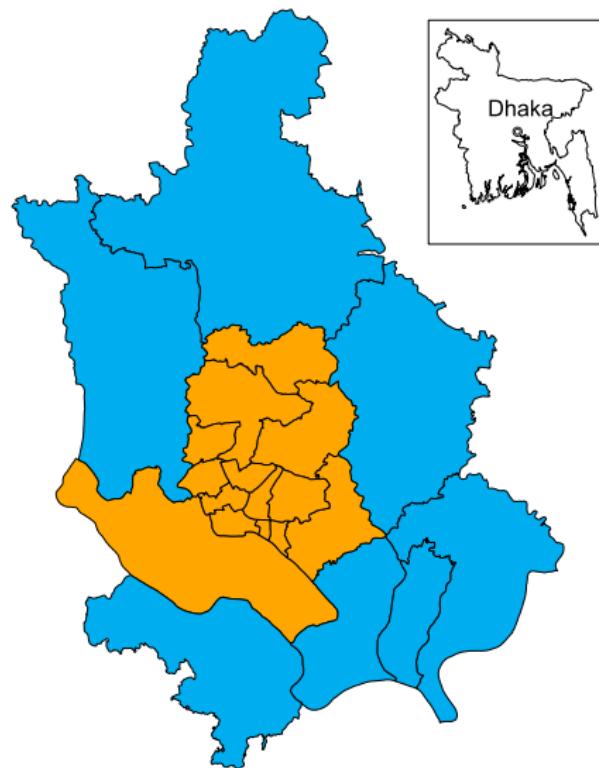


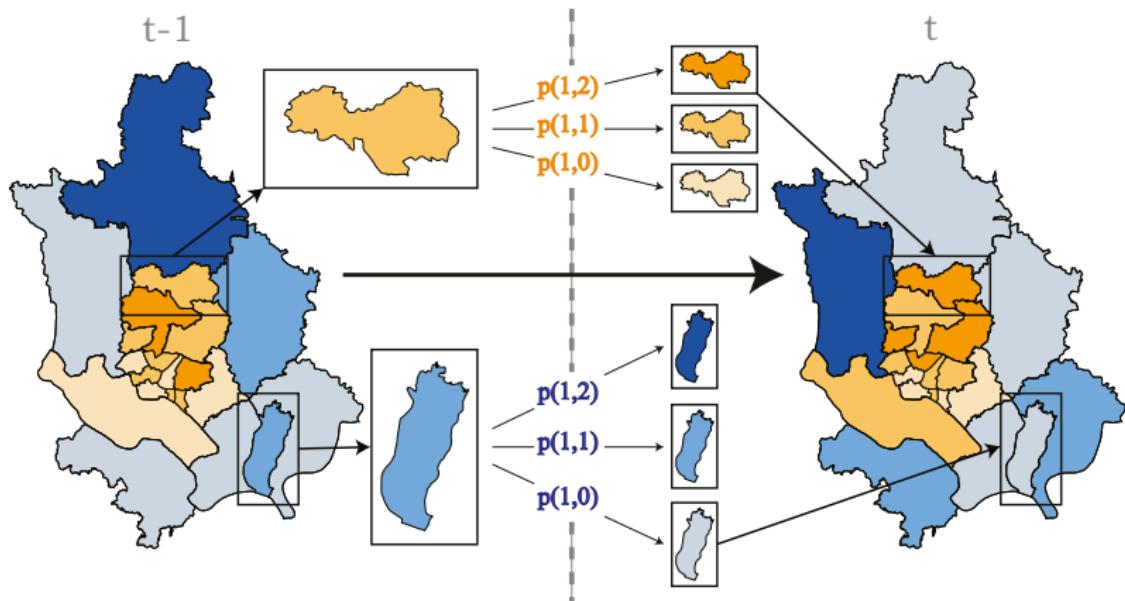
# Cholera in Dhaka





Reiner et al., 2012

# Multidimensional Inhomogenous Markov Chain



Reiner et al., 2012

Basic

Infection

Neighbors

Season

Climate

ENSO

## Transition probabilities

$$p_{i,0,k,t} = \mathbb{P}_{i,0,\mathcal{D}(k)} \times \text{Neigh}(i, 0, \mathcal{V}(k, t - l), \mathcal{D}(k)) \\ \times \text{Seas}(i, 0, t - l, \mathcal{D}(k))$$

$$p_{i,2,k,t} = \mathbb{P}_{i,2,\mathcal{D}(k)} \times \text{Neigh}(i, 2, \mathcal{V}(k, t - l), \mathcal{D}(k)) \\ \times \text{Seas}(i, 2, t - l, \mathcal{D}(k))$$

