

# Deep Neural Networks Laboration

Data used in this laboration are from the Kitsune Network Attack Dataset, <https://archive.ics.uci.edu/ml/datasets/Kitsune+Network+Attack+Dataset> . We will focus on the 'Mirai' part of the dataset. Your task is to make a DNN that can classify if each attack is benign or malicious. The dataset has 116 covariates, but to make it a bit more difficult we will remove the first 24 covariates.

You need to answer all questions in this notebook.

If the training is too slow on your own computer, use the smaller datasets (*half or quarter*).

Dense networks are not optimal for tabular datasets like the one used here, but here the main goal is to learn deep learning.

## Part 1: Get the data

Skip this part if you load stored numpy arrays (Mirai\*.npy) (which is recommended)

Use `wget` in the terminal of your cloud machine (in the same directory as where you have saved this notebook) to download the data, i.e.

```
wget https://archive.ics.uci.edu/ml/machine-learning-databases/00516/mirai/Mirai_dataset.csv.gz
```

```
wget https://archive.ics.uci.edu/ml/machine-learning-databases/00516/mirai/Mirai_labels.csv.gz
```

Then unpack the files using `gunzip` in the terminal, i.e.

```
gunzip Mirai_dataset.csv.gz
```

```
gunzip Mirai_labels.csv.gz
```

## Part 2: Get a graphics card

Skip this part if you run on the CPU (recommended)

Lets make sure that our script can see the graphics card that will be used. The graphics cards will perform all the time consuming calculations in every training iteration.

```
In [3]: import os
import warnings

# Ignore FutureWarning from numpy
warnings.simplefilter(action='ignore', category=FutureWarning)
```

```
import keras.backend as K
import tensorflow as tf

os.environ["CUDA_DEVICE_ORDER"]="PCI_BUS_ID";

# The GPU id to use, usually either "0" or "1";
os.environ["CUDA_VISIBLE_DEVICES"]="0";

# Allow growth of GPU memory, otherwise it will always look like all the mem
#physical_devices = tf.config.experimental.list_physical_devices('GPU')
#tf.config.experimental.set_memory_growth(physical_devices[0], True)
```

## Part 3: Hardware

In deep learning, the computer hardware is very important. You should always know what kind of hardware you are working on. Lets pretend that everyone is using an Nvidia RTX 3090 graphics card.

Question 1: Google the name of the graphics card, how many CUDA cores does it have?

Question 2: How much memory does the graphics card have?

Question 3: What is stored in the GPU memory while training a DNN ?

Answer

- A1 : 10496 CUDA cores.
- A2 : 24 GB
- A3 : The weights and biases for each layers and node. The model parameters, input data, gradient, and all the intermediate results are in Vram. Usually, it is in batches since it is normal that the data cannot fit in limited amount of Vram.

## Part 4: Load the data

To make this step easier, directly load the data from saved numpy arrays (.npy) (recommended)

Load the dataset from the csv files, it will take some time since it is almost 1.4 GB. (not recommended, unless you want to learn how to do it)

We will use the function `genfromtxt` to load the data. (not recommended, unless you want to learn how to do it)

<https://docs.scipy.org/doc/numpy/reference/generated/numpy.genfromtxt.html>

Load the data from csv files the first time, then save the data as numpy files for faster loading the next time.

Remove the first 24 covariates to make the task harder.

```
In [4]: from numpy import genfromtxt # Not needed if you load data from numpy arrays
import numpy as np
```

```

# Load data from numpy arrays, choose reduced files if the training takes to
X = np.load('Mirai_data.npy')
Y = np.load('Mirai_labels.npy')

print(X.shape)
# Remove the first 24 covariates (columns)
X = X[:,24:]
print(X.shape)

print('The covariates have size {}'.format(X.shape))
print('The labels have size {}'.format(Y.shape))

# Print the number of examples of each class
print(f'The number of examples of class 1 are {np.sum(Y == 1)}')
print(f'The number of examples of class 0 are {np.sum(Y == 0)}')

(764137, 116)
(764137, 92)
The covariates have size (764137, 92).
The labels have size (764137,).
The number of examples of class 1 are 642516
The number of examples of class 0 are 121621

```

## Part 5: How good is a naive classifier?

Question 4: Given the number of examples from each class, how high classification performance can a naive classifier obtain? The naive classifier will assume that all examples belong to one class. Note: you do not need to make a naive classifier, this is a theoretical question, just to understand how good performance we can obtain by guessing that all examples belong to one class.

In all classification tasks you should always ask these questions

- How good classification accuracy can a naive classifier obtain? The naive classifier will assume that all examples belong to one class.
- What is random chance classification accuracy if you randomly guess the label of each (test) example? For a balanced dataset and binary classification this is easy (50%), but in many cases it is more complicated and a Monte Carlo simulation may be required to estimate random chance accuracy.

If your classifier cannot perform better than a naive classifier or a random classifier, you are doing something wrong.

### Answer

- A4: A naive classifier that classifies all examples as class 1 will achieve accuracy of 84%

```

In [5]: # It is common to have NaNs in the data, lets check for it. Hint: np.isnan()

print(f'There are {np.sum(np.isnan(np.load("Mirai_data.npy")))} NaNs in the

```

```

# Print the number of NaNs (not a number) in the labels

print(f'There are {np.sum(np.isnan(Y))} NaNs in the labels')

# Print the number of NaNs in the covariates

print(f'There are {np.sum(np.isnan(X))} NaNs in the covariates')

```

There are 0 NaNs in the data  
There are 0 NaNs in the labels  
There are 0 NaNs in the covariates

## Part 6: Preprocessing

Lets do some simple preprocessing

```

In [6]: # Convert covariates to floats
X = X.astype(float)

# Convert labels to integers
Y = Y.astype(int)

# Remove mean of each covariate (column)
for col in range(0,X.shape[1]):
    avg = np.mean(X[:,col])
    X[:,col] = X[:,col] - avg

# Divide each covariate (column) by its standard deviation
for col in range(0,X.shape[1]):
    X[:,col] = X[:,col]/np.std(X[:,col])

# Check that mean is 0 and standard deviation is 1 for all covariates, by pr
for col in range(0,X.shape[1]):
    flag = 0
    meAn = round(np.mean(X[:,col]))
    stdev = round(np.std(X[:,col]))
    if(meAn != 0 and stdev != 1):
        flag = 1
        print(f'For column {col}, the mean is {meAn} and the std deviation i
    if(flag ==0):
        print('Check completed succesfully')

```

[illegible]

[illegible]

## Part 7: Split the dataset

Use the first 70% of the dataset for training, leave the other 30% for validation and test, call the variables

Xtrain (70%)

Xtemp (30%)

Ytrain (70%)

Ytemp (30%)

We use a function from scikit learn. [https://scikit-learn.org/stable/modules/generated/sklearn.model\\_selection.train\\_test\\_split.html](https://scikit-learn.org/stable/modules/generated/sklearn.model_selection.train_test_split.html)

```
In [7]: from sklearn.model_selection import train_test_split

# Your code to split the dataset
Xtrain,Xtemp,Ytrain,Ytemp = train_test_split(X,Y,test_size= 0.3)

print('Xtrain has size {}'.format(Xtrain.shape))
print('Ytrain has size {}'.format(Ytrain.shape))

print('Xtemp has size {}'.format(Xtemp.shape))
print('Ytemp has size {}'.format(Ytemp.shape))

# Print the number of examples of each class, for the training data and the
print(f'There are {np.sum(Ytrain == 1)} examples of class 1 in Ytrain')
print(f'There are {np.sum(Ytrain == 0)} examples of class 0 in Ytrain')
```

```
print(f'There are {np.sum(Ytemp == 1)} examples of class 1 in Ytemp')
print(f'There are {np.sum(Ytemp == 0)} examples of class 0 in Ytemp')
```

```
Xtrain has size (534895, 92).
Ytrain has size (534895,).
Xtemp has size (229242, 92).
Ytemp has size (229242,).
There are 449904 examples of class 1 in Ytrain
There are 84991 examples of class 0 in Ytrain
There are 192612 examples of class 1 in Ytemp
There are 36630 examples of class 0 in Ytemp
```

## Part 8: Split non-training data data into validation and test

Now split your non-training data (Xtemp, Ytemp) into 50% validation (Xval, Yval) and 50% testing (Xtest, Ytest), we use a function from scikit learn. In total this gives us 70% for training, 15% for validation, 15% for test.

[https://scikit-learn.org/stable/modules/generated/sklearn.model\\_selection.train\\_test\\_split.html](https://scikit-learn.org/stable/modules/generated/sklearn.model_selection.train_test_split.html)

Do all variables (Xtrain,Ytrain), (Xval,Yval), (Xtest,Ytest) have the shape that you expect?

```
In [8]: from sklearn.model_selection import train_test_split

# Your code
Xval,Xtest,Yval,Ytest = train_test_split(Xtemp,Ytemp,train_size=0.5)

print('The validation and test data have size {}, {}, {} and {}'.format(Xval
The validation and test data have size (114621, 92), (114621, 92), (114621,)
and (114621,)
```

## Part 9: DNN classification

Finish this code to create a first version of the classifier using a DNN. Start with a simple network with 2 dense layers (with 20 nodes each), using sigmoid activation functions. The final dense layer should have a single node and a sigmoid activation function. We start with the SGD optimizer.

For different parts of this notebook you need to go back here, add more things, and re-run this cell to re-define the build function.

Relevant functions are

`model.add()` , adds a layer to the network

`Dense()` , a dense network layer

`model.compile()` , compile the model, add " metrics=['accuracy'] " to print the classification accuracy during the training

See <https://keras.io/layers/core/> for information on how the `Dense()` function works

Import a relevant cost / loss function for binary classification from keras.losses  
(<https://keras.io/losses/>)

See the following links for how to compile, train and evaluate the model

[https://keras.io/api/models/model\\_training\\_apis/#compile-method](https://keras.io/api/models/model_training_apis/#compile-method)

[https://keras.io/api/models/model\\_training\\_apis/#fit-method](https://keras.io/api/models/model_training_apis/#fit-method)

[https://keras.io/api/models/model\\_training\\_apis/#evaluate-method](https://keras.io/api/models/model_training_apis/#evaluate-method)

Make sure that the last layer always has a sigmoid activation function (why?).

```
In [9]: import os
import tensorflow as tf

# If there are multiple GPUs and we only want to use one/some, set the number
os.environ["CUDA_DEVICE_ORDER"]="PCI_BUS_ID"
os.environ["CUDA_VISIBLE_DEVICES"]="0"

# This sets the GPU to allocate memory only as needed
physical_devices = tf.config.experimental.list_physical_devices('GPU')
if len(physical_devices) != 0:
    tf.config.experimental.set_memory_growth(physical_devices[0], True)
```

```
In [10]: Xtrain.shape
```

```
Out[10]: (534895, 92)
```

```
In [207... from keras.models import Sequential, Model
from keras.layers import Input, Dense, BatchNormalization, Dropout
from tensorflow.keras.optimizers import SGD, Adam
from keras.losses import BinaryCrossentropy

# Set seed from random number generator, for better comparisons
from numpy.random import seed
seed(123)

def build_DNN(input_shape, n_layers, n_nodes, act_fun='sigmoid', optimizer='sgd',
              use_bn=False, use_dropout=False, use_custom_dropout=False):

    # Setup optimizer, depending on input parameter string
    if(optimizer=='sgd'):
        opt = SGD(learning_rate= learning_rate)
    if(optimizer=='adam'):
        opt = Adam(learning_rate = learning_rate)
    # Setup a sequential model
    model = Sequential()

    # Add layers to the model, using the input parameters of the build_DNN f

    # Add first layer, requires input shape
    model.add(Input(shape = input_shape))
    # Add remaining layers, do not require input shape
    for i in range(n_layers):
        model.add(Dense(n_nodes, activation = act_fun))
        if(use_bn):
            model.add(BatchNormalization())
        if(use_dropout):
            model.add(Dropout(0.5))
```



```

        if (use_custom_dropout):
            model.add(myDropout(0.5))

    # Add final layer
    model.add(Dense(1, activation = 'sigmoid'))

    # Compile model
    model.compile(optimizer=opt, loss= 'BinaryCrossentropy', metrics = ['accuracy'])

    return model

```

In [208... *# Lets define a help function for plotting the training results*

```

import matplotlib.pyplot as plt
def plot_results(history):

    val_loss = history.history['val_loss']
    acc = history.history['accuracy']
    loss = history.history['loss']
    val_acc = history.history['val_accuracy']

    plt.figure(figsize=(10,4))
    plt.xlabel('Epochs')
    plt.ylabel('Loss')
    plt.plot(loss)
    plt.plot(val_loss)
    plt.legend(['Training', 'Validation'])

    plt.figure(figsize=(10,4))
    plt.xlabel('Epochs')
    plt.ylabel('Accuracy')
    plt.plot(acc)
    plt.plot(val_acc)
    plt.legend(['Training', 'Validation'])

    plt.show()

```

## Part 10: Train the DNN

Time to train the DNN, we start simple with 2 layers with 20 nodes each, learning rate 0.1.

Relevant functions

`build_DNN` , the function we defined in Part 9, call it with the parameters you want to use

`model.fit()` , train the model with some training data

`model.evaluate()` , apply the trained model to some test data

See the following links for how to train and evaluate the model

[https://keras.io/api/models/model\\_training\\_apis/#fit-method](https://keras.io/api/models/model_training_apis/#fit-method)

[https://keras.io/api/models/model\\_training\\_apis/#evaluate-method](https://keras.io/api/models/model_training_apis/#evaluate-method)

Make sure that you are using learning rate 0.1 !

## 2 layers, 20 nodes

```
In [13]: # Setup some training parameters
batch_size = 10000
epochs = 20

input_shape = Xtrain.shape[1:]

# Build the model
model1 = build_DNN(input_shape=input_shape,n_layers= 2,n_nodes=20,act_fun='s

# Train the model, provide training data and validation data
history1 = model1.fit(x = Xtrain,y = Ytrain,batch_size = batch_size,validati
```

Epoch 1/20

2023-04-26 11:14:37.399783: W tensorflow/tsl/platform/profile\_utils/cpu\_util  
s.cc:128] Failed to get CPU frequency: 0 Hz

```

54/54 [=====] - 0s 4ms/step - loss: 0.4374 - accuracy: 0.8284 - val_loss: 0.4035 - val_accuracy: 0.8388
Epoch 2/20
54/54 [=====] - 0s 2ms/step - loss: 0.3776 - accuracy: 0.8411 - val_loss: 0.3543 - val_accuracy: 0.8388
Epoch 3/20
54/54 [=====] - 0s 4ms/step - loss: 0.3240 - accuracy: 0.8411 - val_loss: 0.2977 - val_accuracy: 0.8388
Epoch 4/20
54/54 [=====] - 0s 3ms/step - loss: 0.2716 - accuracy: 0.8419 - val_loss: 0.2516 - val_accuracy: 0.8484
Epoch 5/20
54/54 [=====] - 0s 3ms/step - loss: 0.2348 - accuracy: 0.8632 - val_loss: 0.2236 - val_accuracy: 0.8702
Epoch 6/20
54/54 [=====] - 0s 3ms/step - loss: 0.2137 - accuracy: 0.8820 - val_loss: 0.2083 - val_accuracy: 0.8915
Epoch 7/20
54/54 [=====] - 0s 3ms/step - loss: 0.2019 - accuracy: 0.8980 - val_loss: 0.1994 - val_accuracy: 0.9029
Epoch 8/20
54/54 [=====] - 0s 3ms/step - loss: 0.1948 - accuracy: 0.9037 - val_loss: 0.1937 - val_accuracy: 0.9044
Epoch 9/20
54/54 [=====] - 0s 3ms/step - loss: 0.1900 - accuracy: 0.9045 - val_loss: 0.1896 - val_accuracy: 0.9049
Epoch 10/20
54/54 [=====] - 0s 3ms/step - loss: 0.1864 - accuracy: 0.9051 - val_loss: 0.1865 - val_accuracy: 0.9054
Epoch 11/20
54/54 [=====] - 0s 3ms/step - loss: 0.1836 - accuracy: 0.9057 - val_loss: 0.1840 - val_accuracy: 0.9059
Epoch 12/20
54/54 [=====] - 0s 3ms/step - loss: 0.1813 - accuracy: 0.9062 - val_loss: 0.1819 - val_accuracy: 0.9063
Epoch 13/20
54/54 [=====] - 0s 3ms/step - loss: 0.1793 - accuracy: 0.9065 - val_loss: 0.1801 - val_accuracy: 0.9065
Epoch 14/20
54/54 [=====] - 0s 3ms/step - loss: 0.1777 - accuracy: 0.9068 - val_loss: 0.1786 - val_accuracy: 0.9068
Epoch 15/20
54/54 [=====] - 0s 3ms/step - loss: 0.1762 - accuracy: 0.9070 - val_loss: 0.1773 - val_accuracy: 0.9070
Epoch 16/20
54/54 [=====] - 0s 3ms/step - loss: 0.1750 - accuracy: 0.9073 - val_loss: 0.1761 - val_accuracy: 0.9072
Epoch 17/20
54/54 [=====] - 0s 3ms/step - loss: 0.1739 - accuracy: 0.9074 - val_loss: 0.1750 - val_accuracy: 0.9073
Epoch 18/20
54/54 [=====] - 0s 3ms/step - loss: 0.1729 - accuracy: 0.9076 - val_loss: 0.1741 - val_accuracy: 0.9075
Epoch 19/20
54/54 [=====] - 0s 3ms/step - loss: 0.1721 - accuracy: 0.9078 - val_loss: 0.1733 - val_accuracy: 0.9077
Epoch 20/20
54/54 [=====] - 0s 3ms/step - loss: 0.1713 - accuracy: 0.9080 - val_loss: 0.1725 - val_accuracy: 0.9078

