

## Leverage II: Rebalancing

```
In [1]: # Working with data:
import numpy as np          # For scientific computing
import pandas as pd        # Working with tables.

# Downloading files:
import requests, zipfile, io # To access websites

# Specific data providers:
from tiingo import TiingoClient # Stock prices.
import quandl                  # Economic data, futures p

# API keys:
tiingo = TiingoClient({'api_key': 'XXXX'})
quandl.ApiConfig.api_key = 'YYYY'

# Plotting:
import matplotlib.pyplot as plt # Basic plot library.
plt.style.use('ggplot')         # Make plots look nice
```

Get prices:

```
In [2]: PRICE = tiingo.get_dataframe(['SPY'], '1900-01-01', metric_name='adjClose')
PRICE.index = pd.to_datetime(PRICE.index).tz_convert(None)
```

```
In [3]: RET = PRICE.pct_change()
RET[-3:]
```

```
Out[3]:
```

	SPY
2021-03-29	-0.000505
2021-03-30	-0.002653
2021-03-31	0.004053

```
In [4]: fedfunds = quandl.get(['FRED/FEDFUNDS']).rename(columns={'FRED/FEDFUNDS - Value'
fedfunds[-3:]
```

```
Out[4]:
```

	Fedfunds
2020-12-01	0.000004
2021-01-01	0.000004
2021-02-01	0.000003

Assume margin rate equals fed funds rate + 100 basis points (1%):

```
In [5]: RET = RET.join(fedfunds, how='outer')
```

```
RET['Fedfunds'] = RET.Fedfunds.ffill()
RET['MarginRate'] = RET.Fedfunds + 0.01/252
RET = RET.dropna()
RET
```

```
Out[5]:
```

	SPY	Fedfunds	MarginRate
1993-02-01	0.007112	0.000120	0.000160
1993-02-02	0.002118	0.000120	0.000160
1993-02-03	0.010572	0.000120	0.000160
1993-02-04	0.004184	0.000120	0.000160
1993-02-05	-0.000696	0.000120	0.000160
...	...	...	...
2021-03-25	0.005626	0.000003	0.000043
2021-03-26	0.016115	0.000003	0.000043
2021-03-29	-0.000505	0.000003	0.000043
2021-03-30	-0.002653	0.000003	0.000043
2021-03-31	0.004053	0.000003	0.000043

7093 rows × 3 columns

```
In [7]: weights = pd.Series({'SPY':1.5, 'MarginRate':-0.5})
weights
```

```
Out[7]: SPY      1.5
MarginRate -0.5
dtype: float64
```

Compound weighted average returns:

```
In [8]: RET.multiply(weights).sum('columns').add(1).cumprod() # rebalance every day
```

```
Out[8]: 1993-02-01    1.010589
1993-02-02    1.013718
1993-02-03    1.029712
1993-02-04    1.036092
1993-02-05    1.034929
...
2021-03-25    24.536645
2021-03-26    25.129230
2021-03-29    25.109653
2021-03-30    25.009192
2021-03-31    25.160715
Length: 7093, dtype: float64
```

Weighted average of compound returns:

```
In [9]: RET.add(1).cumprod() # $1 initial investment in each asset and never rebalance
```

```
Out[9]:
```

	SPY	Fedfunds	MarginRate
--	-----	----------	------------

	SPY	Fedfunds	MarginRate
1993-02-01	1.007112	1.000120	1.000160
1993-02-02	1.009245	1.000240	1.000320
1993-02-03	1.019915	1.000361	1.000480
1993-02-04	1.024182	1.000481	1.000640
1993-02-05	1.023470	1.000601	1.000800
...	...	...	...
2021-03-25	15.059675	2.013265	2.667213
2021-03-26	15.302362	2.013272	2.667328
2021-03-29	15.294633	2.013278	2.667442
2021-03-30	15.254056	2.013285	2.667556
2021-03-31	15.315887	2.013291	2.667670

7093 rows × 3 columns

```
In [10]: RET.add(1).cumprod().multiply(weights) # initial investments: $1.5 in SPY and $
```

