

# Mental health and lifecycle inequality

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# Roadmap

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Introduction and motivation

Data and preliminary evidence

Lifecycle model

Model estimation and validation

Counterfactuals

## Questions and methods

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How much does mental health (MH) inequality matter for lifetime earnings inequality?

- Estimate a life-cycle model of consumption, labor, wealth with heterogeneous MH
- Run counterfactuals with no MH inequality, compare earnings inequality

Eventually: how much does lifetime earnings inequality matter for mental health inequality?

- Run counterfactuals with no lifetime earnings/labor inequality, compare mental health inequality

Note:

$$Earnings = Employed * Hours * Wage$$

## Today...

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- Describe data and show some descriptives
- Describe and estimate a simple model with exogenous health and wage processes
- Show the current somewhat underwhelming counterfactual
  - Current model misses important moments (extensive labor margin)
- Show a “prototype” counterfactual to contextualize where results are headed
- Hope: feedback on empirics, data, framing etc.
  - What would you like to see in the data to get on board with the model/story?

# Motivation

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- Why Mental Health (MH)?
  - Prevalent and costly (Direct costs, Indirect costs)
  - 1 in 5 adults in US experience mental illness each year (NSDUH) (NIMH)
  - Policy makers care but difficult to evaluate (WHO, 2023), (OECD)
- Why MH and Labor?
  - Mental health care policy evaluation
  - Large (physical) health and lifecycle labor literature
  - Newer MH and lifecycle literature: Abramson et al. (2024), Cronin et al. (2023), Jolivet and Postel-Vinay (2020)

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# SF12 and UKHLS

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Table 12: SF-12 Questionnaire

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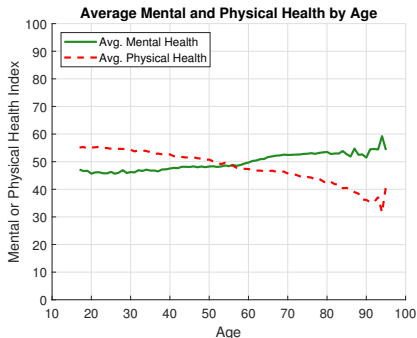
1	How is your health in general?	7	Did your mental health mean you work less carefully?
2	Does your health limit moderate activities?	8	Did the pain interfere with your work?
3	Does your health limit walking up flights of stairs?	9	Did you feel calm and peaceful?
4	Did your physical health limit the amount of work you do?	10	Did you have a lot of energy?
5	Did your physical health limit the kind of work you do?	11	Did you feel downhearted and depressed?
6	Did your mental health mean you accomplish less?	12	Did your health interfere with your social life?

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- UKHLS: Nationally representative survey with income, employment, hours worked, demographics etc.
- SF-12 constructs mental health and physical health indices using principal component analysis
  - shown to be predictive of diagnosis and other health outcomes: Yu et al. (2015), Ohrnberger et al. (2020), Soh et al. (2021).
- Sample is individuals older than 25 in the UK between 2009 and 2020

# Average Health Over the Lifecycle



- Index is standardized to a 50 pt. mean and 10 pt. standard deviation
- Average mental health increases by about 1 standard deviation, while average physical health decreases by about 1.5-2 standard deviations over the lifecycle



# MH affects labor outcomes

Table 1: Mental and Physical Health Quintile Effects and Labor Outcomes

	Year FE				Individ and Year FE			
	Employment	ln(Earnings)	ln(Wage)	ln(Hours)	Employment	ln(Earnings)	ln(Wage)	ln(Hours)
Fair Mental Health	0.198*** (0.008)	0.006 (0.018)	0.012 (0.013)	-0.006 (0.013)	0.033*** (0.005)	-0.001 (0.010)	0.013 (0.009)	-0.014 (0.008)
Good Mental Health	0.269*** (0.009)	0.034 (0.020)	0.032* (0.014)	0.002 (0.014)	0.046*** (0.006)	-0.003 (0.010)	0.016 (0.009)	-0.018* (0.008)
Very Good MH	0.305*** (0.010)	0.087*** (0.022)	0.076*** (0.016)	0.011 (0.015)	0.060*** (0.007)	0.002 (0.012)	0.023* (0.010)	-0.021* (0.009)
Excellent Mental Health	0.320*** (0.007)	0.059*** (0.017)	0.060*** (0.013)	-0.001 (0.012)	0.051*** (0.006)	0.002 (0.010)	0.016 (0.009)	-0.014 (0.008)
Fair Physical Health	0.243*** (0.009)	0.056** (0.017)	0.047*** (0.013)	0.010 (0.012)	0.044*** (0.007)	0.014 (0.009)	0.017* (0.008)	-0.003 (0.008)
Good Physical Health	0.344*** (0.011)	0.073*** (0.017)	0.064*** (0.013)	0.009 (0.013)	0.062*** (0.008)	0.012 (0.010)	0.022* (0.009)	-0.010 (0.008)
Very Good PH	0.351*** (0.013)	0.098*** (0.019)	0.080*** (0.015)	0.018 (0.014)	0.038*** (0.010)	0.017 (0.011)	0.024* (0.010)	-0.008 (0.009)
Excellent Physical Health	0.398*** (0.008)	0.166*** (0.015)	0.140*** (0.011)	0.026* (0.011)	0.060*** (0.007)	-0.001 (0.009)	0.019* (0.008)	-0.020** (0.007)
female	-0.090*** (0.002)	-0.416*** (0.004)	-0.150*** (0.003)	-0.266*** (0.002)	0.002 (0.050)	0.210* (0.082)	0.107* (0.052)	0.104 (0.061)
College	0.070*** (0.003)	0.359*** (0.004)	0.308*** (0.003)	0.051*** (0.002)	0.086*** (0.019)	0.066** (0.021)	0.021 (0.018)	0.045** (0.015)
Observations	142055.000	76858.000	76858.000	76858.000	136652.000	73078.000	73078.000	73078.000
R-Square	0.403	0.320	0.266	0.199	0.810	0.881	0.825	0.790
Adj. R-Square	0.402	0.319	0.265	0.198	0.774	0.857	0.788	0.746