```

```

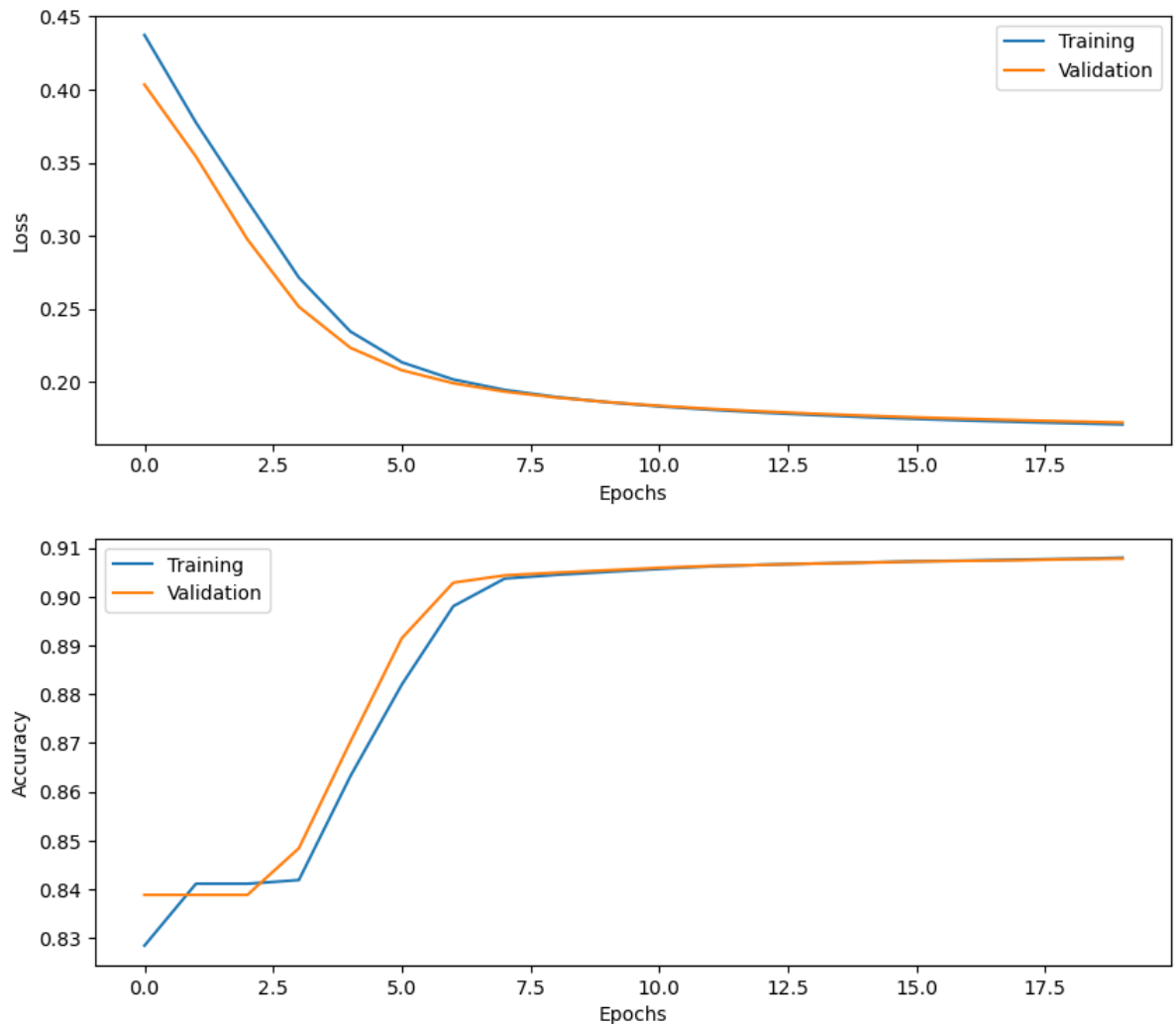
In [14]: # Evaluate the model on the test data
score = model1.evaluate(x = Xtest,y = Ytest)

```

```
print('Test loss: %.4f' % score[0])
print('Test accuracy: %.4f' % score[1])
```

```
3582/3582 [=====] - 1s 219us/step - loss: 0.1705 -
accuracy: 0.9077
Test loss: 0.1705
Test accuracy: 0.9077
```

```
In [15]: # Plot the history from the training run
plot_results(history1)
```



## Part 11: More questions

Question 5: What happens if you add several Dense layers without specifying the activation function?

Question 6: How are the weights in each dense layer initialized as default? How are the bias weights initialized?

## Answer

- The default value for the activation argument is None, meaning that there will be no activation function for that layer, meaning the model will be linear.

- The weights in each dense layers are initialized as default by the kernel\_initializer = 'glorot\_uniform'. The bias weights are initialized by default as zeroes per the Documentation of the Dense function.

## Part 12: Balancing the classes

This dataset is rather unbalanced, we need to define class weights so that the training pays more attention to the class with fewer samples. We use a function in scikit learn

[https://scikit-learn.org/stable/modules/generated/sklearn.utils.class\\_weight.compute\\_class\\_weight.html](https://scikit-learn.org/stable/modules/generated/sklearn.utils.class_weight.compute_class_weight.html)

You need to call the function something like this

```
class_weights = class_weight.compute_class_weight(class_weight = , classes = , y = )
```

otherwise it will complain

```
In [231]: from sklearn.utils import class_weight

# Calculate class weights

class_weights = class_weight.compute_class_weight(classes= np.unique(Ytrain)

# Print the class weights
print(class_weights)

# Keras wants the weights in this form, uncomment and change value1 and value2
# or get them from the array that is returned from class_weight

class_weights = {0: class_weights[0],
                  1: class_weights[1]}
```

[3.14677436 0.59445459]

### 2 layers, 20 nodes, class weights

```
In [17]: # Setup some training parameters
batch_size = 10000
epochs = 20
input_shape = Xtrain.shape[1:]

# Build and train model
model2 = build_DNN(input_shape=input_shape,n_layers= 2,n_nodes=20,act_fun='s

history2 = model2.fit(x = Xtrain,y = Ytrain,batch_size = batch_size,validati
```

```

Epoch 1/20
54/54 [=====] - 0s 3ms/step - loss: 0.6620 - accuracy: 0.8753 - val_loss: 0.5466 - val_accuracy: 0.8920
Epoch 2/20
54/54 [=====] - 0s 3ms/step - loss: 0.4643 - accuracy: 0.8854 - val_loss: 0.3836 - val_accuracy: 0.8808
Epoch 3/20
54/54 [=====] - 0s 3ms/step - loss: 0.3214 - accuracy: 0.8802 - val_loss: 0.3042 - val_accuracy: 0.8796
Epoch 4/20
54/54 [=====] - 0s 3ms/step - loss: 0.2573 - accuracy: 0.8800 - val_loss: 0.2778 - val_accuracy: 0.8798
Epoch 5/20
54/54 [=====] - 0s 3ms/step - loss: 0.2321 - accuracy: 0.8808 - val_loss: 0.2679 - val_accuracy: 0.8818
Epoch 6/20
54/54 [=====] - 0s 3ms/step - loss: 0.2203 - accuracy: 0.8841 - val_loss: 0.2615 - val_accuracy: 0.8853
Epoch 7/20
54/54 [=====] - 0s 3ms/step - loss: 0.2134 - accuracy: 0.8870 - val_loss: 0.2575 - val_accuracy: 0.8882
Epoch 8/20
54/54 [=====] - 0s 3ms/step - loss: 0.2087 - accuracy: 0.8893 - val_loss: 0.2534 - val_accuracy: 0.8902
Epoch 9/20
54/54 [=====] - 0s 3ms/step - loss: 0.2051 - accuracy: 0.8918 - val_loss: 0.2509 - val_accuracy: 0.8930
Epoch 10/20
54/54 [=====] - 0s 3ms/step - loss: 0.2022 - accuracy: 0.8939 - val_loss: 0.2492 - val_accuracy: 0.8946
Epoch 11/20
54/54 [=====] - 0s 3ms/step - loss: 0.1998 - accuracy: 0.8954 - val_loss: 0.2466 - val_accuracy: 0.8959
Epoch 12/20
54/54 [=====] - 0s 3ms/step - loss: 0.1977 - accuracy: 0.8965 - val_loss: 0.2449 - val_accuracy: 0.8969
Epoch 13/20
54/54 [=====] - 0s 3ms/step - loss: 0.1958 - accuracy: 0.8977 - val_loss: 0.2434 - val_accuracy: 0.8977
Epoch 14/20
54/54 [=====] - 0s 3ms/step - loss: 0.1942 - accuracy: 0.8984 - val_loss: 0.2411 - val_accuracy: 0.8985
Epoch 15/20
54/54 [=====] - 0s 3ms/step - loss: 0.1927 - accuracy: 0.8988 - val_loss: 0.2401 - val_accuracy: 0.8988
Epoch 16/20
54/54 [=====] - 0s 3ms/step - loss: 0.1913 - accuracy: 0.8992 - val_loss: 0.2389 - val_accuracy: 0.8990
Epoch 17/20
54/54 [=====] - 0s 3ms/step - loss: 0.1901 - accuracy: 0.8994 - val_loss: 0.2373 - val_accuracy: 0.8993
Epoch 18/20
54/54 [=====] - 0s 4ms/step - loss: 0.1889 - accuracy: 0.8998 - val_loss: 0.2372 - val_accuracy: 0.9000
Epoch 19/20
54/54 [=====] - 0s 3ms/step - loss: 0.1879 - accuracy: 0.9005 - val_loss: 0.2356 - val_accuracy: 0.9008
Epoch 20/20
54/54 [=====] - 0s 3ms/step - loss: 0.1869 - accuracy: 0.9014 - val_loss: 0.2347 - val_accuracy: 0.9017

```

```

In [18]: # Evaluate model on test data
         score = model2.evaluate(Xtest,Ytest)

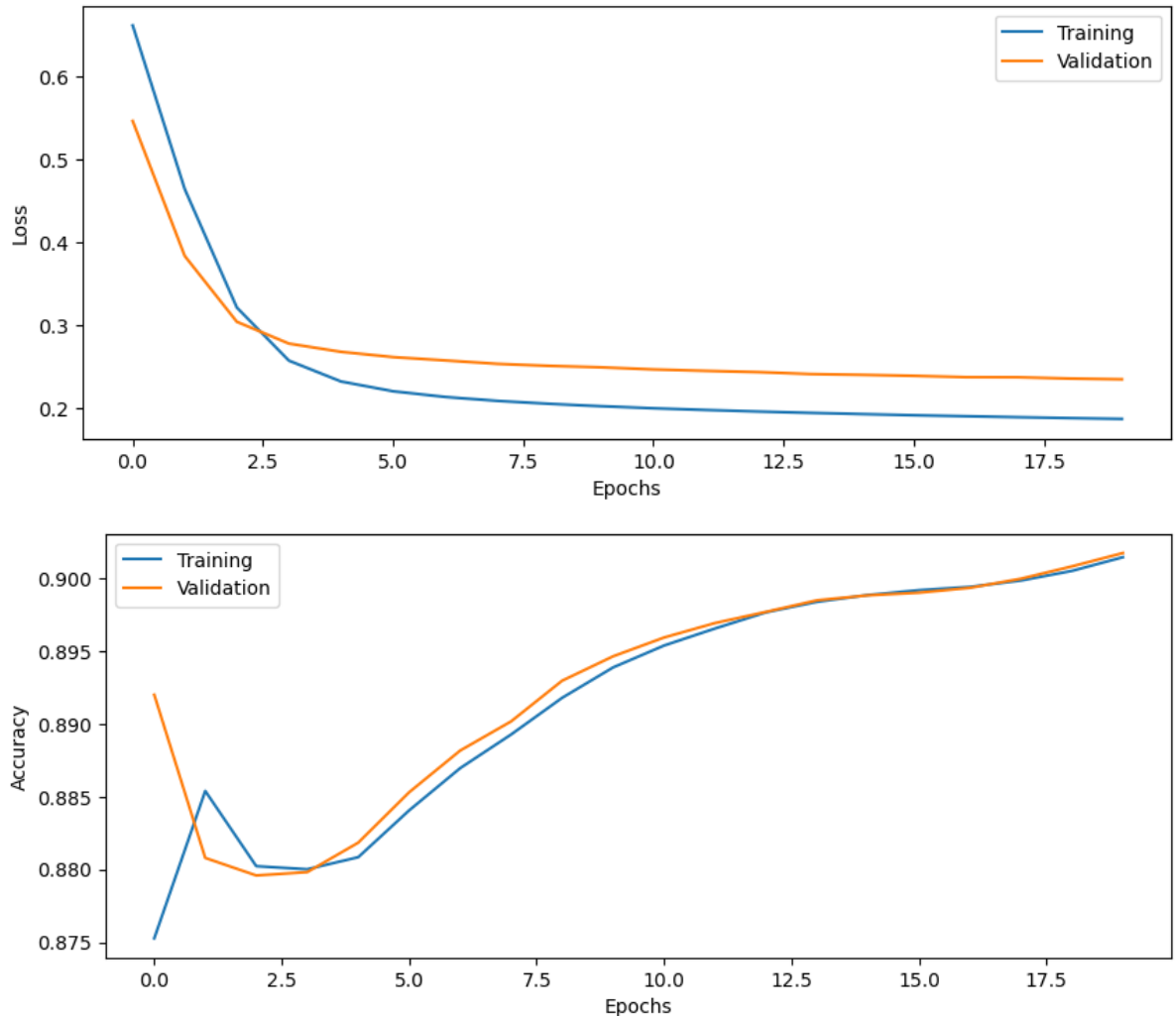
```

```
print('Test loss: %.4f' % score[0])
print('Test accuracy: %.4f' % score[1])
```

```
3582/3582 [=====] - 1s 239us/step - loss: 0.2340 -
accuracy: 0.9019
Test loss: 0.2340
Test accuracy: 0.9019
```

In [ ]:

In [19]: `plot_results(history2)`



## Part 13: More questions

Skip questions 8 and 9 if you run on the CPU (recommended)

Question 7: Why do we have to use a batch size? Why can't we simply use all data at once? This is more relevant for even larger datasets.

Question 8: How busy is the GPU for a batch size of 100? How much GPU memory is used? Hint: run 'nvidia-smi' on the computer a few times during training.

Question 9: What is the processing time for one training epoch when the batch size is 100? What is the processing time for one epoch when the batch size is 1,000? What is the processing time for one epoch when the batch size is 10,000? Explain the results.


Question 10: How many times are the weights in the DNN updated in each training epoch if the batch size is 100? How many times are the weights in the DNN updated in each training epoch if the batch size is 1,000? How many times are the weights in the DNN updated in each training epoch if the batch size is 10,000?

Question 11: What limits how large the batch size can be?

Question 12: Generally speaking, how is the learning rate related to the batch size? If the batch size is decreased, how should the learning rate be changed?

Lets use a batch size of 10,000 from now on, and a learning rate of 0.1.

## Answer

- A7 : We use batch size for **stability and managing the speed of the training**. It also has an impact on the hardware resources we use for the Neural Networks. Using the entire training samples at once will require a lot of processing power and memory in terms of hardware to complete. By using batches, we update the weights for the NN after every batch, leading to a much more stable and faster training.
- 8 and 9 skipped because of work done on a CPU
- A10 : In each training epoch, if the batch size is 100, the weights are updated  $534895/100$  times (~5348). If the batch size is 1000, the weights are updated 534 times and if the batch size is 10000, the weights are updated ~54 times.
- A11 : The memory available affects the batch size. i.e., the hardware resources.
- A12 : The learning rate is proportional related to the batch size, if the batch size is decreased, then the learning rate should be decreased to prevent the gradient from taking too large a step relative to the size of the batch. 

## Part 14: Increasing the complexity

Lets try some different configurations of number of layers and number of nodes per layer.

Question 13: How many trainable parameters does the network with 4 dense layers with 50 nodes each have, compared to the initial network with 2 layers and 20 nodes per layer? Hint: use `model.summary()`

```
In [20]: model2.summary()
```



Model: "sequential\_1"

Layer (type)	Output Shape	Param #
dense_3 (Dense)	(None, 20)	1860
dense_4 (Dense)	(None, 20)	420
dense_5 (Dense)	(None, 1)	21
Total params: 2,301		
Trainable params: 2,301		
Non-trainable params: 0		

## Answer

- A13: The network with 4 dense layers and 50 nodes each has 12,351 trainable params, while the model with 2 layers and 20 nodes has 2301 trainable params.

## 4 layers, 20 nodes, class weights

```
In [21]: # Setup some training parameters
batch_size = 10000
epochs = 20
input_shape = Xtrain.shape[1:]

# Build and train model
model3 = build_DNN(input_shape=input_shape,n_layers= 4,n_nodes=50,act_fun='s

history3 = model3.fit(x = Xtrain,y = Ytrain,batch_size = batch_size,validati
model3.summary()
```

```

Epoch 1/20
54/54 [=====] - 1s 7ms/step - loss: 0.6932 - accuracy: 0.5611 - val_loss: 0.7018 - val_accuracy: 0.1612
Epoch 2/20
54/54 [=====] - 0s 6ms/step - loss: 0.6918 - accuracy: 0.5686 - val_loss: 0.6913 - val_accuracy: 0.8720
Epoch 3/20
54/54 [=====] - 0s 6ms/step - loss: 0.6909 - accuracy: 0.6424 - val_loss: 0.6896 - val_accuracy: 0.8851
Epoch 4/20
54/54 [=====] - 0s 6ms/step - loss: 0.6898 - accuracy: 0.6634 - val_loss: 0.6877 - val_accuracy: 0.8893
Epoch 5/20
54/54 [=====] - 0s 6ms/step - loss: 0.6884 - accuracy: 0.6993 - val_loss: 0.6817 - val_accuracy: 0.8545
Epoch 6/20
54/54 [=====] - 0s 6ms/step - loss: 0.6866 - accuracy: 0.7512 - val_loss: 0.6887 - val_accuracy: 0.8651
Epoch 7/20
54/54 [=====] - 0s 6ms/step - loss: 0.6841 - accuracy: 0.8427 - val_loss: 0.6808 - val_accuracy: 0.8842
Epoch 8/20
54/54 [=====] - 0s 7ms/step - loss: 0.6805 - accuracy: 0.8775 - val_loss: 0.6635 - val_accuracy: 0.8561
Epoch 9/20
54/54 [=====] - 0s 7ms/step - loss: 0.6749 - accuracy: 0.8791 - val_loss: 0.6755 - val_accuracy: 0.8776
Epoch 10/20
54/54 [=====] - 0s 6ms/step - loss: 0.6659 - accuracy: 0.8815 - val_loss: 0.6633 - val_accuracy: 0.8791
Epoch 11/20
54/54 [=====] - 0s 6ms/step - loss: 0.6498 - accuracy: 0.8808 - val_loss: 0.6329 - val_accuracy: 0.8804
Epoch 12/20
54/54 [=====] - 0s 6ms/step - loss: 0.6187 - accuracy: 0.8808 - val_loss: 0.5923 - val_accuracy: 0.8798
Epoch 13/20
54/54 [=====] - 0s 7ms/step - loss: 0.5545 - accuracy: 0.8807 - val_loss: 0.5057 - val_accuracy: 0.8802
Epoch 14/20
54/54 [=====] - 0s 6ms/step - loss: 0.4388 - accuracy: 0.8804 - val_loss: 0.3841 - val_accuracy: 0.8797
Epoch 15/20
54/54 [=====] - 0s 6ms/step - loss: 0.3178 - accuracy: 0.8802 - val_loss: 0.3055 - val_accuracy: 0.8797
Epoch 16/20
54/54 [=====] - 0s 8ms/step - loss: 0.2556 - accuracy: 0.8803 - val_loss: 0.2779 - val_accuracy: 0.8799
Epoch 17/20
54/54 [=====] - 0s 8ms/step - loss: 0.2320 - accuracy: 0.8804 - val_loss: 0.2704 - val_accuracy: 0.8801
Epoch 18/20
54/54 [=====] - 0s 7ms/step - loss: 0.2215 - accuracy: 0.8810 - val_loss: 0.2621 - val_accuracy: 0.8815
Epoch 19/20
54/54 [=====] - 0s 7ms/step - loss: 0.2154 - accuracy: 0.8826 - val_loss: 0.2602 - val_accuracy: 0.8837
Epoch 20/20
54/54 [=====] - 0s 8ms/step - loss: 0.2110 - accuracy: 0.8851 - val_loss: 0.2582 - val_accuracy: 0.8858
Model: "sequential_2"