$$p_{i,l,k,t} = 1 - p_{i,0,k,t} - p_{i,2,k,t}$$

## Neighbors

$$\text{Neigh}(i, j, v, d) = (1 + \alpha_{i,j,d})^v, \quad j = 0, 2$$

## Seasonality

$$\text{Seas}(i, j, t, d) = (1 + \beta_{i,j,d})^{Se(t,d)}, \quad j = 0, 2$$

## Modified transition probability

$$p'_{i,2,k,t} = f(p_{i,2,k,t} \times Nino(t - l, D(k)))$$

$$f(x) = \min(l, \max(0, x))$$

## El Niño

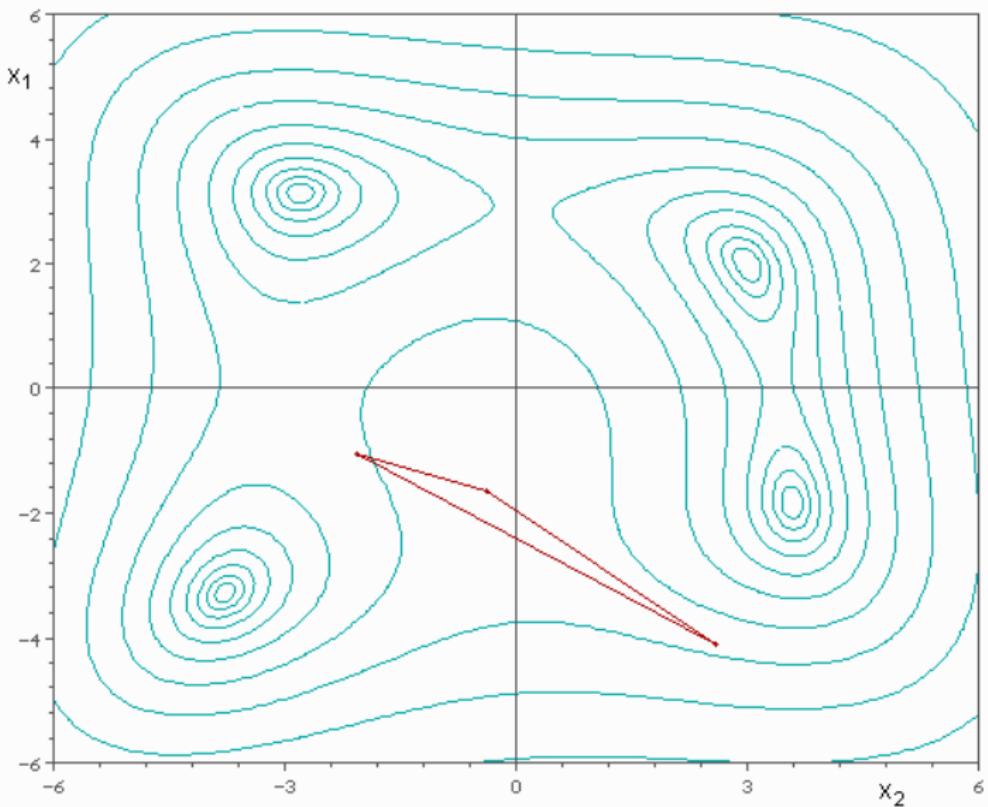
$$Nino(t, d) = l + A_d \frac{\tan\left(\frac{h_d}{2} \cdot \frac{ENSO(t-10)}{M_d}\right)}{\tan\left(\frac{h_d}{2}\right)}$$