All models control for race, marital status, urban location, and an age cubic.

## Define good and bad

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- For simplicity and congruence with the literature I assume two health states  $H \in \{Bad, Good\}$
- Use regression and Wald tests to inform cutoffs.
- Quantile regressions suggests bottom 40% *Bad*, top 60% *Good*
- Other quantile specifications yield low action relative to the increased complexity
  - Might think there are 3 health states G,A,B

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## Model in one slide: words

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- Households (HH) live  $J$  periods and derive utility from consumption and leisure
- Continuous choices in labor  $n$  (switch to discrete), consumption  $c$ , and future assets  $a'$
- Constrained by expendable income and time endowment
- Exogenous wage and health process
- Wage is quadratic in age and linear in health
- Two health states  $H \in \{Bad, Good\}$ : effects wage  $w_H$  and time endowment  $\phi_H$
- Two permanent types
  - Productivity type  $\gamma$  effects the wage process
  - Health type  $u_H$  which effects health transition probabilities

## Model in one slide: math

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$$V_j(a, \gamma, H, u_H) = \max_{c, n, a'} \{u(c, l) + \beta \mathbb{E}_{H'} V_{j+1}(a', \gamma, H', u_H)\}$$

$$\text{s.t. } c + a' = z(\gamma, j, H) \cdot n + a(1 + r); \forall j$$

$$l_j = 1 - \phi_n n_j - \phi_H 1_{H=Bad} \quad (1)$$

$$\ln z(\gamma_i, j, H_{ij}) = w_0 \gamma_i + w_1 j + w_2 j^2 + w_H 1_{H_{ij}=Bad} \quad (2)$$

$$H' \sim \Pi_H \quad (3)$$

$w_0 \gamma_i$  depends on productivity type  $\gamma_i$ . Standard:

$a_0 = a_{J+1} = 0$  and  $a_j > -\kappa, ; c_j, n_j \geq 0; \forall j$ .

## Health states and process

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Health evolves according to the transition matrix

$$\Pi_H = \begin{bmatrix} \pi_{B,B} & \pi_{B,G} \\ \pi_{G,B} & \pi_{G,G} \end{bmatrix} = \begin{bmatrix} 0.67 & 0.33 \\ 0.21 & 0.79 \end{bmatrix}$$

where entry  $\pi_{B,G}$  is the probability of transitioning from health state  $H = \text{Bad}$  to  $H = \text{Good}$ .

- I estimate the transition probabilities as the fraction of individuals that make the relevant transition.
  - E.g. unconditionally  $\hat{\pi}_{B,G}$  is the fraction of people who transition from bad to good health
- The conditional probabilities are estimated similarly.
  - $\hat{\pi}_{B,G}^{u_H,j}$  is the fraction of people of age  $j$  who are health type  $u_H$  who transition from bad to good health.

# Unconditional transitions by age

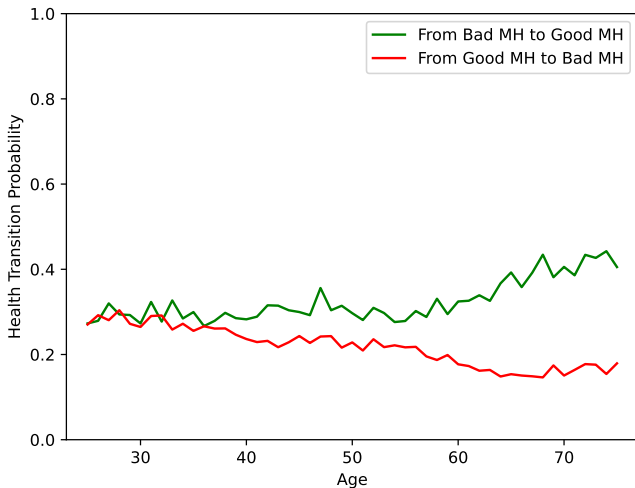


Figure: 1-Year Mental Health Transitions

## Simple health types

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- For now assume that there are only two health types  
 $u_H \in \{u_{Low}, u_{High}\}.$
- We need to establish a cutoff and partition the individuals.
- Sort mental health observations into above and below the 50th percentile by age
- If an individual is in the bottom half of mental health at his age for most of the observations (greater than 50%) he is the low type
- Otherwise he is the high type
- There are issues with this methodology... but this is the current state.