```

Layer (type)	Output Shape	Param #
=====		

dense_6 (Dense)	(None, 50)	4650
dense_7 (Dense)	(None, 50)	2550
dense_8 (Dense)	(None, 50)	2550
dense_9 (Dense)	(None, 50)	2550
dense_10 (Dense)	(None, 1)	51

```

=====
Total params: 12,351
Trainable params: 12,351
Non-trainable params: 0

```

```

In [22]: # Evaluate model on test data
score = model3.evaluate(Xtest,Ytest)

```

```

print('Test loss: %.4f' % score[0])
print('Test accuracy: %.4f' % score[1])

```

```

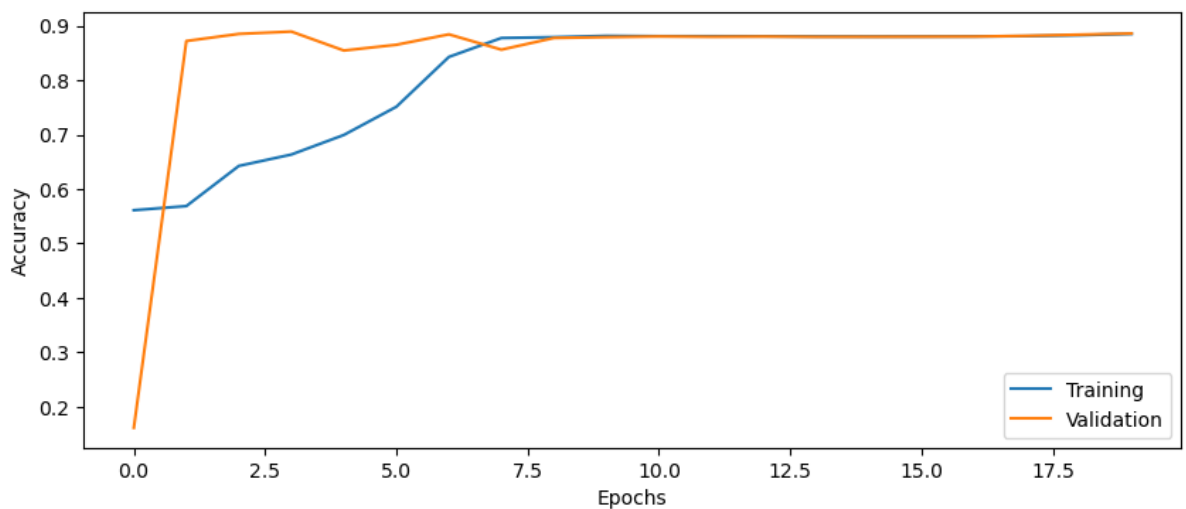
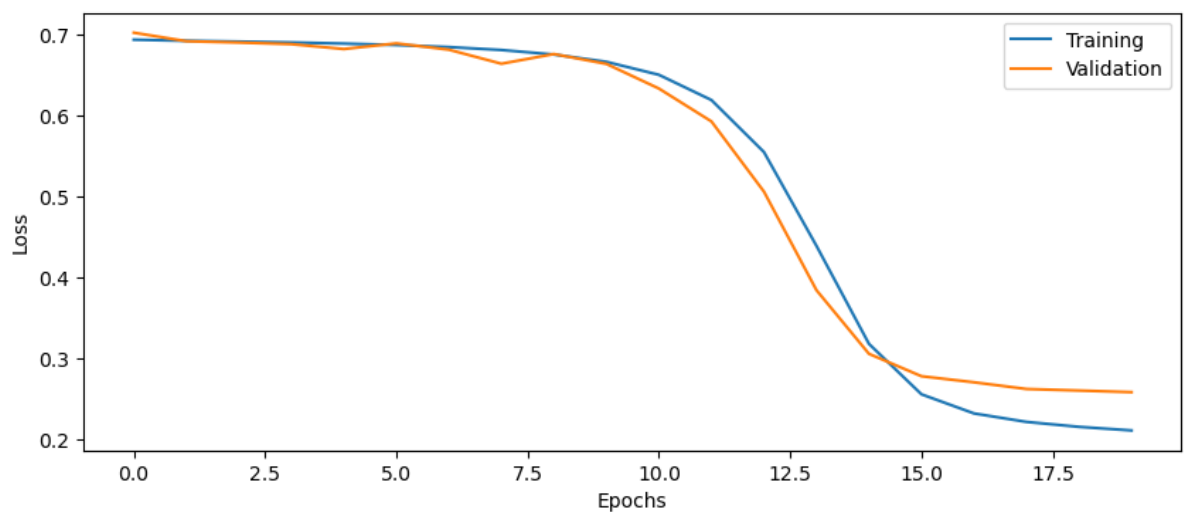
3582/3582 [=====] - 1s 261us/step - loss: 0.2568 -
accuracy: 0.8867
Test loss: 0.2568
Test accuracy: 0.8867

```

```

In [23]: plot_results(history3)

```



## 2 layers, 50 nodes, class weights

```
In [24]: # Setup some training parameters
batch_size = 10000
epochs = 20
input_shape = Xtrain.shape[1:]

# Build and train model
model4 = build_DNN(input_shape,n_layers=2,n_nodes=50,act_fun = 'sigmoid',lea
history4 = model4.fit(x = Xtrain,y = Ytrain,batch_size = batch_size,validati
```

```

Epoch 1/20
54/54 [=====] - 0s 6ms/step - loss: 0.6277 - accuracy: 0.7287 - val_loss: 0.5181 - val_accuracy: 0.8819
Epoch 2/20
54/54 [=====] - 0s 5ms/step - loss: 0.4005 - accuracy: 0.8823 - val_loss: 0.3396 - val_accuracy: 0.8821
Epoch 3/20
54/54 [=====] - 0s 5ms/step - loss: 0.2712 - accuracy: 0.8837 - val_loss: 0.2847 - val_accuracy: 0.8845
Epoch 4/20
54/54 [=====] - 0s 5ms/step - loss: 0.2326 - accuracy: 0.8865 - val_loss: 0.2670 - val_accuracy: 0.8884
Epoch 5/20
54/54 [=====] - 0s 4ms/step - loss: 0.2186 - accuracy: 0.8898 - val_loss: 0.2599 - val_accuracy: 0.8908
Epoch 6/20
54/54 [=====] - 0s 4ms/step - loss: 0.2113 - accuracy: 0.8919 - val_loss: 0.2563 - val_accuracy: 0.8927
Epoch 7/20
54/54 [=====] - 0s 4ms/step - loss: 0.2064 - accuracy: 0.8938 - val_loss: 0.2545 - val_accuracy: 0.8942
Epoch 8/20
54/54 [=====] - 0s 4ms/step - loss: 0.2027 - accuracy: 0.8954 - val_loss: 0.2490 - val_accuracy: 0.8957
Epoch 9/20
54/54 [=====] - 0s 4ms/step - loss: 0.1997 - accuracy: 0.8963 - val_loss: 0.2461 - val_accuracy: 0.8963
Epoch 10/20
54/54 [=====] - 0s 4ms/step - loss: 0.1971 - accuracy: 0.8967 - val_loss: 0.2448 - val_accuracy: 0.8967
Epoch 11/20
54/54 [=====] - 0s 4ms/step - loss: 0.1949 - accuracy: 0.8971 - val_loss: 0.2427 - val_accuracy: 0.8970
Epoch 12/20
54/54 [=====] - 0s 4ms/step - loss: 0.1930 - accuracy: 0.8976 - val_loss: 0.2403 - val_accuracy: 0.8976
Epoch 13/20
54/54 [=====] - 0s 4ms/step - loss: 0.1913 - accuracy: 0.8984 - val_loss: 0.2384 - val_accuracy: 0.8987
Epoch 14/20
54/54 [=====] - 0s 4ms/step - loss: 0.1898 - accuracy: 0.8995 - val_loss: 0.2373 - val_accuracy: 0.8997
Epoch 15/20
54/54 [=====] - 0s 4ms/step - loss: 0.1885 - accuracy: 0.9005 - val_loss: 0.2380 - val_accuracy: 0.9004
Epoch 16/20
54/54 [=====] - 0s 4ms/step - loss: 0.1873 - accuracy: 0.9014 - val_loss: 0.2351 - val_accuracy: 0.9015
Epoch 17/20
54/54 [=====] - 0s 4ms/step - loss: 0.1862 - accuracy: 0.9021 - val_loss: 0.2338 - val_accuracy: 0.9022
Epoch 18/20
54/54 [=====] - 0s 4ms/step - loss: 0.1852 - accuracy: 0.9028 - val_loss: 0.2330 - val_accuracy: 0.9029
Epoch 19/20
54/54 [=====] - 0s 4ms/step - loss: 0.1843 - accuracy: 0.9036 - val_loss: 0.2327 - val_accuracy: 0.9036
Epoch 20/20
54/54 [=====] - 0s 4ms/step - loss: 0.1835 - accuracy: 0.9043 - val_loss: 0.2313 - val_accuracy: 0.9046

```

```

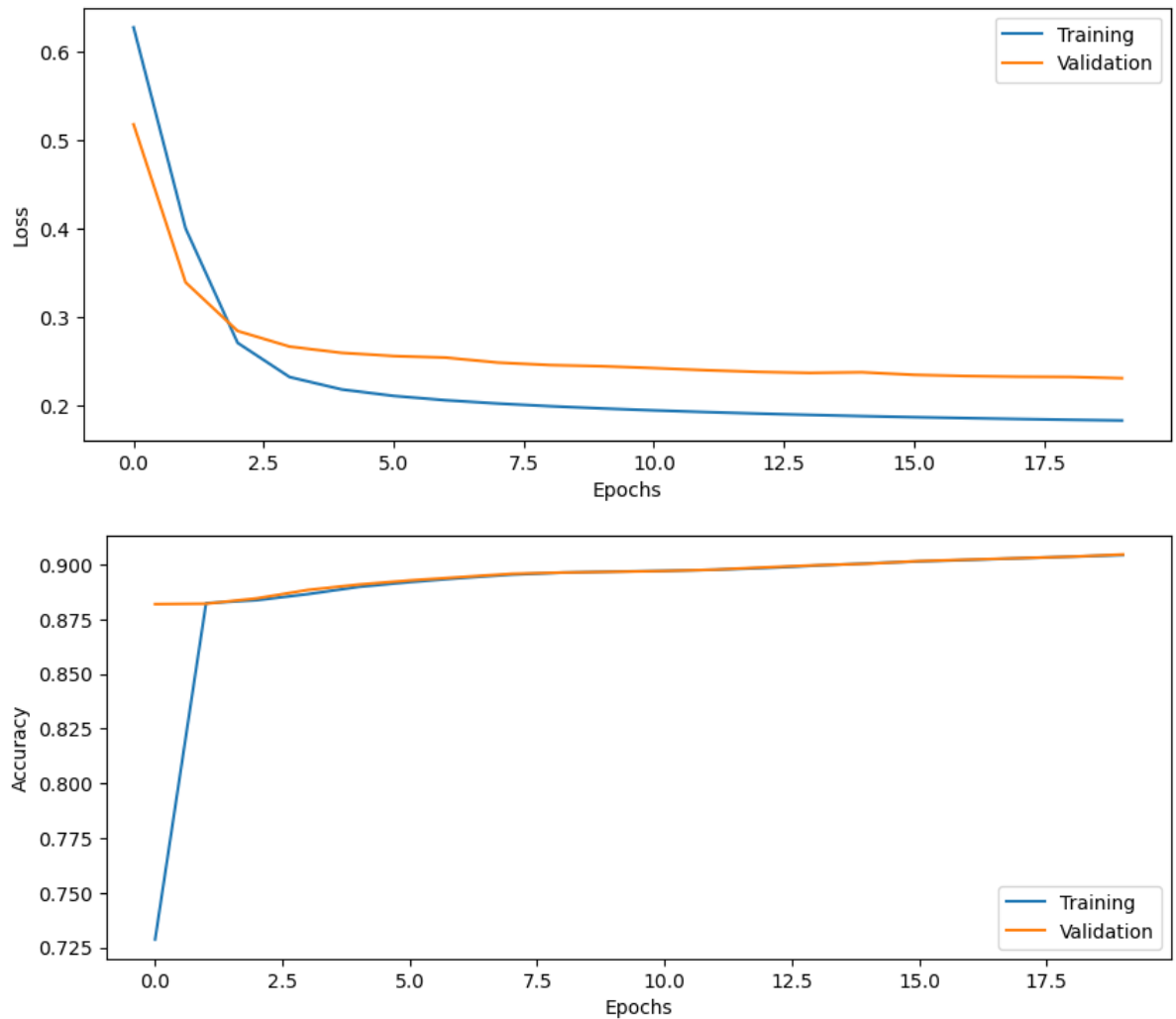
In [25]: # Evaluate model on test data
         score = model4.evaluate(Xtest,Ytest)

```

```
print('Test loss: %.4f' % score[0])
print('Test accuracy: %.4f' % score[1])
```

```
3582/3582 [=====] - 1s 227us/step - loss: 0.2306 -
accuracy: 0.9047
Test loss: 0.2306
Test accuracy: 0.9047
```

In [26]: `plot_results(history4)`



## 4 layers, 50 nodes, class weights

```
In [27]: # Setup some training parameters
batch_size = 10000
epochs = 20
input_shape = X.shape[1:]

# Build and train model
model5 = build_DNN(input_shape=input_shape, n_layers=4, n_nodes=50, act_fun='si
history5 = model5.fit(x = Xtrain, y = Ytrain, batch_size = batch_size, validati
```

```

Epoch 1/20
54/54 [=====] - 1s 8ms/step - loss: 0.6934 - accuracy: 0.5449 - val_loss: 0.6860 - val_accuracy: 0.8388
Epoch 2/20
54/54 [=====] - 0s 7ms/step - loss: 0.6918 - accuracy: 0.6387 - val_loss: 0.6980 - val_accuracy: 0.1612
Epoch 3/20
54/54 [=====] - 0s 7ms/step - loss: 0.6906 - accuracy: 0.6580 - val_loss: 0.6895 - val_accuracy: 0.8705
Epoch 4/20
54/54 [=====] - 0s 7ms/step - loss: 0.6892 - accuracy: 0.7511 - val_loss: 0.6931 - val_accuracy: 0.3818
Epoch 5/20
54/54 [=====] - 0s 7ms/step - loss: 0.6875 - accuracy: 0.7509 - val_loss: 0.6868 - val_accuracy: 0.8725
Epoch 6/20
54/54 [=====] - 0s 7ms/step - loss: 0.6853 - accuracy: 0.8484 - val_loss: 0.6850 - val_accuracy: 0.8761
Epoch 7/20
54/54 [=====] - 0s 7ms/step - loss: 0.6823 - accuracy: 0.8720 - val_loss: 0.6840 - val_accuracy: 0.8733
Epoch 8/20
54/54 [=====] - 0s 7ms/step - loss: 0.6778 - accuracy: 0.8773 - val_loss: 0.6746 - val_accuracy: 0.8733
Epoch 9/20
54/54 [=====] - 0s 7ms/step - loss: 0.6708 - accuracy: 0.8783 - val_loss: 0.6707 - val_accuracy: 0.8762
Epoch 10/20
54/54 [=====] - 0s 7ms/step - loss: 0.6590 - accuracy: 0.8779 - val_loss: 0.6517 - val_accuracy: 0.8779
Epoch 11/20
54/54 [=====] - 0s 6ms/step - loss: 0.6373 - accuracy: 0.8775 - val_loss: 0.6297 - val_accuracy: 0.8774
Epoch 12/20
54/54 [=====] - 0s 7ms/step - loss: 0.5940 - accuracy: 0.8786 - val_loss: 0.5557 - val_accuracy: 0.8789
Epoch 13/20
54/54 [=====] - 0s 7ms/step - loss: 0.5072 - accuracy: 0.8792 - val_loss: 0.4527 - val_accuracy: 0.8785
Epoch 14/20
54/54 [=====] - 0s 7ms/step - loss: 0.3799 - accuracy: 0.8792 - val_loss: 0.3391 - val_accuracy: 0.8785
Epoch 15/20
54/54 [=====] - 0s 7ms/step - loss: 0.2845 - accuracy: 0.8794 - val_loss: 0.2928 - val_accuracy: 0.8788
Epoch 16/20
54/54 [=====] - 0s 7ms/step - loss: 0.2441 - accuracy: 0.8797 - val_loss: 0.2764 - val_accuracy: 0.8792
Epoch 17/20
54/54 [=====] - 0s 7ms/step - loss: 0.2281 - accuracy: 0.8800 - val_loss: 0.2686 - val_accuracy: 0.8795
Epoch 18/20
54/54 [=====] - 0s 7ms/step - loss: 0.2201 - accuracy: 0.8802 - val_loss: 0.2673 - val_accuracy: 0.8797
Epoch 19/20
54/54 [=====] - 0s 7ms/step - loss: 0.2152 - accuracy: 0.8808 - val_loss: 0.2616 - val_accuracy: 0.8814
Epoch 20/20
54/54 [=====] - 0s 7ms/step - loss: 0.2116 - accuracy: 0.8828 - val_loss: 0.2597 - val_accuracy: 0.8835