## Scaling

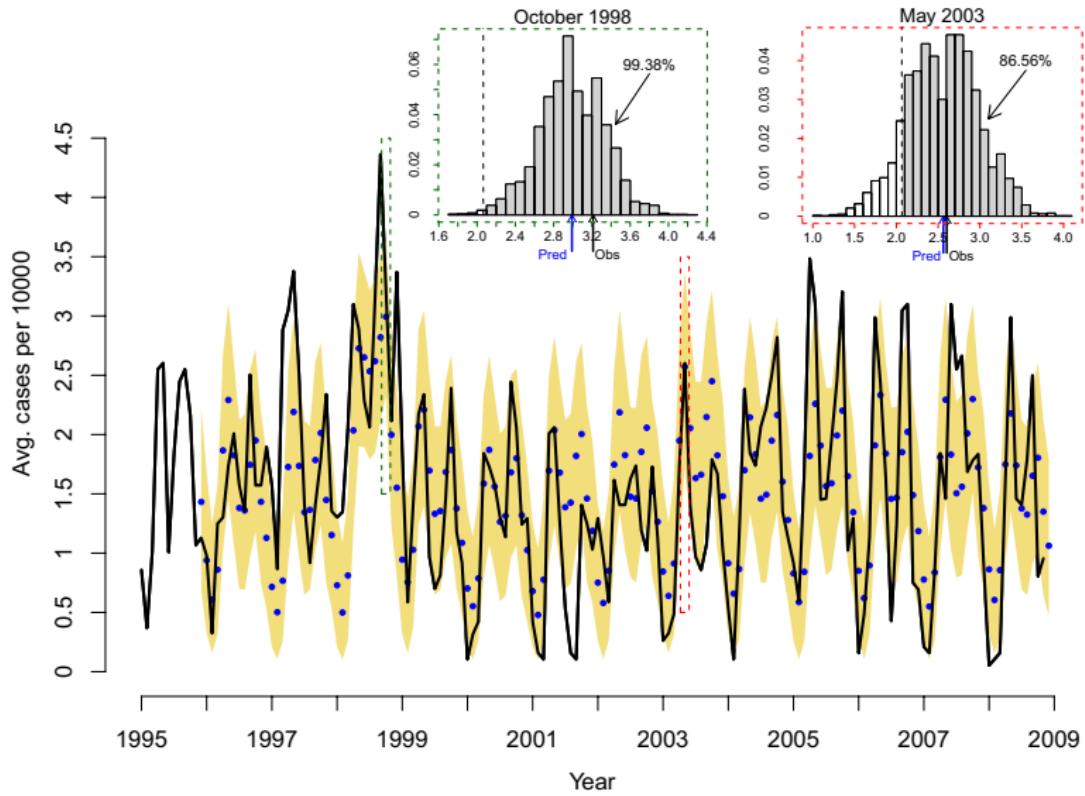
$$p'_{i,0,k,t} = (l - p'_{i,2,k,t}) \frac{p'_{i,0,k,t}}{p'_{i,0,k,t} + p'_{i,l,k,t}}$$

$$p'_{i,l,k,t} = (l - p'_{i,2,k,t}) \frac{p'_{i,l,k,t}}{p'_{i,0,k,t} + p'_{i,l,k,t}}$$

# Model Fitting?



[https://upload.wikimedia.org/wikipedia/commons/9/96/Nelder\\_Mead2.gif](https://upload.wikimedia.org/wikipedia/commons/9/96/Nelder_Mead2.gif)



Reiner et al., 2012

# Spatial SEIR

7

$$\frac{dS_i}{dt} = \mu - \mu S_i - S_i \sum_{j=1}^n \beta_{ij} I_j$$

$$\frac{dE_i}{dt} = S_i \sum_{j=1}^n \beta_{ij} I_j - (\mu + \sigma) E_i$$

$$\frac{dI_i}{dt} = \sigma E_i - (\mu + \gamma) I_i$$

+

$$R_i = I - S_i - E_i - I_i$$

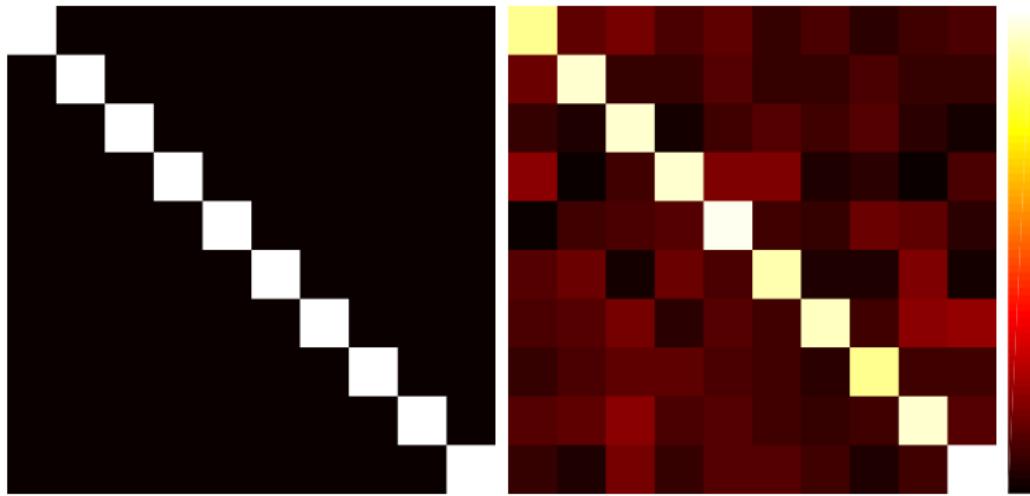
$$\frac{dS_i}{dt} = \mu - \mu S_i - S_i \sum_{j=1}^n \beta_{ij} I_j$$