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## Exogenous parameters

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Parameter	Description	Value	Source
$R$	Gross interest rate	1.02	Benchmark
$\beta$	Patience	0.9804	$1/R$
$\sigma$	CRRA	0.9999	Benchmark
$\phi_n$	Labor time-cost	1.125	Benchmark
$\phi_H$	Health time-cost	0.01	Benchmark
$\omega_{H=0}$	Low type pop. weight	0.5699	UKHLS
$\omega_{H=1}$	High type pop. weight	0.4301	$1 - \omega_{H=0}$

Table: Exogenous parameters

# Calibrated parameters

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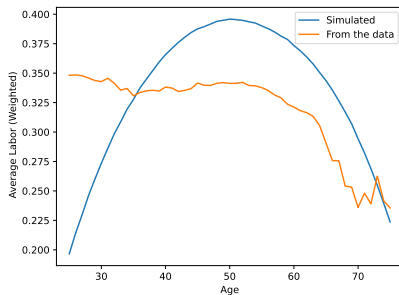
Parameter	Description	Par. Value	Target Moment	Target Value	Model Value
$\alpha$	c utility weight	0.3809	Mean hours worked	33.5	33.51
$w_1$	Linear wage coeff.	0.0266	Wage growth	34.07%	34.14%
$w_2$	Quad. wage coeff.	-0.0005	Wage decay	30.32%	30.31%
$w_H$	Health wage coeff.	0.0439	Healthy wage premium	3.53%	3.62%

Table: Calibrated parameters 1

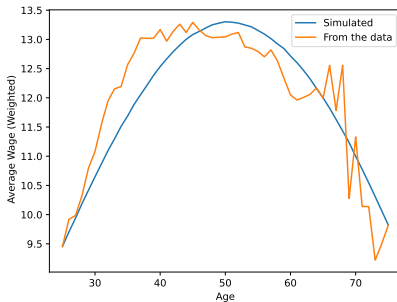
Constant wage coeff.	Ability Level	Value	Weight
$w_{0\gamma_1}$	Low	5	0.28
$w_{0\gamma_2}$	Medium	10	0.59
$w_{0\gamma_3}$	Medium High	15	0.12
$w_{0\gamma_4}$	High	20	0.0
Target Moment	Target Value	Model Value	
Mean wage, $j = 0$	9.454	9.454	
SD wage, $j = 0$	3.201	3.201	

Table: Calibrated parameters 2

# Targeted hours and wage fit



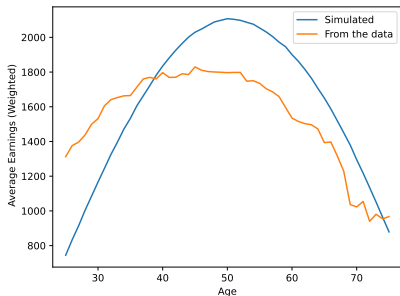
(a) Hours worked (labor)



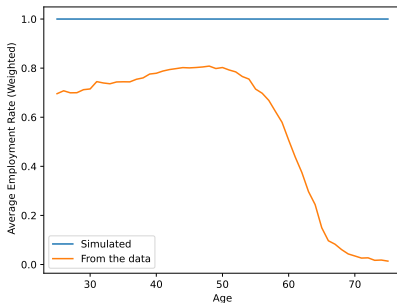
(b) Wage

- Unsurprisingly target moments fit pretty well.

# Untargeted labor earnings and employment



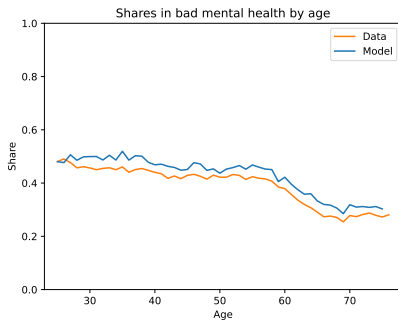
(c) Monthly earnings



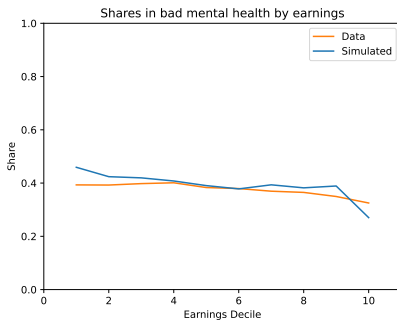
(d) Employment rate

- Earning fit is not great since I entirely miss the extensive margin.