```

```

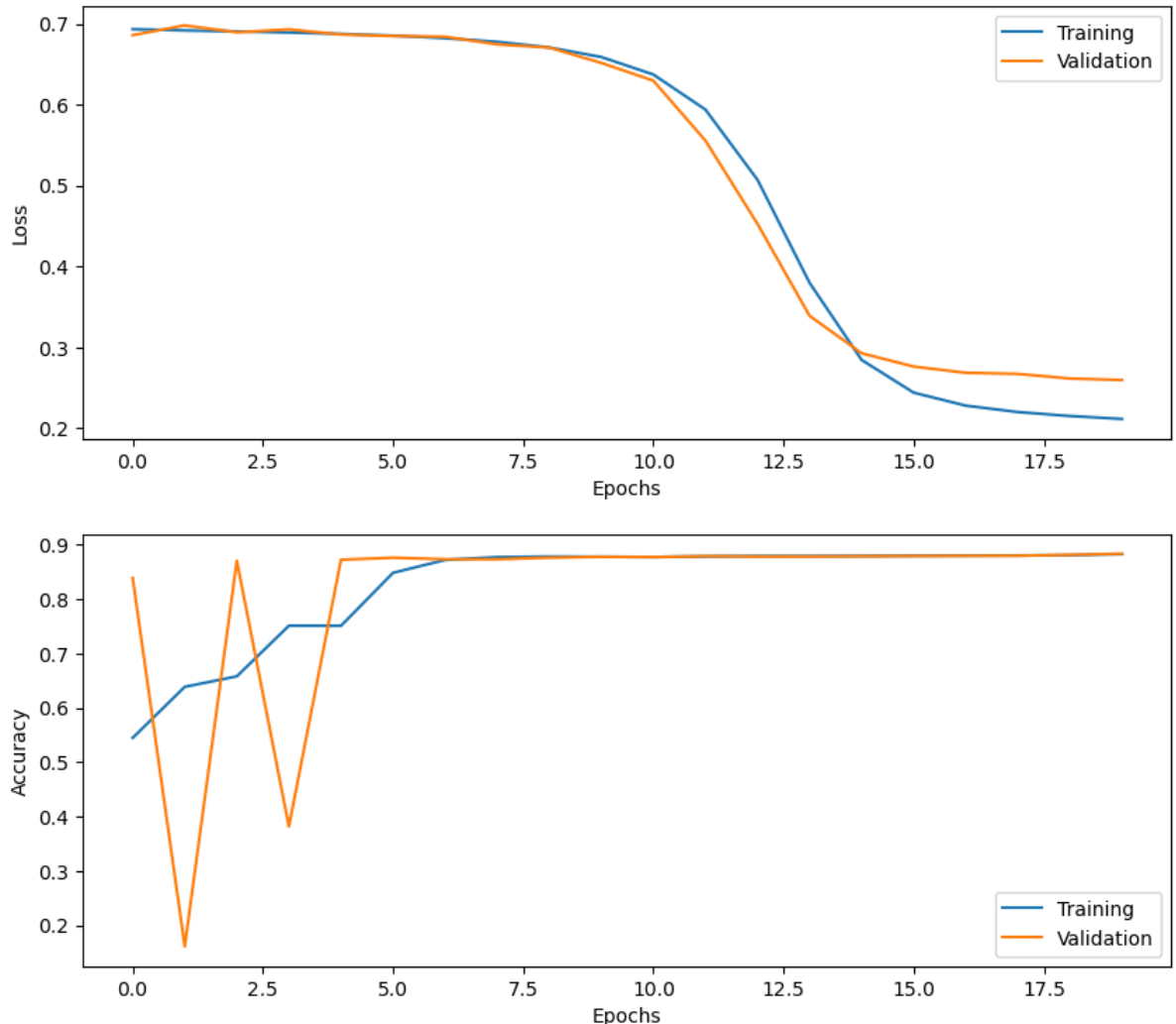
In [28]: # Evaluate model on test data
         score = model5.evaluate(Xtest,Ytest)

```

```
print('Test loss: %.4f' % score[0])
print('Test accuracy: %.4f' % score[1])
```

```
3582/3582 [=====] - 1s 254us/step - loss: 0.2586 -
accuracy: 0.8841
Test loss: 0.2586
Test accuracy: 0.8841
```

In [29]: `plot_results(history5)`



## Part 15: Batch normalization

Now add batch normalization after each dense layer in `build_DNN`. Remember to import `BatchNormalization` from `keras.layers`.

See <https://keras.io/layers/normalization/> for information about how to call the function.

Question 14: Why is batch normalization important when training deep networks?

### Answer

- A14 : Batch normalization is important because it standardizes the inputs for each batch and increases training speed. This is especially important in deep networks with large datasets as training times can be very long.



## 2 layers, 20 nodes, class weights, batch normalization

```
In [30]: # Setup some training parameters
batch_size = 10000
epochs = 20
input_shape = X.shape[1:]

# Build and train model
model6 = build_DNN(input_shape=input_shape,n_layers= 2,n_nodes=20,act_fun='s
history6 = model6.fit(x = Xtrain,y = Ytrain,batch_size = batch_size,validati
```

```

Epoch 1/20
54/54 [=====] - 0s 4ms/step - loss: 0.6655 - accuracy: 0.6485 - val_loss: 0.6123 - val_accuracy: 0.8837
Epoch 2/20
54/54 [=====] - 0s 3ms/step - loss: 0.5349 - accuracy: 0.8829 - val_loss: 0.4497 - val_accuracy: 0.8812
Epoch 3/20
54/54 [=====] - 0s 3ms/step - loss: 0.3702 - accuracy: 0.8809 - val_loss: 0.3294 - val_accuracy: 0.8800
Epoch 4/20
54/54 [=====] - 0s 4ms/step - loss: 0.2748 - accuracy: 0.8806 - val_loss: 0.2872 - val_accuracy: 0.8803
Epoch 5/20
54/54 [=====] - 0s 3ms/step - loss: 0.2387 - accuracy: 0.8812 - val_loss: 0.2715 - val_accuracy: 0.8810
Epoch 6/20
54/54 [=====] - 0s 3ms/step - loss: 0.2235 - accuracy: 0.8822 - val_loss: 0.2640 - val_accuracy: 0.8828
Epoch 7/20
54/54 [=====] - 0s 3ms/step - loss: 0.2153 - accuracy: 0.8845 - val_loss: 0.2601 - val_accuracy: 0.8855
Epoch 8/20
54/54 [=====] - 0s 3ms/step - loss: 0.2099 - accuracy: 0.8870 - val_loss: 0.2552 - val_accuracy: 0.8882
Epoch 9/20
54/54 [=====] - 0s 3ms/step - loss: 0.2059 - accuracy: 0.8894 - val_loss: 0.2525 - val_accuracy: 0.8902
Epoch 10/20
54/54 [=====] - 0s 3ms/step - loss: 0.2026 - accuracy: 0.8921 - val_loss: 0.2485 - val_accuracy: 0.8937
Epoch 11/20
54/54 [=====] - 0s 3ms/step - loss: 0.1999 - accuracy: 0.8950 - val_loss: 0.2468 - val_accuracy: 0.8955
Epoch 12/20
54/54 [=====] - 0s 3ms/step - loss: 0.1976 - accuracy: 0.8969 - val_loss: 0.2450 - val_accuracy: 0.8973
Epoch 13/20
54/54 [=====] - 0s 3ms/step - loss: 0.1956 - accuracy: 0.8981 - val_loss: 0.2428 - val_accuracy: 0.8980
Epoch 14/20
54/54 [=====] - 0s 3ms/step - loss: 0.1938 - accuracy: 0.8988 - val_loss: 0.2411 - val_accuracy: 0.8986
Epoch 15/20
54/54 [=====] - 0s 3ms/step - loss: 0.1922 - accuracy: 0.8994 - val_loss: 0.2398 - val_accuracy: 0.8992
Epoch 16/20
54/54 [=====] - 0s 3ms/step - loss: 0.1908 - accuracy: 0.8998 - val_loss: 0.2388 - val_accuracy: 0.8997
Epoch 17/20
54/54 [=====] - 0s 3ms/step - loss: 0.1896 - accuracy: 0.9002 - val_loss: 0.2371 - val_accuracy: 0.9001
Epoch 18/20
54/54 [=====] - 0s 3ms/step - loss: 0.1884 - accuracy: 0.9005 - val_loss: 0.2368 - val_accuracy: 0.9004
Epoch 19/20
54/54 [=====] - 0s 3ms/step - loss: 0.1874 - accuracy: 0.9011 - val_loss: 0.2342 - val_accuracy: 0.9013
Epoch 20/20
54/54 [=====] - 0s 3ms/step - loss: 0.1864 - accuracy: 0.9019 - val_loss: 0.2339 - val_accuracy: 0.9021

```

```

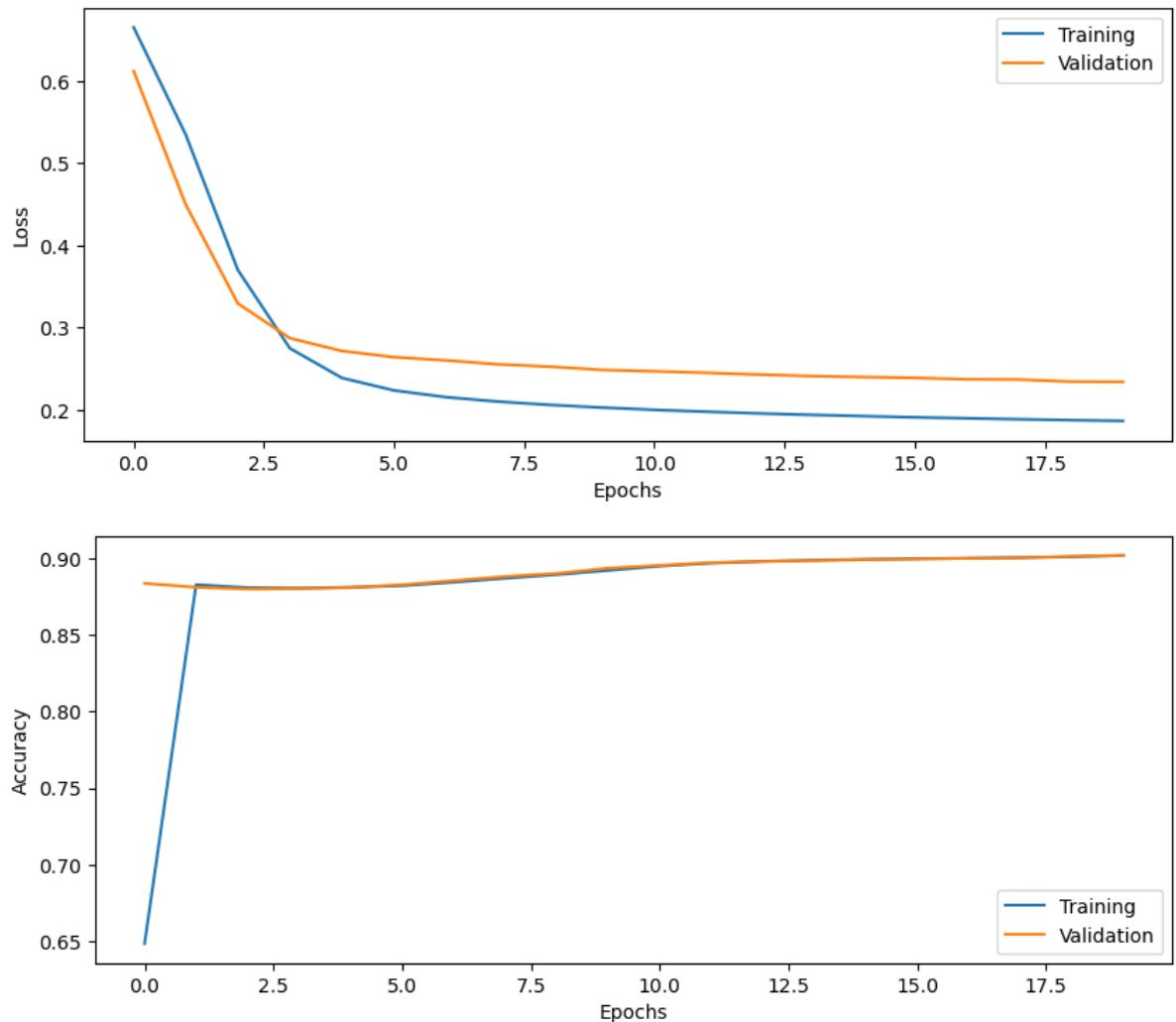
In [31]: # Evaluate model on test data
         score = model6.evaluate(Xtest,Ytest)

```

```
print('Test loss: %.4f' % score[0])
print('Test accuracy: %.4f' % score[1])
```

```
3582/3582 [=====] - 1s 227us/step - loss: 0.2333 -
accuracy: 0.9025
Test loss: 0.2333
Test accuracy: 0.9025
```

In [32]: `plot_results(history6)`



## Part 16: Activation function

Try changing the activation function in each layer from sigmoid to ReLU, write down the test accuracy.

Note: the last layer should still have a sigmoid activation function.

<https://keras.io/api/layers/activations/>

**2 layers, 20 nodes, class weights, ReLU, no batch normalization**

```
In [33]: # Setup some training parameters
batch_size = 10000
epochs = 20
input_shape = X.shape[1:]
```

```
# Build and train model
model7 = build_DNN(input_shape=input_shape,n_layers= 2,n_nodes=20,act_fun='R
history7 = model7.fit(x = Xtrain,y = Ytrain,batch_size = batch_size,validati
```

```
Epoch 1/20
54/54 [=====] - 0s 4ms/step - loss: 0.3232 - accuracy: 0.8627 - val_loss: 0.2774 - val_accuracy: 0.8855
Epoch 2/20
54/54 [=====] - 0s 3ms/step - loss: 0.2080 - accuracy: 0.8901 - val_loss: 0.2505 - val_accuracy: 0.8927
Epoch 3/20
54/54 [=====] - 0s 3ms/step - loss: 0.1932 - accuracy: 0.8949 - val_loss: 0.2414 - val_accuracy: 0.8966
Epoch 4/20
54/54 [=====] - 0s 3ms/step - loss: 0.1857 - accuracy: 0.9003 - val_loss: 0.2350 - val_accuracy: 0.9031
Epoch 5/20
54/54 [=====] - 0s 3ms/step - loss: 0.1813 - accuracy: 0.9044 - val_loss: 0.2297 - val_accuracy: 0.9051
Epoch 6/20
54/54 [=====] - 0s 3ms/step - loss: 0.1781 - accuracy: 0.9064 - val_loss: 0.2260 - val_accuracy: 0.9080
Epoch 7/20
54/54 [=====] - 0s 3ms/step - loss: 0.1754 - accuracy: 0.9088 - val_loss: 0.2247 - val_accuracy: 0.9090
Epoch 8/20
54/54 [=====] - 0s 3ms/step - loss: 0.1733 - accuracy: 0.9099 - val_loss: 0.2231 - val_accuracy: 0.9100
Epoch 9/20
54/54 [=====] - 0s 3ms/step - loss: 0.1716 - accuracy: 0.9113 - val_loss: 0.2181 - val_accuracy: 0.9119
Epoch 10/20
54/54 [=====] - 0s 3ms/step - loss: 0.1700 - accuracy: 0.9125 - val_loss: 0.2171 - val_accuracy: 0.9129
Epoch 11/20
54/54 [=====] - 0s 3ms/step - loss: 0.1687 - accuracy: 0.9133 - val_loss: 0.2146 - val_accuracy: 0.9137
Epoch 12/20
54/54 [=====] - 0s 3ms/step - loss: 0.1676 - accuracy: 0.9144 - val_loss: 0.2133 - val_accuracy: 0.9149
Epoch 13/20
54/54 [=====] - 0s 3ms/step - loss: 0.1666 - accuracy: 0.9154 - val_loss: 0.2153 - val_accuracy: 0.9153
Epoch 14/20
54/54 [=====] - 0s 3ms/step - loss: 0.1657 - accuracy: 0.9157 - val_loss: 0.2154 - val_accuracy: 0.9155
Epoch 15/20
54/54 [=====] - 0s 3ms/step - loss: 0.1650 - accuracy: 0.9158 - val_loss: 0.2119 - val_accuracy: 0.9160
Epoch 16/20
54/54 [=====] - 0s 3ms/step - loss: 0.1644 - accuracy: 0.9160 - val_loss: 0.2103 - val_accuracy: 0.9161
Epoch 17/20
54/54 [=====] - 0s 3ms/step - loss: 0.1638 - accuracy: 0.9162 - val_loss: 0.2125 - val_accuracy: 0.9163
Epoch 18/20
54/54 [=====] - 0s 3ms/step - loss: 0.1633 - accuracy: 0.9163 - val_loss: 0.2089 - val_accuracy: 0.9165
Epoch 19/20
54/54 [=====] - 0s 3ms/step - loss: 0.1628 - accuracy: 0.9165 - val_loss: 0.2104 - val_accuracy: 0.9162
Epoch 20/20
54/54 [=====] - 0s 3ms/step - loss: 0.1624 - accuracy: 0.9165 - val_loss: 0.2073 - val_accuracy: 0.9166
```

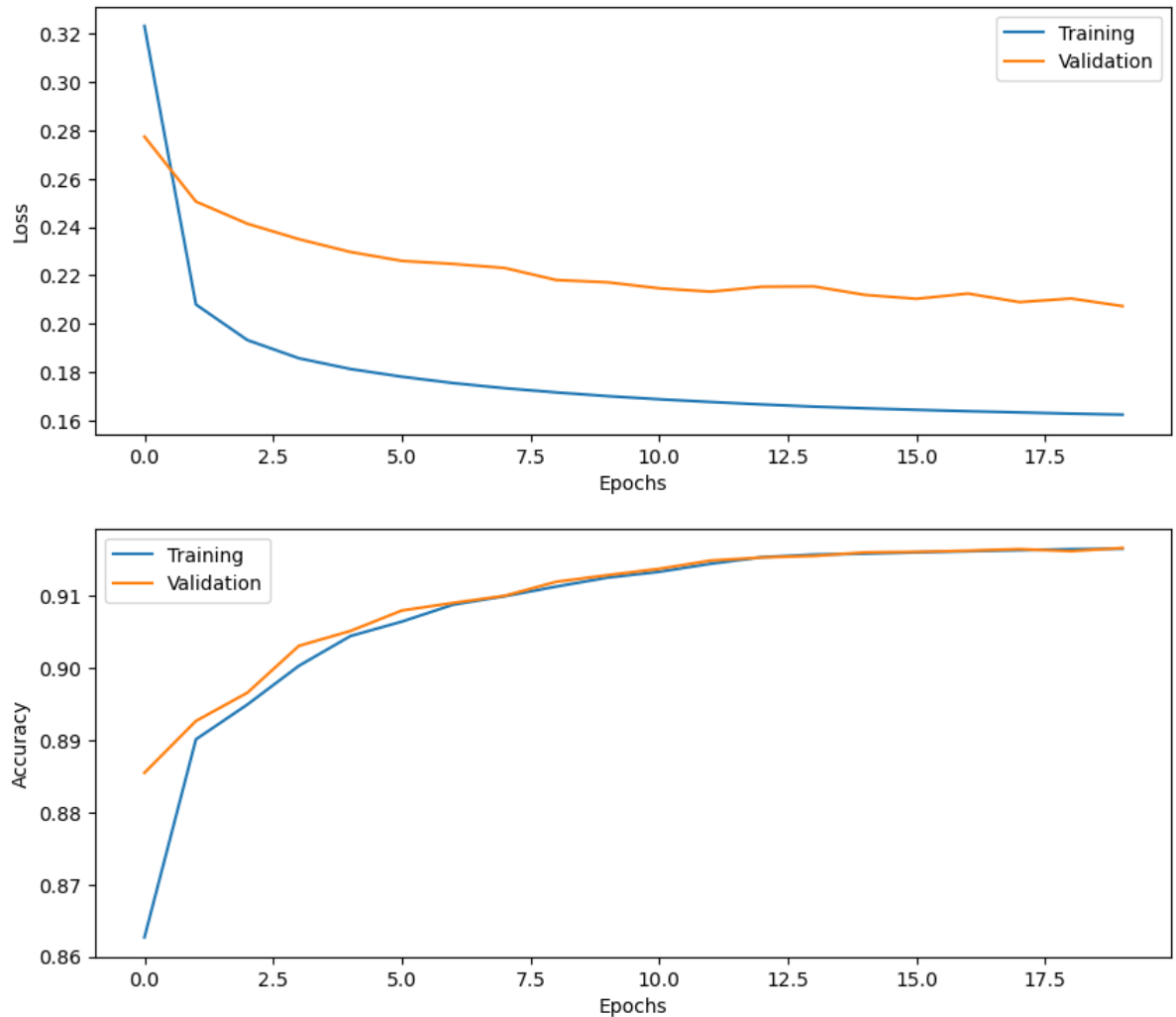
In [ ]:

```
In [34]: # Evaluate model on test data
score = model7.evaluate(Xtest,Ytest)

print('Test loss: %.4f' % score[0])
print('Test accuracy: %.4f' % score[1])
```

```
3582/3582 [=====] - 1s 225us/step - loss: 0.2062 -
accuracy: 0.9165
Test loss: 0.2062
Test accuracy: 0.9165
```

```
In [35]: plot_results(history7)
```



```
In [36]: print(f'The test accuracy is {score[1]}')
```

```
The test accuracy is 0.9165423512458801
```

## Part 17: Optimizer

Try changing the optimizer from SGD to Adam (with learning rate 0.1 as before).  
Remember to import the Adam optimizer from `keras.optimizers`.