	Fedfunds	MarginRate	SPY
1993-02-01	NaN	-0.500080	1.510669
1993-02-02	NaN	-0.500160	1.513867
1993-02-03	NaN	-0.500240	1.529872
1993-02-04	NaN	-0.500320	1.536273
1993-02-05	NaN	-0.500400	1.535205
...	...	...	...
2021-03-25	NaN	-1.333607	22.589513
2021-03-26	NaN	-1.333664	22.953542
2021-03-29	NaN	-1.333721	22.941949
2021-03-30	NaN	-1.333778	22.881084
2021-03-31	NaN	-1.333835	22.973831

7093 rows × 3 columns

```
In [11]: RET.add(1).cumprod().multiply(weights).sum('columns') # Total value of the portf
```

1993-02-01	1.010589
1993-02-02	1.013707
1993-02-03	1.029632
1993-02-04	1.035953
1993-02-05	1.034805
...	...
2021-03-25	21.255907

```

2021-03-26    21.619879
2021-03-29    21.608228
2021-03-30    21.547306
2021-03-31    21.639995
Length: 7093, dtype: float64

```

Compare these two strategies:

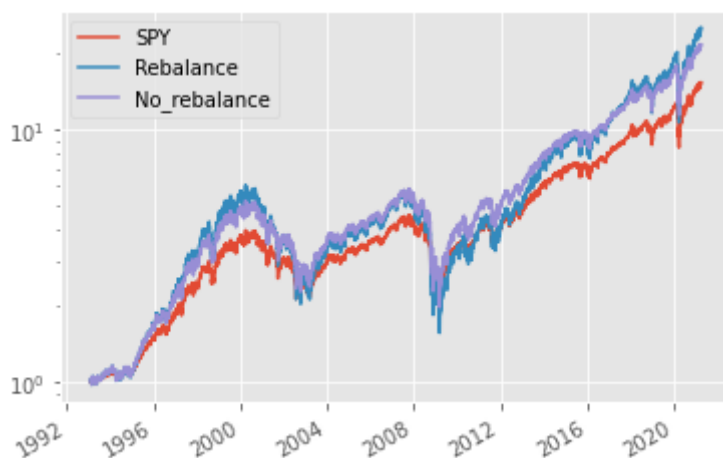
```

In [12]: t = pd.DataFrame()
t['SPY'] = RET.SPY.add(1).cumprod()
t['Rebalance'] = RET[['SPY', 'MarginRate']].multiply(weights).sum('columns').a
t['No_rebalance'] = RET[['SPY', 'MarginRate']].add(1).cumprod().multiply(weights)

t.plot(logy=True)

```

Out[12]: <AxesSubplot:>



Portfolio positions (dollars invested) if we do not rebalance:

```

In [13]: positions = RET[['SPY', 'MarginRate']].add(1).cumprod().multiply(weights)
positions

```

```

Out[13]:

```

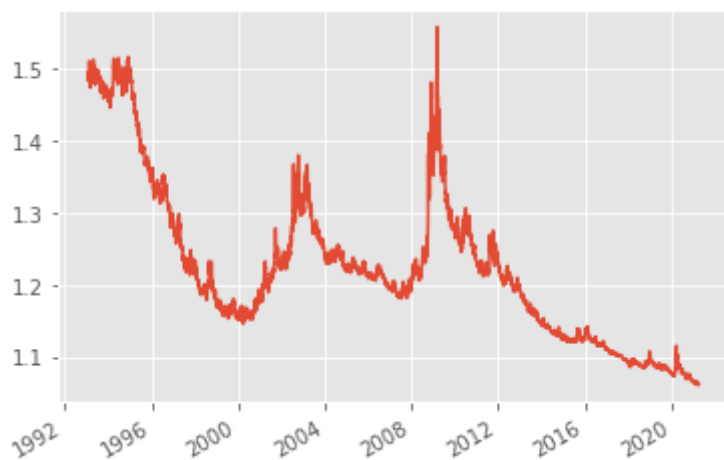
	SPY	MarginRate
1993-02-01	1.510669	-0.500080
1993-02-02	1.513867	-0.500160
1993-02-03	1.529872	-0.500240
1993-02-04	1.536273	-0.500320
1993-02-05	1.535205	-0.500400
...	...	...
2021-03-25	22.589513	-1.333607
2021-03-26	22.953542	-1.333664
2021-03-29	22.941949	-1.333721
2021-03-30	22.881084	-1.333778
2021-03-31	22.973831	-1.333835