# Shares in bad mental health



(e) Bad MH by age



(f) Bad MH by earnings (extra types)

## Earnings by health

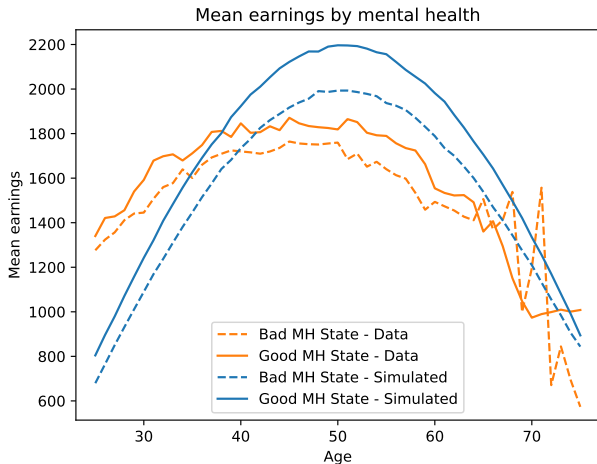
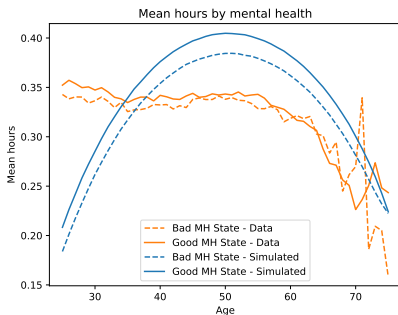


Figure: Mean earnings by MH

- My health states are more different than the data

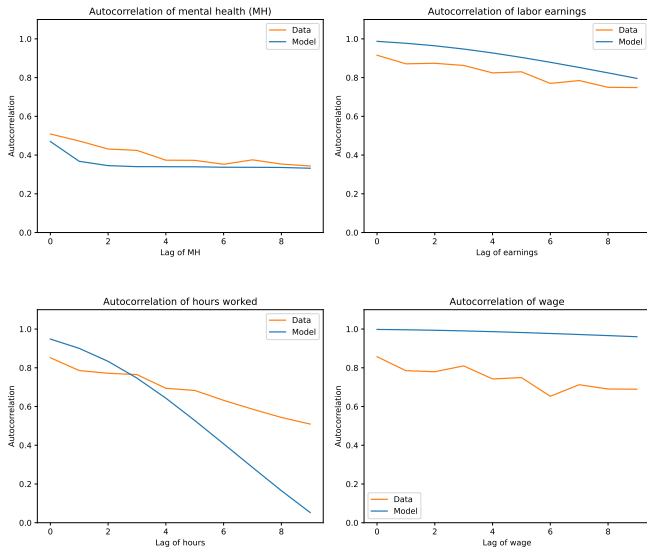
# Wages and hours by health



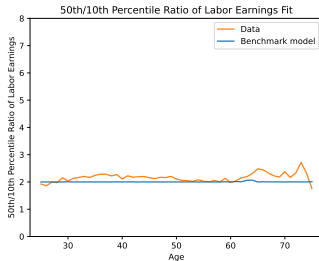
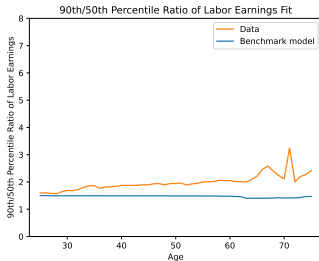
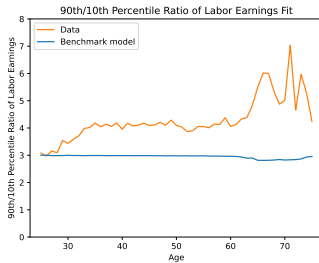
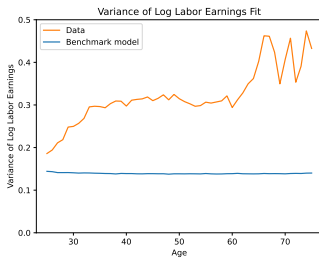
- This is because I have a time cost  $\phi_H$  in the model which is not supported by the data.



# Fit persistence



# Fit inequality in log earnings



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## Four counterfactuals

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I consider four counterfactuals around mental health

- No time cost: the time cost associated with bad health is set  $\phi_H = 0$
- No  $w_H$ : the wage coefficient associated with good health is set  $w_H = 0$
- All low types: the population share of high health types is set  $\omega_{H=Low} = 1.0$
- No mental health: both  $\phi_H = 0$  and  $w_H = 0$ . So that all mental health channels are turned off.