<https://keras.io/optimizers/>

**2 layers, 20 nodes, class weights, Adam optimizer, no batch normalization, sigmoid activations**

```
In [37]: # Setup some training parameters
batch_size = 10000
epochs = 20
input_shape = X.shape[1:]

# Build and train model
model8 = build_DNN(input_shape,n_layers= 2,n_nodes=20,act_fun='ReLU',optimiz
history8 = model8.fit(Xtrain,Ytrain,batch_size = batch_size,epochs = epochs,
```

```

Epoch 1/20
54/54 [=====] - 0s 4ms/step - loss: 0.2342 - accuracy: 0.8930 - val_loss: 0.2332 - val_accuracy: 0.9017
Epoch 2/20
54/54 [=====] - 0s 3ms/step - loss: 0.1763 - accuracy: 0.9059 - val_loss: 0.2511 - val_accuracy: 0.9060
Epoch 3/20
54/54 [=====] - 0s 3ms/step - loss: 0.1709 - accuracy: 0.9115 - val_loss: 0.2023 - val_accuracy: 0.9151
Epoch 4/20
54/54 [=====] - 0s 3ms/step - loss: 0.1608 - accuracy: 0.9163 - val_loss: 0.2067 - val_accuracy: 0.9170
Epoch 5/20
54/54 [=====] - 0s 3ms/step - loss: 0.1574 - accuracy: 0.9175 - val_loss: 0.2033 - val_accuracy: 0.9177
Epoch 6/20
54/54 [=====] - 0s 3ms/step - loss: 0.1552 - accuracy: 0.9190 - val_loss: 0.2177 - val_accuracy: 0.9180
Epoch 7/20
54/54 [=====] - 0s 3ms/step - loss: 0.1531 - accuracy: 0.9196 - val_loss: 0.1771 - val_accuracy: 0.9202
Epoch 8/20
54/54 [=====] - 0s 3ms/step - loss: 0.1535 - accuracy: 0.9199 - val_loss: 0.2026 - val_accuracy: 0.9200
Epoch 9/20
54/54 [=====] - 0s 3ms/step - loss: 0.1536 - accuracy: 0.9199 - val_loss: 0.1934 - val_accuracy: 0.9207
Epoch 10/20
54/54 [=====] - 0s 3ms/step - loss: 0.1498 - accuracy: 0.9211 - val_loss: 0.1744 - val_accuracy: 0.9209
Epoch 11/20
54/54 [=====] - 0s 4ms/step - loss: 0.1479 - accuracy: 0.9211 - val_loss: 0.1801 - val_accuracy: 0.9205
Epoch 12/20
54/54 [=====] - 0s 3ms/step - loss: 0.1456 - accuracy: 0.9221 - val_loss: 0.1753 - val_accuracy: 0.9231
Epoch 13/20
54/54 [=====] - 0s 3ms/step - loss: 0.1474 - accuracy: 0.9206 - val_loss: 0.1998 - val_accuracy: 0.9218
Epoch 14/20
54/54 [=====] - 0s 3ms/step - loss: 0.1448 - accuracy: 0.9235 - val_loss: 0.1691 - val_accuracy: 0.9250
Epoch 15/20
54/54 [=====] - 0s 3ms/step - loss: 0.1429 - accuracy: 0.9243 - val_loss: 0.1761 - val_accuracy: 0.9266
Epoch 16/20
54/54 [=====] - 0s 3ms/step - loss: 0.1521 - accuracy: 0.9193 - val_loss: 0.1538 - val_accuracy: 0.9176
Epoch 17/20
54/54 [=====] - 0s 3ms/step - loss: 0.1421 - accuracy: 0.9222 - val_loss: 0.1747 - val_accuracy: 0.9239
Epoch 18/20
54/54 [=====] - 0s 3ms/step - loss: 0.1434 - accuracy: 0.9247 - val_loss: 0.1583 - val_accuracy: 0.9277
Epoch 19/20
54/54 [=====] - 0s 3ms/step - loss: 0.1412 - accuracy: 0.9256 - val_loss: 0.1956 - val_accuracy: 0.9238
Epoch 20/20
54/54 [=====] - 0s 4ms/step - loss: 0.1380 - accuracy: 0.9280 - val_loss: 0.1368 - val_accuracy: 0.9343

```

```

In [38]: # Evaluate model on test data
         score = model8.evaluate(Xtest,Ytest)

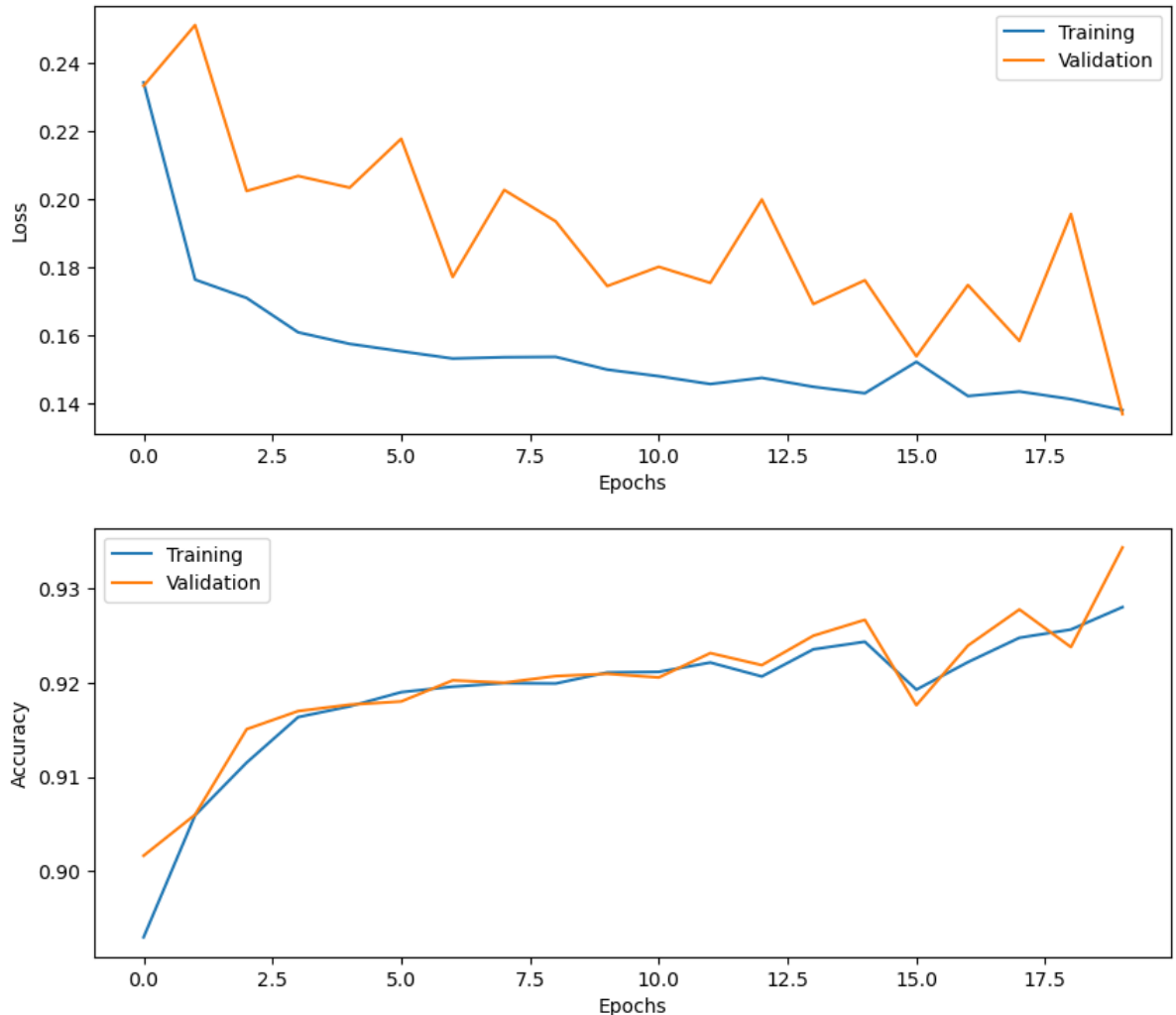
```



```
print('Test loss: %.4f' % score[0])
print('Test accuracy: %.4f' % score[1])
```

```
3582/3582 [=====] - 1s 226us/step - loss: 0.1374 -
accuracy: 0.9340
Test loss: 0.1374
Test accuracy: 0.9340
```

```
In [39]: plot_results(history8)
```



## Part 18: Dropout regularization

Dropout is a type of regularization that can improve accuracy for validation and test data. It randomly removes connections to force the neural network to not rely too much on a small number of weights.

Add a Dropout layer after each Dense layer (but not after the final dense layer) in `build_DNN`, with a dropout probability of 50%. Remember to first import the Dropout layer from `keras.layers`

See [https://keras.io/api/layers/regularization\\_layers/dropout/](https://keras.io/api/layers/regularization_layers/dropout/) for how the Dropout layer works.

---

Question 15: How does the validation accuracy change when adding dropout?

Question 16: How does the test accuracy change when adding dropout?

## Answer

- A15: Comparing the results below to the results obtained in part 12, we see that the validation accuracy is not discernibly different even while using dropout.
- A16: Similarly, the test accuracy is not affected by the addition of dropout regularization. Given that dropout regularization is a method that may increase accuracy for test and validation data, the lack of such an increase in accuracy while using dropout leads us to conclude that the neural network used is perhaps not deep enough to rely excessively on a certain weights.

**2 layers, 20 nodes, class weights, dropout, SGD optimizer, no batch normalization, sigmoid activations**

```
In [41]: # Setup some training parameters
batch_size = 10000
epochs = 20
input_shape = X.shape[1:]

# Build and train model
model9 = build_DNN(input_shape, n_layers= 2, n_nodes=20, act_fun='sigmoid', opti
history9 = model9.fit(Xtrain, Ytrain, batch_size = batch_size, epochs = epochs,
```

```

Epoch 1/20
54/54 [=====] - 0s 4ms/step - loss: 0.6746 - accuracy: 0.8635 - val_loss: 0.6144 - val_accuracy: 0.8780
Epoch 2/20
54/54 [=====] - 0s 3ms/step - loss: 0.5398 - accuracy: 0.8819 - val_loss: 0.4572 - val_accuracy: 0.8817
Epoch 3/20
54/54 [=====] - 0s 3ms/step - loss: 0.3744 - accuracy: 0.8810 - val_loss: 0.3338 - val_accuracy: 0.8797
Epoch 4/20
54/54 [=====] - 0s 4ms/step - loss: 0.2781 - accuracy: 0.8802 - val_loss: 0.2903 - val_accuracy: 0.8798
Epoch 5/20
54/54 [=====] - 0s 3ms/step - loss: 0.2420 - accuracy: 0.8805 - val_loss: 0.2764 - val_accuracy: 0.8808
Epoch 6/20
54/54 [=====] - 0s 3ms/step - loss: 0.2267 - accuracy: 0.8816 - val_loss: 0.2678 - val_accuracy: 0.8825
Epoch 7/20
54/54 [=====] - 0s 4ms/step - loss: 0.2183 - accuracy: 0.8840 - val_loss: 0.2634 - val_accuracy: 0.8846
Epoch 8/20
54/54 [=====] - 0s 4ms/step - loss: 0.2127 - accuracy: 0.8862 - val_loss: 0.2587 - val_accuracy: 0.8869
Epoch 9/20
54/54 [=====] - 0s 4ms/step - loss: 0.2085 - accuracy: 0.8880 - val_loss: 0.2552 - val_accuracy: 0.8884
Epoch 10/20
54/54 [=====] - 0s 3ms/step - loss: 0.2052 - accuracy: 0.8896 - val_loss: 0.2523 - val_accuracy: 0.8908
Epoch 11/20
54/54 [=====] - 0s 4ms/step - loss: 0.2024 - accuracy: 0.8921 - val_loss: 0.2499 - val_accuracy: 0.8925
Epoch 12/20
54/54 [=====] - 0s 4ms/step - loss: 0.2000 - accuracy: 0.8938 - val_loss: 0.2472 - val_accuracy: 0.8946
Epoch 13/20
54/54 [=====] - 0s 4ms/step - loss: 0.1979 - accuracy: 0.8957 - val_loss: 0.2448 - val_accuracy: 0.8961
Epoch 14/20
54/54 [=====] - 0s 4ms/step - loss: 0.1960 - accuracy: 0.8971 - val_loss: 0.2427 - val_accuracy: 0.8973
Epoch 15/20
54/54 [=====] - 0s 4ms/step - loss: 0.1944 - accuracy: 0.8981 - val_loss: 0.2420 - val_accuracy: 0.8979
Epoch 16/20
54/54 [=====] - 0s 4ms/step - loss: 0.1929 - accuracy: 0.8987 - val_loss: 0.2398 - val_accuracy: 0.8984
Epoch 17/20
54/54 [=====] - 0s 4ms/step - loss: 0.1916 - accuracy: 0.8992 - val_loss: 0.2394 - val_accuracy: 0.8990
Epoch 18/20
54/54 [=====] - 0s 4ms/step - loss: 0.1904 - accuracy: 0.8996 - val_loss: 0.2378 - val_accuracy: 0.8996
Epoch 19/20
54/54 [=====] - 0s 4ms/step - loss: 0.1893 - accuracy: 0.9001 - val_loss: 0.2364 - val_accuracy: 0.9001
Epoch 20/20
54/54 [=====] - 0s 4ms/step - loss: 0.1883 - accuracy: 0.9006 - val_loss: 0.2359 - val_accuracy: 0.9005

```

```

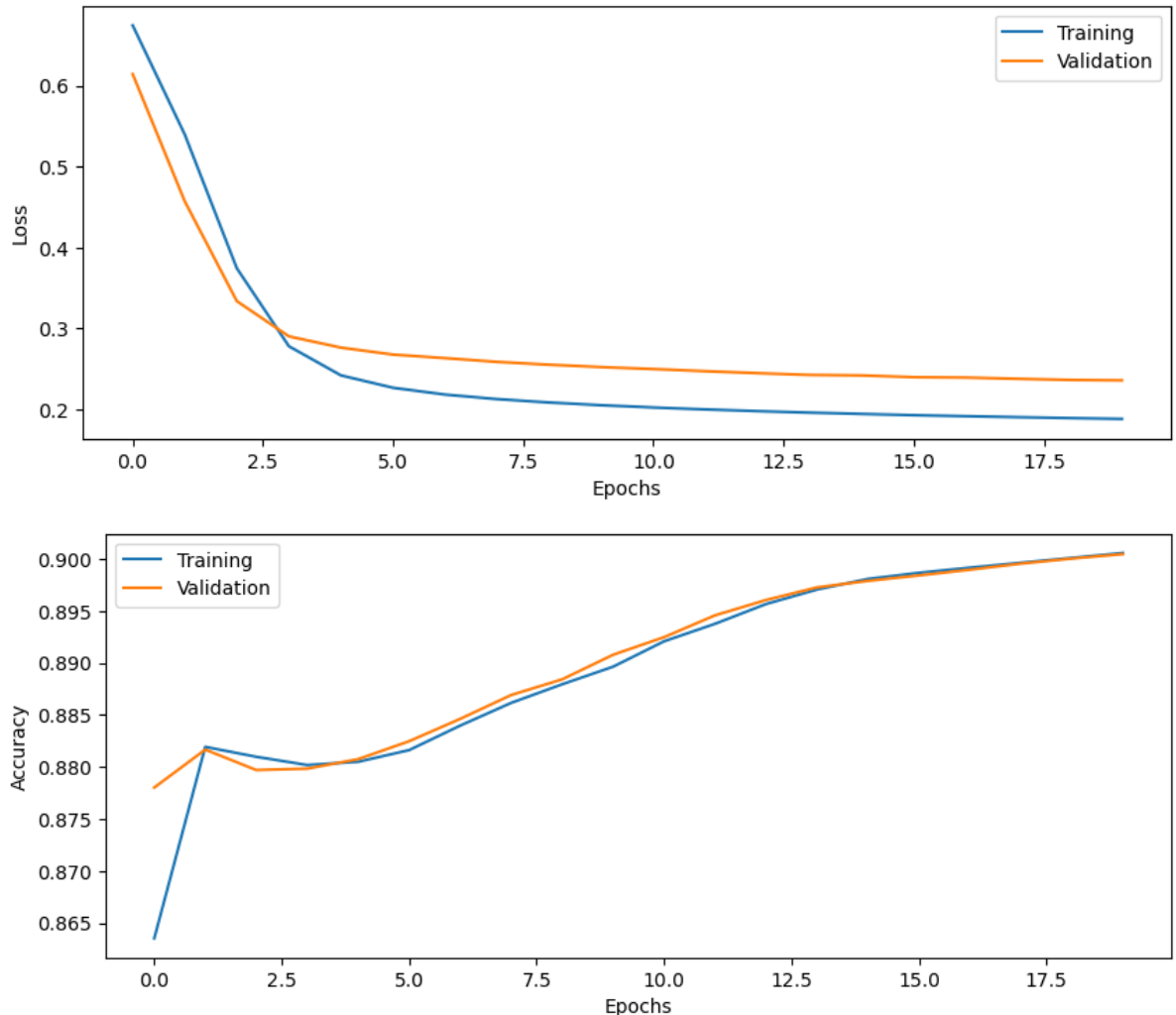
In [42]: # Evaluate model on test data
         score = model9.evaluate(Xtest,Ytest)

```

```
print('Test loss: %.4f' % score[0])
print('Test accuracy: %.4f' % score[1])
```

```
3582/3582 [=====] - 1s 226us/step - loss: 0.2352 -
accuracy: 0.9009
Test loss: 0.2352
Test accuracy: 0.9009
```

In [43]: `plot_results(history9)`



## Part 19: Improving performance

Spend some time (30 - 90 minutes) playing with the network architecture (number of layers, number of nodes per layer, activation function) and other hyper parameters (optimizer, learning rate, batch size, number of epochs, degree of regularization). For example, try a much deeper network. How much does the training time increase for a network with 10 layers?