7093 rows × 2 columns

Leverage ratio:

```
In [14]: (positions.SPY / positions.sum('columns')).plot()
```

Out[14]: <AxesSubplot:>



High water mark:

```
In [15]: hwm = t.cummax() # cummax: maximum value from 1st row to current row (date)
         hwm
```

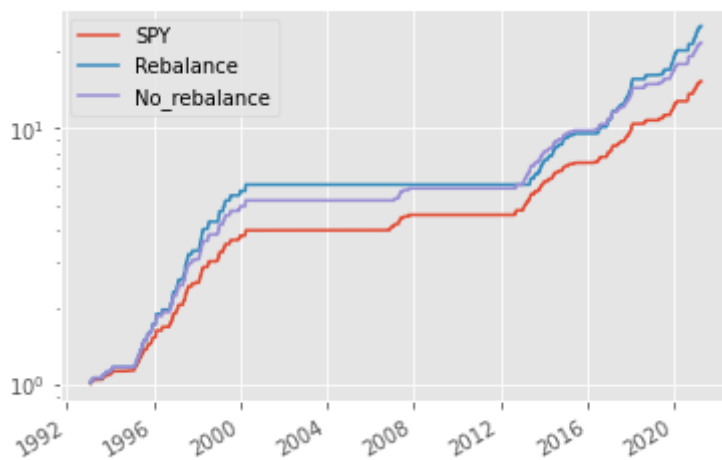
Out[15]:

	SPY	Rebalance	No_rebalance
1993-02-01	1.007112	1.010589	1.010589
1993-02-02	1.009245	1.013718	1.013707
1993-02-03	1.019915	1.029712	1.029632
1993-02-04	1.024182	1.036092	1.035953
1993-02-05	1.024182	1.036092	1.035953
...	...	...	...
2021-03-25	15.301625	25.137373	21.619174
2021-03-26	15.302362	25.137373	21.619879
2021-03-29	15.302362	25.137373	21.619879
2021-03-30	15.302362	25.137373	21.619879
2021-03-31	15.315887	25.160715	21.639995

7093 rows × 3 columns

```
In [16]: hwm.plot(logy=True)
```

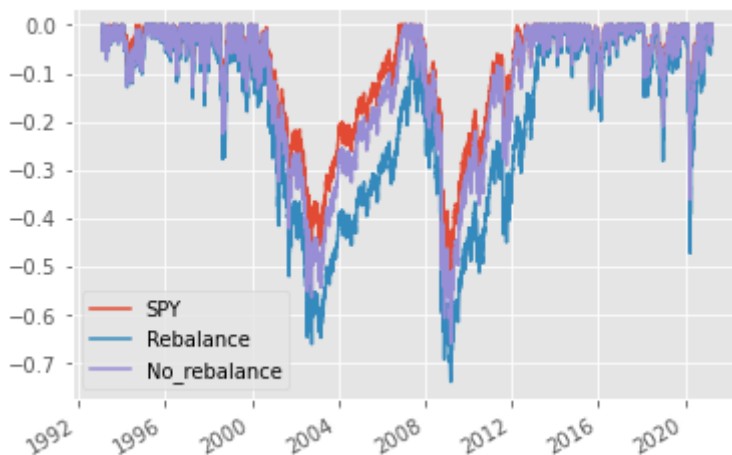
Out[16]: <AxesSubplot:>



Portfolio drawdown:

```
In [17]: drawdown = t/hwm - 1.0    # % portfolio loss relative to most recent peak (high w
drawdown.plot()
```