# Variance of log earnings current counterfactuals

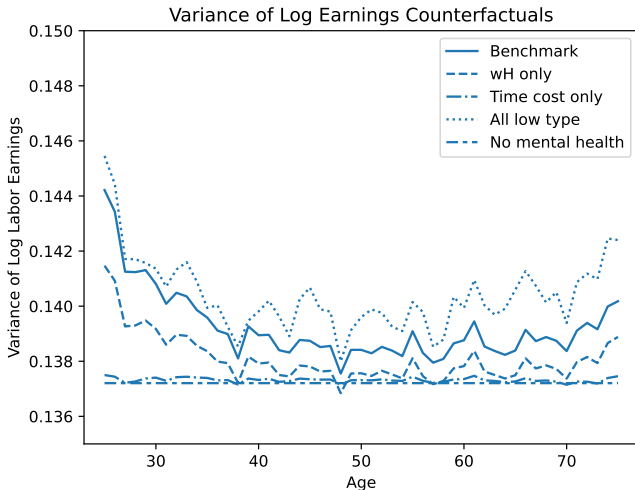
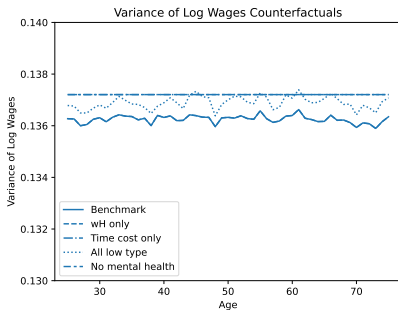
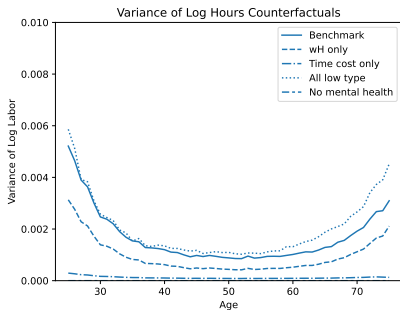


Figure: Variance of log earnings counterfactuals

# Decomposing the variance of log earnings



## Prototype (preview) results

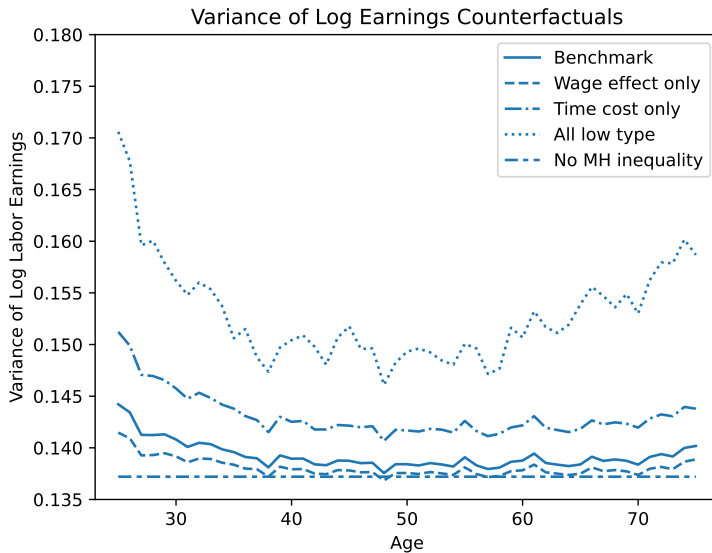
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- Recall Equation 1. The time endowment:

$$l_j = 1 - \phi_n n_j - \phi_H 1_{H=Bad}$$

- In the benchmark we set  $\phi_H = 0.01 \equiv 1$  hour.
- Now let  $\phi_H = 0.07$ . Think 1 hour of “rumination” each day per week.

# Prototype results





## Conclusion and next steps

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- Developed a simple lifecycle model with mental health
- Matches some important moments, misses others
- Previewed some results
- Mechanical next steps
  - Match the extensive margin employment and retirement
- More interesting but later..
  - Endogenize mental health (e.g. treatment decisions)
  - Add physical health. How does it effect mental health and vice versa?
  - Are my symptoms caused by stress?

# Thank You!

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**Thank you!**

Any questions? I appreciate your feedback!

## Utility and time endowment

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Individuals derive period utility from consumption and leisure

$$u(c_j, l_j) = \frac{\left(c_j^\alpha l_j^{1-\alpha}\right)^{1-\sigma}}{1-\sigma}$$

where the time endowment is s.t.

$$l_j = 1 - \phi_n n_j - \phi_H 1_{H=Bad} \quad (4)$$

$\phi_n$  the time cost of work  $> 1$  to account for commuting etc, for now  $\phi_H$  is the time cost of bad health.

## Consumption constraints

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Choices must be s.t.

$$c + a' = z(\gamma, j, H) \cdot n + a(1 + r); \forall j$$

and

$$\ln z(\gamma_i, j, H_{ij}) = w_0 \gamma_i + w_1 j + w_2 j^2 + w_H 1_{H_{ij}=Bad} \quad (5)$$

$w_0 \gamma$  depends on productivity type  $\gamma_i$ .

Standard:  $a_0 = a_{J+1} = 0$  and  $a_j > -\kappa, ; c_j, n_j \geq 0; \forall j$ .