Question 17: How high classification accuracy can you achieve for the test data? What is your best configuration?

```
In [247... # Find your best configuration for the DNN

# Build and train DNN
model10 = build_DNN(input_shape, n_layers=4, n_nodes=60, act_fun='sigmoid', opti
```

```
history10 = model10.fit(Xtrain,Ytrain,batch_size = 5000,epochs = 35,class_we
```

Epoch 1/35  
107/107 [=====] - 2s 12ms/step - loss: 0.2520 - accuracy: 0.8872 - val\_loss: 0.4995 - val\_accuracy: 0.8388  
Epoch 2/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1789 - accuracy: 0.9138 - val\_loss: 0.1743 - val\_accuracy: 0.9043  
Epoch 3/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1752 - accuracy: 0.9143 - val\_loss: 0.1790 - val\_accuracy: 0.9159  
Epoch 4/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1745 - accuracy: 0.9146 - val\_loss: 0.2132 - val\_accuracy: 0.9165  
Epoch 5/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1736 - accuracy: 0.9151 - val\_loss: 0.2095 - val\_accuracy: 0.9159  
Epoch 6/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1720 - accuracy: 0.9154 - val\_loss: 0.2314 - val\_accuracy: 0.9163  
Epoch 7/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1713 - accuracy: 0.9157 - val\_loss: 0.2171 - val\_accuracy: 0.9164  
Epoch 8/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1707 - accuracy: 0.9157 - val\_loss: 0.2081 - val\_accuracy: 0.9163  
Epoch 9/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1701 - accuracy: 0.9160 - val\_loss: 0.2118 - val\_accuracy: 0.9170  
Epoch 10/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1699 - accuracy: 0.9164 - val\_loss: 0.2184 - val\_accuracy: 0.9168  
Epoch 11/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1687 - accuracy: 0.9167 - val\_loss: 0.2294 - val\_accuracy: 0.9165  
Epoch 12/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1678 - accuracy: 0.9174 - val\_loss: 0.2212 - val\_accuracy: 0.9166  
Epoch 13/35  
107/107 [=====] - 1s 12ms/step - loss: 0.1683 - accuracy: 0.9172 - val\_loss: 0.2056 - val\_accuracy: 0.9186  
Epoch 14/35  
107/107 [=====] - 1s 12ms/step - loss: 0.1671 - accuracy: 0.9178 - val\_loss: 0.2183 - val\_accuracy: 0.9176  
Epoch 15/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1660 - accuracy: 0.9181 - val\_loss: 0.2222 - val\_accuracy: 0.9178  
Epoch 16/35  
107/107 [=====] - 1s 12ms/step - loss: 0.1671 - accuracy: 0.9178 - val\_loss: 0.2169 - val\_accuracy: 0.9189  
Epoch 17/35  
107/107 [=====] - 1s 12ms/step - loss: 0.1658 - accuracy: 0.9183 - val\_loss: 0.2166 - val\_accuracy: 0.9197  
Epoch 18/35  
107/107 [=====] - 1s 12ms/step - loss: 0.1653 - accuracy: 0.9185 - val\_loss: 0.2073 - val\_accuracy: 0.9189  
Epoch 19/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1653 - accuracy: 0.9185 - val\_loss: 0.2061 - val\_accuracy: 0.9206  
Epoch 20/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1654 - accuracy: 0.9189 - val\_loss: 0.2027 - val\_accuracy: 0.9206  
Epoch 21/35  
107/107 [=====] - 1s 13ms/step - loss: 0.1645 - accuracy: 0.9191 - val\_loss: 0.2132 - val\_accuracy: 0.9205  
Epoch 22/35

```

107/107 [=====] - 1s 12ms/step - loss: 0.1641 - acc
uracy: 0.9193 - val_loss: 0.2211 - val_accuracy: 0.9180
Epoch 23/35
107/107 [=====] - 1s 13ms/step - loss: 0.1637 - acc
uracy: 0.9191 - val_loss: 0.2089 - val_accuracy: 0.9211
Epoch 24/35
107/107 [=====] - 1s 13ms/step - loss: 0.1637 - acc
uracy: 0.9191 - val_loss: 0.2206 - val_accuracy: 0.9195
Epoch 25/35
107/107 [=====] - 1s 13ms/step - loss: 0.1633 - acc
uracy: 0.9189 - val_loss: 0.2074 - val_accuracy: 0.9207
Epoch 26/35
107/107 [=====] - 1s 12ms/step - loss: 0.1627 - acc
uracy: 0.9195 - val_loss: 0.2040 - val_accuracy: 0.9203
Epoch 27/35
107/107 [=====] - 1s 12ms/step - loss: 0.1626 - acc
uracy: 0.9190 - val_loss: 0.2077 - val_accuracy: 0.9213
Epoch 28/35
107/107 [=====] - 1s 12ms/step - loss: 0.1622 - acc
uracy: 0.9193 - val_loss: 0.2071 - val_accuracy: 0.9208
Epoch 29/35
107/107 [=====] - 1s 12ms/step - loss: 0.1621 - acc
uracy: 0.9196 - val_loss: 0.1870 - val_accuracy: 0.9213
Epoch 30/35
107/107 [=====] - 1s 12ms/step - loss: 0.1608 - acc
uracy: 0.9197 - val_loss: 0.2152 - val_accuracy: 0.9198
Epoch 31/35
107/107 [=====] - 1s 13ms/step - loss: 0.1605 - acc
uracy: 0.9195 - val_loss: 0.2118 - val_accuracy: 0.9211
Epoch 32/35
107/107 [=====] - 1s 12ms/step - loss: 0.1608 - acc
uracy: 0.9193 - val_loss: 0.1850 - val_accuracy: 0.9218
Epoch 33/35
107/107 [=====] - 1s 13ms/step - loss: 0.1607 - acc
uracy: 0.9193 - val_loss: 0.1896 - val_accuracy: 0.9212
Epoch 34/35
107/107 [=====] - 1s 13ms/step - loss: 0.1600 - acc
uracy: 0.9198 - val_loss: 0.1946 - val_accuracy: 0.9210
Epoch 35/35
107/107 [=====] - 1s 13ms/step - loss: 0.1592 - acc
uracy: 0.9200 - val_loss: 0.1961 - val_accuracy: 0.9211

```

```

In [248... # Evaluate DNN on test data
score = model10.evaluate(Xtest,Ytest)

print('Test loss: %.4f' % score[0])
print('Test accuracy: %.4f' % score[1])

```

```

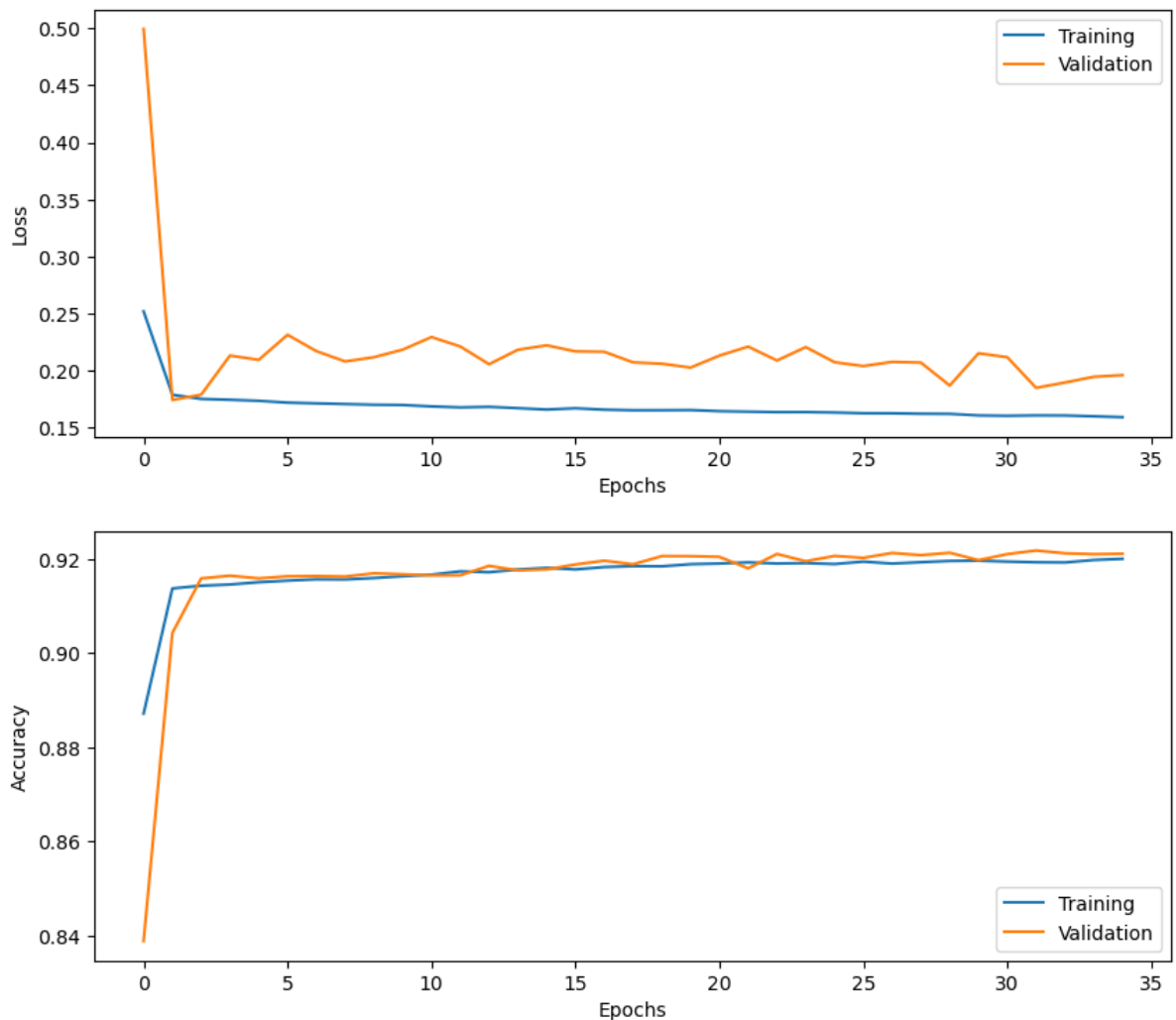
3582/3582 [=====] - 1s 291us/step - loss: 0.1964 -
accuracy: 0.9209
Test loss: 0.1964
Test accuracy: 0.9209

```

```

In [249... plot_results(history10)

```



## answer

- A17: Best configuration
- batch\_size = 5000
- epochs = 35
- n\_layers = 4
- n\_nodes=60
- act\_fun='sigmoid',
- optimizer='adam'
- learning\_rate=0.01
- use\_bn=True
- use\_dropout=True
- Highest classification for test accuracy is 92.09%

## Part 20: Dropout uncertainty

Dropout can also be used during testing, to obtain an estimate of the model uncertainty. Since dropout will randomly remove connections, the network will produce different results every time the same (test) data is put into the network. This technique is called



Monte Carlo dropout. For more information, see this paper

<http://proceedings.mlr.press/v48/gal16.pdf>

To achieve this, we need to redefine the Keras Dropout call by running the cell below, and use 'myDropout' in each call to Dropout, in the cell that defines the DNN. The

`build_DNN` function takes two boolean arguments, `use_dropout` and `use_custom_dropout`, add a standard Dropout layer if `use_dropout` is true, add a `myDropout` layer if `use_custom_dropout` is true.

Run the same test data through the trained network 100 times, with dropout turned on.

Question 18: What is the mean and the standard deviation of the test accuracy?

```
In [200... import keras.backend as K
import keras

class myDropout(keras.layers.Dropout):
    """Applies Dropout to the input.
    Dropout consists in randomly setting
    a fraction `rate` of input units to 0 at each update during training time
    which helps prevent overfitting.
    # Arguments
        rate: float between 0 and 1. Fraction of the input units to drop.
        noise_shape: 1D integer tensor representing the shape of the
            binary dropout mask that will be multiplied with the input.
            For instance, if your inputs have shape
            `(batch_size, timesteps, features)` and
            you want the dropout mask to be the same for all timesteps,
            you can use `noise_shape=(batch_size, 1, features)`.
        seed: A Python integer to use as random seed.
    # References
        - [Dropout: A Simple Way to Prevent Neural Networks from Overfitting]
          http://www.jmlr.org/papers/volume15/srivastava14a/srivastava14a.p
    """
    def __init__(self, rate, training=True, noise_shape=None, seed=None, **kwargs):
        super(myDropout, self).__init__(rate, noise_shape=None, seed=None, **kwargs)
        self.training = training

    def call(self, inputs, training=None):
        if 0. < self.rate < 1.:
            noise_shape = self._get_noise_shape(inputs)

            def dropped_inputs():
                return K.dropout(inputs, self.rate, noise_shape,
                                seed=self.seed)

            if not training:
                return K.in_train_phase(dropped_inputs, inputs, training=self.training)
            return K.in_train_phase(dropped_inputs, inputs, training=training)
        return inputs
```

## Your best config, custom dropout

```
In [250... # Your best training parameters
batch_size = 5000
epochs = 35
```

```
# Build and train model
model11 = build_DNN(input_shape,n_layers=4,n_nodes=60,act_fun='sigmoid',opti
history11 = model11.fit(Xtrain,Ytrain,batch_size = batch_size,epochs = epoch
```

Epoch 1/35  
107/107 [=====] - 3s 18ms/step - loss: 0.3133 - accuracy: 0.8559 - val\_loss: 0.2365 - val\_accuracy: 0.8388  
Epoch 2/35  
107/107 [=====] - 2s 17ms/step - loss: 0.2084 - accuracy: 0.8976 - val\_loss: 0.1688 - val\_accuracy: 0.9105  
Epoch 3/35  
107/107 [=====] - 2s 18ms/step - loss: 0.1922 - accuracy: 0.9080 - val\_loss: 0.1861 - val\_accuracy: 0.9140  
Epoch 4/35  
107/107 [=====] - 2s 19ms/step - loss: 0.1876 - accuracy: 0.9102 - val\_loss: 0.2095 - val\_accuracy: 0.9127  
Epoch 5/35  
107/107 [=====] - 2s 17ms/step - loss: 0.1844 - accuracy: 0.9115 - val\_loss: 0.2173 - val\_accuracy: 0.9142  
Epoch 6/35  
107/107 [=====] - 2s 18ms/step - loss: 0.1813 - accuracy: 0.9124 - val\_loss: 0.2149 - val\_accuracy: 0.9148  
Epoch 7/35  
107/107 [=====] - 2s 17ms/step - loss: 0.1801 - accuracy: 0.9132 - val\_loss: 0.2288 - val\_accuracy: 0.9134  
Epoch 8/35  
107/107 [=====] - 2s 17ms/step - loss: 0.1777 - accuracy: 0.9132 - val\_loss: 0.2260 - val\_accuracy: 0.9146  
Epoch 9/35  
107/107 [=====] - 2s 17ms/step - loss: 0.1780 - accuracy: 0.9127 - val\_loss: 0.2250 - val\_accuracy: 0.9138  
Epoch 10/35  
107/107 [=====] - 2s 17ms/step - loss: 0.1768 - accuracy: 0.9132 - val\_loss: 0.2242 - val\_accuracy: 0.9139  
Epoch 11/35  
107/107 [=====] - 2s 19ms/step - loss: 0.1756 - accuracy: 0.9134 - val\_loss: 0.2256 - val\_accuracy: 0.9149  
Epoch 12/35  
107/107 [=====] - 2s 17ms/step - loss: 0.1750 - accuracy: 0.9138 - val\_loss: 0.2183 - val\_accuracy: 0.9150  
Epoch 13/35  
107/107 [=====] - 2s 17ms/step - loss: 0.1745 - accuracy: 0.9137 - val\_loss: 0.2147 - val\_accuracy: 0.9147  
Epoch 14/35  
107/107 [=====] - 2s 17ms/step - loss: 0.1747 - accuracy: 0.9134 - val\_loss: 0.2106 - val\_accuracy: 0.9148  
Epoch 15/35  
107/107 [=====] - 2s 17ms/step - loss: 0.1747 - accuracy: 0.9136 - val\_loss: 0.2267 - val\_accuracy: 0.9145  
Epoch 16/35  
107/107 [=====] - 2s 19ms/step - loss: 0.1738 - accuracy: 0.9141 - val\_loss: 0.2125 - val\_accuracy: 0.9148  
Epoch 17/35  
107/107 [=====] - 2s 19ms/step - loss: 0.1735 - accuracy: 0.9141 - val\_loss: 0.2149 - val\_accuracy: 0.9156  
Epoch 18/35  
107/107 [=====] - 2s 19ms/step - loss: 0.1740 - accuracy: 0.9141 - val\_loss: 0.2185 - val\_accuracy: 0.9151  
Epoch 19/35  
107/107 [=====] - 2s 17ms/step - loss: 0.1734 - accuracy: 0.9141 - val\_loss: 0.2335 - val\_accuracy: 0.9151  
Epoch 20/35  
107/107 [=====] - 2s 17ms/step - loss: 0.1739 - accuracy: 0.9142 - val\_loss: 0.2188 - val\_accuracy: 0.9145  
Epoch 21/35  
107/107 [=====] - 2s 16ms/step - loss: 0.1730 - accuracy: 0.9141 - val\_loss: 0.2178 - val\_accuracy: 0.9151  
Epoch 22/35

```

107/107 [=====] - 2s 18ms/step - loss: 0.1731 - acc
uracy: 0.9143 - val_loss: 0.2081 - val_accuracy: 0.9153
Epoch 23/35
107/107 [=====] - 2s 17ms/step - loss: 0.1727 - acc
uracy: 0.9143 - val_loss: 0.2198 - val_accuracy: 0.9153
Epoch 24/35
107/107 [=====] - 2s 18ms/step - loss: 0.1727 - acc
uracy: 0.9145 - val_loss: 0.2020 - val_accuracy: 0.9154
Epoch 25/35
107/107 [=====] - 2s 18ms/step - loss: 0.1730 - acc
uracy: 0.9143 - val_loss: 0.2225 - val_accuracy: 0.9155
Epoch 26/35
107/107 [=====] - 2s 17ms/step - loss: 0.1719 - acc
uracy: 0.9147 - val_loss: 0.2152 - val_accuracy: 0.9154
Epoch 27/35
107/107 [=====] - 2s 19ms/step - loss: 0.1725 - acc
uracy: 0.9144 - val_loss: 0.2207 - val_accuracy: 0.9154
Epoch 28/35
107/107 [=====] - 2s 20ms/step - loss: 0.1731 - acc
uracy: 0.9145 - val_loss: 0.2092 - val_accuracy: 0.9153
Epoch 29/35
107/107 [=====] - 2s 18ms/step - loss: 0.1729 - acc
uracy: 0.9145 - val_loss: 0.2138 - val_accuracy: 0.9153
Epoch 30/35
107/107 [=====] - 2s 17ms/step - loss: 0.1725 - acc
uracy: 0.9143 - val_loss: 0.2088 - val_accuracy: 0.9158
Epoch 31/35
107/107 [=====] - 2s 17ms/step - loss: 0.1728 - acc
uracy: 0.9145 - val_loss: 0.2146 - val_accuracy: 0.9157
Epoch 32/35
107/107 [=====] - 2s 17ms/step - loss: 0.1732 - acc
uracy: 0.9143 - val_loss: 0.2148 - val_accuracy: 0.9156
Epoch 33/35
107/107 [=====] - 2s 17ms/step - loss: 0.1728 - acc
uracy: 0.9143 - val_loss: 0.2239 - val_accuracy: 0.9156
Epoch 34/35
107/107 [=====] - 2s 17ms/step - loss: 0.1733 - acc
uracy: 0.9141 - val_loss: 0.2250 - val_accuracy: 0.9153
Epoch 35/35
107/107 [=====] - 2s 17ms/step - loss: 0.1727 - acc
uracy: 0.9144 - val_loss: 0.2239 - val_accuracy: 0.9151

