmpSSmixI/model-6899b70c2b466.stan', line 74, column 4 to column 55) If this warning occurs sporadically, such as for highly constrained variable types like covariance matrices, then the sampler is fine, but if this warning occurs often then your model may be either severely ill-conditioned or misspecified.

Suppressing all messages is generally a bad idea (it might suppress other messages that you do want to see), but there's no obvious way to suppress just these messages when they occur in the warmup phase, which seems to be a harmless case.

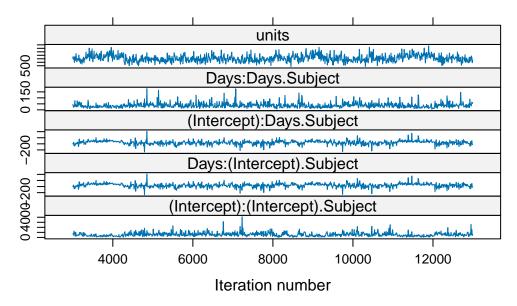
From the Stan forums:

This is common and not a problem, the algorithm explores a large range of values in the warm-up phase and often triggers numerical problems that go away.

```
print(bayestestR::diagnostic_posterior(b_reg),
                                                      digits = 4)
    Parameter
                Rhat ESS
                              MCSE
       b Days 0.9999 3998 0.01643
2 b_Intercept 1.0001 2952 0.05493
## debug(MCMCglmm:::priorformat)
m <- MCMCglmm(Reaction ~ Days, random = ~us(1+Days):Subject,
              data = sleepstudy,
              verbose=FALSE,
              prior = list(G=list(G1=list(V=diag(2), nu = 0.1))))
broom.mixed::tidy(m)
# A tibble: 6 x 5
  effect
           group
                     term
                                            estimate std.error
  <chr>
           <chr>>
                     <chr>
                                               <dbl>
                                                         <dbl>
1 fixed
           <NA>
                     (Intercept)
                                               251.
                                                          6.97
2 fixed
           <NA>
                    Days
                                                10.5
                                                          1.63
3 ran_pars Subject var__(Intercept)
                                               586.
                                                        384.
4 ran_pars Subject
                    cov__(Intercept).Days
                                                         60.9
                                                39.1
5 ran_pars Subject
                    var__Days
                                                37.3
                                                         17.8
6 ran_pars Residual var__Observation
                                               705.
                                                        102.
```

Error in priorformat(if (NOpriorG) { :
 alpha.mu is the wrong length for some prior\$G/prior\$R elements

lattice::xyplot(m2\$VCV)



Run longer (and thin)? Strengthen prior?

to do

- test silencing of brms messages
- improve tidy for rstanarm

- better ways to get draws
- prior pred sims for MCMCglmm? (examples of parameter-expansion)
- SBC examples?
- figure out compilation caching for brms?
- contact Hadfield about MCMCglmm tweaks
- Gelman, Andrew, Aki Vehtari, Daniel Simpson, Charles C. Margossian, Bob Carpenter, Yuling Yao, Lauren Kennedy, Jonah Gabry, Paul-Christian Bürkner, and Martin Modrák. 2020. "Bayesian Workflow." arXiv:2011.01808 [Stat], November. http://arxiv.org/abs/2011.01808.
- Talts, Sean, Michael Betancourt, Daniel Simpson, Aki Vehtari, and Andrew Gelman. 2020. "Validating Bayesian Inference Algorithms with Simulation-Based Calibration." arXiv:1804.06788 [Stat], October. http://arxiv.org/abs/1804.06788.
- Vehtari, Aki, Andrew Gelman, Daniel Simpson, Bob Carpenter, and Paul-Christian Bürkner. 2021. "Rank-Normalization, Folding, and Localization: An Improved R-hat for Assessing Convergence of MCMC (with Discussion)." Bayesian Analysis 16 (2): 667–718. https://doi.org/10.1214/20-BA1221.