## Health transitions

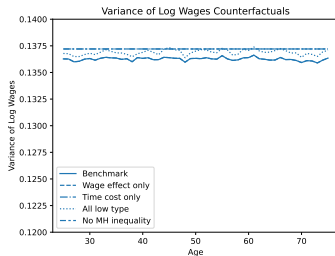
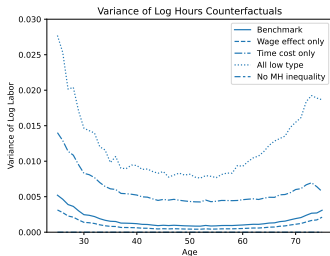
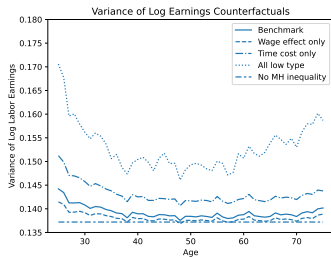
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Health evolves according to the transition matrix

$$\Pi_H = \begin{bmatrix} \pi_{B,B} & \pi_{B,G} \\ \pi_{G,B} & \pi_{G,G} \end{bmatrix} = \begin{bmatrix} 0.67 & 0.33 \\ 0.21 & 0.79 \end{bmatrix}$$

where entry  $\pi_{B,G}$  is the probability of transitioning from health state  $H = \text{Bad}$  to  $H = \text{Good}$ .

# Prototype results

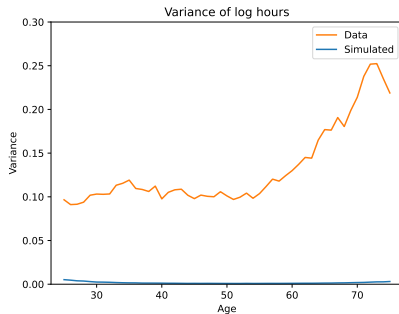


## Some Literature

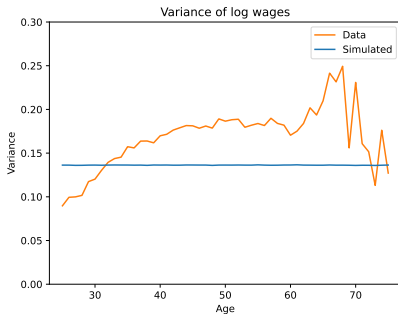
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- Physical Health & Labor: Empirical
  - Health effects labor, justify single index: (Bound et al., 1999),(Blundell et al., 2023)
  - Labor effects health (risky behavior & MH) (Schaller and Stevens, 2015)
- Health & the Lifecycle
  - Abramson et al. (2024), Cronin et al. (2023),Jolivet and Postel-Vinay (2020)
  - Borella et al. (2024), (Dal Bianco and Moro, 2022), De Nardi et al. (2021), Hosseini et al. (2021)
- Mental Health & Labor (Econ)
  - MH on employment, maybe wages in NLSY79: (Germinario et al., 2022)
  - Career Effects of Mental Health (Biasi et al., 2021)
  - Retirement effects mental health (Spearing, 2023)

# Variance of log hours and log wages



(h) Var of log hours



(i) Var of log wages

- All the action is in hours



## Ratio 90th/50th percentile

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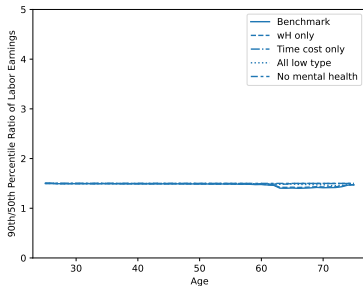


Figure: 90/50 Labor earnings

## Ratio 50th/10th percentile

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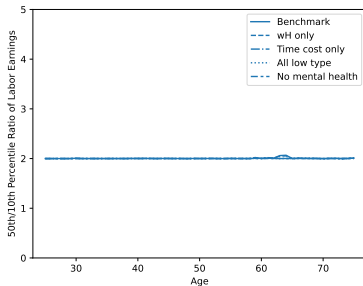


Figure: 50/10 Labor earnings

## Some results from a toy calibration?

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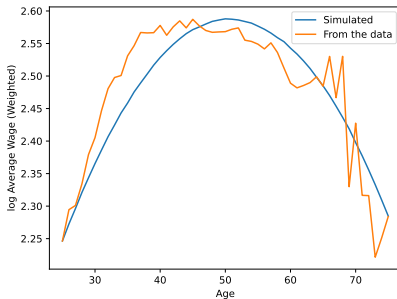
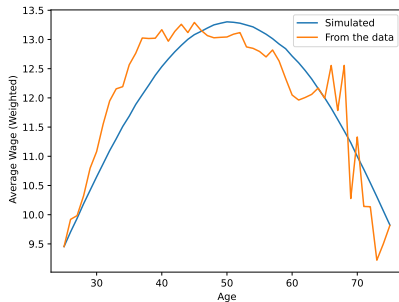
- Maybe not? Maybe if comparative statics become relevant later when estimating different health transitions by type
- i.e. if conditional transitions are more uncertain and comparative statics say something about choices changing with increased uncertainty then this slide could speak to those statics and a calibration with such relatively uncertain transitions

Consider persistent health transitions with moderate uncertainty

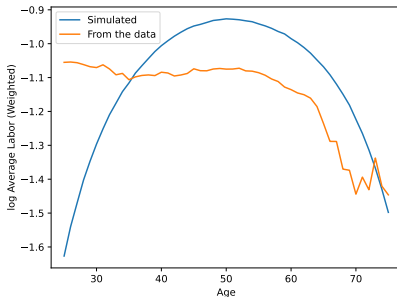
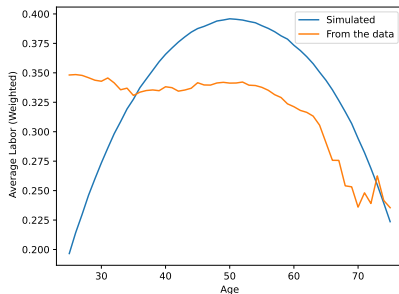
$$\Pi_H = \begin{bmatrix} \pi_{B,B} & \pi_{B,G} \\ \pi_{G,B} & \pi_{G,G} \end{bmatrix} = \begin{bmatrix} 0.7 & 0.3 \\ 0.3 & 0.7 \end{bmatrix}$$

That is a individual has 0.7 chance of remaining in their current health state in the next period.

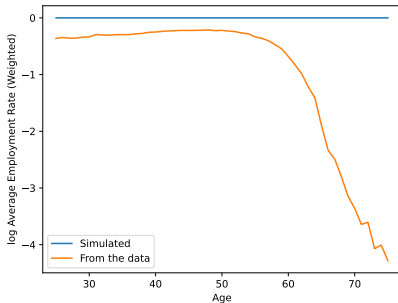
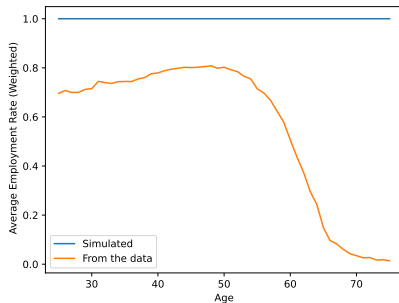
# Aggregate wage fit



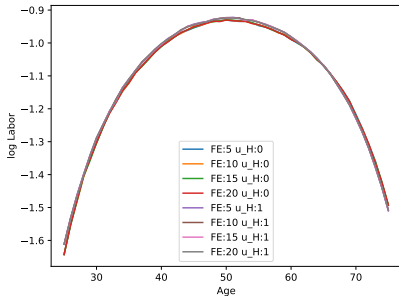
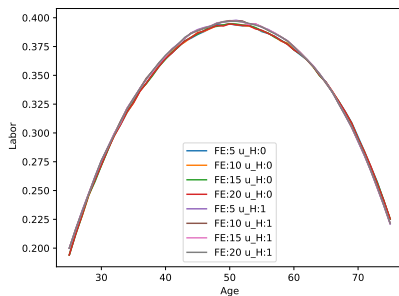
# Aggregate labor fit



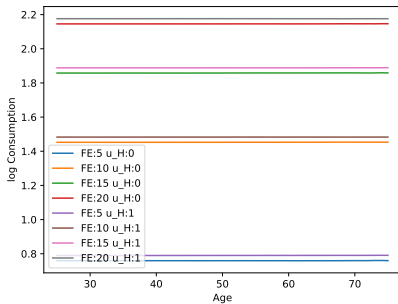
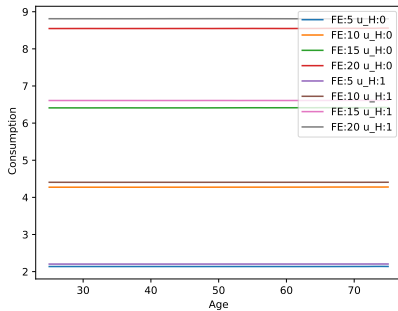
# Aggregate employment fit



# Labor profiles



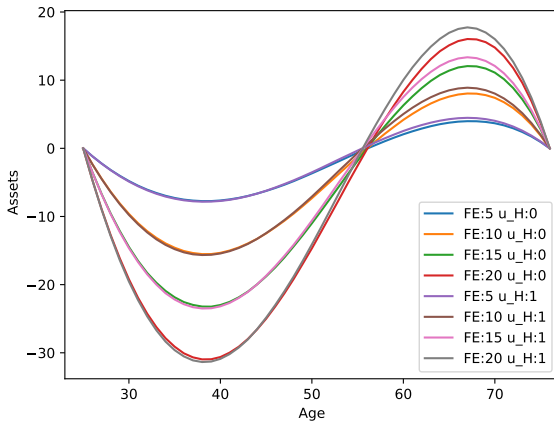
# Consumption profiles



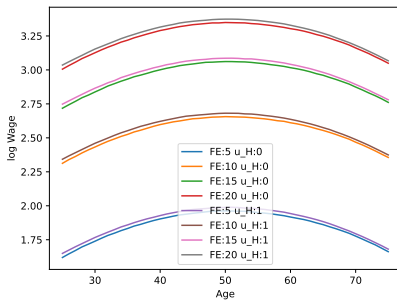
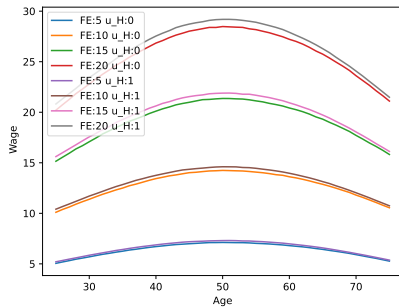