```

```

In [251]: # Run this cell a few times to evaluate the model on test data,
# if you get slightly different test accuracy every time, Dropout during tes

# Evaluate model on test data
score = model11.evaluate(Xtest,Ytest)

print('Test accuracy: %.4f' % score[1])

3582/3582 [=====] - 1s 340us/step - loss: 0.2234 -
accuracy: 0.9152
Test accuracy: 0.9152

```

```

In [252]: # Run the testing 100 times, and save the accuracies in an array

test_results = []

for i in range(0,100):
    score = model11.evaluate(Xtest,Ytest)
    test_results.append(score[1])

# Calculate and print mean and std of accuracies

```

```
print(f'Mean accuracy is {np.mean(test_results)}')  
print(f'Standard Deviation of accuracy is {np.std(test_results)}')
```

3582/3582 [=====] - 1s 342us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 340us/step - loss: 0.2236 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 339us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 340us/step - loss: 0.2232 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 348us/step - loss: 0.2237 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 339us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 353us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 349us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 342us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 340us/step - loss: 0.2238 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 339us/step - loss: 0.2236 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 340us/step - loss: 0.2234 -  
accuracy: 0.9153  
3582/3582 [=====] - 1s 339us/step - loss: 0.2238 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 339us/step - loss: 0.2233 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 339us/step - loss: 0.2235 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 349us/step - loss: 0.2235 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 339us/step - loss: 0.2236 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 340us/step - loss: 0.2234 -  
accuracy: 0.9153  
3582/3582 [=====] - 1s 340us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 340us/step - loss: 0.2237 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 339us/step - loss: 0.2236 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 355us/step - loss: 0.2236 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 380us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 365us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 362us/step - loss: 0.2234 -  
accuracy: 0.9153  
3582/3582 [=====] - 1s 347us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 337us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 337us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 339us/step - loss: 0.2236 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 348us/step - loss: 0.2238 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 339us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 340us/step - loss: 0.2237 -  
accuracy: 0.9151

3582/3582 [=====] - 1s 340us/step - loss: 0.2235 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 357us/step - loss: 0.2238 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 365us/step - loss: 0.2236 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 358us/step - loss: 0.2236 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 362us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 360us/step - loss: 0.2235 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 348us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 364us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 341us/step - loss: 0.2235 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 341us/step - loss: 0.2237 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 364us/step - loss: 0.2234 -  
accuracy: 0.9153  
3582/3582 [=====] - 1s 351us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 349us/step - loss: 0.2237 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 339us/step - loss: 0.2237 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 341us/step - loss: 0.2237 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 341us/step - loss: 0.2235 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 339us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 340us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 364us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 346us/step - loss: 0.2232 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 339us/step - loss: 0.2236 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 339us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 358us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 340us/step - loss: 0.2237 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 347us/step - loss: 0.2235 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 340us/step - loss: 0.2233 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 353us/step - loss: 0.2235 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 340us/step - loss: 0.2233 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 339us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 354us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 353us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 342us/step - loss: 0.2234 -  
accuracy: 0.9152

3582/3582 [=====] - 1s 363us/step - loss: 0.2237 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 340us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 339us/step - loss: 0.2236 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 339us/step - loss: 0.2235 -  
accuracy: 0.9153  
3582/3582 [=====] - 1s 347us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 355us/step - loss: 0.2237 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 340us/step - loss: 0.2236 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 359us/step - loss: 0.2233 -  
accuracy: 0.9153  
3582/3582 [=====] - 1s 376us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 351us/step - loss: 0.2237 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 344us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 341us/step - loss: 0.2234 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 352us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 362us/step - loss: 0.2237 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 362us/step - loss: 0.2236 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 357us/step - loss: 0.2235 -  
accuracy: 0.9153  
3582/3582 [=====] - 1s 354us/step - loss: 0.2235 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 357us/step - loss: 0.2236 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 341us/step - loss: 0.2235 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 358us/step - loss: 0.2236 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 341us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 340us/step - loss: 0.2237 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 340us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 350us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 341us/step - loss: 0.2237 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 342us/step - loss: 0.2234 -  
accuracy: 0.9153  
3582/3582 [=====] - 1s 341us/step - loss: 0.2235 -  
accuracy: 0.9153  
3582/3582 [=====] - 1s 341us/step - loss: 0.2235 -  
accuracy: 0.9151  
3582/3582 [=====] - 1s 349us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 341us/step - loss: 0.2235 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 339us/step - loss: 0.2234 -  
accuracy: 0.9152  
3582/3582 [=====] - 1s 353us/step - loss: 0.2234 -  
accuracy: 0.9153



```

3582/3582 [=====] - 1s 350us/step - loss: 0.2235 -
accuracy: 0.9152
3582/3582 [=====] - 1s 370us/step - loss: 0.2239 -
accuracy: 0.9151
3582/3582 [=====] - 1s 340us/step - loss: 0.2234 -
accuracy: 0.9152
3582/3582 [=====] - 1s 340us/step - loss: 0.2235 -
accuracy: 0.9152
Mean accuracy is 0.9151729607582092
Standard Deviation of accuracy is 5.403450932067144e-05

```

## Answer :

- A18 :
  - Mean accuracy is 91.5172%
  - Std Dev of accuracy is 0.000054

## Part 21: Cross validation uncertainty

Cross validation (CV) is often used to evaluate a model, by training and testing using different subsets of the data it is possible to get the uncertainty as the standard deviation over folds. We here use a help function from scikit-learn `test_results` the CV, see [https://scikit-learn.org/stable/modules/generated/sklearn.model\\_selection.StratifiedKFold.html](https://scikit-learn.org/stable/modules/generated/sklearn.model_selection.StratifiedKFold.html) . Use 10 folds with shuffling, random state 1234.

Note: We here assume that you have found the best hyper parameters, so here the data are only split into training and testing, no validation.

---

Question 19: What is the mean and the standard deviation of the test accuracy?

Question 20: What is the main advantage of dropout compared to CV for estimating test uncertainty? The difference may not be so large in this notebook, but imagine that you have a network that takes 24 hours to train.

## answer

- A19 : - Mean accuracy is 0.9153960585594177 ~91.5%
  - Standard Deviation of accuracy is 0.001176243275679351
- A20 : The main advantage of dropout over CV is that for large network that take a lot of time to train, the drop out method is much faster and less expensive, computationally.

```

In [253... from sklearn.model_selection import StratifiedKFold

cv_accuracy = []

# Define 10-fold cross validation
skf = StratifiedKFold(n_splits=10, random_state=1234, shuffle=True)
# Loop over cross validation folds
for i, (train_index, test_index) in enumerate(skf.split(X, Y)):

```

```

x_train_cv,x_test_cv = X[train_index],X[test_index]
y_train_cv,y_test_cv = Y[train_index],Y[test_index]

# Calculate class weights for current split
class_weights = class_weight.compute_class_weight(classes= np.unique(y_t
class_weights = {0: class_weights[0],
                  1: class_weights[1]}

# Rebuild the DNN model, to not continue training on the previously trai
model12 = build_DNN(input_shape,n_layers=4,n_nodes=60,act_fun='sigmoid',
# Fit the model with training set and class weights for this fold
history12 = model12.fit(x_train_cv,y_train_cv,batch_size = 5000,epochs =
# Evaluate the model using the test set for this fold
score = model12.evaluate(x_test_cv,y_test_cv)
# Save the test accuracy in an array
cv_accuracy.append(score[1])

# Calculate and print mean and std of accuracies

print(f'Mean accuracy is {np.mean(cv_accuracy)}')
print(f'Standard Deviation of accuracy is {np.std(cv_accuracy)}')

```

Epoch 1/35  
138/138 [=====] - 3s 15ms/step - loss: 0.2864 - accuracy: 0.8659  
Epoch 2/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1951 - accuracy: 0.9071  
Epoch 3/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1874 - accuracy: 0.9107  
Epoch 4/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1838 - accuracy: 0.9113  
Epoch 5/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1800 - accuracy: 0.9132  
Epoch 6/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1791 - accuracy: 0.9128  
Epoch 7/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1769 - accuracy: 0.9134  
Epoch 8/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1761 - accuracy: 0.9134  
Epoch 9/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1750 - accuracy: 0.9139  
Epoch 10/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1744 - accuracy: 0.9139  
Epoch 11/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1736 - accuracy: 0.9143  
Epoch 12/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1740 - accuracy: 0.9141  
Epoch 13/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1738 - accuracy: 0.9142  
Epoch 14/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1743 - accuracy: 0.9137  
Epoch 15/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1736 - accuracy: 0.9141  
Epoch 16/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1733 - accuracy: 0.9143  
Epoch 17/35  
138/138 [=====] - 3s 19ms/step - loss: 0.1730 - accuracy: 0.9146  
Epoch 18/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1723 - accuracy: 0.9146  
Epoch 19/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1730 - accuracy: 0.9143  
Epoch 20/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1727 - accuracy: 0.9146  
Epoch 21/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1734 - accuracy: 0.9142  
Epoch 22/35

138/138 [=====] - 3s 18ms/step - loss: 0.1729 - accuracy: 0.9146  
Epoch 23/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1737 - accuracy: 0.9138  
Epoch 24/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1732 - accuracy: 0.9143  
Epoch 25/35  
138/138 [=====] - 3s 18ms/step - loss: 0.1728 - accuracy: 0.9148  
Epoch 26/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1729 - accuracy: 0.9146  
Epoch 27/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1725 - accuracy: 0.9148  
Epoch 28/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1721 - accuracy: 0.9148  
Epoch 29/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1729 - accuracy: 0.9145  
Epoch 30/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1728 - accuracy: 0.9145  
Epoch 31/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1721 - accuracy: 0.9148  
Epoch 32/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1721 - accuracy: 0.9149  
Epoch 33/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1723 - accuracy: 0.9148  
Epoch 34/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1721 - accuracy: 0.9149  
Epoch 35/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1729 - accuracy: 0.9143  
2388/2388 [=====] - 1s 392us/step - loss: 0.2102 - accuracy: 0.9149  
Epoch 1/35  
138/138 [=====] - 3s 15ms/step - loss: 0.2900 - accuracy: 0.8635  
Epoch 2/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1979 - accuracy: 0.9046  
Epoch 3/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1886 - accuracy: 0.9096  
Epoch 4/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1843 - accuracy: 0.9112  
Epoch 5/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1807 - accuracy: 0.9127  
Epoch 6/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1800 - accuracy: 0.9124  
Epoch 7/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1774 - accuracy: 0.9129

Epoch 8/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1771 - accuracy: 0.9131  
Epoch 9/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1768 - accuracy: 0.9129  
Epoch 10/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1761 - accuracy: 0.9131  
Epoch 11/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1757 - accuracy: 0.9132  
Epoch 12/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1743 - accuracy: 0.9138  
Epoch 13/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1743 - accuracy: 0.9136  
Epoch 14/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1746 - accuracy: 0.9134  
Epoch 15/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1740 - accuracy: 0.9138  
Epoch 16/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1732 - accuracy: 0.9141  
Epoch 17/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1738 - accuracy: 0.9141  
Epoch 18/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1737 - accuracy: 0.9141  
Epoch 19/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1730 - accuracy: 0.9142  
Epoch 20/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1727 - accuracy: 0.9144  
Epoch 21/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1727 - accuracy: 0.9145  
Epoch 22/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1729 - accuracy: 0.9142  
Epoch 23/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1725 - accuracy: 0.9147  
Epoch 24/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1729 - accuracy: 0.9143  
Epoch 25/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1734 - accuracy: 0.9140  
Epoch 26/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1731 - accuracy: 0.9142  
Epoch 27/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1738 - accuracy: 0.9137  
Epoch 28/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1732 - accuracy: 0.9141  
Epoch 29/35

138/138 [=====] - 2s 16ms/step - loss: 0.1735 - accuracy: 0.9139  
Epoch 30/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1728 - accuracy: 0.9145  
Epoch 31/35  
138/138 [=====] - 3s 18ms/step - loss: 0.1732 - accuracy: 0.9141  
Epoch 32/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1729 - accuracy: 0.9141  
Epoch 33/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1735 - accuracy: 0.9139  
Epoch 34/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1727 - accuracy: 0.9145  
Epoch 35/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1730 - accuracy: 0.9144  
2388/2388 [=====] - 1s 352us/step - loss: 0.2017 - accuracy: 0.9176  
Epoch 1/35  
138/138 [=====] - 3s 17ms/step - loss: 0.2963 - accuracy: 0.8656  
Epoch 2/35  
138/138 [=====] - 3s 20ms/step - loss: 0.1961 - accuracy: 0.9064  
Epoch 3/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1875 - accuracy: 0.9105  
Epoch 4/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1836 - accuracy: 0.9116  
Epoch 5/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1809 - accuracy: 0.9124  
Epoch 6/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1791 - accuracy: 0.9128  
Epoch 7/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1775 - accuracy: 0.9132  
Epoch 8/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1764 - accuracy: 0.9134  
Epoch 9/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1755 - accuracy: 0.9136  
Epoch 10/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1752 - accuracy: 0.9137  
Epoch 11/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1745 - accuracy: 0.9136  
Epoch 12/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1746 - accuracy: 0.9137  
Epoch 13/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1737 - accuracy: 0.9138  
Epoch 14/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1735 - accuracy: 0.9141

Epoch 15/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1735 - accuracy: 0.9141  
Epoch 16/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1738 - accuracy: 0.9138  
Epoch 17/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1733 - accuracy: 0.9143  
Epoch 18/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1728 - accuracy: 0.9145  
Epoch 19/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1727 - accuracy: 0.9144  
Epoch 20/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1727 - accuracy: 0.9145  
Epoch 21/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1730 - accuracy: 0.9144  
Epoch 22/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1730 - accuracy: 0.9145  
Epoch 23/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1727 - accuracy: 0.9146  
Epoch 24/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1720 - accuracy: 0.9150  
Epoch 25/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1720 - accuracy: 0.9150  
Epoch 26/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1722 - accuracy: 0.9146  
Epoch 27/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1720 - accuracy: 0.9147  
Epoch 28/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1725 - accuracy: 0.9148  
Epoch 29/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1721 - accuracy: 0.9149  
Epoch 30/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1726 - accuracy: 0.9143  
Epoch 31/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1722 - accuracy: 0.9145  
Epoch 32/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1728 - accuracy: 0.9144  
Epoch 33/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1724 - accuracy: 0.9145  
Epoch 34/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1727 - accuracy: 0.9146  
Epoch 35/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1733 - accuracy: 0.9140  
2388/2388 [=====] - 1s 339us/step - loss: 0.2082 -

accuracy: 0.9151  
Epoch 1/35  
138/138 [=====] - 3s 15ms/step - loss: 0.2917 - accuracy: 0.8653  
Epoch 2/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1961 - accuracy: 0.9057  
Epoch 3/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1889 - accuracy: 0.9096  
Epoch 4/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1846 - accuracy: 0.9111  
Epoch 5/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1808 - accuracy: 0.9127  
Epoch 6/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1787 - accuracy: 0.9131  
Epoch 7/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1773 - accuracy: 0.9131  
Epoch 8/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1756 - accuracy: 0.9138  
Epoch 9/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1751 - accuracy: 0.9139  
Epoch 10/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1749 - accuracy: 0.9134  
Epoch 11/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1750 - accuracy: 0.9134  
Epoch 12/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1747 - accuracy: 0.9135  
Epoch 13/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1739 - accuracy: 0.9139  
Epoch 14/35  
138/138 [=====] - 3s 18ms/step - loss: 0.1739 - accuracy: 0.9140  
Epoch 15/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1731 - accuracy: 0.9142  
Epoch 16/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1733 - accuracy: 0.9140  
Epoch 17/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1734 - accuracy: 0.9143  
Epoch 18/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1729 - accuracy: 0.9144  
Epoch 19/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1723 - accuracy: 0.9145  
Epoch 20/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1729 - accuracy: 0.9142  
Epoch 21/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1729 - accuracy: 0.9144