Out[17]: <AxesSubplot:>



With rebalance loop:

```
In [18]: def get_rebalance_dates(frequency):
    group = getattr(PRICE.index, frequency)
    return PRICE[:1].index.union(PRICE.groupby([PRICE.index.year, group]).tail(1

def run_backtest(frequency):

    weights = pd.Series({'SPY':1.5, 'MarginRate':-0.5})

    rebalance_dates = get_rebalance_dates(frequency)

    portfolio_value = pd.Series(1, index=rebalance_dates
    leverage = pd.Series(weights.SPY, index=rebalance_dates
    trades = pd.DataFrame(columns=weights.index, index=rebalance_dates
    previous_positions = weights

    for i in range(len(rebalance_dates)-1):
        start_date = rebalance_dates[i]
```

```

end_date = rebalance_dates[i+1]

cum_ret = RET[start_date:end_date][1:].add(1).cumprod()

new_positions = portfolio_value.iloc[-1] * weights

start_to_end_positions = new_positions * cum_ret

portfolio_value = portfolio_value.append(start_to_end_positions.sum('col'))
leverage = leverage.append(start_to_end_positions.SPY / start_to_end_pos

trades.loc[start_date] = new_positions - previous_positions
previous_positions = start_to_end_positions.iloc[-1] # Previous

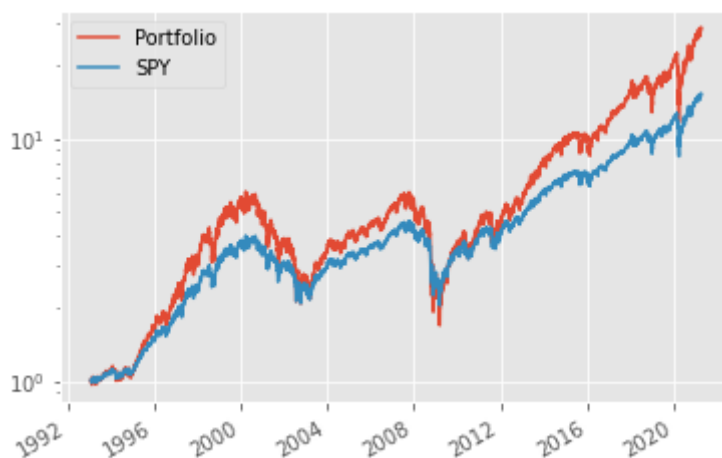
return portfolio_value, leverage, trades

portfolio_value, leverage, trades = run_backtest('month')

portfolio_value.to_frame('Portfolio').join(RET.SPY.add(1).cumprod()).plot(logy=True)

```

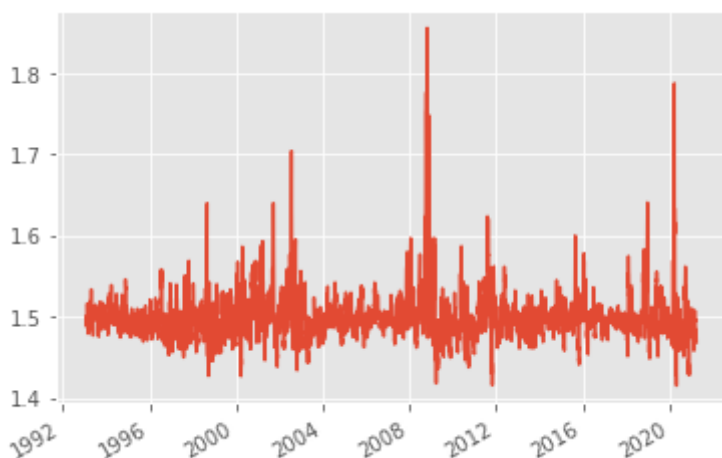
Out[18]: <AxesSubplot:>



Leverage:

In [19]: `leverage.plot()` # Leverage if we rebalance once per month to target weights 150

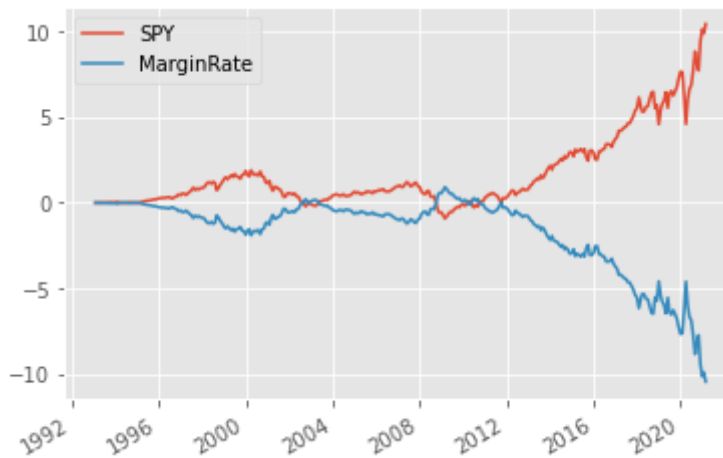
Out[19]: <AxesSubplot:>



Cumulative trades:

```
In [20]: trades.cumsum().plot()      # Total dollars moved between cash and stocks
```