# Asset profiles

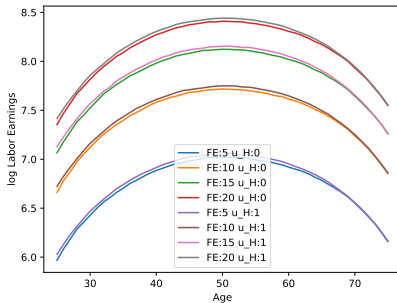
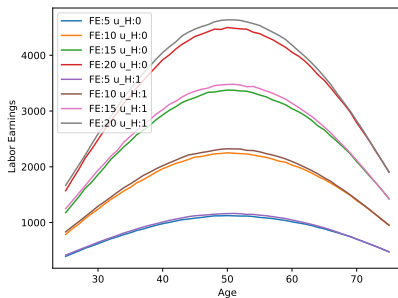
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# Wage profiles



# Labor income



## More on k-means clustering

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The goal is to minimize the within-cluster sum of squares:

$$\min \sum_{n=1}^k \sum_{\bar{m}_i \in C_n} \|\bar{m}_i - \mu_n\|^2$$

where  $\mu_n$  is mean of cluster  $n$  and  $\bar{m}_i$  is an arbitrary data moment:  
think individual  $i$ 's mean lifecycle mental health index

- ① Randomly select  $k$  centroids from the data.
- ② Cluster/assign each individual to the nearest centroid.
- ③ Update centroids by calculating means of clusters
- ④ Repeat by clustering individuals to the updated centroids
- ⑤ Convergence: clusters stabilize.
  - ① individuals are consistently assigned to the same cluster

# Comparing health transitions

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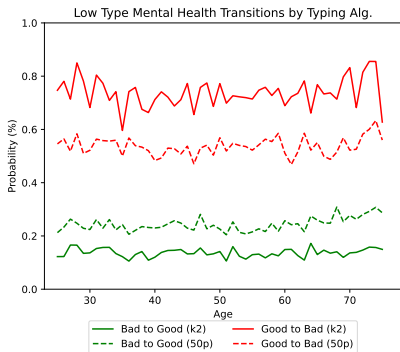
Consider the transition probabilities that result from the two versions of type assignment

Typing Method	Low Type(50.0%)	Bad	Good	High Type(50.0%)	Bad	Good
50pth Cutoff	Bad	0.756	0.244	Bad	0.183	0.817
50pth Cutoff	Good	0.534	0.466	Good	0.098	0.902
Typing Method	Low Type(42.4%)	Bad	Good	High Type(57.6%)	Bad	Good
$k$ -means( $k = 2$ )	Bad	0.861	0.139	Bad	0.376	0.624
$k$ -means( $k = 2$ )	Good	0.729	0.271	Good	0.165	0.835

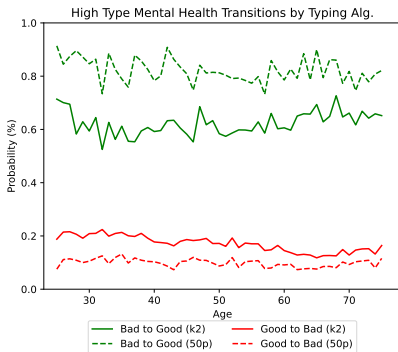
Some text for a footnote?

**Table:** Health transition matrices by health typing algorithm

# Comparing health transitions



(o)



(p)

- compare when conditioned on type to show trajectories not just average probabilities/levels matter by types

## Validating health types: explaining health variation

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*Outcome Variable: Mental Health Index (SF-12)*

Lagged MH	x			x	x	-
MH Type 50pth		x		x		-
MH Type k-means ( $k = 2$ )			x		x	-
$R^2$	0.374	0.375	0.425	0.461	0.483	-
$R^2$ with controls	0.382	0.386	0.434	0.466	0.487	0.072

Some text for a footnote.

**Table:** Validating mental health types

- Health types are just as/more predictive than rich observables

## Validating health types: health trajectories

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Graph of percentage in bad health over lifecycle by type for 50th percentile type, k-means  $k = 2$   $\bar{m}_i$  types, and k-means  $k = 2$   $h_i$  types (maybe also  $k = k^*$   $h_i$  types but maybe not since comparing apples to oranges)

- The point
  - Types have different trajectories, miss extra variation if only use means and not histories in k-means procedure



## References

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