Epoch 22/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1729 - accuracy: 0.9145  
Epoch 23/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1724 - accuracy: 0.9145  
Epoch 24/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1719 - accuracy: 0.9148  
Epoch 25/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1719 - accuracy: 0.9150  
Epoch 26/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1720 - accuracy: 0.9147  
Epoch 27/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1718 - accuracy: 0.9150  
Epoch 28/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1718 - accuracy: 0.9150  
Epoch 29/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1720 - accuracy: 0.9148  
Epoch 30/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1723 - accuracy: 0.9150  
Epoch 31/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1724 - accuracy: 0.9147  
Epoch 32/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1720 - accuracy: 0.9146  
Epoch 33/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1728 - accuracy: 0.9144  
Epoch 34/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1721 - accuracy: 0.9146  
Epoch 35/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1723 - accuracy: 0.9147  
2388/2388 [=====] - 1s 341us/step - loss: 0.2316 - accuracy: 0.9137  
Epoch 1/35  
138/138 [=====] - 3s 15ms/step - loss: 0.2844 - accuracy: 0.8710  
Epoch 2/35  
138/138 [=====] - 2s 15ms/step - loss: 0.1942 - accuracy: 0.9070  
Epoch 3/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1888 - accuracy: 0.9090  
Epoch 4/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1837 - accuracy: 0.9116  
Epoch 5/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1806 - accuracy: 0.9127  
Epoch 6/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1789 - accuracy: 0.9127  
Epoch 7/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1775 - accuracy: 0.9127

uracy: 0.9134  
Epoch 8/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1758 - acc  
uracy: 0.9135  
Epoch 9/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1757 - acc  
uracy: 0.9134  
Epoch 10/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1748 - acc  
uracy: 0.9138  
Epoch 11/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1741 - acc  
uracy: 0.9136  
Epoch 12/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1746 - acc  
uracy: 0.9135  
Epoch 13/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1744 - acc  
uracy: 0.9137  
Epoch 14/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1743 - acc  
uracy: 0.9139  
Epoch 15/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1735 - acc  
uracy: 0.9144  
Epoch 16/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1737 - acc  
uracy: 0.9139  
Epoch 17/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1738 - acc  
uracy: 0.9141  
Epoch 18/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1735 - acc  
uracy: 0.9142  
Epoch 19/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1730 - acc  
uracy: 0.9145  
Epoch 20/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1730 - acc  
uracy: 0.9145  
Epoch 21/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1730 - acc  
uracy: 0.9142  
Epoch 22/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1730 - acc  
uracy: 0.9142  
Epoch 23/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1734 - acc  
uracy: 0.9141  
Epoch 24/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1724 - acc  
uracy: 0.9146  
Epoch 25/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1723 - acc  
uracy: 0.9147  
Epoch 26/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1719 - acc  
uracy: 0.9149  
Epoch 27/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1722 - acc  
uracy: 0.9148  
Epoch 28/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1725 - acc  
uracy: 0.9145

Epoch 29/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1718 - accuracy: 0.9148  
Epoch 30/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1719 - accuracy: 0.9148  
Epoch 31/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1722 - accuracy: 0.9148  
Epoch 32/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1722 - accuracy: 0.9148  
Epoch 33/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1719 - accuracy: 0.9149  
Epoch 34/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1715 - accuracy: 0.9150  
Epoch 35/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1720 - accuracy: 0.9146  
2388/2388 [=====] - 1s 345us/step - loss: 0.2124 - accuracy: 0.9143  
Epoch 1/35  
138/138 [=====] - 3s 15ms/step - loss: 0.2960 - accuracy: 0.8589  
Epoch 2/35  
138/138 [=====] - 2s 17ms/step - loss: 0.2177 - accuracy: 0.8882  
Epoch 3/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1930 - accuracy: 0.9062  
Epoch 4/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1847 - accuracy: 0.9106  
Epoch 5/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1818 - accuracy: 0.9122  
Epoch 6/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1788 - accuracy: 0.9132  
Epoch 7/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1772 - accuracy: 0.9133  
Epoch 8/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1765 - accuracy: 0.9134  
Epoch 9/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1758 - accuracy: 0.9136  
Epoch 10/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1753 - accuracy: 0.9137  
Epoch 11/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1745 - accuracy: 0.9140  
Epoch 12/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1746 - accuracy: 0.9138  
Epoch 13/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1743 - accuracy: 0.9139  
Epoch 14/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1737 - accuracy: 0.9140

```
uracy: 0.9141
Epoch 15/35
138/138 [=====] - 2s 17ms/step - loss: 0.1734 - acc
uracy: 0.9142
Epoch 16/35
138/138 [=====] - 2s 16ms/step - loss: 0.1731 - acc
uracy: 0.9142
Epoch 17/35
138/138 [=====] - 2s 16ms/step - loss: 0.1728 - acc
uracy: 0.9143
Epoch 18/35
138/138 [=====] - 2s 17ms/step - loss: 0.1734 - acc
uracy: 0.9138
Epoch 19/35
138/138 [=====] - 2s 17ms/step - loss: 0.1730 - acc
uracy: 0.9144
Epoch 20/35
138/138 [=====] - 2s 17ms/step - loss: 0.1728 - acc
uracy: 0.9142
Epoch 21/35
138/138 [=====] - 2s 17ms/step - loss: 0.1729 - acc
uracy: 0.9143
Epoch 22/35
138/138 [=====] - 2s 17ms/step - loss: 0.1733 - acc
uracy: 0.9144
Epoch 23/35
138/138 [=====] - 2s 17ms/step - loss: 0.1728 - acc
uracy: 0.9143
Epoch 24/35
138/138 [=====] - 2s 16ms/step - loss: 0.1725 - acc
uracy: 0.9147
Epoch 25/35
138/138 [=====] - 2s 17ms/step - loss: 0.1729 - acc
uracy: 0.9144
Epoch 26/35
138/138 [=====] - 2s 16ms/step - loss: 0.1734 - acc
uracy: 0.9141
Epoch 27/35
138/138 [=====] - 2s 17ms/step - loss: 0.1730 - acc
uracy: 0.9143
Epoch 28/35
138/138 [=====] - 2s 17ms/step - loss: 0.1730 - acc
uracy: 0.9143
Epoch 29/35
138/138 [=====] - 2s 17ms/step - loss: 0.1724 - acc
uracy: 0.9146
Epoch 30/35
138/138 [=====] - 2s 16ms/step - loss: 0.1731 - acc
uracy: 0.9143
Epoch 31/35
138/138 [=====] - 2s 16ms/step - loss: 0.1731 - acc
uracy: 0.9143
Epoch 32/35
138/138 [=====] - 2s 17ms/step - loss: 0.1725 - acc
uracy: 0.9147
Epoch 33/35
138/138 [=====] - 2s 16ms/step - loss: 0.1727 - acc
uracy: 0.9147
Epoch 34/35
138/138 [=====] - 2s 17ms/step - loss: 0.1729 - acc
uracy: 0.9146
Epoch 35/35
138/138 [=====] - 2s 17ms/step - loss: 0.1725 - acc
uracy: 0.9145
```

2388/2388 [=====] - 1s 386us/step - loss: 0.2166 - accuracy: 0.9150  
Epoch 1/35  
138/138 [=====] - 3s 16ms/step - loss: 0.2887 - accuracy: 0.8614  
Epoch 2/35  
138/138 [=====] - 2s 17ms/step - loss: 0.2063 - accuracy: 0.8970  
Epoch 3/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1893 - accuracy: 0.9084  
Epoch 4/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1862 - accuracy: 0.9098  
Epoch 5/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1814 - accuracy: 0.9122  
Epoch 6/35  
138/138 [=====] - 3s 18ms/step - loss: 0.1791 - accuracy: 0.9125  
Epoch 7/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1778 - accuracy: 0.9129  
Epoch 8/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1765 - accuracy: 0.9131  
Epoch 9/35  
138/138 [=====] - 3s 18ms/step - loss: 0.1750 - accuracy: 0.9140  
Epoch 10/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1751 - accuracy: 0.9136  
Epoch 11/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1740 - accuracy: 0.9139  
Epoch 12/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1740 - accuracy: 0.9138  
Epoch 13/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1733 - accuracy: 0.9142  
Epoch 14/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1734 - accuracy: 0.9142  
Epoch 15/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1734 - accuracy: 0.9142  
Epoch 16/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1738 - accuracy: 0.9139  
Epoch 17/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1740 - accuracy: 0.9139  
Epoch 18/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1739 - accuracy: 0.9141  
Epoch 19/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1732 - accuracy: 0.9143  
Epoch 20/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1736 - accuracy: 0.9141  
Epoch 21/35  
138/138 [=====] - 3s 18ms/step - loss: 0.1733 - accuracy: 0.9141

uracy: 0.9141  
Epoch 22/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1740 - acc  
uracy: 0.9140  
Epoch 23/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1734 - acc  
uracy: 0.9139  
Epoch 24/35  
138/138 [=====] - 3s 18ms/step - loss: 0.1728 - acc  
uracy: 0.9144  
Epoch 25/35  
138/138 [=====] - 3s 18ms/step - loss: 0.1727 - acc  
uracy: 0.9143  
Epoch 26/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1730 - acc  
uracy: 0.9143  
Epoch 27/35  
138/138 [=====] - 3s 19ms/step - loss: 0.1732 - acc  
uracy: 0.9140  
Epoch 28/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1737 - acc  
uracy: 0.9141  
Epoch 29/35  
138/138 [=====] - 3s 20ms/step - loss: 0.1727 - acc  
uracy: 0.9144  
Epoch 30/35  
138/138 [=====] - 3s 19ms/step - loss: 0.1722 - acc  
uracy: 0.9148  
Epoch 31/35  
138/138 [=====] - 3s 18ms/step - loss: 0.1727 - acc  
uracy: 0.9145  
Epoch 32/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1724 - acc  
uracy: 0.9145  
Epoch 33/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1726 - acc  
uracy: 0.9142  
Epoch 34/35  
138/138 [=====] - 3s 18ms/step - loss: 0.1729 - acc  
uracy: 0.9143  
Epoch 35/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1727 - acc  
uracy: 0.9146  
2388/2388 [=====] - 1s 367us/step - loss: 0.2174 -  
accuracy: 0.9173  
Epoch 1/35  
138/138 [=====] - 3s 16ms/step - loss: 0.2847 - acc  
uracy: 0.8690  
Epoch 2/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1940 - acc  
uracy: 0.9071  
Epoch 3/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1883 - acc  
uracy: 0.9096  
Epoch 4/35  
138/138 [=====] - 3s 18ms/step - loss: 0.1839 - acc  
uracy: 0.9116  
Epoch 5/35  
138/138 [=====] - 3s 18ms/step - loss: 0.1820 - acc  
uracy: 0.9119  
Epoch 6/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1788 - acc  
uracy: 0.9131  
Epoch 7/35

138/138 [=====] - 2s 17ms/step - loss: 0.1773 - accuracy: 0.9135  
Epoch 8/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1767 - accuracy: 0.9135  
Epoch 9/35  
138/138 [=====] - 3s 18ms/step - loss: 0.1752 - accuracy: 0.9136  
Epoch 10/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1754 - accuracy: 0.9133  
Epoch 11/35  
138/138 [=====] - 3s 19ms/step - loss: 0.1750 - accuracy: 0.9136  
Epoch 12/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1745 - accuracy: 0.9137  
Epoch 13/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1735 - accuracy: 0.9140  
Epoch 14/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1733 - accuracy: 0.9141  
Epoch 15/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1732 - accuracy: 0.9141  
Epoch 16/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1734 - accuracy: 0.9144  
Epoch 17/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1737 - accuracy: 0.9139  
Epoch 18/35  
138/138 [=====] - 3s 19ms/step - loss: 0.1728 - accuracy: 0.9143  
Epoch 19/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1730 - accuracy: 0.9143  
Epoch 20/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1725 - accuracy: 0.9146  
Epoch 21/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1727 - accuracy: 0.9144  
Epoch 22/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1731 - accuracy: 0.9142  
Epoch 23/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1729 - accuracy: 0.9142  
Epoch 24/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1735 - accuracy: 0.9139  
Epoch 25/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1723 - accuracy: 0.9146  
Epoch 26/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1725 - accuracy: 0.9145  
Epoch 27/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1731 - accuracy: 0.9140  
Epoch 28/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1732 - accuracy: 0.9140

uracy: 0.9144  
Epoch 29/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1732 - acc  
uracy: 0.9141  
Epoch 30/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1725 - acc  
uracy: 0.9145  
Epoch 31/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1728 - acc  
uracy: 0.9144  
Epoch 32/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1726 - acc  
uracy: 0.9145  
Epoch 33/35  
138/138 [=====] - 3s 19ms/step - loss: 0.1725 - acc  
uracy: 0.9146  
Epoch 34/35  
138/138 [=====] - 3s 19ms/step - loss: 0.1720 - acc  
uracy: 0.9147  
Epoch 35/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1725 - acc  
uracy: 0.9144  
2388/2388 [=====] - 1s 359us/step - loss: 0.2197 -  
accuracy: 0.9160  
Epoch 1/35  
138/138 [=====] - 3s 16ms/step - loss: 0.2842 - acc  
uracy: 0.8671  
Epoch 2/35  
138/138 [=====] - 3s 20ms/step - loss: 0.1951 - acc  
uracy: 0.9068  
Epoch 3/35  
138/138 [=====] - 3s 18ms/step - loss: 0.1879 - acc  
uracy: 0.9099  
Epoch 4/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1835 - acc  
uracy: 0.9117  
Epoch 5/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1806 - acc  
uracy: 0.9124  
Epoch 6/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1783 - acc  
uracy: 0.9131  
Epoch 7/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1772 - acc  
uracy: 0.9131  
Epoch 8/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1763 - acc  
uracy: 0.9133  
Epoch 9/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1753 - acc  
uracy: 0.9136  
Epoch 10/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1757 - acc  
uracy: 0.9134  
Epoch 11/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1748 - acc  
uracy: 0.9139  
Epoch 12/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1733 - acc  
uracy: 0.9142  
Epoch 13/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1733 - acc  
uracy: 0.9144  
Epoch 14/35



138/138 [=====] - 2s 17ms/step - loss: 0.1727 - accuracy: 0.9144  
Epoch 15/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1729 - accuracy: 0.9144  
Epoch 16/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1731 - accuracy: 0.9142  
Epoch 17/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1726 - accuracy: 0.9144  
Epoch 18/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1730 - accuracy: 0.9143  
Epoch 19/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1730 - accuracy: 0.9143  
Epoch 20/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1729 - accuracy: 0.9143  
Epoch 21/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1730 - accuracy: 0.9144  
Epoch 22/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1739 - accuracy: 0.9139  
Epoch 23/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1731 - accuracy: 0.9144  
Epoch 24/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1730 - accuracy: 0.9143  
Epoch 25/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1730 - accuracy: 0.9146  
Epoch 26/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1731 - accuracy: 0.9142  
Epoch 27/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1732 - accuracy: 0.9140  
Epoch 28/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1726 - accuracy: 0.9144  
Epoch 29/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1728 - accuracy: 0.9143  
Epoch 30/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1736 - accuracy: 0.9138  
Epoch 31/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1727 - accuracy: 0.9145  
Epoch 32/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1730 - accuracy: 0.9142  
Epoch 33/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1730 - accuracy: 0.9144  
Epoch 34/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1731 - accuracy: 0.9146  
Epoch 35/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1725 - accuracy: 0.9144

uracy: 0.9148  
2388/2388 [=====] - 1s 356us/step - loss: 0.2212 -  
accuracy: 0.9151  
Epoch 1/35  
138/138 [=====] - 3s 16ms/step - loss: 0.2895 - acc  
uracy: 0.8625  
Epoch 2/35  
138/138 [=====] - 2s 17ms/step - loss: 0.2008 - acc  
uracy: 0.9020  
Epoch 3/35  
138/138 [=====] - 2s 16ms/step - loss: 0.1880 - acc  
uracy: 0.9101  
Epoch 4/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1833 - acc  
uracy: 0.9119  
Epoch 5/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1809 - acc  
uracy: 0.9124  
Epoch 6/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1790 - acc  
uracy: 0.9129  
Epoch 7/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1772 - acc  
uracy: 0.9130  
Epoch 8/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1759 - acc  
uracy: 0.9136  
Epoch 9/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1763 - acc  
uracy: 0.9130  
Epoch 10/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1750 - acc  
uracy: 0.9137  
Epoch 11/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1742 - acc  
uracy: 0.9137  
Epoch 12/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1756 - acc  
uracy: 0.9130  
Epoch 13/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1745 - acc  
uracy: 0.9138  
Epoch 14/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1740 - acc  
uracy: 0.9140  
Epoch 15/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1737 - acc  
uracy: 0.9140  
Epoch 16/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1731 - acc  
uracy: 0.9142  
Epoch 17/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1740 - acc  
uracy: 0.9140  
Epoch 18/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1735 - acc  
uracy: 0.9145  
Epoch 19/35  
138/138 [=====] - 2s 17ms/step - loss: 0.1737 - acc  
uracy: 0.9139  
Epoch 20/35  
138/138 [=====] - 2s 18ms/step - loss: 0.1729 - acc  
uracy: 0.9148  
Epoch 21/35

```

138/138 [=====] - 2s 17ms/step - loss: 0.1740 - acc
uracy: 0.9138
Epoch 22/35
138/138 [=====] - 2s 17ms/step - loss: 0.1730 - acc
uracy: 0.9144
Epoch 23/35
138/138 [=====] - 2s 17ms/step - loss: 0.1728 - acc
uracy: 0.9143
Epoch 24/35
138/138 [=====] - 2s 17ms/step - loss: 0.1731 - acc
uracy: 0.9140
Epoch 25/35
138/138 [=====] - 2s 17ms/step - loss: 0.1736 - acc
uracy: 0.9140
Epoch 26/35
138/138 [=====] - 2s 17ms/step - loss: 0.1733 - acc
uracy: 0.9144
Epoch 27/35
138/138 [=====] - 2s 17ms/step - loss: 0.1729 - acc
uracy: 0.9142
Epoch 28/35
138/138 [=====] - 2s 17ms/step - loss: 0.1731 - acc
uracy: 0.9143
Epoch 29/35
138/138 [=====] - 2s 17ms/step - loss: 0.1721 - acc
uracy: 0.9150
Epoch 30/35
138/138 [=====] - 2s 17ms/step - loss: 0.1729 - acc
uracy: 0.9142
Epoch 31/35
138/138 [=====] - 2s 17ms/step - loss: 0.1731 - acc
uracy: 0.9144
Epoch 32/35
138/138 [=====] - 2s 17ms/step - loss: 0.1726 - acc
uracy: 0.9149
Epoch 33/35
138/138 [=====] - 2s 18ms/step - loss: 0.1735 - acc
uracy: 0.9137
Epoch 34/35
138/138 [=====] - 2s 17ms/step - loss: 0.1723 - acc
uracy: 0.9145
Epoch 35/35
138/138 [=====] - 2s 18ms/step - loss: 0.1733 - acc
uracy: 0.9142
2388/2388 [=====] - 1s 353us/step - loss: 0.2145 -
accuracy: 0.9148
Mean accuracy is 0.9153960585594177
Standard Deviation of accuracy is 0.001176243275679351

```

## Part 22: DNN regression

A similar DNN can be used for regression, instead of classification.

Question 21: How would you change the DNN used in this lab in order to use it for regression instead?

## Answer

- A21 : By use a different loss function, one that is suited for regression and replacing the activation function in the output layer with a linear function (or no activation function).

## Report

Send in this jupyter notebook, with answers to all questions.