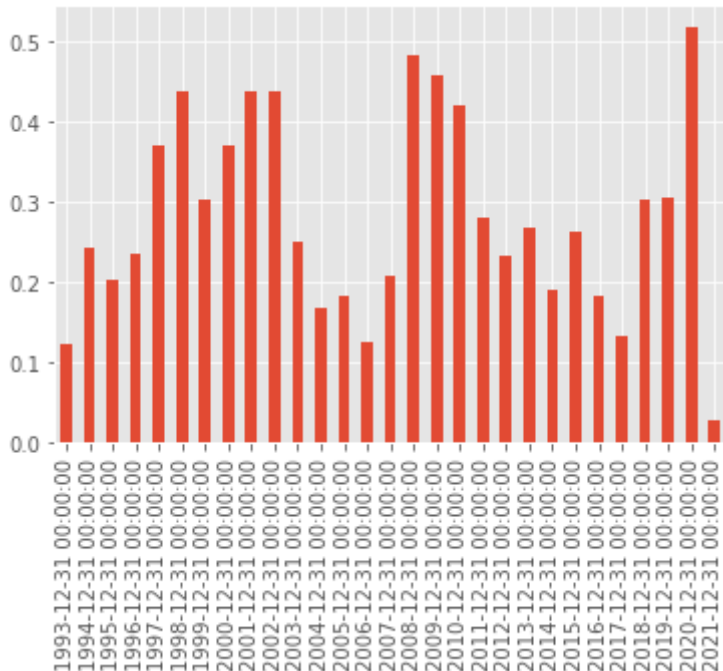
Out[20]: <AxesSubplot:>



Annual turnover ratio:

```
In [21]: turnover = trades.abs().sum('columns').div(2)
turnover.resample('A').sum().div( portfolio_value.resample('A').mean() ).plot.ba
```

Out[21]: <AxesSubplot:>



Rebalance only when leverage too far away from target weights:

- leverage > 1.7: rebalance back to 1.5
- leverage < 1.3: rebalance back to 1.5
- else: do nothing