$$\frac{dE_i}{dt} = S_i \sum_{j=1}^n \beta_{ij} I_j - (\mu + \sigma) E_i$$

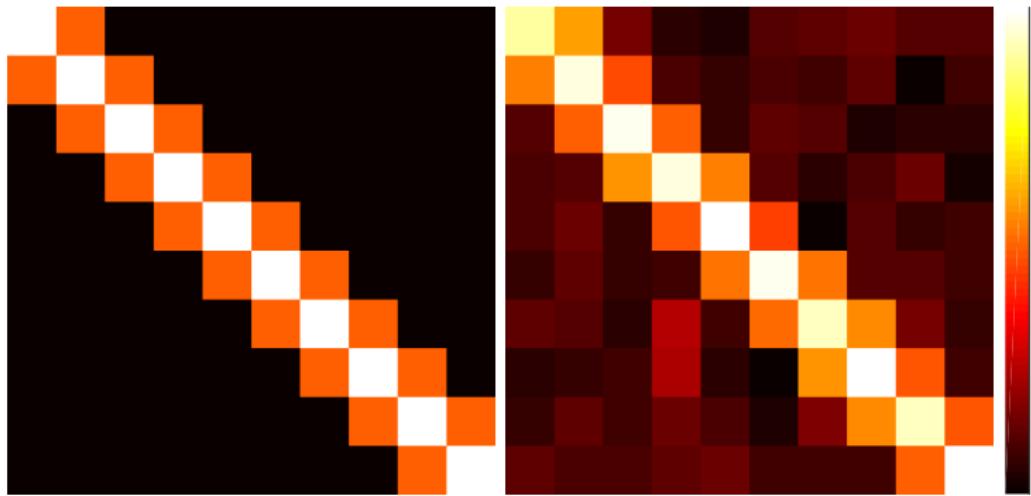
$$\frac{dI_i}{dt} = \sigma E_i - (\mu + \gamma) I_i$$

+

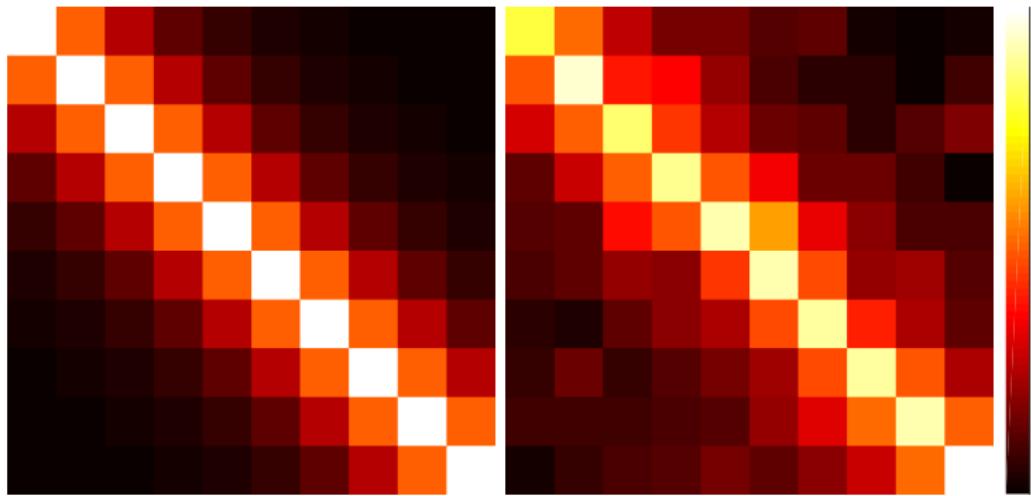
$$R_i = I - S_i - E_i - I_i$$



Isolated



Nearest Neighbour



Exponential Cooling

Making Waves



$$\frac{dS_i}{dt} = -\beta_i S_i I_i \left(1 - \phi \frac{M}{M+I}\right) - \frac{\phi}{M+I} \sum_{j=1}^M \beta_{ij} I_j$$

$$\frac{dI_i}{dt} = \beta_i S_i I_i \left(1 - \phi \frac{M}{M+I}\right) + \frac{\phi}{M+I} \sum_{j=1}^M \beta_{ij} I_j - \gamma I_i$$

$$\frac{dR_i}{dt} = \gamma I_i$$

$$+ \\$$

$$\beta_{i,t+l}=\bar{\beta}_i+\eta\big(\beta_{i,t}-\bar{\beta}_i\big)+\epsilon_{i,t}$$

$$\frac{dS_i}{dt} = -\beta_i S_i I_i \left( 1 - \phi \frac{M}{M+I} \right) - \frac{\phi}{M+I} \sum_{j=1}^M \beta_{ij} I_j$$

$$\frac{dI_i}{dt} = \beta_i S_i I_i \left( 1 - \phi \frac{M}{M+I} \right) + \frac{\phi}{M+I} \sum_{j=1}^M \beta_{ij} I_j - \gamma I_i$$

$$\frac{dR_i}{dt}=\gamma I_i$$

$$+\,$$

$$\beta_{i,t+l} = \bar{\beta}_i + \eta(\beta_{i,t} - \bar{\beta}_i) + \epsilon_{i,t}$$

# Animation!