In [23]:



```

def run_backtest(frequency):

    weights = pd.Series({'SPY':1.5, 'MarginRate':-0.5})

    rebalance_dates = get_rebalance_dates(frequency) # PRICE.index

    portfolio_value = pd.Series(1, index=[rebalance_dates
    leverage         = pd.Series(weights.SPY, index=[rebalance_dates
    trades           = pd.DataFrame(columns=weights.index, index=[rebalance_dates
    previous_positions = weights

    for i in range(len(rebalance_dates)-1):
        start_date = rebalance_dates[i]
        end_date   = rebalance_dates[i+1]

        cum_ret = RET[start_date:end_date][1:].add(1).cumprod()

        if((leverage[-1]<weights.SPY-0.2) | (leverage[-1]>weights.SPY+0.2)):
            new_positions = portfolio_value.iloc[-1] * weights
        else:
            new_positions = previous_positions

        start_to_end_positions = new_positions * cum_ret

        portfolio_value = portfolio_value.append(start_to_end_positions.sum('col
        leverage = leverage.append(start_to_end_positions.SPY / start_to_end_pos

        trades.loc[start_date] = new_positions - previous_positions
        previous_positions      = start_to_end_positions.iloc[-1] # Previous

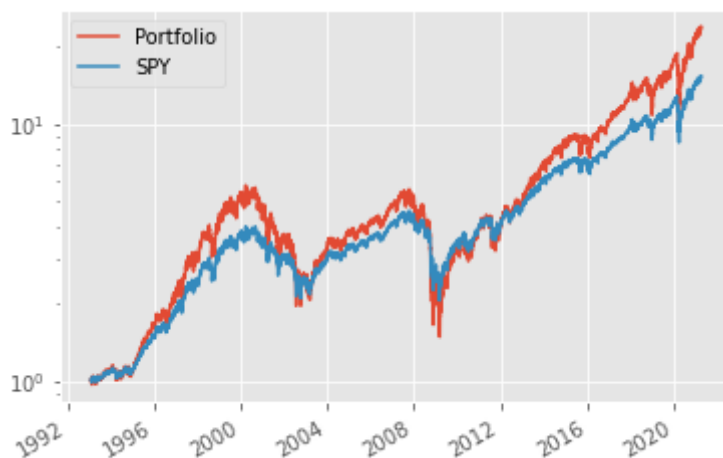
    return portfolio_value, leverage, trades

portfolio_value, leverage, trades = run_backtest('month')

portfolio_value.to_frame('Portfolio').join(RET.SPY.add(1).cumprod()).plot(logy=True

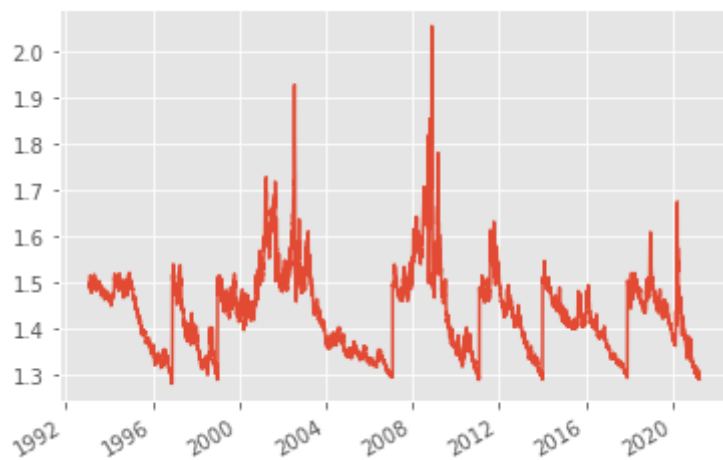
```

Out[23]: <AxesSubplot:>



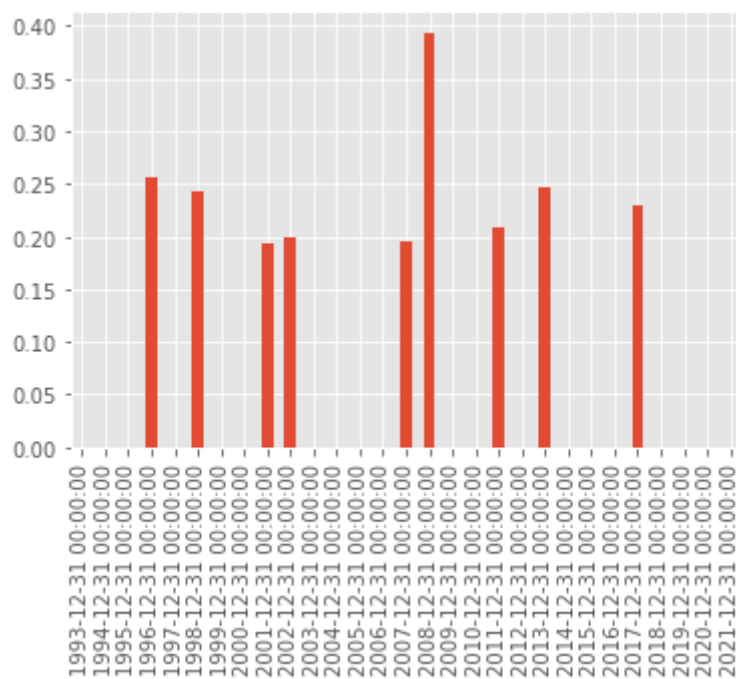
In [24]: leverage.plot()

Out[24]: <AxesSubplot:>



```
In [25]: turnover = trades.abs().sum('columns').div(2)
turnover.resample('A').sum().div( portfolio_value.resample('A').mean() ).plot.ba
```

Out[25]: <AxesSubplot:>



In [ ]:

In [ ]: