

Lecture 1a

Visualization: History and Examples

Data visualization · 1-DAV-105

Lecture by Broňa Brejová

René Descartes, La Géométrie, 1637

Introduced Cartesian coordinate system,
similar ideas also Nicole Oresme (14th
century)

L A
G E O M E T R I E.
L I V R E P R E M I E R.

*Des problemes qu'on peut construire sans
y employer que des cercles & des
lignes droites.*

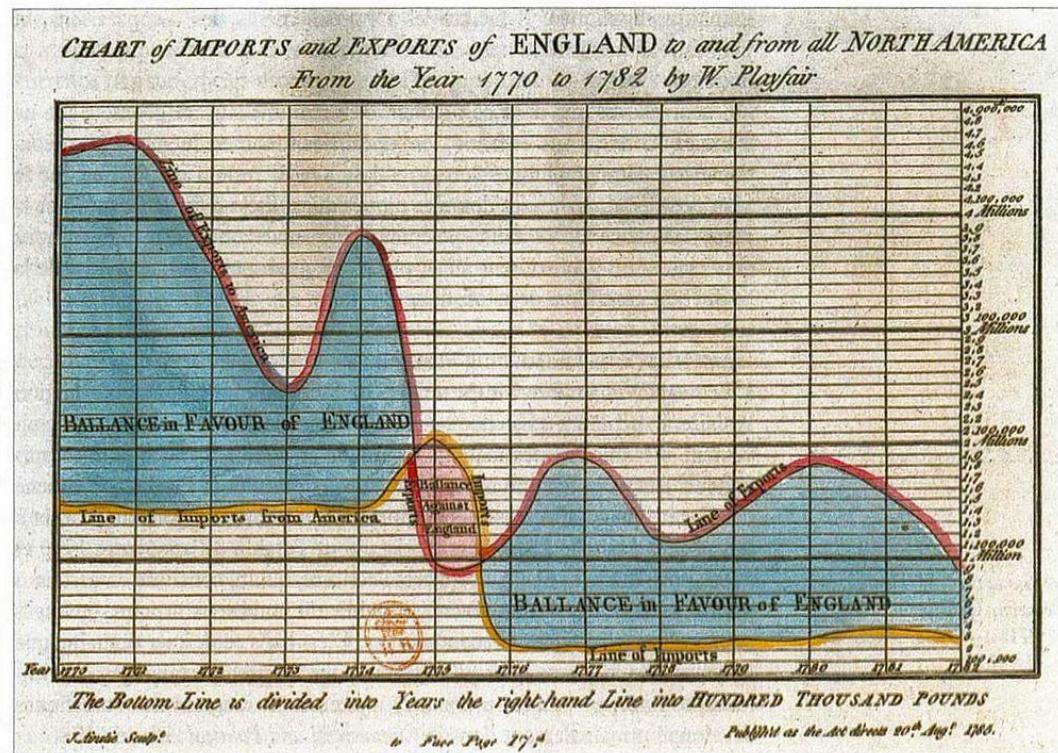


O u s les Problemes de Geometrie se
peuvent facilement reduire a tels termes,
qu'il n'est besoin par apres que de connoi-
tre la longeur de quelques lignes droites,
pour les construire.

Et comme toute l'Arithmetique n'est composée, que
de quatre ou cinq operations, qui sont l'Addition, la
Soustraction, la Multiplication, la Division, & l'Extraction
des racines, qu'on peut prendre pour une espece
de Division : Ainsi n'at'on autre chose a faire en Geome-
trie touchant les lignes qu'on cherche, pour les pre-
parer a estre connues, que leur en adiouster d'autres, ou
en oster, Oubien en ayant une, que je nommeray l'vnité
pour la rapporter d'autant mieux aux nombres, & qui
peut ordinairement estre prise a discretion, puis en ayant
encore deux autres, en trouver une quatriesme, qui soit
a l'une de ces deux, comme l'autre est a l'vnité, ce qui est
le mesme que la Multiplication, oubien en trouver une
quatriesme, qui soit a l'une de ces deux, comme l'vnité

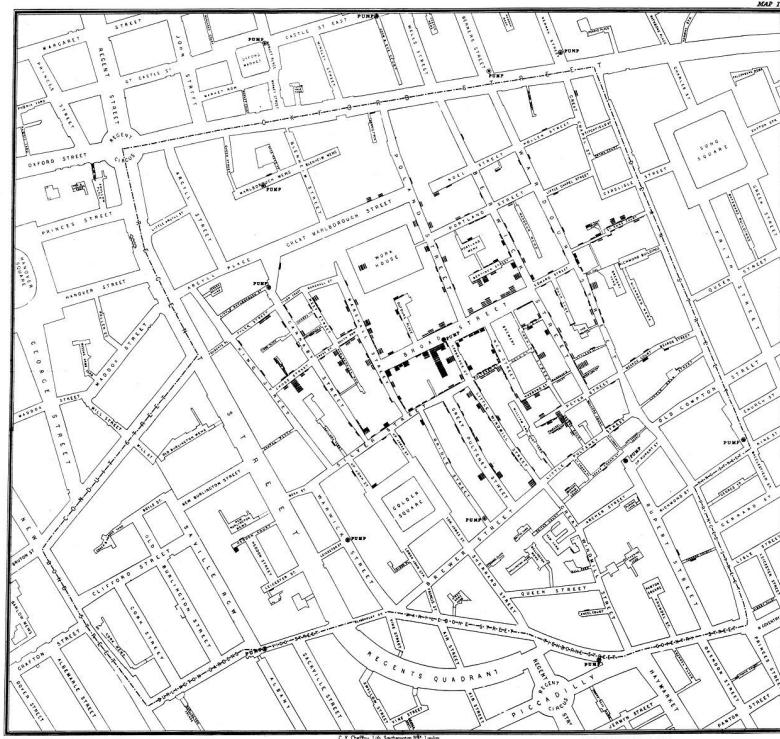
William Playfair, Commercial and Political Atlas, 1786

Playfair invented or popularized different types of graphs (line and area graphs, bar graphs, pie charts)



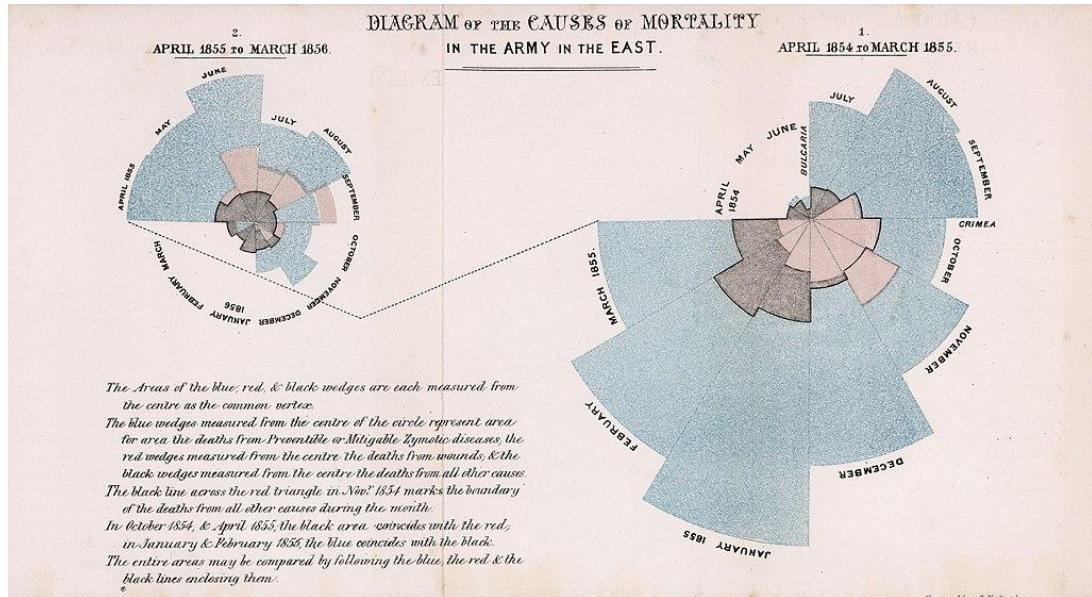
John Snow, On the Mode of Communication of Cholera, 1854

Snow tracked cholera cases in 1854 outbreak and displayed them clustered around a single London well

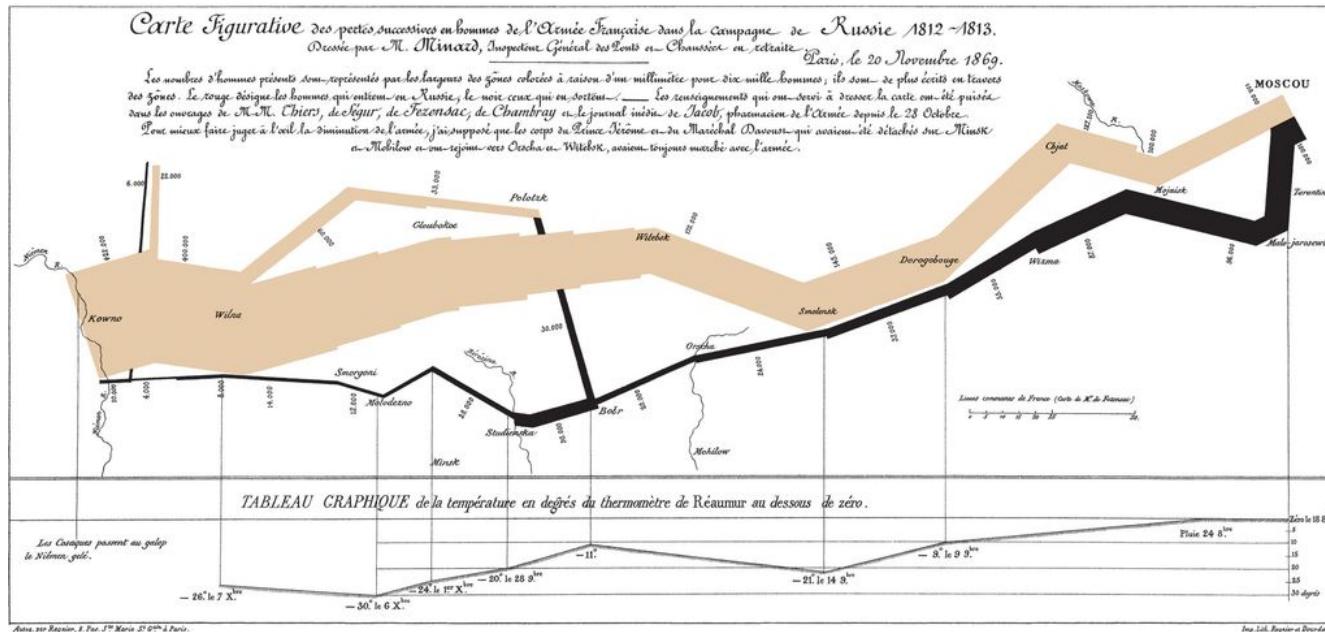


Florence Nightingale, Diagram of the causes of mortality in the army in the East, 1858

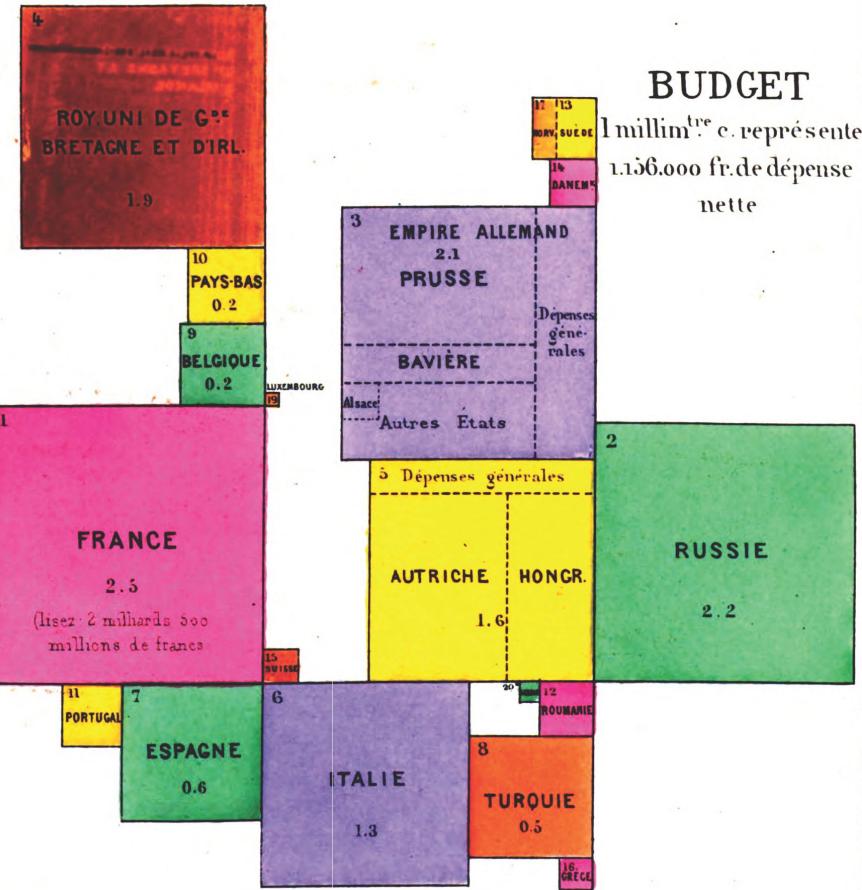
Nightingale led a field hospital during Crimean War, reported to the government on poor conditions causing deaths from typhus, cholera etc



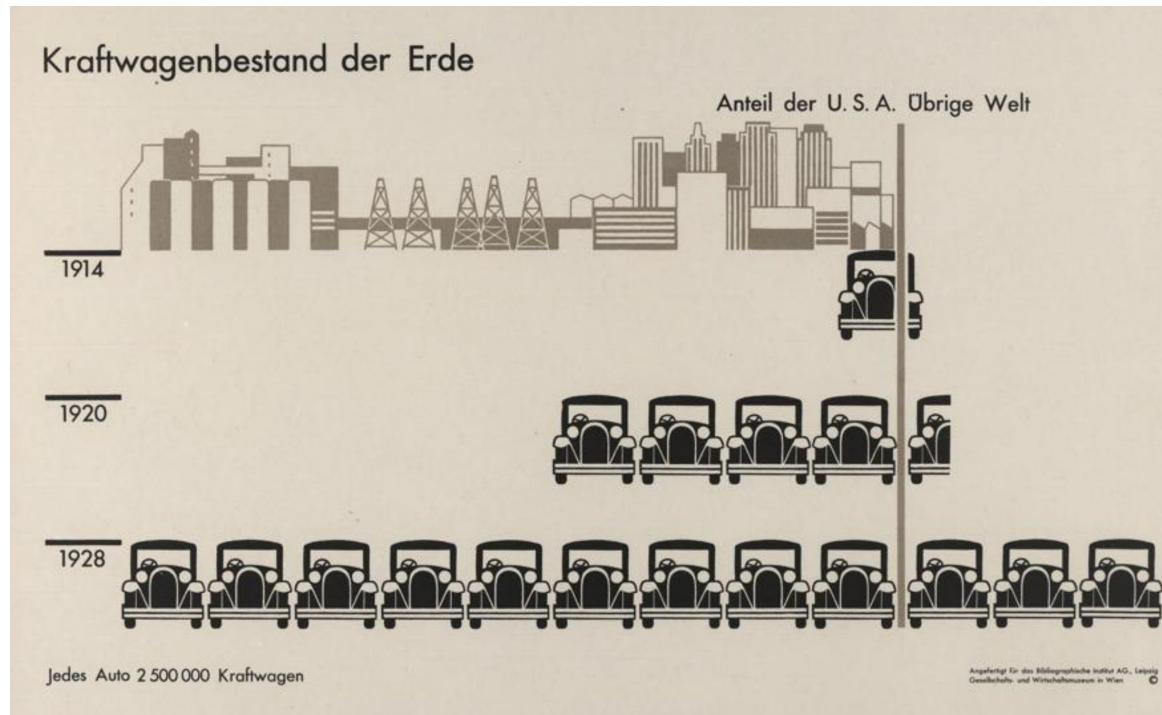
Charles Minard, Figurative Map of the successive losses in men of the French Army in the Russian campaign 1812–1813, 1869



Pierre Émile Levasseur, 1876

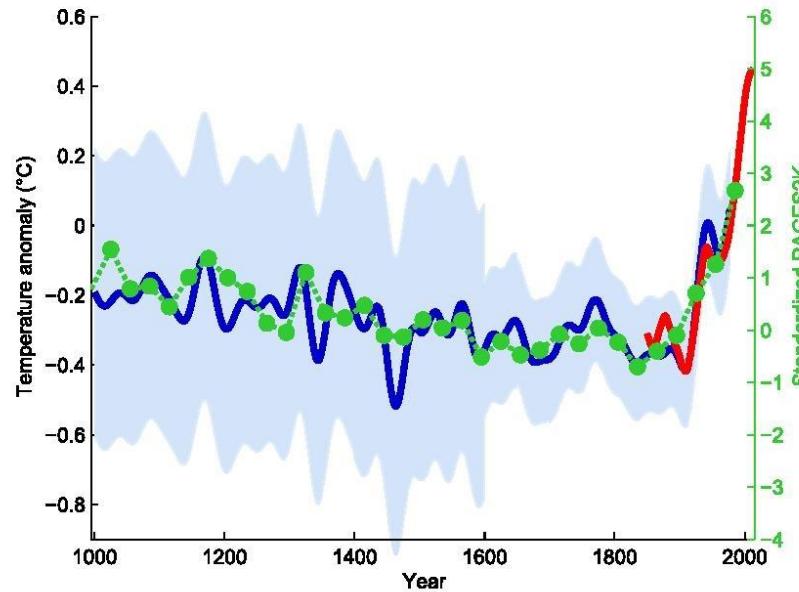


Otto Neurath, Gesellschaft und Wirtschaft, 1930

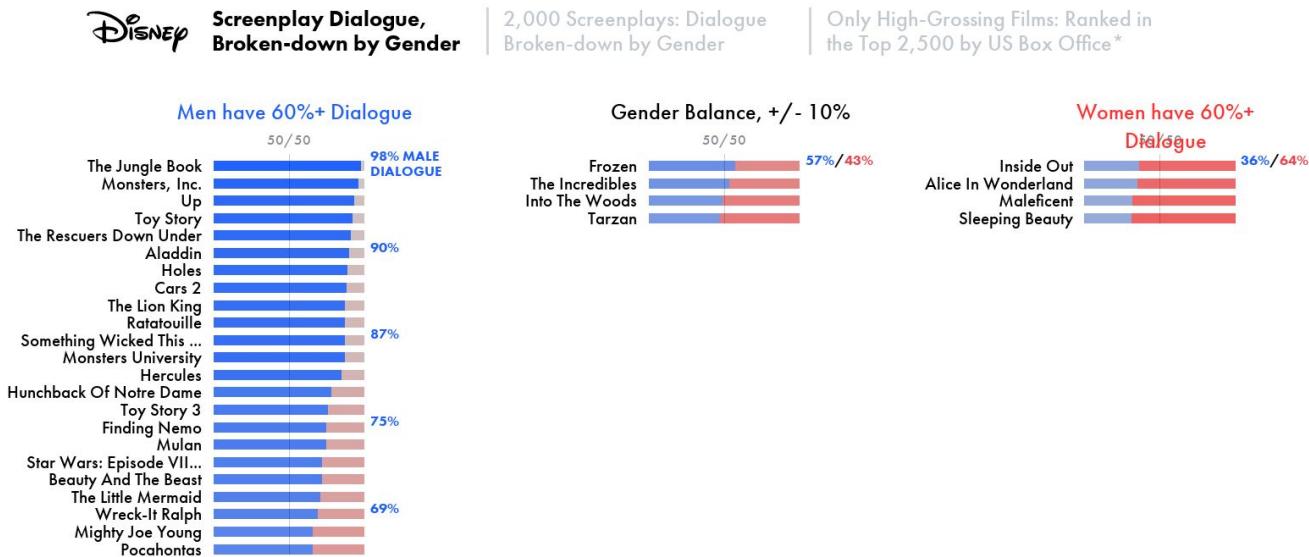


Mann, Bradley & Hughes: Northern hemisphere temperatures during the past millennium [...] 1999

Hockey stick graph, created publicity and controversy, featured also in 2001 Intergovernmental Panel on Climate Change Third Assessment Report

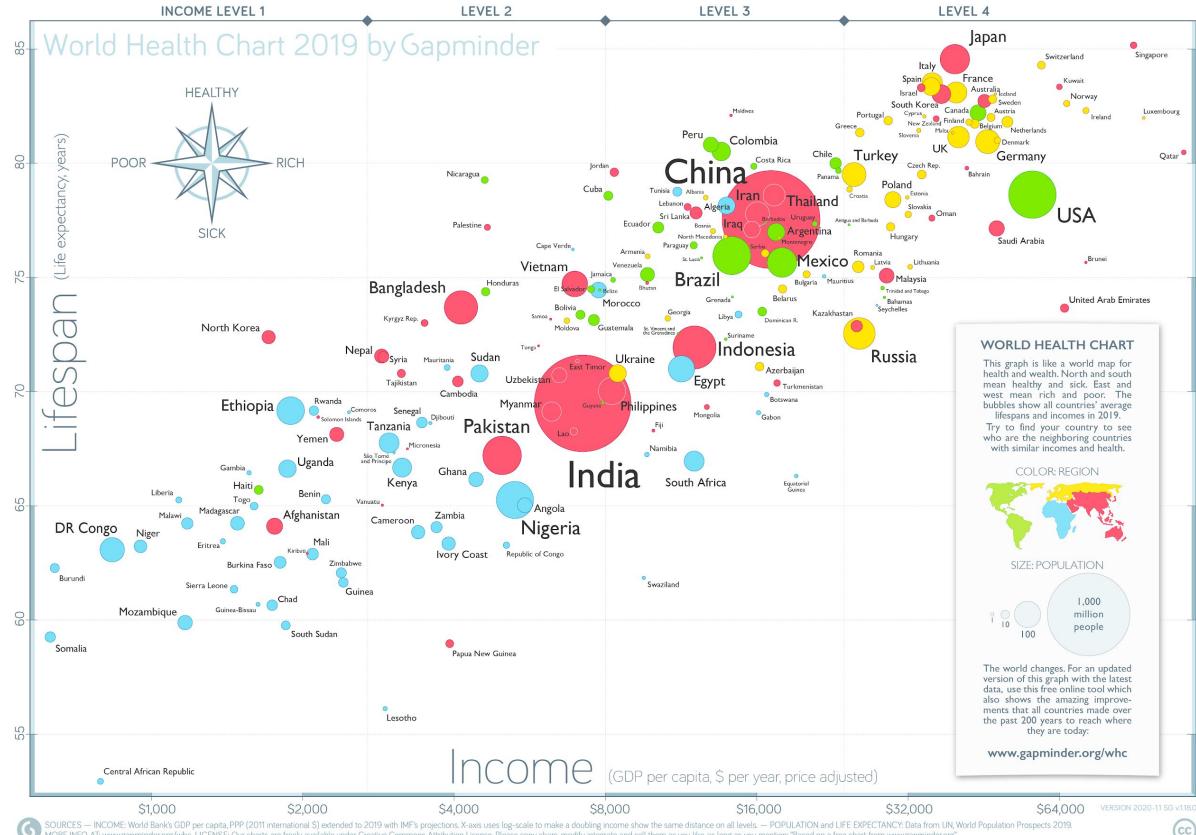


Anderson & Daniels: Film Dialog from 2,000 Screenplays, Broken Down by Gender and Age, 2016



Gapminder foundation, World Health Chart 2019, 2020

Original version by Hans Rosling in his 2006 TED talk



Two other recent examples

Comparing size of software

<https://www.informationisbeautiful.net/visualizations/million-lines-of-code/>

Deadly pandemics in history

<https://www.visualcapitalist.com/history-of-pandemics-deadliest/>

Additional resources

- Tableaux.com: Data is beautiful: 10 of the best data visualization examples from history to today
<https://www.tableau.com/learn/articles/best-beautiful-data-visualization-examples>
- Michael Friendly: History of Data Visualization
<https://friendly.github.io/HistDataVis/>
- Hans Rosling The best stats you've ever seen (TED Talk)
https://www.ted.com/talks/hans_rosling_the_best_stats_you_ve_ever_seen

1 Lecture 1b: Introduction to Jupyter Notebooks, Google Colab and Matplotlib

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Lecture by Broňa Brejová

1.1 Jupyter Notebook

- [Jupyter](#) Notebook is a web-based software for interactive work in Python.
- It is frequently used for data processing and visualization.
- A document called **notebook** consists of **cells**.
- Each cell contains either text or Python code.
- The text may include formatting in [Markdown](#) language.
- A cell with Python code can be executed and the results display below, including images.
- This presentation is a Jupyter notebook.
- Notebook files have extension `.ipynb`.

1.2 Google Colab and alternatives

- You can work with Jupyter notebooks on many platforms (both online and installed on your computer).
- In this course, we will primarily use [Google Colab](#).
- Colab stores your notebooks on Google drive, executes them on Google servers, you only need web browser on your computer.
- It integrates well with Google Classroom, which we use as well.
- You are free to use other options as long as the submitted notebooks can be executed in Colab.
- One popular option is [VS Code](#). It requires Jupyter software to be installed as well, see [documentation](#).

1.3 How to use Notebooks

- Notebooks have an intuitive interface with menus, toolbars, context menus (right-click) etc.
- It is useful to learn some keyboard shortcuts.

When you are not editting a cell:

- use Up and Down arrows to move between cells
- use **Enter** (or double-click) to start editing a cell
- use **Esc** to stop editing a cell
- use **Ctrl-Enter** to run a code in a cell, **Shift-Enter** to run the code and move to the next cell

1.3.1 An example of a code cell

- A cell can include imports, function definitions, commands.
- Variables will be visible in other cells.
- The results of print are shown below the cell when executed.
- The last expression is printed below the cell when executed.

```
[1]: # create variable x with list of numbers 0,1,...,19
x = list(range(20))
# variable y will contain squares of values in x
y = [xval * xval for xval in x]
# print x and y
print(x)
print(y)
# the last value (the first 5 values in y) is also printed automatically
y[0:5]
```

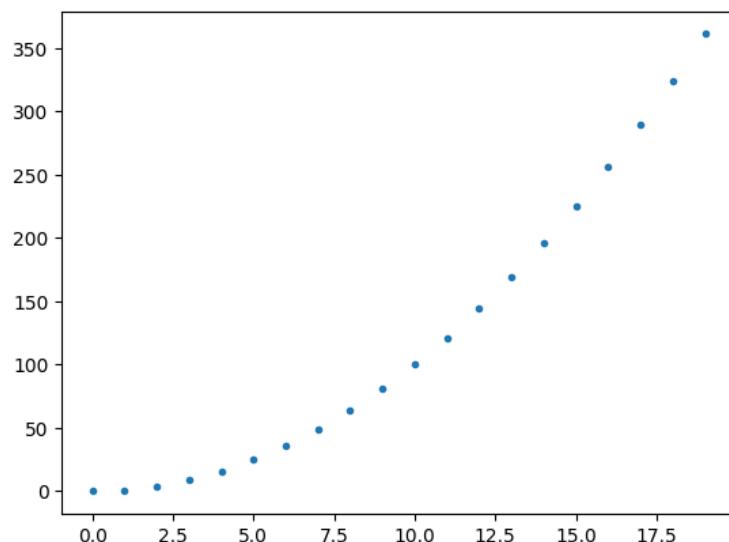
```
[0, 1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13, 14, 15, 16, 17, 18, 19]
[0, 1, 4, 9, 16, 25, 36, 49, 64, 81, 100, 121, 144, 169, 196, 225, 256, 289,
324, 361]
```

```
[1]: [0, 1, 4, 9, 16]
```

1.3.2 Example of a cell with a plot

The plot uses variables x and y from the previous cell to plot the quadratic function.

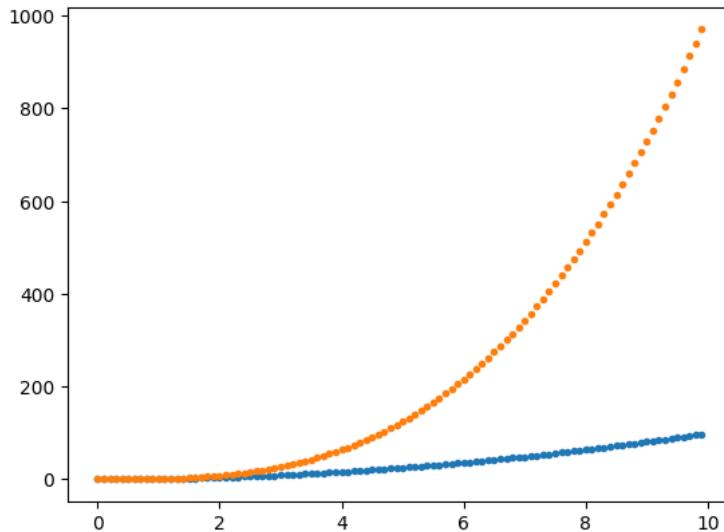
```
[2]: import matplotlib.pyplot as plt
# create figure with a single plot (axes)
figure, axes = plt.subplots()
# plot x vs y
axes.plot(x, y, '.')
# command pass to suppress unwanted output from plot
pass
```



1.4 Matplotlib library

- **Matplotlib** is a Python library for creating plots.
- In the code above, axes is the Matplotlib name for a single plot.
- Let us now plot two functions: quadratic and cubic in the same plot.

```
[3]: # x_dense is values from 0 to 10 with step 0.1
x_dense = [val / 10 for val in range(0, 100)]
# values in y2_dense are values from x_dense squared
y2_dense = [xval ** 2 for xval in x_dense]
# values in y3_dense are values from x_dense to the power of 3
y3_dense = [xval ** 3 for xval in x_dense]
# plot the quadratic and cubic function in a single plot
figure, axes = plt.subplots()
axes.plot(x_dense, y2_dense, '.')
axes.plot(x_dense, y3_dense, '.')
pass
```



1.4.1 Setting labels and titles in Matplotlib

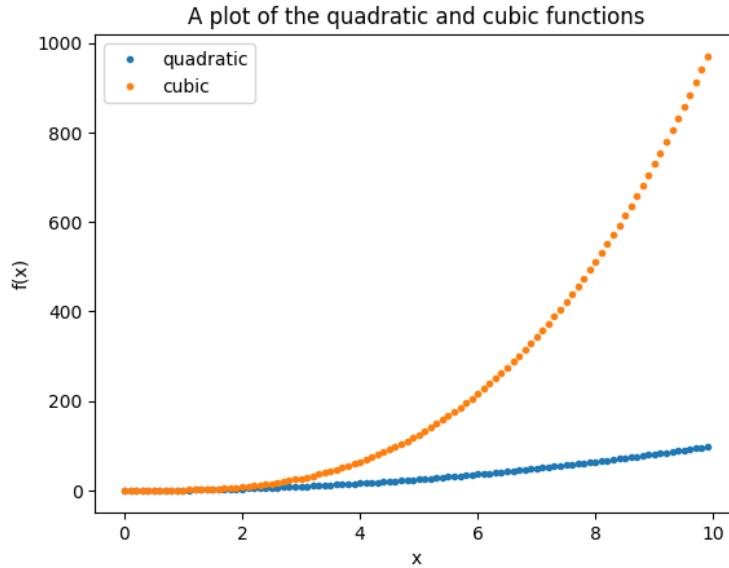
```
[4]: # the same plot as before, but name the two sets of points by label
figure, axes = plt.subplots()
axes.plot(x_dense, y2_dense, '.', label="quadratic")
axes.plot(x_dense, y3_dense, '.', label="cubic")

# add titles for axes (usually use a more descriptive titles)
axes.set_xlabel("x")
axes.set_ylabel("f(x)")
# legend (which plot is which function), uses the labels set in plt.plot
```

```

axes.legend()
# a title of the whole plot
axes.set_title("A plot of the quadratic and cubic functions")
pass

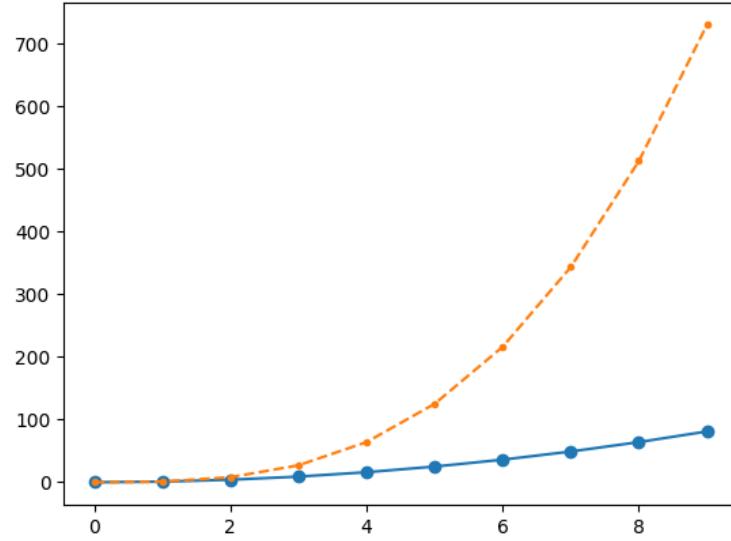
```



1.4.2 Setting lines, markers and colors

- In the `axes.plot` command, `'.'` represents formatting, in this case a small dot.
- The formatting string has three optional parts: marker, line, color.
- Examples: `'or'` red circle, `'-g'` green solid line, `'--'` dashed line.
- See more in [documentation](#).

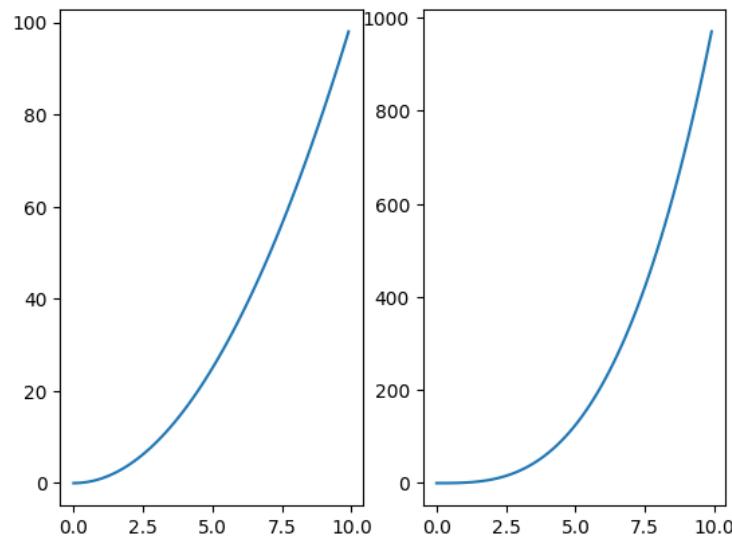
```
[5]: x_sparse = range(0, 10)
y2_sparse = [xval ** 2 for xval in x_sparse]
y3_sparse = [xval ** 3 for xval in x_sparse]
figure, axes = plt.subplots()
axes.plot(x_sparse, y2_sparse, 'o-')
axes.plot(x_sparse, y3_sparse, '.--')
pass
```



1.4.3 Multiple plots per image

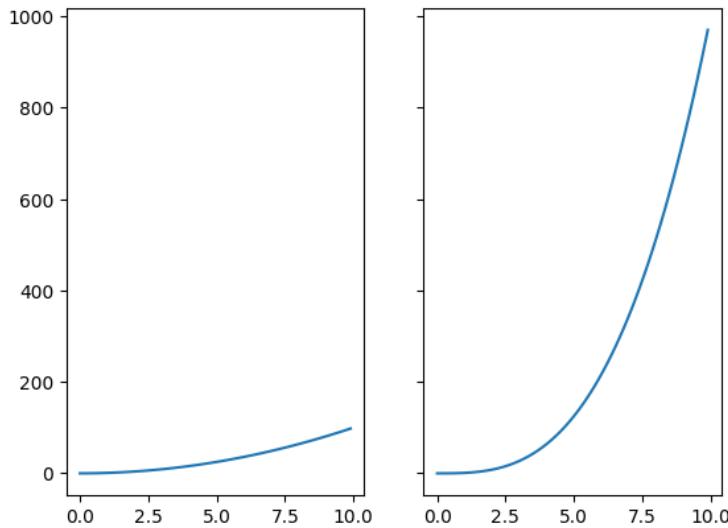
- Function `plt.subplots` can take as arguments the number of rows and the number of columns and creates multiple subplots per image.
- Why is this figure not an ideal visual comparison of the quadratic and cubic function?

```
[6]: figure, axes = plt.subplots(1, 2)
axes[0].plot(x_dense, y2_dense)
axes[1].plot(x_dense, y3_dense)
pass
```



- Each plot has a different y-axis, which is not good, because we do not immediately see that the cubic function grows much faster than the quadratic.
- We will fix this in the next plot using `sharey=True` setting (`sharex=True` also exists but here it is not needed).

```
[7]: # fixing the problem with different y-axis
figure, axes = plt.subplots(1, 2, sharey=True)
axes[0].plot(x_dense, y2_dense)
axes[1].plot(x_dense, y3_dense)
pass
```



1.5 Dangers of notebooks

- Frequent use pattern: the users have several cells finished and executed, they work on the last cell in the notebook, and run it repeatedly until it works correctly. This avoids repeated execution of the top cells, which may be slow.
- Notebooks do not force you to run cells in order from top to bottom. This generates problems if you skip some cells or execute them repeatedly.

Good practice suggestions:

- Do not modify variables introduced in other cells.
- Refactor bigger or repeated parts of code to functions. This also hides local variables from the rest of the notebook and thus prevents clashes.
- Ideally move functions to separate modules but this is harder in Colab.
- Avoid running cells out of order and occasionally restart the kernel (to remove variables) and run all cells (using a menu function).

Below we see an example not obeying the first recommendation; the value printed will depend on how many times we execute the second cell. This can lead to hard-to-find errors in a more complex case.

```
[8]: value = 0
```

```
[9]: value += 1  
      print(value)
```

1

1.6 Additional resources

- [Python Data Science Handbook](#) by Jake VanderPlas, O'Reilly 2016
- [Jupyter Notebook documentation](#)
- [Google Colab website](#) and [introductory video](#)
- [Matplotlib tutorials](#)
- [I don't like notebooks](#) by Joel Grus (entertaining video explaining some of the pitfalls of notebooks)

1 Lecture 1b: Quick Introduction to New Libraries

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Lecture by Broňa Brejová

- We will now briefly discuss several libraries which will be used in the next tutorial.
- We will cover details of these libraries in the coming weeks, this is just a glimpse of things to come.

```
[1]: # importing libraries
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import plotly.express as px
```

1.1 Libraries NumPy and Pandas

- [Pandas](#) is a Python library for working with tabular data.
- [NumPy](#) is a library of efficient multi-dimensional arrays used for numerical computations.

1.1.1 NumPy array and arithmetical operations with arrays

- Function [np.arange](#) below creates a list of numbers in interval [1, 3) with step 0.5 (generalization of Python [range](#)).
- It is stored as an object of [array](#) class from the Numpy library.

```
[2]: x = np.arange(1, 3, 0.5)
print('x:', x)
```

x: [1. 1.5 2. 2.5]

- We can do various arithmetic operations on whole NumPy arrays or apply predefined functions such as [np.exp](#).
- Such operations are typically done element-by-element.

```
[3]: print('x:', x)
print('x+1:', x+1)
print('x*x:', x*x)
print('np.exp(x):', np.exp(x))
```

x: [1. 1.5 2. 2.5]
x+1: [2. 2.5 3. 3.5]
x*x: [1. 2.25 4. 6.25]
np.exp(x): [2.71828183 4.48168907 7.3890561 12.18249396]

1.1.2 Creating Pandas DataFrame

- Below we create an object of Pandas DataFrame class.

- We will cover most Pandas functions used below next week, for now the details are not important.

```
[4]: def convert_table(x, function_dict):
    """ x is a list (or Numpy array) of values of x,
    function_dict is a dictionary containing function names as keys
    and lists of function values as values. The result will be a Pandas
    DataFrame (table) with each row containing triple x, function, value.
    Zeroes and negative values are masked as missing
    to avoid problems with logarithmic y axis."""
    # check that all functions have the same number of values as x
    for f in function_dict:
        assert(len(function_dict[f])==len(x))

    # create a wide table with each function as one columns
    functions_wide = pd.DataFrame(function_dict, index=x)
    # reformat to long format
    # where each row is a triple x, function name, function value
    functions = (functions_wide.reset_index()
                 .melt(id_vars='index')
                 .rename(columns={'variable':'function', 'index':'x'}))
    # mask values <= 0 as missing values
    val = functions['value']
    functions['value'] = val.mask(val <= 0, np.nan)
    return functions
```

```
[5]: functions = convert_table(x, {'quadratic': x * x, 'cubic': x * x * x})
```

Let us look at the resulting table `functions`:

- It has three columns named '`x`', '`function`' and '`value`'.
- Each row is a triple, containing a function name and the values of x and $f(x)$.
- E.g. one of the rows for the cubic function has $x = 2$ and $f(x) = 2^3 = 8$.

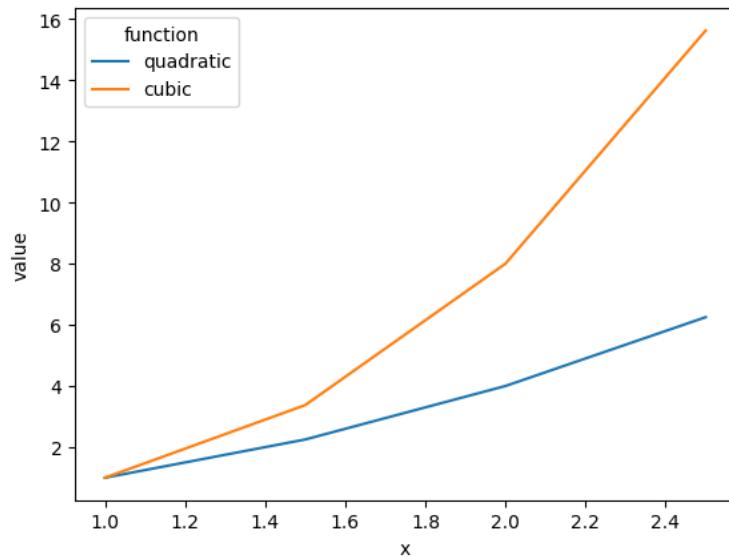
```
[6]: display(functions)
```

| | x | function | value |
|---|-----|-----------|--------|
| 0 | 1.0 | quadratic | 1.000 |
| 1 | 1.5 | quadratic | 2.250 |
| 2 | 2.0 | quadratic | 4.000 |
| 3 | 2.5 | quadratic | 6.250 |
| 4 | 1.0 | cubic | 1.000 |
| 5 | 1.5 | cubic | 3.375 |
| 6 | 2.0 | cubic | 8.000 |
| 7 | 2.5 | cubic | 15.625 |

1.2 Displaying Pandas DataFrame using Seaborn and Plotly libraries

- [Seaborn](#) library is an extension of Matplotlib.
- It is very convenient for displaying tables.
- In the `sns.lineplot` we first give the table and then specify, which columns should be used as x coordinate, y coordinate and color (`hue`).
- One line will be automatically drawn for each distinct value in the `hue` column and a legend will be added.

```
[7]: figure, axes = plt.subplots()
sns.lineplot(functions, x='x', y='value', hue='function', ax=axes)
pass
```



- Another popular library is [Plotly](#).
- It provides some additional plot types and all plots are interactive.
- For example, we can also zoom into parts of the plot by selecting a rectangle.
- A menu with additional options appears in the top right corner of the plot.
- A line plot is created similarly as in Seaborn (option `color` is used instead of `hue`).

```
[8]: figure = px.line(functions, x="x", y="value", color='function')
figure.show()
```

1.3 Interactive plots in Plotly Dash

- [Dash](#) library by Plotly allows adding control elements (selectors, sliders, buttons, ...).
- It is not preinstalled in Colab, so the next line will install it.

```
[ ]: ! pip install dash
```

- The code below creates an interactive plot in which the user can choose which functions from the list to display.
- The code has many comments so read through it carefully.

```
[10]: from dash import Dash, dcc, html, Input, Output

# create a list of all functions
all_functions = list(functions['function'].unique())

# create a new dash application app
app = Dash(__name__)

# Create layout of items in application
# one html <div> item containing text as small headers (H4),
# items for individual inputs and a graph at the bottom
# Currently we have two inputs:
# an input field for entering title text
# checkboxes for selecting functions
# These elements have identifiers which will be used later in the code
app.layout = html.Div([
    html.H4("Plot title: "),
    # input field for entering title text:
    dcc.Input(
        id='graph-title',
        type='text',
        value='My plot'
    ),
    html.H4("Select functions: "),
    # checkboxes for selecting functions:
    dcc.Checklist(
        id='selected-functions',
        options=all_functions,
        value=['quadratic'],
        inline=True # place checkboxes horizontally
    ),
    # graph itself
    dcc.Graph(id='graph-content')
])

# @app.callback is a function decorator applied to function update_figure below.
# It defines that this function will be called to update the graph when the user makes a change.
# Input will be the value entered to the input field with id graph-title and the list of functions selected in dcc.Checklist object with id 'selected-functions'.
# Output will be the graph created by the function update_figure below, which will be used
```

```

#      to update dcc.Graph object with id 'graph-content'
@app.callback(
    Output('graph-content', 'figure'),
    [Input('graph-title', 'value'),
     Input('selected-functions', 'value')])
)

def update_figure(title, selected_functions):
    """ Function for plotting functions listed in list selected_functions
    with plot title given in title"""

    # select a subset of functions table with just those functions in input list
    functions_subset = functions.query('function in @selected_functions')

    # create a plotly line plot using the smaller table in functions_subset
    figure = px.line(
        functions_subset, x="x", y="value", color="function",
        width=800, height=500
    )

    # add title to the plot
    figure.update_layout(title_text=title)

    return figure

# run the whole application
app.run_server(mode='inline')

```

<IPython.lib.display.IFrame at 0x7f8f001c8e80>

1 Lecture 2: Data processing in Pandas library

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Lecture by Broňa Brejová

1.1 Tabular data

- We will often work with data in the form of tables.
- Columns represent different features / variables (príznaky, atribúty, veličiny, premenné).
- Rows represent different items / data points / observations (countries, people, dates of measurement, ...).
- A small example:

| Country | Region | Population | Area (km2) | Landlocked |
|----------------|--------|------------|------------|------------|
| Slovakia | Europe | 5450421 | 49035 | yes |
| Czech Republic | Europe | 10649800 | 78866 | yes |
| Hungary | Europe | 9772756 | 93030 | yes |
| Poland | Europe | 38386000 | 312696 | no |

1.2 Pandas library

- [Pandas](#) is a Python library for data manipulation and analysis.
- It is fast and has many functions for data import and export in various formats.
- [Documentation, overview, tutorial](#)

Basic data structures

- **Series**: 1D table, all elements of the same type.
- **DataFrame**: 2D table, elements within each column of the same type.

NumPy library

- [NumPy](#) is a library of efficient multi-dimensional arrays used for numerical computations.
- We will mostly use Pandas, but some NumPy functions will be useful.
- [Tutorial, reference](#)

```
[93]: import numpy as np
import pandas as pd
from IPython.display import Markdown
import matplotlib.pyplot as plt
```

1.2.1 Creating Series and DataFrames

- Below we show two manual ways of creating a DataFrame containing the small table of countries above.
- The first way gets a Series for each column, the second way gets a dictionary (or a tuple) for each row.
- We will usually read tabular data from files, see an example in the second half this lecture.

```
[94]: countries = pd.Series(['Slovakia', 'Czech Republic', 'Hungary', 'Poland'])
regions = pd.Series(['Europe', 'Europe', 'Europe', 'Europe'])
populations = pd.Series([5450421, 10649800, 9772756, 38386000])
areas = pd.Series([49035, 78866, 93030, 312696])
landlocked = pd.Series([True, True, True, False])
table = pd.DataFrame({'country':countries,
                      'region':regions,
                      'population':populations,
                      'area':areas,
                      'landlocked':landlocked})
# display: special notebook command for pretty-printing data
display(table)
```

| | country | region | population | area | landlocked |
|---|----------------|--------|------------|--------|------------|
| 0 | Slovakia | Europe | 5450421 | 49035 | True |
| 1 | Czech Republic | Europe | 10649800 | 78866 | True |
| 2 | Hungary | Europe | 9772756 | 93030 | True |
| 3 | Poland | Europe | 38386000 | 312696 | False |

```
[95]: list_of_dicts = [
    {'country':'Slovakia', 'region':'Europe', 'population':5450421, 'area':
     ↪49035, 'landlocked':True},
    {'country':'Czech Republic', 'region':'Europe', 'population':10649800, ↪
     ↪'area':78866, 'landlocked':True},
    {'country':'Hungary', 'region':'Europe', 'population':9772756, 'area':
     ↪93030, 'landlocked':True},
    {'country':'Poland', 'region':'Europe', 'population':38386000, 'area':
     ↪312696, 'landlocked':False},
]
table_from_list = pd.DataFrame.from_records(list_of_dicts)
display(table_from_list)
```

| | country | region | population | area | landlocked |
|---|----------------|--------|------------|--------|------------|
| 0 | Slovakia | Europe | 5450421 | 49035 | True |
| 1 | Czech Republic | Europe | 10649800 | 78866 | True |
| 2 | Hungary | Europe | 9772756 | 93030 | True |
| 3 | Poland | Europe | 38386000 | 312696 | False |

1.2.2 Accessing elements of Series and DataFrame by position

- Attribute `ndim` is the number of dimensions. E.g. `areas.ndim` is 1, `table.ndim` is 2.
- Attribute `shape` is a tuple holding the size in each dimension. E.g. `areas.shape` is (4,), `table.shape` is (4,5).
- Rows and columns are numbered 0, 1, ...
- To access a particular column / row, use `some_series.iloc[row]` or `some_table.iloc[row, column]`.
- Rows and columns in `iloc` can be
 - a single number e.g. 0,

- a slice (range) e.g. 0:2 or : for everything,
- a list of positions e.g. [0, 2, 3]
- a list of boolean values [True, False, True, True].
- The result is a single element or a Series / DataFrame of a smaller size.

```
[96]: display(Markdown("/**table:**"), table)
display(Markdown("/**table.iloc[1, 2]**"), table.iloc[1, 2])
display(Markdown("/**table.iloc[[0, 2, 3], 0:2]**"), table.iloc[[0, 2, 3], 0:2])
display(Markdown("/**table.iloc[[True, False, True, True], :]**"),
       table.iloc[[True, False, True, True], :])
```

table:

| | country | region | population | area | landlocked |
|---|----------------|--------|------------|--------|------------|
| 0 | Slovakia | Europe | 5450421 | 49035 | True |
| 1 | Czech Republic | Europe | 10649800 | 78866 | True |
| 2 | Hungary | Europe | 9772756 | 93030 | True |
| 3 | Poland | Europe | 38386000 | 312696 | False |

table.iloc[1, 2]:

10649800

table.iloc[[0, 2, 3], 0:2]

| | country | region |
|---|----------|--------|
| 0 | Slovakia | Europe |
| 2 | Hungary | Europe |
| 3 | Poland | Europe |

table.iloc[[True, False, True, True], :]

| | country | region | population | area | landlocked |
|---|----------|--------|------------|--------|------------|
| 0 | Slovakia | Europe | 5450421 | 49035 | True |
| 2 | Hungary | Europe | 9772756 | 93030 | True |
| 3 | Poland | Europe | 38386000 | 312696 | False |

1.2.3 Views vs. copies

- Accessing parts of tables by iloc may return a partial copy or simply a “view”.
- If we later modify this result, it is not clear if the original table is modified.
- Direct assignment of new values to a part of the table works: some_table.iloc[row, column] = new_value modifies some_table.
- To copy a table, use other_table = some_table.copy(deep=True).

```
[97]: table2 = table.copy(deep=True)
# create a copy of the original table

table2.iloc[0,0] = 'Slovensko'
display(table2)
# table2 now has Slovensko instead of Slovakia
```

```

countries2 = table2.iloc[:, 0]
# countries2 is now a view or a copy of one column of table2
countries2.iloc[2] = 'Maďarsko'
display(table2)
# table2 now can have Hungary or Maďarsko
# we get a warning

```

| | country | region | population | area | landlocked |
|---|----------------|--------|------------|--------|------------|
| 0 | Slovensko | Europe | 5450421 | 49035 | True |
| 1 | Czech Republic | Europe | 10649800 | 78866 | True |
| 2 | Hungary | Europe | 9772756 | 93030 | True |
| 3 | Poland | Europe | 38386000 | 312696 | False |

```

/tmp/ipykernel_1087193/2667016646.py:10: SettingWithCopyWarning:
A value is trying to be set on a copy of a slice from a DataFrame

```

See the caveats in the documentation: https://pandas.pydata.org/pandas-docs/stable/user_guide/indexing.html#returning-a-view-versus-a-copy

```

countries2.iloc[2] = 'Maďarsko'
```

| | country | region | population | area | landlocked |
|---|----------------|--------|------------|--------|------------|
| 0 | Slovensko | Europe | 5450421 | 49035 | True |
| 1 | Czech Republic | Europe | 10649800 | 78866 | True |
| 2 | Maďarsko | Europe | 9772756 | 93030 | True |
| 3 | Poland | Europe | 38386000 | 312696 | False |

1.2.4 Inplace operations

- Many operations return a new table.
- If you do not need the original table, you can specify option `inplace=True`.
- The example below sorts a table by a specified column, returning a new table or replacing the old one.

```

[98]: # copy original table to table2
table2 = table.copy(deep=True)

# table3 is a copy of table2 sorted by population size
table3 = table2.sort_values(by="population")

# display both table2 and table3
display(Markdown("Original table2:"), table2)
display(Markdown("Sorted table3:"), table3)

# now change table2 to be sorted by name of the country
table2.sort_values(by="country", inplace=True)
display(Markdown("Sorted table2:"), table2)

```

Original table2:

| | country | region | population | area | landlocked |
|--|---------|--------|------------|------|------------|
|--|---------|--------|------------|------|------------|

| | | | | | |
|---|----------------|--------|----------|--------|-------|
| 0 | Slovakia | Europe | 5450421 | 49035 | True |
| 1 | Czech Republic | Europe | 10649800 | 78866 | True |
| 2 | Hungary | Europe | 9772756 | 93030 | True |
| 3 | Poland | Europe | 38386000 | 312696 | False |

Sorted table3:

| | country | region | population | area | landlocked |
|---|----------------|--------|------------|--------|------------|
| 0 | Slovakia | Europe | 5450421 | 49035 | True |
| 2 | Hungary | Europe | 9772756 | 93030 | True |
| 1 | Czech Republic | Europe | 10649800 | 78866 | True |
| 3 | Poland | Europe | 38386000 | 312696 | False |

Sorted table2:

| | country | region | population | area | landlocked |
|---|----------------|--------|------------|--------|------------|
| 1 | Czech Republic | Europe | 10649800 | 78866 | True |
| 2 | Hungary | Europe | 9772756 | 93030 | True |
| 3 | Poland | Europe | 38386000 | 312696 | False |
| 0 | Slovakia | Europe | 5450421 | 49035 | True |

1.2.5 Indexes

- Rows and columns have both an integer location (0,1,2,...) and an index (name).
- In our table, column names are 'country', 'region' etc.
- We have not named rows, so a default location-based index was constructed.
 - See the sorted tables above—their index labels are kept from the original.
- Indexes can be obtained by attributes `index` and `columns`.
- We can set the country name as an index using `set_index`, the opposite is `reset_index` (in Series, use `set_axis` and `reset_index`).
- Index can be more complex (multiindex), we will see later.

```
[99]: display(Markdown("```table.columns` is an object of class `Index`:````"),
             table.columns)
display(Markdown("```table.columns.values` is an array of column names:````"),
        table.columns.values)

display(Markdown("```table.index.values` is an array of row names, "
                + "here equal to location:````"),
        table.index.values)
display(Markdown("```index` for Series `areas`:````"), areas.index.values)

display(Markdown("```table` after setting country name as index:````"))
table2 = table.set_index('country')
display(table2)

display(Markdown("```reset_index` will put the index back as a column:````"))
table3 = table2.reset_index()
display(table3)
```

`table.columns` is an object of class `Index`:

```
Index(['country', 'region', 'population', 'area', 'landlocked'], dtype='object')
```

`table.columns.values` is an array of column names:

```
array(['country', 'region', 'population', 'area', 'landlocked'],
      dtype=object)
```

`table.index.values` is an array of row names, here equal to location:

```
array([0, 1, 2, 3])
```

index for Series areas:

```
array([0, 1, 2, 3])
```

table after setting country name as index:

| | | region | population | area | landlocked |
|----------------|--------|----------|------------|-------|------------|
| country | | | | | |
| Slovakia | Europe | 5450421 | 49035 | True | |
| Czech Republic | Europe | 10649800 | 78866 | True | |
| Hungary | Europe | 9772756 | 93030 | True | |
| Poland | Europe | 38386000 | 312696 | False | |

`reset_index` will put the index back as a column:

| | country | region | population | area | landlocked |
|---|----------------|--------|------------|--------|------------|
| 0 | Slovakia | Europe | 5450421 | 49035 | True |
| 1 | Czech Republic | Europe | 10649800 | 78866 | True |
| 2 | Hungary | Europe | 9772756 | 93030 | True |
| 3 | Poland | Europe | 38386000 | 312696 | False |

1.2.6 Accessing elements by index

- Method `some_table.loc[row, column]` is an analog of `iloc`, but using indexes rather than locations.
- You can also use `[]`, and pandas will try to guess whether it is an index or location (but sometimes it may guess wrong, so it is better to use explicit `iloc` and `loc`).
- Some examples for `Series`:

```
[100]: populations2 = populations.set_axis(countries)
display(Markdown("```\npopulations2` Series with index:\n```"), populations2)
display(Markdown("```\npopulations2.loc['Slovakia']\n```"),
       populations2.loc['Slovakia'])
display(Markdown("```\npopulations2.loc[['Slovakia', 'Poland']]`"
                  "```\n`populations2.loc[['Slovakia', 'Poland']]`"),
       populations2.loc[['Slovakia', 'Poland']])

display(Markdown("```\npopulations2[1]` and `populations2['Czech Republic']\n```"))
display(populations2[1], populations2['Czech Republic'])
```

`populations2 Series with index:`

```

Slovakia      5450421
Czech Republic 10649800
Hungary        9772756
Poland         38386000
dtype: int64

populations2.loc['Slovakia']:
5450421

populations2.loc[['Slovakia','Poland']]:
Slovakia      5450421
Poland         38386000
dtype: int64

populations2[1] and populations2['Czech Republic']:
10649800

10649800

```

1.2.7 Operations and functions on Series

- Operations such as `+`, `*` can be applied on two Series, causing them to be used on each corresponding pair of elements.
- For example, `populations / areas` will compute population density for each country.
- You can also use a single number (scalar) as an operand, e.g. `populations / 1e6` will get population in millions.
- NumPy also contains functions that can be applied to each element of a series, e.g. `np.log(populations)`.
- Relational operators such as `populations < 10e6` produce Series of boolean values.
 - Those can be then used in `[]` or `loc`.

```
[101]: # creating two Series with country as index
populations2 = populations.set_axis(countries)
areas2 = areas.set_axis(countries)
display(Markdown("**`populations2 / areas2`**"), populations2 / areas2)
display(Markdown("**`populations2 / 1e6`**"), populations2 / 1e6)
display(Markdown("**`populations2 > 10e6`**"), populations2 > 10e6)
display(Markdown("**`areas2[populations2 > 10e6]`**"),
       areas2.loc[populations2 > 10e6])
display(Markdown("**`np.log10(populations2)`**"), np.log10(populations2))
```

```

populations2 / areas2:
Slovakia      111.153686
Czech Republic 135.036644
Hungary        105.049511
Poland         122.758206
dtype: float64

populations2 / 1e6:
```

```

Slovakia      5.450421
Czech Republic 10.649800
Hungary       9.772756
Poland        38.386000
dtype: float64

populations2 > 10e6:

Slovakia      False
Czech Republic True
Hungary       False
Poland        True
dtype: bool

areas2[populations2 > 10e6]:

Czech Republic    78866
Poland            312696
dtype: int64

np.log10(populations2):

Slovakia      6.736430
Czech Republic 7.027341
Hungary       6.990017
Poland        7.584173
dtype: float64

```

Beware: when we combine two Series, e.g. by +, Pandas will use index, not position, to pair up elements.

```
[102]: a = pd.Series([1, 2, 3, 4], index=['a', 'b', 'c', 'd'])
b = pd.Series([10, 20, 30], index=['c', 'a', 'e'])
c = pd.Series([100, 200])
display(Markdown("##Series a:##"), a)
display(Markdown("##Series b:##"), b)
display(Markdown("##Series c:##"), c)
display(Markdown("##Series a+b:##"), a + b)
display(Markdown("##Series a+c:##"), a + c)
```

Series a:

```

a    1
b    2
c    3
d    4
dtype: int64

```

Series b:

```

c    10
a    20

```

```
e      30  
dtype: int64
```

Series c:

```
0      100  
1      200  
dtype: int64
```

Series a+b:

```
a    21.0
b    NaN
c    13.0
d    NaN
e    NaN
dtype: float64
```

Series a+c:

```
a    NaN  
b    NaN  
c    NaN  
d    NaN  
0    NaN  
1    NaN  
dtype: float64
```

1.2.8 Working with DataFrame columns

- DataFrame is similar to a dictionary of Series objects (columns).
 - For example, `table['area']` or `table.area` is the **column** of country areas.
 - New columns can be added to a DataFrame: `table['density'] = table['population'] / table['area']`
 - But `table[0:2]` are the first 2 **rows** of the table.
 - To be save, use `loc[]` / `iloc[]` rather than just `[]`.
 - By `table[table['population'] > 1e7]` we get countries with more than 10 million people (CZ, PL).

```
[103]: display(Markdown("```table['area']```"), table['area'])
display(Markdown("```table.area```"), table.area)
display(Markdown("Adding density"))
display(Markdown("`table['density'] = table['population'] / table['area']`"))
table['density'] = table['population'] / table['area']
display(Markdown("```table[0:2]```"), table[0:2])
display(Markdown("```table[table['population'] > 1e7]```"),
       table[table['population'] > 1e7])
```

```
table['area'];
```

0 49035
1 78866

```

2      93030
3      312696
Name: area, dtype: int64

Adding density:

table['density'] = table['population'] / table['area']



```

1.2.9 Selecting table rows with query

- Method `query` is very useful for selecting DataFrame rows satisfying some properties.
- In examples below, `@` substitutes variable value.
- While `loc[]` and `iloc[]` raise an exception if the requested value is not found, `query` can return an empty table.

```
[104]: display(Markdown("```table.query(\"country=='Slovakia'\")```"),
               table.query("country=='Slovakia'"))

def get_country(table, country):
    """Get a given country from the table"""
    return table.query("country == @country")
display(Markdown("```The same but for Hungary and using a function:```"),
       get_country(table, 'Hungary'))

display(Markdown("```Query with an empty result:```"))
display(Markdown("`table.query(\"population < 10e6 and not landlocked\")`"))
display(table.query("population < 10e6 and not landlocked"))
```

```
table.query("country=='Slovakia'):

    country  region  population     area  landlocked      density
0  Slovakia  Europe      5450421   49035        True  111.153686
```

The same but for Hungary and using a function:

```
country  region  population   area  landlocked      density
2  Hungary    Europe      9772756  93030        True  105.049511
```

Query with an empty result:

```
table.query("population < 10e6 and not landlocked"):

Empty DataFrame
Columns: [country, region, population, area, landlocked, density]
Index: []
```

1.2.10 Importing and exporting data

- Import and export is possible using many [file formats](#) (text-based CSV, JSON, HTML; binary Excel, HDF5 etc.).
- We will mostly use CSV (=comma separated values) format.
 - Each table row is one line of the file.
 - Columns are separated by commas.
 - Columns containing commas or end-of-line characters may be enclosed in quotation marks.
 - Sometimes a different column separator is used, e.g. tab "\t".
- Writing our table to a csv file: `table.to_csv("countries.csv")`.
 - If run in Colab, this will create a temporary file, which you can save on your computer (see the right panel, tab Files).
- Conversely, `table2 = pd.read_csv("countries.csv", index_col=0)` will read data from the file to a new `DataFrame` called `table2`.
- Input and output functions allow you to set many optional arguments to tweak the format.

1.3 Example: a table of country populations from the United Nations

- Obtained from the UN webpage <https://data.un.org/>
- We will read the table in CSV format directly from a URL.
- We need to play a bit with settings:
 - We skip the top two lines.
 - We supply our own (simpler) column names.
 - We specify character encoding (default is UTF8) and that thousands are separated by a comma in numerical values, such as 1,000,000.
 - Note that empty fields (missing values) are imported as `np.Nan`.

```
[105]: # original source:
# url = 'https://data.un.org/_Docs/SYB/CSV/
#         ↪SYB65_1_202209_Population,%20Surface%20Area%20and%20Density.csv'
# our local copy:
url = 'https://bbrejova.github.io/viz/data/Un_population.csv'
column_names = ['Region ID', 'Region', 'Year',
                 'Series', 'Value', 'Footnotes', 'Source']
un_table = pd.read_csv(url, encoding='latin-1', names=column_names,
                       skiprows=2, thousands=",")
```

```
# print the first 5 rows to check the result
un_table.head()
```

```
[105]:    Region ID          Region  Year  \
0           1  Total, all countries or areas  2010
1           1  Total, all countries or areas  2010
2           1  Total, all countries or areas  2010
3           1  Total, all countries or areas  2010
4           1  Total, all countries or areas  2010

                                         Series  Value  Footnotes  \
0  Population mid-year estimates (millions)  6985.60      NaN
1  Population mid-year estimates for males (milli...  3514.41      NaN
2  Population mid-year estimates for females (mil...  3471.20      NaN
3  Sex ratio (males per 100 females)        101.20      NaN
4  Population aged 0 to 14 years old (percentage)   27.10      NaN

                                         Source
0  United Nations Population Division, New York, ...
1  United Nations Population Division, New York, ...
2  United Nations Population Division, New York, ...
3  United Nations Population Division, New York, ...
4  United Nations Population Division, New York, ...
```

```
[106]: # print the last 5 rows, to see if the bottom looks ok
un_table.tail()
```

```
[106]:    Region ID  Region  Year  \
7868       716  Zimbabwe  2022
7869       716  Zimbabwe  2022
7870       716  Zimbabwe  2022
7871       716  Zimbabwe  2022
7872       716  Zimbabwe  2022

                                         Series  Value  \
7868  Population mid-year estimates for females (mil...  8.61
7869  Sex ratio (males per 100 females)                89.40
7870  Population aged 0 to 14 years old (percentage)  40.60
7871  Population aged 60+ years old (percentage)       4.80
7872  Population density                           42.20

                                         Footnotes  \
7868  Projected estimate (medium fertility variant).
7869  Projected estimate (medium fertility variant).
7870  Projected estimate (medium fertility variant).
7871  Projected estimate (medium fertility variant).
7872  Projected estimate (medium fertility variant).
```

| | Source |
|------|---|
| 7868 | United Nations Population Division, New York, ... |
| 7869 | United Nations Population Division, New York, ... |
| 7870 | United Nations Population Division, New York, ... |
| 7871 | United Nations Population Division, New York, ... |
| 7872 | United Nations Population Division, New York, ... |

[107]: `# check types of columns; strings are imported as object, which is expected
un_table.dtypes`

```
Region ID      int64
Region        object
Year          int64
Series        object
Value         float64
Footnotes     object
Source        object
dtype: object
```

- Each country has data for several years.
- There are several values per country and year, e.g. total population, the number of men and women, sizes of three age groups.
- The first part of the table contains various continents and regions, later individual countries arranged alphabetically from 'Afghanistan' to 'Zimbabwe'.

1.3.1 A simple table with total population across years

We will create a simpler table `country_pop`.

- It will contain only countries, not regions.
- It will contain only rows with total population, all available years.
- It will contain columns `Country` (originally `Region`), `Year`, and `Population` (originally `Value`).

[108]: `# get all rows for Afghanistan, choose the label for the first of them
first_country = un_table.query('Region == "Afghanistan"').index[0]
get all rows from the first Afghanistan onwards and all columns
un_countries = un_table.iloc[first_country:, :]
get only rows with total population and select only some columns using loc
country_pop = (un_countries
 .query('Series=="Population mid-year estimates (millions)"')
 .loc[:, ['Region', 'Year', 'Value']]
 .rename(columns={'Value':'Population', 'Region':'Country'}))
print the start of the result
country_pop.head()`

```
[108]:      Country  Year  Population
930  Afghanistan  2010    28.19
937  Afghanistan  2015    33.75
945  Afghanistan  2020    38.97
953  Afghanistan  2022    41.13
960    Albania    2010    2.91
```

1.4 Tidy data, wide and long tables

- The original UN table has in column `Value` various values, including population size, sex ratio, population density, etc.
- In general, one column of a table should contain values of the same type.
- This is true in our `country_pop` table with columns `Country`, `Year`, and `Population`.
- This type of table is called **long** and is usually preferable.
- For some analysis, we may want to have countries as rows and years as columns; this is called a **wide table**.
- Pandas has methods to convert between the two formats, e.g. `wide_to_long`, `melt`, `pivot`, `unstack` etc.
- See the article [Tidy data](#) by Hadley Wickham for a longer discussion.

1.5 Back to example: comparing populations in 2010 and 2022

- We select only two years from `country_pop`.
- Function `pivot` will use the column `Country` as the row index, values from column `Year` as new column names and values from column `Population` as values to populate the table itself.
- Finally we rename the columns so that they are strings starting with a letter; otherwise they are harder to be used in query.

```
[109]: display(Markdown("**Original `country_pop` table:**"), country_pop.head())
```

```
pop = (country_pop.query("Year==2010 or Year==2022")
       .pivot(index='Country', columns=['Year'], values='Population')
       .rename(columns={2010:'pop2010', 2022:'pop2022'}))

display(Markdown("**New `pop` table:**"), pop.head())
```

Original `country_pop` table:

| | Country | Year | Population |
|-----|-------------|------|------------|
| 930 | Afghanistan | 2010 | 28.19 |
| 937 | Afghanistan | 2015 | 33.75 |
| 945 | Afghanistan | 2020 | 38.97 |
| 953 | Afghanistan | 2022 | 41.13 |
| 960 | Albania | 2010 | 2.91 |

New pop table:

| Year | pop2010 | pop2022 |
|----------------|---------|---------|
| Country | | |
| Afghanistan | 28.19 | 41.13 |
| Albania | 2.91 | 2.84 |
| Algeria | 35.86 | 44.90 |
| American Samoa | 0.05 | 0.04 |
| Andorra | 0.07 | 0.08 |

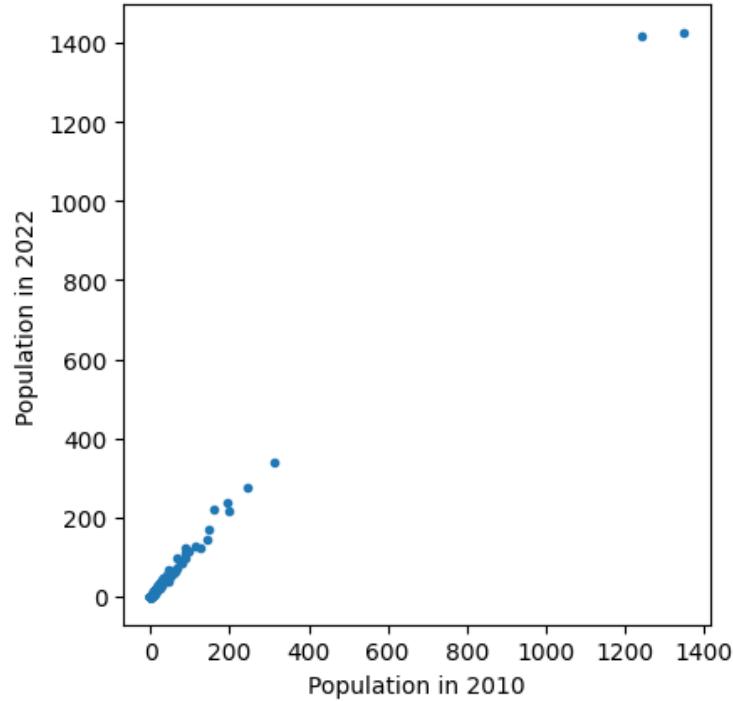
```
[110]: # compute the difference between years for each country (positive = increase)
pop['difference'] = pop['pop2022'] - pop['pop2010']
# relative difference, as a fraction of population in 2010
# (value 1 means 100% increase)
pop['relDifference'] = pop['difference'] / pop['pop2010']
pop.head()
```

```
[110]: Year          pop2010    pop2022   difference   relDifference
Country
Afghanistan      28.19      41.13      12.94       0.459028
Albania           2.91       2.84      -0.07      -0.024055
Algeria            35.86      44.90       9.04       0.252091
American Samoa    0.05       0.04      -0.01      -0.200000
Andorra            0.07       0.08       0.01       0.142857
```

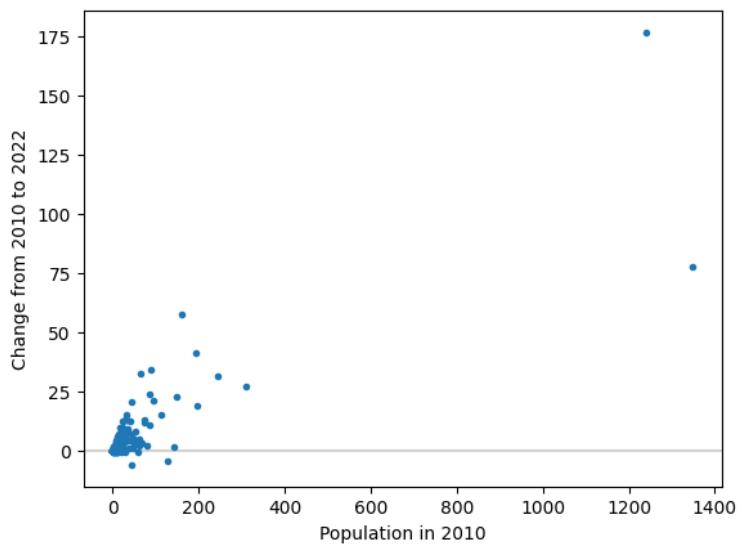
Now we will use this table to create some plots and tables.

- What can you observe from these data displays?
- Are some of these visualizations more useful than others or are they complementary? How could we improve them?
- What other questions you could ask about this table and how would you answer them using plots or tables?

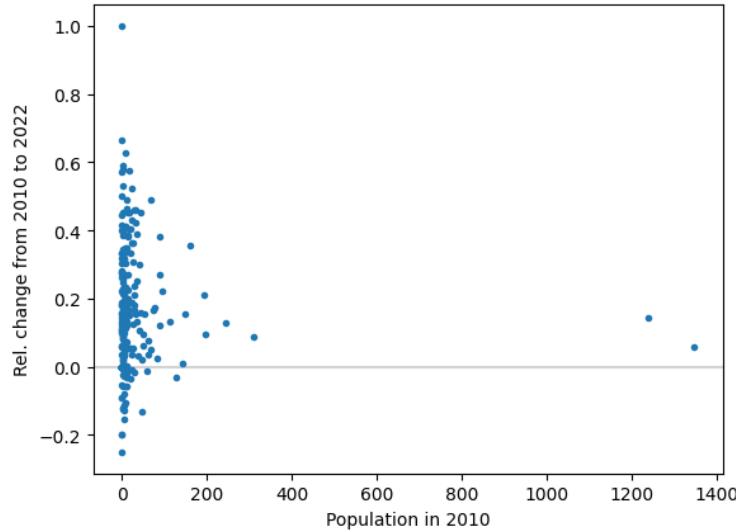
```
[111]: figure, axes = plt.subplots()
axes.plot(pop.pop2010, pop.pop2022, '.')
axes.set_aspect('equal')
axes.set_xlabel('Population in 2010')
axes.set_ylabel('Population in 2022')
pass
```



```
[112]: figure, axes = plt.subplots()
axes.axhline(0, color="lightgrey")
axes.plot(pop.pop2010, pop.difference, '.')
axes.set_xlabel('Population in 2010')
axes.set_ylabel('Change from 2010 to 2022')
pass
```



```
[113]: figure, axes = plt.subplots()
axes.axhline(0, color="lightgrey")
axes.plot(pop.pop2010, pop.relDifference, '.')
axes.set_xlabel('Population in 2010')
axes.set_ylabel('Rel. change from 2010 to 2022')
pass
```



```
[114]: pop.sort_values('relDifference').head(10)
```

| Year Country | pop2010 | pop2022 | difference | relDifference |
|----------------------------|---------|---------|------------|---------------|
| Saint Martin (French part) | 0.04 | 0.03 | -0.01 | -0.250000 |
| American Samoa | 0.05 | 0.04 | -0.01 | -0.200000 |
| Marshall Islands | 0.05 | 0.04 | -0.01 | -0.200000 |
| Bosnia and Herzegovina | 3.81 | 3.23 | -0.58 | -0.152231 |
| Ukraine | 45.68 | 39.70 | -5.98 | -0.130911 |
| Puerto Rico | 3.72 | 3.25 | -0.47 | -0.126344 |
| Lithuania | 3.14 | 2.75 | -0.39 | -0.124204 |
| Latvia | 2.10 | 1.85 | -0.25 | -0.119048 |
| Republic of Moldova | 3.68 | 3.27 | -0.41 | -0.111413 |
| Bulgaria | 7.59 | 6.78 | -0.81 | -0.106719 |

```
[115]: pop.sort_values('relDifference', ascending=False).head(10)
```

| Year Country | pop2010 | pop2022 | difference | relDifference |
|-----------------|---------|---------|------------|---------------|
| Anguilla | 0.01 | 0.02 | 0.01 | 1.000000 |

| | | | | |
|-------------------------------|-------|-------|-------|----------|
| Turks and Caicos Islands | 0.03 | 0.05 | 0.02 | 0.666667 |
| Jordan | 6.93 | 11.29 | 4.36 | 0.629149 |
| Oman | 2.88 | 4.58 | 1.70 | 0.590278 |
| Qatar | 1.71 | 2.70 | 0.99 | 0.578947 |
| Niger | 16.65 | 26.21 | 9.56 | 0.574174 |
| Mayotte | 0.21 | 0.33 | 0.12 | 0.571429 |
| Equatorial Guinea | 1.09 | 1.67 | 0.58 | 0.532110 |
| Angola | 23.36 | 35.59 | 12.23 | 0.523545 |
| Bonaire, St. Eustatius & Saba | 0.02 | 0.03 | 0.01 | 0.500000 |

```
[116]: neighbor_countries =_
    ['Slovakia', 'Czechia', 'Hungary', 'Poland', 'Austria', 'Ukraine']
neighbors = pop.loc[neighbor_countries, : ]
display(neighbors)
```

| Year | pop2010 | pop2022 | difference | relDifference |
|----------|---------|---------|------------|---------------|
| Country | | | | |
| Slovakia | 5.40 | 5.64 | 0.24 | 0.044444 |
| Czechia | 10.46 | 10.49 | 0.03 | 0.002868 |
| Hungary | 9.99 | 9.97 | -0.02 | -0.002002 |
| Poland | 38.60 | 39.86 | 1.26 | 0.032642 |
| Austria | 8.36 | 8.94 | 0.58 | 0.069378 |
| Ukraine | 45.68 | 39.70 | -5.98 | -0.130911 |

1.6 Summary and outlook

- We will work mostly with tabular data.
- We will store them in `DataFrame` from Pandas library.
- This is more convenient and more efficient than regular Python lists.
- We have seen several functions for basic manipulation:
 - `iloc[]`, `loc[]`, `query`, `head`, `set_index`, `reset_index`, `rename`, `pivot`, `copy`, `sort_values`, operations and functions on `Series`.
- Next lecture will be focused on examples of different chart types.
- More Pandas later.

Lecture 3a

Overview of Plot Types

Data visualization · 1-DAV-105

Lecture by Broňa Brejová

Plan for today

- Types of variables (columns)
- Gallery of different plot types, some discussion of their properties
- Some notes on how to draw them in Python (more in a notebook)

Types of variables (columns)

Categorical / qualitative

- **Nominal:** values have no fixed ordering (for example, gender, country, color)
- **Ordinal:** values are ordered (for example education level primary / secondary / university; star ranking 0-5)

Numerical / quantitative

- **Discrete:** typically counts
- **Continuous:** typically measurements

Types of variables (columns)

Numerical / quantitative

- **Discrete:** typically counts
- **Continuous:** typically measurements

Numerical variables also categorized as follows:

- **Ratio (pomerová):** if zero means "none", and it is meaningful to compute ratios / percentages (mass, length, duration, cost, ...)
- **Interval:** does not have "true zero", we can subtract but not make ratios (temperature in degrees C, date)

Data for today

- Various country indicators downloaded from the World Bank for years 2000, 2010, 2020
- Population, area, GDP per capita, life expectancy, fertility (number of children per woman)
- Also classification into regions and income groups
- Which are categorical / numerical?

We will also use Gapminder life expectancy 1990-2021 from I01

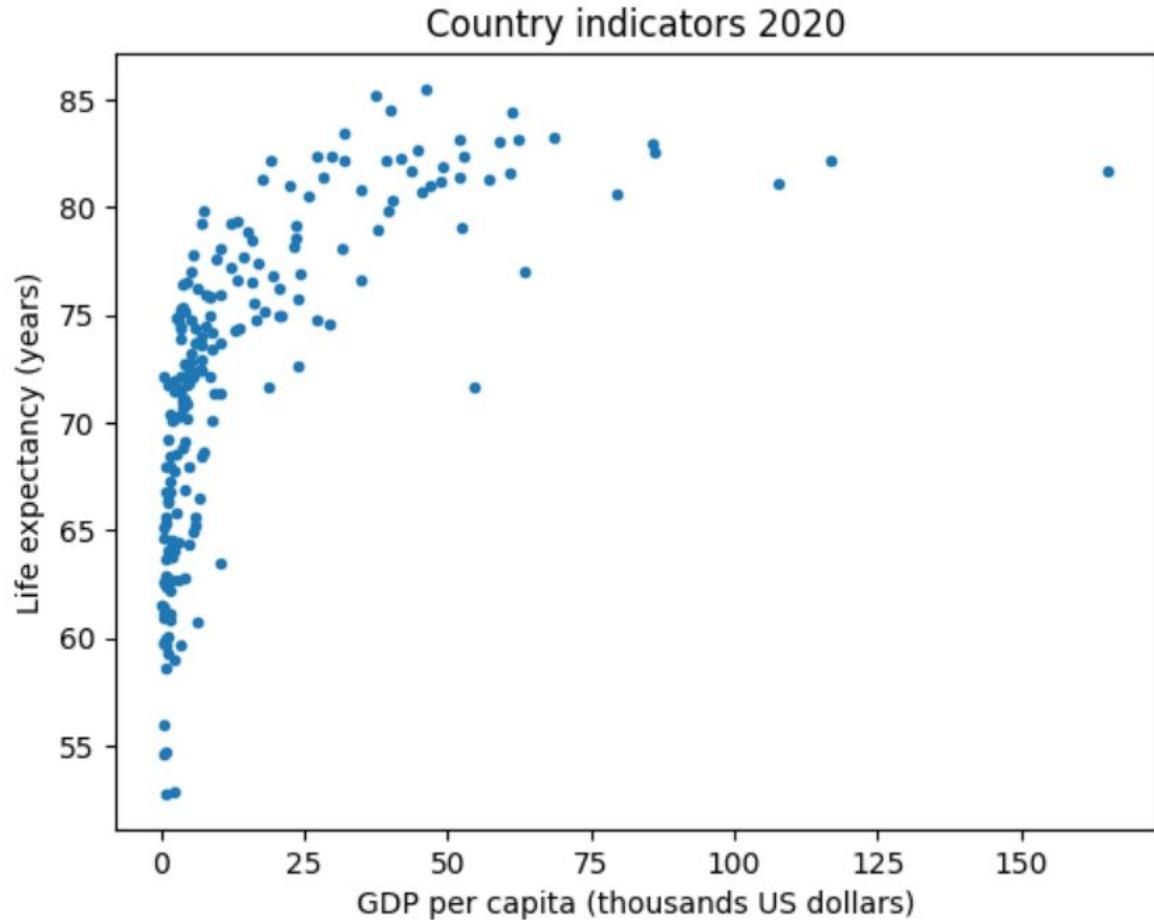
Scatter plot (bodový graf)

Good for two numerical variables (x and y).

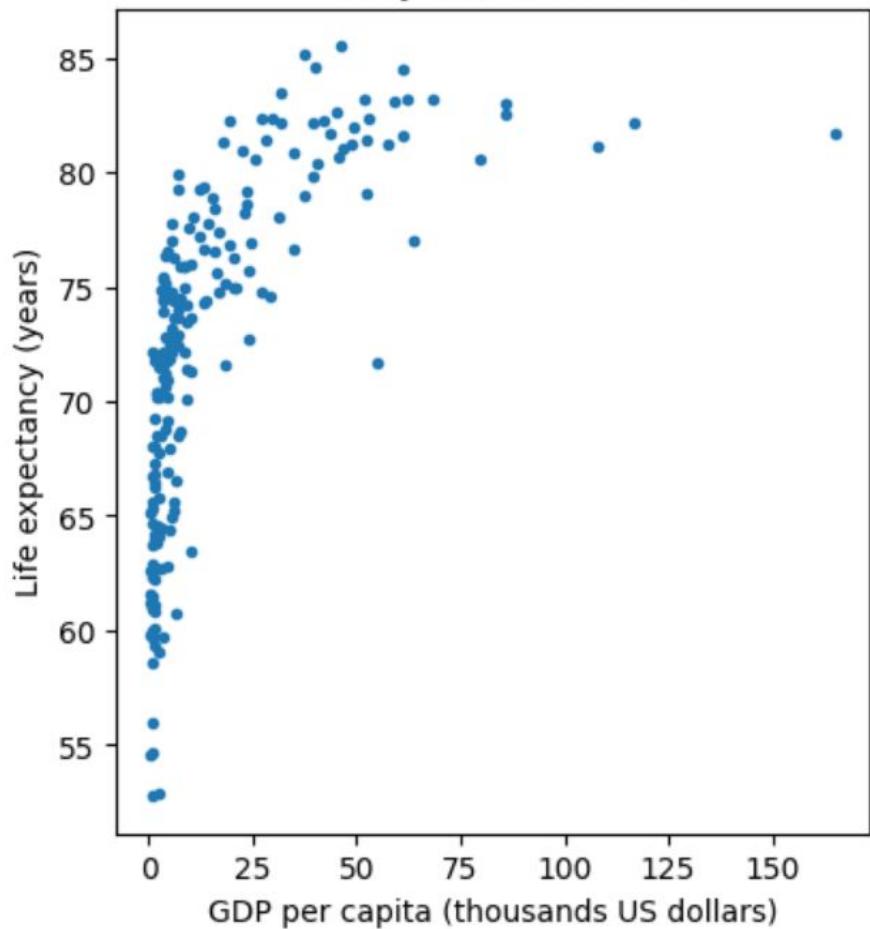
In this plot, many points near left boundary, most space empty.

Solution 1: combine overall view and detail

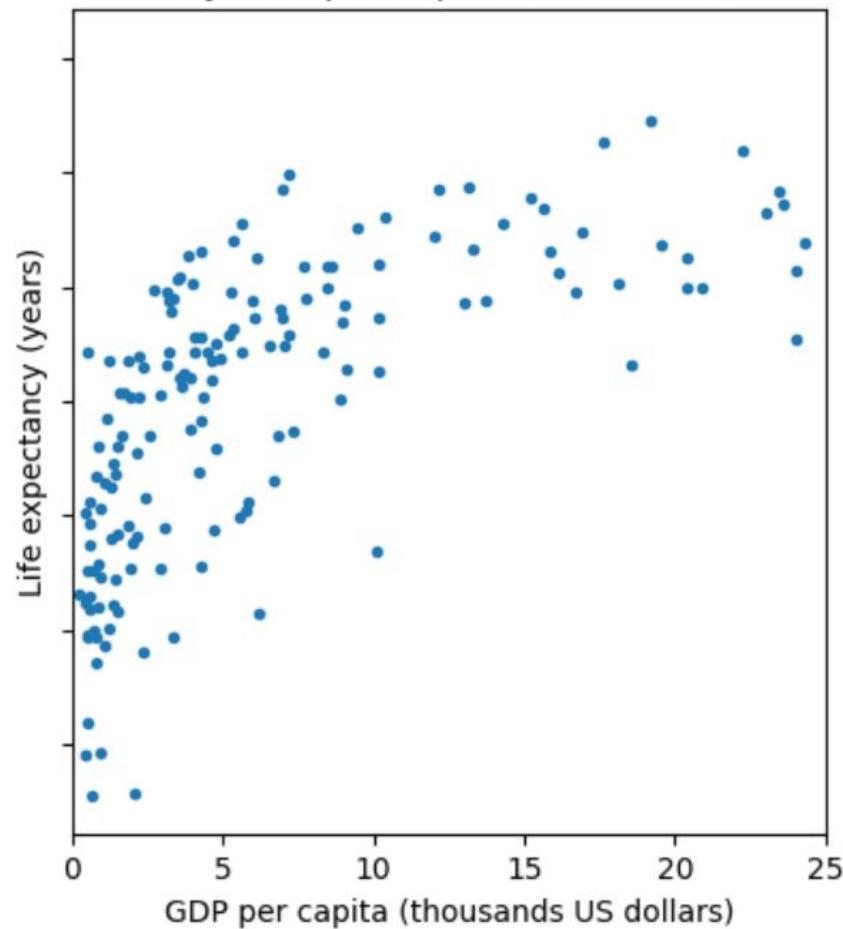
Solution 2: log scale



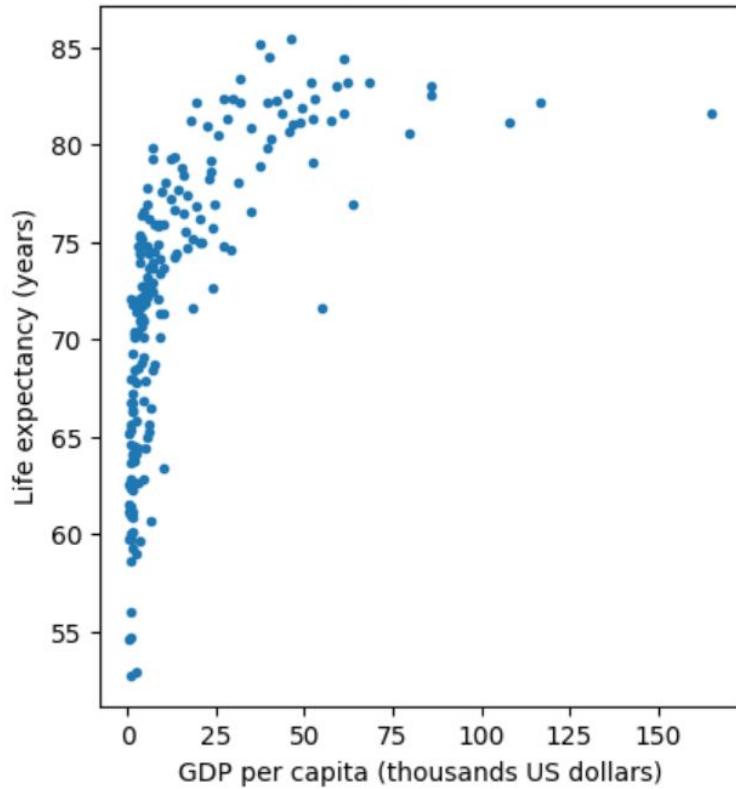
Country indicators 2020



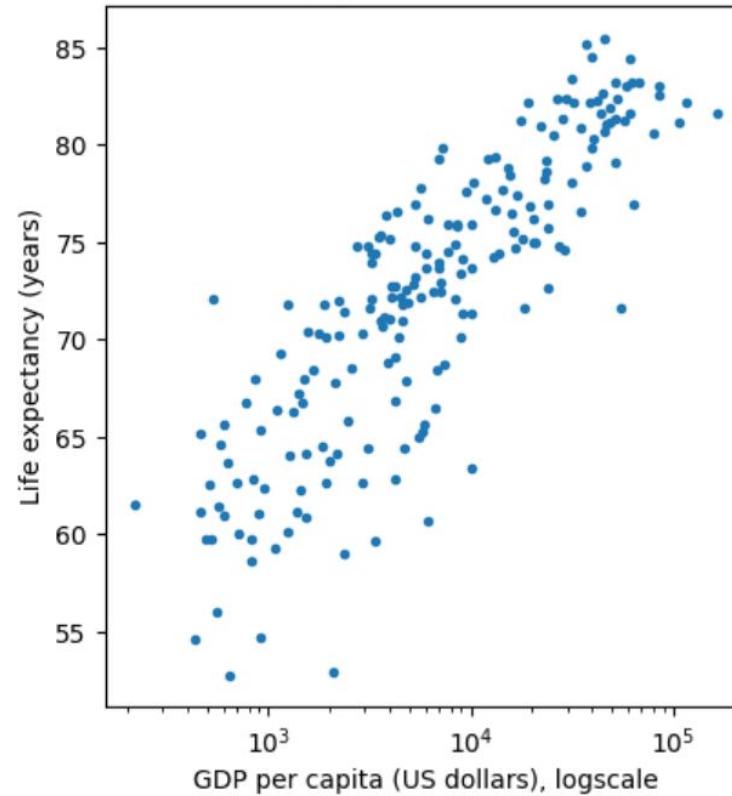
Only GDP per capita < 25000 USD



Country indicators 2020

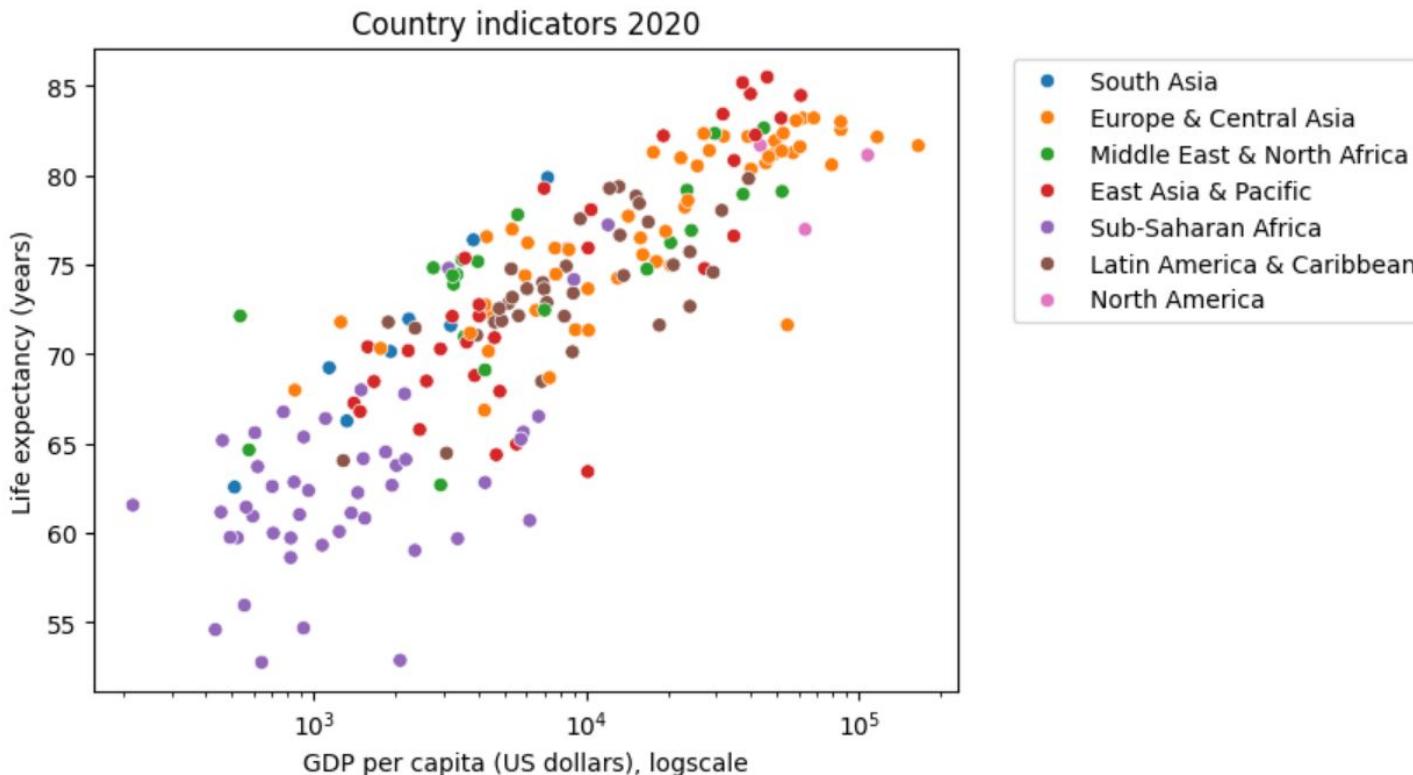


Country indicators 2020

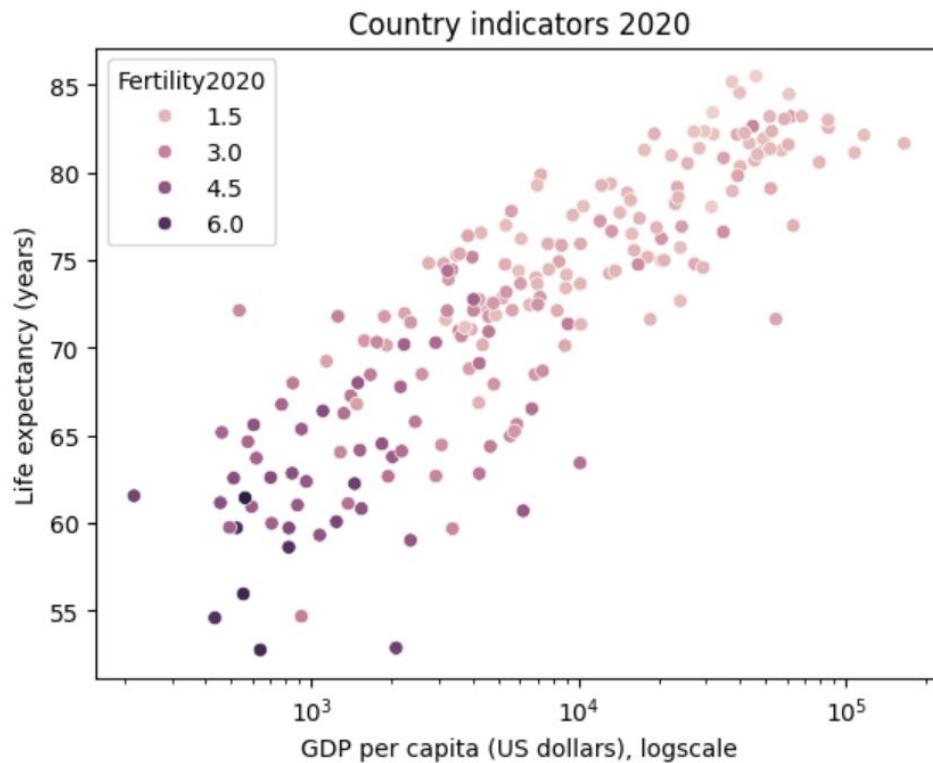


Log-scale x-axis: draw at $\log(x)$ instead of x , but axis ticks show values of x

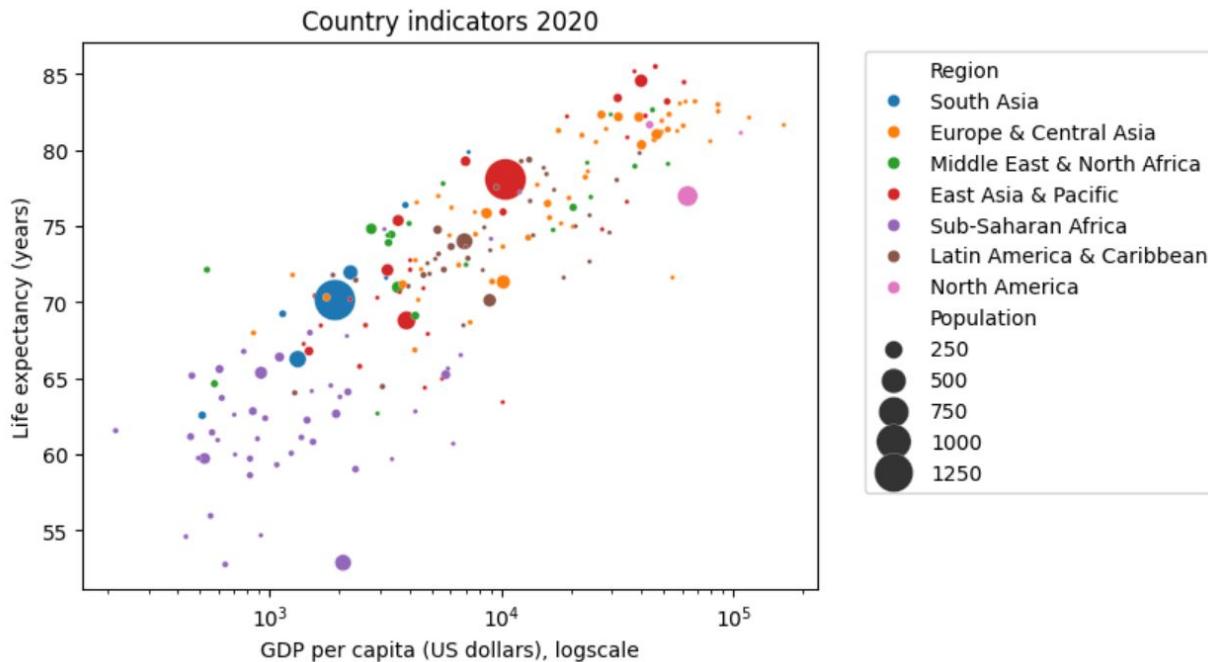
Adding a categorical variable with color



Adding a numerical variable with color scale

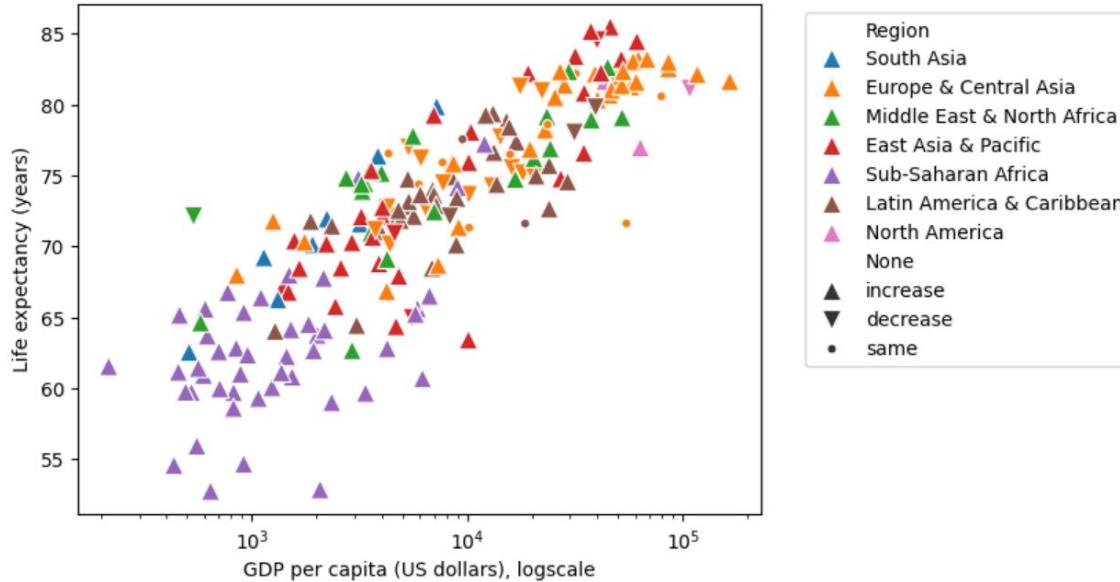


Adding numerical variable with marker size



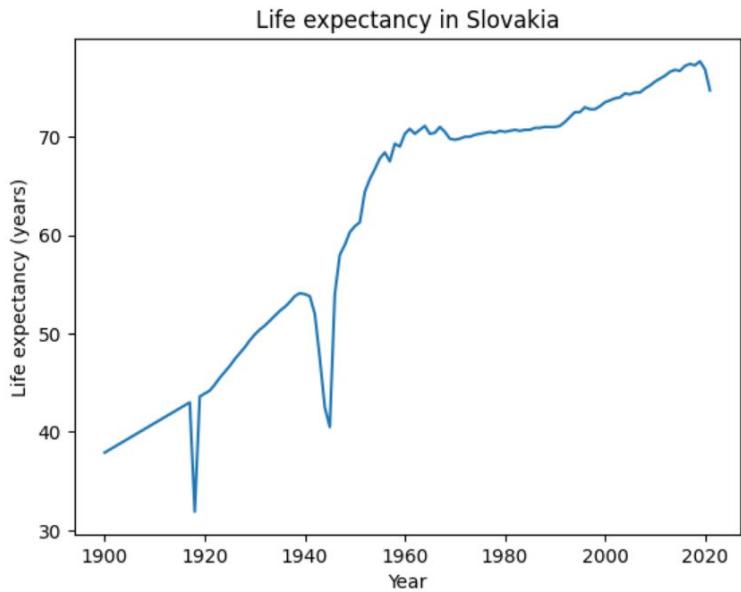
Variable value should be proportional to circle area, not diameter!

Adding categorical variable with marker shape



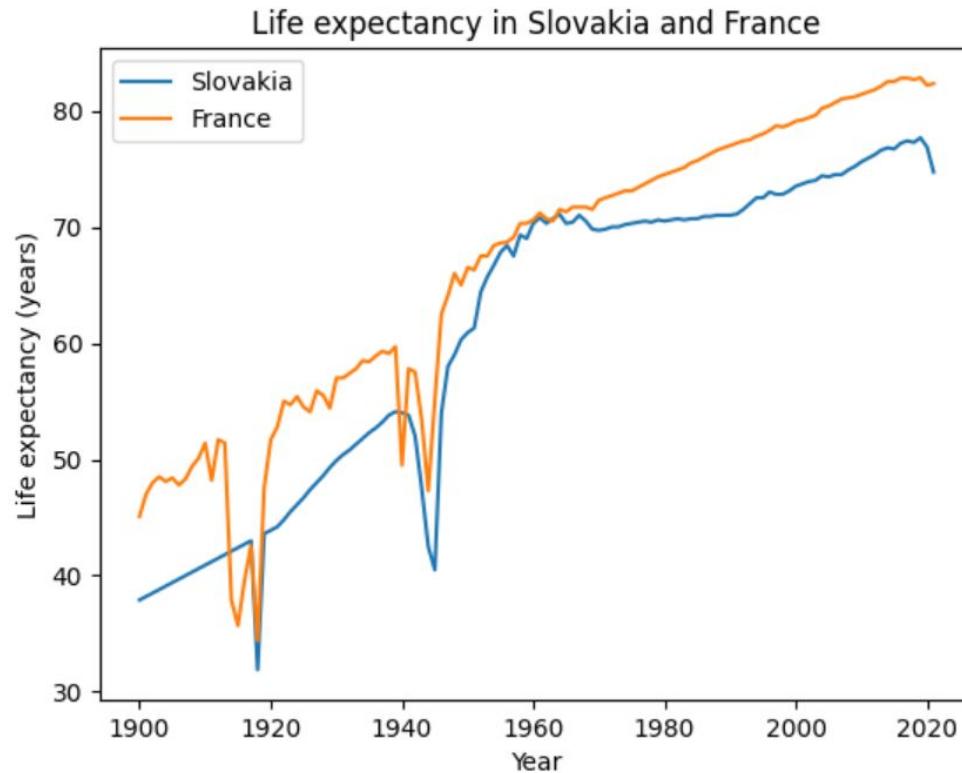
Hard to read, particularly for many data points
Showing population change between 2000 and 2020
If less than 1% change, marked as equal

Line graph (čiarový graf)

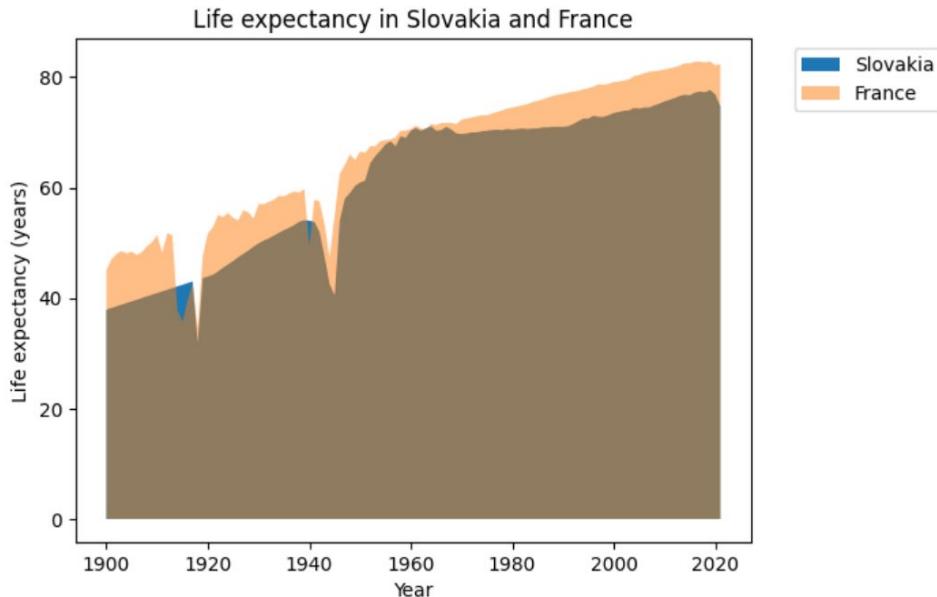


Emphasizing continuity between data points
Data points can be also shown as markers

Adding categorical variable with color



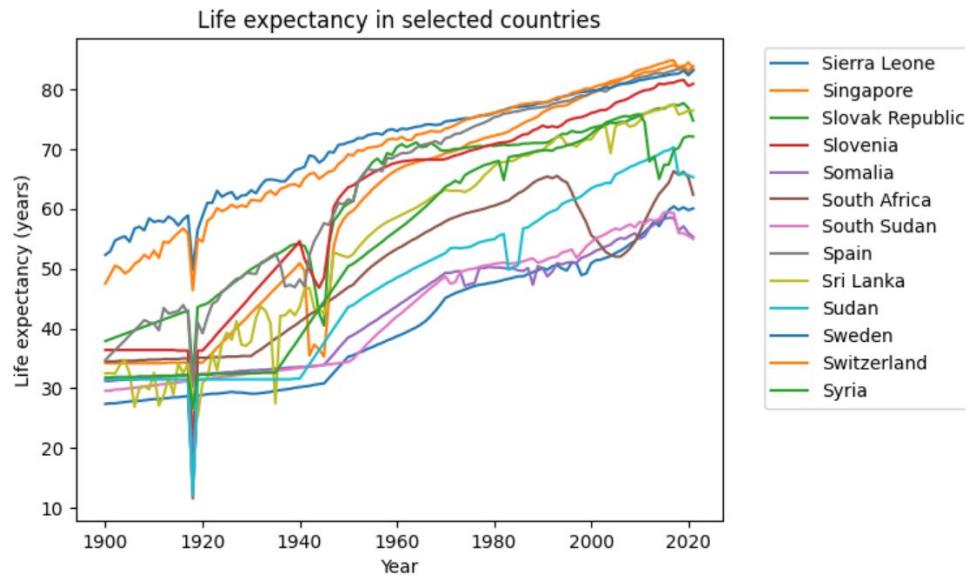
Area graph (plošný graf)



Y-axis must start at 0

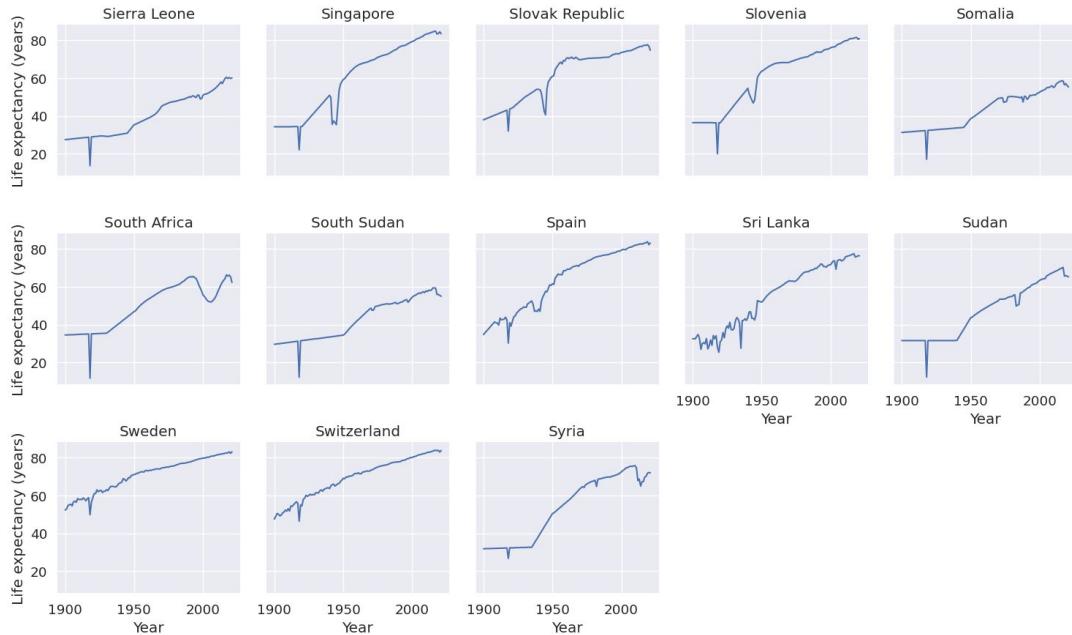
Emphasizes differences more than line graph, but also more cluttered

Line graph with many lines



Hard to follow individual lines, but shows general trends and comparisons.
Countries with names Si..Sw, and having population at least 1 million.
Note that colors start to repeat.

Small multiples



A small plot for each value of a categorical variable

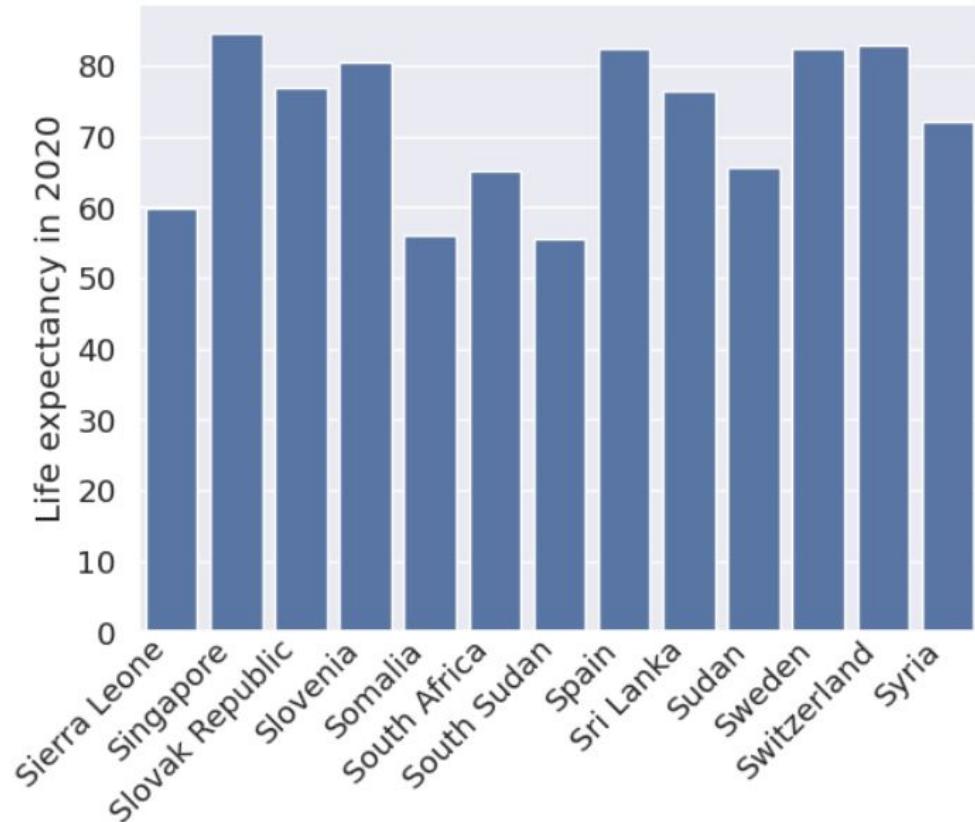
Must have the same axes!

Exact comparison difficult, but it is possible to notice different trends

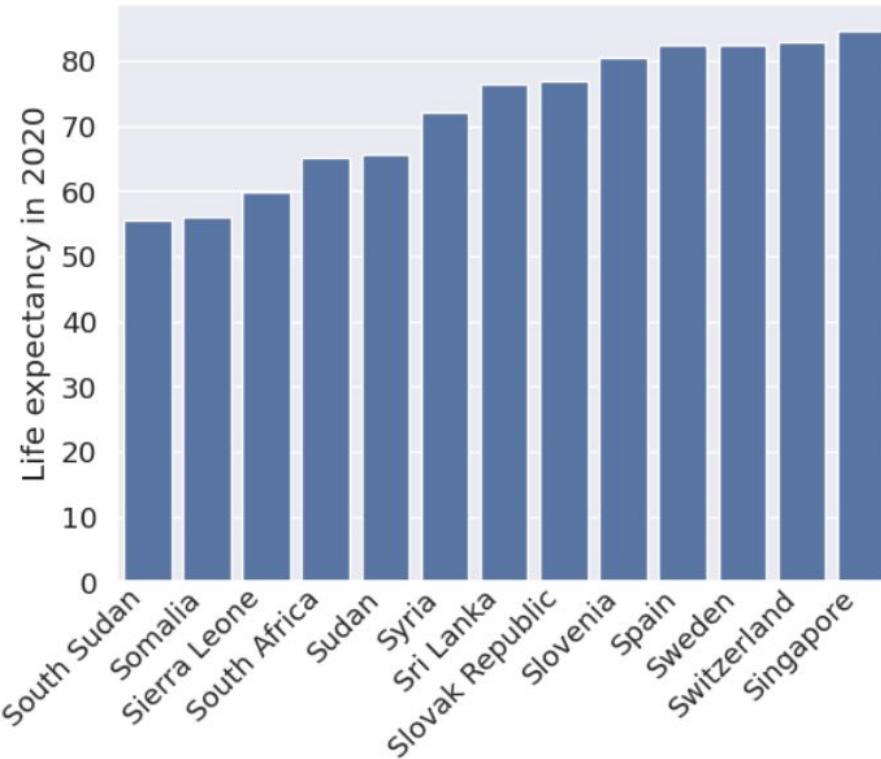
Bar graph (stípcový/pruhový graf)

X-axis is categorical

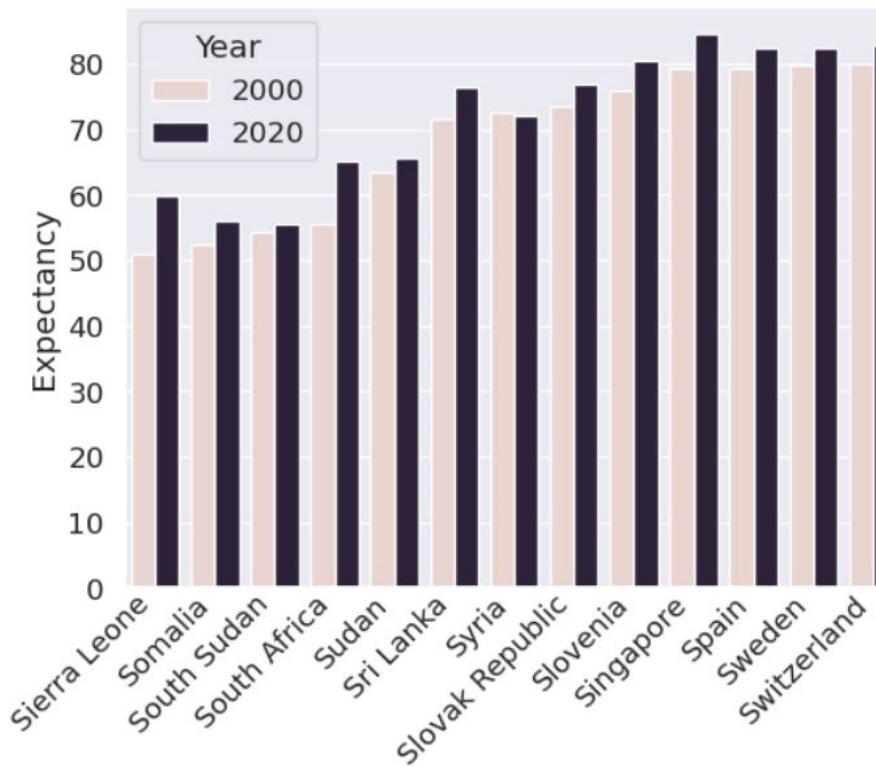
Y-axis must start at 0



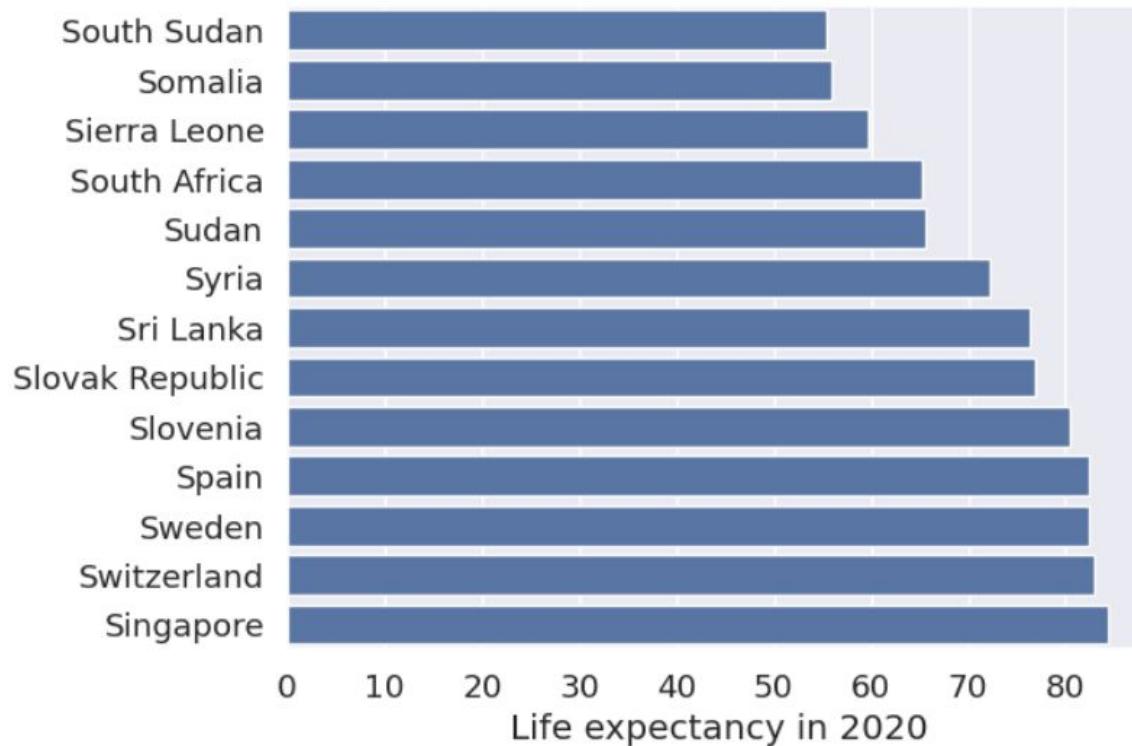
Bar graph with sorted columns



Bar graph with colored columns



Bar graphs can be horizontal



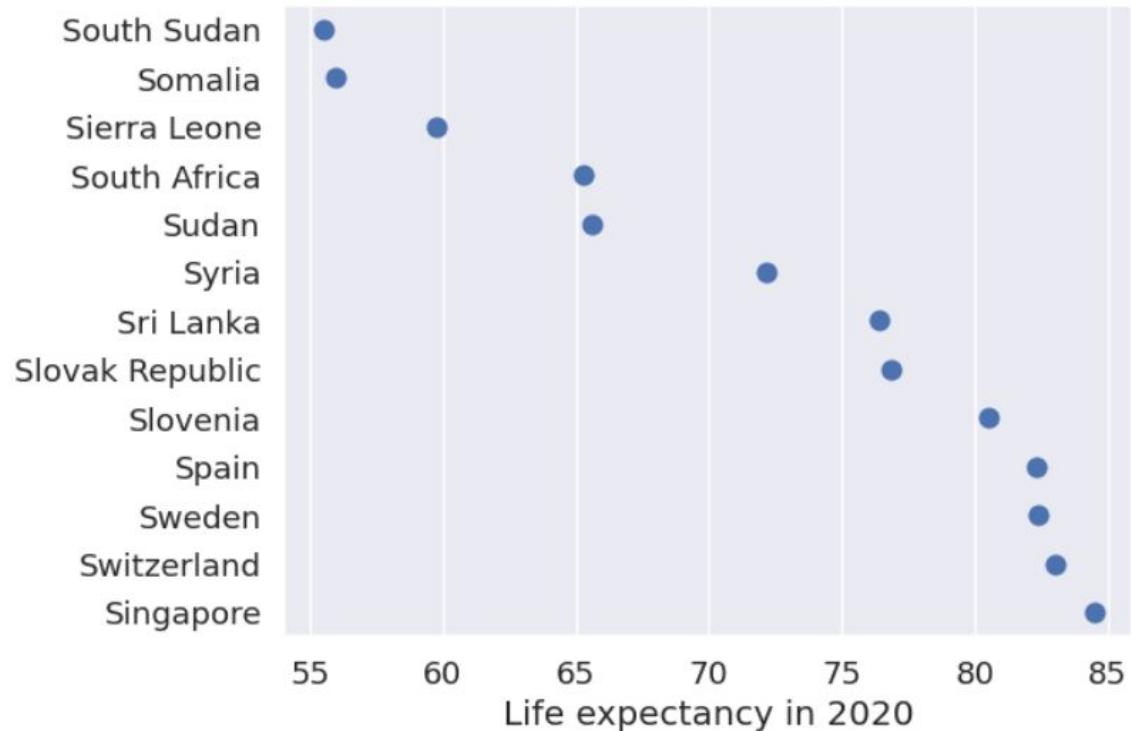
Dot plot

As bar graph but only dots shown at the top of the bar

Less clutter

X-axis does not need to start at 0 - better use of space

Can use multiple colors

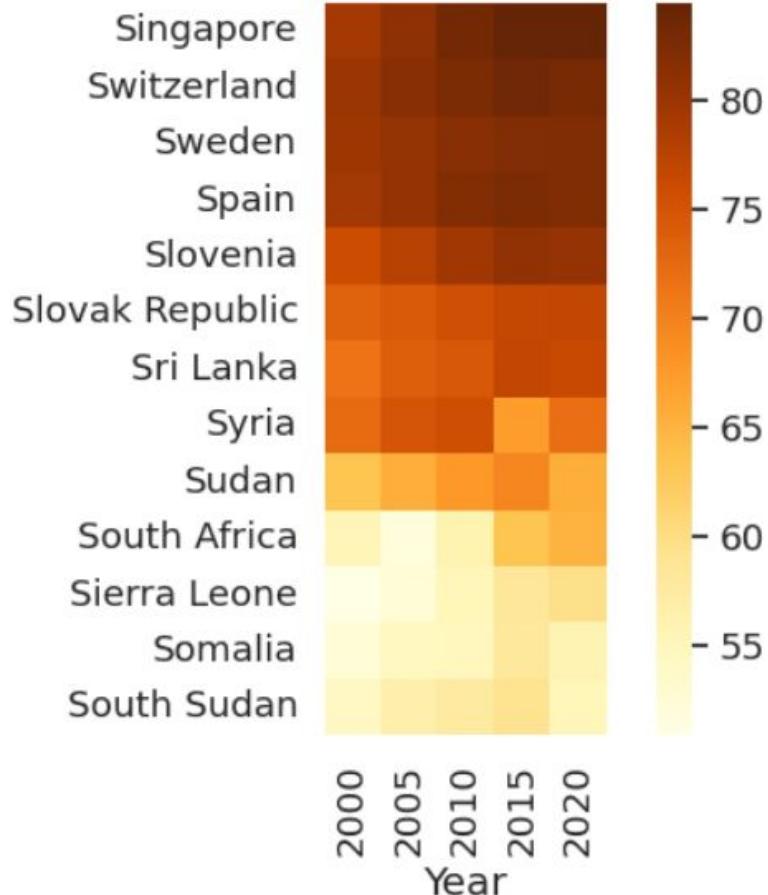


Heatmap

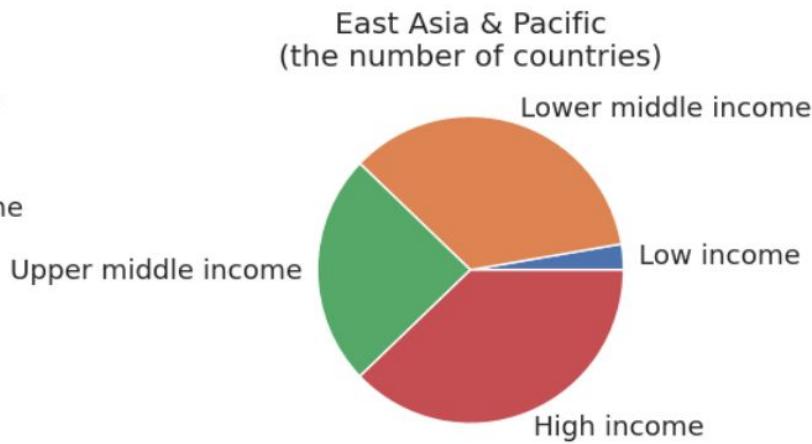
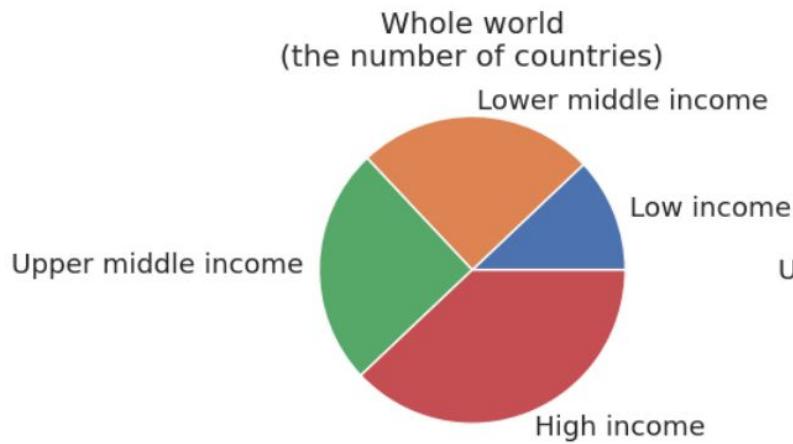
Both axes categorical

Numerical value shown in a color scale

Compact display, but color scales harder to read



Pie chart (koláčový graf)



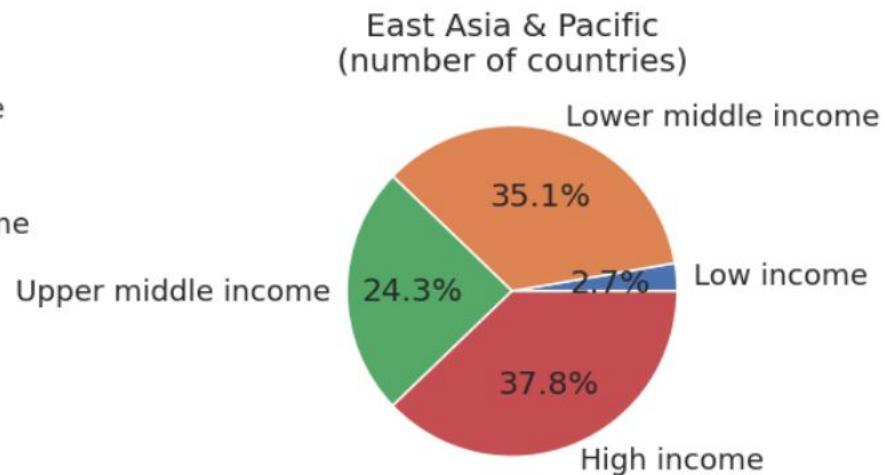
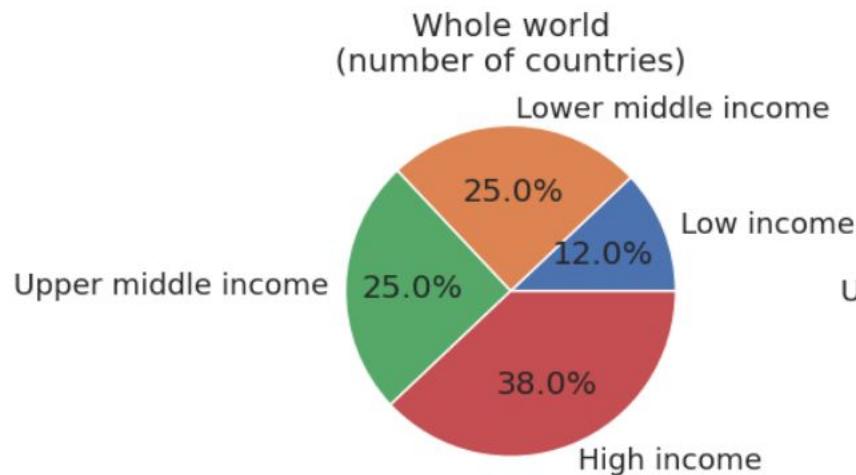
Obvious that percentages displayed

Very large values are easy to see (here high income)

Hard to compare similar values to each other

Space use not good

Pie chart with values labeled



Easier to compare but still not ideal
Labeling values also useful in other types of graphs

Stacked (skladaný) bar graph instead of pie chart



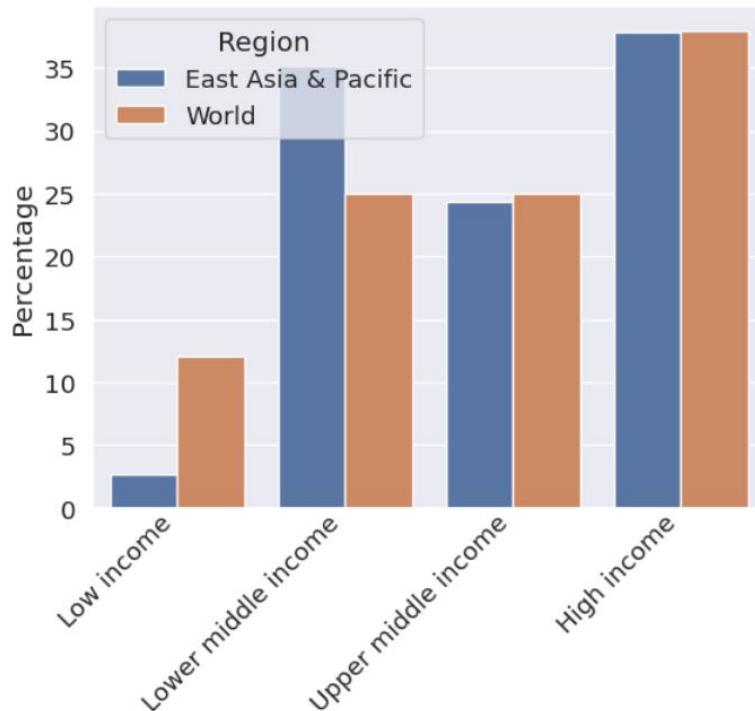
Rectangles easier to compare than wedges

Benefits from labeled values

Middle colors hard to compare across bars

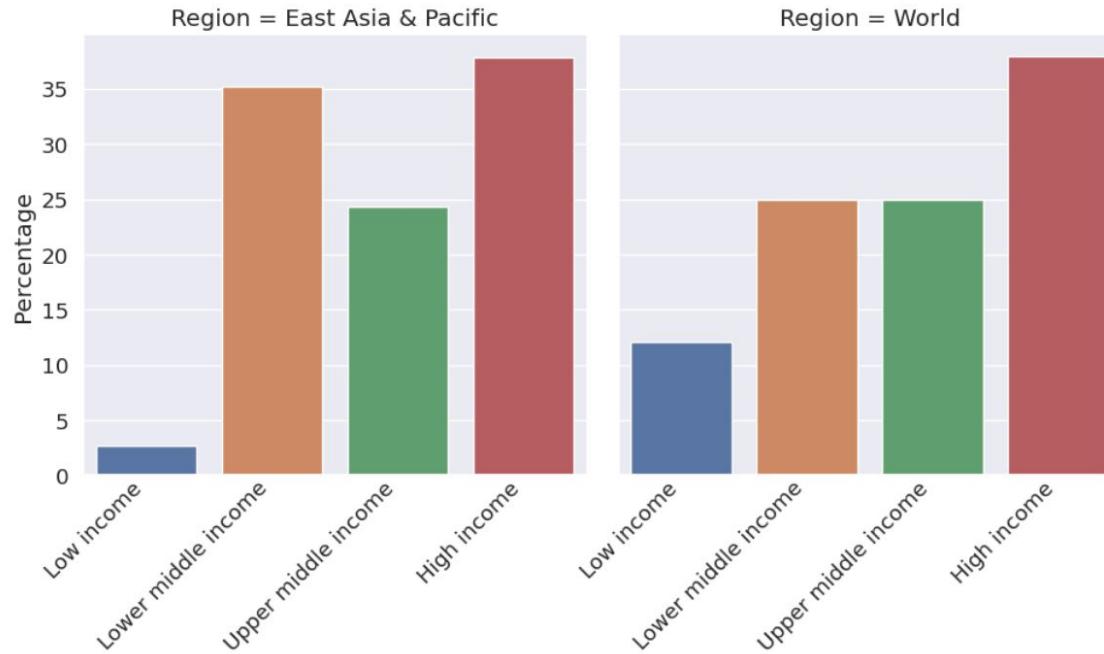
Similar idea: stacked area plot (change in percentages over time)

Colored bar graph instead of pie chart



Easy to compare East Asia vs whole world.
Not obvious that we show parts of a whole.

Colored bar graph instead of pie chart



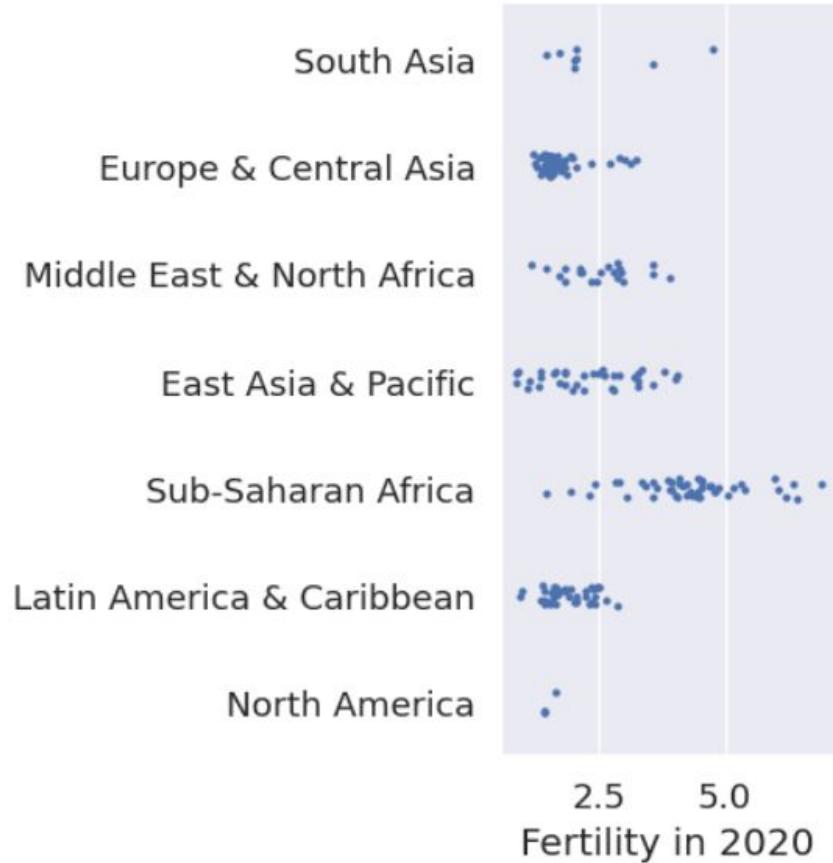
Easy to compare income groups within region

Strip plot

One axis categorical

Other axis shows individual data points

Jitter added in categorical axis to avoid point overlap

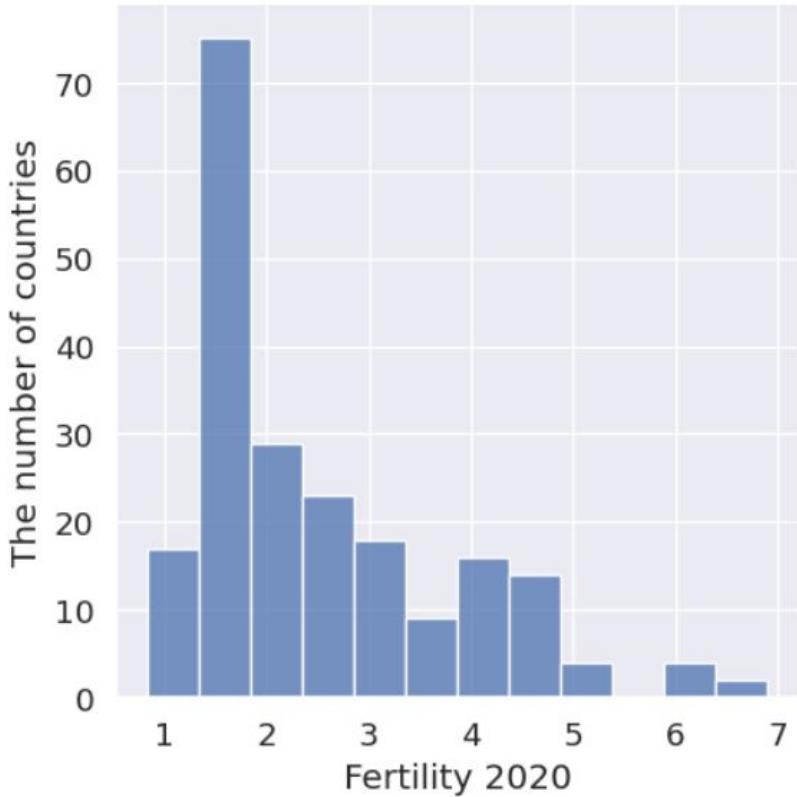


Histogram

For 1D numerical data

Split values into bins, show bin sizes as bar graph

We could use colors to display 2 or more histograms



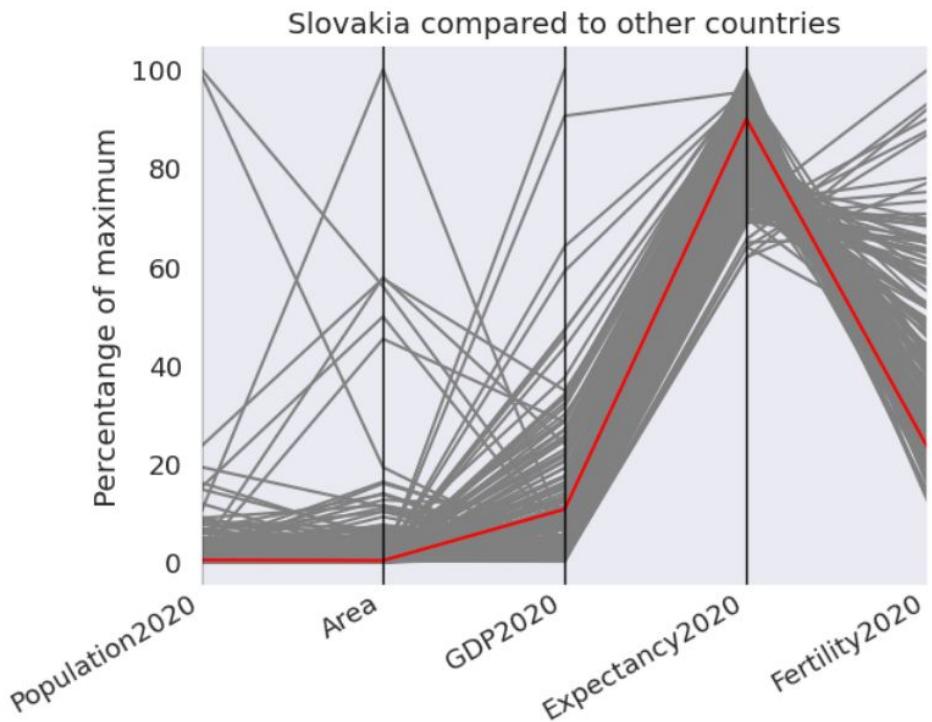
Parallel coordinates

Good for multidimensional numerical data

Each column one dimension

Here scaled as % of maximum value

Hard to see individual lines, but can show trends, compare groups shown in color or selected data point vs others

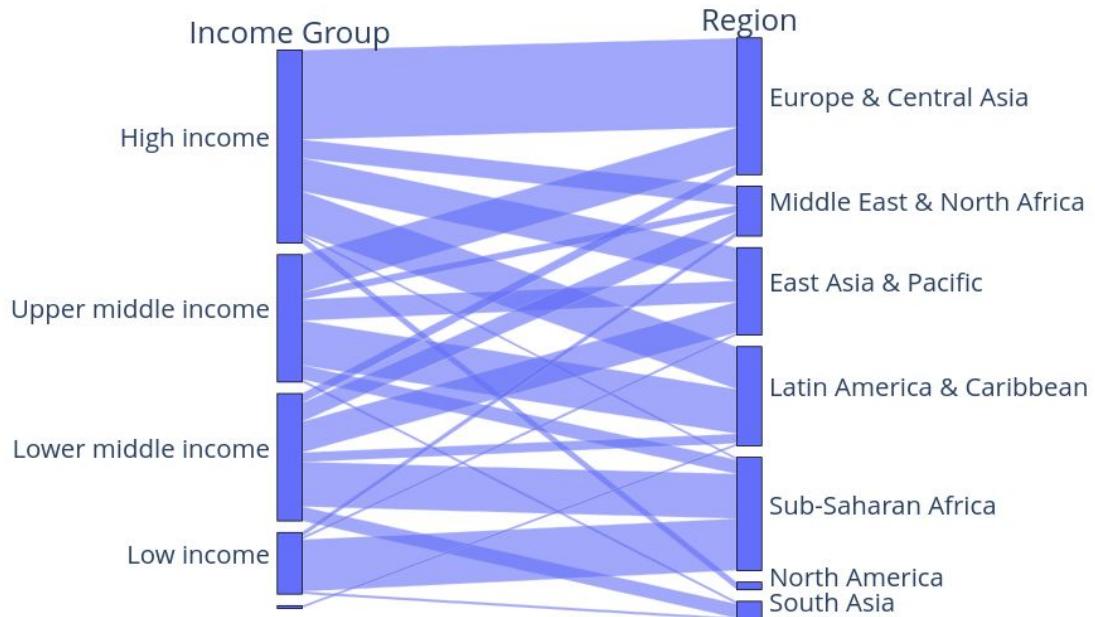


Parallel categories

Good for multidimensional categorical data

Each column one dimension

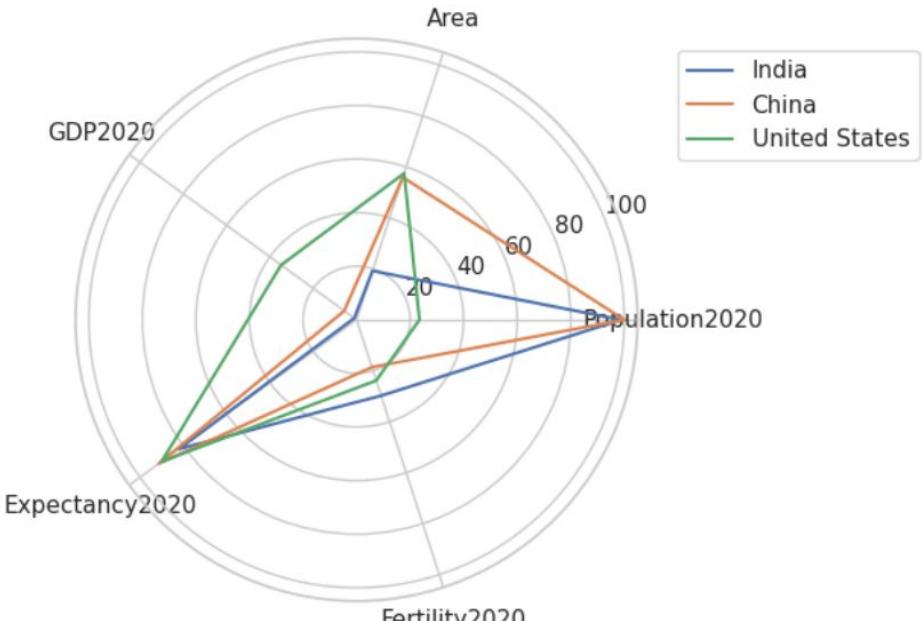
The widths of ribbons correspond to the number of countries



Radar chart (radarový graf)

Hard-to-read version of parallel coordinates

Perhaps some justification in cyclical domains, such as average temperature in months of a year



Now some Python

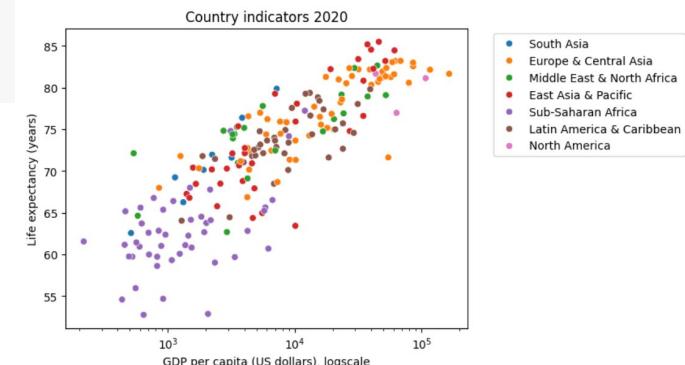
Overview of libraries

- Matplotlib
- Seaborn: an extension of Matplotlib, convenient for many types of plots
- Plotly: basic usage similar to Seaborn, plots interactive by default

Part of the main table countries

| | IS03 | Region | Income Group | Population2000 | Population2010 | Population2020 | Area | GDP2000 | GDP2010 |
|----------------|------|----------------------------|---------------------|----------------|----------------|----------------|-----------|--------------|--------------|
| Country | | | | | | | | | |
| Afghanistan | AFG | South Asia | Low income | 19542983.0 | 28189672.0 | 38972231.0 | 652860.0 | NaN | 562.499219 |
| Albania | ALB | Europe & Central Asia | Upper middle income | 3089026.0 | 2913021.0 | 2837849.0 | 28750.0 | 1126.683340 | 4094.349686 |
| Algeria | DZA | Middle East & North Africa | Lower middle income | 30774621.0 | 35856344.0 | 43451666.0 | 2381741.0 | 1780.376063 | 4495.921476 |
| American Samoa | ASM | East Asia & Pacific | High income | 58229.0 | 54849.0 | 46189.0 | 200.0 | NaN | 10446.863206 |
| Andorra | AND | Europe & Central Asia | High income | 66097.0 | 71519.0 | 77699.0 | 470.0 | 21620.465102 | 48237.890541 |

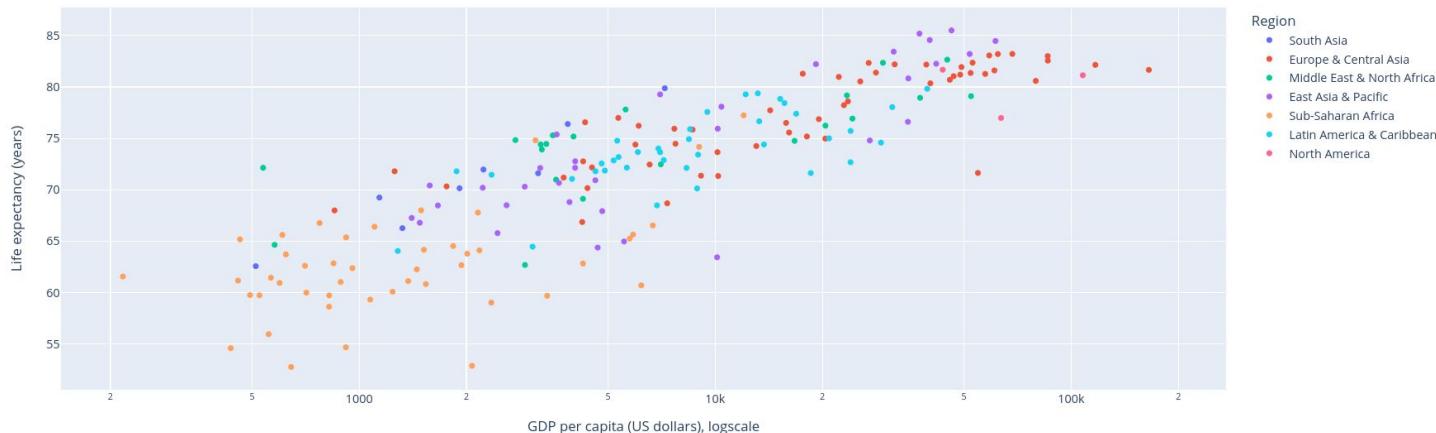
```
# create plot using Seaborn
axes = sns.scatterplot(data=countries, x='GDP2020', y='Expectancy2020',
                       hue='Region')
# set plot properties using methods from Matplotlib
axes.set_xlabel('GDP per capita (US dollars), logscale')
axes.set_ylabel('Life expectancy (years)')
axes.set_title('Country indicators 2020')
axes.semilogx()
# place legend outside the plot:
axes.legend(bbox_to_anchor=(1.05, 1), loc=2)
pass
```



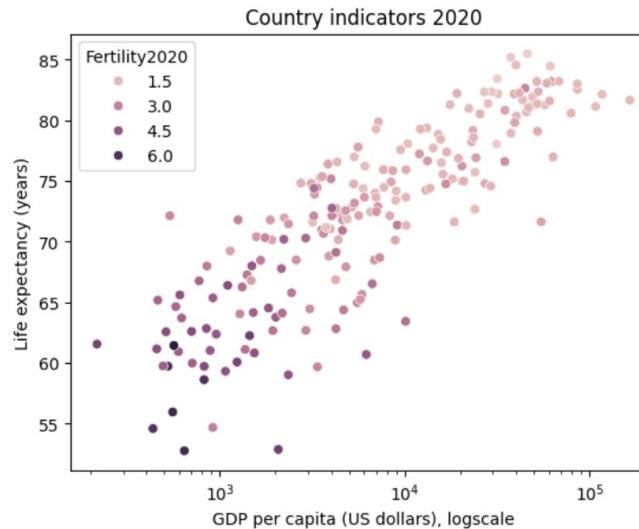
```

# The same plot in Plotly
# We want to use index (country name) in the figure for tooltip info
# therefore we create a temporary table with column Country instead of index
temp_table = countries.reset_index()
# how to rename automated axis labels
fig_labels = {'GDP2020':'GDP per capita (US dollars), logscale',
              'Expectancy2020':'Life expectancy (years)'}
# create Plotly plot, add countryr name to tooltip data
fig = px.scatter(data_frame=temp_table,
                  x="GDP2020", y="Expectancy2020", color="Region",
                  hover_data=['Country'], log_x=True,
                  labels = fig_labels)
fig.show()

```



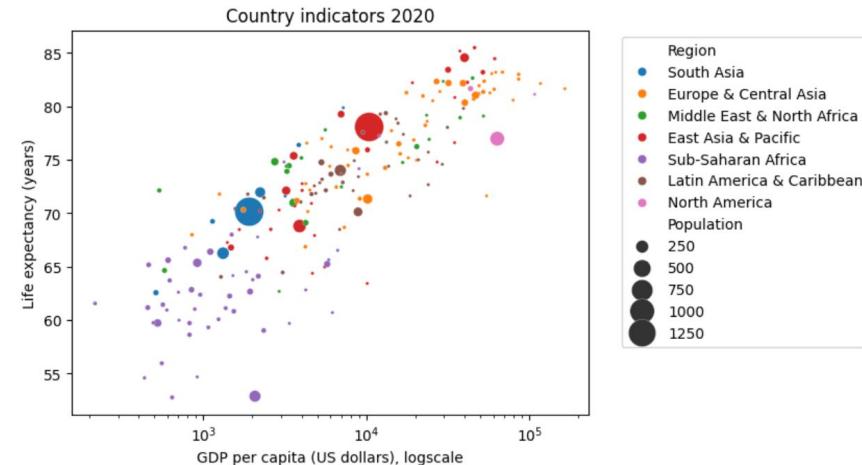
```
# Seaborn automatically detects if the column used as hue is categorical or numerical
axes = sns.scatterplot(data=countries, x='GDP2020', y='Expectancy2020',
                      hue='Fertility2020')
axes.set_xlabel('GDP per capita (US dollars), logscale')
axes.set_ylabel('Life expectancy (years)')
axes.set_title('Country indicators 2020')
axes.semilogx()
pass
```



```

# add a column representing population in millions to table countries
countries['Population'] = countries['Population2020'] / 1e6
# create the plot
# parameter sizes sets the minimum and maximum point size to be used
axes = sns.scatterplot(data=countries,
                        x='GDP2020', y='Expectancy2020', hue='Region',
                        size='Population', sizes=(5, 400))
# set titles, log axes and legend location as before

```

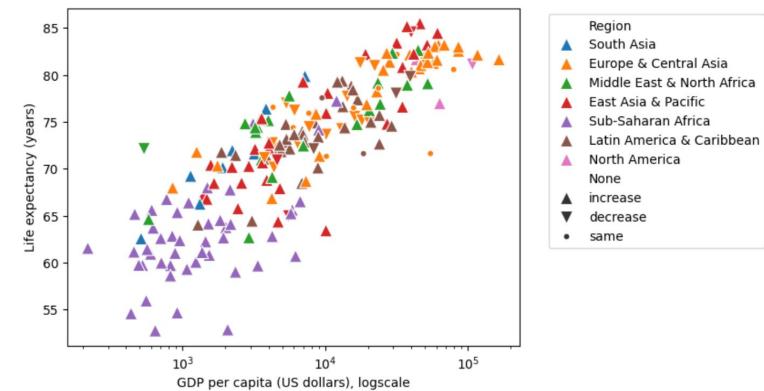


```

# compute relative differences in population between years 2010 and 2020
diff = (countries.Population2020 - countries.Population2010) / countries.Population2010
# new series with values 'increase', 'decrease' and 'same'
diff_class = diff.apply(lambda x : 'decrease' if x < -0.01
                        else 'increase' if x > 0.01 else 'same')

# create plot
# parameter s sets marker size
axes = sns.scatterplot(data=countries,
                        x='GDP2020', y='Expectancy2020', hue='Region',
                        style=diff_class, s=100,
                        markers={'increase': '^', 'decrease': 'v', 'same': '.'})

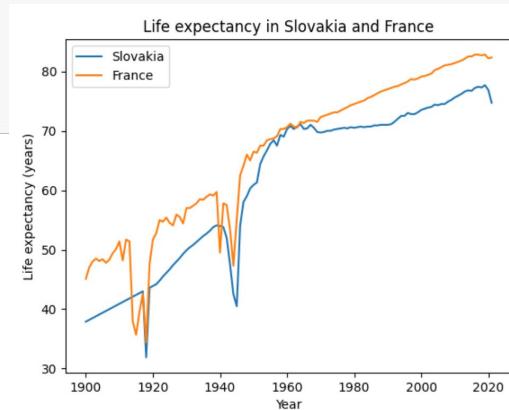
```



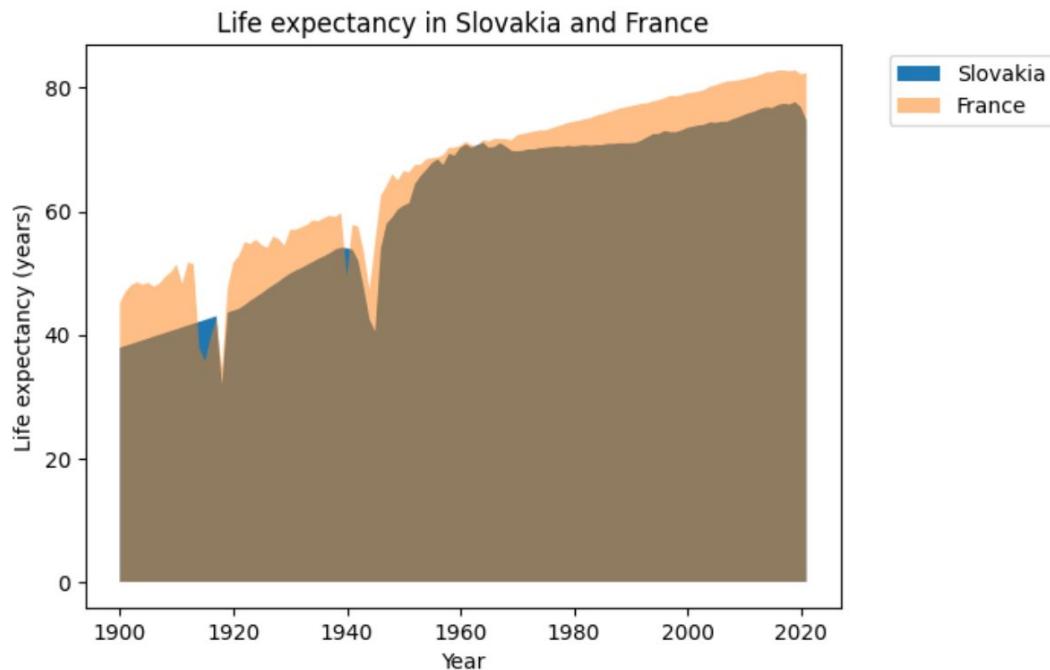
```
display(life_exp_years)
```

```
# list of numerical years from column names
years = [int(x) for x in life_exp_years.columns]

figure, axes = plt.subplots()
# plot two lines
axes.plot(years, life_exp_years.loc['Slovak Republic'], label='Slovakia')
axes.plot(years, life_exp_years.loc['France'], label='France')
# plot settings
axes.set_xlabel('Year')
axes.set_ylabel('Life expectancy (years)')
axes.set_title('Life expectancy in Slovakia and France')
axes.legend()
pass
```



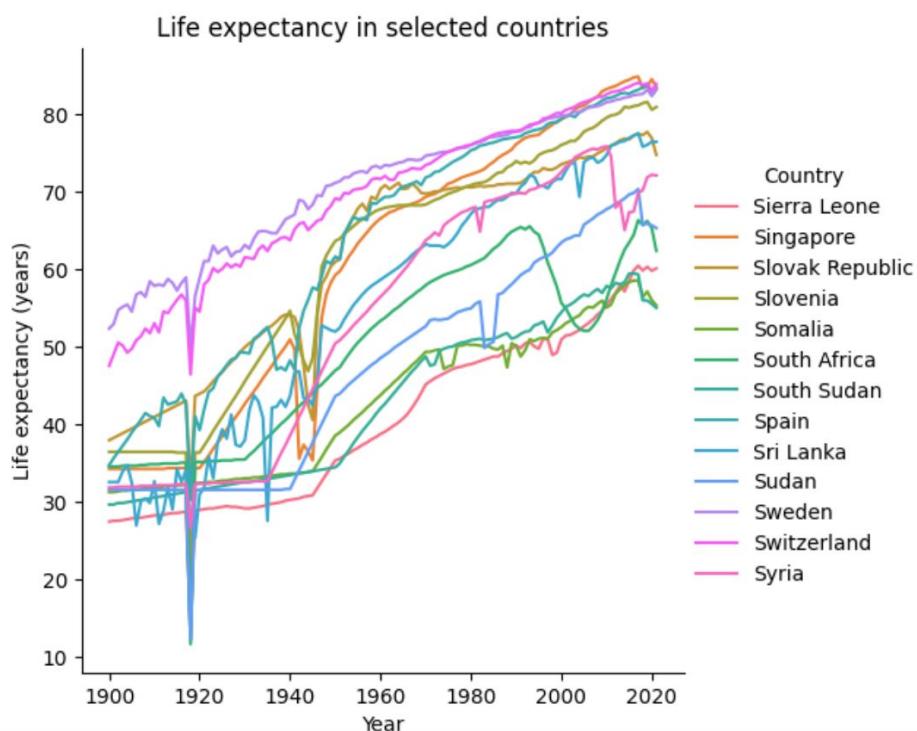
```
figure, axes = plt.subplots()  
# two filled areas, the second is semi-transparent  
axes.fill_between(years, 0, life_exp_years.loc['Slovak Republic'], label='Slovakia')  
axes.fill_between(years, 0, life_exp_years.loc['France'], label='France', alpha=0.5)  
# plot settings as before...
```



```
# Lines for many countries easy in Seaborn
# ... works better with long table
life_exp_sel_long = (
    life_exp_sel.reset_index()
    .melt(id_vars=['Country'])
    .rename(columns={'variable':'Year', 'value':'Expectancy'})
    .astype({'Year':'int32'})
)
display(life_exp_sel_long)
```

| | Country | Year | Expectancy |
|------|-----------------|------|------------|
| 0 | Sierra Leone | 1900 | 27.400000 |
| 1 | Singapore | 1900 | 34.200000 |
| 2 | Slovak Republic | 1900 | 37.900000 |
| 3 | Slovenia | 1900 | 36.400000 |
| 4 | Somalia | 1900 | 31.200000 |
| ... | ... | ... | ... |
| 1581 | Sri Lanka | 2021 | 76.399000 |
| 1582 | Sudan | 2021 | 65.267000 |
| 1583 | Sweden | 2021 | 83.156098 |
| 1584 | Switzerland | 2021 | 83.851220 |
| 1585 | Syria | 2021 | 72.063000 |

```
grid = sns.relplot(data=life_exp_sel_long, x='Year', y='Expectancy',
                    hue='Country', kind="line")
grid.set_axis_labels('Year', 'Life expectancy (years)')
grid.set(title='Life expectancy in selected countries')
```

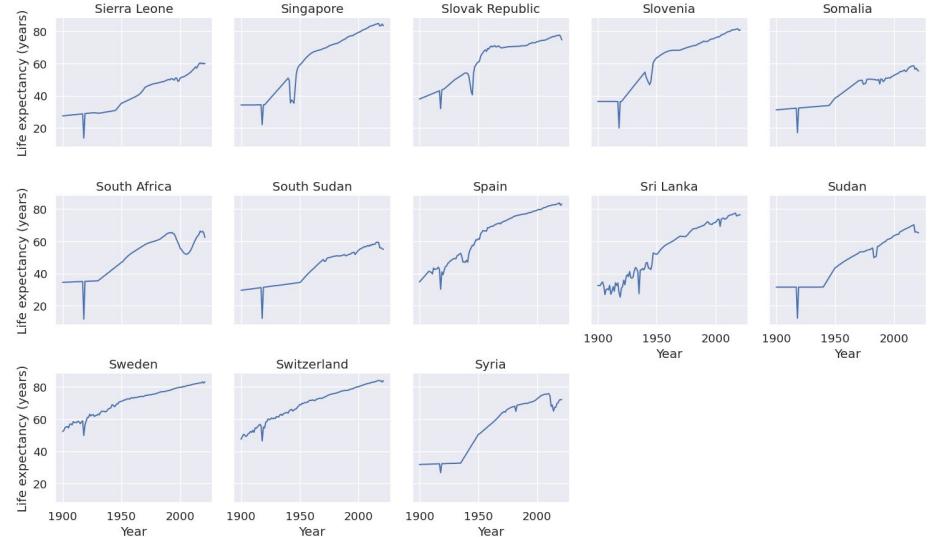


```

sns.set_theme(font_scale=1.2)
# create a grid of small multiple plots
# use col_wrap=5 columns
grid = sns.relplot(data=life_exp_sel_long,
                    x='Year', y='Expectancy', col='Country',
                    col_wrap=5, kind="line", height=3, aspect=1)

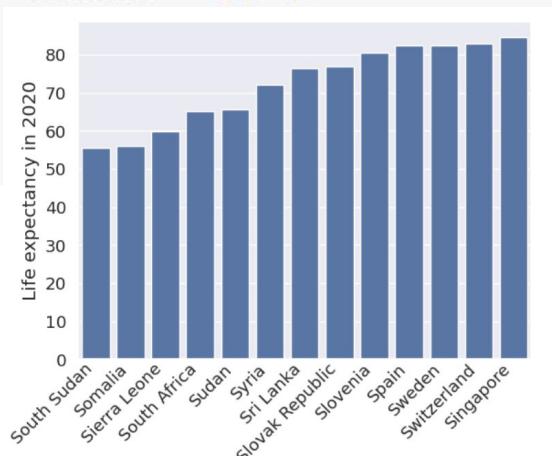
grid.set_axis_labels('Year', 'Life expectancy (years)')
grid.set_titles("{col_name}") # title of each plot will be country name

```



```
def rotate_bar_labels(axes, angle=45):
    """Auxiliary function for rotating bar plot labels by 45 degrees"""
    axes.tick_params(axis='x', labelrotation=angle, pad=-5)
    plt.setp(axes.get_xticklabels(), ha='right')
```

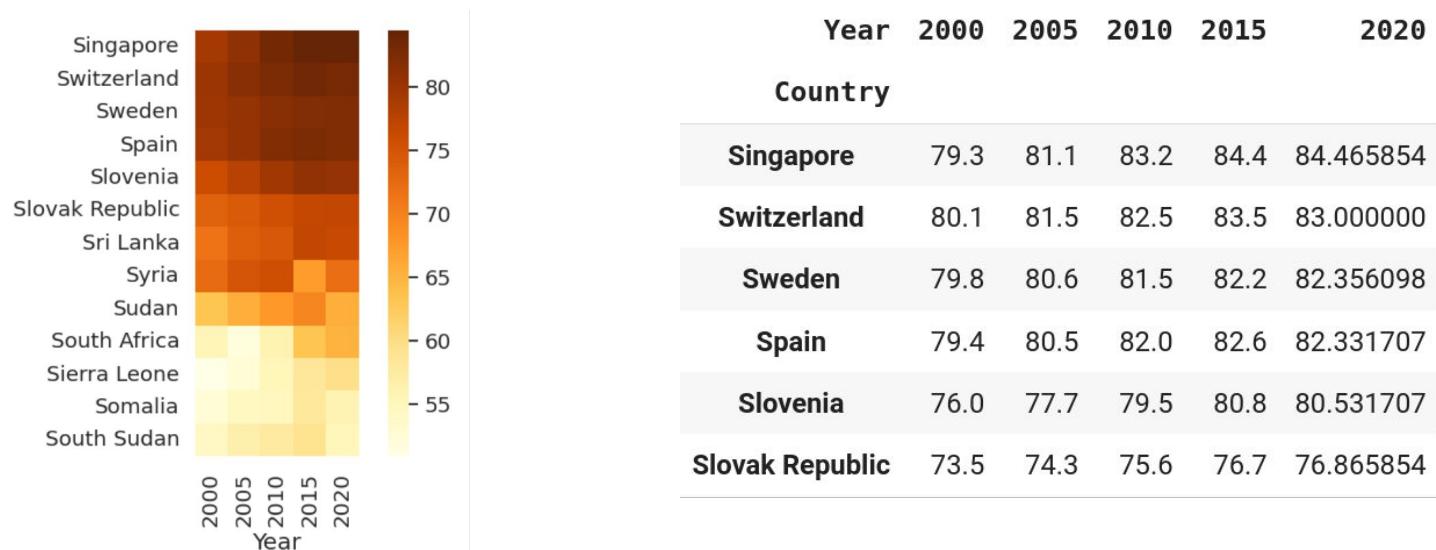
```
# sorting
life_exp_sel_2020_sorted = life_exp_sel_2020.sort_values('Expectancy')
# plotting
axes = sns.barplot(data=life_exp_sel_2020_sorted,
                     x='Country', y='Expectancy', color="C0")
axes.set_ylabel("Life expectancy in 2020")
axes.set_xlabel(None)
rotate_bar_labels(axes)
```



```

# set of years to be used
sel_years={2000, 2005, 2010, 2015, 2020}
# create desired wide table
life_exp_sel_wide = (life_exp_sel_long.query('Year in @sel_years')
                      .pivot(index='Country', columns='Year', values='Expectancy')
                      .sort_values(2020, ascending=False))
# show the table
display(life_exp_sel_wide)
axes = sns.heatmap(data=life_exp_sel_wide, square=True, cmap="YlOrBr")

```



1 Lecture 3b: Source code for plots from Lecture 3a + introduction to Seaborn and Plotly libraries

Data Visualization · 1-DAV-105

Lecture by Broňa Brejová

This notebook contains the source code for all the plots shown in the first part of the lecture. It also introduces two new plotting libraries: Seaborn and Plotly.

1.1 Seaborn library

- [Seaborn](#) library is an extension of Matplotlib.
- Seaborn is more convenient for many types of plots; we will use it for more complex scatter plots and line plots, for bar plots, strip plots, histograms and heatmaps.
- In Seaborn functions, a whole DataFrame can be added using option `data=`. DataFrame column names are then used as `x`, `y`, `hue` (color), `col` (one of subfigures).
- Seaborn creates Matplotlib objects (e.g. figure, axes) which can be then modified using Matplotlib methods.
- The first example of this library is in section [Categorical variable via color](#)

1.2 Plotly library for interactive plots

- Another popular library is [Plotly](#).
- It provides some additional plot types and all plots are interactive.
- For example, in the [scatter plot](#), we can find information about each dot by hovering a mouse over it.
- We can also zoom into parts of the plot by selecting a rectangle.
- A menu with additional options appears in the top right corner of the plot.
- Plotly is also used the first time in section [Categorical variable via color](#).

1.3 Used libraries

```
[1]: import numpy as np
import pandas as pd
from IPython.display import Markdown
import matplotlib.pyplot as plt
import seaborn as sns
import plotly.express as px
```

1.4 Importing World Bank data

Country indicators from World Bank, <https://databank.worldbank.org/home> under CC BY 4.0 license.

Country population, surface area in km squared, GDP per capita (current US\$), life expectancy at birth (years), fertility rate (births per woman); in years 2000, 2010, 2020.

```
[2]: url = 'https://bbrejova.github.io/viz/data/World_bank.csv'
countries = pd.read_csv(url).set_index('Country')
display(countries)
```

| | IS03 | Region | Income Group | \ |
|--------------------|----------------|----------------------------|---------------------|------------------|
| Country | | | | |
| Afghanistan | AFG | South Asia | Low income | |
| Albania | ALB | Europe & Central Asia | Upper middle income | |
| Algeria | DZA | Middle East & North Africa | Lower middle income | |
| American Samoa | ASM | East Asia & Pacific | High income | |
| Andorra | AND | Europe & Central Asia | High income | |
| ... | ... | ... | ... | |
| Virgin Islands | VIR | Latin America & Caribbean | High income | |
| West Bank and Gaza | PSE | Middle East & North Africa | Upper middle income | |
| Yemen | YEM | Middle East & North Africa | Low income | |
| Zambia | ZMB | Sub-Saharan Africa | Lower middle income | |
| Zimbabwe | ZWE | Sub-Saharan Africa | Lower middle income | |
| | Population2000 | Population2010 | Population2020 | Area \ |
| Country | | | | |
| Afghanistan | 19542983.0 | 28189672.0 | 38972231.0 | 652860.0 |
| Albania | 3089026.0 | 2913021.0 | 2837849.0 | 28750.0 |
| Algeria | 30774621.0 | 35856344.0 | 43451666.0 | 2381741.0 |
| American Samoa | 58229.0 | 54849.0 | 46189.0 | 200.0 |
| Andorra | 66097.0 | 71519.0 | 77699.0 | 470.0 |
| ... | ... | ... | ... | ... |
| Virgin Islands | 108642.0 | 108356.0 | 106291.0 | 350.0 |
| West Bank and Gaza | 2922153.0 | 3786161.0 | 4803269.0 | 6020.0 |
| Yemen | 18628701.0 | 24743945.0 | 32284046.0 | 527970.0 |
| Zambia | 9891135.0 | 13792087.0 | 18927715.0 | 752610.0 |
| Zimbabwe | 11834676.0 | 12839770.0 | 15669667.0 | 390760.0 |
| | GDP2000 | GDP2010 | GDP2020 | Expectancy2000 \ |
| Country | | | | |
| Afghanistan | NaN | 562.499219 | 512.055098 | 55.298000 |
| Albania | 1126.683340 | 4094.349686 | 5343.037704 | 75.404000 |
| Algeria | 1780.376063 | 4495.921476 | 3354.153164 | 70.478000 |
| American Samoa | NaN | 10446.863206 | 15609.777220 | NaN |
| Andorra | 21620.465102 | 48237.890541 | 37207.238871 | NaN |
| ... | ... | ... | ... | ... |
| Virgin Islands | NaN | 39905.128418 | 39411.045254 | 76.619512 |
| West Bank and Gaza | 1476.171850 | 2557.075624 | 3233.568638 | 70.388000 |
| Yemen | 519.591639 | 1249.063085 | 578.512010 | 62.588000 |
| Zambia | 364.026145 | 1469.361450 | 956.831729 | 45.231000 |
| Zimbabwe | 565.284390 | 937.840340 | 1372.696674 | 44.686000 |
| | Expectancy2010 | Expectancy2020 | Fertility2000 | \ |

| Country | Fertility2010 | Fertility2020 | |
|--------------------|---------------|---------------|-------|
| Afghanistan | 60.851000 | 62.575000 | 7.534 |
| Albania | 77.936000 | 76.989000 | 2.231 |
| Algeria | 73.808000 | 74.453000 | 2.566 |
| American Samoa | NaN | NaN | NaN |
| Andorra | NaN | NaN | NaN |
| ... | ... | ... | ... |
| Virgin Islands | 77.865854 | 79.819512 | 2.060 |
| West Bank and Gaza | 73.004000 | 74.403000 | 5.443 |
| Yemen | 67.280000 | 64.650000 | 6.318 |
| Zambia | 56.799000 | 62.380000 | 5.926 |
| Zimbabwe | 50.652000 | 61.124000 | 3.974 |

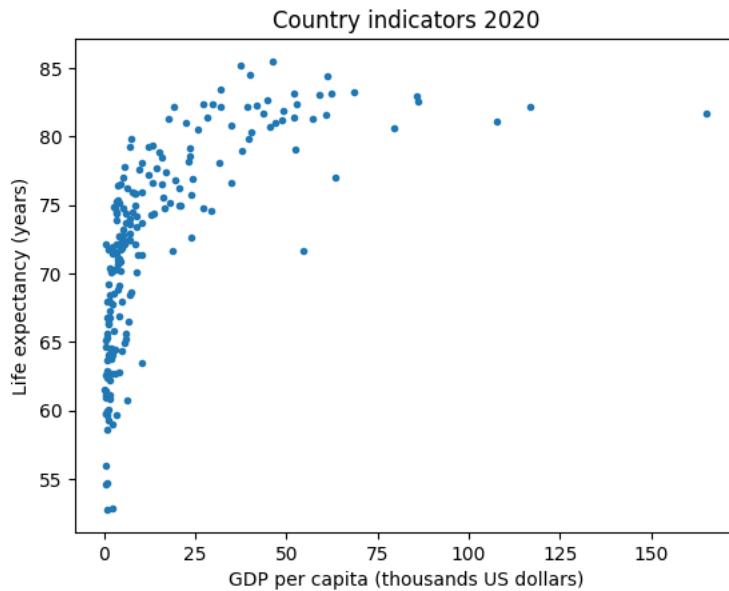
| Country | Fertility2010 | Fertility2020 |
|--------------------|---------------|---------------|
| Afghanistan | 6.099 | 4.750 |
| Albania | 1.656 | 1.400 |
| Algeria | 2.843 | 2.942 |
| American Samoa | NaN | NaN |
| Andorra | 1.270 | NaN |
| ... | ... | ... |
| Virgin Islands | 2.300 | 2.030 |
| West Bank and Gaza | 4.383 | 3.570 |
| Yemen | 4.855 | 3.886 |
| Zambia | 5.363 | 4.379 |
| Zimbabwe | 4.025 | 3.545 |

[217 rows x 16 columns]

1.5 A simple scatterplot

To create a simple scatterplot, commands from the previous lectures suffice. Note that we divide GDP by 1000 and add this information to the axis title. This makes the axis easier to read.

```
[3]: figure, axes = plt.subplots()
axes.plot(countries.GDP2020 / 1000, countries.Expectancy2020, '.')
axes.set_xlabel('GDP per capita (thousands US dollars)')
axes.set_ylabel('Life expectancy (years)')
axes.set_title('Country indicators 2020')
pass
```



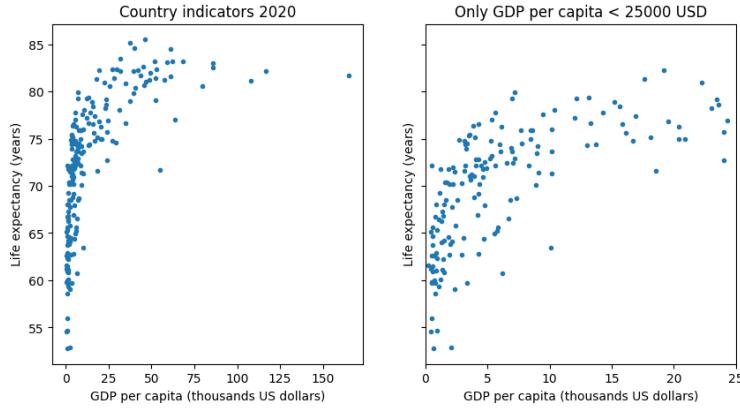
1.6 Zooming in

Limits on x axis are set using `set_xlim` method in order to zoom in on countries with lower GDP.

```
[4]: # create two subplots
figure, axes = plt.subplots(1, 2, figsize=(10, 5), sharey=True)

# the left subplot - full range of data
axes[0].plot(countries.GDP2020 / 1000, countries.Expectancy2020, '.')
axes[0].set_xlabel('GDP per capita (thousands US dollars)')
axes[0].set_ylabel('Life expectancy (years)')
axes[0].set_title('Country indicators 2020')

# the right subplot - smaller values of GDP
axes[1].plot(countries.GDP2020 / 1000, countries.Expectancy2020, '.')
axes[1].set_xlabel('GDP per capita (thousands US dollars)')
axes[1].set_ylabel('Life expectancy (years)')
axes[1].set_title('Only GDP per capita < 25000 USD')
axes[1].set_xlim(0, 25)
pass
```



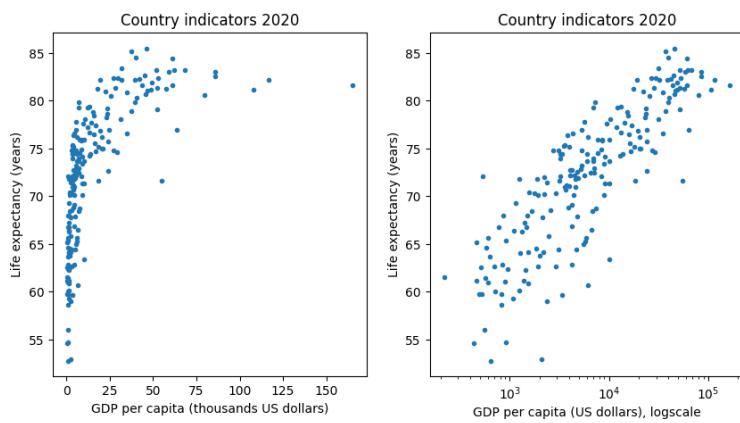
1.7 Log-scale plot

In this plot, the log-scale on the x-axis is switched on by `semilogx` method; similarly there is `semilogy` for the y-axis and `loglog` for both axes.

```
[5]: figure, axes = plt.subplots(1, 2, figsize=(10, 5))

# linear scale plot
axes[0].plot(countries.GDP2020 / 1000, countries.Expectancy2020, '.')
axes[0].set_xlabel('GDP per capita (thousands US dollars)')
axes[0].set_ylabel('Life expectancy (years)')
axes[0].set_title('Country indicators 2020')

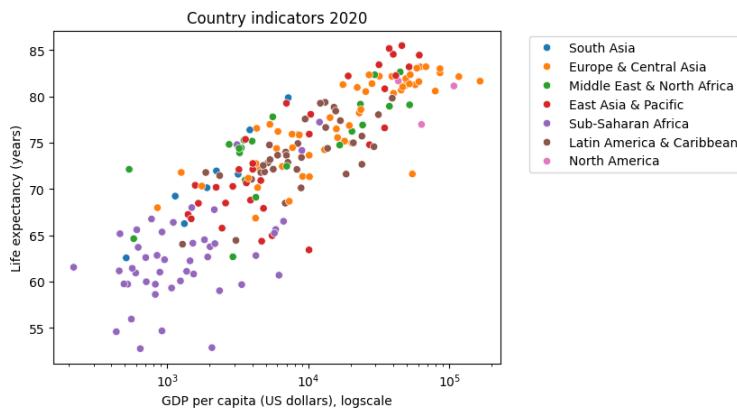
# log scale plot
axes[1].plot(countries.GDP2020, countries.Expectancy2020, '.')
axes[1].set_xlabel('GDP per capita (US dollars), logscale')
axes[1].set_ylabel('Life expectancy (years)')
axes[1].set_title('Country indicators 2020')
axes[1].semilogx()
pass
```



1.8 Categorical variable via color

Here we color countries by their region. Seaborn function `scatterplot` can do this easily via `hue` parameter. This function returns Matplotlib axes which can be then modified by familiar methods such as `set_xlabel`.

```
[6]: # create plot using Seaborn
axes = sns.scatterplot(data=countries, x='GDP2020', y='Expectancy2020',
                       hue='Region')
# set plot properties using methods from Matplotlib
axes.set_xlabel('GDP per capita (US dollars), logscale')
axes.set_ylabel('Life expectancy (years)')
axes.set_title('Country indicators 2020')
axes.semilogx()
# place legend outside the plot:
axes.legend(bbox_to_anchor=(1.05, 1), loc=2)
pass
```



- The same plot in Plotly is even easier and interactive.
- Both Plotly and Seaborn automatically label axes with column names, such as `GDP2020`.
- Here we override such automated labels with longer ones using a dictionary `fig_labels`.

```
[7]: # we want to use index (country name) in the figure for tooltip info
# therefore we create a temporary table with column Country instead of index
temp_table = countries.reset_index()
# how to rename automated axis labels
fig_labels = {'GDP2020':'GDP per capita (US dollars), logscale',
              'Expectancy2020':'Life expectancy (years)'}
# create Plotly plot, add country name to tooltip data
fig = px.scatter(data_frame=temp_table,
                  x="GDP2020", y="Expectancy2020", color="Region",
```

```

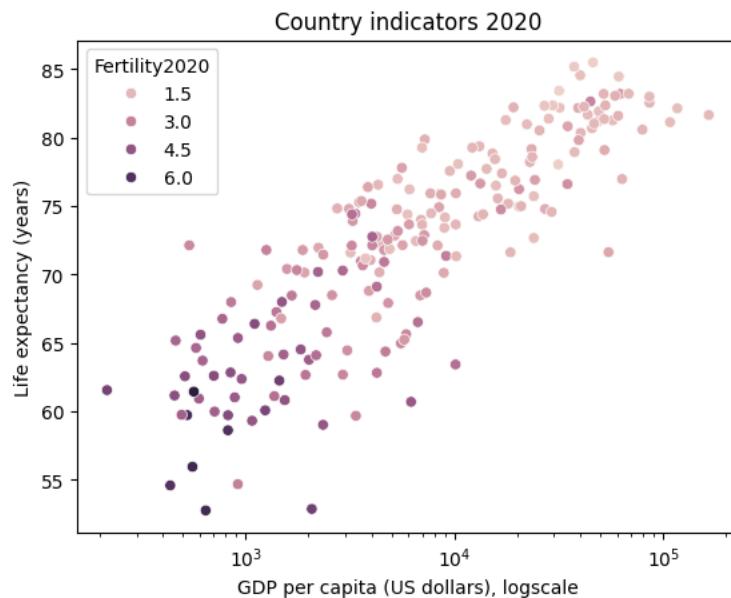
        hover_data=['Country'], log_x=True,
        labels = fig_labels)
fig.show()

```

1.9 Numerical variable via color

Seaborn automatically detects if the column used as `hue` is a categorical or numerical variable. In the previous graph, regions were used as `hue` and Seaborn chose a color palette with a different color for each category. Here we have a numerical variable so a continuous palette with different shades of pink and purple is used by default. We will discuss color palettes later in the course.

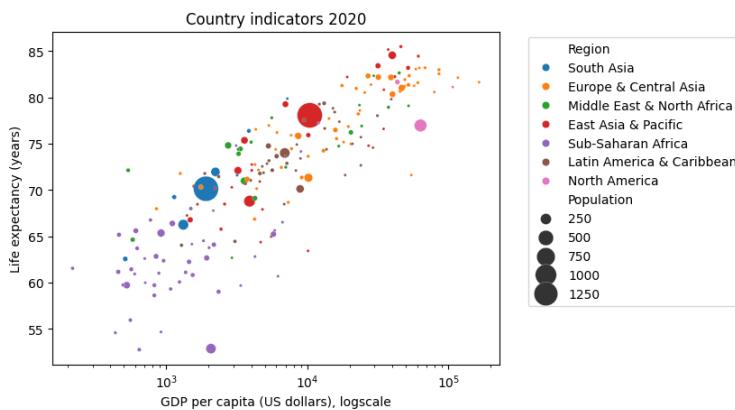
```
[8]: axes = sns.scatterplot(data=countries, x='GDP2020', y='Expectancy2020',
                           hue='Fertility2020')
axes.set_xlabel('GDP per capita (US dollars), logscale')
axes.set_ylabel('Life expectancy (years)')
axes.set_title('Country indicators 2020')
axes.semilogx()
pass
```



1.10 Numerical variable as point size

We will now use the population of each country as the size of each point (also called bubble), and we will color countries by regions. Sizing points according to the values in a specified table column is again simple to do in Seaborn using parameter `size` in `sns.scatterplot`. Parameter `sizes` sets the minimum and maximum point size to be used. For simplicity, population in millions is added as a new column to `countries`.

```
[9]: # add a column representing population in millions to table countries
countries['Population'] = countries['Population2020'] / 1e6
# create the plot
axes = sns.scatterplot(data=countries,
                        x='GDP2020', y='Expectancy2020', hue='Region',
                        size='Population',
                        sizes=(5, 400))
# set various plot properties
axes.set_xlabel('GDP per capita (US dollars), logscale')
axes.set_ylabel('Life expectancy (years)')
axes.set_title('Country indicators 2020')
axes.semilogx()
axes.legend(bbox_to_anchor=(1.05, 1), loc=2)
pass
```



1.11 Categorical variable as marker type

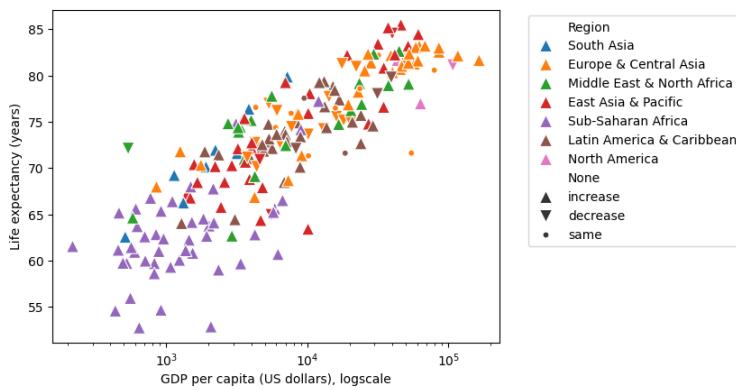
- We add a new column named `Population_change` with categories `increase`, `decrease` and `same` depending on how the population of a country changed between 2010 and 2020. Category `same` is applied to countries with population change less than 1% in either direction.
- This column is created using `apply` command, which applies a function (here a `lambda expression`) to `diff` Series containing relative change in population.
- This column is then used as argument `style` in `sns.scatterplot`. Size of markers is set to 100 (more than default) by argument `s`. Particular markers are selected by `markers` argument.
- Note that in the `scatterplot` we use both columns of `countries` table and separate Series.

```
[10]: # compute relative differences in population between years 2010 and 2020
diff = (countries.Population2020 - countries.Population2010) / countries.Population2010
# new series with values 'increase', 'decrease' and 'same'
diff_class = diff.apply(lambda x : 'decrease' if x < -0.01
                        else 'increase' if x > 0.01 else 'same')
```

```

# create plot
axes = sns.scatterplot(data=countries,
                        x='GDP2020', y='Expectancy2020', hue='Region',
                        style=diff_class, s=100,
                        markers={'increase': '^', 'decrease': 'v', 'same': '.'})
# plot settings
axes.semilogx()
axes.set_xlabel('GDP per capita (US dollars), logscale')
axes.set_ylabel('Life expectancy (years)')
axes.legend(bbox_to_anchor=(1.05, 1), loc=2)
pass

```



1.12 Importing Gapminder life expectancy

We import life expectancy data provided free by the [Gapminder foundation](#) under the CC-BY license. The data set gives for each year and each country an estimate of how many years newborn babies would live on average if the trends in mortality of different age groups that were prevailing in the year of their birth would prevail through their entire life.

```
[11]: url="https://bbrejova.github.io/viz/data/life_expectancy_years.csv"
life_exp = pd.read_csv(url, index_col=0)
life_exp_years = life_exp.iloc[:, 1:]
display(life_exp)
```

| Country | IS03 | 1900 | 1901 | 1902 | 1903 | 1904 | 1905 | 1906 | 1907 | \ |
|---------------------|------|------|------|------|------|------|------|------|------|---|
| Afghanistan | AFG | 29.4 | 29.5 | 29.5 | 29.6 | 29.7 | 29.7 | 29.8 | 29.9 | |
| Albania | ALB | 35.4 | 35.4 | 35.4 | 35.4 | 35.4 | 35.4 | 35.4 | 35.4 | |
| Algeria | DZA | 30.2 | 30.3 | 30.4 | 31.4 | 25.4 | 28.1 | 29.6 | 29.5 | |
| Angola | AGO | 29.0 | 29.1 | 29.2 | 29.3 | 29.3 | 29.4 | 29.4 | 29.5 | |
| Antigua and Barbuda | ATG | 33.8 | 33.8 | 33.8 | 33.8 | 33.8 | 33.8 | 33.8 | 33.8 | |
| ... | ... | ... | ... | ... | ... | ... | ... | ... | ... | |
| Venezuela | VEN | 32.4 | 32.4 | 32.4 | 32.4 | 32.4 | 32.4 | 32.5 | 32.5 | |
| Vietnam | VNM | 31.2 | 31.1 | 31.1 | 31.1 | 31.1 | 31.0 | 31.0 | 31.0 | |

| | | | | | | | | | |
|---------------------|-----|--------|--------|--------|------|------|------|------|--------|
| Yemen | YEM | 23.5 | 23.5 | 23.5 | 23.5 | 23.5 | 23.6 | 23.6 | 23.6 |
| Zambia | ZMB | 33.6 | 33.6 | 33.6 | 33.7 | 33.7 | 33.8 | 33.8 | 33.8 |
| Zimbabwe | ZWE | 34.1 | 34.1 | 34.1 | 34.1 | 34.1 | 34.1 | 34.1 | 34.1 |
| | | 1908 | ... | 2012 | 2013 | 2014 | 2015 | 2016 | 2017 |
| Country | | | ... | | | | | | |
| Afghanistan | | 29.9 | ... | 60.8 | 61.3 | 61.2 | 61.2 | 61.2 | 63.4 |
| Albania | | 35.4 | ... | 77.8 | 77.9 | 77.9 | 78.0 | 78.1 | 78.2 |
| Algeria | | 29.5 | ... | 76.8 | 76.9 | 77.0 | 77.1 | 77.4 | 77.7 |
| Angola | | 29.6 | ... | 61.3 | 61.9 | 62.8 | 63.3 | 63.8 | 64.2 |
| Antigua and Barbuda | | 33.8 | ... | 76.7 | 76.8 | 76.8 | 76.9 | 77.0 | 78.511 |
| ... | | ... | ... | ... | ... | ... | ... | ... | ... |
| Venezuela | | 32.5 | ... | 75.2 | 75.2 | 75.0 | 75.0 | 75.3 | 75.3 |
| Vietnam | | 30.9 | ... | 73.8 | 74.0 | 74.1 | 74.3 | 74.4 | 74.5 |
| Yemen | | 23.6 | ... | 68.3 | 68.9 | 69.0 | 68.6 | 68.1 | 68.1 |
| Zambia | | 33.9 | ... | 58.8 | 60.0 | 61.1 | 62.0 | 62.8 | 63.2 |
| Zimbabwe | | 34.2 | ... | 54.9 | 56.8 | 58.5 | 59.6 | 60.5 | 61.4 |
| | | | 2019 | 2020 | 2021 | | | | |
| Country | | | | | | | | | |
| Afghanistan | | 63.565 | 62.575 | 61.982 | | | | | |
| Albania | | 79.282 | 76.989 | 76.463 | | | | | |
| Algeria | | 76.474 | 74.453 | 76.377 | | | | | |
| Angola | | 62.448 | 62.261 | 61.643 | | | | | |
| Antigua and Barbuda | | 78.691 | 78.841 | 78.497 | | | | | |
| ... | | ... | ... | ... | | | | | |
| Venezuela | | 72.161 | 71.095 | 70.554 | | | | | |
| Vietnam | | 74.093 | 75.378 | 73.618 | | | | | |
| Yemen | | 65.092 | 64.650 | 63.753 | | | | | |
| Zambia | | 62.793 | 62.380 | 61.223 | | | | | |
| Zimbabwe | | 61.292 | 61.124 | 59.253 | | | | | |

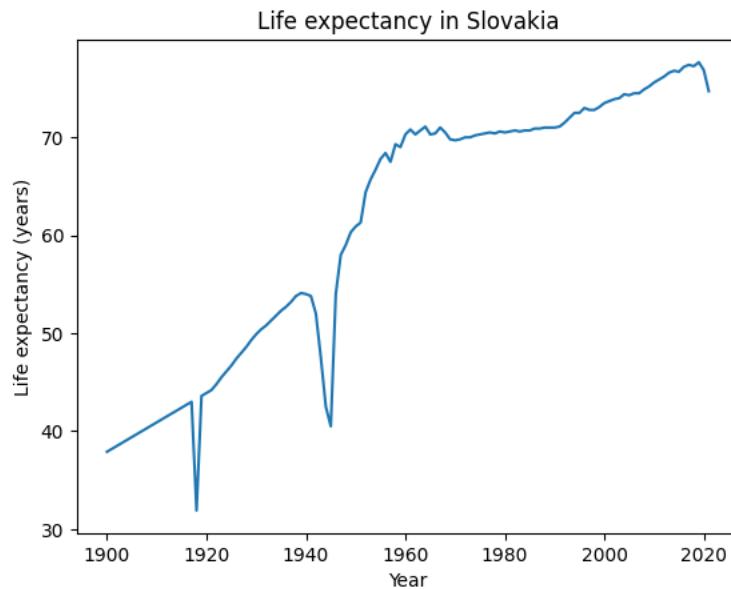
[184 rows x 123 columns]

1.13 A simple line graph

Here we use `plot` from `matplotlib` to plot life expectancy over the years for Slovakia. Years are column names which need to be converted from string to integer using Python list comprehension.

```
[12]: # list of numerical years from column names
years = [int(x) for x in life_exp_years.columns]
# simple plot for one row of the table
figure, axes = plt.subplots()
axes.plot(years, life_exp_years.loc['Slovak Republic'])
# plot settings
axes.set_xlabel('Year')
axes.set_ylabel('Life expectancy (years)')
axes.set_title('Life expectancy in Slovakia')
```

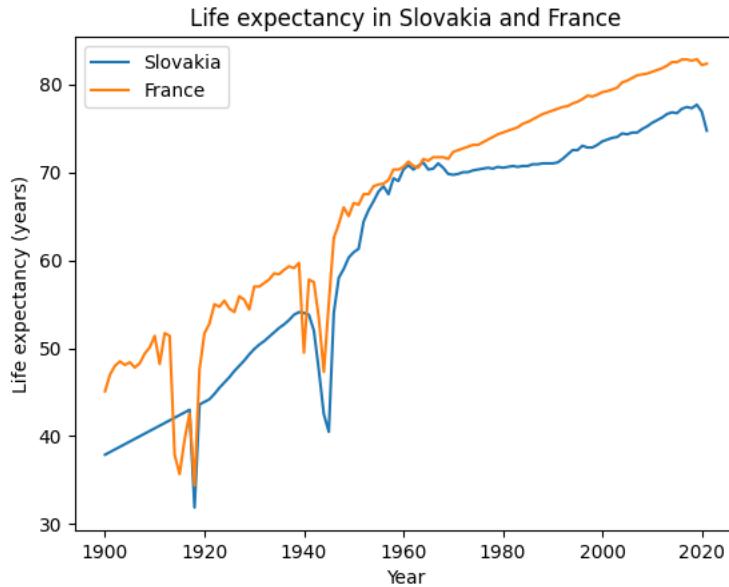
```
pass
```



1.14 A line graph with multiple lines

Here we plot two lines, each by a separate call to `plot`. Each line has a label to show in the legend.

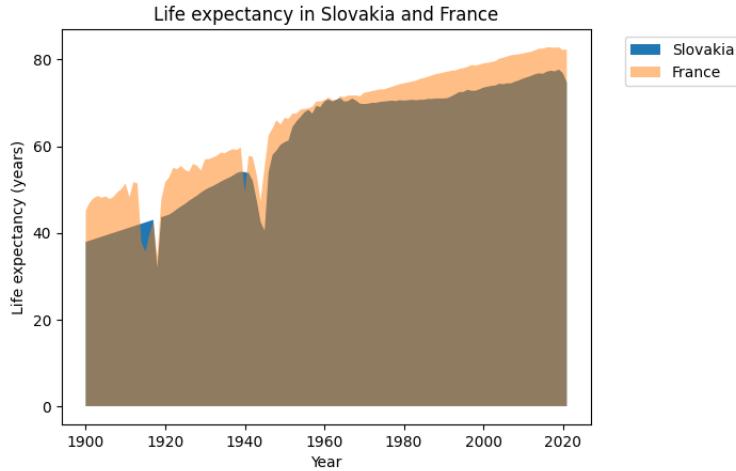
```
[13]: figure, axes = plt.subplots()
# plot two lines
axes.plot(years, life_exp_years.loc['Slovak Republic'], label='Slovakia')
axes.plot(years, life_exp_years.loc['France'], label='France')
# plot settings
axes.set_xlabel('Year')
axes.set_ylabel('Life expectancy (years)')
axes.set_title('Life expectancy in Slovakia and France')
axes.legend()
pass
```



1.15 Area graph

Here we fill in the area between x-axis (value 0) and a table row using `fill_between` method. France is plotted on top and is set to be semi-transparent using `alpha=0.5`.

```
[14]: figure, axes = plt.subplots()
# two filled areas, the second is semi-transparent
axes.fill_between(years, 0, life_exp_years.loc['Slovak Republic'], label='Slovakia')
axes.fill_between(years, 0, life_exp_years.loc['France'], label='France', alpha=0.5)
# plot settings
axes.set_xlabel('Year')
axes.set_ylabel('Life expectancy (years)')
axes.set_title('Life expectancy in Slovakia and France')
axes.legend(bbox_to_anchor=(1.05, 1), loc=2)
pass
```



1.16 Line graph with many lines

- Here we want to plot lines for all countries alphabetically between Si and Sz and having at least million inhabitants.
- First we select such countries from `countries` to table `selection`.
- Using `intersection`, we get only countries from our selection that are also in Gapminder table (`life_exp`).
- Part of the Gapminder table for these countries is then stored as `life_exp_sel`.

```
[15]: selection = countries.query('Population2020 > 1e6 and Country >= "Si" and '
                                'Country <= "Sz"')
life_exp_iso3 = life_exp.reset_index().set_index('ISO3')
life_exp_sel = life_exp_iso3.loc[life_exp_iso3.index.intersection(selection.
                                'ISO3'), :].set_index('Country')
display(life_exp_sel)
```

| Country | 1900 | 1901 | 1902 | 1903 | 1904 | 1905 | 1906 | 1907 | 1908 | 1909 | \ |
|-----------------|------|------|------|------|------|------|------|------|------|------|------|
| Sierra Leone | 27.4 | 27.5 | 27.5 | 27.6 | 27.7 | 27.8 | 27.9 | 27.9 | 28.0 | 28.1 | |
| Singapore | 34.2 | 34.2 | 34.2 | 34.2 | 34.2 | 34.2 | 34.2 | 34.2 | 34.2 | 34.2 | 34.2 |
| Slovak Republic | 37.9 | 38.2 | 38.5 | 38.8 | 39.1 | 39.4 | 39.7 | 40.0 | 40.3 | 40.6 | |
| Slovenia | 36.4 | 36.4 | 36.4 | 36.4 | 36.4 | 36.4 | 36.4 | 36.4 | 36.4 | 36.4 | 36.4 |
| Somalia | 31.2 | 31.2 | 31.3 | 31.4 | 31.4 | 31.5 | 31.5 | 31.6 | 31.7 | 31.7 | |
| South Africa | 34.5 | 34.5 | 34.5 | 34.6 | 34.6 | 34.6 | 34.6 | 34.7 | 34.7 | 34.8 | |
| South Sudan | 29.6 | 29.6 | 29.8 | 29.8 | 29.9 | 30.0 | 30.1 | 30.2 | 30.3 | 30.4 | |
| Spain | 34.7 | 35.6 | 36.4 | 37.2 | 38.0 | 38.9 | 39.7 | 40.5 | 41.4 | 41.0 | |
| Sri Lanka | 32.5 | 32.5 | 32.5 | 33.9 | 34.7 | 32.4 | 26.9 | 30.0 | 30.4 | 29.8 | |
| Sudan | 31.5 | 31.5 | 31.5 | 31.5 | 31.5 | 31.5 | 31.5 | 31.5 | 31.5 | 31.5 | 31.5 |
| Sweden | 52.3 | 52.9 | 54.7 | 55.1 | 55.4 | 54.5 | 56.7 | 57.0 | 56.4 | 58.4 | |
| Switzerland | 47.5 | 49.0 | 50.5 | 50.1 | 49.2 | 49.7 | 50.8 | 51.3 | 52.3 | 51.7 | |
| Syria | 31.8 | 31.8 | 31.9 | 31.9 | 31.9 | 31.9 | 31.9 | 31.9 | 32.0 | 32.0 | 32.0 |

| | ... | 2012 | 2013 | 2014 | 2015 | 2016 | 2017 | 2018 | \ |
|-----------------|-----|-----------|-----------|------|-----------|------|------|-----------|---|
| Country | ... | | | | | | | | |
| Sierra Leone | ... | 56.9 | 57.9 | 57.1 | 58.5 | 59.8 | 60.4 | 59.796000 | |
| Singapore | ... | 83.6 | 83.9 | 84.2 | 84.4 | 84.7 | 84.8 | 83.297561 | |
| Slovak Republic | ... | 76.2 | 76.6 | 76.8 | 76.7 | 77.2 | 77.4 | 77.265854 | |
| Slovenia | ... | 79.9 | 80.2 | 80.9 | 80.8 | 81.0 | 81.1 | 81.378049 | |
| Somalia | ... | 56.8 | 57.4 | 57.9 | 58.3 | 58.5 | 58.5 | 56.375000 | |
| South Africa | ... | 59.5 | 61.1 | 62.5 | 63.4 | 64.4 | 66.3 | 65.674000 | |
| South Sudan | ... | 58.2 | 58.0 | 58.3 | 59.4 | 59.4 | 59.3 | 55.950000 | |
| Spain | ... | 82.3 | 82.6 | 82.7 | 82.6 | 82.9 | 83.1 | 83.431707 | |
| Sri Lanka | ... | 76.1 | 76.4 | 76.5 | 76.9 | 77.2 | 77.5 | 75.748000 | |
| Sudan | ... | 68.4 | 68.7 | 69.1 | 69.6 | 69.8 | 70.3 | 65.681000 | |
| Sweden | ... | 81.8 | 81.9 | 82.1 | 82.2 | 82.4 | 82.5 | 82.558537 | |
| Switzerland | ... | 82.9 | 83.0 | 83.3 | 83.5 | 83.8 | 84.0 | 83.753659 | |
| Syria | ... | 67.9 | 68.7 | 65.0 | 67.3 | 67.4 | 69.8 | 70.145000 | |
| | | 2019 | | 2020 | | 2021 | | | |
| Country | | | | | | | | | |
| Sierra Leone | | 60.255000 | 59.763000 | | 60.062000 | | | | |
| Singapore | | 83.595122 | 84.465854 | | 83.441463 | | | | |
| Slovak Republic | | 77.665854 | 76.865854 | | 74.714634 | | | | |
| Slovenia | | 81.529268 | 80.531707 | | 80.875610 | | | | |
| Somalia | | 57.078000 | 55.967000 | | 55.280000 | | | | |
| South Africa | | 66.175000 | 65.252000 | | 62.341000 | | | | |
| South Sudan | | 55.912000 | 55.480000 | | 54.975000 | | | | |
| Spain | | 83.831707 | 82.331707 | | 83.178049 | | | | |
| Sri Lanka | | 76.008000 | 76.393000 | | 76.399000 | | | | |
| Sudan | | 65.876000 | 65.614000 | | 65.267000 | | | | |
| Sweden | | 83.109756 | 82.356098 | | 83.156098 | | | | |
| Switzerland | | 83.904878 | 83.000000 | | 83.851220 | | | | |
| Syria | | 71.822000 | 72.140000 | | 72.063000 | | | | |

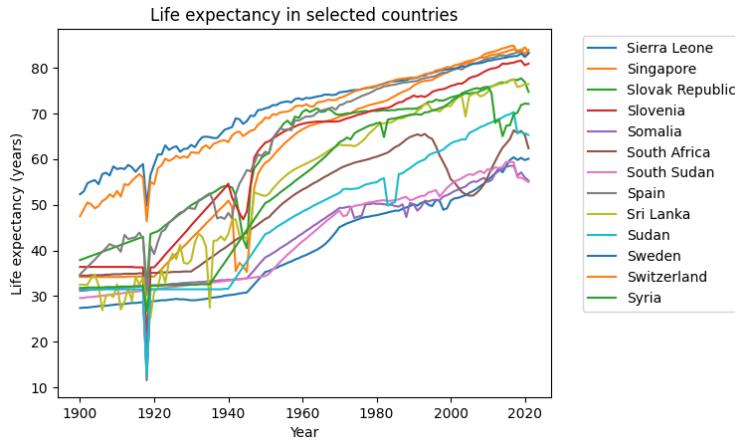
[13 rows x 122 columns]

- In Matplotlib, each country from `life_exp_sel` is plotted separately in a for-loop, similarly as for two countries above.
- Note that colors repeat because the default palette is not large enough.

```
[16]: figure, axes = plt.subplots()
# loop over countries
for country in life_exp_sel.index:
    axes.plot(years, life_exp_sel.loc[country], label=country)

# plot settings
axes.set_xlabel('Year')
axes.set_ylabel('Life expectancy (years)')
axes.set_title('Life expectancy in selected countries')
```

```
axes.legend(bbox_to_anchor=(1.05, 1), loc=2)
pass
```



- To use Seaborn for the same plot, it is better to change `life_exp_sel` table from wide to long format using `melt` method. Year is converted from strings to integers.
- This creates a table with columns Country, Year, Expectancy.

```
[17]: life_exp_sel_long = (
    life_exp_sel.reset_index()
    .melt(id_vars=['Country'])
    .rename(columns={'variable':'Year', 'value':'Expectancy'})
    .astype({'Year':'int32'})
)
display(life_exp_sel_long)
```

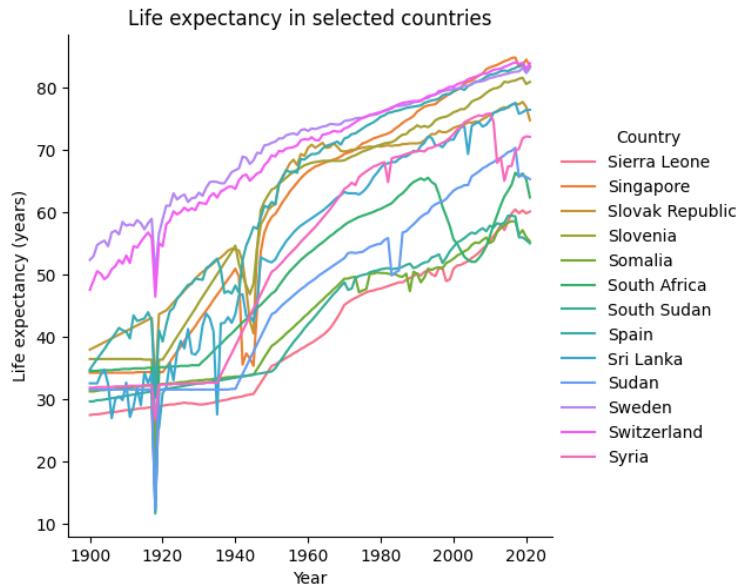
| | Country | Year | Expectancy |
|------|-----------------|------|------------|
| 0 | Sierra Leone | 1900 | 27.400000 |
| 1 | Singapore | 1900 | 34.200000 |
| 2 | Slovak Republic | 1900 | 37.900000 |
| 3 | Slovenia | 1900 | 36.400000 |
| 4 | Somalia | 1900 | 31.200000 |
| ... | ... | ... | ... |
| 1581 | Sri Lanka | 2021 | 76.399000 |
| 1582 | Sudan | 2021 | 65.267000 |
| 1583 | Sweden | 2021 | 83.156098 |
| 1584 | Switzerland | 2021 | 83.851220 |
| 1585 | Syria | 2021 | 72.063000 |

[1586 rows x 3 columns]

- Now we use Seaborn function `relplot`, setting parameters `x`, `y` and `hue` to column names in our long table and specifying that we want lineplot using `kind="line"`.

- The function returns `FacetGrid`, which potentially contains multiple axes, so we ned to use slightly different methods to set labels.
- Seaborn created a sufficiently large color palette but some colors are then hard to distinguish.

```
[18]: grid = sns.relplot(data=life_exp_sel_long, x='Year', y='Expectancy',
                      hue='Country', kind="line")
grid.set_axis_labels('Year', 'Life expectancy (years)')
grid.set(title='Life expectancy in selected countries')
pass
```

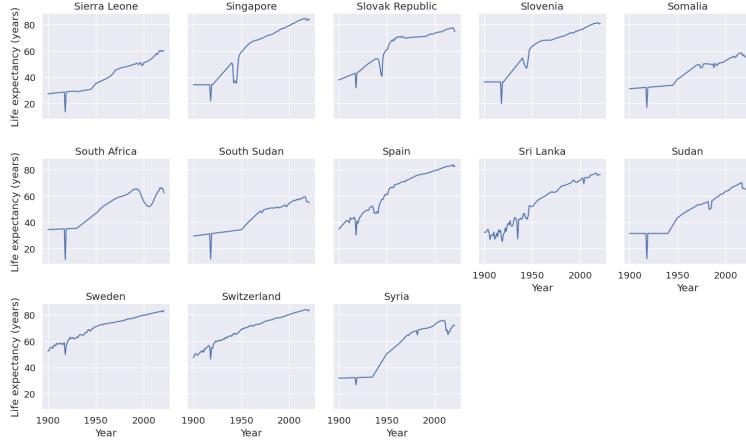


1.17 Small multiples

- Small multiples, with each country in our selection as a separate plot, is very easy to do in Seaborn from a long-format table using `relplot`, using column `Country` in option `col` which selects one of subplots for each data point.
- Option `col_wrap` selects how many subplots will be placed ion one row of the overall figure.

```
[19]: # create grid of small multiple plots
sns.set_theme(font_scale=1.2)
grid = sns.relplot(data=life_exp_sel_long,
                    x='Year', y='Expectancy', col='Country',
                    col_wrap=5, kind="line", height=3, aspect=1)

grid.set_axis_labels('Year', 'Life expectancy (years)')
grid.set_titles("{col_name}") # title of each plot will be country name
pass
```

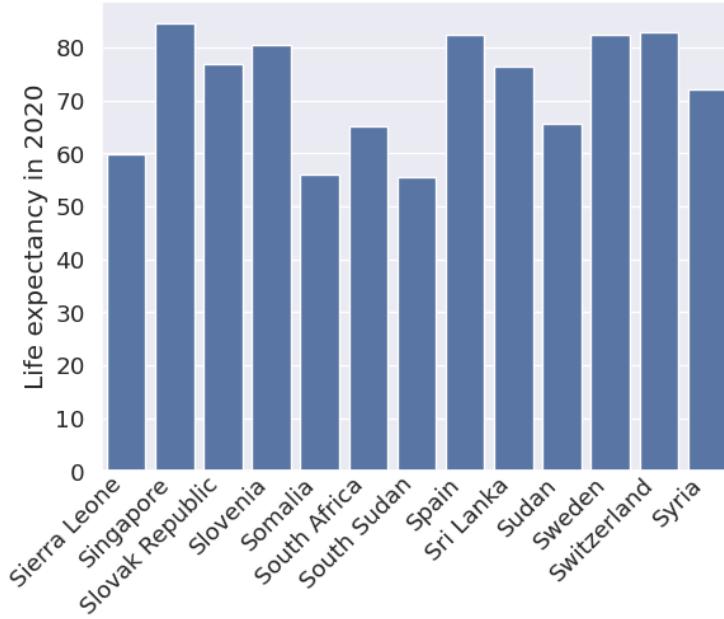


1.18 Bar graph

- We plot a bargraph of life expectancy in our selected countries by Seaborn function `barplot`.
- All bars are plotted by the same color using setting `color="C0"`.
- We rotate tick labels on the x axes to fit them in the given space.

```
[20]: def rotate_bar_labels(axes, angle=45):
    """Auxiliary function for rotating bar plot labels by 45 degrees"""
    axes.tick_params(axis='x', labelrotation=angle, pad=-5)
    plt.setp(axes.get_xticklabels(), ha='right')

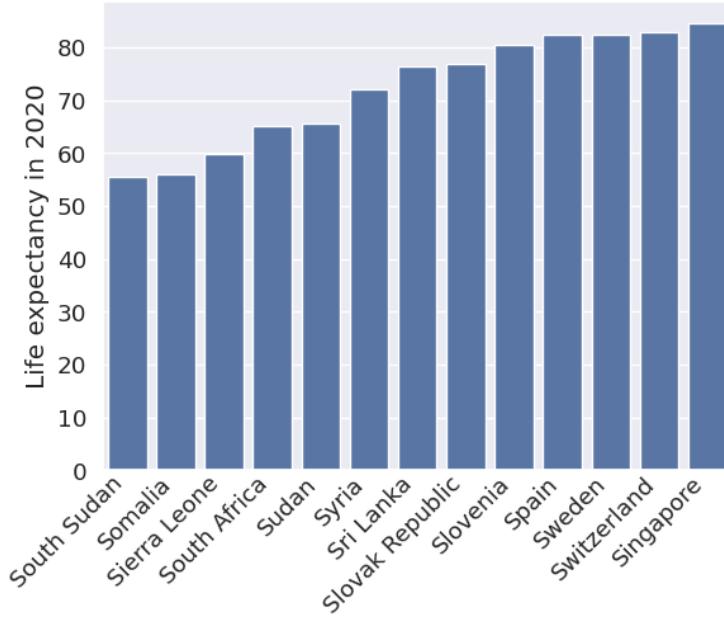
# select one year from the long table
life_exp_sel_2020 = life_exp_sel_long.query('Year==2020')
# create barplot
axes = sns.barplot(data=life_exp_sel_2020,
                    x='Country', y='Expectancy', color="C0")
axes.set_ylabel("Life expectancy in 2020")
axes.set_xlabel(None)
rotate_bar_labels(axes)
pass
```



1.19 Bar graph with sorted columns

Countries are sorted by value in preprocessing, then plotted as before.

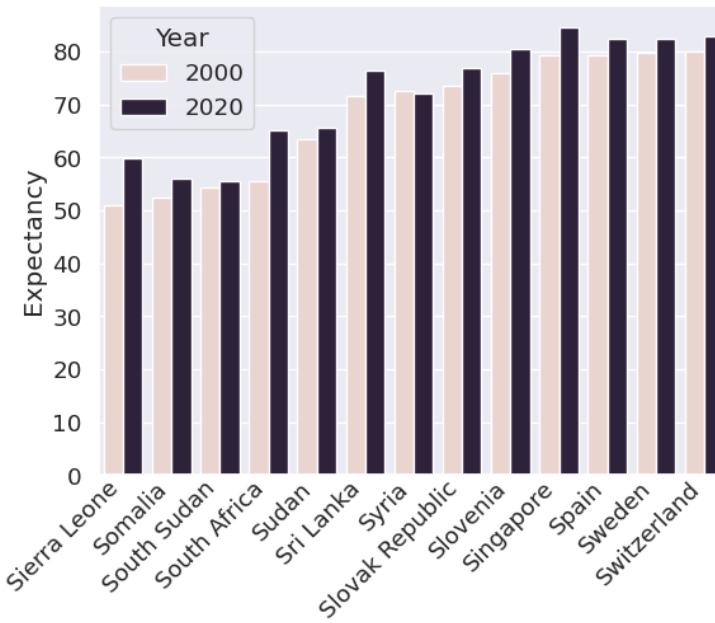
```
[21]: # sorting
life_exp_sel_2020_sorted = life_exp_sel_2020.sort_values('Expectancy')
# plotting
axes = sns.barplot(data=life_exp_sel_2020_sorted,
                     x='Country', y='Expectancy', color="CO")
axes.set_ylabel("Life expectancy in 2020")
axes.set_xlabel(None)
rotate_bar_labels(axes)
pass
```



1.20 Bar graph with multiple colors

- Now we compare life expectancy in two years in a bargraph with the colors of columns.
- After selecting appropriate rows of the long table, we use column `Year` in the `hue` parameter of `barplot`.

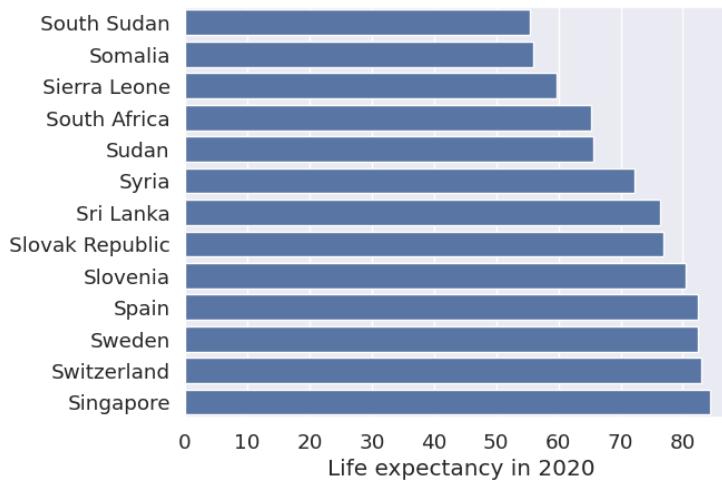
```
[22]: # select only years 2000 and 2020 from the table, sort
life_exp_sel_comp = life_exp_sel_long.query('Year==2020 or Year==2000').
    ↪sort_values('Expectancy')
# plotting
axes = sns.barplot(data=life_exp_sel_comp, x='Country', y='Expectancy',
    ↪hue='Year')
axes.set_xlabel(None)
rotate_bar_labels(axes)
pass
```



1.21 Horizontal bar graph

- Longer bar labels are easier to read in a horizontal barplot.
- In Seaborn, it is sufficient to switch x and y arguments.

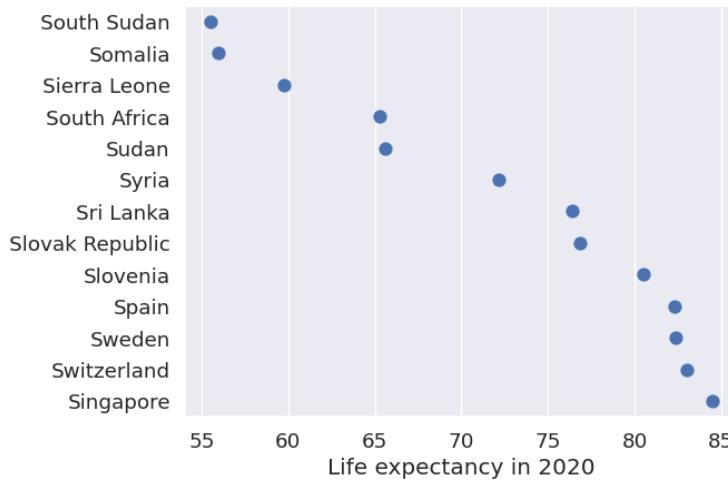
```
[23]: axes = sns.barplot(data=life_exp_sel_2020_sorted,
                      y='Country', x='Expectancy', color="CO")
axes.set_xlabel("Life expectancy in 2020")
axes.set_ylabel(None)
pass
```



1.22 Dot plot

- Dot plot shows only the end of each bar as a dot.
- Seaborn's `pointplot` joins these dots by lines by default, `linestyle='none'` prevents this.
- Note that in contrast to barplots, the x axis does not start at 0 (we could make it so by `set_xlim`).

```
[24]: axes = sns.pointplot(data=life_exp_sel_2020_sorted,
                           y='Country', x='Expectancy',
                           color="C0", linestyle='none')
axes.set_xlabel("Life expectancy in 2020")
axes.set_ylabel(None)
pass
```



1.23 Heatmap

- The goal is to create heatmap with countries as rows, several years as columns and life expectancy values as colors.
- We first need to create a DataFrame with these values in such an arrangement by selecting rows with appropriate years from our long table and pivoting the table by year to make it wide.
- Finally we sort the table by the expectancy in the last year.

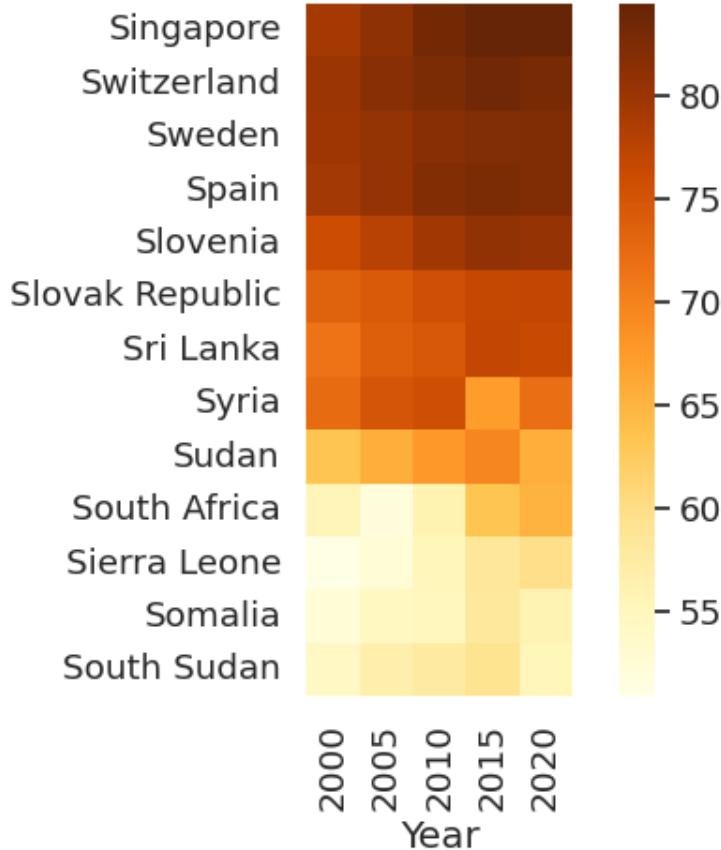
```
[25]: # set of years to be used
sel_years=[2000, 2005, 2010, 2015, 2020]
# create desired wide table
life_exp_sel_wide = (life_exp_sel_long.query('Year in @sel_years')
                      .pivot(index='Country', columns='Year', □
                     ↵values='Expectancy')
                      .sort_values(2020, ascending=False))
# show the table
```

```
display(life_exp_sel_wide)
```

| Year | 2000 | 2005 | 2010 | 2015 | 2020 |
|-----------------|------|------|------|------|-----------|
| Country | | | | | |
| Singapore | 79.3 | 81.1 | 83.2 | 84.4 | 84.465854 |
| Switzerland | 80.1 | 81.5 | 82.5 | 83.5 | 83.000000 |
| Sweden | 79.8 | 80.6 | 81.5 | 82.2 | 82.356098 |
| Spain | 79.4 | 80.5 | 82.0 | 82.6 | 82.331707 |
| Slovenia | 76.0 | 77.7 | 79.5 | 80.8 | 80.531707 |
| Slovak Republic | 73.5 | 74.3 | 75.6 | 76.7 | 76.865854 |
| Sri Lanka | 71.6 | 73.8 | 74.7 | 76.9 | 76.393000 |
| Syria | 72.5 | 75.0 | 75.8 | 67.3 | 72.140000 |
| Sudan | 63.4 | 65.7 | 67.7 | 69.6 | 65.614000 |
| South Africa | 55.6 | 52.0 | 56.1 | 63.4 | 65.252000 |
| Sierra Leone | 50.9 | 52.6 | 55.4 | 58.5 | 59.763000 |
| Somalia | 52.5 | 54.7 | 55.0 | 58.3 | 55.967000 |
| South Sudan | 54.4 | 56.7 | 57.8 | 59.4 | 55.480000 |

- Heatmap is plotted by `sns.heatmap` function.
- We have used options to set the shape of individual cells to square and change the color palette ('cmap').

```
[26]: axes = sns.heatmap(data=life_exp_sel_wide, square=True, cmap="YlOrBr")
axes.set_ylabel(None)
pass
```



1.24 Pie chart

- To prepare data for pie chart, we use two features of Pandas which we will cover in a later lecture: converting the Income Group column to a categorical type and computing the number of countries in various income groups using `groupby`.
- In this way we create two Series: `groups` with counts for the whole world and `groups_asia` for just East Asian countries.

```
[27]: # creating a categorical type
income_categories = ["Low income", "Lower middle income",
                      "Upper middle income", "High income"]
cat_type = pd.api.types.CategoricalDtype(categories=income_categories,
                                         ordered=True)

# converting Income Group column to cat_type
countries_cat = countries.astype({'Income Group': cat_type})

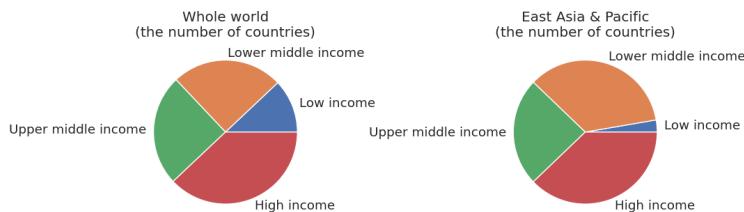
# aggregation using groupby
groups = countries_cat.groupby('Income Group').size().rename('Count')
# the same but only on countries selected by query
groups_asia = (countries_cat.query('Region=="East Asia & Pacific"')
               .groupby('Income Group').size().rename('Count'))
```

```
display(groups)
```

```
Income Group
Low income           26
Lower middle income 54
Upper middle income 54
High income          82
Name: Count, dtype: int64
```

- The plotting is done by the `pie` function from Matplotlib.
- It gets the series with counts as parameter `x` and country names as `labels`.

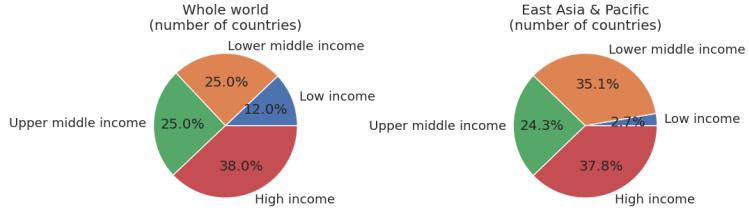
```
[28]: figure, axes = plt.subplots(1,2, figsize=(10,5))
axes[0].pie(x=groups, labels=groups.index)
axes[0].set_title('Whole world\n(the number of countries)')
axes[1].pie(x=groups_asia, labels=groups_asia.index)
axes[1].set_title('East Asia & Pacific\n(the number of countries)')
figure.subplots_adjust(wspace=1)
pass
```



1.25 Pie chart with labels

- Labels are added by `autopct` setting in `pie`. This setting provides a formatting string for the values, here we print one decimal place.

```
[29]: figure, axes = plt.subplots(1,2, figsize=(10,5))
axes[0].pie(x=groups, labels=groups.index, autopct=".1f%%")
axes[0].set_title('Whole world\n(number of countries)')
axes[1].pie(x=groups_asia, labels=groups_asia.index, autopct=".1f%%")
axes[1].set_title('East Asia & Pacific\n(number of countries)')
figure.subplots_adjust(wspace=1)
pass
```



1.26 Stacked bar graph instead of pie chart

- To prepare data for stacked bar graph, we need to combine our two count Series (`groups` and `groups_asia`) to one long table `groups_concat`.
- This is a DataFrame, because `Income Group` was moved from index to a column.
- We also add percentage column, which will be used in the plot. Percentage is computed by divided counts with the sum of all counts.
- We also add a column with region name, because we will consider two regions (East Asia and the whole world).

```
[30]: # first create DataFrame for East Asia
# add Income Group index as a column
temp_asia = groups_asia.reset_index()
# compute percentages and add as a new column
temp_asia['Percentage'] = temp_asia['Count'] * 100 / temp_asia['Count'].sum()
# add Region as a new column, filled with copies of the same string
temp_asia['Region'] = ["East Asia & Pacific"] * len(groups_asia)

# the same three steps for World
temp_world = groups.reset_index()
temp_world['Percentage'] = temp_world['Count'] * 100 / temp_world['Count'].sum()
temp_world['Region'] = ["World"] * len(groups)

# concatenate two DataFrames and display
groups_concat = pd.concat([temp_asia, temp_world], axis=0)
display(groups_concat)
```

| | Income Group | Count | Percentage | Region |
|---|---------------------|-------|------------|---------------------|
| 0 | Low income | 1 | 2.702703 | East Asia & Pacific |
| 1 | Lower middle income | 13 | 35.135135 | East Asia & Pacific |
| 2 | Upper middle income | 9 | 24.324324 | East Asia & Pacific |
| 3 | High income | 14 | 37.837838 | East Asia & Pacific |
| 0 | Low income | 26 | 12.037037 | World |
| 1 | Lower middle income | 54 | 25.000000 | World |
| 2 | Upper middle income | 54 | 25.000000 | World |
| 3 | High income | 82 | 37.962963 | World |

- Stacked bar graph is not very automated in Matplotlib.

- Left coordinate for each rectangle needs to be computed manually, then function `barh` is used (see also [tutorial](#)).
- Each bar is labeled with the percentage using `bar_label` function.

```
[31]: # list of regions and income groups
tmp_regions = groups_concat['Region'].unique()
tmp_groups = groups_concat['Income Group'].unique()
# the first rectangles start at 0
starts = pd.Series([0] * tmp_regions.shape[0])
# create plot
figure, axes = plt.subplots()

# iterate through income groups
for group in tmp_groups:
    # select data for this income group from both regions
    tmp_data = groups_concat.query("`Income Group` == @group")
    # plot
    rectangles = axes.barh(y=tmp_data['Region'], width=tmp_data['Percentage'],
                           left=starts, label=group)
    # add labels
    axes.bar_label(rectangles, label_type='center', fmt=".0f%%")
    # move starts by the size of each rectangle
    starts += tmp_data['Percentage'].reset_index(drop=True)

axes.legend(bbox_to_anchor=(1, 1), loc=2)
# hide plot frame and x-axis ticks
axes.xaxis.set_visible(False)
axes.set_frame_on(False)
pass
```



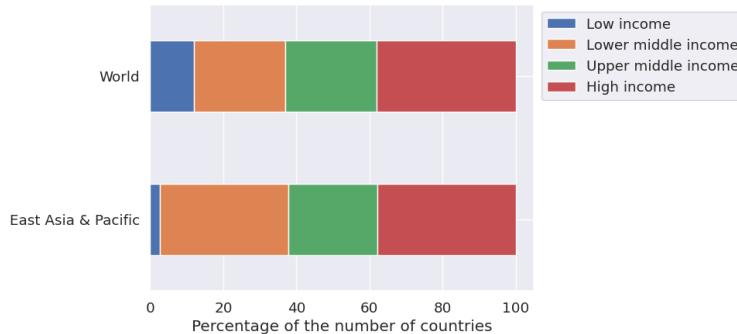
- Stacked bar charts are much easier in Plotly using `px.bar` function.

```
[32]: fig = px.bar(groups_concat, x="Region", y="Percentage", color="Income Group",
                  text="Percentage", text_auto=".0f")
fig.update_layout(font=dict(size=20), xaxis_title=None,)
fig.show()
```

It can also be drawn easily directly by Pandas, but values (sizes of rectangles) are not shown. The table is first converted to wide form with different income groups as columns.

```
[33]: groups_concat_wide = groups_concat.pivot(columns='Income Group', index='Region', values='Percentage')
display(groups_concat_wide)
axes = groups_concat_wide.plot(kind='barh', stacked=True)
axes.legend(bbox_to_anchor=(1, 1), loc=2)
axes.set_ylabel(None)
axes.set_xlabel('Percentage of the number of countries')
pass
```

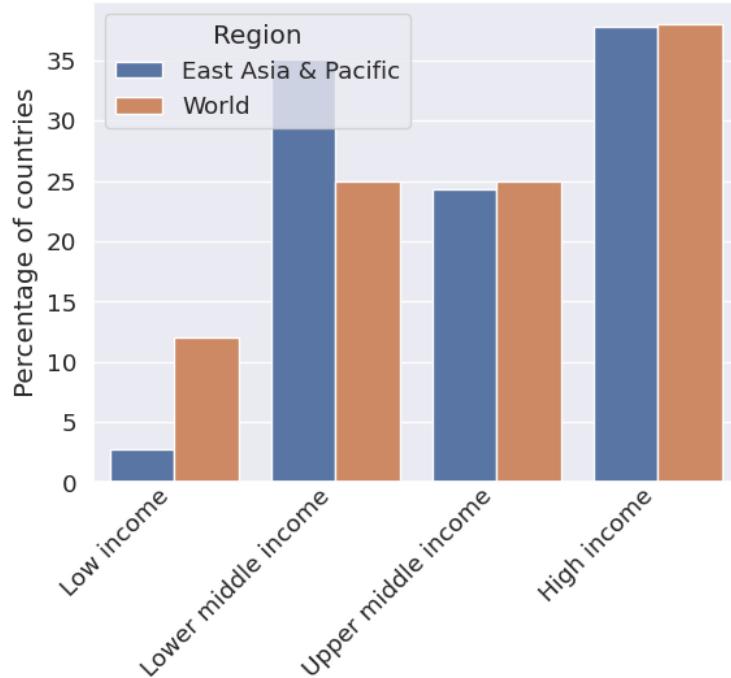
| Income Group | Low income | Lower middle income | Upper middle income | \ |
|---------------------|-------------|---------------------|---------------------|-----------|
| Region | | | | |
| East Asia & Pacific | 2.702703 | | 35.135135 | 24.324324 |
| World | 12.037037 | | 25.000000 | 25.000000 |
| Income Group | High income | | | |
| Region | | | | |
| East Asia & Pacific | 37.837838 | | | |
| World | 37.962963 | | | |



1.27 Colored bar graphs insteads of pie chart

- As we have seen before, colored bar graphs are easy in Seaborn from a long table.
- Therefore we use `groups_concat` DataFrame.

```
[34]: axes = sns.barplot(data=groups_concat,
                      x='Income Group', y='Percentage', hue='Region')
rotate_bar_labels(axes)
axes.set_xlabel(None)
axes.set_ylabel("Percentage of countries")
pass
```

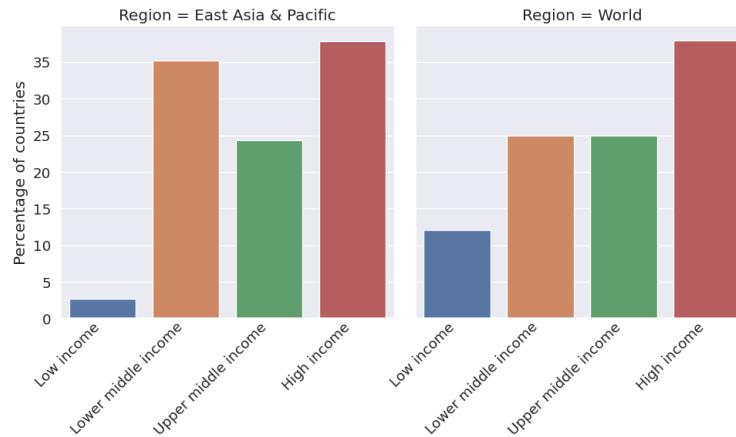


1.28 Multiple bar graphs instead of pie chart

- In the next plot a separate bar graph for each region.
- This is also very simple in Seaborn using `catplot` with setting `col='Region'` and `kind='bar'`.
- Labels are rotated in each subplot using a for-loop.

```
[35]: grid = sns.catplot(kind='bar', data=groups_concat,
                      x='Income Group', y='Percentage',
                      col='Region', hue='Income Group')

# label rotation
for which in [0,1]:
    rotate_bar_labels(grid.axes[0,which])
    grid.axes[0,which].set_xlabel(None)
    grid.axes[0,which].set_ylabel("Percentage of countries")
pass
```



1.29 Strip plot

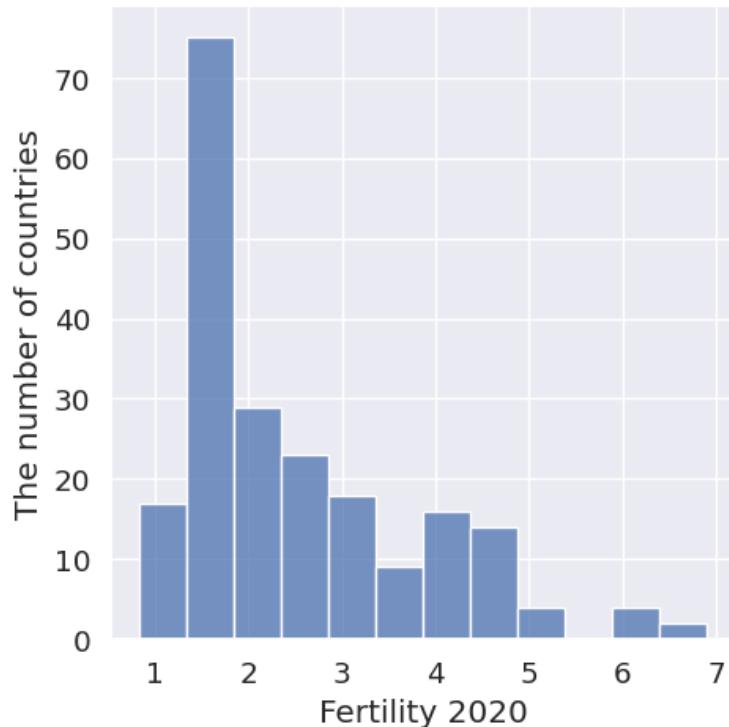
- Strip plot of fertility per region is also very simple in `sns.catplot`.
- Setting `kind='strip'` is default for `catplot`, so it is omitted here.
- Size of dots is reduced to limit overlapping markers.

```
[36]: grid = sns.catplot(x="Fertility2020", y="Region", data=countries, size=3)
grid.set_axis_labels("Fertility in 2020", "")
pass
```



1.30 Histogram

```
[37]: grid = sns.displot(countries, x="Fertility2020", binwidth=0.5)
grid.set_axis_labels("Fertility 2020", "The number of countries")
pass
```



1.31 Parallel coordinates

- We want to display various properties of individual countries as parallel coordinate plot.
- We first create table `for_parallel` with selected columns and express all numbers as percentage of the maximum value.
- We add `selected` column which has True in row for Slovakia and False elsewhere. This is used to highlight Slovakia in the plot.
- Also ordering is changed to draw Slovakia the last.

```
[38]: # selecting columns
for_parallel_sel = countries.loc[:, ['Population2020', 'Area', 'GDP2020',
                                      'Expectancy2020', 'Fertility2020']]
# computing maximum in each column
for_parallel_max = for_parallel_sel.max(axis=0)
# dividing values by the maximum and multiplying by 100 to get percentage
for_parallel = for_parallel_sel.div(for_parallel_max, axis=1) * 100
```

```
# creating column of booleans called 'selected' which highlights Slovakia with True
for_parallel['selected'] = countries.index=="Slovak Republic"
# sort by 'selected' to put Slovakia last
for_parallel.sort_values('selected', inplace=True)
# show end of the table
display(for_parallel.tail())
```

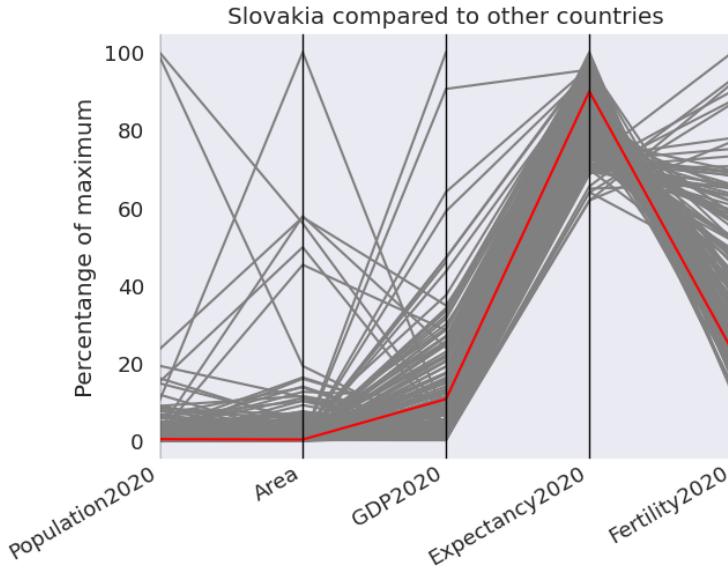
| Country | Population2020 | Area | GDP2020 | Expectancy2020 | \ |
|-----------------|----------------|----------|-----------|----------------|---|
| Greece | 0.758174 | 0.771775 | 9.651333 | 95.076168 | |
| Greenland | 0.003995 | 2.400538 | 29.962671 | 83.788155 | |
| Fiji | 0.065227 | 0.106853 | 2.638193 | 79.445541 | |
| Zimbabwe | 1.110458 | 2.285380 | 0.752009 | 71.492098 | |
| Slovak Republic | 0.386849 | 0.286754 | 10.711280 | 89.904148 | |

| Country | Fertility2020 | selected |
|-----------------|---------------|----------|
| Greece | 20.168311 | False |
| Greenland | 29.294835 | False |
| Fiji | 36.201393 | False |
| Zimbabwe | 51.436448 | False |
| Slovak Republic | 23.070226 | True |

- Parallel coordinates are drawn using Pandas `parallel_coordinates` function, which internally calls Matplotlib and returns Axes object.

```
[39]: axes = pd.plotting.parallel_coordinates(for_parallel, class_column='selected',
                                             color=['gray', 'red'])

axes.get_legend().remove()
axes.set_ylabel("Percentange of maximum")
axes.set_title("Slovakia compared to other countries")
rotate_bar_labels(axes, angle=30)
pass
```



1.32 Parallel categories

- We will use two categorical columns from the countries table, but more categorical columns could be easily added.
- We use the version of the table with a categorical income groups and sort countries by income.
- Now we use `parallel-categories` function from Plotly.
- This function orders each column of the figure by size. By calling `update_traces`, we reorder the first column by the same order as they first occur in our table.

```
[40]: for_parallel_cat = (countries_cat.loc[:,['Income Group', 'Region']]
                           .sort_values('Income Group', ascending=False))
fig = px.parallel_categories(for_parallel_cat, width=800)
fig.update_traces(dimensions=[{"categoryorder": "array"}, {}])
fig.update_layout(font_size=20)
fig.update_layout(margin={'l':200, 'r':200})
fig.show()
```

1.33 Radar chart

- Radar charts are not well supported in any of the used libraries.
- Below we compute angles of each axis manually, then use `plot` from Matplotlib.
- When creating axes, we specify polar coordinates `subplot_kw={'projection': 'polar'}`.
- We also use `set_thetagrids`

```
[41]: # skip 'selected' column, use only 3 countries
for_radar = for_parallel.loc[['India','China','United States'], :].iloc[:, 0:-1]
display(for_radar.head())
```

```

# setup plot with polar coordinates
sns.set_theme(style="whitegrid")
figure, axes = plt.subplots(subplot_kw={'projection': 'polar'})
categories = list(for_radar.columns)
import math
angles = [ i * 2 * math.pi / len(categories) for i in range(len(categories))]
angles_deg = [x / math.pi * 180 for x in angles]
axes.set_thetagrids(angles_deg, labels=categories)

# for plotting, we will need to return to starting point in each line
angles.append(angles[0])

# for each country create list of values, add the starting point, plot
for country in for_radar.index:
    values = list(for_radar.loc[country, :])
    values.append(values[0])
    axes.plot(angles, values, label=country)

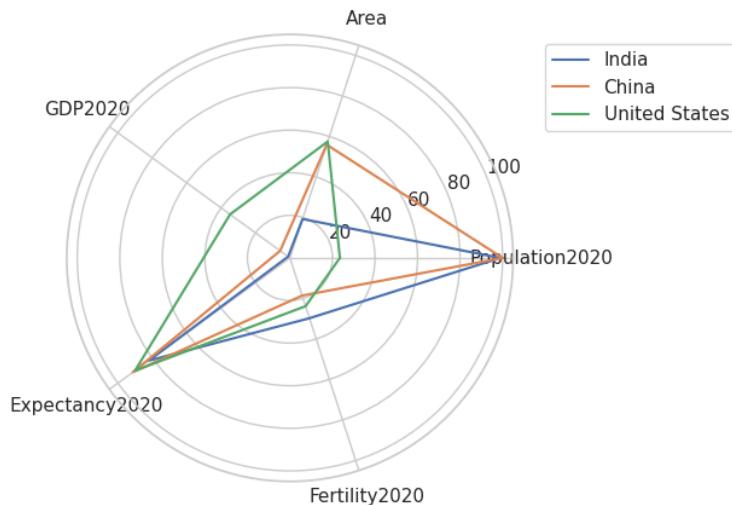
axes.legend(bbox_to_anchor=(1.05, 1), loc=2)
pass

```

| | Population2020 | Area | GDP2020 | Expectancy2020 | \ |
|---------------|----------------|-----------|-----------|----------------|---|
| Country | | | | | |
| India | 98.957347 | 19.225710 | 1.048125 | 82.049124 | |
| China | 100.000000 | 55.929174 | 5.702240 | 91.320734 | |
| United States | 23.493127 | 57.500095 | 34.803081 | 90.038227 | |

Fertility2020

| Country | |
|---------------|-----------|
| India | 29.759141 |
| China | 18.586767 |
| United States | 23.817470 |



Lecture 4

Summary statistics

[Data visualization · 1-DAV-105](#)

Lecture by Broňa Brejová

More details in the [notebook version](#)

Introduction

Summary statistics (popisné charakteristiky / štatistiky):

quantities that summarize basic properties of a single variable (a table column), such as the mean.

We can also characterize dependencies between pairs of variables.

Together with simple plots, they give us the first glimpse at the data when working with a new data set.

Data set for today

- The same data set as in group tasks 04.
- The data set describes 2049 movies.
- Originally downloaded from
<https://www.kaggle.com/rounakbanik/the-movies-dataset> and preprocessed,
keeping only movies with at least 500 viewer votes.

```
url = 'https://bbrejova.github.io/viz/data/Movies\_small.csv'  
movies = pd.read_csv(url)  
display(movies.head())
```

| title | year | budget | revenue | original_language | runtime | release_date | vote_average | vote_count | overview |
|--------------|-------------|---------------|----------------|--------------------------|----------------|---------------------|---------------------|-------------------|---|
| Toy Story | 1995 | 30000000.0 | 373554033.0 | en | 81.0 | 1995-10-30 | 7.7 | 5415.0 | Led by Woody, Andy's toys live happily in his ... |
| Jumanji | 1995 | 65000000.0 | 262797249.0 | en | 104.0 | 1995-12-15 | 6.9 | 2413.0 | When siblings Judy and Peter discover an encha... |
| Heat | 1995 | 60000000.0 | 187436818.0 | en | 170.0 | 1995-12-15 | 7.7 | 1886.0 | Obsessive master thief, Neil McCauley leads a ... |
| GoldenEye | 1995 | 58000000.0 | 352194034.0 | en | 130.0 | 1995-11-16 | 6.6 | 1194.0 | James Bond must unmask the mysterious head of ... |
| Casino | 1995 | 52000000.0 | 116112375.0 | en | 178.0 | 1995-11-22 | 7.8 | 1343.0 | The life of the gambling paradise – Las Vegas ... |

Measures of central tendency (miery stredu / polohy)

These represent a **typical value** in a sample $x = x_1, \dots, x_n$ (one numerical column).

Mean (priemer) $\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$

This is the arithmetic mean, there are also geometric and harmonic means.

Median (medián) is the middle value when the values ordered by size.

For even n usually defined as the average of the two middle values.

Example:

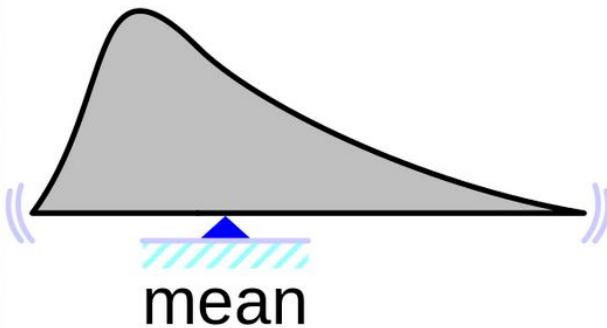
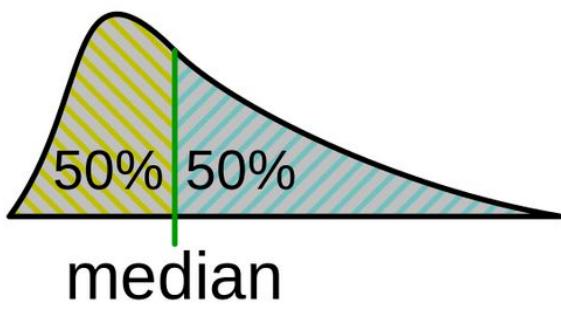
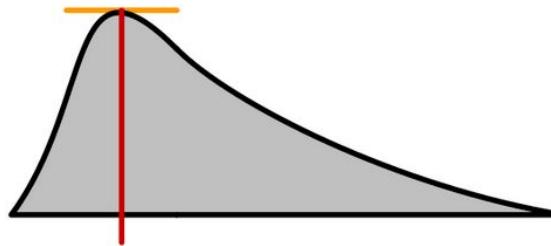
Median of 10, 12, 15, 16, 16 is 15.

Median of 10, 12, 15, 16, 16, 20 is 15.5.

Measures of central tendency (cont.)

- **Mean (priemer)**
- **Median (medián)**
- **Mode (modus)** is the most frequent value (for a discrete variable).
Mode of 10,12,15,16,16 is 16.

For continuous variables, we may look for a mode in a histogram.
This is sensitive to bin size.



https://commons.wikimedia.org/wiki/File:Visualisation_mode_median_mean.svg

Properties of the measures

If we apply **linear transformation** $a \cdot x_i + b$ with the same a and b to all x_i , mean, median and mode will be transformed **in the same way**.

This corresponds e.g. to the change in the units of measurement
(grams vs kilograms, degrees C vs degrees F)

Mean can be heavily influenced by outliers

800, 1000, 1100, 1200, 1800, 2000, 30000: mean 5414.3, median 1200

800, 1000, 1100, 1200, 1800, 2000, 10000: mean 2557.1, median 1200

Therefore we often **prefer median** (e.g. median salary).

Computation in Pandas

```
display(Markdown("Properties of the column `year` in our table:"))
print(f"Mean: {movies['year'].mean():.2f}")
print(f"Median: {movies['year'].median()}")
print(f"Mode:\n{movies['year'].mode()}")
```

Properties of the column year in our table:

Mean: 2004.14

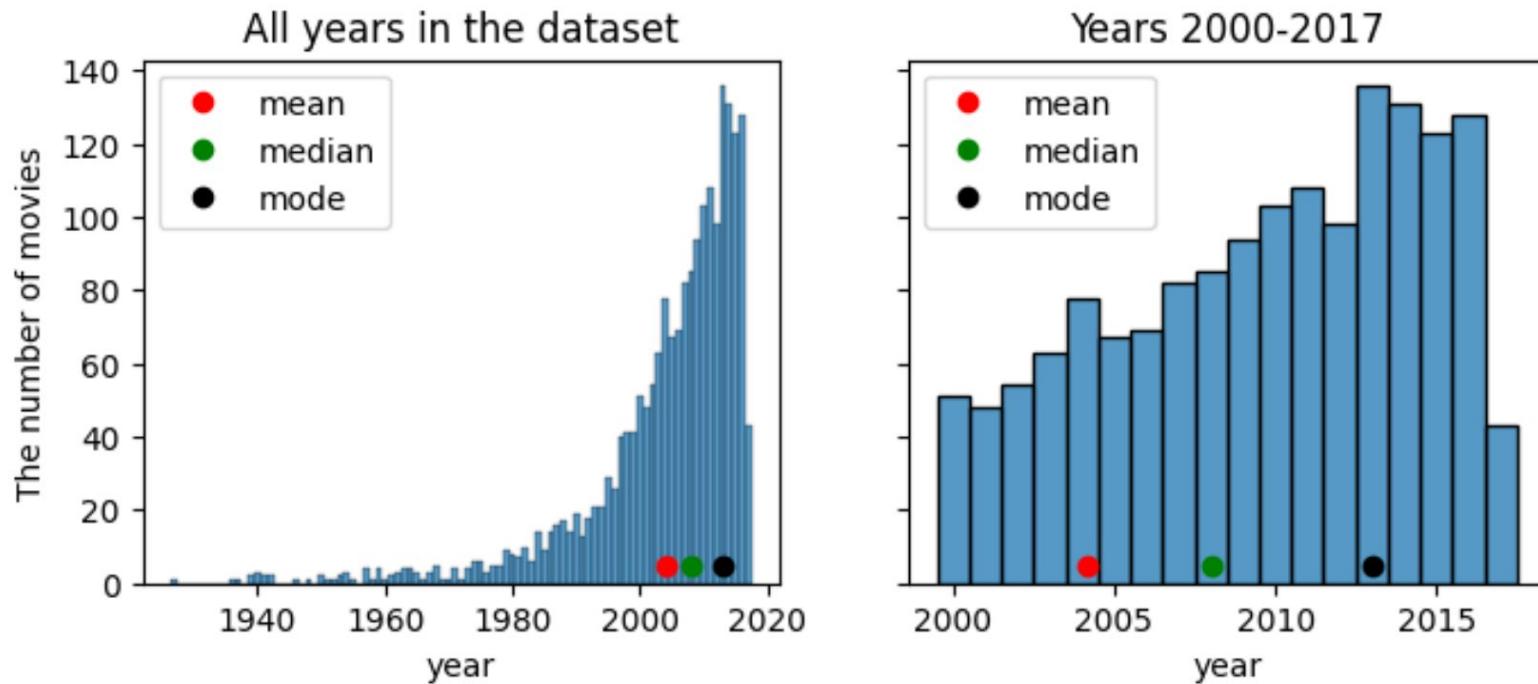
Median: 2008.0

Mode:

0 2013

Name: year, dtype: int64

Shown in a histogram (whole and detail)



What causes the difference between the mean and the median?

Summarizing many columns or rows

- Functions `mean` and `median` can be applied to all numerical columns
- With `axis=1` we get means or medians in rows

```
display(movies.mean(numeric_only=True))
```

```
year                  2,004.1
budget                55,108,939.7
revenue               198,565,134.3
runtime                112.7
vote_average            6.6
vote_count              1,704.6
dtype: float64
```

Quantiles, percentiles and quartiles (kvantly, percentily, kvartily)

Median is the middle value in a sorted order;
about 50% of values are smaller and 50% larger.

For a percentage p , the **p -th percentile** is at position roughly $(p/100) \cdot n$ in the sorted order of values.

Similarly **quantile** (in Pandas), but we give fraction between 0 and 1 rather than percentage.

Quartiles are three values Q_1 , Q_2 and Q_3 that split input data into quarters.
Therefore, Q_2 is the median.

Quantiles in Pandas

```
display(Markdown("Median:"),  
        movies['year'].median())  
display(Markdown("Quantile for 0.5:"),  
        movies['year'].quantile(0.5))  
display(Markdown("All quartiles:"),  
        movies['year'].quantile([0.25, 0.5, 0.75]))  
display(Markdown("With step 0.1:"),  
        movies['year'].quantile(np.arange(0.1, 1, 0.1)))
```

Median:

2008.0

Quantile for 0.5:

2008.0

All quartiles:

0.25 2,000.00

0.50 2,008.00

0.75 2,013.00

Name: year, dtype: float64

With step 0.1:

0.10 1,988.80

0.20 1,998.00

0.30 2,002.00

0.40 2,005.00

0.50 2,008.00

0.60 2,010.00

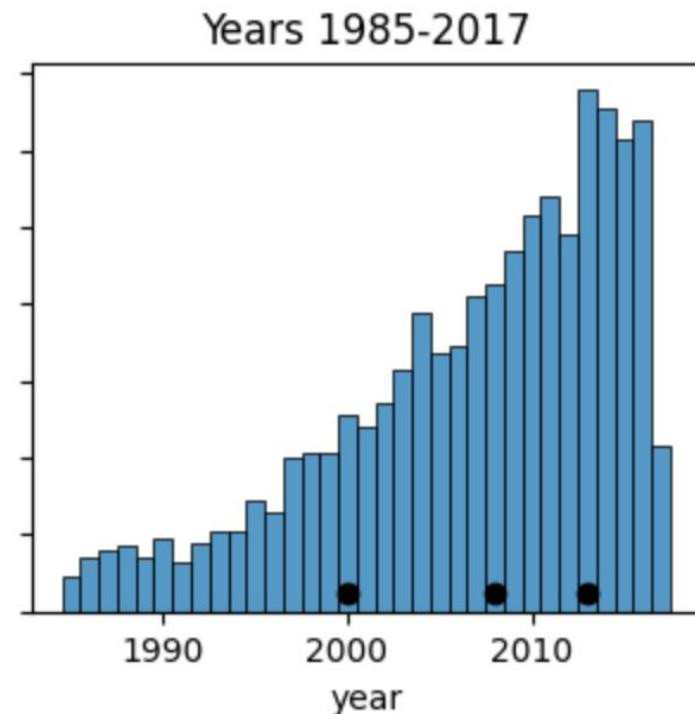
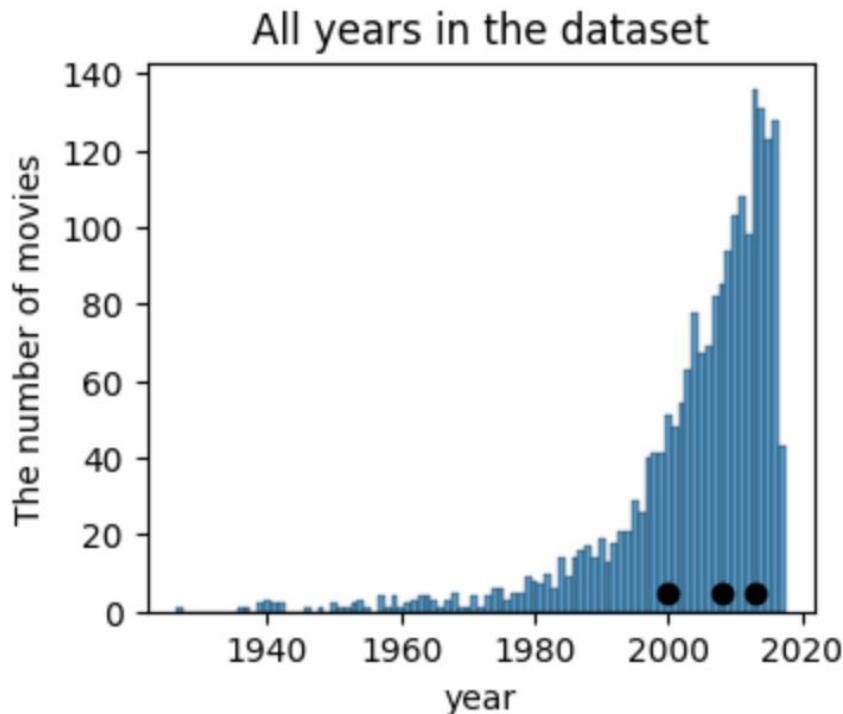
0.70 2,012.00

0.80 2,014.00

0.90 2,015.00

Name: year, dtype: float64

Quartiles in a histogram (whole and detail)



Quantile interpolation

Optional parameter `interpolation` accepts values 'linear' (default), 'lower', 'higher', 'midpoint', 'nearest'.

Minimum is at quantile 0, maximum at quantile 1, the rest evenly spaced between.

The quantile between two elements is influenced only by its two neighbors.

Example: list [0,10,20,100]

p=0: 0, p=1/3: 10, p=2/3: 20, p=1: 100

p=1/4: by default linear interpolation at 3/4 between 0 and 10, i.e. 7.5.

Linear interpolation is continuous as p changes from 0 to 1.

Quantile interpolation

Quantiles for [0, 10, 20, 100]

```
0.01      0.30
0.25      7.50
0.50     15.00
0.75     40.00
dtype: float64
```

Quantiles for [0, 10, 20, 100] with interpolation='lower'

```
0.01      0
0.25      0
0.50     10
0.75     20
dtype: int64
```

Measures of variability (miery variability)

Values in the sample may be close to central values or spread widely.

Examples of measures:

Range of values from **minimum** to **maximum** (sensitive to outliers).

Interquartile range IQR (kvartilové rozpätie): range between Q_1 and Q_3 (contains the middle half of the data).

Variance and standard deviation (next)

Variance (rozptyl)

For each x_i square its difference from the mean

Squaring gives non-negative values (and squares are easier to work with mathematically than absolute values).

Variance is the mean of these squares, but we divide by $n-1$ rather than n :

$$s^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n - 1}$$

Division by n would underestimate the true variance of the underlying population (more in the statistics course).

Standard deviation (smerodajná odchýlka)

Square root of the variance

$$s = \sqrt{s^2}$$

It is in the same units as the original values
(variance is in units squared).

Recall:

$$s^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n - 1}$$

Properties

Larger variance and standard deviation mean that data are spread farther from the mean.

If we apply **linear transformation** $a \cdot x_i + b$ with the a and b to all x_i :

Neither variance nor standard deviation change with b .

Variance is multiplied by a^2 , standard deviation by $|a|$.

These measures are strongly **influenced by outliers**:

800, 1000, 1100, 1200, 1800, 2000, 30000: st. dev. 10850.0, IQR 850

800, 1000, 1100, 1200, 1800, 2000, 10000: st. dev. 3310.5, IQR 850.

| | |
|---|--------------------|
| display(Markdown("**Minimum**"), | Minimum |
| movies['year'].min()) | 1927 |
| display(Markdown("**Maximum**"), | Maximum |
| movies['year'].max()) | 2017 |
| display(Markdown("**Mean**"), | Mean |
| movies['year'].mean()) | 2004.1449487554905 |
| display(Markdown("**Variance**"), | Variance |
| movies['year'].var()) | 161.2714600681735 |
| display(Markdown("**Standard deviation**"), | Standard deviation |
| movies['year'].std()) | 12.699270060447313 |
| q1 = movies['year'].quantile(0.25) | Q1, Q3 and IQR: |
| q3 = movies['year'].quantile(0.75) | |
| display(Markdown("**Q1, Q3 and IQR:**"), | 2000.0 |
| q1, q3, q3-q1) | 2013.0 |
| | 13.0 |

Outliers (odl'ahlé hodnoty)

Outliers are the values which are far from the typical range of values.

In data analysis, it is important to **check outliers**.

If they represent **errors**, we may try to correct or remove them.

They can also represent **interesting anomalies**.

Different definitions of outliers may be appropriate in different situations.

One possible definition of outliers

The criterion by statistician John Tukey:

Outliers are the values outside of the range $[Q_1 - k \cdot IQR, Q_3 + k \cdot IQR]$,
e.g. for $k = 1.5$.

In our example 800, 1000, 1100, 1200, 1800, 2000, 30000:

$$Q_1 = 1050, Q_3 = 1900, IQR = 850.$$

$$Q_1 - 1.5 \cdot IQR = -225, Q_3 + 1.5 \cdot IQR = 3175.$$

Outliers are values smaller than -225 or larger than 3175 ; here only 30000.

The range of outliers is not influenced if we change the outliers.

Computation in Pandas

```
# get quartiles and iqr
q1 = movies['year'].quantile(0.25)
q3 = movies['year'].quantile(0.75)
iqr = q3 - q1
# compute thresholds for outliers
lower = q1 - 1.5 * iqr
upper = q3 + 1.5 * iqr
# count outliers
count = movies.query('year < @lower or year > @upper')['year'].count()
```

Outliers outside of range: [1980.5, 2032.5]

Outlier count: 112

Total count: 2049

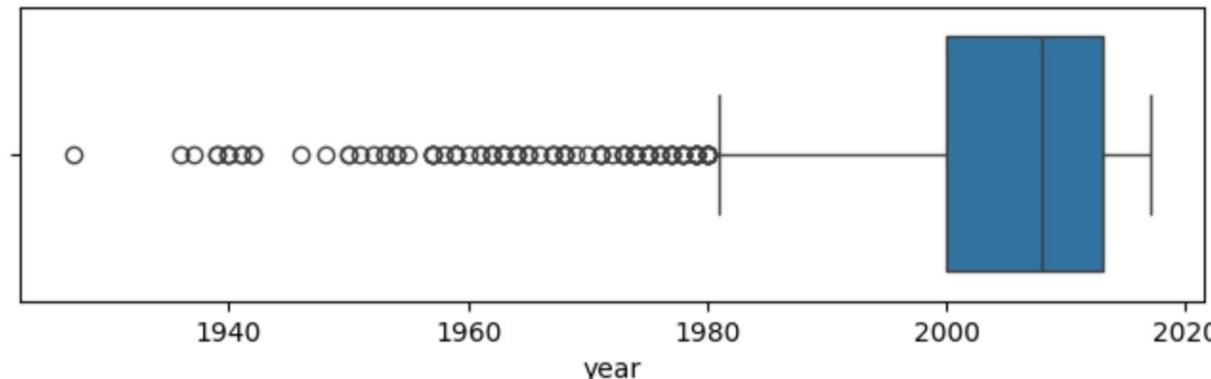
Boxplot (krabicový graf)

Developed by Mary Eleanor Hunt Spear and John Tukey.

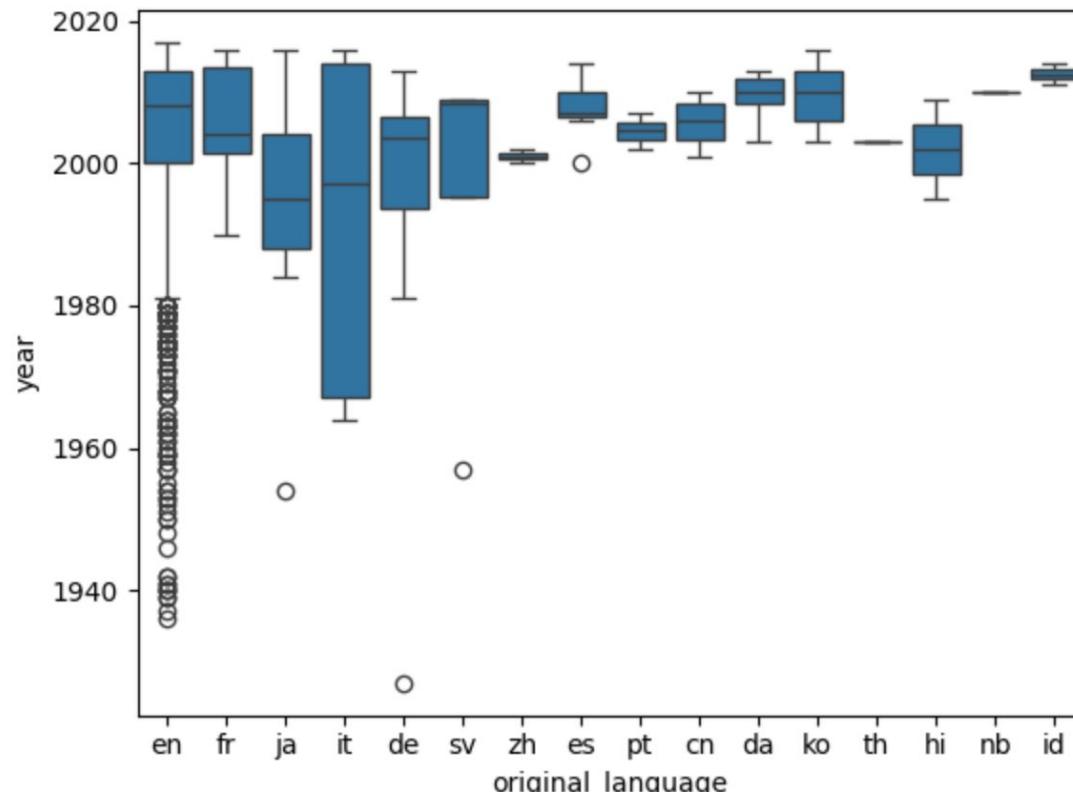
It shows the **five-number summary**: min, $Q1$, median ($Q2$), $Q3$, max

$Q1$ and $Q3$: a box, median: line through box, min and max: whiskers

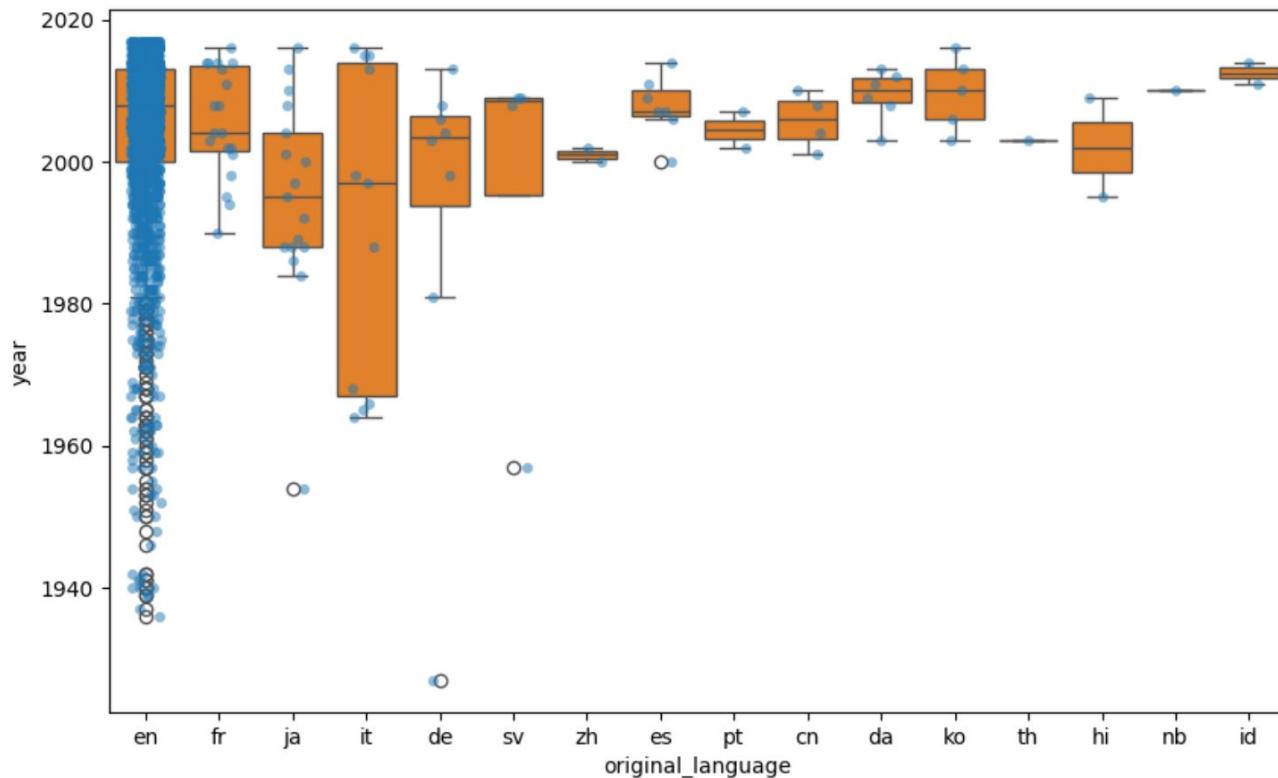
Outliers often excluded from the whiskers and shown as points.



Boxplots are used for quick comparison



For small datasets we may add strip plot

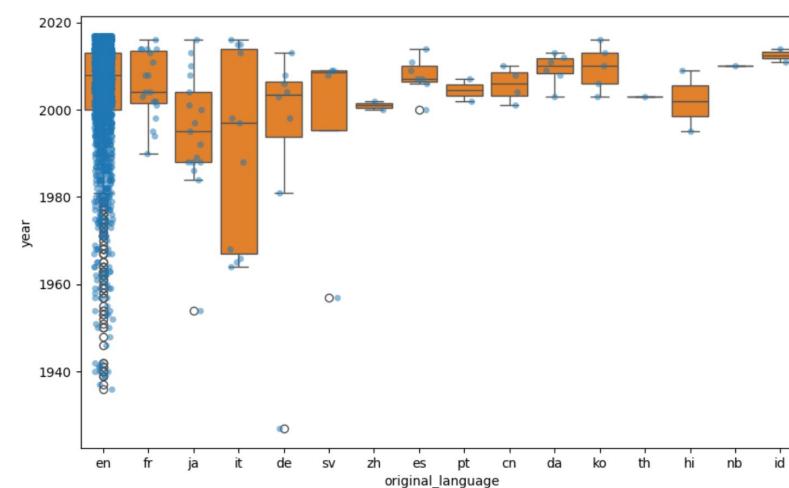


Works well for smaller languages, mess for en.

What do we see for sv, pt, th, hi, nb, id?

Code for the plot

```
axes = sns.boxplot(data=movies, x='original_language',
                    y='year', color='C1')
sns.stripplot(data=movies, x='original_language',
               y='year', color='C0',
               alpha=0.5, size=5, jitter=0.2)
```



Quick overview of a data set: describe in Pandas

```
movies.describe()
```

| | year | budget | revenue | runtime | vote_average | vote_count |
|-------|----------|----------------|------------------|----------|--------------|------------|
| count | 2,049.00 | 1,959.00 | 1,965.00 | 2,049.00 | 2,049.00 | 2,049.00 |
| mean | 2,004.14 | 55,108,939.70 | 198,565,134.28 | 112.66 | 6.63 | 1,704.64 |
| std | 12.70 | 53,139,663.86 | 233,028,732.94 | 24.76 | 0.77 | 1,607.89 |
| min | 1,927.00 | 1.00 | 15.00 | 7.00 | 4.00 | 501.00 |
| 25% | 2,000.00 | 16,000,000.00 | 52,882,018.00 | 97.00 | 6.10 | 709.00 |
| 50% | 2,008.00 | 38,000,000.00 | 122,200,000.00 | 109.00 | 6.60 | 1,092.00 |
| 75% | 2,013.00 | 75,000,000.00 | 250,200,000.00 | 124.00 | 7.20 | 2,000.00 |
| max | 2,017.00 | 380,000,000.00 | 2,787,965,087.00 | 705.00 | 9.10 | 14,075.00 |

```
movies.describe(include='all').transpose()
```

| | count | unique | top | freq | mean | std | min | 25% | 50% |
|--------------------------|----------|--------|-------------------------------------|---------------|----------------|----------------|----------|---------------|----------------|
| title | 2049 | 2018 | Beauty and the Beast | 3 | NaN | NaN | NaN | NaN | NaN |
| year | 2,049.00 | NaN | NaN | NaN | 2,004.14 | 12.70 | 1,927.00 | 2,000.00 | 2,008.00 |
| budget | 1,959.00 | NaN | NaN | NaN | 55,108,939.70 | 53,139,663.86 | 1.00 | 16,000,000.00 | 38,000,000.00 |
| revenue | 1,965.00 | NaN | NaN | NaN | 198,565,134.28 | 233,028,732.94 | 15.00 | 52,882,018.00 | 122,200,000.00 |
| original_language | 2049 | 16 | en | 1958 | NaN | NaN | NaN | NaN | NaN |
| runtime | 2,049.00 | NaN | NaN | NaN | 112.66 | 24.76 | 7.00 | 97.00 | 109.00 |
| release_date | 2049 | 1740 | 2014-12-25 | 6 | NaN | NaN | NaN | NaN | NaN |
| vote_average | 2,049.00 | NaN | NaN | NaN | 6.63 | 0.77 | 4.00 | 6.10 | 6.60 |
| vote_count | 2,049.00 | NaN | NaN | NaN | 1,704.64 | 1,607.89 | 501.00 | 709.00 | 1,092.00 |
| overview | 2049 | 2049 | Andy's toys live happily in his ... | Led by Woody, | 1 | NaN | NaN | NaN | NaN |

Correlation (korelácia)

We are often interested in **relationships** among variables (data columns).

Next: two correlation coefficients that measure strength of such relationships.

Beware: **correlation does not imply causation**

Correlation does not imply causation

If electricity consumption grows in a very cold weather, there might be **cause-and-effect** relationship: the cold weather is causing people to use more electricity for heating.

If healthier people tend to be happier, which is the cause and which is effect?

Both studied variables can be also influenced by some third, **unknown factor**. For example, within a year, deaths by drowning increase with increased ice cream consumption. Both increases are spurred by warm weather.

The observed correlation can be just a **coincidence**,
see the [Redskins rule](#) and a specialized webpage [Spurious Correlations](#).
You can easily find such "coincidences" by comparing many pairs of variables.

Pearson correlation coefficient

It measures linear relationship between two variables.

Consider pairs of values $(x_1, y_1), \dots, (x_n, y_n)$, where (x_i, y_i) are two different features of the same object.

$$r = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2} \sqrt{\sum_{i=1}^n (y_i - \bar{y})^2}}$$
$$r = \frac{1}{n-1} \sum_{i=1}^n \left(\frac{x_i - \bar{x}}{s_x} \right) \left(\frac{y_i - \bar{y}}{s_y} \right).$$

where s_x is the standard deviation of variable x .

Pearson correlation coefficient

$$r = \frac{1}{n-1} \sum_{i=1}^n \left(\frac{x_i - \bar{x}}{s_x} \right) \left(\frac{y_i - \bar{y}}{s_y} \right).$$

Expression $(x_i - \bar{x})/s_x$ is called the **standard score** or **z-score**:
how many standard deviations above or below the mean is x_i ?

The product of z-scores for x_i and y_i is positive
iff they lie on the same side of the respective means of x and y .

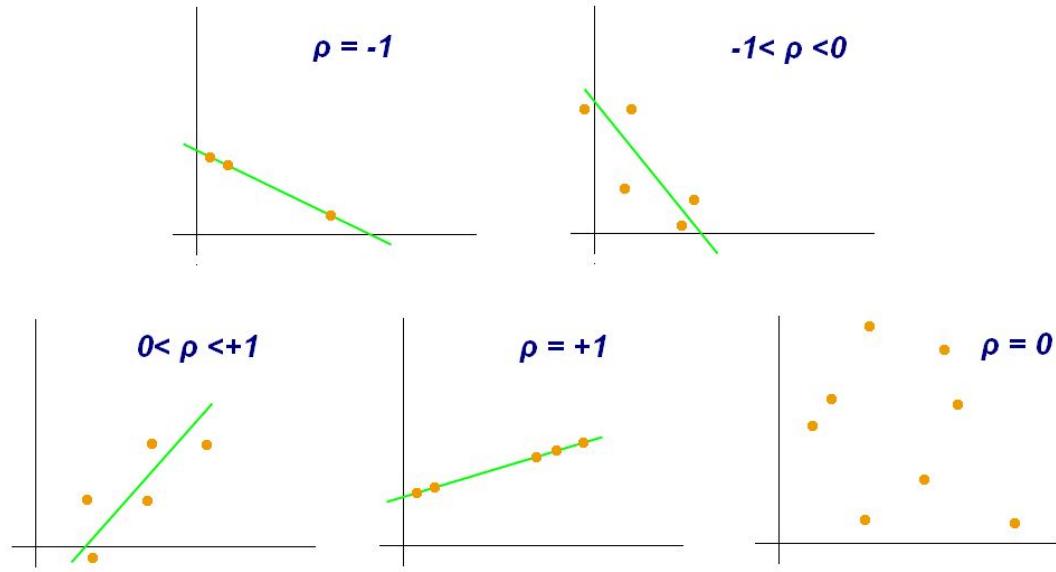
Properties of Pearson correlation coefficient

The value of r is always from interval $[-1,1]$.

1 if y grows linearly with x ,

-1 if y decreases linearly

0 means no correlation.

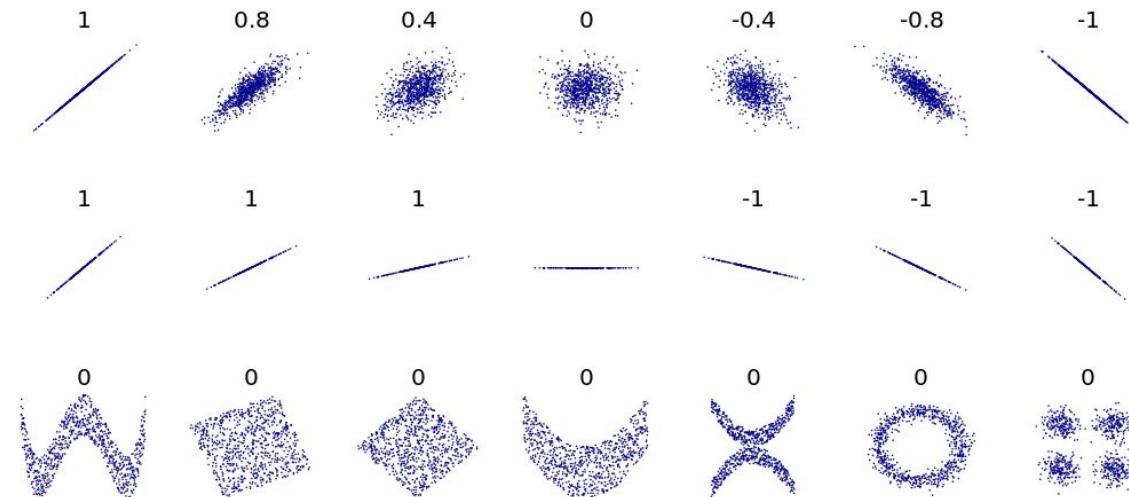


https://commons.wikimedia.org/wiki/File:Correlation_coefficient.png

Some cautions

Pearson correlation measures only linear relationships (bottom row)

Pearson correlation does not depend on the slope of the best-fit line (middle row)



https://commons.wikimedia.org/wiki/File:Correlation_examples2.svg

Properties of Pearson correlation

What if we linearly scale each variable, i.e. ax_i+b , cy_i+d ?

What if $a>0$, $a=0$, $a<0$?

What if we switch x and y?

$$r = \frac{1}{n-1} \sum_{i=1}^n \left(\frac{x_i - \bar{x}}{s_x} \right) \left(\frac{y_i - \bar{y}}{s_y} \right).$$

Properties of Pearson correlation

Pearson correlation does not change if we linearly scale each variable,
i.e. $ax_i + b$, $cy_i + d$ (for $a,c > 0$).

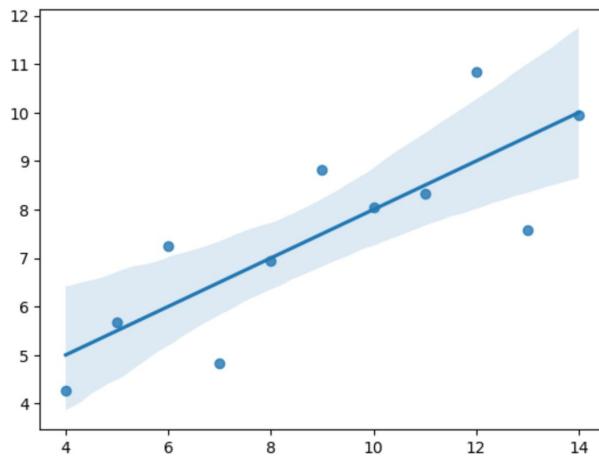
Pearson correlation is symmetric wrt. x and y .

Due to reliance on mean and std.dev. it is sensitive to outliers.

$$r = \frac{1}{n-1} \sum_{i=1}^n \left(\frac{x_i - \bar{x}}{s_x} \right) \left(\frac{y_i - \bar{y}}{s_y} \right).$$

Linear regression

The process of finding the line best representing the relationship of x and y .
In higher dimensions we can predict one variable as a linear combination of many.
You will study linear regression in later courses.
We may draw regression lines in some plots.



```
x = [10, 8, 13, 9, 11, 14, 6, 4, 12, 7, 5]
y1 = [8.04, 6.95, 7.58, 8.81, 8.33, 9.96,
      7.24, 4.26, 10.84, 4.82, 5.68]
sns.regplot(x=x, y=y1)
```

Spearman's rank correlation coefficient

It can detect **non-linear relationships**.

We first convert each variable into **ranks**:

Rank of x_i is its index in the sorted order of x_1, \dots, x_n .

Equal values get the same (average) rank.

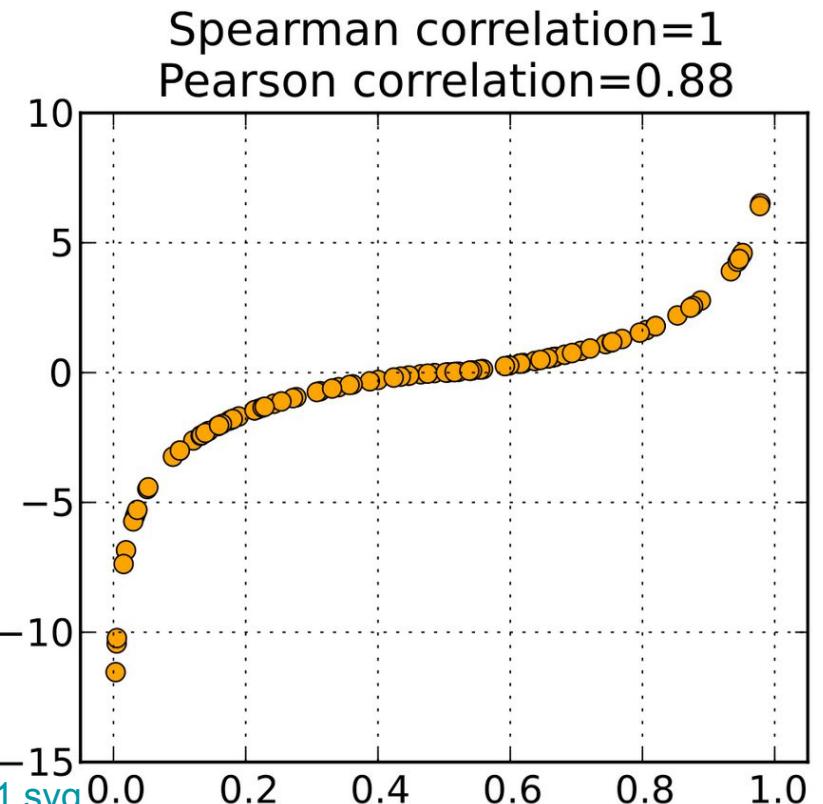
For example, the ranks of 10, 0, 10, 20, 10, 20 are 3, 1, 3, 5.5, 3, 5.5.

Then we compute **Pearson correlation coefficient of the two rank sequences**.

Properties of Spearman's rank correlation coefficient

Values of 1, -1 if y monotonically increases or decreases with x .

It is less sensitive to outliers (actual values of x and y are not important).



Computation in Pandas

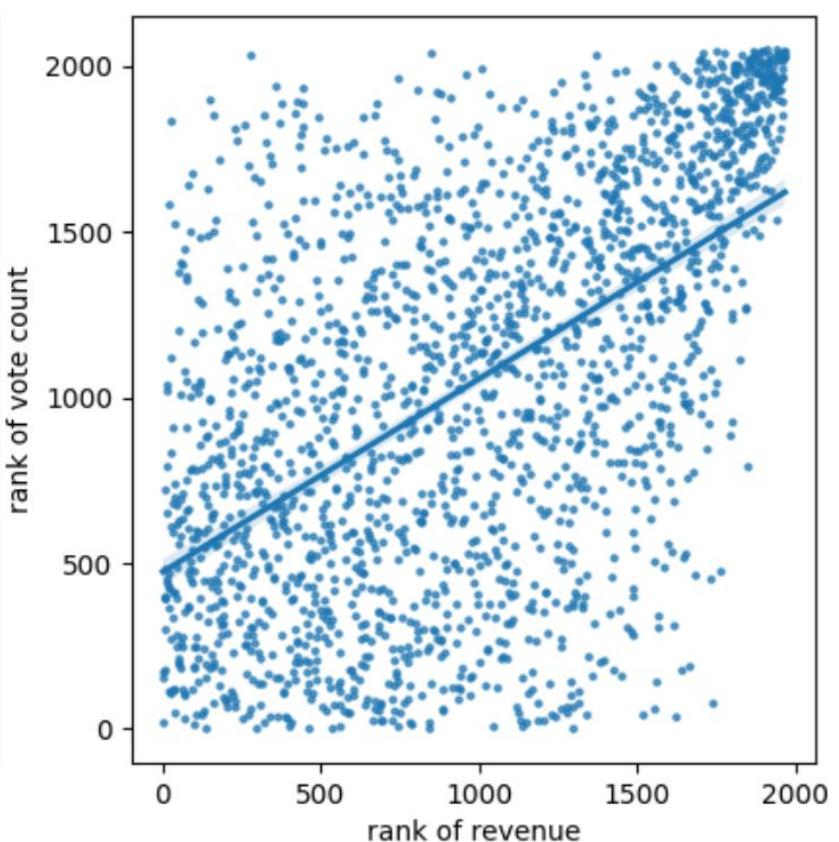
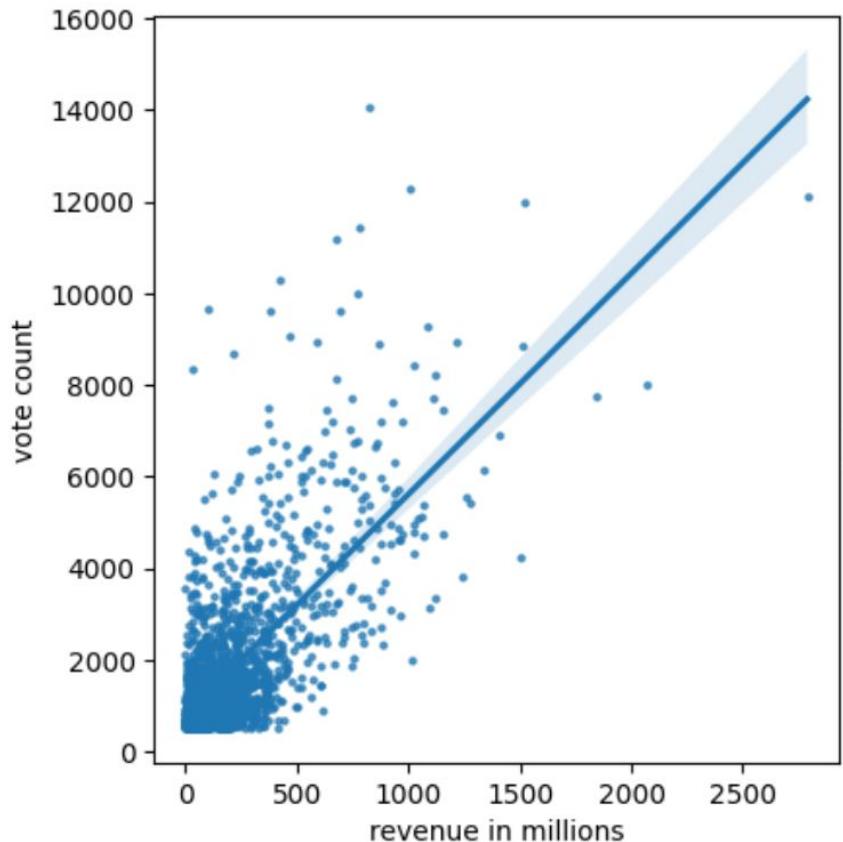
```
movies.corr(numeric_only=True)
```

| | year | budget | revenue | runtime | vote_average | vote_count |
|--------------|-------|--------|---------|---------|--------------|------------|
| year | 1.00 | 0.28 | 0.12 | -0.07 | -0.34 | 0.12 |
| budget | 0.28 | 1.00 | 0.69 | 0.22 | -0.18 | 0.47 |
| revenue | 0.12 | 0.69 | 1.00 | 0.25 | 0.06 | 0.69 |
| runtime | -0.07 | 0.22 | 0.25 | 1.00 | 0.31 | 0.25 |
| vote_average | -0.34 | -0.18 | 0.06 | 0.31 | 1.00 | 0.33 |
| vote_count | 0.12 | 0.47 | 0.69 | 0.25 | 0.33 | 1.00 |

Computation in Pandas (cont.)

```
movies.corr(method='spearman', numeric_only=True)
```

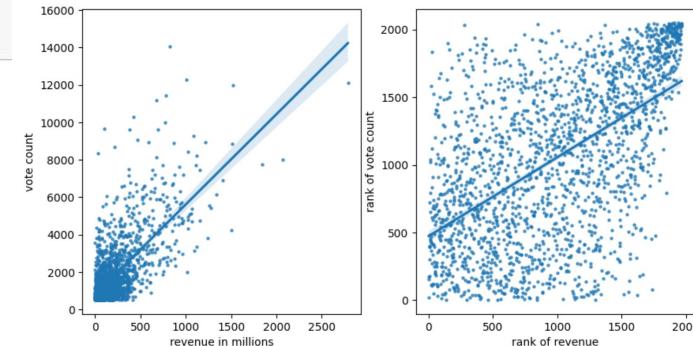
| | year | budget | revenue | runtime | vote_average | vote_count |
|--------------|-------|--------|---------|---------|--------------|------------|
| year | 1.00 | 0.21 | 0.02 | -0.03 | -0.27 | 0.14 |
| budget | 0.21 | 1.00 | 0.68 | 0.24 | -0.28 | 0.37 |
| revenue | 0.02 | 0.68 | 1.00 | 0.21 | -0.08 | 0.56 |
| runtime | -0.03 | 0.24 | 0.21 | 1.00 | 0.32 | 0.27 |
| vote_average | -0.27 | -0.28 | -0.08 | 0.32 | 1.00 | 0.29 |
| vote_count | 0.14 | 0.37 | 0.56 | 0.27 | 0.29 | 1.00 |



```

figure, axes = plt.subplots(1, 2, figsize=(10,5))
# plot of values
sns.regplot(x=movies['revenue'] / 1e6, y=movies['vote_count'],
             ax=axes[0], scatter_kws={'alpha':0.7, 's':5})
axes[0].set_xlabel('revenue in millions')
axes[0].set_ylabel('vote count')
# compute ranks
revenue_rank = movies['revenue'].rank()
vote_count_rank = movies['vote_count'].rank()
# plot of ranks
sns.regplot(x=revenue_rank, y=vote_count_rank,
             ax=axes[1], scatter_kws={'alpha':0.7, 's':5})
axes[1].set_xlabel('rank of revenue')
axes[1].set_ylabel('rank of vote count')

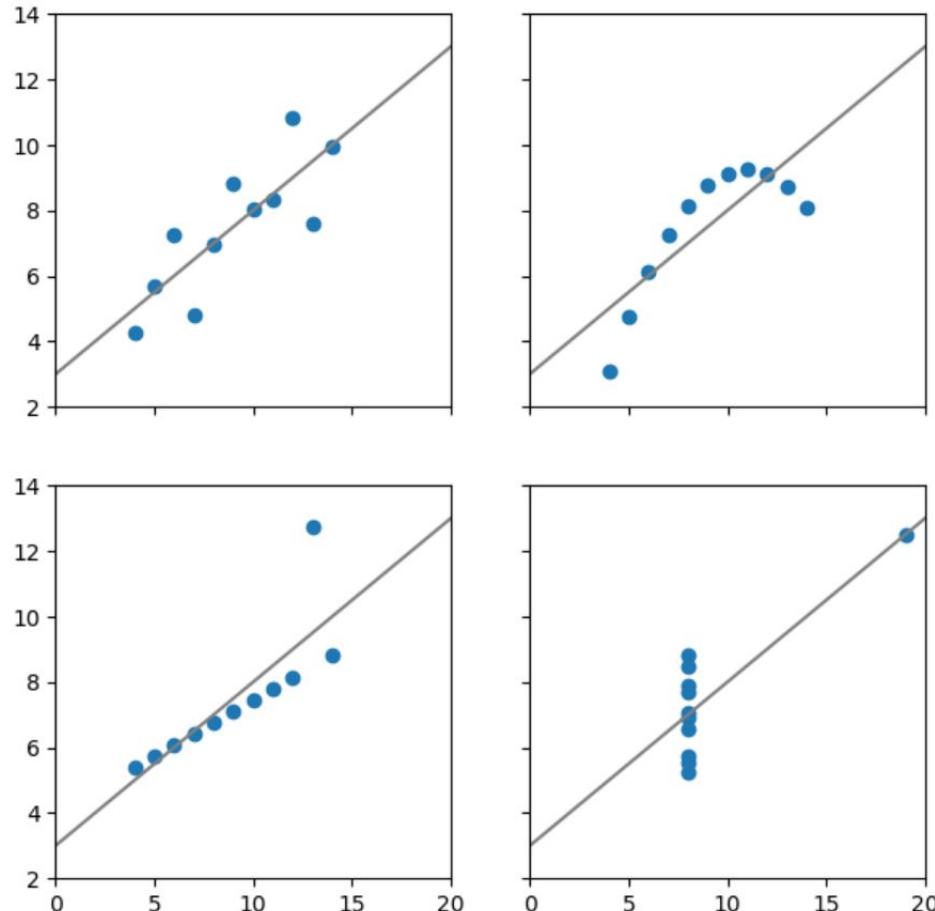
```



Anscombe's quartet

Four **artificial data sets** designed by Francis Anscombe.

The same or very similar values of:
means and variances of x and y ,
Pearson correlation coefficient
(0.816) and linear regression line.



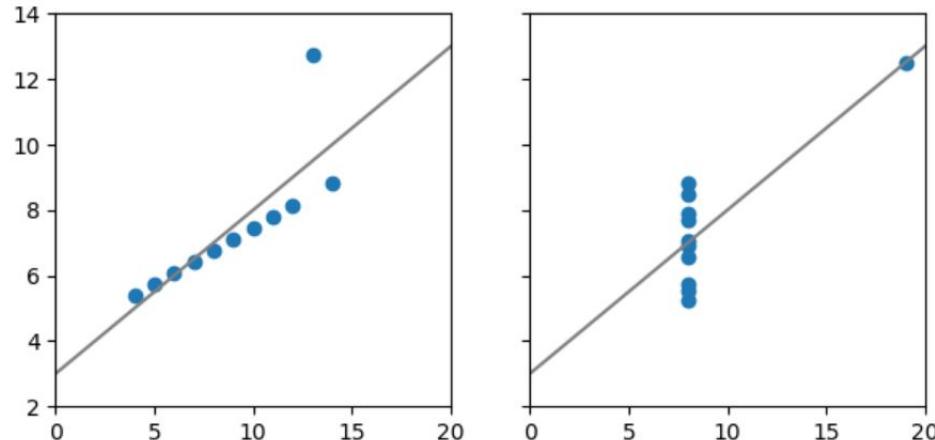
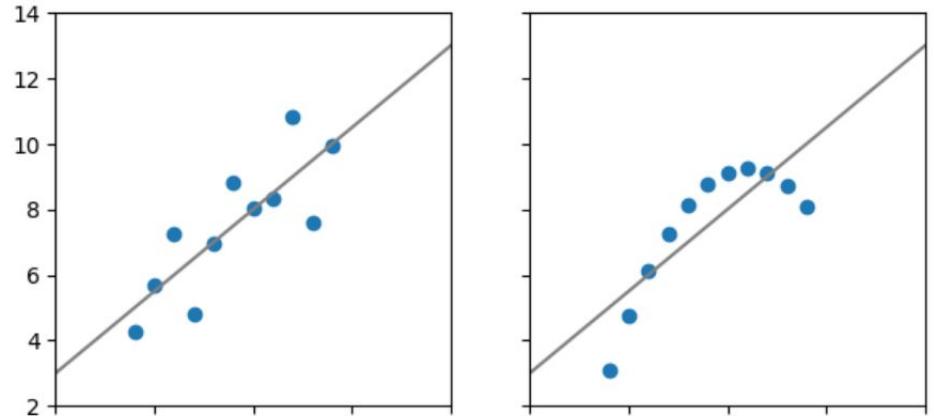
Anscombe's quartet

The same summary statistics,
but visually very different

Importance of visualization:

Plots often give us a much better idea
of the properties of a data set than
simple numerical summaries.

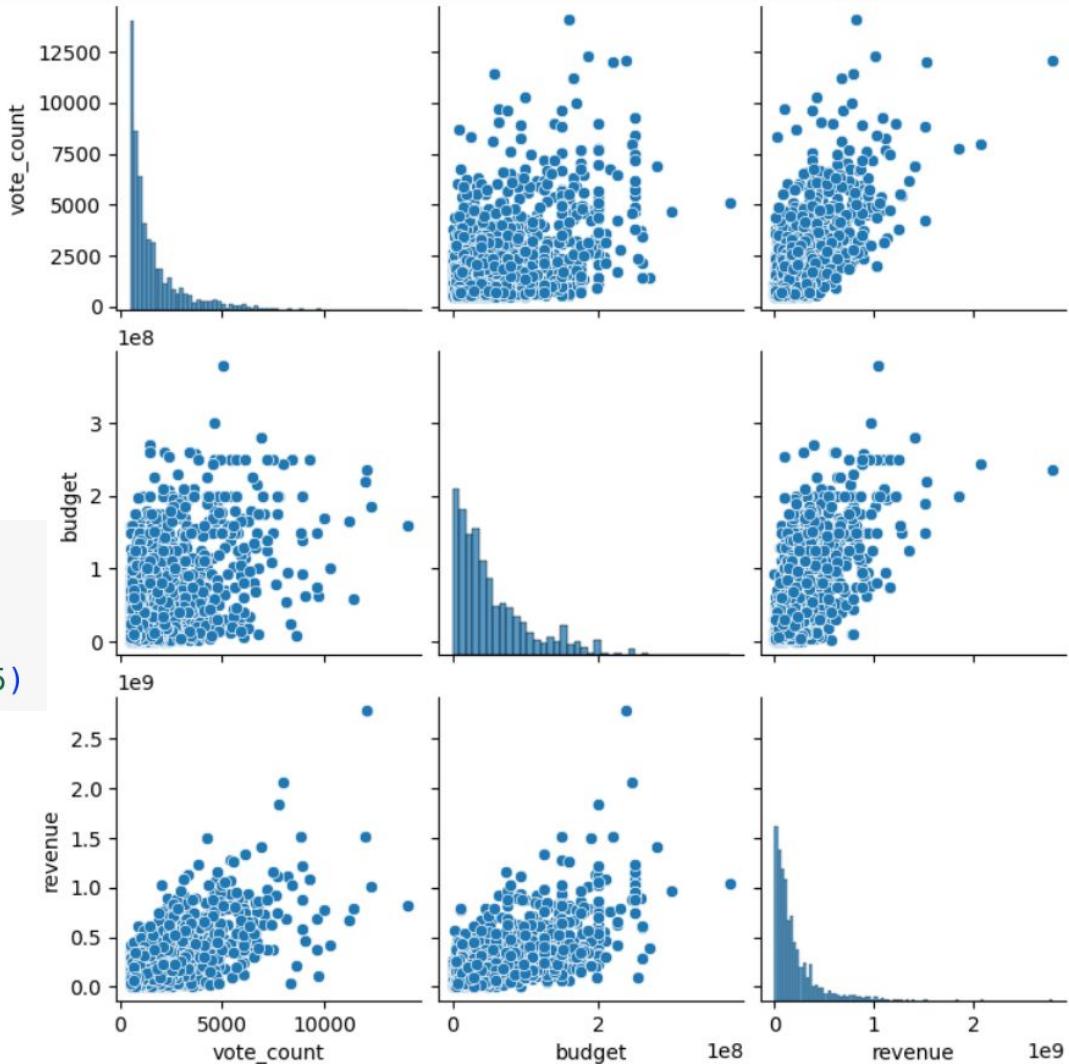
The bottom row illustrates the
influence of outliers on correlation and
regression.



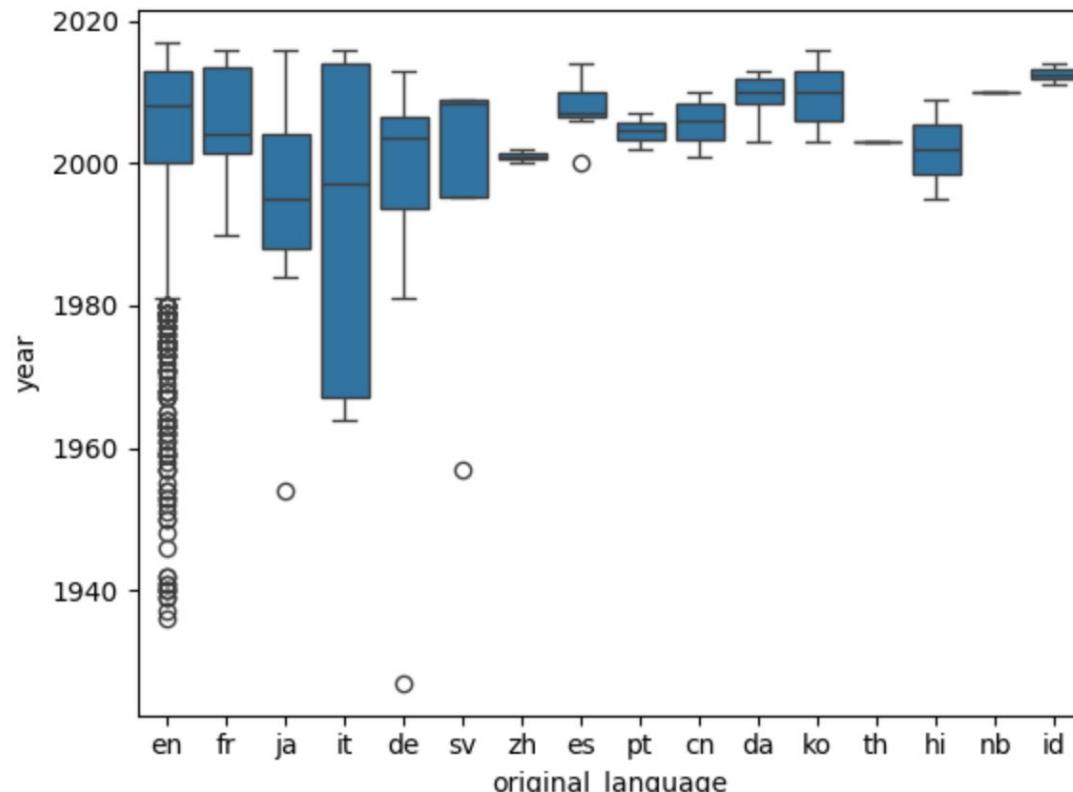
Visual overview of a data set: pairplot in Seaborn

```
subset = movies.loc[:, ['vote_count',
                       'budget',
                       'revenue']]
grid = sns.pairplot(subset, height=2.5)
```

All histograms +
scatterplots



How to compute summaries for groups?



How to compute summaries for groups?

Method `groupby` splits the table into groups based on values of some column.

We can apply a summary statistics function or `describe` on each group.

```
movies.groupby('original_language').median(numeric_only=True).head()
```

| original_language | year | budget | revenue | runtime | vote_average | vote_count |
|-------------------|----------|---------------|----------------|---------|--------------|------------|
| cn | 2,006.00 | 12,902,809.00 | 39,388,380.00 | 108.50 | 7.20 | 762.50 |
| da | 2,010.00 | 10,000,000.00 | 16,740,418.00 | 119.00 | 6.80 | 867.50 |
| de | 2,003.50 | 6,250,000.00 | 70,000,000.00 | 129.00 | 7.60 | 669.00 |
| en | 2,008.00 | 40,000,000.00 | 126,397,819.00 | 109.00 | 6.60 | 1,126.00 |
| es | 2,007.00 | 2,000,000.00 | 30,448,000.00 | 118.00 | 7.60 | 797.00 |

```
subset = movies.loc[:, ['original_language', 'year', 'budget']]
subset.groupby('original_language').describe().head(3).transpose()
```

| original_language | cn | da | de | |
|-------------------|-------|---------------|---------------|---------------|
| year | count | 4.00 | 6.00 | 8.00 |
| | mean | 2,005.75 | 2,009.33 | 1,992.50 |
| | std | 4.03 | 3.61 | 28.13 |
| | min | 2,001.00 | 2,003.00 | 1,927.00 |
| | 25% | 2,003.25 | 2,008.25 | 1,993.75 |
| | 50% | 2,006.00 | 2,010.00 | 2,003.50 |
| | 75% | 2,008.50 | 2,011.75 | 2,006.50 |
| | max | 2,010.00 | 2,013.00 | 2,013.00 |
| budget | count | 3.00 | 5.00 | 8.00 |
| | mean | 14,872,795.67 | 13,440,000.00 | 18,223,718.75 |

Summary

Summary statistics:

- mean, median, mode
- percentiles, quantiles, quartiles
- min, max, interquartile range, variance, standard deviation
- Pearson and Spearman correlation

More details in a statistics course

Visualization:

- boxplot
- scatter plots with regression lines
- pairplot

Pandas:

- functions for computing statistics, `describe`
- `groupby`

Next week: more Pandas

1 Lecture 4: Summary statistics

Data Visualization · 1-DAV-105

Lecture by Broňa Brejová

1.1 Introduction

- Summary statistics (popisné charakteristiky / štatistiky) are quantities that summarize basic properties of a single variable (a table column), such as the mean.
- We can also characterize dependencies between pairs of variables.
- Together with simple plots, such as histograms, they give us the first glimpse at the data when working with a new data set.
- We start by loading the movie data set, which we use to illustrate these terms.

1.2 Importing the movie data set

- The same data set as in group tasks 04.
- The data set describes 2049 movies.
- The data set was downloaded from <https://www.kaggle.com/rounakbanik/the-movies-dataset> and preprocessed, keeping only movies with at least 500 viewer votes.

```
[1]: import numpy as np
import pandas as pd
from IPython.display import Markdown
import matplotlib.pyplot as plt
import seaborn as sns
pd.options.display.float_format = '{:.2f}'.format
```

```
[2]: url = 'https://bbrejova.github.io/viz/data/Movies_small.csv'
movies = pd.read_csv(url)
display(movies.head())
```

| | title | year | budget | revenue | original_language | runtime | \ |
|---|-----------|------|---------------|----------------|-------------------|---------|--------|
| 0 | Toy Story | 1995 | 30,000,000.00 | 373,554,033.00 | | en | 81.00 |
| 1 | Jumanji | 1995 | 65,000,000.00 | 262,797,249.00 | | en | 104.00 |
| 2 | Heat | 1995 | 60,000,000.00 | 187,436,818.00 | | en | 170.00 |
| 3 | GoldenEye | 1995 | 58,000,000.00 | 352,194,034.00 | | en | 130.00 |
| 4 | Casino | 1995 | 52,000,000.00 | 116,112,375.00 | | en | 178.00 |

| | release_date | vote_average | vote_count | \ |
|---|--------------|--------------|------------|---|
| 0 | 1995-10-30 | 7.70 | 5,415.00 | |
| 1 | 1995-12-15 | 6.90 | 2,413.00 | |
| 2 | 1995-12-15 | 7.70 | 1,886.00 | |
| 3 | 1995-11-16 | 6.60 | 1,194.00 | |
| 4 | 1995-11-22 | 7.80 | 1,343.00 | |

| | overview |
|---|---|
| 0 | Led by Woody, Andy's toys live happily in his ... |

- 1 When siblings Judy and Peter discover an encha...
- 2 Obsessive master thief, Neil McCauley leads a ...
- 3 James Bond must unmask the mysterious head of ...
- 4 The life of the gambling paradise - Las Vegas ...

1.3 Measures of central tendency (miery stredu / polohy)

These represent a typical value in a sample x with values x_1, \dots, x_n (one numerical column of a table).

- **Mean (priemer)** $\bar{x} = \frac{\sum_{i=1}^n x_i}{n}$
 - This is the arithmetic mean, there are also geometric and harmonic means.
- **Median (medián)** is the middle value when the values ordered from smallest to largest.
 - For even n usually defined as the average of the two middle values.
 - Median of 10, 12, 15, 16, 16 is 15.
 - Median of 10, 12, 15, 16, 16, 20 is 15.5.
- **Mode (modus)** is the most frequent value (for a discrete variable).
 - Mode of 10, 12, 15, 16, 16 is 16.
 - For continuous variables, we may look for a mode in a histogram (this is sensitive to bin size).

https://commons.wikimedia.org/wiki/File:Visualisation_mode_median_mean.svg Cmglee, CC BY-SA 3.0

1.3.1 Properties of the measures

- If we apply linear transformation $a \cdot x_i + b$ with the same constants a and b to all values x_i , mean, median and mode will be also transformed in the same way.
 - This corresponds e.g. to the change in the units of measurement (grams vs kilograms, degrees C vs degrees F)
- Mean can be heavily influenced by outliers.
 - Mean of 800, 1000, 1100, 1200, 1800, 2000 and 30000 is 5414.3, median 1200.
 - Mean of 800, 1000, 1100, 1200, 1800, 2000 and 10000 is 2557.1, median 1200.
- Therefore we often prefer median (e.g. median salary).

1.3.2 Computation in Pandas

Below we apply functions `mean`, `median`, `mode` to a Series (column `year` of our table).

Note that `mode` returns a Series of results (for case of ties). Here just a single value 2013.

Note the use of `Python f-strings` to print the results.

```
[3]: display(Markdown("Properties of the column `year` in our table:"))
print(f"Mean: {movies['year'].mean():.2f}")
print(f"Median: {movies['year'].median()}")
print(f"Mode:\n{movies['year'].mode()}")
```

Properties of the column `year` in our table:

```

Mean: 2004.14
Median: 2008.0
Mode:
0    2013
Name: year, dtype: int64

```

Let us see these values in a histogram of the column values (overall view and detail).

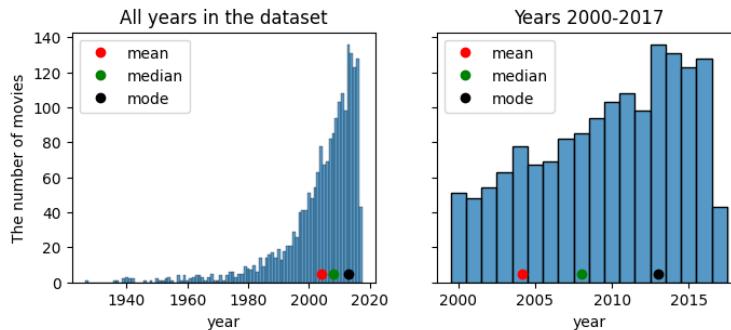
```
[4]: # set up figure with two plots
figure, axes = plt.subplots(1, 2, figsize=(8,3), sharey=True)

# plot histograms, use discrete=True to have each year in one bin
sns.histplot(data=movies, x='year', discrete=True, ax=axes[0])
sns.histplot(x=movies.query('year>=2000')['year'], discrete=True, ax=axes[1])

# titles and axis labels
axes[0].set_ylabel("The number of movies")
axes[0].set_title('All years in the dataset')
axes[1].set_title('Years 2000-2017')

# compute three summary statics, set up their color and label
stats = [{label:'mean', 'value':movies['year'].mean(), 'color':'red'},
          {'label':'median', 'value':movies['year'].median(), 'color':'green'},
          {'label':'mode', 'value':movies['year'].mode(), 'color':'black'}]
# add dots for all statistics to both plots (at y=5)
for a in axes:
    for s in stats:
        a.plot(s['value'], 5, 'o', color=s['color'], label=s['label'])
    a.legend()

pass
```



- Functions `mean` and `median` can be applied to all numerical columns in a table.
- With `axis=1` we can compute means or medians in rows.

```
[5]: display(Markdown("```\nmovies.mean(numeric_only=True)\n```"), movies.\n    ↪mean(numeric_only=True))\n\ndisplay(Markdown("```\nmovies.median(numeric_only=True)\n```"), movies.\n    ↪median(numeric_only=True))
```

```
movies.mean(numeric_only=True):\n\nyear           2,004.14\nbudget        55,108,939.70\nrevenue       198,565,134.28\nruntime        112.66\nvote_average     6.63\nvote_count      1,704.64\ndtype: float64\n\nmovies.median(numeric_only=True):\n\nyear           2,008.00\nbudget        38,000,000.00\nrevenue       122,200,000.00\nruntime        109.00\nvote_average     6.60\nvote_count      1,092.00\ndtype: float64
```

1.4 Quantiles, percentiles and quartiles (kvantly, percentilly, kvartily)

- Median is the middle value in a sorted order.
- Therefore about 50% of values are smaller and 50% larger.
- For a different percentage p , the p -th **percentile** is at position roughly $(p/100) \cdot n$ in the sorted order of values.
- Similarly **quantile** (in Pandas), but we give fraction between 0 and 1 rather than percentage.
- Specifically **quartiles** are three values Q_1 , Q_2 and Q_3 that split input data into quarters.
 - Therefore, Q_2 is the median.
- Many definitions exist regarding situations when the desired fraction falls between two values (we can take lower, higher, mean, weighted mean etc).

1.4.1 Computation in Pandas

- Function `quantile` gets a single value between 0 and 1 or a list of values and returns corresponding quantiles.
- To get quantiles for 0.1, 0.2, ..., 0.9, we generate a regular sequence of values using `np.arange`.

```
[6]: display(Markdown("```\nMedian:\n```"), movies['year'].median())\ndisplay(Markdown("```\nQuantile for 0.5:\n```"), movies['year'].quantile(0.5))\ndisplay(Markdown("```\nAll quartiles:\n```"), movies['year'].quantile([0.25, 0.5, 0.\n    ↪75]))\ndisplay(Markdown("```\nWith step 0.1:\n```"), movies['year'].quantile(np.arange(0.1,\n    ↪1, 0.1)))
```

Median:

2008.0

Quantile for 0.5:

2008.0

All quartiles:

| | |
|------|----------|
| 0.25 | 2,000.00 |
| 0.50 | 2,008.00 |
| 0.75 | 2,013.00 |

Name: year, dtype: float64

With step 0.1:

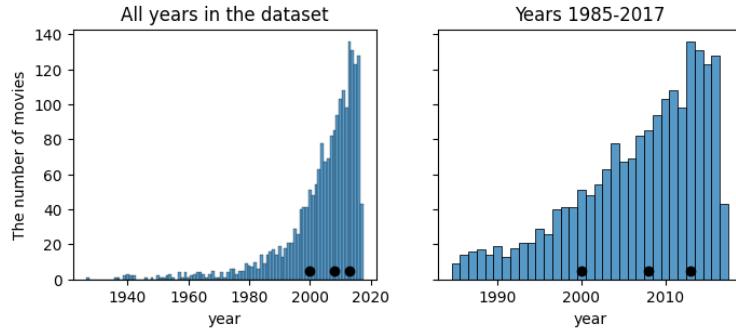
| | |
|------|----------|
| 0.10 | 1,988.80 |
| 0.20 | 1,998.00 |
| 0.30 | 2,002.00 |
| 0.40 | 2,005.00 |
| 0.50 | 2,008.00 |
| 0.60 | 2,010.00 |
| 0.70 | 2,012.00 |
| 0.80 | 2,014.00 |
| 0.90 | 2,015.00 |

Name: year, dtype: float64

The code below plots the quartiles highlighted in a histogram.

```
[7]: # setup histograms
figure, axes = plt.subplots(1, 2, figsize=(8,3), sharey=True)
sns.histplot(data=movies, x='year', discrete=True, ax=axes[0])
sns.histplot(x=movies.query('year>=1985')['year'], discrete=True, ax=axes[1])
axes[0].set_ylabel("The number of movies")
axes[0].set_title('All years in the dataset')
axes[1].set_title('Years 1985-2017')

# compute and display quartiles
quartiles = movies['year'].quantile([0.25, 0.5, 0.75])
for a in axes:
    a.plot(quartiles, [5] * len(quartiles), 'o', color='black')
pass
```



- The code below illustrates how the `quantile` function works when returning quantiles which do not correspond to a single input value.
- Optional parameter `interpolation` accepts values ‘`linear`’ (default), ‘`lower`’, ‘`higher`’, ‘`midpoint`’, ‘`nearest`’.
- Imagine the lowest element at quantile 0, the highest element at quantile 1 and the rest evenly spaced between. The quantile at position between two elements is influenced only by its two neighbors.

For example, consider list of values $[0, 10, 20, 100]$. * Values taken from the list: $p = 0: 0$, $p = 1/3: 10$, $p = 2/3: 20$, $p = 1: 100$ * Example of a different value: $p = 1/4$: by default linear interpolation at $3/4$ between 0 and 10, i.e. 7.5.

Note that linear interpolation is continuous as p changes from 0 to 1.

```
[8]: a = pd.Series([0, 100])
b = pd.Series([0, 10, 20, 30, 100])
c = pd.Series([0, 10, 20, 100])
quantiles = [0.01, 0.25, 0.5, 0.75]
display(Markdown(f"**Quantiles for {list(a)}**"), a.quantile(quantiles))
display(Markdown(f"**Quantiles for {list(b)}**"), b.quantile(quantiles))
display(Markdown(f"**Quantiles for {list(c)}**"), c.quantile(quantiles))
display(Markdown(f"**Quantiles for {list(c)} with `interpolation='lower'"**"),
       c.quantile(quantiles, interpolation='lower'))
```

Quantiles for [0, 100]

```
0.01    1.00
0.25   25.00
0.50   50.00
0.75   75.00
dtype: float64
```

Quantiles for [0, 10, 20, 30, 100]

```
0.01    0.40
0.25   10.00
0.50   20.00
```

```
0.75    30.00
dtype: float64
```

Quantiles for [0, 10, 20, 100]

```
0.01    0.30
0.25    7.50
0.50    15.00
0.75    40.00
dtype: float64
```

Quantiles for [0, 10, 20, 100] with interpolation='lower'

```
0.01    0
0.25    0
0.50    10
0.75    20
dtype: int64
```

1.5 Measures of variability (miery variability)

- Values in the sample may be close to their mean or median, or they can spread widely.
- It is important to consider how representative is the mean or median of the whole set.

Examples of measures:

- Range of values from **minimum** to **maximum** (sensitive to outliers).
- **Interquartile range IQR** (kvartilové rozpätie): range between Q_1 and Q_3 (contains the middle half of the data).
- Variance and standard deviation (described next).

1.5.1 Variance and standard deviation (rozptyl a smerodajná odchýlka)

Variance

- For each value in the sample compute its difference from the mean and square it: $(x_i - \bar{x})^2$.
- After squaring, we get non-negative values (and squares are easier to work with mathematically than absolute values).
- Variance is the mean of these squares, but we divide by $n - 1$ rather than n :

$$s^2 = \frac{\sum_{i=1}^n (x_i - \bar{x})^2}{n - 1}$$

- We divide by $n - 1$ rather than n , because we would otherwise underestimate the true variance of the underlying population (more in the statistics course).
- For large n , the difference between dividing by n and $n - 1$ is negligible.

Standard deviation

- Square root of the variance

$$s = \sqrt{s^2}$$

- It is expressed in the same units as the original values (variance is in units squared).

Properties

- Larger variance and standard deviation mean that data are spread farther from the mean
- If we apply linear transformation $a \cdot x_i + b$ with the same constants a and b to all values x_i :
 - Neither variance nor standard deviation change with b .
 - Variance is multiplied by a^2 , standard deviation by $|a|$.
- These measures are strongly influenced by outliers:
 - For 800, 1000, 1100, 1200, 1800, 2000, 30000 st. dev. is 10850.0, IQR 850.
 - For 800, 1000, 1100, 1200, 1800, 2000, 10000 st. dev. is 3310.5, IQR 850.

1.5.2 Computation in Pandas

We can use functions `min`, `max`, `std`, `var`, which work similarly to `mean`.

```
[9]: display(Markdown(""), movies['year'].min())
display(Markdown(""), movies['year'].max())
display(Markdown(""), movies['year'].mean())
display(Markdown(""), movies['year'].var())
display(Markdown(""), movies['year'].std())
q1 = movies['year'].quantile(0.25)
q3 = movies['year'].quantile(0.75)
display(Markdown(""), q1, q3, q3-q1)
```

Minimum

1927

Maximum

2017

Mean

2004.1449487554905

Variance

161.2714600681735

Standard deviation

12.699270060447313

Q1, Q3 and interquartile range:

2000.0

2013.0

13.0

1.6 Outliers (odníahlé hodnoty)

- Outliers are the values which are far from the typical range of values.
- In data analysis, it is important to **check the outliers**.
- If they represent errors, we may try to correct or remove them.

- They can also represent interesting anomalies.
- Different definitions of outliers may be appropriate in different situations.
- The criterion by statistician John Tukey is often used:
 - Outliers are the values outside of the range $Q_1 - k \cdot IQR, Q_3 + k \cdot IQR$, e.g. for $k = 1.5$.
- In our example 800, 1000, 1100, 1200, 1800, 2000, 30000:
 - $Q_1 = 1050, Q_3 = 1900, IQR = 850$.
 - $Q_1 - 1.5 \cdot IQR = -225, Q_3 + 1.5 \cdot IQR = 3175$.
 - Outliers are values smaller than -225 or larger than 3175 ; here only 30000.
 - The range of outliers is not influenced if we change outliers values (as long as they stay outside of range Q1-Q3).

1.6.1 Computation in Pandas

- The code below finds outliers in the `year` column.
- We compute the lower and upper thresholds manually from quartiles.
- Then we use `query` to select rows and count how many there are.
- Function `count` counts the values in a Series or columns of a DataFrame, ignoring missing values.

```
[10]: # get quartiles and iqr
q1 = movies['year'].quantile(0.25)
q3 = movies['year'].quantile(0.75)
iqr = q3 - q1
# compute thresholds for outliers
lower = q1 - 1.5 * iqr
upper = q3 + 1.5 * iqr
# count outliers
count = movies.query('year < @lower or year > @upper')['year'].count()
# print results
display(Markdown(f"**Outliers outside of range:** [{lower}, {upper}]"))
display(Markdown(f"**Outlier count:** {count}"))
display(Markdown(f"**Total count:** {movies['year'].count()}"))
```

Outliers outside of range: [1980.5, 2032.5]

Outlier count: 112

Total count: 2049

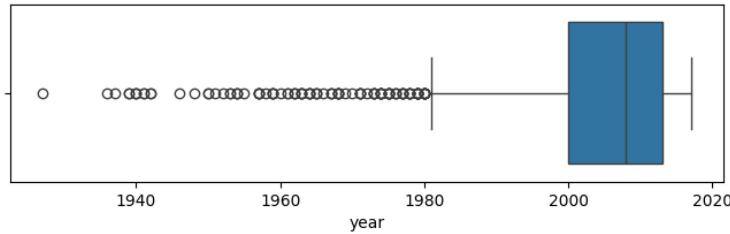
1.7 Boxplot (krabicový graf)

- Boxplots were developed by [Mary Eleanor Hunt Spear](#) and [John Tukey](#).
- For a single numerical variable it shows the **five-number summary** consisting of the minimum, Q_1 , median (Q_2), Q_3 and the maximum.
- Median is shown as a thick line, Q_1 and Q_3 as a box and minimum and maximum as “whiskers”.
- Outliers are often excluded from the whiskers and shown as individual points.
- Summaries of different samples are often compared in a single boxplot.
- Boxplots allow clear comparison of basic characteristics.

1.7.1 Boxplots in Seaborn

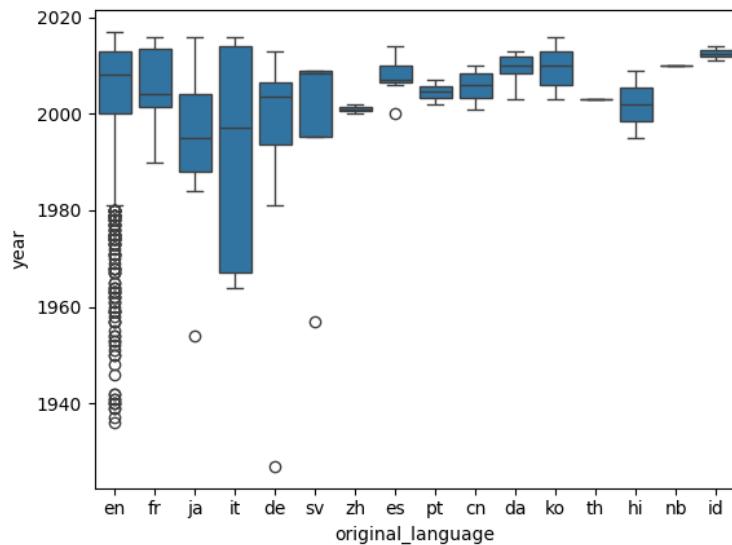
- We use `boxplot` function from Seaborn.
- Below is a simple horizontal boxplot of the `year` column.
- Recall that quartiles are 2000, 2008 and 2013, minimum 1927, maximum 2017, outliers outside of [1980.5, 2032.5].

```
[11]: axes = sns.boxplot(data=movies, x='year')
axes.figure.set_size_inches(8,2)
```



- Below is a vertical boxplot of the `year` column split into groups according to language.
- This is achieved by specifying both `x` and `y` options.

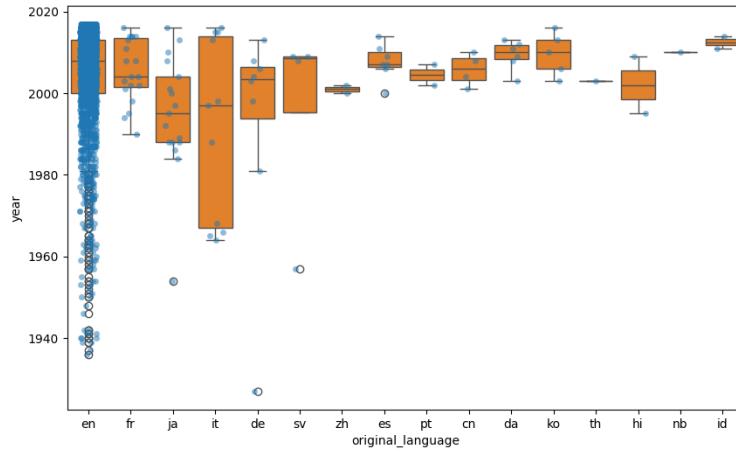
```
[12]: sns.boxplot(data=movies, x='original_language', y='year')
pass
```



- Below we draw a strip plot on top of the boxplot.
- This allows us to see both individual data points and the summary.
- Here it does not work very well for `en`, better suited for smaller datasets.

- We see that some languages have extremely low number of points, boxplots not ideal in that case.

```
[13]: axes = sns.boxplot(data=movies, x='original_language', y='year', color='C1')
sns.stripplot(data=movies, x='original_language', y='year', color='C0',
               alpha=0.5, size=5, jitter=0.2)
axes.figure.set_size_inches(10,6)
pass
```



1.8 Quick overview of a data set: `describe` in Pandas

Function `describe` gives a quick overview of a data set with many statistics described today.

```
[14]: movies.describe()
```

```
[14]:      year      budget      revenue  runtime  vote_average \
count  2,049.00    1,959.00    1,965.00  2,049.00    2,049.00
mean   2,004.14  55,108,939.70  198,565,134.28   112.66      6.63
std     12.70  53,139,663.86  233,028,732.94    24.76      0.77
min    1,927.00        1.00        15.00      7.00      4.00
25%   2,000.00  16,000,000.00   52,882,018.00     97.00      6.10
50%   2,008.00  38,000,000.00  122,200,000.00    109.00      6.60
75%   2,013.00  75,000,000.00  250,200,000.00    124.00      7.20
max   2,017.00 380,000,000.00 2,787,965,087.00    705.00      9.10

      vote_count
count      2,049.00
mean       1,704.64
std        1,607.89
min         501.00
25%        709.00
50%       1,092.00
```

```
75%      2,000.00
max     14,075.00
```

- By default `describe` only considers numerical columns.
- Other columns can be included by `include='all'`.
- Different statistics reported for categorical columns (`unique`, `top`, `freq`).

```
[15]: movies.describe(include='all').transpose()
```

| | count | unique | \ |
|-------------------|----------|--------|---|
| title | 2049 | 2018 | |
| year | 2,049.00 | NaN | |
| budget | 1,959.00 | NaN | |
| revenue | 1,965.00 | NaN | |
| original_language | 2049 | 16 | |
| runtime | 2,049.00 | NaN | |
| release_date | 2049 | 1740 | |
| vote_average | 2,049.00 | NaN | |
| vote_count | 2,049.00 | NaN | |
| overview | 2049 | 2049 | |

| | top | freq | \ |
|-------------------|---|------|---|
| title | Beauty and the Beast | 3 | |
| year | NaN | NaN | |
| budget | NaN | NaN | |
| revenue | NaN | NaN | |
| original_language | en | 1958 | |
| runtime | NaN | NaN | |
| release_date | 2014-12-25 | 6 | |
| vote_average | NaN | NaN | |
| vote_count | NaN | NaN | |
| overview | Led by Woody, Andy's toys live happily in his ... | 1 | |

| | mean | std | min | 25% | \ |
|-------------------|----------------|----------------|----------|---------------|---|
| title | NaN | NaN | NaN | NaN | |
| year | 2,004.14 | 12.70 | 1,927.00 | 2,000.00 | |
| budget | 55,108,939.70 | 53,139,663.86 | 1.00 | 16,000,000.00 | |
| revenue | 198,565,134.28 | 233,028,732.94 | 15.00 | 52,882,018.00 | |
| original_language | Nan | Nan | NaN | NaN | |
| runtime | 112.66 | 24.76 | 7.00 | 97.00 | |
| release_date | Nan | Nan | NaN | NaN | |
| vote_average | 6.63 | 0.77 | 4.00 | 6.10 | |
| vote_count | 1,704.64 | 1,607.89 | 501.00 | 709.00 | |
| overview | NaN | NaN | NaN | NaN | |

| | 50% | 75% | max |
|-------|-----|-----|-----|
| title | NaN | NaN | NaN |

| | | | |
|-------------------|----------------|----------------|------------------|
| year | 2,008.00 | 2,013.00 | 2,017.00 |
| budget | 38,000,000.00 | 75,000,000.00 | 380,000,000.00 |
| revenue | 122,200,000.00 | 250,200,000.00 | 2,787,965,087.00 |
| original_language | Nan | Nan | Nan |
| runtime | 109.00 | 124.00 | 705.00 |
| release_date | Nan | Nan | Nan |
| vote_average | 6.60 | 7.20 | 9.10 |
| vote_count | 1,092.00 | 2,000.00 | 14,075.00 |
| overview | Nan | Nan | Nan |

1.9 Correlation (korelácia)

- We are often interested in relationships among different variables (data columns).
- We will see two correlation coefficients that measure the strength of such relationships.
- Beware: **correlation does not imply causation**.
 - If electricity consumption grows in a very cold weather, there might be **cause-and-effect** relationship: the cold weather is causing people to use more electricity for heating.
 - If healthier people tend to be happier, which is the cause and which is effect?
 - Both studied variables can be also influenced by some third, unknown factor. For example, within a year, deaths by drowning increase with increased ice cream consumption. Both increases are spurred by warm weather.
 - The observed correlation can be just a coincidence, see the [Redskins rule](#) and a specialized webpage [Spurious Correlations](#).
 - You can easily find such “coincidences” by comparing many pairs of variables (a practice called data dredging).

1.9.1 Pearson correlation coefficient

- It measures linear relationship between two variables.
- Consider pairs of values $(x_1, y_1), \dots, (x_n, y_n)$, where (x_i, y_i) are two different features of the same object.

$$r = \frac{\sum_{i=1}^n (x_i - \bar{x})(y_i - \bar{y})}{\sqrt{\sum_{i=1}^n (x_i - \bar{x})^2} \sqrt{\sum_{i=1}^n (y_i - \bar{y})^2}}$$

- Or equivalently:

$$r = \frac{1}{n-1} \sum_{i=1}^n \left(\frac{x_i - \bar{x}}{s_x} \right) \left(\frac{y_i - \bar{y}}{s_y} \right).$$

- where s_x is the standard deviation of variable x .
- Expression $(x_i - \bar{x})/s_x$ is called the **standard score** or **z-score**, and it tells us how many standard deviations above or below the mean value x_i is.
- The product of $(x_i - \bar{x})/s_x$ and $(y_i - \bar{y})/s_y$ is positive if x_i and y_i lie on the same side of the respective means of x and y and negative if they lie on the opposite sides.

1.9.2 Properties of Pearson correlation coefficient

Values of Pearson correlation coefficient

- The value of r is always from interval $[-1, 1]$.

- It is 1 if y grows linearly with x , -1 if y decreases linearly with increasing x .
- Zero means no correlation.
- Values between 0 and 1 mean intermediate value of positive correlation, values between -1 and 0 negative correlation.

https://commons.wikimedia.org/wiki/File:Correlation_coefficient.png Kiatdd, CC BY-SA 3.0

Some cautions

- Pearson correlation measures only linear relationships (x and y in the bottom row have non-linear relationships but their correlation is 0).
- Pearson correlation does not depend on the slope of the best-fit line (see the middle row below).

https://commons.wikimedia.org/wiki/File:Correlation_examples2.svg public domain

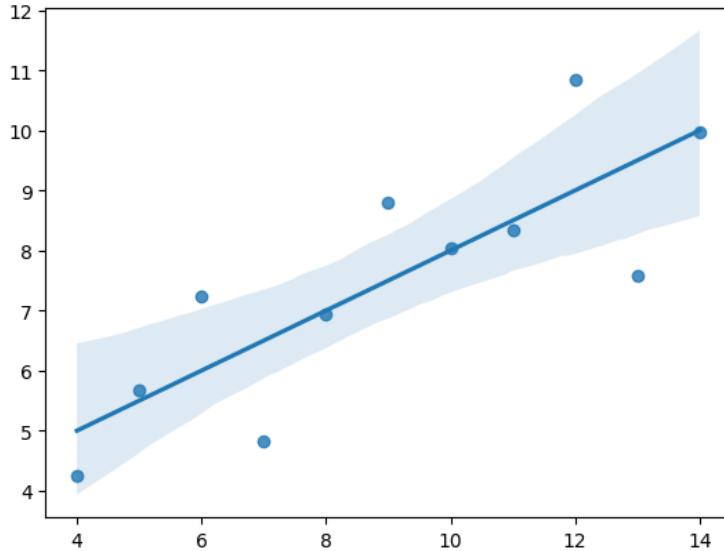
Other properties

- Pearson correlation does not change if we linearly scale each variable, i.e. $ax_i + b$, $cy_i + d$ (for $a, c > 0$).
- Pearson correlation is symmetric $r_{x,y} = r_{y,x}$.

1.9.3 Linear regression

- The process of finding the line best representing the relationship of x and y is called linear regression.
- It can be used in higher dimensions to predict one variable as a linear combination of many others.
- You will study linear regression in later courses, but we may draw regression lines in some plots.

```
[16]: x = [10, 8, 13, 9, 11, 14, 6, 4, 12, 7, 5]
y1 = [8.04, 6.95, 7.58, 8.81, 8.33, 9.96, 7.24, 4.26, 10.84, 4.82, 5.68]
sns.regplot(x=x, y=y1)
pass
```



1.9.4 Spearman's rank correlation coefficient

- It can detect non-linear relationships.
- We first convert each variable into ranks:
 - Rank of x_i is its index in the sorted order of x_1, \dots, x_n .
 - Equal values get the same (average) rank.
 - For example, the ranks of 10, 0, 10, 20, 10, 20 are 3, 1, 3, 5.5, 3, 5.5.
- Then we compute Pearson correlation coefficient of the two rank sequences.
- Values of 1, -1 if y monotonically increases or decreases with x .
- It is less sensitive to distant outliers (actual values of x and y are not important).

https://commons.wikimedia.org/wiki/File:Spearman_fig1.svg Skbkekas, CC BY-SA 3.0

1.9.5 Computation in Pandas

Function `corr` computes correlation between all pairs of numerical columns. There is also a `version` to compare two Series.

In our table, the highest Pearson correlation is 0.69 for pairs (`budget, revenue`), (`vote_count, revenue`)

```
[17]: movies.corr(numeric_only=True)
```

| | year | budget | revenue | runtime | vote_average | vote_count |
|--------------|-------|--------|---------|---------|--------------|------------|
| year | 1.00 | 0.28 | 0.12 | -0.07 | -0.34 | 0.12 |
| budget | 0.28 | 1.00 | 0.69 | 0.22 | -0.18 | 0.47 |
| revenue | 0.12 | 0.69 | 1.00 | 0.25 | 0.06 | 0.69 |
| runtime | -0.07 | 0.22 | 0.25 | 1.00 | 0.31 | 0.25 |
| vote_average | -0.34 | -0.18 | 0.06 | 0.31 | 1.00 | 0.33 |
| vote_count | 0.12 | 0.47 | 0.69 | 0.25 | 0.33 | 1.00 |

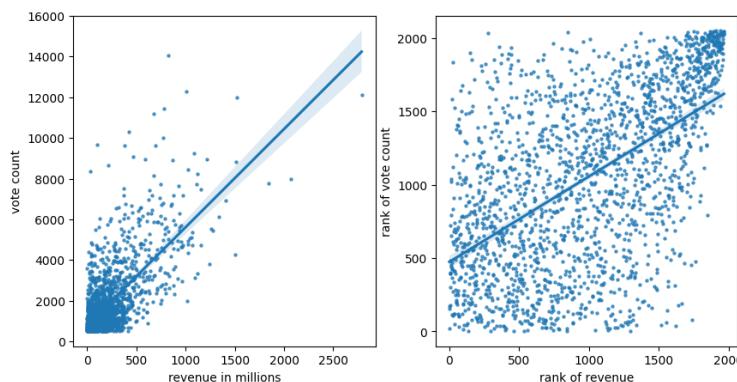
With Spearman rank correlation, the correlation between `revenue` and `budget` remains similar, but correlation between `vote_count` and `budget` decreases from 0.69 to 0.56.

```
[18]: movies.corr(method='spearman', numeric_only=True)
```

| | year | budget | revenue | runtime | vote_average | vote_count |
|--------------|-------|--------|---------|---------|--------------|------------|
| year | 1.00 | 0.21 | 0.02 | -0.03 | -0.27 | 0.14 |
| budget | 0.21 | 1.00 | 0.68 | 0.24 | -0.28 | 0.37 |
| revenue | 0.02 | 0.68 | 1.00 | 0.21 | -0.08 | 0.56 |
| runtime | -0.03 | 0.24 | 0.21 | 1.00 | 0.32 | 0.27 |
| vote_average | -0.27 | -0.28 | -0.08 | 0.32 | 1.00 | 0.29 |
| vote_count | 0.14 | 0.37 | 0.56 | 0.27 | 0.29 | 1.00 |

- Here we illustrate the regression line for `revenue` versus `vote_count`.
- We use Seaborn `regplot` to draw scatterplot together with the regression line.
- Points are made smaller and transparent by `scatter_kws={'alpha':0.7, 's':5}`.
- The plot on the right shows ranks instead of actual values.
- Ranks are computed using `rank` function for Series.
- Pearson correlation coefficient is probably driven by outliers.

```
[19]: # figure with two plots
figure, axes = plt.subplots(1, 2, figsize=(10,5))
# plot of values
sns.regplot(x=movies['revenue'] / 1e6, y=movies['vote_count'],
             ax=axes[0], scatter_kws={'alpha':0.7, 's':5})
axes[0].set_xlabel('revenue in millions')
axes[0].set_ylabel('vote count')
# compute ranks
revenue_rank = movies['revenue'].rank()
vote_count_rank = movies['vote_count'].rank()
# plot of ranks
sns.regplot(x=revenue_rank, y=vote_count_rank,
             ax=axes[1], scatter_kws={'alpha':0.7, 's':5})
axes[1].set_xlabel('rank of revenue')
axes[1].set_ylabel('rank of vote count')
pass
```



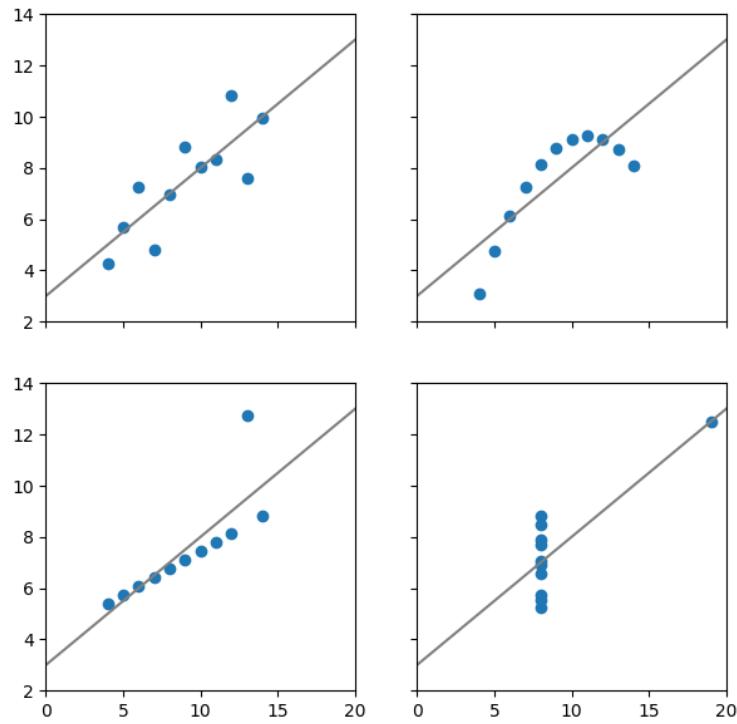
1.10 Anscombe's quartet and importance of visualization

- Anscombe's quartet are four artificial [data sets](#) designed by [Francis Anscombe](#).
- All have the same or very similar values of means and variances of both x and y , Pearson correlation coefficient (0.816) and linear regression line.
- But visually we see each has a very different character.
- The bottom row illustrates the influence of outliers on correlation and regression.
- Overall this shows that plots give us a much better idea of the properties of a data set than simple numerical summaries.

```
[20]: # adapted from https://matplotlib.org/stable/gallery/specialty_plots/anscombe.
↪html
x = [10, 8, 13, 9, 11, 14, 6, 4, 12, 7, 5]
y1 = [8.04, 6.95, 7.58, 8.81, 8.33, 9.96, 7.24, 4.26, 10.84, 4.82, 5.68]
y2 = [9.14, 8.14, 8.74, 8.77, 9.26, 8.10, 6.13, 3.10, 9.13, 7.26, 4.74]
y3 = [7.46, 6.77, 12.74, 7.11, 7.81, 8.84, 6.08, 5.39, 8.15, 6.42, 5.73]
x4 = [8, 8, 8, 8, 8, 8, 19, 8, 8, 8]
y4 = [6.58, 5.76, 7.71, 8.84, 8.47, 7.04, 5.25, 12.50, 5.56, 7.91, 6.89]
datasets = [(x, y1), (x, y2), (x, y3), (x4, y4)]

figure, axes = plt.subplots(2, 2, sharex=True, sharey=True, figsize=(7, 7))
axes[0, 0].set(xlim=(0, 20), ylim=(2, 14))

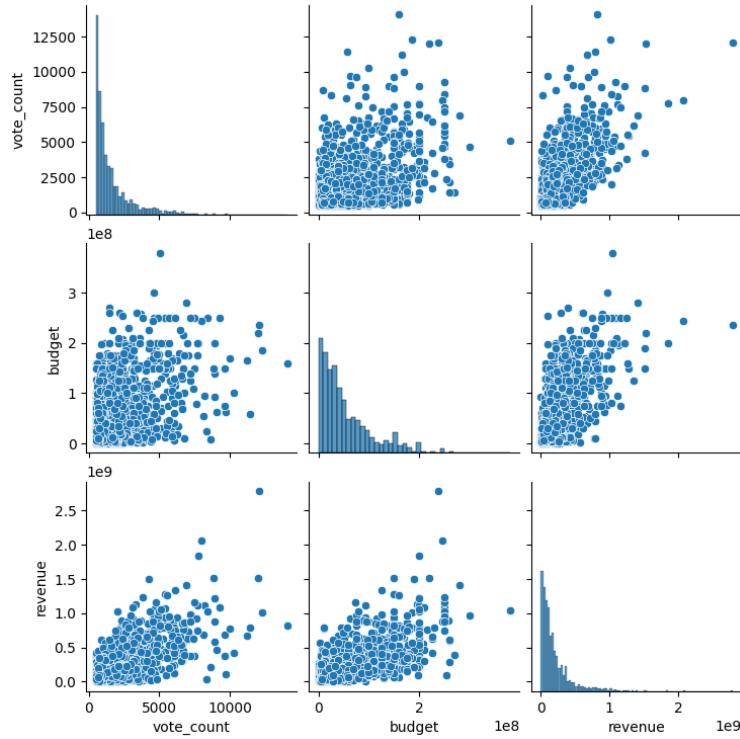
for ax, (x, y) in zip(axes.flat, datasets):
    ax.plot(x, y, 'o')
    # linear regression
    slope, intercept = np.polyfit(x, y, deg=1)
    ax.axline(xy1=(0, intercept), slope=slope, color='gray')
```



1.10.1 Visual overview of a data set: pairplot in Seaborn

- Seaborn `pairplot` generates a matrix of plots for all numerical columns.
- The diagonal contains histograms of individual columns.
- Off-diagonal entries are scatterplots of two columns.
- Here only 3 columns shown for simpler examination.

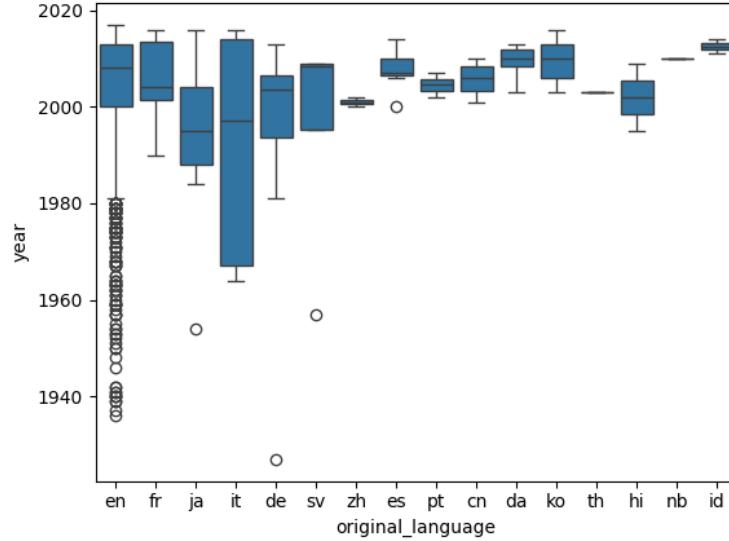
```
[21]: subset = movies.loc[:, ['vote_count', 'budget', 'revenue']]
grid = sns.pairplot(subset, height=2.5)
pass
```



1.11 Computing summaries of subsets of data: groupby from Pandas

- We have seen that Seaborn can create plots where data are split into groups according to a categorical variable.
- One example are boxplots, which we have seen today.
- How can we compute summary statistics for each such group in Pandas?

```
[22]: sns.boxplot(data=movies, x='original_language', y='year')
      pass
```



- Pandas DataFrame supports function `groupby` which splits the table into groups based on values of some column.
- We can apply a summary statistics function on each group.
- Below we compute medians of all numerical columns for each language and show the first 5 languages.

```
[23]: movies.groupby('original_language').median(numeric_only=True).head()
```

```
[23]:      year      budget      revenue  runtime \
original_language
cn        2,006.00  12,902,809.00  39,388,380.00    108.50
da        2,010.00 10,000,000.00  16,740,418.00    119.00
de        2,003.50  6,250,000.00  70,000,000.00    129.00
en        2,008.00 40,000,000.00 126,397,819.00    109.00
es        2,007.00  2,000,000.00  30,448,000.00    118.00

      vote_average  vote_count
original_language
cn            7.20      762.50
da            6.80      867.50
de            7.60      669.00
en            6.60     1,126.00
es            7.60      797.00
```

- We can also apply `describe` on the `groupby` groups.
- Here only two numerical columns of the original table are shown.

```
[24]: subset = movies.loc[:, ['original_language', 'year', 'budget']]
subset.groupby('original_language').describe().head()
```

[24] :

| | year | | | | | | | \ |
|-------------------|---------------|---------------|---------------|----------------|---------------|----------|----------|---|
| | count | mean | std | min | 25% | 50% | 75% | |
| original_language | | | | | | | | |
| cn | 4.00 | 2,005.75 | 4.03 | 2,001.00 | 2,003.25 | 2,006.00 | 2,008.50 | |
| da | 6.00 | 2,009.33 | 3.61 | 2,003.00 | 2,008.25 | 2,010.00 | 2,011.75 | |
| de | 8.00 | 1,992.50 | 28.13 | 1,927.00 | 1,993.75 | 2,003.50 | 2,006.50 | |
| en | 1,958.00 | 2,004.30 | 12.54 | 1,936.00 | 2,000.00 | 2,008.00 | 2,013.00 | |
| es | 7.00 | 2,007.71 | 4.39 | 2,000.00 | 2,006.50 | 2,007.00 | 2,010.00 | |
| | | | | | | | | |
| | budget | | | | | | | \ |
| | max | count | mean | std | min | | | |
| original_language | | | | | | | | |
| cn | 2,010.00 | 3.00 | 14,872,795.67 | 4,479,793.25 | 11,715,578.00 | | | |
| da | 2,013.00 | 5.00 | 13,440,000.00 | 12,369,640.25 | 3,800,000.00 | | | |
| de | 2,013.00 | 8.00 | 18,223,718.75 | 30,623,544.47 | 1,530,000.00 | | | |
| en | 2,017.00 | 1,891.00 | 56,637,200.97 | 53,394,829.52 | | 1.00 | | |
| es | 2,014.00 | 5.00 | 7,500,000.00 | 8,046,738.47 | 1,500,000.00 | | | |
| | | | | | | | | |
| | 25% | 50% | 75% | max | | | | |
| original_language | | | | | | | | |
| cn | 12,309,193.50 | 12,902,809.00 | 16,451,404.50 | 20,000,000.00 | | | | |
| da | 7,400,000.00 | 10,000,000.00 | 11,000,000.00 | 35,000,000.00 | | | | |
| de | 4,100,000.00 | 6,250,000.00 | 15,084,937.50 | 92,620,000.00 | | | | |
| en | 18,000,000.00 | 40,000,000.00 | 80,000,000.00 | 380,000,000.00 | | | | |
| es | 2,000,000.00 | 2,000,000.00 | 13,000,000.00 | 19,000,000.00 | | | | |

1.12 Summary

We have seen several summary statistics:

- mean, median, mode
- percentiles, quantiles, quartiles
- min, max, interquartile range, variance, standard deviation
- Pearson and Spearman correlation

Visualization:

- boxplot
- scatter plots with regression lines
- pairplot

Pandas:

- functions for computing statistics, `describe`
- `groupby`
- next week: more Pandas

More details in a statistics course.

1 Lecture 5: Advanced Pandas

Data Visualization · 1-DAV-105

Lecture by Broňa Brejová

As usual, we start by importing libraries. We also import the country data set from World Bank <https://databank.worldbank.org/home> under CC BY 4.0 license (see Lecture 03b).

```
[1]: import numpy as np
import pandas as pd
from IPython.display import Markdown
import matplotlib.pyplot as plt
import seaborn as sns
pd.options.display.float_format = '{:.2f}'.format
```

```
[2]: url = 'https://bbrejova.github.io/viz/data/World_bank.csv'
countries = pd.read_csv(url).set_index('Country')
```

1.1 Hierarchical index (MultiIndex)

1.1.1 A small example table

To illustrate a hierarchical index, we first create a very small table consisting of two countries and their population in two years, and convert this table from wide to long format.

```
[3]: example_countries = countries.loc[['Slovak Republic', 'Austria'],
                                       ['Population2010', 'Population2020']]
display(Markdown("**A small subset of countries table:**"), example_countries)
# change to long format
example_long = (example_countries.reset_index()
                 .melt(id_vars=['Country'],
                       var_name='Year',
                       value_name='Population'))
# change year from string such as "Population2010" to int 2010
example_long.Year = example_long.Year.apply(lambda x : int(x[-4:]))
display(Markdown("**Changed to long format:**"), example_long)
```

A small subset of countries table:

| | Population2010 | Population2020 |
|-----------------|----------------|----------------|
| Country | | |
| Slovak Republic | 5,391,428.00 | 5,458,827.00 |
| Austria | 8,363,404.00 | 8,916,864.00 |

Changed to long format:

| | Country | Year | Population |
|---|-----------------|------|--------------|
| 0 | Slovak Republic | 2010 | 5,391,428.00 |
| 1 | Austria | 2010 | 8,363,404.00 |

```

2 Slovak Republic 2020 5,458,827.00
3 Austria 2020 8,916,864.00

```

1.1.2 An index with duplicate labels

The original wide table had country as index, but in the long table, each country can have multiple rows. Pandas still allows us to use country as index with [duplicate values](#). Selecting the name of the country then gives us multiple rows.

```
[4]: # set country name as index in a copy of the table
example_long_indexed = example_long.set_index('Country')
# display table with index
display(Markdown("Table with country as index:"), example_long_indexed)
# select Slovakia from this table
display(Markdown("Selecting multiple rows using `example_long_indexed.\n`loc['Slovak Republic']`"))
display(example_long_indexed.loc['Slovak Republic'])
```

Table with country as index:

| | Year | Population |
|-----------------|------|--------------|
| Country | | |
| Slovak Republic | 2010 | 5,391,428.00 |
| Austria | 2010 | 8,363,404.00 |
| Slovak Republic | 2020 | 5,458,827.00 |
| Austria | 2020 | 8,916,864.00 |

Selecting multiple rows using `example_long_indexed.loc['Slovak Republic']`:

| | Year | Population |
|-----------------|------|--------------|
| Country | | |
| Slovak Republic | 2010 | 5,391,428.00 |
| Slovak Republic | 2020 | 5,458,827.00 |

1.1.3 Finally the hierarchical index

Our table can be more naturally indexed by a pair (country, year), which uniquely specifies a row. An index consisting of two or more levels is called [hierarchical or multi-level](#).

- MultiIndex can be created by `set_index` with a list of columns to use as index.
- For faster operations, it is a good idea to sort the table by the index using `sort_index`.
- In `loc` use a tuple with one value per level, or only several initial levels.
- To specify other levels, use `xs`.

```
[5]: # create MultiIndex by choosing a list of columns
example_multiindexed = example_long.set_index(['Country', 'Year']).sort_index()
display(Markdown("Table with a multiindex:"), example_multiindexed)
```

Table with a multiindex:

| | | Population |
|-----------------|------|--------------|
| Country | Year | |
| Austria | 2010 | 8,363,404.00 |
| | 2020 | 8,916,864.00 |
| Slovak Republic | 2010 | 5,391,428.00 |
| | 2020 | 5,458,827.00 |

```
[6]: display(Markdown("**Selecting a row by using a tuple in `loc`:**"))
display(example_multiindexed.loc[('Slovak Republic', 2010)])
```

Selecting a row by using a tuple in loc:

| Population | 5,391,428.00 |
|------------|-------------------------|
| Name: | (Slovak Republic, 2010) |
| | dtype: float64 |

```
[7]: display(Markdown("**Selecting all rows for a country using a shorter tuple in `loc`:**"))
display(example_multiindexed.loc[('Slovak Republic',)])
```

Selecting all rows for a country using a shorter tuple in loc:

| Population |
|-------------------|
| Year |
| 2010 5,391,428.00 |
| 2020 5,458,827.00 |

```
[8]: display(Markdown("**Selecting all rows for a year using `xs`:**"))
display(example_multiindexed.xs(2010, level='Year'))
```

Selecting all rows for a year using xs:

| Population |
|------------------------------|
| Country |
| Austria 8,363,404.00 |
| Slovak Republic 5,391,428.00 |

```
[9]: display(Markdown("**Names of index levels can be used in `query`:**"))
display(example_multiindexed.query('Year > 2015'))
```

Names of index levels can be used in query:

| Population | |
|-----------------------------------|------|
| Country | Year |
| Austria 2020 8,916,864.00 | |
| Slovak Republic 2020 5,458,827.00 | |

1.2 Combining tables

1.2.1 Concatenating tables using concat

- Function `concat` can be used to concatenate several tables.

- At the default settings, it combines along axis 0, meaning that the rows of second table are added after the rows of the first table.
- We will also use it for `axis=1`, in which case it finds rows with the same index in both tables and combines their columns.
- By default, the result has union of rows of the two tables, but intersection can be obtained by `join='inner'`.

Example Create a second small table of countries and display both tables. Then illustrate various concatenation modes using these tables.

```
[10]: example_countries2 = countries.loc[[ "Slovak Republic", "Austria", "Hungary"],  
                                         [ "Area", "Region"]]  
display(Markdown("/**The first small table:**"), example_countries)  
display(Markdown("/**The second small table:**"), example_countries2)
```

The first small table:

| Country | Population2010 | Population2020 |
|-----------------|----------------|----------------|
| Slovak Republic | 5,391,428.00 | 5,458,827.00 |
| Austria | 8,363,404.00 | 8,916,864.00 |

The second small table:

| Country | Area | Region |
|-----------------|-----------|-----------------------|
| Slovak Republic | 49,030.00 | Europe & Central Asia |
| Austria | 83,879.00 | Europe & Central Asia |
| Hungary | 93,030.00 | Europe & Central Asia |

```
[11]: display(Markdown("/**Tables concatenated along axis 0:**"))  
display(pd.concat([example_countries, example_countries2]))
```

Tables concatenated along axis 0:

| Country | Population2010 | Population2020 | Area | \ |
|-----------------|----------------|----------------|-----------|---|
| Slovak Republic | 5,391,428.00 | 5,458,827.00 | NaN | |
| Austria | 8,363,404.00 | 8,916,864.00 | NaN | |
| Slovak Republic | | NaN | 49,030.00 | |
| Austria | | NaN | 83,879.00 | |
| Hungary | | NaN | 93,030.00 | |

| Country | Region |
|-----------------|-----------------------|
| Slovak Republic | NaN |
| Austria | NaN |
| Slovak Republic | Europe & Central Asia |
| Austria | Europe & Central Asia |
| Hungary | Europe & Central Asia |

```
[12]: display(Markdown("**Tables concatenated along axis 1:**"))
display(pd.concat([example_countries, example_countries2], axis=1))
```

Tables concatenated along axis 1:

| Country | Population2010 | Population2020 | Area | \ |
|-----------------|----------------|----------------|-----------|---|
| Slovak Republic | 5,391,428.00 | 5,458,827.00 | 49,030.00 | |
| Austria | 8,363,404.00 | 8,916,864.00 | 83,879.00 | |
| Hungary | | NaN | 93,030.00 | |

| Country | Region |
|-----------------|-----------------------|
| Slovak Republic | Europe & Central Asia |
| Austria | Europe & Central Asia |
| Hungary | Europe & Central Asia |

```
[13]: display(Markdown("**Tables concatenated along axis 1 with inner join:**"))
display(pd.concat([example_countries, example_countries2], axis=1, ↴
join='inner'))
```

Tables concatenated along axis 1 with inner join:

| Country | Population2010 | Population2020 | Area | \ |
|-----------------|----------------|----------------|-----------|---|
| Slovak Republic | 5,391,428.00 | 5,458,827.00 | 49,030.00 | |
| Austria | 8,363,404.00 | 8,916,864.00 | 83,879.00 | |

| Country | Region |
|-----------------|-----------------------|
| Slovak Republic | Europe & Central Asia |
| Austria | Europe & Central Asia |

1.2.2 Merging tables with `merge`

- Function `merge` works similarly as `concat` with `axis=1`, but it will match lines of two tables using any specified columns, not necessarily index.
- If values in these columns repeat, it combines all matching pairs of rows.
- Setting `how` in `merge` allows us to include rows that do not have a matching row in the other table.

```
[14]: # a small example of how all combinations of matching rows are returned:
tab1 = pd.DataFrame({'name': ['a','a','a','b'], 'value': [1,2,3,4]})
tab2 = pd.DataFrame({'name': ['a','a','b'], 'value': [10,20,30]})
display(Markdown("**DataFrame `tab1`:**"))
display(tab1)
display(Markdown("**DataFrame `tab2`:**"))
display(tab2)
display(Markdown("**Result of `pd.merge(tab1, tab2, on='name')`:**"))
```

```
display(pd.merge(tab1, tab2, on='name'))
```

DataFrame tab1:

| | name | value |
|---|------|-------|
| 0 | a | 1 |
| 1 | a | 2 |
| 2 | a | 3 |
| 3 | b | 4 |

DataFrame tab2:

| | name | value |
|---|------|-------|
| 0 | a | 10 |
| 1 | a | 20 |
| 2 | b | 30 |

Result of pd.merge(tab1, tab2, on='name'):

| | name | value_x | value_y |
|---|------|---------|---------|
| 0 | a | 1 | 10 |
| 1 | a | 1 | 20 |
| 2 | a | 2 | 10 |
| 3 | a | 2 | 20 |
| 4 | a | 3 | 10 |
| 5 | a | 3 | 20 |
| 6 | b | 4 | 30 |

Example of using merge on countries

- Countries belong to various international organizations and a single country can belong to many. We will represent this as a table having one row for each pair of country and an organization it belongs to.
- To combine this with other country data, we apply `merge` to get a table in which each country is copied for each organization it is in.
- Then we can for example compute the total number of people living in countries covered by individual organizations.

```
[15]: # we create a small membership table by parsing a CSV-format string
import io
membership_str = io.StringIO("""Country,Member
Slovak Republic,NATO
Slovak Republic,EU
Slovak Republic,UN
Austria,UN
Austria,EU
""")
membership = pd.read_csv(membership_str)
display(Markdown("##A small country membership table:##"), membership)
```

A small country membership table:

```

    Country Member
0 Slovak Republic    NATO
1 Slovak Republic     EU
2 Slovak Republic     UN
3      Austria        UN
4      Austria        EU

```

[16]: # merging tables using column *Country* in both
`example_membership = pd.merge(example_countries, membership, on='Country')`
`display(Markdown(""), example_membership)`

Merged table:

| | Country | Population2010 | Population2020 | Member |
|---|-----------------|----------------|----------------|--------|
| 0 | Slovak Republic | 5,391,428.00 | 5,458,827.00 | NATO |
| 1 | Slovak Republic | 5,391,428.00 | 5,458,827.00 | EU |
| 2 | Slovak Republic | 5,391,428.00 | 5,458,827.00 | UN |
| 3 | Austria | 8,363,404.00 | 8,916,864.00 | UN |
| 4 | Austria | 8,363,404.00 | 8,916,864.00 | EU |

[17]: # compute the total number of people in EU (here only for our two countries)
`display(example_membership.query('Member == "EU"')['Population2020'].sum())`

14375691.0

As we will see in the next section, we can also use `groupby` to compute sums for all organizations.

[18]: `display(Markdown("\n"))`
`display(example_membership.groupby('Member')['Population2020'].sum())`

The sum of country populations for each organization (only for our two countries)

```

Member
EU      14,375,691.00
NATO    5,458,827.00
UN      14,375,691.00
Name: Population2020, dtype: float64

```

Similar operations are often done in relational databases, where `merge` is called join. Aggregation as in `groupby` is also frequently used. More in a specialized database course in the third year.

1.3 Aggregation, split-apply-combine (`groupby`)

We have already seen simple examples of aggregation by `groupby` in Lecture 04. Here we discuss it in more detail.

Pandas follow the [split-apply-combine strategy](#) introduced in R by [Hadley Wickham](#).

Split: split data into groups, often by values in some column, such as `Region` in the `countries` table.

Apply: apply some computation on each group, obtaining some result (single value, Series, DataFrame).

Combine: concatenate results for all groups together to a new table.

Typical operations in the apply step:

- **aggregation:** e.g. compute group size, mean, median etc.
- **transformation:** e.g. compute percentage or rank of each item within a group
- **filtering:** e.g. include only groups that are large enough

In Pandas, this is done by combination of `groupby` for the split step and additional functions for the apply step. The combine step is done implicitly. Pandas library provides many options, we will cover only basics.

1.3.1 Simple aggregation in the apply step

Apply functions such as `sum`, `mean`, `median`, `min`, `max`, `size`, `count`, `describe` after `groupby`.

- `size` gives the number of rows in the group.
- `count` gives the number of non-missing values in each column.

```
[19]: display(Markdown("**The number of countries in each region:**"))
display(countries.groupby('Region').size())
```

The number of countries in each region:

```
Region
East Asia & Pacific      37
Europe & Central Asia     58
Latin America & Caribbean 42
Middle East & North Africa 21
North America              3
South Asia                 8
Sub-Saharan Africa        48
dtype: int64
```

```
[20]: display(Markdown("**Sums of country indicators in each region**"))
display(Markdown(" (including nonsense sums such as life expectation or GDP per capita)"))
display(countries.groupby('Region').sum(numeric_only=True))
```

Sums of country indicators in each region

(including nonsense sums such as life expectation or GDP per capita)

| Region | Population2000 | Population2010 | Population2020 | \ |
|----------------------------|------------------|------------------|------------------|---|
| East Asia & Pacific | 2,025,976,167.00 | 2,187,065,378.00 | 2,340,350,517.00 | |
| Europe & Central Asia | 862,786,208.00 | 889,169,626.00 | 922,353,365.00 | |
| Latin America & Caribbean | 521,281,151.00 | 588,873,865.00 | 650,534,988.00 | |
| Middle East & North Africa | 321,037,455.00 | 397,997,552.00 | 479,966,650.00 | |

| | | | | |
|----------------------------|------------------|------------------|------------------|--------------|
| North America | 312,909,973.00 | 343,397,156.00 | 369,582,572.00 | |
| South Asia | 1,406,945,496.00 | 1,660,546,144.00 | 1,882,531,621.00 | |
| Sub-Saharan Africa | 671,212,484.00 | 879,797,424.00 | 1,151,302,077.00 | |
| | | | | \ |
| Region | Area | GDP2000 | GDP2010 | GDP2020 |
| East Asia & Pacific | 24,794,669.42 | 233,980.83 | 506,478.43 | 569,610.58 |
| Europe & Central Asia | 28,813,751.77 | 883,386.74 | 1,752,994.15 | 1,966,242.67 |
| Latin America & Caribbean | 20,523,017.36 | 194,902.34 | 462,544.16 | 522,816.20 |
| Middle East & North Africa | 11,385,553.90 | 172,013.59 | 327,153.10 | 293,809.50 |
| North America | 19,715,550.00 | 116,885.13 | 198,088.01 | 214,882.96 |
| South Asia | 5,135,270.00 | 5,525.87 | 16,479.92 | 21,370.63 |
| Sub-Saharan Africa | 24,328,265.87 | 43,582.79 | 108,587.66 | 96,165.83 |
| | Expectancy2000 | Expectancy2010 | Expectancy2020 | \ |
| Region | | | | |
| East Asia & Pacific | 2,436.61 | 2,454.65 | 2,520.88 | |
| Europe & Central Asia | 4,053.36 | 4,204.81 | 4,255.06 | |
| Latin America & Caribbean | 2,931.71 | 3,013.73 | 2,957.72 | |
| Middle East & North Africa | 1,496.97 | 1,557.33 | 1,568.09 | |
| North America | 234.66 | 240.36 | 239.79 | |
| South Asia | 511.70 | 546.95 | 568.09 | |
| Sub-Saharan Africa | 2,547.64 | 2,803.97 | 3,003.10 | |
| | Fertility2000 | Fertility2010 | Fertility2020 | |
| Region | | | | |
| East Asia & Pacific | 103.92 | 91.58 | 80.30 | |
| Europe & Central Asia | 94.74 | 100.09 | 93.30 | |
| Latin America & Caribbean | 108.07 | 90.74 | 76.61 | |
| Middle East & North Africa | 71.54 | 59.86 | 52.64 | |
| North America | 5.31 | 5.28 | 4.45 | |
| South Asia | 31.62 | 24.66 | 19.56 | |
| Sub-Saharan Africa | 262.34 | 237.78 | 205.94 | |

```
[21]: display(Markdown("**Specifically sum only population in 2020 per region:**"))
display(countries.groupby('Region')['Population2020'].sum())
```

Specifically sum only population in 2020 per region:

| | |
|--------------------------------------|------------------|
| Region | |
| East Asia & Pacific | 2,340,350,517.00 |
| Europe & Central Asia | 922,353,365.00 |
| Latin America & Caribbean | 650,534,988.00 |
| Middle East & North Africa | 479,966,650.00 |
| North America | 369,582,572.00 |
| South Asia | 1,882,531,621.00 |
| Sub-Saharan Africa | 1,151,302,077.00 |
| Name: Population2020, dtype: float64 | |

1.3.2 Transformation in the apply step

Here we use `transform` method which get a function which is used on every group and should produce a group with the same index. We could write our own function (e.g. a lambda expression) or we can use one the built-in functions specified by a string.

Here we compute for each country what percentage is its population from the population of the region.

```
[22]: # group countries by region, compute the sum of each region
# and copy the regional sum for each country
region_sums = countries.groupby('Region')['Population2020'].transform('sum')
display(Markdown("For each country, what is the total population of its region"))
display(region_sums)
# now divide the population of the country by the regional total
pop_within_group = countries['Population2020'] / region_sums
display(Markdown("For each country, what fraction is its population within its region"))
display(pop_within_group.head())
```

For each country, what is the total population of its region:

```
Country
Afghanistan      1,882,531,621.00
Albania          922,353,365.00
Algeria          479,966,650.00
American Samoa   2,340,350,517.00
Andorra          922,353,365.00
...
Virgin Islands    650,534,988.00
West Bank and Gaza 479,966,650.00
Yemen            479,966,650.00
Zambia           1,151,302,077.00
Zimbabwe         1,151,302,077.00
Name: Population2020, Length: 217, dtype: float64
```

For each country, what fraction is its population within region:

```
Country
Afghanistan      0.02
Albania          0.00
Algeria          0.09
American Samoa   0.00
Andorra          0.00
Name: Population2020, dtype: float64
```

Bellow we see an alternative form of the same computation when transformation is done via a lambda function that takes a list `x` of country sizes within a region and divides them by the sum of `x`.

The use of lambda functions applied on each element is often convenient but might be slow on large data.

```
[23]: pop_within_group = (countries.groupby('Region')['Population2020']
                           .transform(lambda x : x / x.sum()))
display(Markdown("For each country, what fraction is its population within region:"))
display(pop_within_group.head())
```

For each country, what fraction is its population within region:

```
Country
Afghanistan      0.02
Albania          0.00
Algeria          0.09
American Samoa   0.00
Andorra          0.00
Name: Population2020, dtype: float64
```

Lambda expression `lambda x : x / x.sum()` above is a shorthand for defining a function which gets `x` and returns `x / x.sum()`. Below we show a version with function explicitly defined.

```
[24]: def group_fraction(x):
        return x / x.sum()
pop_within_group = (countries.groupby('Region')['Population2020']
                     .transform(group_fraction))
display(Markdown("For each country, what fraction is its population within region:"))
display(pop_within_group.head())
```

For each country, what fraction is its population within region:

```
Country
Afghanistan      0.02
Albania          0.00
Algeria          0.09
American Samoa   0.00
Andorra          0.00
Name: Population2020, dtype: float64
```

```
[25]: display(Markdown("Add back region name using concat:"))
pop_within_group2 = pd.concat([pop_within_group, countries['Region']], axis=1)
display(pop_within_group2.head())

display(Markdown("Look up value for Slovakia:"))
display(pop_within_group2.loc["Slovak Republic"])
```

Add back region name using concat:

| Population2020 | Region |
|----------------|----------------|
| 0.02 | Afghanistan |
| 0.00 | Albania |
| 0.09 | Algeria |
| 0.00 | American Samoa |
| 0.00 | Andorra |

| Country | | |
|----------------|------|----------------------------|
| Afghanistan | 0.02 | South Asia |
| Albania | 0.00 | Europe & Central Asia |
| Algeria | 0.09 | Middle East & North Africa |
| American Samoa | 0.00 | East Asia & Pacific |
| Andorra | 0.00 | Europe & Central Asia |

Look up value for Slovakia:

```
Population2020          0.01
Region                  Europe & Central Asia
Name: Slovak Republic, dtype: object
```

```
[26]: display(Markdown("**Check that the sum of each region is 1:**"))
display(pop_within_group2.groupby('Region').sum())
```

Check that the sum of each region is 1:

| Region | Population2020 |
|----------------------------|----------------|
| East Asia & Pacific | 1.00 |
| Europe & Central Asia | 1.00 |
| Latin America & Caribbean | 1.00 |
| Middle East & North Africa | 1.00 |
| North America | 1.00 |
| South Asia | 1.00 |
| Sub-Saharan Africa | 1.00 |

1.3.3 Filtering in the apply step

Finally, groupby can be followed by `filter` to use only some of the groups in the result.

Here we report all countries in regions that have at least one billion inhabitants.

```
[27]: # filter gets a function returning a boolean value for each group
filtered = (countries.groupby("Region")
            .filter(lambda x : x['Population2020'].sum() > 1e9))
display(Markdown("**Filtered data:**"))
display(filtered.head())
display(Markdown("**Check sums in regions for selected countries:**"))
display(filtered.groupby('Region')['Population2020'].sum())
```

Filtered data:

| Country | IS03 | Region | Income Group | Population2000 |
|----------------|------|---------------------|---------------------|----------------|
| Afghanistan | AFG | South Asia | Low income | 19,542,983.00 |
| American Samoa | ASM | East Asia & Pacific | High income | 58,229.00 |
| Angola | AGO | Sub-Saharan Africa | Lower middle income | 16,394,062.00 |
| Australia | AUS | East Asia & Pacific | High income | 19,028,802.00 |
| Bangladesh | BGD | South Asia | Lower middle income | 129,193,327.00 |

| Country | Population2010 | Population2020 | Area | GDP2000 | \ |
|----------------|----------------|----------------|--------------|-----------|---|
| Afghanistan | 28,189,672.00 | 38,972,231.00 | 652,860.00 | NaN | |
| American Samoa | 54,849.00 | 46,189.00 | 200.00 | NaN | |
| Angola | 23,364,186.00 | 33,428,486.00 | 1,246,700.00 | 556.88 | |
| Australia | 22,031,750.00 | 25,649,247.00 | 7,741,220.00 | 21,870.42 | |
| Bangladesh | 148,391,139.00 | 167,420,950.00 | 147,570.00 | 413.10 | |

| Country | GDP2010 | GDP2020 | Expectancy2000 | Expectancy2010 | \ |
|----------------|-----------|-----------|----------------|----------------|---|
| Afghanistan | 562.50 | 512.06 | 55.30 | 60.85 | |
| American Samoa | 10,446.86 | 15,609.78 | NaN | NaN | |
| Angola | 3,586.66 | 1,450.91 | 46.02 | 56.73 | |
| Australia | 52,147.02 | 51,868.25 | 79.23 | 81.70 | |
| Bangladesh | 776.86 | 2,233.31 | 65.78 | 68.64 | |

| Country | Expectancy2020 | Fertility2000 | Fertility2010 | Fertility2020 |
|----------------|----------------|---------------|---------------|---------------|
| Afghanistan | 62.58 | 7.53 | 6.10 | 4.75 |
| American Samoa | NaN | NaN | NaN | NaN |
| Angola | 62.26 | 6.64 | 6.19 | 5.37 |
| Australia | 83.20 | 1.76 | 1.93 | 1.58 |
| Bangladesh | 71.97 | 3.22 | 2.34 | 2.00 |

Check sums in regions for selected countries:

| Region | |
|--------------------------------------|------------------|
| East Asia & Pacific | 2,340,350,517.00 |
| South Asia | 1,882,531,621.00 |
| Sub-Saharan Africa | 1,151,302,077.00 |
| Name: Population2020, dtype: float64 | |

1.3.4 Grouping by multiple values

Function groupby can get a single column, but also a list of columns or a Series which will be used as if it was a column of the table.

```
[28]: display(Markdown("**Populations split by both region and income group**"))
display(countries.groupby(['Region', "Income Group"])['Population2020'].sum())
```

Populations split by both region and income group

| Region | Income Group | |
|-----------------------|---------------------|------------------|
| East Asia & Pacific | High income | 223,971,823.00 |
| | Low income | 25,867,467.00 |
| | Lower middle income | 301,779,468.00 |
| | Upper middle income | 1,788,731,759.00 |
| Europe & Central Asia | High income | 522,292,344.00 |
| | Lower middle income | 94,487,207.00 |

| | | |
|----------------------------|---------------------|------------------|
| | Upper middle income | 305,573,814.00 |
| Latin America & Caribbean | High income | 34,033,357.00 |
| | Lower middle income | 40,120,621.00 |
| | Upper middle income | 547,890,556.00 |
| Middle East & North Africa | High income | 68,156,525.00 |
| | Low income | 53,056,642.00 |
| | Lower middle income | 304,739,289.00 |
| | Upper middle income | 54,014,194.00 |
| North America | High income | 369,582,572.00 |
| South Asia | Low income | 38,972,231.00 |
| | Lower middle income | 1,843,044,952.00 |
| | Upper middle income | 514,438.00 |
| Sub-Saharan Africa | High income | 98,462.00 |
| | Low income | 549,157,331.00 |
| | Lower middle income | 533,054,222.00 |
| | Upper middle income | 68,992,062.00 |

Name: Population2020, dtype: float64

- Now we create a Series classifying each country as small, medium and large using cutoff 1 million for small and 100 million for medium.
- We then use this series in groupby.
- The classification is created by `pd.cut` function.

```
[29]: bin_ends = [0, 1e6, 1e8, 1e10]
bin_labels = ["small", "medium", "large"]
size_groups = pd.cut(countries['Population2020'],
                      bins=bin_ends, labels=bin_labels).rename("SizeCategory")
display(Markdown("**Country size classification:**"))
display(size_groups.head())
```

Country size classification:

| | |
|----------------|--------|
| Country | |
| Afghanistan | medium |
| Albania | medium |
| Algeria | medium |
| American Samoa | small |
| Andorra | small |

Name: SizeCategory, dtype: category
Categories (3, object): ['small' < 'medium' < 'large']

Now we can use `size_groups` Series in groupby.

Parameter `observed=True` is related to the fact that `size_groups` is has a categorial variable type to be explained next.

```
[30]: # now use size_groups in groupby
display(Markdown("**The number of countries in each size group:**"))
display(countries.groupby(size_groups, observed=True).size())
display(Markdown("**The number of countries in each size group and region:**"))
```

```
display(countries.groupby(['Region', 'size_groups'], observed=True).size())
```

The number of countries in each size group:

```
SizeCategory
small      57
medium     146
large      14
dtype: int64
```

The number of countries in each size group and region:

```
Region           SizeCategory
East Asia & Pacific    small        18
                           medium       15
                           large        4
Europe & Central Asia   small       12
                           medium      45
                           large        1
Latin America & Caribbean small      19
                           medium      21
                           large        2
Middle East & North Africa small       1
                           medium      19
                           large        1
North America          small       1
                           medium       1
                           large        1
South Asia             small       2
                           medium       3
                           large        3
Sub-Saharan Africa     small       4
                           medium      42
                           large        2
dtype: int64
```

1.4 Categorical variables

Categorical variables have values from a small set, such as region and income group in the table of countries. So far we have represented them only as strings, but we can explicitly convert them to a [categorical data type](#) in Pandas.

This has several advantages: * Strings are internally replaced by numerical IDs within the table, potentially saving memory. * Categories can be ordered and then sorting, minimum, maximum etc works as desired, not alphabetically. * Pandas is aware of the full set of possible values. For example categories without members can appear in the `groupby` results.

Example Income groups in our table are strings, we will convert them to an ordered categorical variable.

```
[31]: # creating a categorical type
cat_type = pd.api.types.CategoricalDtype(categories=["Low income",
                                                    "Lower middle income",
                                                    "Upper middle income",
                                                    "High income"],
                                         ordered=True)

# converting Income Group column to cat_type in a new DataFrame
countries_cat = countries.astype({'Income Group': cat_type})

display(Markdown("##Income Group column in the old table:"),
        countries['Income Group'].head(3))
display(Markdown("##Income Group column in the new table:"),
        countries_cat['Income Group'].head(3))
```

Income Group column in the old table:

```
Country
Afghanistan      Low income
Albania          Upper middle income
Algeria          Lower middle income
Name: Income Group, dtype: object
```

Income Group column in the new table:

```
Country
Afghanistan      Low income
Albania          Upper middle income
Algeria          Lower middle income
Name: Income Group, dtype: category
Categories (4, object): ['Low income' < 'Lower middle income' < 'Upper middle income' < 'High income']
```

```
[32]: display(Markdown("##Minimum and maximum income group in the table with categorical values:"))
        " (manually fixed order):")
display(countries_cat['Income Group'].min())
display(countries_cat['Income Group'].max())

display(Markdown("##Minimum and maximum income group in the table with strings"))
        " (alphabetical order):")
display(countries['Income Group'].dropna().min())
display(countries['Income Group'].dropna().max())
```

Minimum and maximum income group in the table with categorical values: (manually fixed order):

'Low income'

'High income'

Minimum and maximum income group in the table with strings (alphabetical order):

'High income'

'Upper middle income'

- Note that if categories do not need a fixed order, they can be created automatically by the `astype` function as in the code below.
- Notice that `groupby` creates even empty groups which would not happen with strings. This is caused by `observed=False` setting.

```
[33]: # convert region to an unordered category
countries_cat2 = countries_cat.astype({'Region': 'category'})
# count the number of countries for each combination of income group and region
countries_cat2.groupby(['Income Group', 'Region'], observed=False).size()
```

| Income Group | Region | |
|---------------------|----------------------------|----|
| Low income | East Asia & Pacific | 1 |
| | Europe & Central Asia | 0 |
| | Latin America & Caribbean | 0 |
| | Middle East & North Africa | 2 |
| | North America | 0 |
| | South Asia | 1 |
| | Sub-Saharan Africa | 22 |
| Lower middle income | East Asia & Pacific | 13 |
| | Europe & Central Asia | 4 |
| | Latin America & Caribbean | 4 |
| | Middle East & North Africa | 8 |
| | North America | 0 |
| | South Asia | 6 |
| | Sub-Saharan Africa | 19 |
| Upper middle income | East Asia & Pacific | 9 |
| | Europe & Central Asia | 16 |
| | Latin America & Caribbean | 19 |
| | Middle East & North Africa | 3 |
| | North America | 0 |
| | South Asia | 1 |
| | Sub-Saharan Africa | 6 |
| High income | East Asia & Pacific | 14 |
| | Europe & Central Asia | 38 |
| | Latin America & Caribbean | 18 |
| | Middle East & North Africa | 8 |
| | North America | 3 |
| | South Asia | 0 |
| | Sub-Saharan Africa | 1 |

dtype: int64

1.5 Dates and times

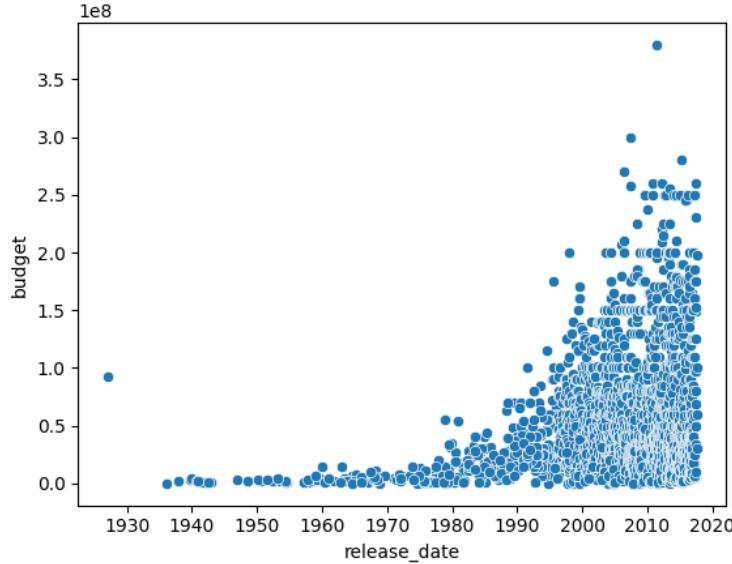
An important type of data sets are time series, where some variables are measured repeatedly over time. Pandas has an extensive support for work with times and dates. Here we show only a small example.

- We illustrate this on the movie dataset from Kaggle (see lecture 04).
- The column labeled `release_date` is recognized as date by passing `parse_dates` parameter to `read_csv`.
- Then we call function `day_name()` to get the day of week for each release day and use `value_counts` to see which days are most frequent as movie release dates.
- We also use the release date as the x-coordinate in a scatterplot.

```
[34]: # import data, including parsing of dates
url = 'https://bbrejova.github.io/viz/data/Movies_small.csv'
movies = pd.read_csv(url, parse_dates=['release_date'])
# get days of week for realse dates
days = movies['release_date'].apply(lambda x : x.day_name())
days.value_counts()
```

```
[34]: release_date
Friday      639
Thursday    515
Wednesday   474
Tuesday     175
Saturday    94
Monday      87
Sunday      65
Name: count, dtype: int64
```

```
[35]: # use release date is x-coordinate
sns.scatterplot(data=movies, x='release_date', y='budget')
pass
```



1.6 Missing values

Data sets are often incomplete, and Pandas provides techniques for [working with missing data](#).

- Missing data are typically imported as `np.nan` (not-a-number).
- These cannot occur in int-type columns, so ints are converted to floats, but can be handled in a [special way](#).

Bellow we show a small example what happens when working with missing data, including functions `isna`, `dropna`, `fillna`.

```
[36]: # create a small series with one missing value
a = pd.Series([1, 2, np.nan, 3])
display(Markdown("```\n`a.sum()` ` skips missing values`\n`a.sum()`"))
display(Markdown("```\n`a.count()` ` counts non-missing values`\n`a.count()`"))
display(Markdown("```\n`a.mean()` ` also considers only non-missing`\n`a.mean()`"))
display(Markdown("```\n`a > 2` ` evaluates missing values as `False` , similarly `<` ,\n`>` `==` :\n`a > 2`"))
display(Markdown("```\n`a == np.nan` ` also evaluates as `False`\n`a == np.nan`"))
display(Markdown("```\n`a.isna()` ` can be used to detect missing values`\n`a.isna()`"))
display(Markdown("```\n`a.dropna()` ` omits missing values`\n`a.dropna()`"))
display(Markdown("```\n`a.fillna(-1)` ` replaces them with a specified value`\n`a.fillna(-1)`"))
```

```
a.fillna(-1))
```

a.sum() skips missing values:

```
6.0
```

a.count() counts non-missing values:

```
3
```

a.mean() also considers only non-missing:

```
2.0
```

a > 2 evaluates missing values as False, similarly <, ==:

```
0    False
1    False
2    False
3    True
dtype: bool
```

a == np.nan also evaluates as False:

```
0    False
1    False
2    False
3    False
dtype: bool
```

a.isna() can be used to detect missing values:

```
0    False
1    False
2    True
3    False
dtype: bool
```

a.dropna() omits missing values:

```
0    1.00
1    2.00
3    3.00
dtype: float64
```

a.fillna(-1) replaces them with a specified value:

```
0    1.00
1    2.00
2   -1.00
3    3.00
dtype: float64
```

1.7 Pandas efficiency

Below we show several examples how different ways of implementing the same operation can have very different running time on large data. Pandas functions are usually much faster than manual iteration. However, if you do not work on huge data sets, the difference is not so important.

To measure time, we use a special Jupyter command `%timeit`. * It runs the code several times to estimate the time per one repeat.

```
[37]: # generate a Series of million random numbers and also convert it to Python list
length = int(1e6)
xs = pd.Series(np.random.uniform(0,100, length))
xl = list(xs)
```

Below we see that method `sum()` on Series is faster than Python built-in `sum` on a Python list, but Python built-in `sum` on Series is much slower, because it iterates over elements of Series.

```
[38]: display(Markdown("<!--Method `sum` on `Series` `xs.sum()`--"))
%timeit result = xs.sum()
display(Markdown("<!--Python `sum` on Python list `sum(xl)`--"))
%timeit result = sum(xl)
display(Markdown("<!--Python `sum` on Series `sum(xs)`--"))
%timeit result = sum(xs)</pre>
```

Method sum on Series `xs.sum()`:

1.12 ms ± 104 µs per loop (mean ± std. dev. of 7 runs, 1,000 loops each)

Python sum on Python list `sum(xl)`:

6.77 ms ± 401 µs per loop (mean ± std. dev. of 7 runs, 100 loops each)

Python sum on Series `sum(xs)`:

58.3 ms ± 351 µs per loop (mean ± std. dev. of 7 runs, 10 loops each)

Below we compare three ways of generating a sequence of squared values. Multiplying Series with `*` is the fastest, Python list comprehension is much slower and `apply` function from Pandas is even slower.

```
[39]: display(Markdown("<!--Pandas `Series` multiplication `x2s = xs * xs`--"))
%timeit x2s = xs * xs
display(Markdown("<!--Python list comprehension on a list `x2l = [x * x for x in xl]`--"))
%timeit x2l = [x * x for x in xl]
display(Markdown("<!--Pandas `apply` function `x2s = xs.apply(lambda x : x * x)`--"))
%timeit x2s = xs.apply(lambda x : x * x)</pre>
```

Pandas Series multiplication `x2s = xs * xs`:

1.67 ms ± 50.2 µs per loop (mean ± std. dev. of 7 runs, 1,000 loops each)

Python list comprehension on a list `x21 = [x * x for x in x1]:`

53.6 ms ± 6.34 ms per loop (mean ± std. dev. of 7 runs, 10 loops each)

Pandas apply function `x2s = xs.apply(lambda x : x * x)`

234 ms ± 12.3 ms per loop (mean ± std. dev. of 7 runs, 1 loop each)

The code below creates the Series of squares by creating a Series filled with zeroes and then assigning individual values using for-loop. This is again much slower than all methods above, so to make the code reasonably fast, we run it on data which is 100 times smaller than above.

[40]:

```
length2 = 10000
xs_small = xs.iloc[0:length2]
def assignments(len, x):
    x2 = pd.Series([0.0] * len)
    for i in range(len):
        x2[i] = x[i] * x[i]
    return x2
%timeit x2s_small = assignments(length2, xs_small)
```

173 ms ± 1.02 ms per loop (mean ± std. dev. of 7 runs, 10 loops each)

Finally the code below is even worse. It appends individual squares to a Series which starts with size 1. We run it on even smaller list of size 1000.

[41]:

```
length3 = 1000
xs_tiny = xs.iloc[0:length3]
def assignments(len, x):
    x2 = pd.Series([0.0])
    for i in range(len):
        x2[i] = x[i] * x[i]
    return x2
%timeit x2s_tiny = assignments(length3, xs_tiny)
```

286 ms ± 16 ms per loop (mean ± std. dev. of 7 runs, 1 loop each)

Lecture 6

Maps, graphs, time series

[Data visualization · 1-DAV-105](#)

Lecture by Broňa Brejová

More details in the [notebook version](#)

Part I: Maps

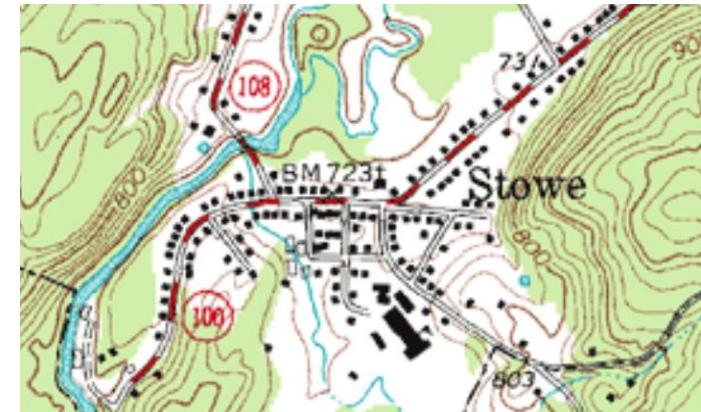
Maps

Each map is a visualization of data about location of objects.

Conventions about colors and symbols, orientation etc. allow us to quickly understand a map.

Example:

A topographic map from US

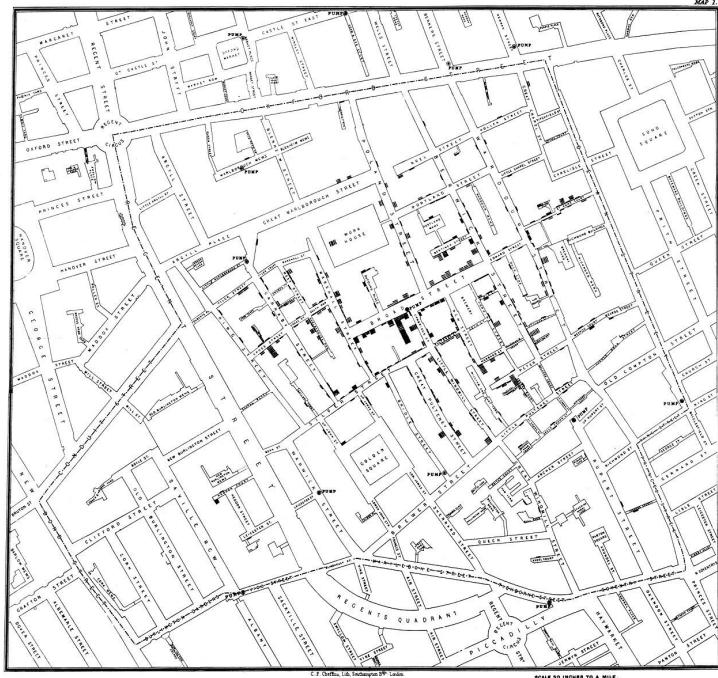


Data visualization in maps

Thematic maps (tematické mapy) visualize data other than typical geographical features

Recall Snow's map of cholera cases (1854)

Additional examples: [Wikipedia](#), [GeoPlot library gallery](#).



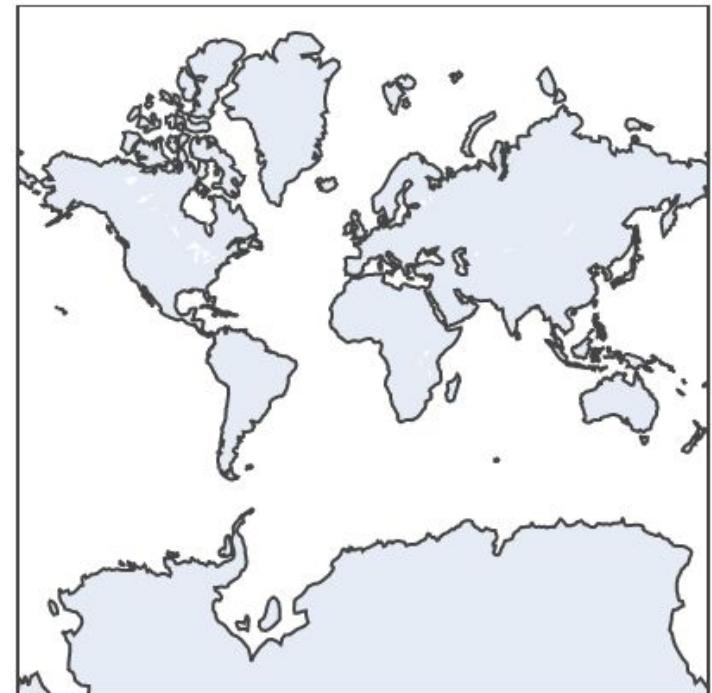
Map projection (kartografické zobrazenie)

A transformation to project the surface of a globe onto a plane

Each projection introduces some distortion

Conformal projections preserve local angles, but distort other aspects, such as lengths, areas etc.

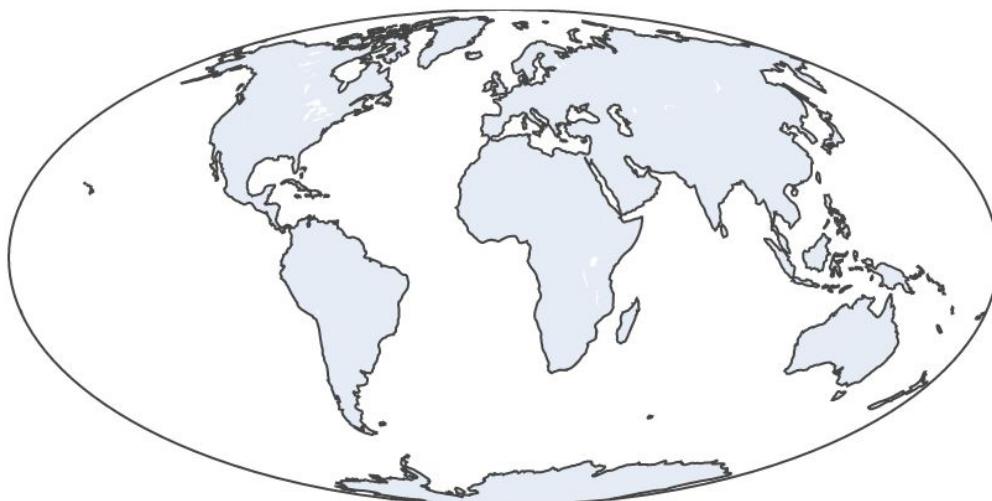
For example, **Mercator projection** (1569) developed for navigation, but shows Greenland bigger than Africa, while in fact it is 14x smaller.



Map projection (kartografické zobrazenie)

Equal-area projections preserve areas (cannot be conformal at the same time).

These are typically good for data visualization, as they make areas comparable.



Example: **Mollweide
equal-area projection
(1805)**

Map projection (kartografické zobrazenie)

Orthographic projection is similar to a photograph of the Earth from a very distant point.

It is not an equal-area projection, but our sense of perspective may compensate.

It displays one hemisphere.



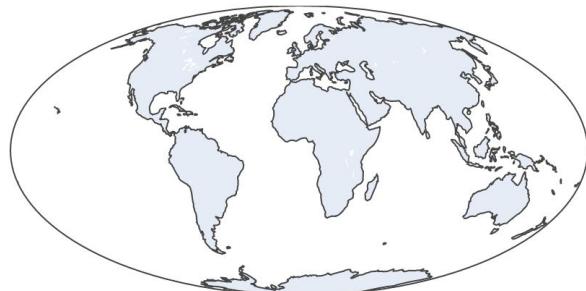
Recommended projections (Cairo, The Truthful Art)

Whole world: e.g. Mollweide equal-area projection (1805)

Continents / large countries: e.g. Lambert azimuthal equal-area projection (1772)

Countries in mid-latitudes: e.g. Albers equal-area conic projection (1805)

Polar regions: e.g. Lambert azimuthal equal-area projection (1772)



Mollweide

Lambert



Projection examples in Plotly

```
def show_world(projection, scope=None):
    # create a map figure with an empty scatterplot
    fig = go.Figure(go.Scattergeo())
    # set the desired projection
    fig.update_geos(projection_type=projection)
    # we can also limit the scope of the map
    if scope is not None:
        fig.update_geos(scope=scope)
    # finally, make the image smaller and with 0 margins
    fig.update_layout(height=200,
                      margin={"r":0,"t":0,"l":0,"b":0})
    # show the figure
    fig.show()

show_world("azimuthal equal area", "europe")
```

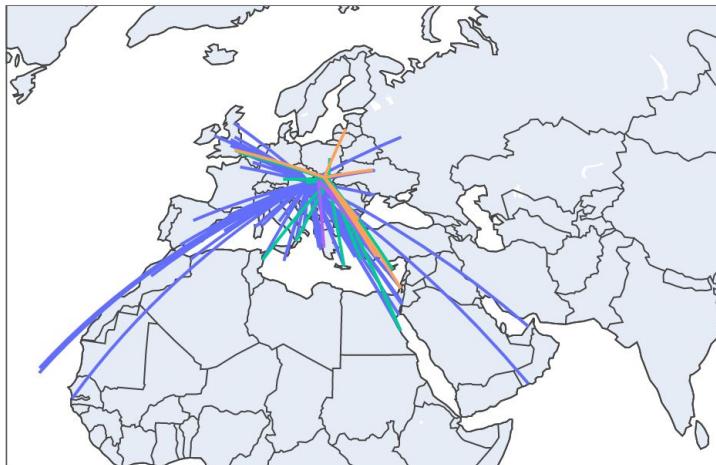
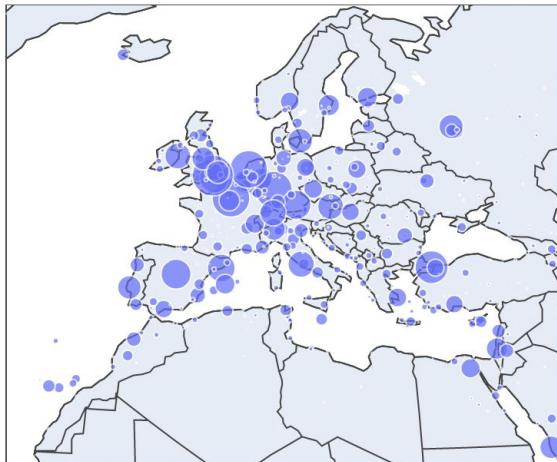


Adding data as points and lines to a map

Geographic coordinates of places can be projected as x and y.

Additional values can be shown using marker color / size or line color / width.

Example: airport locations in Europe and airline connections from Slovakia.



color

- BTS
- KSC
- SLD
- TAT

Our airport dataset

- The dataset of 2173 international airports of the world from the World Bank under the CC-BY 4.0 license, and preprocessed.
- For each airport its 3-letter code, name, country, 3-letter code of the country, the number of airplane seats per year (from unknown years) and the location.
- Stored in **GeoJSON** format.
- We parse the file using **GeoPandas** library for working with geographical data.
- It is an extension of Pandas DataFrame, with location information.

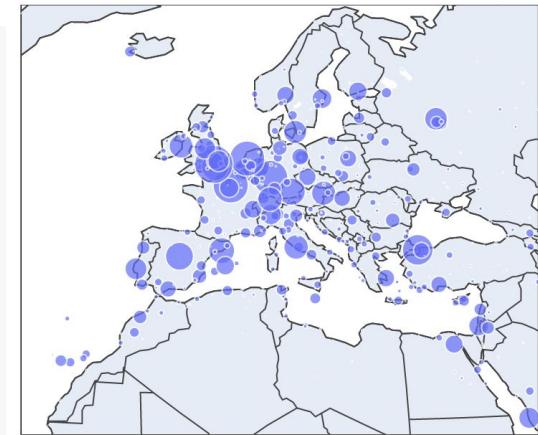
Importing airports in GeoPandas

```
import geopandas as gpd  
airports = gpd.read_file("https://bbrejova.github.io/viz/data/airports.geojson")  
display(airports.query('Country == "Slovakia"'))
```

| | Orig | Name | TotalSeats | Country | ISO3 | geometry |
|------|------|------------------|-------------|----------|------|---------------------------|
| 1489 | BTS | M.R. Stefanik | 1211732.116 | Slovakia | SVK | POINT (17.21670 48.16670) |
| 1490 | ILZ | Zilina | 3986.360 | Slovakia | SVK | POINT (18.76670 49.23330) |
| 1491 | KSC | Barca | 323259.132 | Slovakia | SVK | POINT (21.25000 48.66670) |
| 1492 | PZY | Piestany Airport | 1403.892 | Slovakia | SVK | POINT (17.83330 48.63330) |
| 1493 | SLD | Sliac | 11876.753 | Slovakia | SVK | POINT (19.13330 48.63330) |
| 1494 | TAT | Tatry/Poprad | 39612.286 | Slovakia | SVK | POINT (20.24030 49.07190) |

Drawing airport bubble graph in Plotly

```
fig = px.scatter_geo(  
    airports,  
    lat=airports.geometry.y,  
    lon=airports.geometry.x,  
    size="TotalSeats",  
    hover_name="Name"  
)  
  
fig.update_geos(  
    projection_type="azimuthal equal area",  
    lonaxis_range= [-20, 40],  
    lataxis_range= [20, 70],  
    showcountries = True  
)  
  
fig.update_layout(height=300, margin={"r":0,"t":0,"l":0,"b":0})  
fig.show()
```



Interactive plot:
zooming, panning,
tooltips

Importing airport connections in GeoPandas

```
connections = gpd.read_file("https://bbrejova.github.io/viz/data/airport_pairs_svk.geojson")
display(connections.head())
```

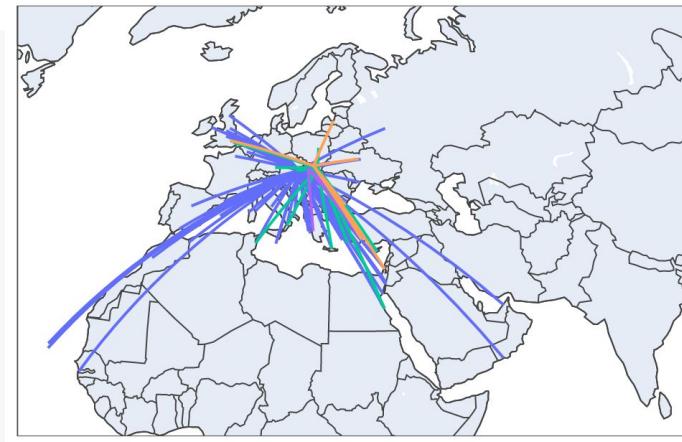
| | OrigCode | DestCode | TotalSeats | geometry |
|---|----------|----------|------------|---|
| 0 | BTS | ADB | 7370.433 | LINESTRING (17.21670 48.16670, 27.15620 38.29430) |
| 1 | BTS | AGP | 15152.501 | LINESTRING (17.21670 48.16670, -4.49810 36.67170) |
| 2 | BTS | AHO | 14740.866 | LINESTRING (17.21670 48.16670, 8.28890 40.63060) |
| 3 | BTS | AQJ | 3275.748 | LINESTRING (17.21670 48.16670, 35.01940 29.61250) |
| 4 | BTS | ATH | 19654.488 | LINESTRING (17.21670 48.16670, 23.94440 37.93640) |

Drawing airline connections in Plotly

```
lats = []
lons = []
origCodes = []
destCodes = []

for index, row in connections.iterrows():
    x, y = row['geometry'].xy
    lats.extend(list(y) + [None])
    lons.extend(list(x) + [None])
    origCodes.extend([row['OrigCode']] * len(x) + [None])
    destCodes.extend([row['DestCode']] * len(x) + [None])

fig = px.line_geo(lat=lats, lon=lons, hover_name=destCodes, color=origCodes)
fig.update_geos(
    projection_type="azimuthal equal area",
    lonaxis_range= [-25, 55],
    lataxis_range= [10, 60],
    showcountries = True
)
fig.update_layout(height=300, margin={"r":0,"t":0,"l":0,"b":0})
fig.show()
```



| color |
|-------|
| BTS |
| KSC |
| SLD |
| TAT |

Displaying variables that vary over space

Elevation can be measured at any point on land.

How is it visualized on geographic maps?

Displaying variables that vary over space

Elevation can be measured at any point on land.
How is it visualized on geographic maps?



https://upload.wikimedia.org/wikipedia/commons/d/d9/Slovakia_general_relief_map.svg

https://en.wikipedia.org/wiki/Map#/media/File:Topographic_map_example.png

Isarithmic maps / isoline maps / heatmaps

Display a continuous variable over the map area (elevation, temperature etc.)

Value in each point can be shown by a color scale.

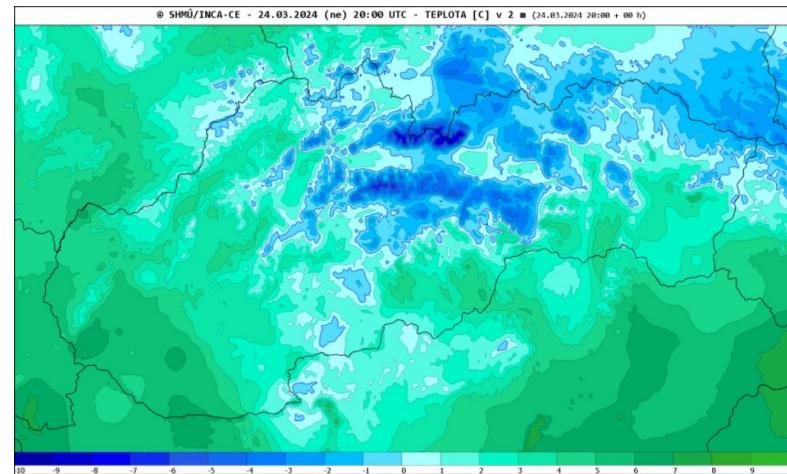
Some contour lines can be displayed as well.

A **contour line** (isoline, isopleth, isarithm, izočiara)

connects points of the same value.

Example: short-term forecasts from
the Slovak Hydrometeorological Institute.

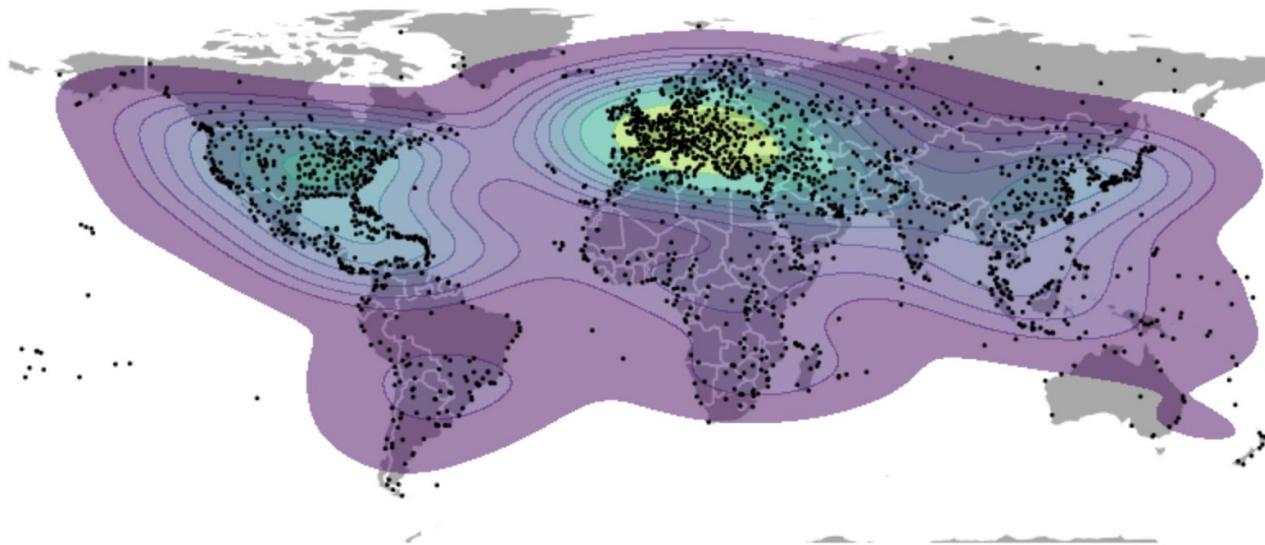
https://www.shmu.sk/sk/?page=1&id=meteo_inca_base



Density of airports as a isarithmic map

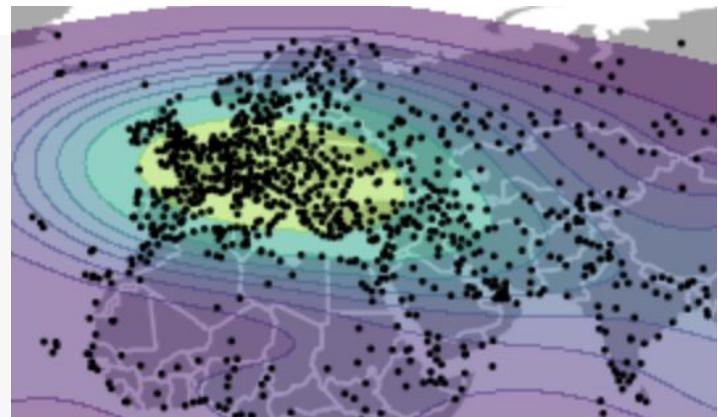
We use kdeplot function from the Geoplot library.

KDE stands for kernel density estimation (next lecture).



Density of airports in Geoplot library

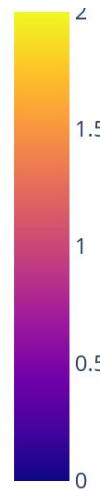
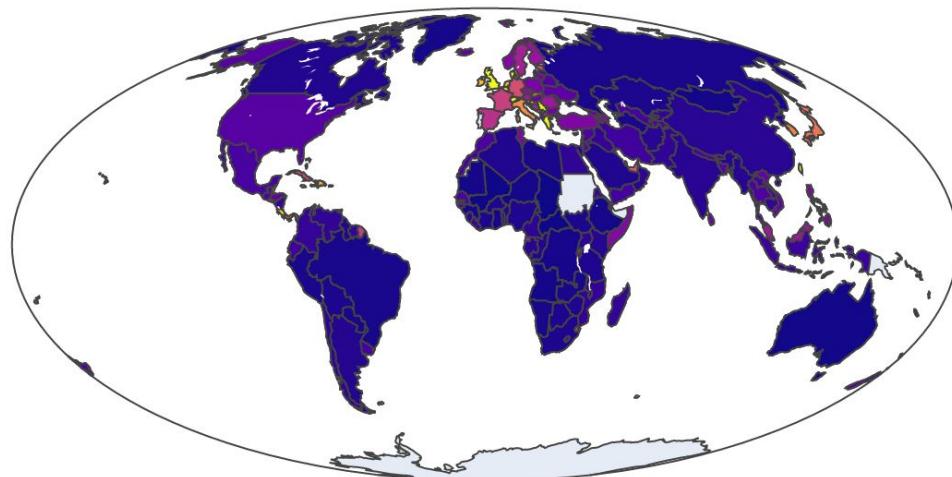
```
import geoplot as gplt
# plot countries as a background
ax = gplt.polyplot(
    countries.explode(index_parts=True),
    edgecolor='white',
    facecolor='darkgray',
    figsize=(10, 5),
)
# plot semi-transparent isarithmic map
gplt.kdeplot(
    airports, cmap='viridis',
    fill=True, alpha=0.5, ax=ax
)
# plot points on top
gplt.pointplot(airports, s=1, color='black', ax=ax
pass
```



Choropleth maps (kartogramy)

These show numerical / categorical values for administrative regions (countries, districts, etc.) via colors applied to the whole region.

Example: The number of airports in a country per 10000 km²



Types of variables over regions

Spatially extensive: apply to the unit as a whole. If we subdivide the region, spatially extensive variable will be often the sum of its parts.

Examples: total population, area, the number of airports in the country

Spatially intensive: may stay the same if you divide the unit, provided the unit is homogeneous without regional differences.

Examples: population density, life expectancy, GDP per person.

Spatially extensive variables are not appropriate for choropleths
(large value for a large country is visually attributed to each small subregion)

Computing airport stats per country in GeoPandas

```
# compute the number of airports per country by groupby
airports_per_country = airports.groupby('ISO3').size()
# add the new column to a copy of the old table
countries2 = countries.copy(deep=True)
countries2['Airports'] = airports_per_country
# remove countries where airports or location are missing
countries2.dropna(subset=['geometry', 'Airports'], inplace=True)
# add columns with airport density and airports per million people
countries2['Airport_density'] = (countries2['Airports']
                                 / countries2['Area'] * 10000)
countries2['Airports_per_mil'] = (countries2['Airports']
                                 / countries2['Population'] * 1e6)
display(countries2.loc['SVK'])
```

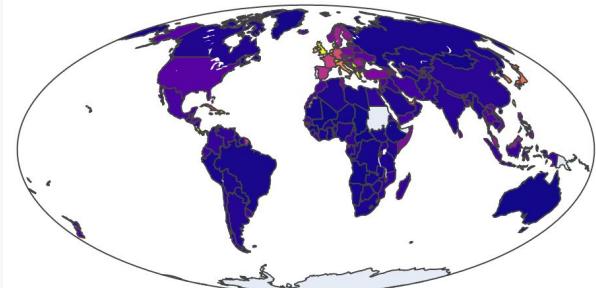
Computing airport stats per country in GeoPandas

```
Type           Sovereign country
Name          Slovakia
Population    5454073.0
Region        Europe & Central Asia
geometry      POLYGON ((22.558137648211755 49.08573802346714...
Area          47069.779734
Airports      6.0
Airport_density 1.274703
Airports_per_mil 1.100095
Name: SVK, dtype: object
```

Drawing choropleth map in Plotly

```
def draw_choropleth(data, column, range_color=None, label=None):
    fig = px.choropleth(
        data, locations=data.index, color=column,
        range_color=range_color,
        labels={column:label},
        hover_name="Name",
        projection = "mollweide"
    )
    fig.update_layout(height=300, margin={"r":0,"t":0,"l":0,"b":0})
    fig.show()

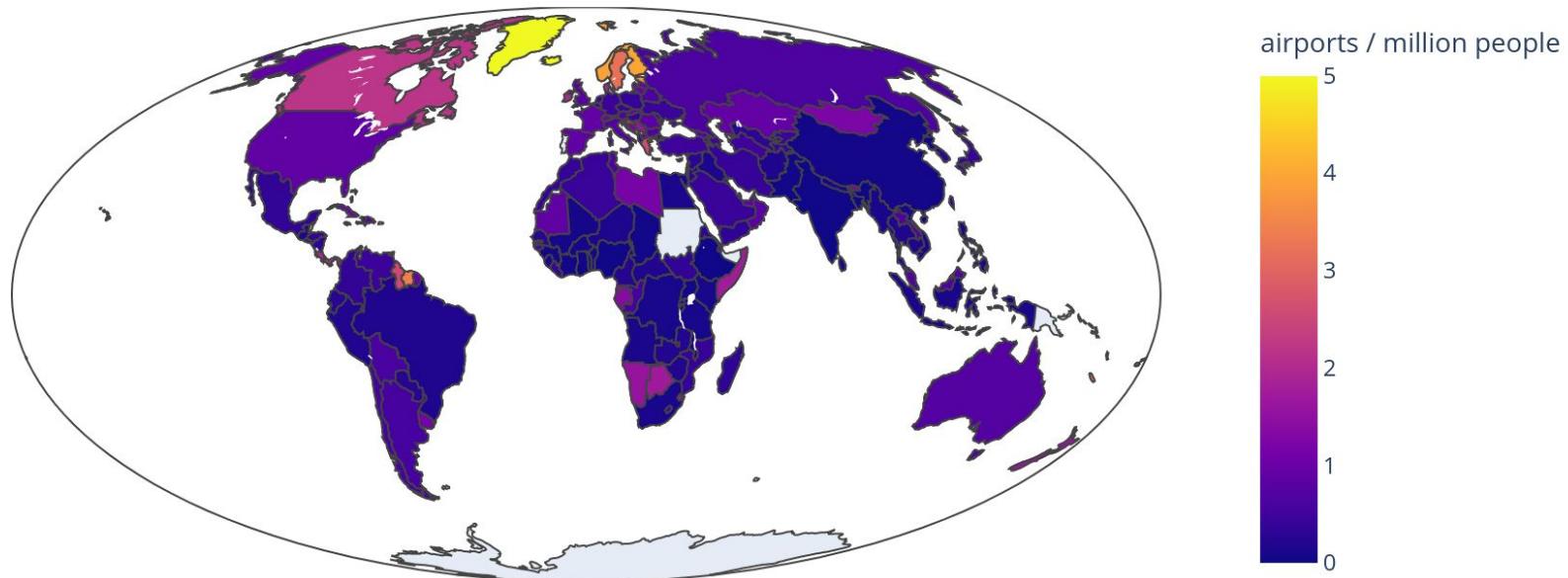
display(Markdown("The number of airports per 10000 squared km"))
draw_choropleth(countries2, 'Airport_density', (0, 2), 'airports / 10000 km2')
```



Another intensive variable

```
display(Markdown("The number of airports per million inhabitants"))
draw_choropleth(countries2, 'Airports_per_mil', (0, 5), 'airports / million people')
```

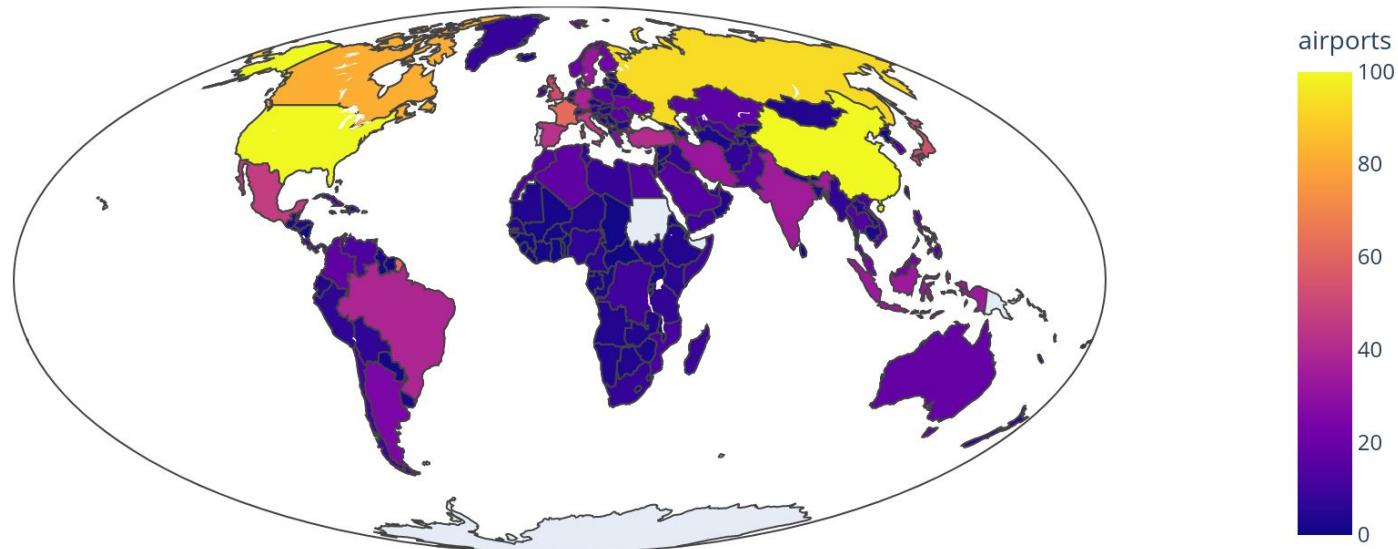
The number of airports per million inhabitants



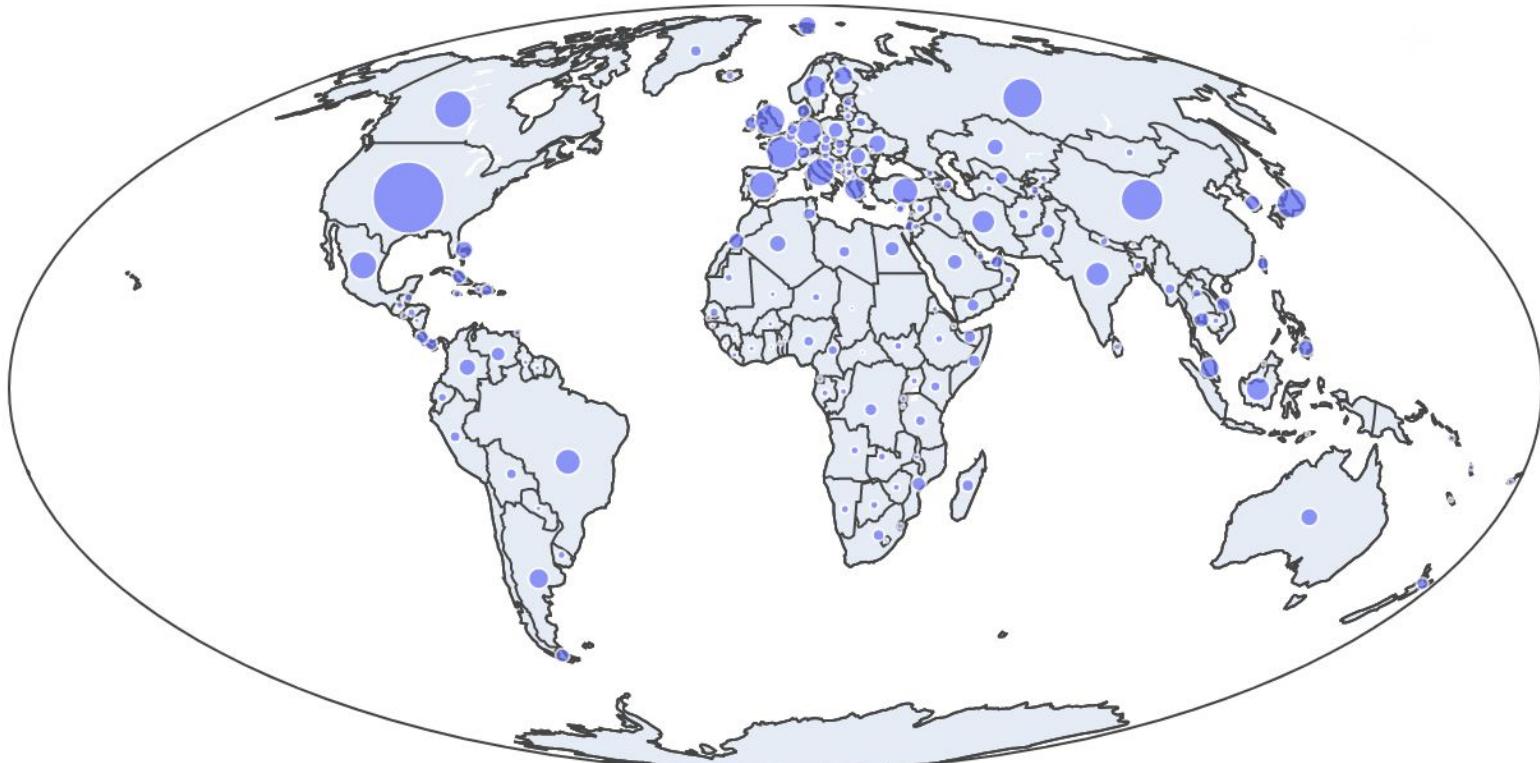
The number of airports is extensive (not good)

```
display(Markdown("The number of airports in a country"))
draw_choropleth(countries2, 'Airports', (0, 100), 'airports')
```

The number of airports in a country



The number of airports as a bubble plot (better)



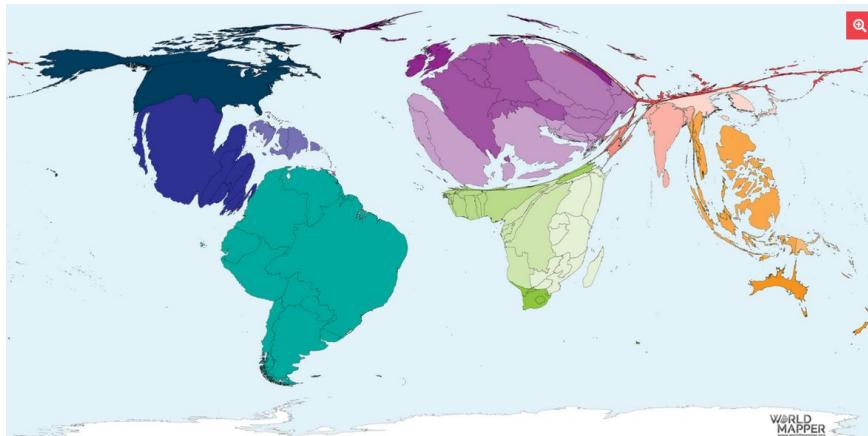
Cartogram vs kartogram

A choropleth map is called kartogram in Slovak.

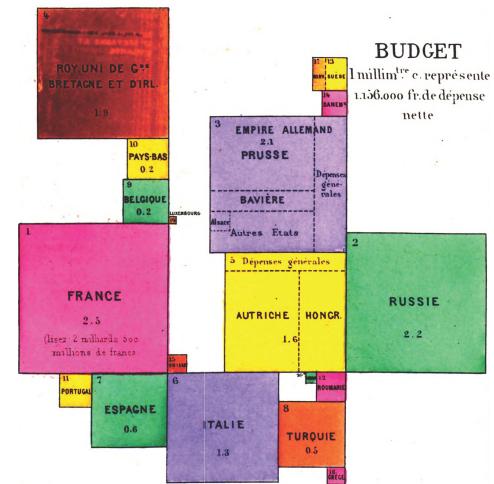
In English, cartogram is a map with regions rescaled according to some variable

Examples: World's Catholic Population by World Mapper

Levasseur's cartogram of country budgets



<https://worldmapper.org/maps/catholic-population-2005/>



https://commons.wikimedia.org/wiki/File:Levasseur_cartogram.png

Summary of maps

- Many data sets contain geographic entities (countries, cities, coordinates)
- Displaying such data on maps shows spatial relationships
- Use appropriate equal-area projections
- Bubble plots: add points of various sizes
- Isarithmic maps / isoline maps / heatmaps: continuously varying variables
- Choropleth map: variables characterizing whole region
 - The variable should be intensive, e.g. normalized by area or population

Several useful libraries

- Geopandas for working with geographical data, extension of DataFrame
- Geoplot and Plotly for visualization

Part II: Graphs / networks

Graph / network

Vertices (vrcholy; also nodes, uzly) often real-world entities

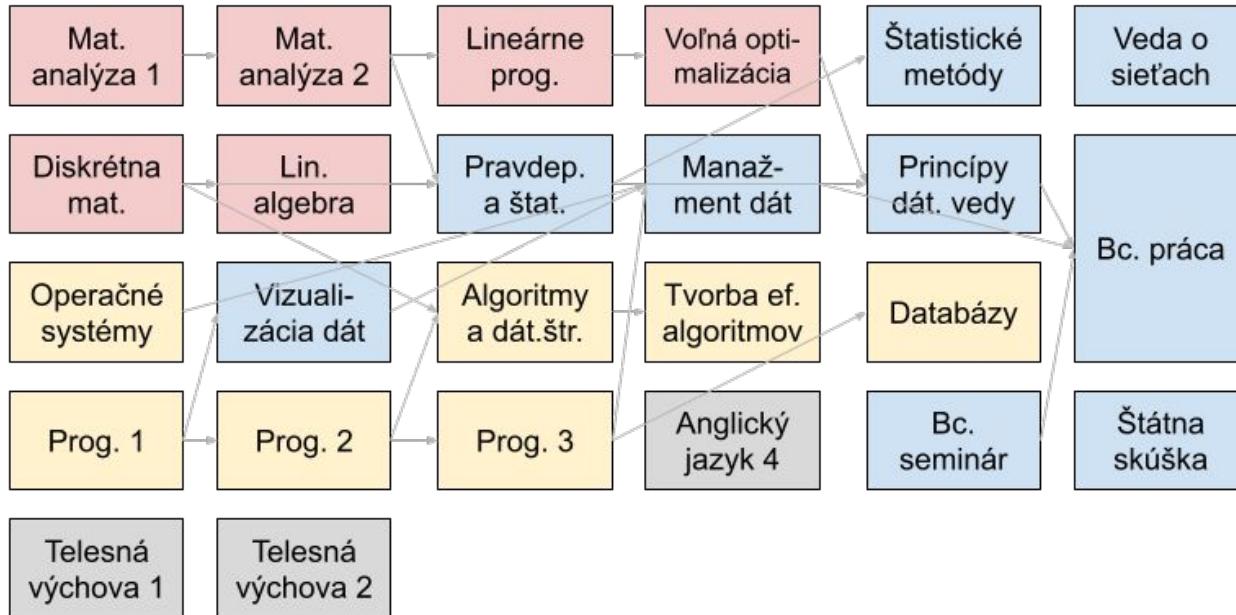
Edges (hrany; also links, arcs) often relationships / connections between pairs of vertices

Many real-world examples:

places connected by roads, computers connected by network cables,
people connected by family or work relationships,
companies connected by financial transactions, texts connected by references,
tasks or courses connected by dependencies,
any objects connected based on similarity / shared features, ...

Graphs are very important in both computer science and data science.

Example: dependencies between DAV courses



Graph / network (cont.)

Edges: Directed (orientované) or undirected (for symmetric relationships)

Recall: how did you define directed / undirected edges in discrete mathematics?

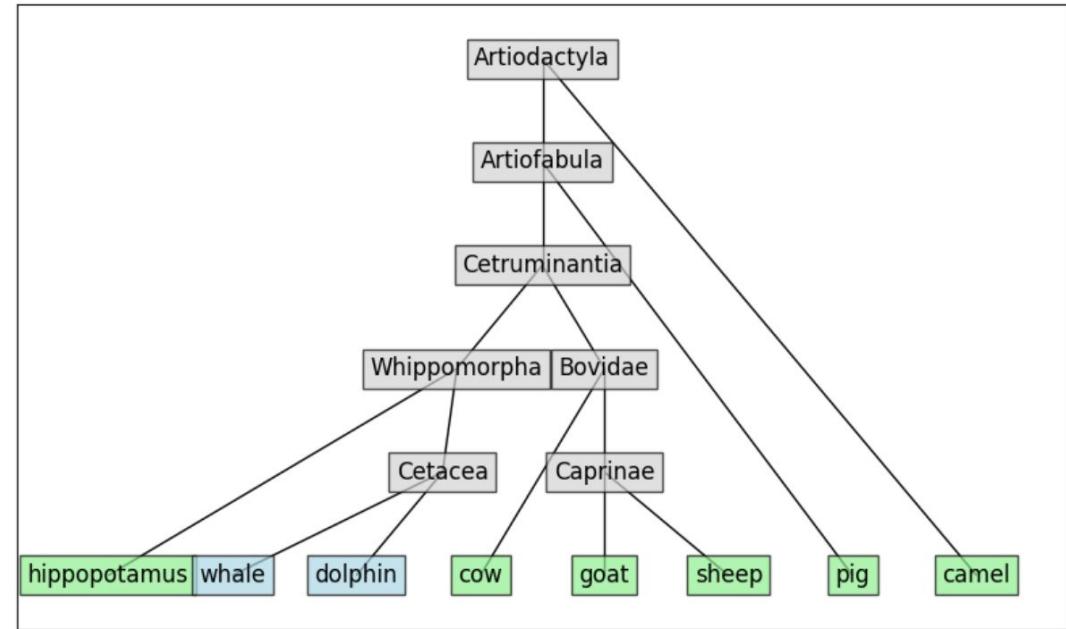
Graphs are covered in several courses: discrete mathematics, programming, design of efficient algorithms, network science.

Trees

An undirected graph is called a tree if it is connected and without cycles.

In practice we usually encounter rooted (directed) trees,
which have a single root,
all other vertices
can be reached from the root
via a unique path.

Creates parent / child
relationships between nodes



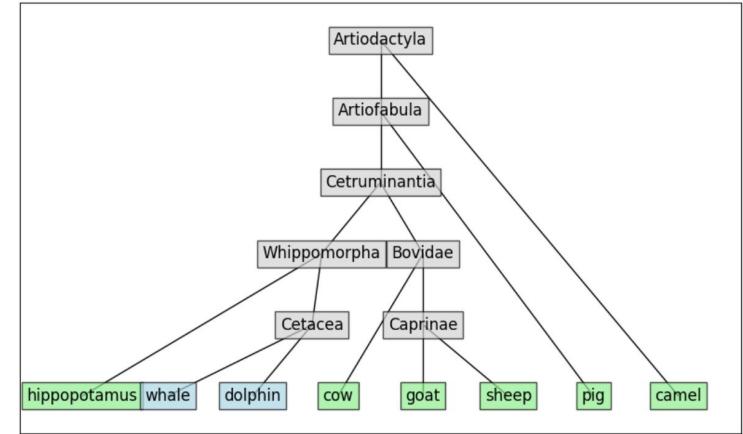
Trees and hierarchies

Trees can express hierarchies in which each entity has a single direct superior
Examples:

Company structure in which each employee (except for the head of the company)
has a single supervisor (similarly army command)

Administrative divisions (country, region, district)

Species taxonomy
(animals, mammals, primates, ...)



More general hierarchies

Some hierarchies allow multiple direct superiors, for example:

- family tree where each person has two parents (and they may be distantly related),
- geometrical shapes, where a square is both a special case of a regular polygon and a special case of a rectangle and both of these are a special case of a polygon.

These hierarchies can be represented as directed acyclic graphs

- Acyclic means that by following edges we never get back to the starting node (nobody is their own ancestor).

What to study / visualize in real-life graphs?

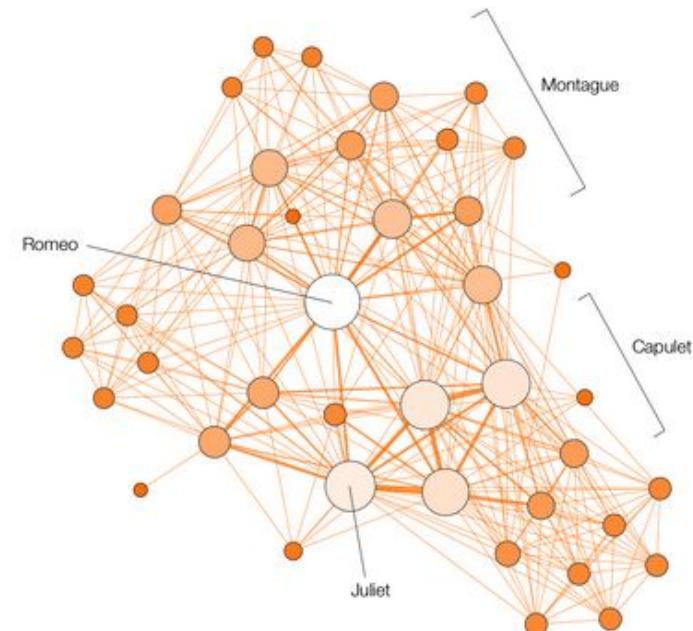
Details of connections for a particular node
(requires zooming in large networks).

Overall structure of the graph: connected components, density of edges, presence of cycles, weak places (bridges and articulations), densely connected clusters

Do nodes with some property cluster together? (Are they connected by many edges?)

Example: character co-occurrence in Shakespeare

<http://www.martingrandjean.ch/network-visualization-shakespeare/>



ROMEO AND JULIET

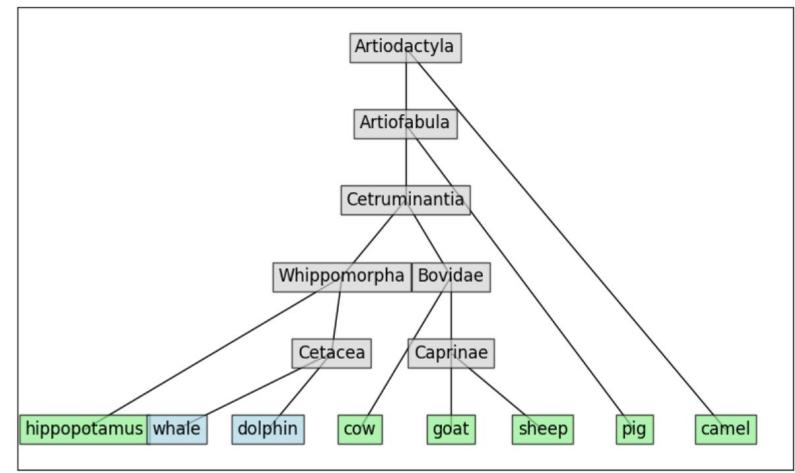
Number of characters **41** | Network density **37%**

Basics of graph drawing

Vertices typically shown as markers (circles, rectangles etc.), possibly with labels, size, color, ...

Edges shown as lines connecting them, possibly of different color or width. They can be straight lines, arcs, polygonal lines or arbitrary curves.

Edge direction displayed as arrows
or all edges drawn to point in one direction,
e.g. downwards.



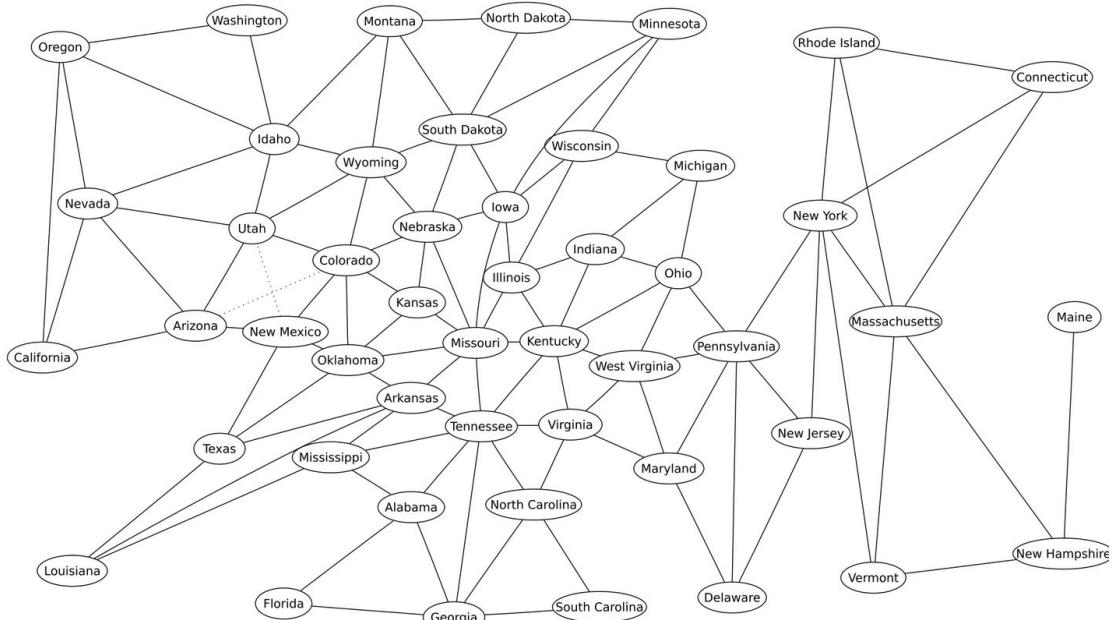
Desirable properties of a graph drawing

Nodes do not overlap.

Edges are not too long and have a simple shape without many bends.

The number of edge crossings is small.

The graph uses the space of the figure well without large empty regions.

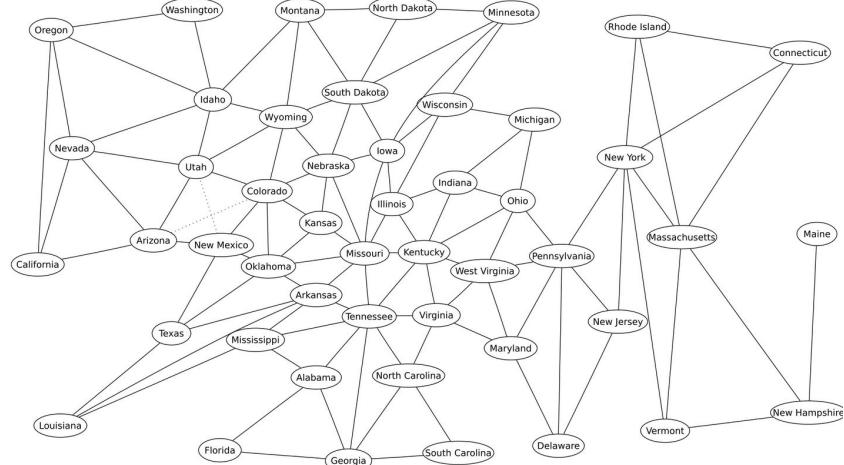


<https://commons.wikimedia.org/wiki/File:UnitedStatesGraphViz.svg>

Node positioning in graph drawing

Sometimes the position of nodes is given by their properties, e.g. on a map (airline connections), level of a hierarchy, timeline.

Otherwise we place nodes to optimize desirable properties, e.g. using **force-directed layout**, which assigns attractive forces (springs) between nodes connected by edges and repulsive forces between other pairs of nodes.



Our hierarchy: manually created DataFrame of animals

Taxonomy of even-toed ungulates
(párnokopytníky)

Level along tree (1=leaves, 6=root)

Category: land / sea / group

| | | name | parent | level | category |
|----|---------------|---------------|--------------|-------|----------|
| 0 | | camel | Artiodactyla | 1 | land |
| 1 | | pig | Artiofabula | 1 | land |
| 2 | | sheep | Caprinae | 1 | land |
| 3 | | goat | Caprinae | 1 | land |
| 4 | | cow | Bovidae | 1 | land |
| 5 | | dolphin | Cetacea | 1 | sea |
| 6 | | whale | Cetacea | 1 | sea |
| 7 | hippopotamus | Whippomorpha | | 1 | land |
| 8 | Caprinae | Bovidae | | 2 | group |
| 9 | Cetacea | Whippomorpha | | 2 | group |
| 10 | Bovidae | Cetruminantia | | 3 | group |
| 11 | Whippomorpha | Cetruminantia | | 3 | group |
| 12 | Cetruminantia | Artiofabula | | 4 | group |
| 13 | Artiofabula | Artiodactyla | | 5 | group |
| 14 | Artiodactyla | Nan | | 6 | group |

NetworkX: library for working with graphs

```
# create empty graph in NetworkX
G = nx.Graph()

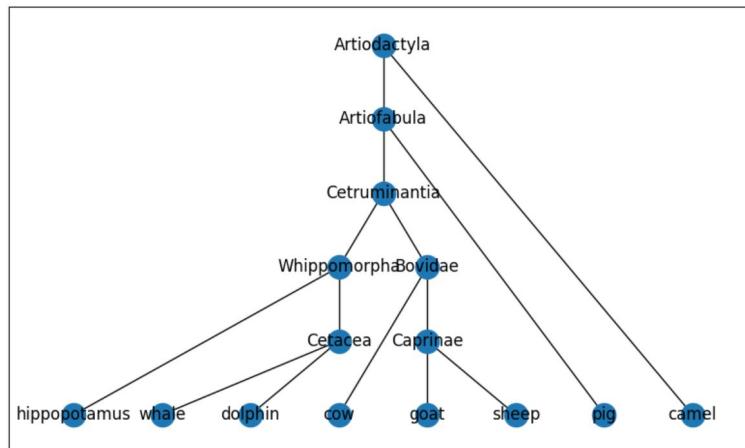
# adding each table row as a node
for index, row in animals.iterrows():
    G.add_node(row['name'], level=row['level'],
               category=row['category'])

# adding an edge to each node from its parent
for index, row in animals.iterrows():
    if row['parent'] is not np.nan:
        G.add_edge(row['parent'], row['name'])
```

Basic graph drawing in NetworkX

```
# computing coordinates of nodes
coordinates = nx.multipartite_layout(G, subset_key="level",
                                      align='horizontal')

# drawing the graph
(figure, axes) = plt.subplots(figsize=(10, 6))
nx.draw_networkx(G, coordinates, ax=axes)
```

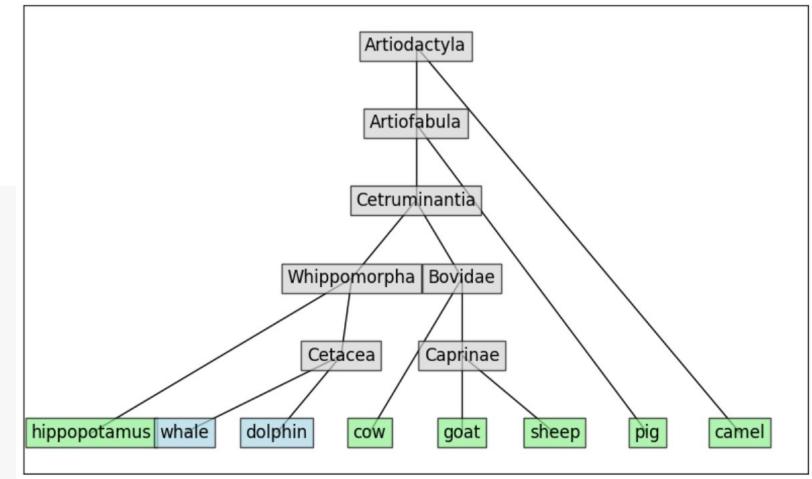


Improving the plot

```
# again compute coordinates and move some of them manually
coordinates2 = nx.multipartite_layout(G, subset_key="level",
                                      align='horizontal')
coordinates2["Whippomorpha"] += (-0.05, 0)
coordinates2["Cetacea"] += (-0.08, 0)

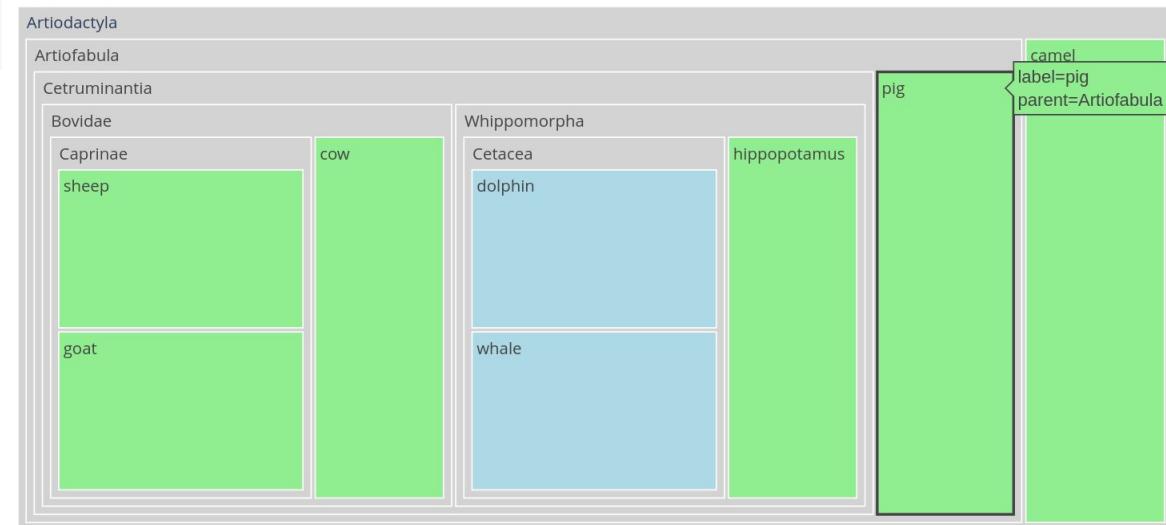
# plot edges only, omit nodes for now
(figure, axes) = plt.subplots(figsize=(10, 6))
nx.draw_networkx_edges(G, coordinates2, ax=axes)

# plot each category of nodes by a different color
color_dict = {'group':'lightgray', 'land':'lightgreen', 'sea':'lightblue'}
for category in color_dict:
    # create a list of nodes on the category
    category_nodes = [v for v in G.nodes if G.nodes[v]['category']==category]
    # select subgraph H of G
    H = G.subgraph(category_nodes)
    # create a dictionary of node label attributes
    label_options = {"ec": "black", "fc": color_dict[category], "alpha": 0.7}
    # draw the node labels as boxes
    nx.draw_networkx_labels(H, coordinates2, font_size=12, b
                           box=label_options, ax=axes)
```



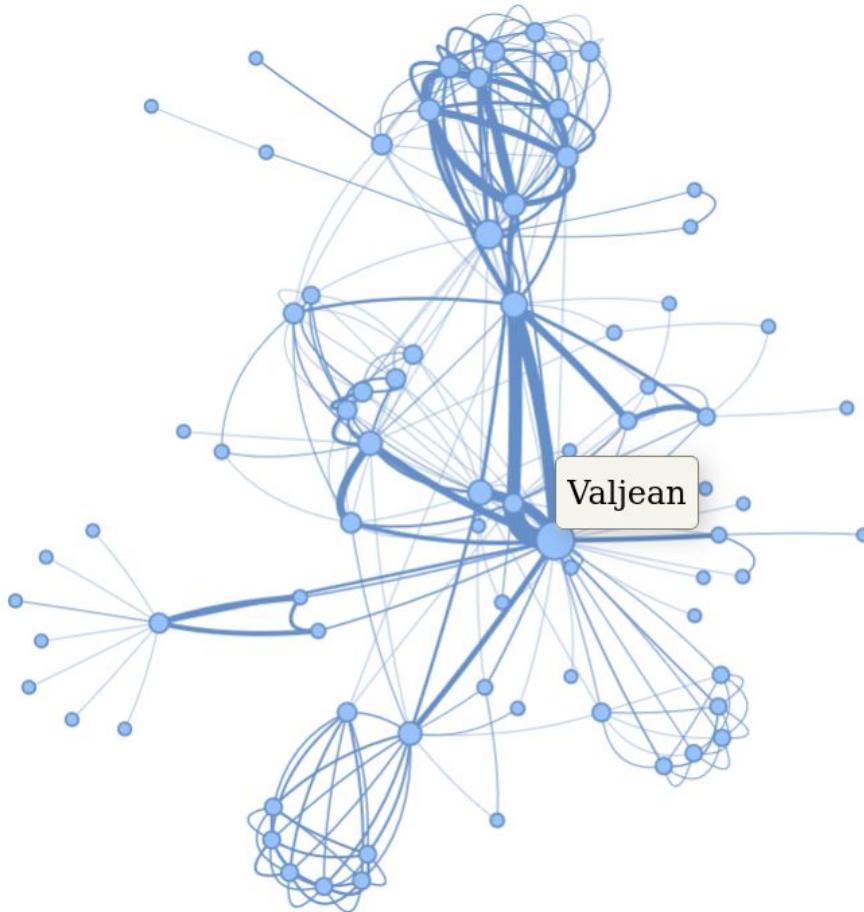
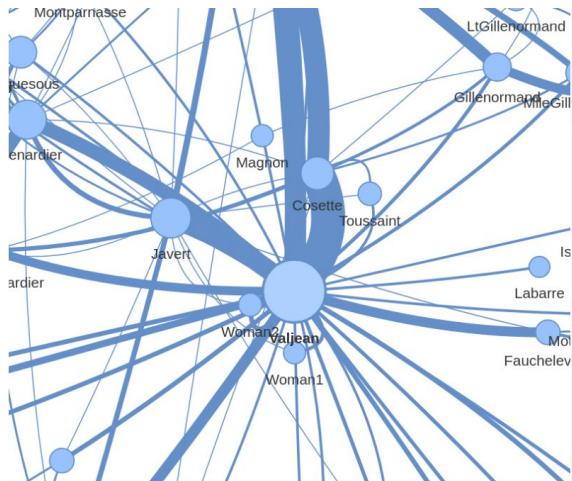
Hierarchy as a treemap in Plotly Express

```
import plotly.express as px
fig = px.treemap(
    names=animals['name'],
    parents=animals['parent'],
    color=animals['category'],
    color_discrete_map=color_dict
)
fig.show()
```



Interactive graphs in Pyvis

- Example from NetworkX: character co-occurrence in *Les Misérables* by Victor Hugo.
- Edges weighted by frequency



```
# initializing an empty network, setup plot properties
pyvis_net = Network("500px", "500px", notebook=True,
                     cdn_resources='in_line')
# loading network from NetworkX
pyvis_net.from_nx(nx.les_miserables_graph())

# get a dictionary of neighbors for each node
neighbors = pyvis_net.get_adj_list()
# add additional node properties
# used as tooltip and size
for node in pyvis_net.nodes:
    node["title"] = node["id"]
    node["value"] = len(neighbors[node["id"]])

# saving the visualization in an html file
pyvis_net.show("net.html")
# displaying the html file in the notebook
from IPython.display import display, HTML
display(HTML('net.html'))
```

Summary of graphs

- Graphs important in **many applications**
- **NetworkX** library has many functions for working with graphs, several layout algorithms for visualization
- **Pyvis** allows interactive visualization
- **Plotly** can visualize trees as **treemaps**

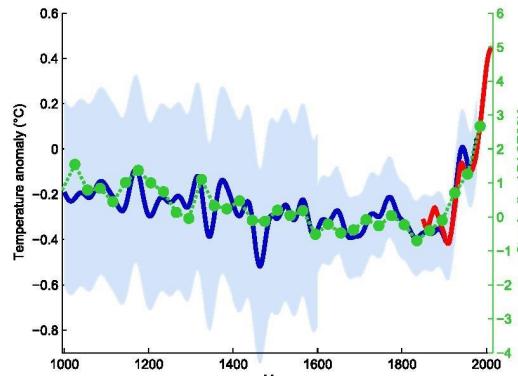
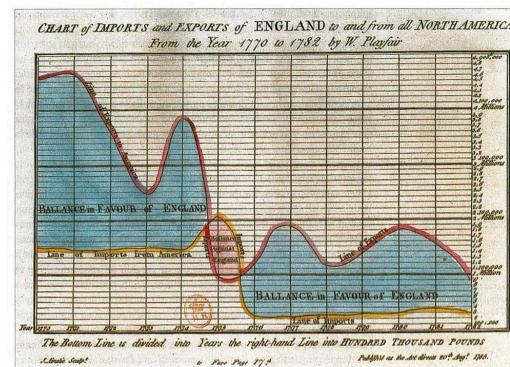
Part III: Time series

Time series (časové rady)

Sequences of measurements over time (regular or irregular time intervals).

Typically displayed as a **line graph**, with time as x-axis, time flowing from left to right (a cultural convention in western countries).

Other options: bar graphs, heat maps, box plots, ...



Recall:
Playfair 1786,
Mann, Bradley &
Hughes 1999

https://commons.wikimedia.org/wiki/File:1786_Playfair_-_Chart_of_import_and_exports_of_England_to_and_from_all_North_America_from_the_year_1770_to_1782.jpg https://en.wikipedia.org/wiki/File:T_comp_61-90.pdf

Typical features of a time series

Overall trend (increasing / decreasing / flat; rate of change),

Seasonality (daily / weekly / yearly cycles),

Noise (general variability / outliers)

Two Google trend time series

[Google trends](#) compare frequency
of search terms over time and to each other.

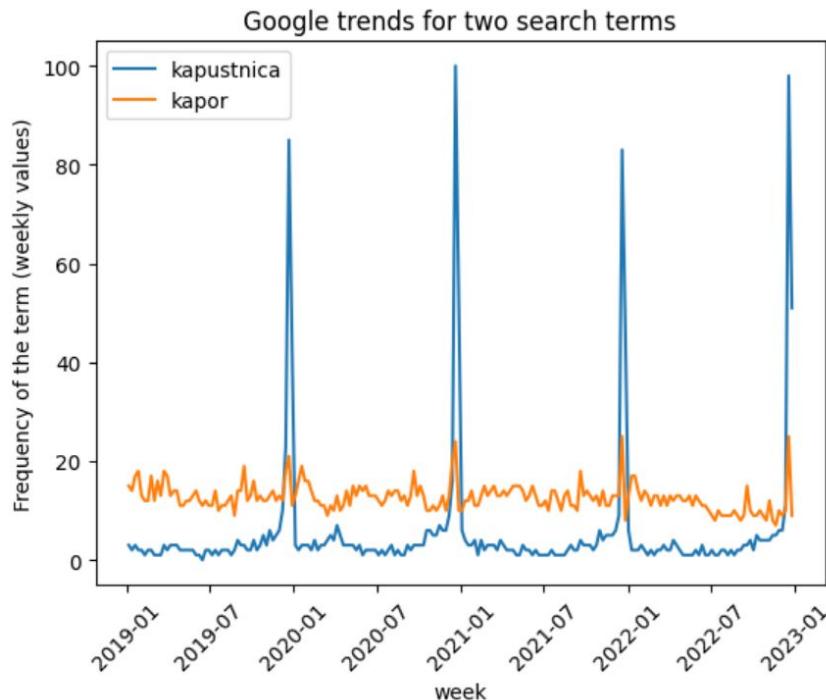
Here we use Christmas-related terms
kapustnica and kapor.

```
display(trends1.head(4))
```

| | kapustnica | kapor |
|------------|------------|-------|
| week | | |
| 2019-01-06 | 3 | 15 |
| 2019-01-13 | 2 | 14 |
| 2019-01-20 | 3 | 17 |
| 2019-01-27 | 2 | 18 |
| 2019-02-03 | 2 | 13 |

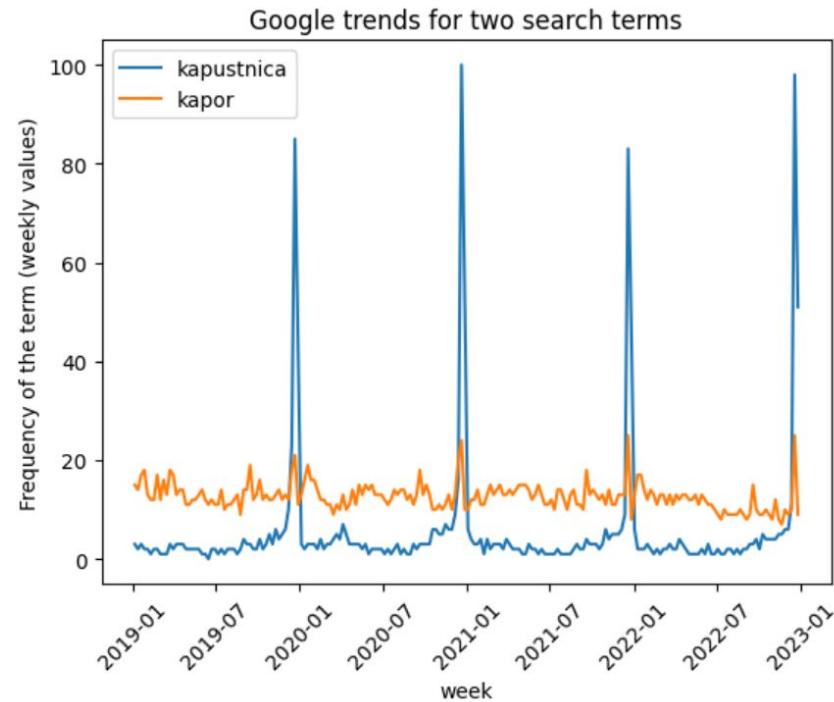
What can we see on the plot?
(trend, seasonality, noise)

Comparison of the two terms?



```
axes = sns.lineplot(trends1, dashes=False)
axes.set_ylabel("Frequency of the term (weekly values)")
axes.set_title("Google trends for two search terms")
# rotate tick labels
axes.tick_params(axis='x', labelrotation = 45)
```

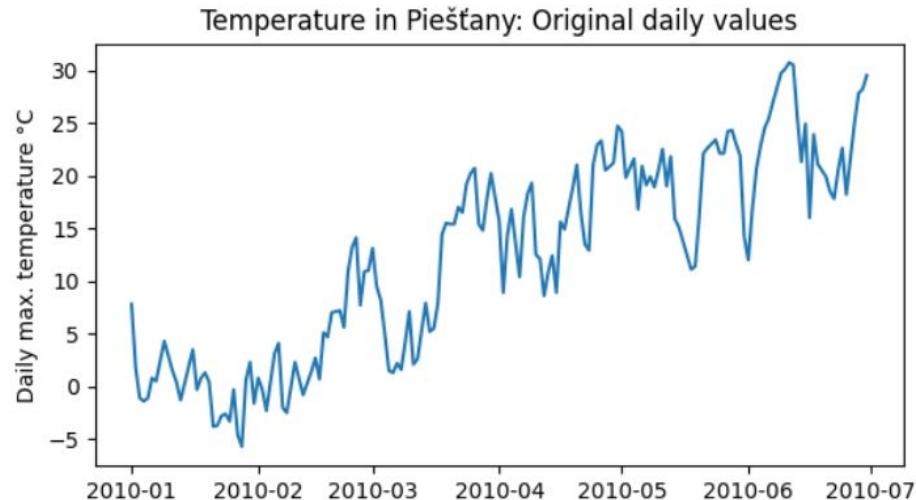
Search terms related to kapor: zbgis kataster, zbgis mapa, zgbis, katasterportal list vlastnictva, dážďovka.



Trend: temperatures are growing in spring

Second dataset:

Maximum daily temperature values
from Piešťany January-June 2010,
from US National Oceanic
and Atmospheric Administration



Smoothing data (vyrovnanie, vyhľadenie)

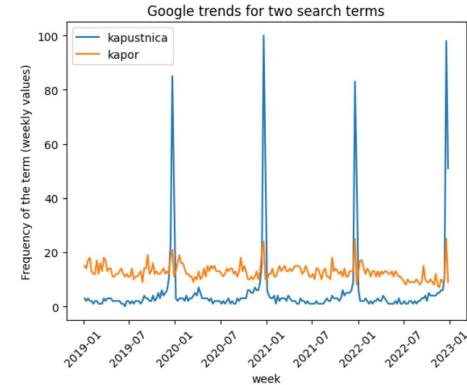
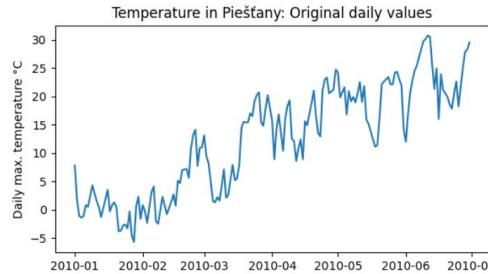
Our time series are quite noisy.

Two options for **smoothing** data:

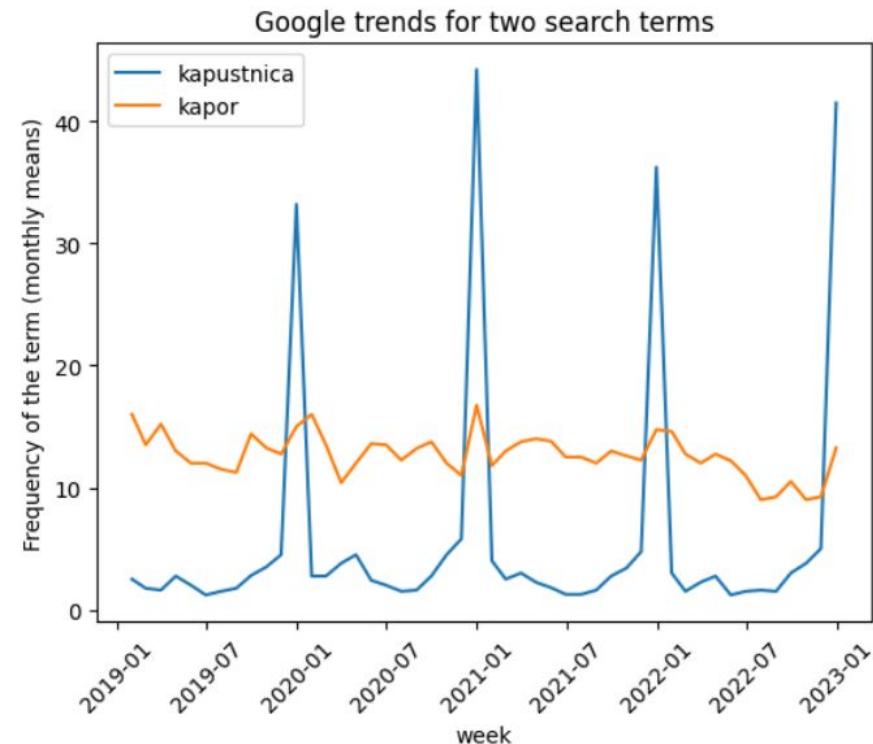
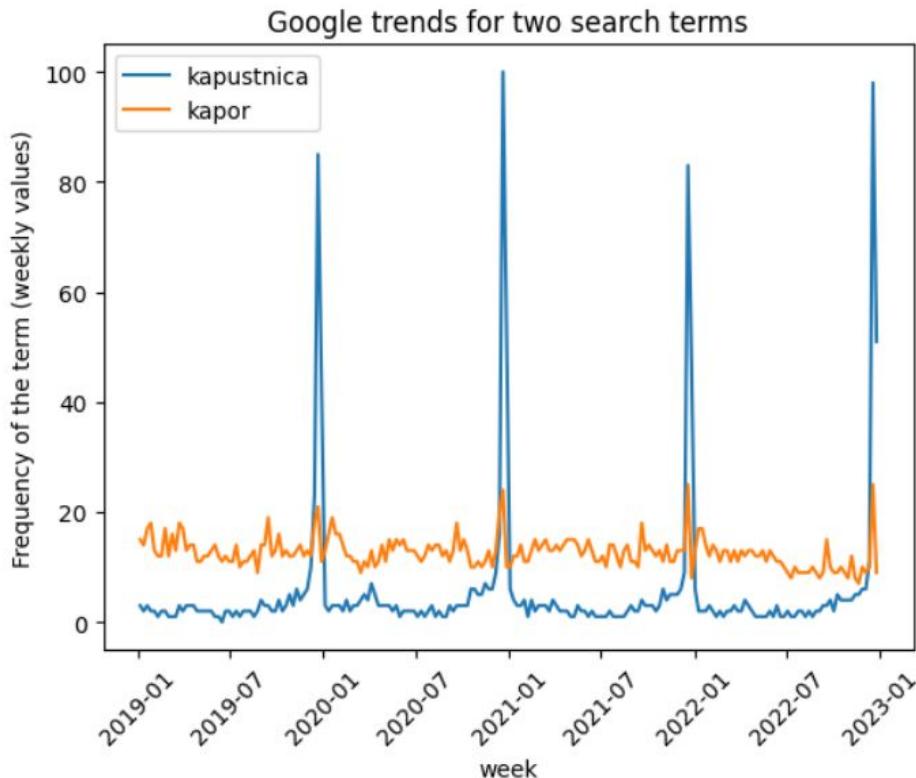
Aggregating them in longer time intervals (e.g. months).

Sliding window (kĺzavé okno): we choose a window size w and compute a new series, each value being mean or other summary of w consecutive windows in the input.

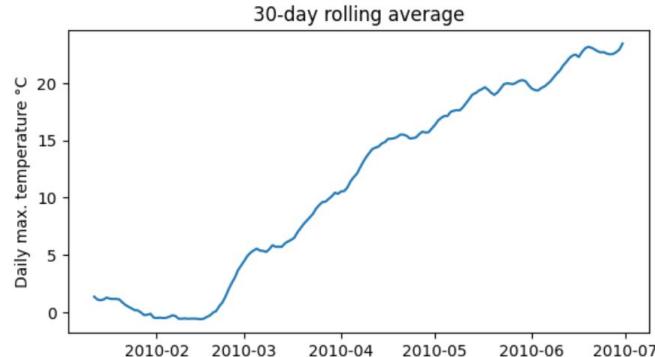
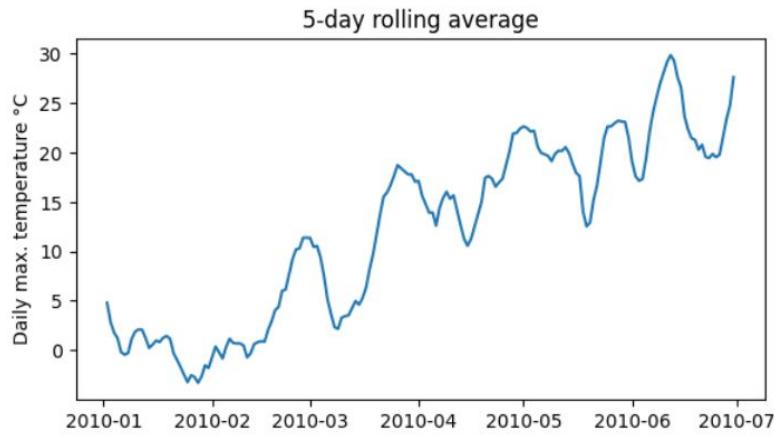
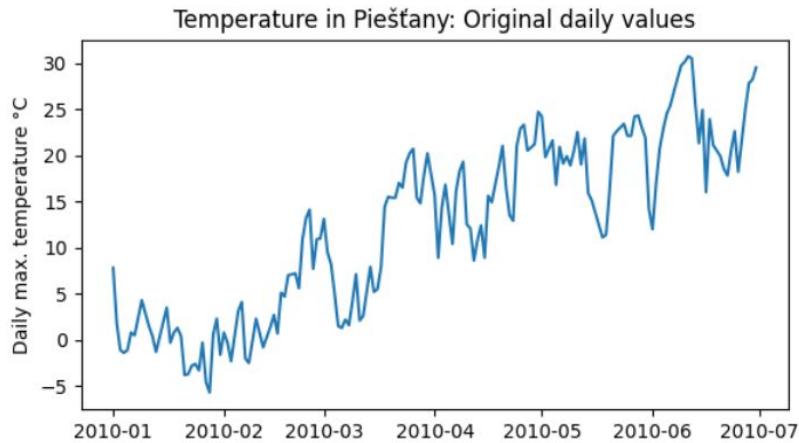
For example with values 2,6,4,2,8,2 and window size 4, we get window means 3.5, 5, 4.



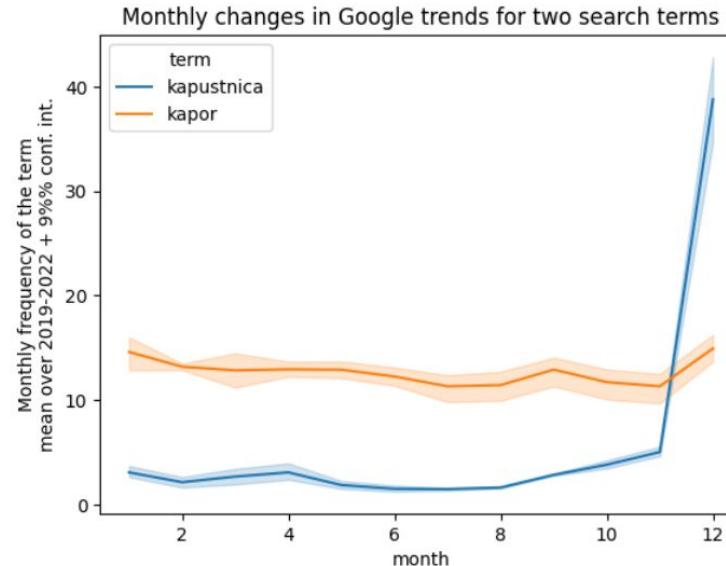
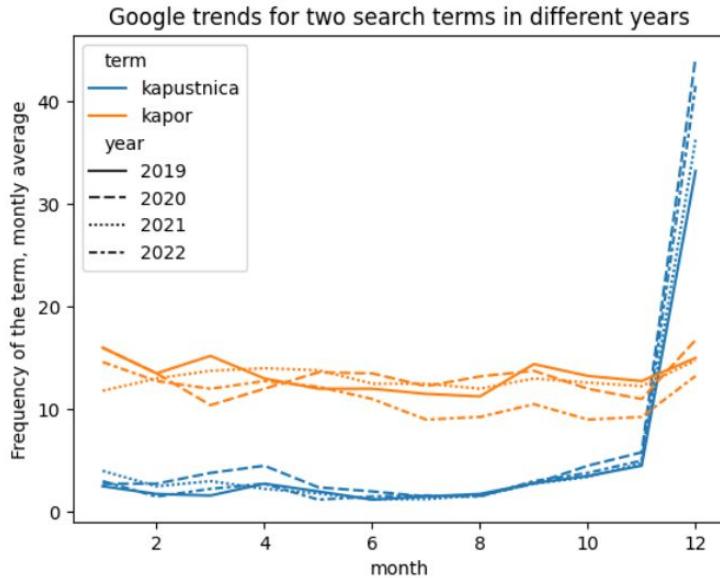
Smoothing Google trends by monthly aggregation



Smoothing temperatures by sliding window

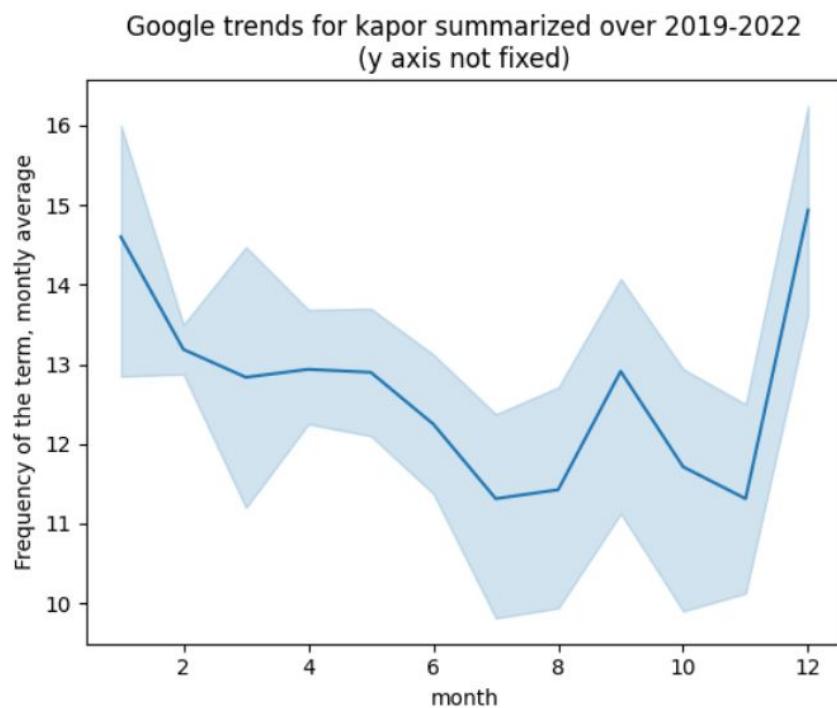
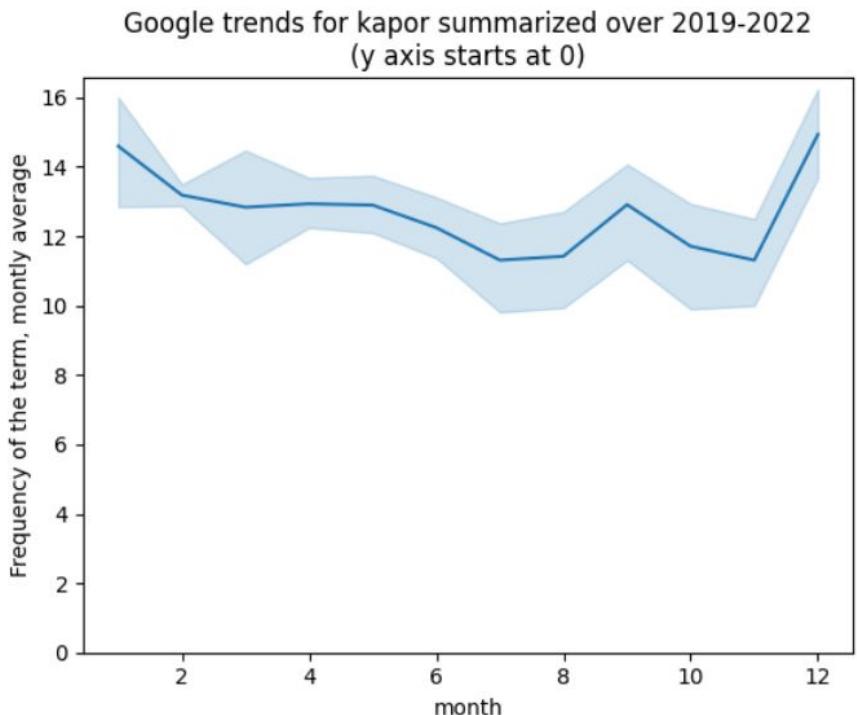


Overlapping timescales to display seasonality / showing uncertainty



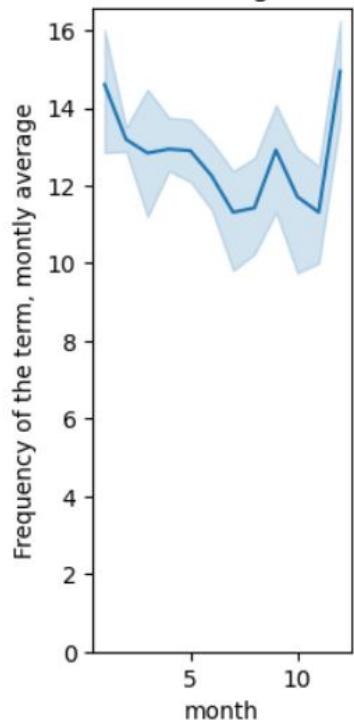
Right: multiple years summarized as the mean and its 95% confidence interval expressing uncertainty in the true value of the mean due to noise in data.

Importance of scales

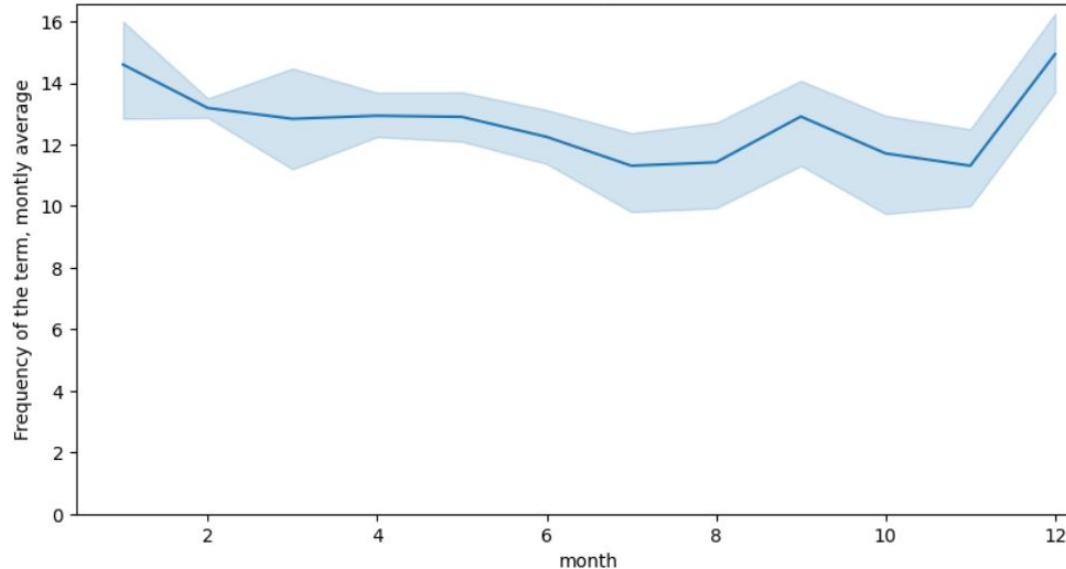


Importance of scales

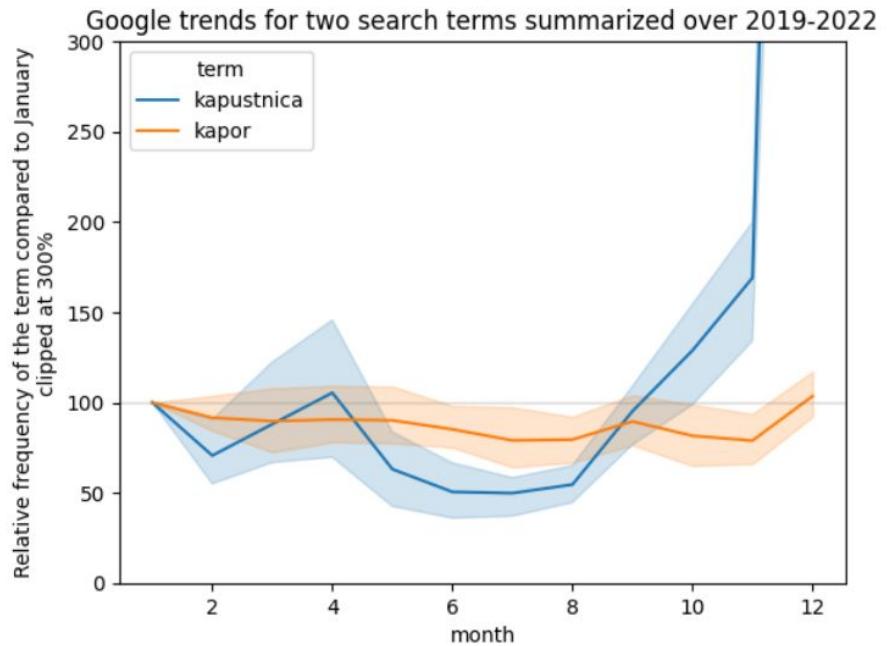
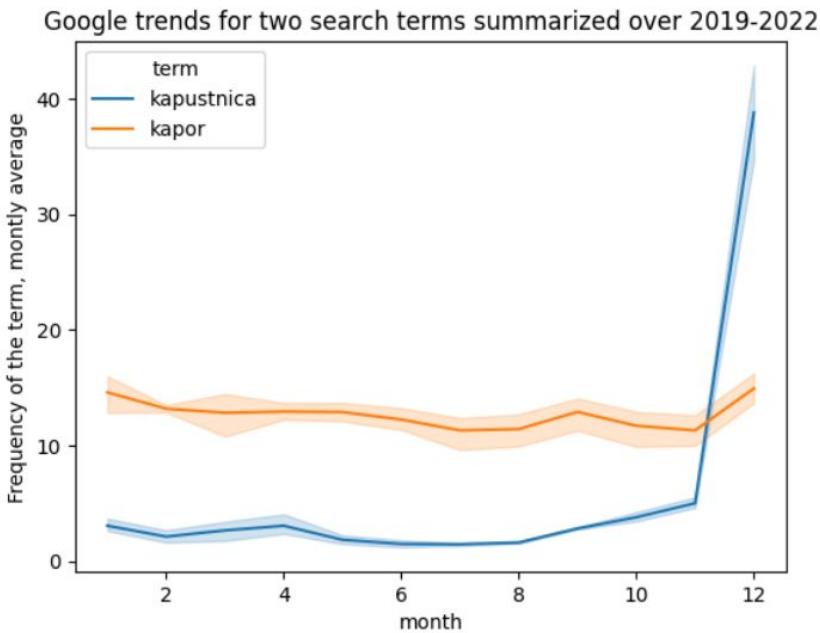
Google trends for kapor summarized over 2019-2022
(narrow figure)



Google trends for kapor summarized over 2019-2022
(wide figure)

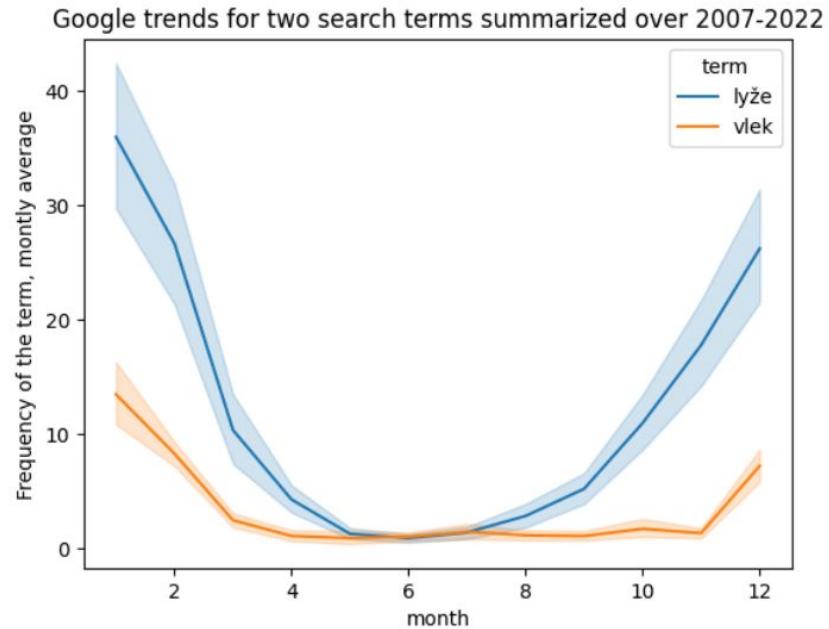
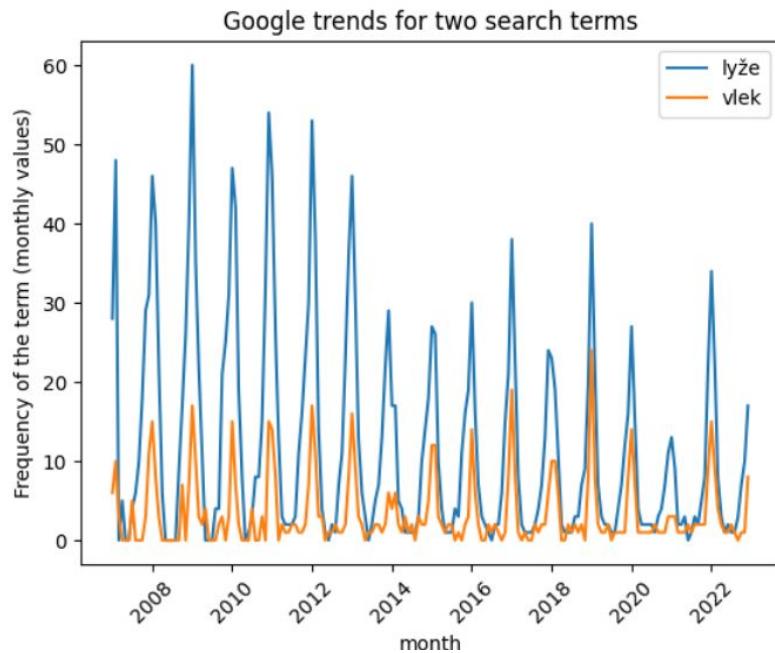


Relative scales

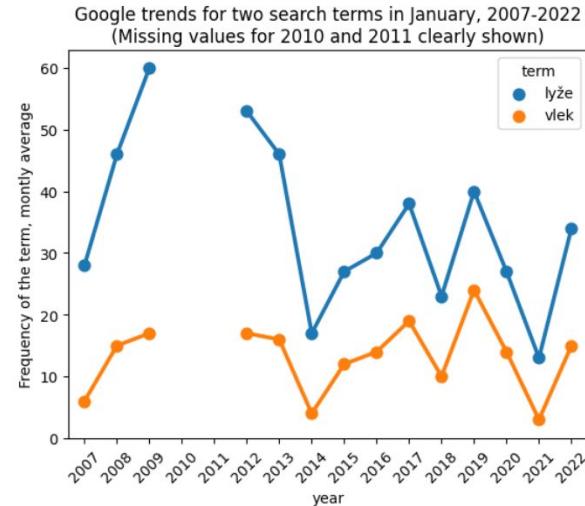
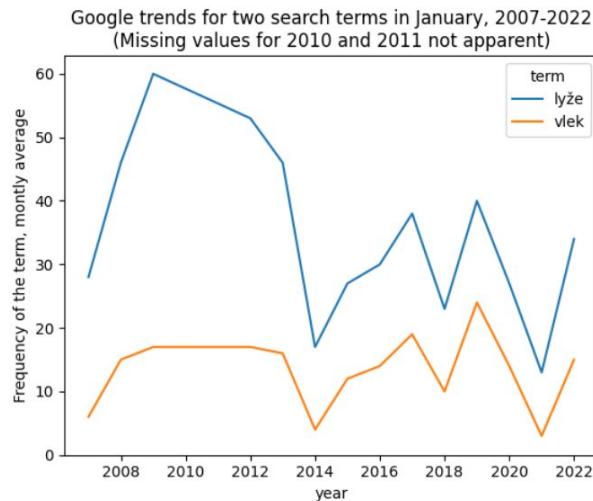
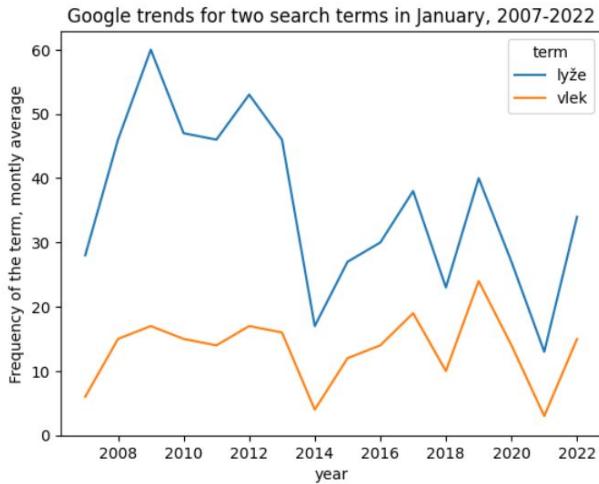


Right: monthly values relative to January
(can be used to compare trends even if overall values vary different)

One more pair of Google trend lines



Acknowledging missing values



Middle and right: values for 2010 and 2011 missing

Middle: missing values are not visible, misleading plot

Right: missing values are easy to spot

Summary of time series

Typical goals are to observe and study:

- overall trend (increasing / decreasing / flat; rate of change),
- seasonality (daily / weekly / yearly cycles),
- noise (general variability / outliers)

Useful techniques:

- smoothing by aggregation and sliding window
- overlapping timescales
- relative scales
- showing uncertainty and missing values

1 Lecture 6: Maps, graphs, time series

Data Visualization · 1-DAV-105

Lecture by Broňa Brejová

1.1 Package installation

We need to install several packages which are not pre-installed in Colab.

```
[1]: ! pip install geoplot pyvis
```

```
[2]: # importing our usual libraries
import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import plotly.express as px
from IPython.display import Markdown

# new libraries for today:
# geopandas is a library for working with geographical data
import geopandas as gpd
# geoplot is a library for visualizing geographical data
import geoplot as gplt
# we also will use a submodule of plotly
import plotly.graph_objects as go
# networkx is a library for working with graphs and networks
import networkx as nx
# Pyvis is a library for drawing networks
from pyvis.network import Network
```

1.2 Maps

1.2.1 Introduction

- Each map is a visualization of data about location of objects.
- Maps have a rich set of conventions about colors and symbols, orientation etc. This allows us to quickly understand a map.

Examples:

- A topographic map from US looks similar to maps used in Slovakia, but striped lines are typically used for railroads in Slovakia ([example](#)).
- A map of European countries from 1721 can still be easily read by today's audience.

Data visualization in maps

- Maps visualizing data other than typical geographical features are usually called thematic maps (tematické mapy).

- We will see several examples, for others see e.g. [Wikipedia](#), [GeoPlot library gallery](#).
- Also recall [Snow's map of cholera cases](#) from the first lecture.

1.2.2 Map projection (kartografické zobrazenie)

- A map projection is a transformation to project the surface of a globe onto a plane.
- Each projection introduces **some distortion**.

Conformal projections preserve local angles, but distort other aspects, such as lengths, areas etc.

- For example, Mercator projection (1569) was developed for navigation, but shows Greenland bigger than Africa, while in fact it is 14x smaller.

Equal-area projections preserve areas (cannot be conformal at the same time).

- Equal-area projections are typically good for data visualization, as they make areas comparable.

Orthographic projection is similar to a photograph of the Earth from a very distant point.

- It is not an equal-area projection, but our sense of perspective may compensate.
- It displays one hemisphere.

Recommended projections (Cairo, The Truthful Art):

- Whole world: e.g. Mollweide equal-area projection (1805)
- Continents / large countries: e.g. Lambert azimuthal equal-area projection (1772)
- Countries in mid-latitudes: e.g. Albers equal-area conic projection (1805)
- Polar regions: e.g. Lambert azimuthal equal-area projection (1772)

Examples of projections in Plotly

- Plotly allows us to set projections for our plot. Here we use it to illustrate the [projections](#) on the map of continent outlines.
- The maps are interactive.

```
[3]: def show_world(projection, scope=None):
    """A function to display the whole Earth or a desired
    area (scope) using a selected projection. Both arguments
    are strings that name projections or scopes supported by Plotly."""
    # create a map figure with an empty scatterplot
    fig = go.Figure(go.Scattergeo())
    # set the desired projection
    fig.update_geos(projection_type=projection)
    # we can also limit the scope of the map
    if scope is not None:
        fig.update_geos(scope=scope)
    # finally, make the image smaller and with 0 margins
    fig.update_layout(height=200, margin={"r":0, "t":0, "l":0, "b":0})
    # show the figure
    fig.show()
```

```
[4]: display(Markdown("##Orthographic projection"))
show_world("orthographic")
```

Orthographic projection

```
[5]: display(Markdown("##Mollweide equal-area projection"))
show_world("mollweide")
```

Mollweide equal-area projection

```
[6]: display(Markdown("##Mercator conformal projection (not recommended for data visualization)")
show_world("mercator"))
```

Mercator conformal projection (not recommended for data visualization)

```
[7]: display(Markdown("##Lambert azimuthal equal-area projection"))
show_world("azimuthal equal area", "europe")
```

Lambert azimuthal equal-area projection

1.2.3 Adding data as points and lines to a map

- Geographic coordinates of places can be projected as x and y. Additional values can be shown using marker color and size or line color and width.
- We illustrate this using datasets of airport locations and airline connections.

Importing datasets

- The dataset of international airports of the world was [downloaded](#) from the World Bank under the CC-BY 4.0 license, and preprocessed. It includes the number of seats within a year, which is from unknown years, possibly not comparable between countries.
- Our preprocessed file is in [GeoJSON](#) format used for describing simple geographical features. It contains both location data and other attributes.
- We parse the file using [GeoPandas](#), which is a library for working with geographical data.
- It is an extension of Pandas DataFrame, with location information.
- Each row of the table contains one airport, with its 3-letter code, name, country, 3-letter code of the country, the number of airplane seats per year and the location.

```
[8]: display(Markdown("##Importing the list of airports"))
# parse the file
airports = gpd.read_file("https://bbrejova.github.io/viz/data/airports.geojson")
# show the first 5 rows
display(Markdown("##The first five rows:"), airports.head())
# show the total number of rows
display(Markdown(f"##The number of rows:{airports.shape[0]}"))
display(Markdown("##International airports in Slovakia"))
display(airports.query('Country == "Slovakia"'))
```

Importing the list of airports

The first five rows:

```
Orig           Name  TotalSeats   Country ISO3 \
0  HEA          Herat    22041.971 Afghanistan AFG
1  JAA          Jalalabad  6343.512 Afghanistan AFG
2  KBL          Kabul International 1016196.825 Afghanistan AFG
3  KDH          Kandahar International 39924.262 Afghanistan AFG
4  MZR          Mazar-e-Sharif    58326.513 Afghanistan AFG
```

```
geometry
0  POINT (62.22670 34.20690)
1  POINT (70.50000 34.40000)
2  POINT (69.21390 34.56390)
3  POINT (65.84750 31.50690)
4  POINT (67.20830 36.70420)
```

The number of rows: 2173

International airports in Slovakia

```
Orig           Name  TotalSeats   Country ISO3 \
1489  BTS      M.R. Stefanik 1211732.116 Slovakia SVK
1490  ILZ      Zilina     3986.360 Slovakia SVK
1491  KSC      Barca      323259.132 Slovakia SVK
1492  PZY      Piestany Airport 1403.892 Slovakia SVK
1493  SLD      Sliac      11876.753 Slovakia SVK
1494  TAT      Tatry/Poprad 39612.286 Slovakia SVK
```

```
geometry
1489  POINT (17.21670 48.16670)
1490  POINT (18.76670 49.23330)
1491  POINT (21.25000 48.66670)
1492  POINT (17.83330 48.63330)
1493  POINT (19.13330 48.63330)
1494  POINT (20.24030 49.07190)
```

- We will later need a datasets of country boundaries proved by [Natural Earth](#).
- Below we estimate country area from its low resolution borders. For example, area of Slovakia estimated as 47070km², while World Bank lists as 49030km².

```
[9]: # read world countries as a dataset provided by Natural Earth
countries = gpd.read_file("https://bbrejova.github.io/viz/data/
                           ↪country_boundaries.geojson")
# set 3-letter code as the index
countries = countries.set_index('ISO3')
# estimate country area in square km from geometry
# first the geometry is projected by equal-area projection
# the result is in square meters, converted to squared km (divide by 1e6)
```

```

# beware that areas are approximate due to low resolution borders
country_areas = countries['geometry'].to_crs({'proj':'cea'}).area / 1e6
# add areas to countries
countries['Area'] = country_areas

display(Markdown("**Table of countries of the world**"))
display(countries.head())
display(Markdown("**Data for Slovakia**"))
display(countries.loc['SVK', :])

```

Table of countries of the world

| | Type | Name | Population | \ |
|------|---|--------------------------|-------------|---|
| IS03 | | | | |
| FJI | Sovereign country | Fiji | 889953.0 | |
| TZA | Sovereign country | Tanzania | 58005463.0 | |
| B28 | Indeterminate | W. Sahara | 603253.0 | |
| CAN | Sovereign country | Canada | 37589262.0 | |
| USA | Country | United States of America | 328239523.0 | |
| | | Region | \ | |
| IS03 | | | | |
| FJI | East Asia & Pacific | | | |
| TZA | Sub-Saharan Africa | | | |
| B28 | Middle East & North Africa | | | |
| CAN | North America | | | |
| USA | North America | | | |
| | | geometry | Area | |
| IS03 | | | | |
| FJI | MULTIPOLYGON (((180.00000 -16.06713, 180.00000... 1.928760e+04 | | | |
| TZA | POLYGON ((33.90371 -0.95000, 34.07262 -1.05982... 9.327793e+05 | | | |
| B28 | POLYGON ((-8.66559 27.65643, -8.66512 27.58948... 9.666925e+04 | | | |
| CAN | MULTIPOLYGON ((((-122.84000 49.00000, -122.9742... 1.003773e+07 | | | |
| USA | MULTIPOLYGON ((((-122.84000 49.00000, -120.0000... 9.509851e+06 | | | |

Data for Slovakia

| | |
|------------|---|
| Type | Sovereign country |
| Name | Slovakia |
| Population | 5454073.0 |
| Region | Europe & Central Asia |
| geometry | POLYGON ((22.558137648211755 49.08573802346714... |
| Area | 47069.779734 |
| Name: | SVK, dtype: object |

All airports as points using Plotly

- We use `scatter_geo` function from Plotly Express.

- We set parts of `geometry` column as latitude and longitude. Column `Name` is used as a tooltip.

```
[10]: fig = px.scatter_geo(
    airports,
    lat=airports.geometry.y,
    lon=airports.geometry.x,
    hover_name="Name",
    projection="mollweide"
)
fig.update_layout(height=300, margin={"r":0,"t":0,"l":0,"b":0})
fig.show()
```

Adding the size of the airport

- We use size of the circle to represent the number of seats.
- Scatterplots with point sizes are often called bubble graphs.
- We focus on Europe, add country borders and change the projection.

```
[11]: fig = px.scatter_geo(
    airports,
    lat=airports.geometry.y,
    lon=airports.geometry.x,
    size="TotalSeats",
    hover_name="Name"
)
fig.update_geos(
    projection_type="azimuthal equal area",
    lonaxis_range= [-20, 40],
    lataxis_range= [20, 70],
    showcountries = True
)
fig.update_layout(height=300, margin={"r":0,"t":0,"l":0,"b":0})
fig.show()
```

Airline connections from Slovakia as lines

- We import another table (originating from World bank as above), which shows international airline connections from Slovak airports (in an unknown year).
- Each connection is given by two airport codes, the number of airplane seats within a year, and geometry with a segment connecting the two airport locations.
- Line color will correspond to the airport of origin in Slovakia.
- The code is adapted from [examples](#) in the Plotly [documentation](#).

```
[12]: display(Markdown("## Importing airline connections"))
connections = gpd.read_file("https://bbrejova.github.io/viz/data/
                           airport_pairs_svk.geojson")
```

```
display(connections.head())
```

Importing airline connections

```
OrigCode DestCode TotalSeats \
0      BTS      ADB    7370.433
1      BTS      AGP   15152.501
2      BTS      AHO  14740.866
3      BTS      AQJ   3275.748
4      BTS      ATH  19654.488

                           geometry
0  LINESTRING (17.21670 48.16670, 27.15620 38.29430)
1  LINESTRING (17.21670 48.16670, -4.49810 36.67170)
2  LINESTRING (17.21670 48.16670, 8.28890 40.63060)
3  LINESTRING (17.21670 48.16670, 35.01940 29.61250)
4  LINESTRING (17.21670 48.16670, 23.94440 37.93640)
```

```
[13]: def draw_lines(connections):
    # create two lists with x and y coordinates of polylines
    # separated by None
    lats = []
    lons = []
    # also create lists of origin and destination codes parallel to lists above
    origCodes = []
    destCodes = []

    # iterate through table rows
    for index, row in connections.iterrows():
        # get lists of x and y coordinates (of length 2 in this case)
        x, y = row['geometry'].xy
        # add coordinates and None separator to lists
        lats.extend(list(y) + [None])
        lons.extend(list(x) + [None])
        # add airport codes for each coordinate and None separator
        origCodes.extend([row['OrigCode']] * len(x) + [None])
        destCodes.extend([row['DestCode']] * len(x) + [None])

    # create figure with these lists
    fig = px.line_geo(lat=lats, lon=lons, hover_name=destCodes, color=origCodes)
    # setup projection
    fig.update_geos(
        projection_type="azimuthal equal area",
        lonaxis_range= [-25, 55],
        lataxis_range= [10, 60],
        showcountries = True
    )
    fig.update_layout(height=300, margin={"r":0, "t":0, "l":0, "b":0})
```

```

fig.show()

# call the function to draw the map
display(Markdown("**Airline connections from Slovak airports**"))
draw_lines(connections)

```

Airline connections from Slovak airports

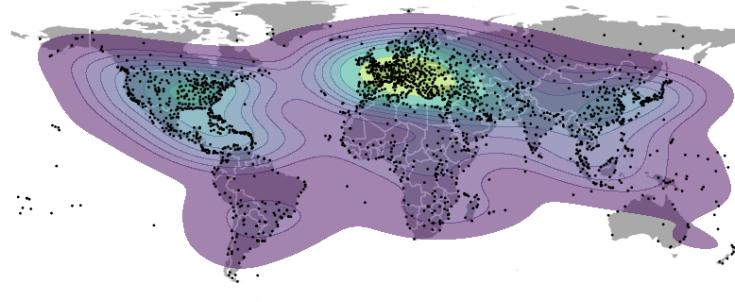
1.2.4 Isarithmic maps / isoline maps / heatmaps

- These maps display a continuous variable over the map area (elevation, temperature and other weather phenomena etc.).
- Value in each point can be shown by a color scale.
- Some contour lines can be displayed as well.
- A contour line (isoline, isopleth, isarithm, izočiara) connects points of the same value.
- Example: [short-term forecasts](#) from the Slovak Hydrometeorological Institute.

Density of airports

- Here we show world airports as both points and their local density as a isarithmic map.
- This is achieved using `kdeplot` function from the Geoplot library.
- KDE stands for kernel density estimation, and we will explain it in the next lecture.

```
[14]: # plot countries as a background
ax = gplt.polyplot(
    countries.explode(index_parts=True),
    edgecolor='white',
    facecolor='darkgray',
    figsize=(10, 5),
)
# plot semi-transparent isarithmic map
gplt.kdeplot(
    airports, cmap='viridis',
    fill=True, alpha=0.5, ax=ax
)
# plot points on top
gplt.pointplot(airports, s=1, color='black', ax=ax)
pass
```



1.2.5 Choropleth maps (kartogramy)

- Often we have numerical / categorical values for administrative regions (countries, districts, etc.).
- Choropleth maps show such variables via colors applied to the whole region.

Variables over regions:

- **Spatially extensive** variables apply to the unit as a whole (e.g. total population, area, the number of airports in the country). If we subdivide the region, spatially extensive variable will be often the sum of its parts (but not always, e.g. perimeter)
- **Spatially intensive** variables may stay the same if you divide the unit, provided the unit is homogeneous without regional differences. Examples include population density, life expectancy, GDP per person.
- Spatially extensive variables are not appropriate for choropleths, because large value for a large country is visually attributed to each small subregion of the country. If counts are of interest, better use a bubble graph with marker of appropriate size in the region center.

Beware:

- A choropleth map is called kartogram in Slovak.
- English word **cartogram** means a map with regions rescaled according to some variable (such as the [Levasseur's cartogram of country budgets](#) and [a modern example](#)).

Choropleth maps of airports per country We will show three choropleth maps:

- the number of airports per 10000 km² (spatially intensive variable),
- the number of airports per million inhabitants (also spatially intensive),
- the number of airports (spatially extensive, not recommended for choropleth), We will also show the number of airports as a bubble graph (more appropriate than extensive variable).

All choropleth maps are created by [Plotly](#). The bubble graph is also created by plotly, and the bubble is placed to the [representative point](#) of each country.

```
[15]: # compute the number of airports per country by groupby
airports_per_country = airports.groupby('ISO3').size()
# add the new column to a copy of the old table
countries2 = countries.copy(deep=True)
# add the number of airports as a new column
countries2['Airports'] = airports_per_country
# remove countries where airports or location are missing
countries2.dropna(subset=['geometry', 'Airports'], inplace=True)
# add columns with airport density and airports per million people
countries2['Airport_density'] = (countries2['Airports']
                                  / countries2['Area'] * 10000)
countries2['Airports_per_mil'] = (countries2['Airports']
                                  / countries2['Population'] * 1e6)
# show the new table
```

```

display(Markdown("##The first five rows of `countries2` table:"))
display(countries2.head())
display(Markdown("##The values for Slovakia:"))
display(countries2.loc['SVK'])

```

The first five rows of countries2 table:

| | Type | Name | Population | \ |
|------|--|--------------------------|------------------|---|
| IS03 | | | | |
| FJI | Sovereign country | Fiji | 889953.0 | |
| TZA | Sovereign country | Tanzania | 58005463.0 | |
| CAN | Sovereign country | Canada | 37589262.0 | |
| USA | Country | United States of America | 328239523.0 | |
| KAZ | Sovereignty | Kazakhstan | 18513930.0 | |
| | Region | \ | | |
| IS03 | | | | |
| FJI | East Asia & Pacific | | | |
| TZA | Sub-Saharan Africa | | | |
| CAN | North America | | | |
| USA | North America | | | |
| KAZ | Europe & Central Asia | | | |
| | | geometry | Area | \ |
| IS03 | | | | |
| FJI | MULTIPOLYGON (((180.00000 -16.06713, 180.00000... 1.928760e+04 | | | |
| TZA | POLYGON ((33.90371 -0.95000, 34.07262 -1.05982... 9.327793e+05 | | | |
| CAN | MULTIPOLYGON ((((-122.84000 49.00000, -122.9742... 1.003773e+07 | | | |
| USA | MULTIPOLYGON ((((-122.84000 49.00000, -120.00000... 9.509851e+06 | | | |
| KAZ | POLYGON ((87.35997 49.21498, 86.59878 48.54918... 2.728701e+06 | | | |
| | Airports | Airport_density | Airports_per_mil | |
| IS03 | | | | |
| FJI | 2.0 | 1.036935 | 2.247310 | |
| TZA | 7.0 | 0.075045 | 0.120678 | |
| CAN | 82.0 | 0.081692 | 2.181474 | |
| USA | 291.0 | 0.305998 | 0.886548 | |
| KAZ | 17.0 | 0.062301 | 0.918228 | |

The values for Slovakia:

| | |
|-----------------|---|
| Type | Sovereign country |
| Name | Slovakia |
| Population | 5454073.0 |
| Region | Europe & Central Asia |
| geometry | POLYGON ((22.558137648211755 49.08573802346714... |
| Area | 47069.779734 |
| Airports | 6.0 |
| Airport_density | 1.274703 |

```
Airports_per_mil           1.100095
Name: SVK, dtype: object
```

```
[16]: def draw_choropleth(data, column, range_color=None, label=None):
    fig = px.choropleth(
        data, locations=data.index, color=column,
        range_color=range_color,
        labels={column:label},
        hover_name="Name",
        projection = "mollweide"
    )
    fig.update_layout(height=300, margin={"r":0,"t":0,"l":0,"b":0})
    fig.show()

display(Markdown("**The number of airports per 10000 squared km**"))
draw_choropleth(countries2, 'Airport_density', (0, 2), 'airports / 10000 km2')
```

The number of airports per 10000 squared km

```
[17]: display(Markdown("**The number of airports per million inhabitans**"))
draw_choropleth(countries2, 'Airports_per_mil', (0, 5), 'airports / million ↴people')
```

The number of airports per million inhabitans

```
[18]: display(Markdown("**The number of airports in a country**"))
draw_choropleth(countries2, 'Airports', (0, 100), 'airports')
```

The number of airports in a country

```
[19]: # make a new table of countries in which geometry is replaced
# with a single representative point
countries3 = countries2.copy(deep=True)
countries3['geometry'] = countries2['geometry'].representative_point()

# plot as a bubble plot
display(Markdown("**The number of airports in a country**"))
fig = px.scatter_geo(
    countries3,
    lat=countries3.geometry.y,
    lon=countries3.geometry.x,
    size="Airports",
    hover_name="Name",
    projection = "mollweide"
)
fig.update_geos(showcountries = True)
fig.update_layout(height=300, margin={"r":0,"t":0,"l":0,"b":0})
fig.show()
```

The number of airports in a country

1.2.6 Summary of maps

- Many data sets contain geographic entities (countries, cities, coordinates).
- Displaying such data on maps highlights spatial relationships.
- In your maps, use appropriate equal-area projections.

Types of thematic maps:

- Bubble plots contain points of various sizes and colors.
- Isarithmic maps / isoline maps / heatmaps display continuously varying variables, such as elevation or temperature using color scales or isolines.
- Choropleth map display variables characterizing whole region using colors. The variable used in choropleth should be intensive, e.g. normalized by area or population.

Several useful libraries:

- Geopandas for working with geographical data, extension of DataFrame
- Geoplot and Plotly for visualization

1.3 Graphs and hierarchies

1.3.1 Graphs

- A **graph** / **network** consists of **vertices** (vrcholy; also nodes, uzly) and **edges** (hrany; also links, arcs).
- Vertices often represent real-world **entities**.
- Edges often represent **relationships** and connections between pairs of vertices.

Many real-world examples of graphs: places connected by roads, computers connected by network cables, people connected by family or work relationships, companies connected by financial transactions, texts connected by references, tasks or courses connected by dependencies, any objects connected based on similarity / shared features.

- Edges can be directed (orientované) or undirected depending on whether the relationship is symmetrical.
- Recall: how did you define directed / undirected edges in discrete mathematics?

Graphs are very important in both computer science and data science. They are covered in several courses: discrete mathematics, programming, design of efficient algorithms, network science.

1.3.2 Trees and hierarchies

- An undirected graph is called a **tree** if it is connected and without cycles.
- In practice we usually encounter rooted (directed) trees, which have a single **root**, all other vertices can be reached from the root via a unique path.
- This gives rise to parent / child relationships between nodes (parent is the node closer to the root).
- Trees can express hierarchies in which each entity has a single direct superior, for example:
 - company structure in which each employee (except for the head of the company) has a single supervisor (similarly army command),
 - administrative divisions (country, region, district),

- species taxonomy (animals, mammals, primates, ...).
- However some hierarchies allow multiple direct superiors, for example:
 - family tree where each person has two parents (and they may be distantly related),
 - geometrical shapes, where a square is both a special case of a regular polygon and a special case of a rectangle and both of these are a special case of a polygon.
- These hierarchies can be represented as directed acyclic graphs.
 - Acyclic means that by following edges we never get back to the starting node (nobody is their own ancestor).

1.3.3 What do we study / visualize in real-life graphs?

- Details of connections for a particular node (requires zooming in large networks).
- Overall structure of the graph: connected components, density of edges, presence of cycles, weak places (bridges and articulations), clusters of densely connected nodes.
- Do nodes with some property cluster together? (Are they connected by many edges?)

See for example character co-occurrence in [Shakespeare's tragedies](#).

1.3.4 Basics of graph drawing

- Vertices are typically displayed as markers (circles, rectangles etc.), possibly with labels, size, color, ...
- Edges are displayed as lines connecting them, possibly of different color or width. They can be straight lines, arcs, polygonal lines or arbitrary curves.
- Edge direction displayed as arrows or in a hierarchy edges may be drawn to point in one direction, e.g. downwards.

Desirable properties:

- Nodes do not overlap.
- Edges are not too long and have a simple shape without many bends.
- The number of edge crossings is small.
- The graph uses the space of the figure well without large empty regions.

Node positioning:

- Sometimes the position of nodes is given by their properties, e.g. on a map (see airline connections), level of a hierarchy, timeline.
- Otherwise we try to place nodes to optimize desirable properties, e.g. using force-directed layout, which assigns attractive forces (springs) between nodes connected by edges and repulsive forces between other pairs of nodes.

Examples:

- <https://en.wikipedia.org/wiki/Graphviz#/media/File:UnitedStatesGraphViz.svg>
- https://upload.wikimedia.org/wikipedia/commons/9/90/Visualization_of_wiki_structure_using_prefuse_.svg

1.3.5 Displaying a simple hierarchy in NetworkX

- We start by creating a simple tree representing taxonomy of selected even-toed ungulates (párnokopytníky) as a Pandas DataFrame.

- Each row of the data frame describes each node, giving its name, parent, level along the tree (leaves are 1, root is 5) and category, which is `land` for land animals, `sea` for sea animals and `group` for taxonomy groups.
- Group `Artiodactyla` is the root without a parent.

```
[20]: from io import StringIO

animal_csv = StringIO("""name,parent,level,category
camel,Artiodactyla,1,land
pig,Artiofabula,1,land
sheep,Caprinae,1,land
goat,Caprinae,1,land
cow,Bovidae,1,land
dolphin,Cetacea,1,sea
whale,Cetacea,1,sea
hippopotamus,Whippomorpha,1,land
Caprinae,Bovidae,2,group
Cetacea,Whippomorpha,2,group
Bovidae,Cetruminantia,3,group
Whippomorpha,Cetruminantia,3,group
Cetruminantia,Artiofabula,4,group
Artiofabula,Artiodactyla,5,group
Artiodactyla,,6,group""")

animals = pd.read_csv(animal_csv)
animals['category'] = animals['category'].astype('category')
display(animals)
```

| | name | parent | level | category |
|----|---------------|---------------|-------|----------|
| 0 | camel | Artiodactyla | 1 | land |
| 1 | pig | Artiofabula | 1 | land |
| 2 | sheep | Caprinae | 1 | land |
| 3 | goat | Caprinae | 1 | land |
| 4 | cow | Bovidae | 1 | land |
| 5 | dolphin | Cetacea | 1 | sea |
| 6 | whale | Cetacea | 1 | sea |
| 7 | hippopotamus | Whippomorpha | 1 | land |
| 8 | Caprinae | Bovidae | 2 | group |
| 9 | Cetacea | Whippomorpha | 2 | group |
| 10 | Bovidae | Cetruminantia | 3 | group |
| 11 | Whippomorpha | Cetruminantia | 3 | group |
| 12 | Cetruminantia | Artiofabula | 4 | group |
| 13 | Artiofabula | Artiodactyla | 5 | group |
| 14 | Artiodactyla | NaN | 6 | group |

- `NetworkX` is a large library for working with graphs, it implements many graph algorithms.
- Below we convert our DataFrame to `Graph` class from NetworkX by adding nodes and edges.
- Nodes and edges can have arbitrary attributes attached, here `level` and `category`.

- Then we plot basic representation of the graph.
- The plotting works in two steps: first we compute coordinates of all nodes using `multipartite_layout`.
- Then we plot the network using `draw_networkx` into Matplotlib axes.
- The plot is not very nice, we will improve it below.

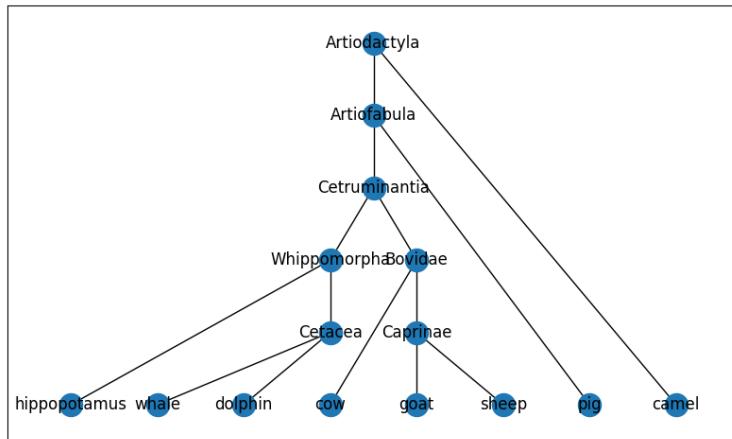
```
[21]: # create empty graph in NetworkX
G = nx.Graph()

# adding each table row as a node
for index, row in animals.iterrows():
    G.add_node(row['name'], level=row['level'], category=row['category'])

# adding an edge to each node from its parent
for index, row in animals.iterrows():
    if row['parent'] is not np.nan:
        G.add_edge(row['parent'], row['name'])

# computing coordinates of nodes
coordinates = nx.multipartite_layout(G, subset_key="level", align='horizontal')
# drawing the graph
(figure, axes) = plt.subplots(figsize=(10, 6))
nx.draw_networkx(G, coordinates, ax=axes)

pass
```



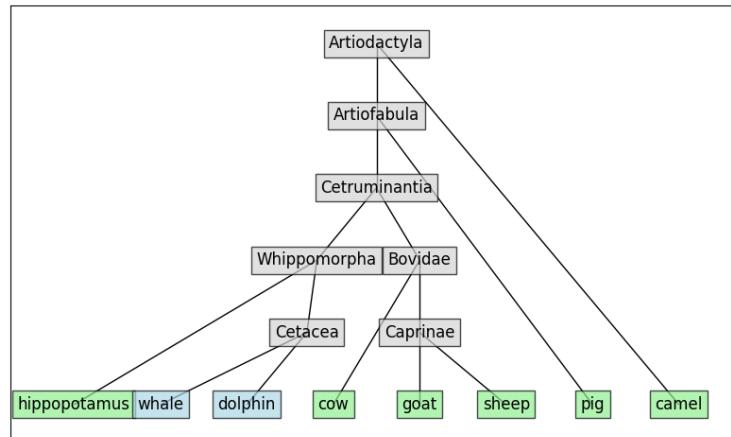
- Below we show an improved version of the plot.
- Two nodes are moved manually to reduce overlaps.
- Edges are plotted first.
- Then we draw node labels as boxes with text.
- Each category of nodes is drawn separately with a different background color.

```
[22]: # again compute coordinates and move some of them manually
coordinates2 = nx.multipartite_layout(G, subset_key="level", align='horizontal')
coordinates2["Whippomorpha"] += (-0.05, 0)
coordinates2["Cetacea"] += (-0.08, 0)

# plot edges only, omit nodes for now
(figure, axes) = plt.subplots(figsize=(10, 6))
nx.draw_networkx_edges(G, coordinates2, ax=axes)

# plot each category of nodes by a different color
color_dict = {'group':'lightgray', 'land':'lightgreen', 'sea':'lightblue'}
for category in color_dict:
    # create a list of nodes on the category
    category_nodes = [v for v in G.nodes if G.nodes[v]['category']==category]
    # select subgraph H of G
    H = G.subgraph(category_nodes)
    # create a dictionary of node label attributes
    label_options = {"ec": "black", "fc": color_dict[category], "alpha": 0.7}
    # draw the node labels as boxes
    nx.draw_networkx_labels(H, coordinates2, font_size=12, bbox=label_options, ax=axes)

pass
```



1.3.6 Hierarchy as a treemap in Plotly Express

- PlotlyExpress can be used to easily create treemaps.
- Leaves of the tree are empty labeled rectangles, upper categories are enclosing boxes.
- To select box colors, we use `color_dict` created above.

```
[23]: import plotly.express as px
fig = px.treemap(
    names=animals['name'],
    parents=animals['parent'],
    color=animals['category'],
    color_discrete_map=color_dict
)
fig.show()
```

1.3.7 Book character connections in Pyvis

- Here we use an example network from the NetworkX library.
- It represents [character co-occurrence](#) in the novel Les Misérables by Victor Hugo.
- Edges are weighted by how often characters co-occur.
- To make the plot interactive, we use [Pyvis](#) library.
- We convert NetworkX graph to [Network](#) class from Pyvis.
- We add two new features for each node: `title` (used as a tooltip, name of the character) and `value` (used as a size of the node, representing its number of neighbors, i.e. degree).
- Visualization is saved as a HTML file which is then displayed using [HTML](#) class from IPython library.

```
[24]: # initializing an empty network, setup plot properties
pyvis_net = Network("500px", "500px", notebook=True, cdn_resources='in_line')
# loading network from NetworkX
pyvis_net.from_nx(nx.les_miserables_graph())

# get a dictionary of neighbors for each node
neighbors = pyvis_net.get_adj_list()
# add additional node properties
# used as tooltip and size
for node in pyvis_net.nodes:
    node["title"] = node["id"]
    node["value"] = len(neighbors[node["id"]])

# saving the visualization in an html file
pyvis_net.show("net.html")
# displaying the html file in the notebook
from IPython.display import display, HTML
display(HTML('net.html'))
pass
```

`net.html`

1.3.8 Summary of graphs

- Graphs are important in many applications.
- NetworkX library has many functions for working with graphs, including several layout algorithms for visualization.

- Pyvis allows interactive visualization of graphs.
- Plotly can visualize trees as treemaps.

1.4 Time series (časové rady)

- Time series are sequences of measurements or values over time (in regular or irregular time intervals).
- Typically displayed as a line graph, with time as x-axis, time flowing from left to right (a cultural convention in western countries).
- Other options for drawing time series exist (bar graphs, heat maps, box plots, ...).

Typical features of a time series:

- overall trend (increasing / decreasing / flat; rate of change),
- seasonality (daily / weekly / yearly cycles),
- noise (general variability / outliers)

We have seen some examples in the first lecture:

- Playfair's atlas, foreign trade
- Hockey stick graph of global temperature (Fig.3a)

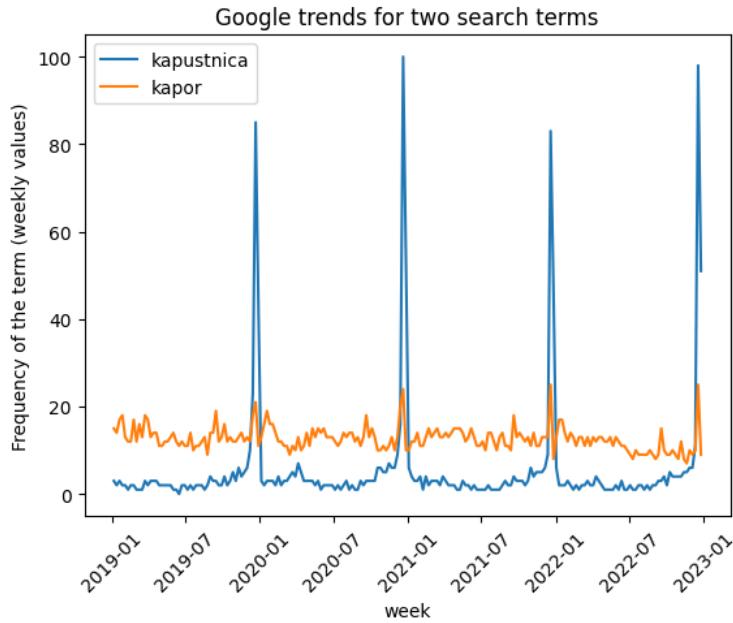
1.4.1 Two Google trend time series

- Google trends allow users to compare frequency of search terms over time and to each other.
- Here we use Christmas-related terms *kapustnica* and *kapor*.

```
[25]: url = "https://bbrejova.github.io/viz/data/kapustnica-kapor.csv"
trends1 = pd.read_csv(url, parse_dates=['week']).set_index('week')
display(trends1.head())
```

| | kapustnica | kapor |
|------------|------------|-------|
| week | | |
| 2019-01-06 | 3 | 15 |
| 2019-01-13 | 2 | 14 |
| 2019-01-20 | 3 | 17 |
| 2019-01-27 | 2 | 18 |
| 2019-02-03 | 2 | 13 |

```
[26]: axes = sns.lineplot(trends1, dashes=False)
axes.set_ylabel("Frequency of the term (weekly values)")
axes.set_title("Google trends for two search terms")
# rotate tick labels
axes.tick_params(axis='x', labelrotation = 45)
pass
```



- With kapustnica we see a clear seasonal trend.
- But kapor behaves differently. As related search terms Google reports zbgis kataster, zbgis mapa, zgbis, katasterportal list vlastnictva, dáždovka. Can you explain this?

1.4.2 Smoothing data (vyrovnanie, vyhľadenie)

- Time series above is measured weekly and is quite noisy.
- We can smooth the data e.g. by **aggregating** them in longer time intervals. Here we compute mean value in each month (4 or 5 weeks).
- This is done using `resample` method from Pandas.
- An alternative is to use a **sliding window** (klzavé okno), where we choose a window size. e.g. 4 weeks and compute a new series, each value being mean or other summary of 4 consecutive windows in the input.
- For example with values 2,6,4,2,8,2 and window size 4, we get window means 3.5, 5, 4.

```
[27]: # aggregate google trends from weekly to monthly mean (ME means month-end, in
      ↴older versions use M)
trends1monthly = trends1.resample('ME').mean()
display(Markdown("**New table of monthly means** (the first 5 rows)"))
display(trends1monthly.head())
display(Markdown("**The number of values aggregated in each month** (the first
      ↴5 values)"))
display(trends1.resample('ME').size().head())
```

New table of monthly means (the first 5 rows)

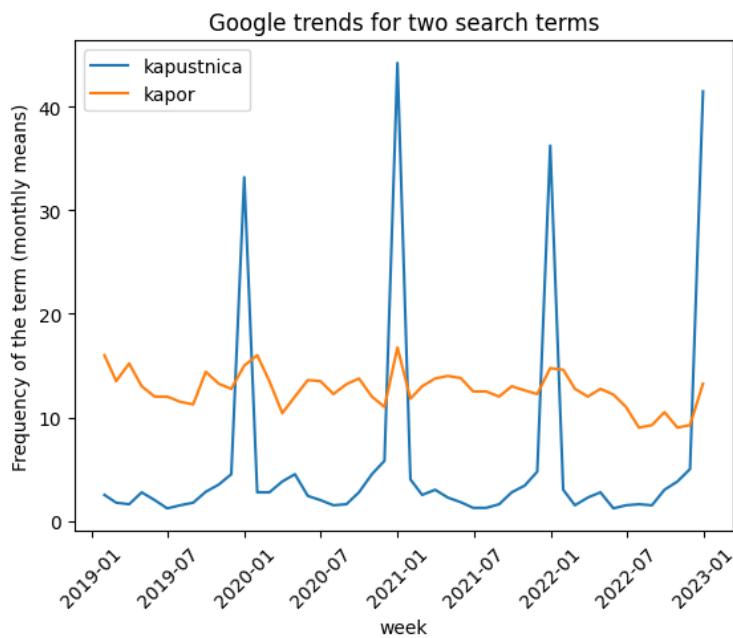
| week | kapustnica | kapor |
|------|------------|-------|
|------|------------|-------|

| | | |
|------------|------|------|
| 2019-01-31 | 2.50 | 16.0 |
| 2019-02-28 | 1.75 | 13.5 |
| 2019-03-31 | 1.60 | 15.2 |
| 2019-04-30 | 2.75 | 13.0 |
| 2019-05-31 | 2.00 | 12.0 |

The number of values aggregated in each month (the first 5 values)

```
week
2019-01-31    4
2019-02-28    4
2019-03-31    5
2019-04-30    4
2019-05-31    4
Freq: ME, dtype: int64
```

```
[28]: axes = sns.lineplot(trends1monthly, dashes=False)
axes.set_ylabel("Frequency of the term (monthly means)")
axes.set_title("Google trends for two search terms")
axes.tick_params(axis='x', labelrotation = 45)
pass
```



1.4.3 Trend: temperatures are growing in spring

- We will also look at a dataset displaying a trend: series of temperature values from Piešťany from January to June 2010, downloaded from [US National Oceanic and Atmospheric Administration](#).
- We show both the original data and values smoothed with rolling average.

```
[29]: # read a dataset of temperatures in Piešťany
url="https://bbrejova.github.io/viz/data/piestany-weather.csv"
weather = pd.read_csv(url, parse_dates=['DATE']).set_index('DATE')
# select only columns with daily maximum temperatures
temperature = weather["TMAX"]
# select only period from January to June 2010
spring2010 = temperature[pd.Timestamp('2010-01-01'):pd.Timestamp('2010-06-30')]
display(spring2010)
```

DATE

| | |
|------------|------|
| 2010-01-01 | 7.8 |
| 2010-01-02 | 1.8 |
| 2010-01-03 | -1.1 |
| 2010-01-04 | -1.4 |
| 2010-01-05 | -1.1 |
| | .. |
| 2010-06-26 | NaN |
| 2010-06-27 | 25.0 |
| 2010-06-28 | 27.8 |
| 2010-06-29 | 28.2 |
| 2010-06-30 | 29.5 |

Name: TMAX, Length: 181, dtype: float64

```
[30]: # compute rolling averages in a window of 5 and 30 days
spring2010rolling5 = spring2010.rolling(5, min_periods=2).mean()
spring2010rolling30 = spring2010.rolling(30, min_periods=10).mean()
spring2010rolling5.head(10)
```

[30]: DATE

| | |
|------------|-----------|
| 2010-01-01 | NaN |
| 2010-01-02 | 4.800000 |
| 2010-01-03 | 2.833333 |
| 2010-01-04 | 1.775000 |
| 2010-01-05 | 1.200000 |
| 2010-01-06 | -0.200000 |
| 2010-01-07 | -0.460000 |
| 2010-01-08 | -0.300000 |
| 2010-01-09 | 1.125000 |
| 2010-01-10 | 1.866667 |

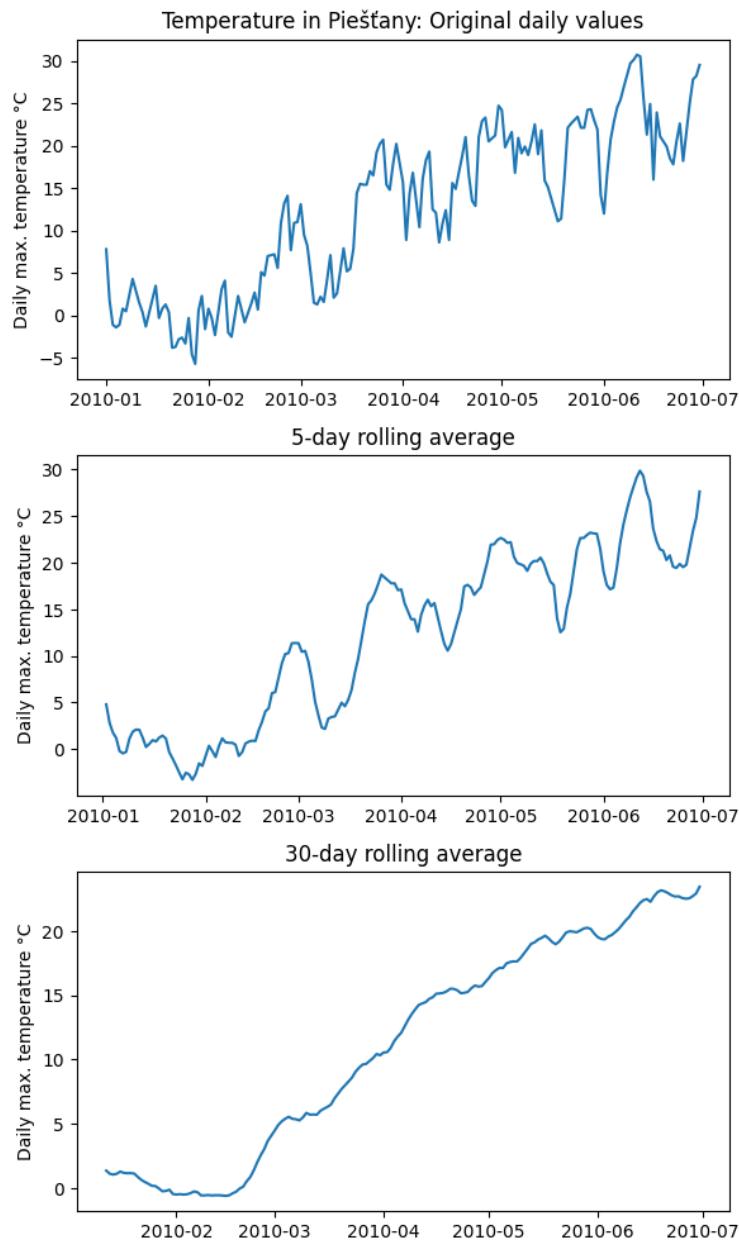
Name: TMAX, dtype: float64

```
[31]: (figure, axes) = plt.subplots(3, 1, figsize=(6, 10))
sns.lineplot(spring2010, ax=axes[0])
sns.lineplot(spring2010rolling5, ax=axes[1])
sns.lineplot(spring2010rolling30, ax=axes[2])
axes[0].set_title("Temperature in Piešťany: Original daily values")
axes[1].set_title("5-day rolling average")
```

```

axes[2].set_title("30-day rolling average")
for i in range(3):
    axes[i].set_ylabel("Daily max. temperature °C")
    axes[i].set_xlabel(None)
figure.tight_layout(pad=1.0)
pass

```



1.4.4 Overlapping timescales to display seasonality

- We can better see cyclical trends if we plot each cycle on the same x-axis scale.
- In our Google example, we will use the month as the x axis and plot individual years as lines.

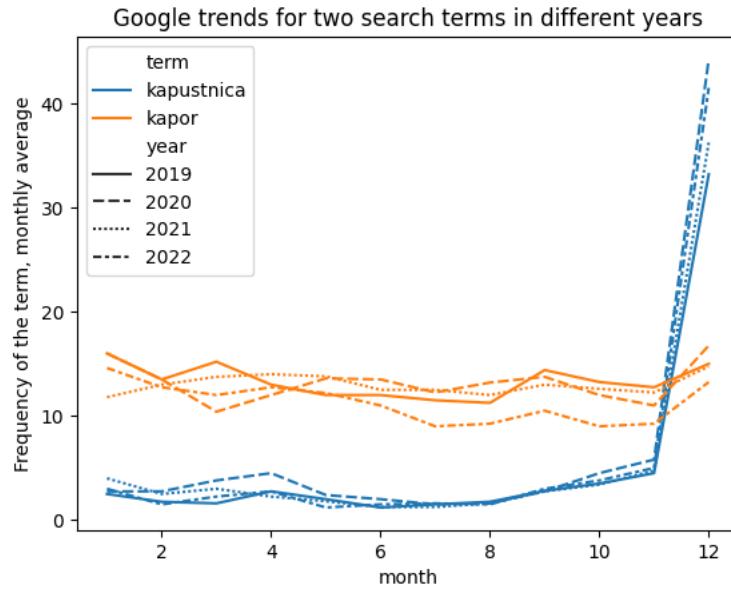
```
[32]: # convert monthly table to long format with separate rows for kapustnica and kapor
trends1monthlyLong = trends1monthly.reset_index().melt(id_vars=['week'])
trends1monthlyLong.rename(columns={'variable':'term', 'value':'frequency'}, inplace=True)
# create separate columns with year and month
trends1monthlyLong['month'] = trends1monthlyLong['week'].dt.month
trends1monthlyLong['year'] = trends1monthlyLong['week'].dt.year
display(Markdown("**Monthly table in the long format**"))
display(trends1monthlyLong)
```

Monthly table in the long format

| | week | term | frequency | month | year |
|----|------------|------------|-----------|-------|------|
| 0 | 2019-01-31 | kapustnica | 2.50 | 1 | 2019 |
| 1 | 2019-02-28 | kapustnica | 1.75 | 2 | 2019 |
| 2 | 2019-03-31 | kapustnica | 1.60 | 3 | 2019 |
| 3 | 2019-04-30 | kapustnica | 2.75 | 4 | 2019 |
| 4 | 2019-05-31 | kapustnica | 2.00 | 5 | 2019 |
| .. | .. | .. | .. | .. | .. |
| 91 | 2022-08-31 | kapor | 9.25 | 8 | 2022 |
| 92 | 2022-09-30 | kapor | 10.50 | 9 | 2022 |
| 93 | 2022-10-31 | kapor | 9.00 | 10 | 2022 |
| 94 | 2022-11-30 | kapor | 9.25 | 11 | 2022 |
| 95 | 2022-12-31 | kapor | 13.25 | 12 | 2022 |

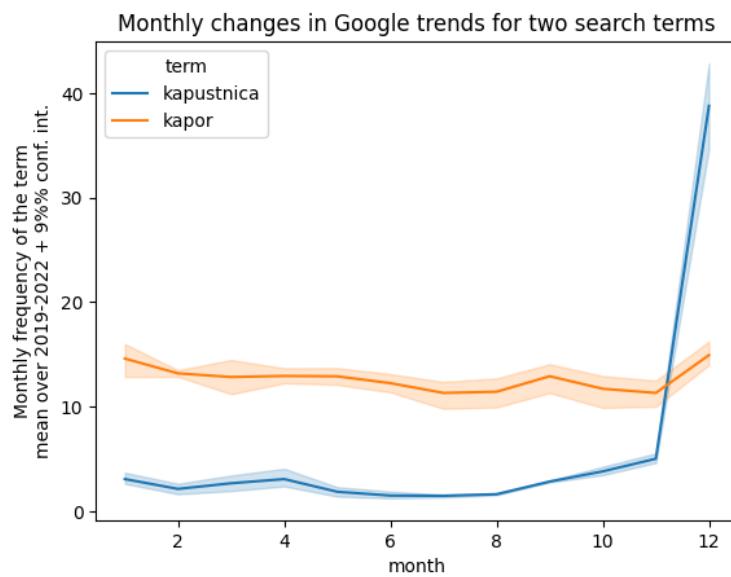
[96 rows x 5 columns]

```
[33]: # use month as x, separate years by line style and search terms by color
axes = sns.lineplot(trends1monthlyLong, x='month', y='frequency', hue='term', style='year')
axes.set_title("Google trends for two search terms in different years")
axes.set_ylabel("Frequency of the term, monthly average")
pass
```



- We can see that across years the trend is quite stable.
- Below we see another version of the figure where multiple lines for years are replaced with mean and its 95% confidence interval expressing our uncertainty in the true value of the mean due to noise in data.

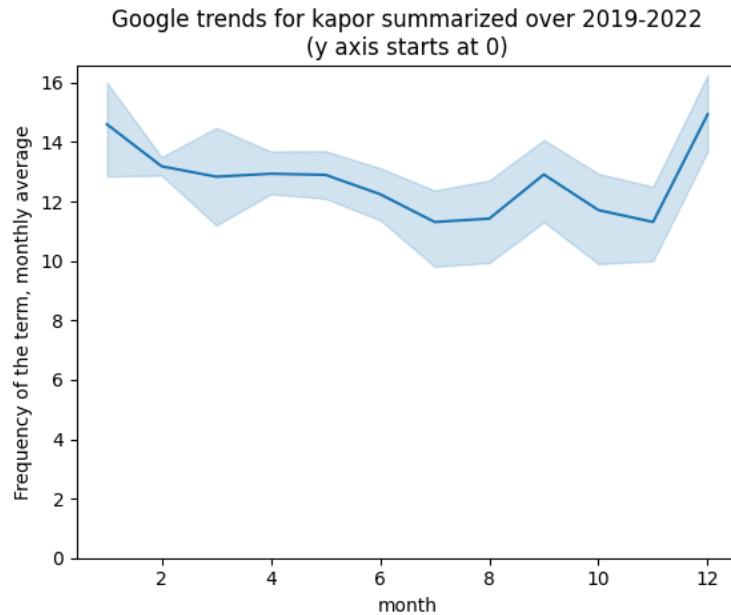
```
[34]: axes = sns.lineplot(trends1monthlyLong, x='month', y='frequency', hue='term')
axes.set_title("Monthly changes in Google trends for two search terms")
axes.set_ylabel("Monthly frequency of the term\nmean over 2019-2022 + 95% conf.\u2022int.")
pass
```



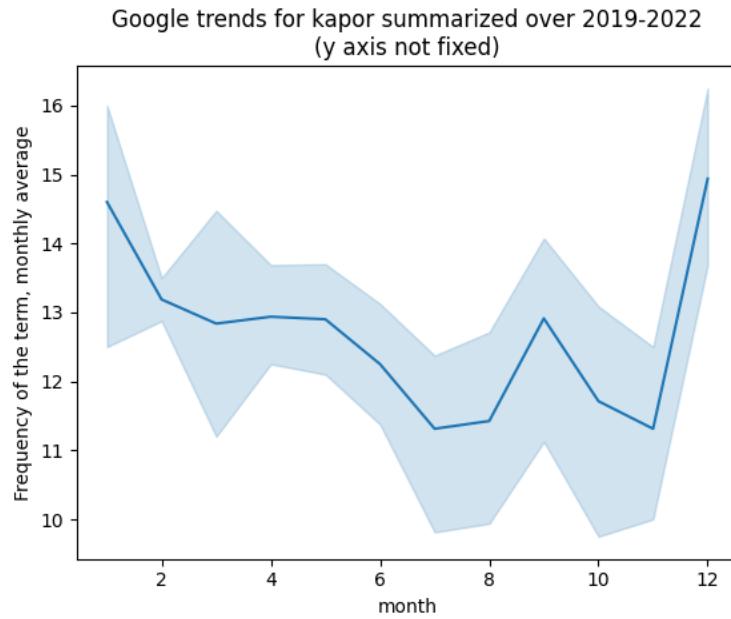
1.4.5 Importance of scales

- The plot below shows that if we do not start y axis at 0, differences in kapor searches may appear exaggerated.
- The next two plots show that even with y axis starting at 0, the time series may appear more variable with narrower aspect ratio of the figure.

```
[35]: kapor = trends1monthlyLong.query("term=='kapor'")  
axes = sns.lineplot(kapor, x='month', y='frequency')  
axes.set_title("Google trends for kapor summarized over 2019-2022\n(y axis  
starts at 0)")  
axes.set_ylabel("Frequency of the term, monthly average")  
axes.set_ylim(ymin=0)  
pass
```

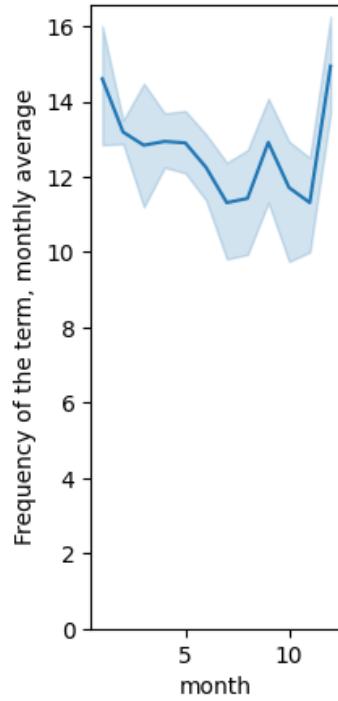


```
[36]: axes = sns.lineplot(kapor, x='month', y='frequency')  
axes.set_title("Google trends for kapor summarized over 2019-2022\n(y axis not  
fixed)")  
axes.set_ylabel("Frequency of the term, monthly average")  
pass
```

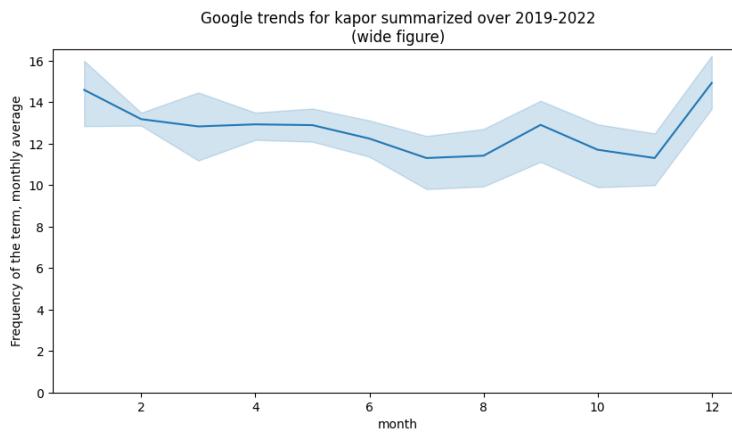


```
[37]: (figure, axes) = plt.subplots(figsize=(2,5))
sns.lineplot(kapor, x='month', y='frequency', ax=axes)
axes.set_title("Google trends for kapor summarized over 2019-2022\n(narrowed figure)")
axes.set_ylabel("Frequency of the term, monthly average")
axes.set_ylim(ymin=0)
pass
```

Google trends for kapor summarized over 2019-2022
(narrow figure)



```
[38]: (figure, axes) = plt.subplots(figsize=(10,5))
sns.lineplot(kapor, x='month', y='frequency', ax=axes)
axes.set_title("Google trends for kapor summarized over 2019-2022\n(wide figure)")
axes.set_ylabel("Frequency of the term, monthly average")
axes.set_ylim(ymin=0)
pass
```



1.4.6 Relative scales

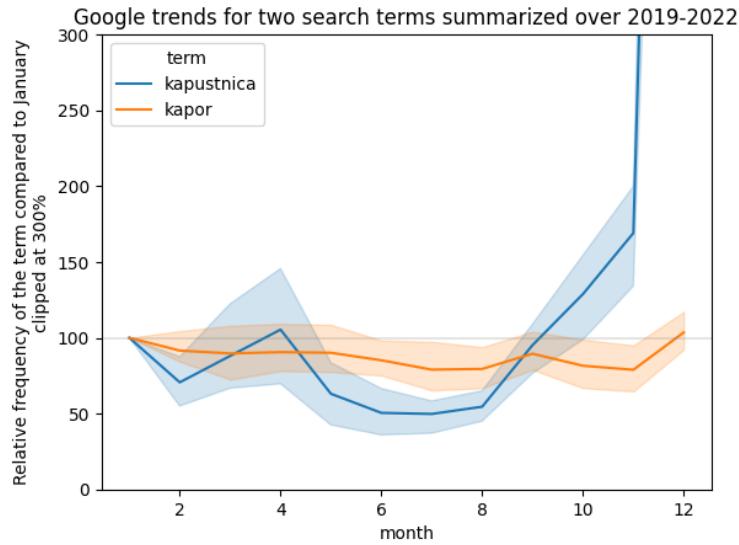
- When we care about rate of increase or decrease, it might be better to express values as a percentage compared to initial value.
- Here we compare values in each month with values in January of the same year.
- In this way even two time series with quite different values can be plotted in the same plot (e.g. revenue of a small and a large company and their relative changes within a year).

```
[39]: # compute relative values by transforming each group of monthly values
# by dividing them by the first value (January)
relValue = (trends1monthlyLong.groupby(['year', 'term'])['frequency']
            .transform(lambda x : x * 100 / x.iloc[0]))
# add relative values as a column to the long table
relTable = trends1monthlyLong.assign(relValue=relValue)
display(Markdown("'''Relative values added'''"))
relTable.head()
```

Relative values added

```
[39]:      week      term  frequency  month  year    relValue
 0 2019-01-31  kapustnica      2.50      1  2019     100.0
 1 2019-02-28  kapustnica      1.75      2  2019      70.0
 2 2019-03-31  kapustnica      1.60      3  2019      64.0
 3 2019-04-30  kapustnica      2.75      4  2019     110.0
 4 2019-05-31  kapustnica      2.00      5  2019      80.0
```

```
[40]: axes = sns.lineplot(relTable, x='month', y='relValue', hue='term')
axes.set_ylim(ymin=0, ymax=300)
axes.axhline(100, color="gray", alpha=0.2)
axes.set_title("Google trends for two search terms summarized over 2019-2022")
axes.set_ylabel("Relative frequency of the term compared to January\nclipped at\u2248300%")
pass
```



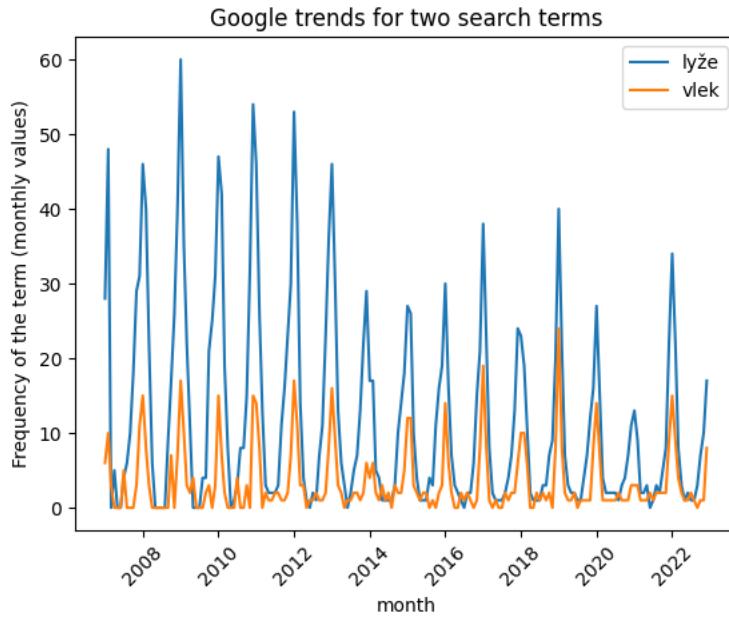
1.4.7 One more pair of Google trend lines

- Again very seasonal: lyže and vlek.
- This time we have monthly data over a longer period of time.
- We display the original data as well as yearly seasonal trend.
- The peak month is January for both queries, so we also display January values changing over the years.

```
[41]: url = "https://bbrejova.github.io/viz/data/lyze-vlek.csv"
trends2 = pd.read_csv(url, parse_dates=['month']).set_index('month')
display(trends2.head())
```

| month | lyže | vlek |
|------------|------|------|
| 2007-01-01 | 28 | 6 |
| 2007-02-01 | 48 | 10 |
| 2007-03-01 | 0 | 3 |
| 2007-04-01 | 5 | 0 |
| 2007-05-01 | 0 | 0 |

```
[42]: axes = sns.lineplot(trends2, dashes=False)
axes.set_title("Google trends for two search terms")
axes.set_ylabel("Frequency of the term (monthly values)")
# rotate tick labels
axes.tick_params(axis='x', labelrotation = 45)
pass
```

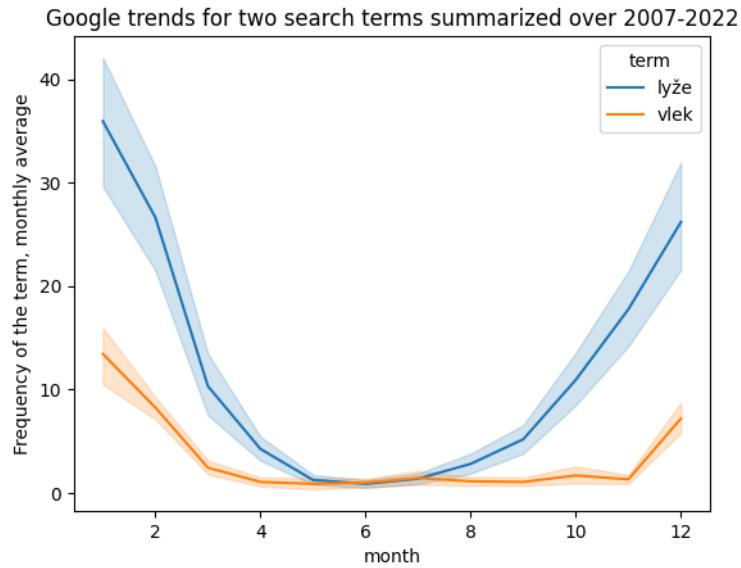


```
[43]: trends2long = trends2.reset_index().melt(id_vars=['month'])
trends2long.rename(columns={'month': 'date', 'variable': 'term', 'value':
    'frequency'}, inplace=True)
trends2long['month'] = trends2long['date'].dt.month
trends2long['year'] = trends2long['date'].dt.year
display(trends2long)
```

| | date | term | frequency | month | year |
|-----|------------|------|-----------|-------|------|
| 0 | 2007-01-01 | lyže | 28 | 1 | 2007 |
| 1 | 2007-02-01 | lyže | 48 | 2 | 2007 |
| 2 | 2007-03-01 | lyže | 0 | 3 | 2007 |
| 3 | 2007-04-01 | lyže | 5 | 4 | 2007 |
| 4 | 2007-05-01 | lyže | 0 | 5 | 2007 |
| .. | .. | .. | .. | .. | .. |
| 379 | 2022-08-01 | vlek | 1 | 8 | 2022 |
| 380 | 2022-09-01 | vlek | 0 | 9 | 2022 |
| 381 | 2022-10-01 | vlek | 1 | 10 | 2022 |
| 382 | 2022-11-01 | vlek | 1 | 11 | 2022 |
| 383 | 2022-12-01 | vlek | 8 | 12 | 2022 |

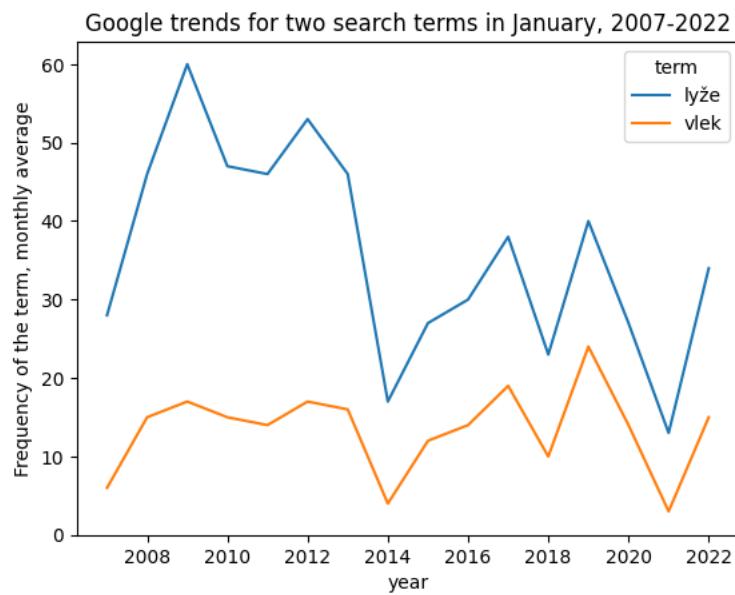
[384 rows x 5 columns]

```
[44]: axes = sns.lineplot(trends2long, x='month', y='frequency', hue='term')
axes.set_title("Google trends for two search terms summarized over 2007-2022")
axes.set_ylabel("Frequency of the term, monthly average")
pass
```



```
[45]: lyzeJan = trends2long.query("month==1")
axes = sns.lineplot(lyzeJan, x='year', y='frequency', hue='term')
axes.set_ylim(ymin=0)
axes.set_title("Google trends for two search terms in January, 2007-2022")
axes.set_ylabel("Frequency of the term, monthly average")

pass
```

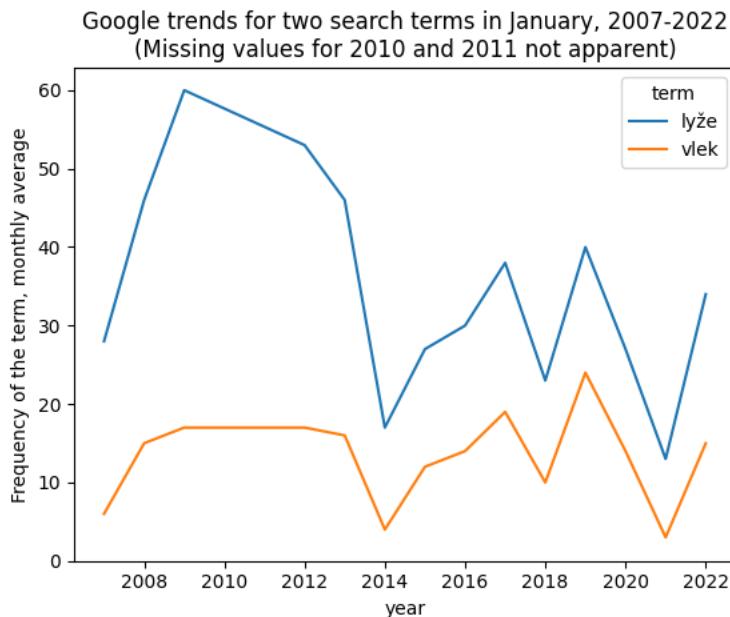


The drop in 2021 was due to pandemics, but what about 2014 and 2018?

1.4.8 Acknowledging missing values

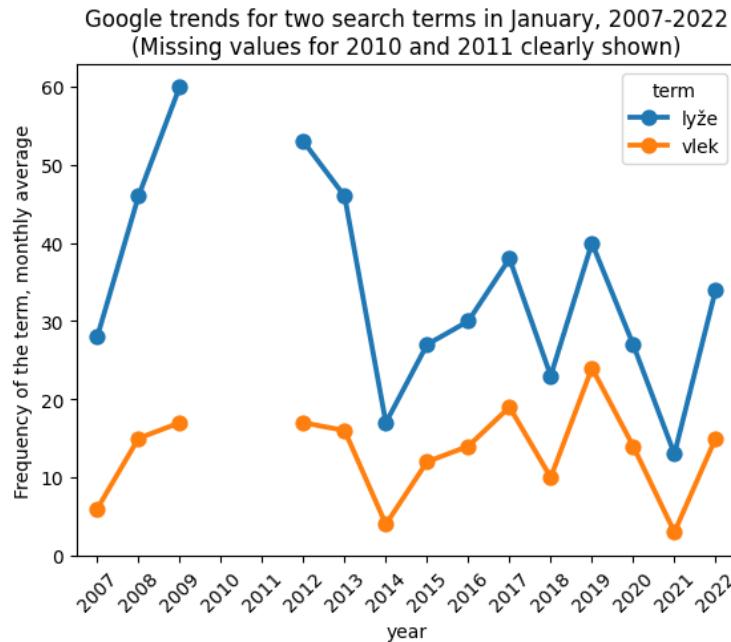
- Let us imagine that January values for 2010 and 2011 are missing.
- If we draw a `lineplot` in Seaborn, years 2009 and 2012 are connected by a straight line and viewer does not know that something is missing.
- This is not a good idea.
- Below we use `pointplot` which nicely shows the missing data and also locations of measured values.

```
[46]: # remove values for two years
to_remove = lyzeJan["year"].isin([2010,2011])
lyzeJanMissing = lyzeJan.copy(deep=True)
lyzeJanMissing.loc[to_remove, 'frequency'] = np.nan
axes = sns.lineplot(lyzeJanMissing, x='year', y='frequency', hue='term')
axes.set_ylim(ymin=0)
axes.set_title("Google trends for two search terms in January,\n ↴2007-2022\n(Missing values for 2010 and 2011 not apparent)")
axes.set_ylabel("Frequency of the term, monthly average")
pass
```



```
[47]: axes = sns.pointplot(lyzeJanMissing, x='year', y='frequency', hue='term')
axes.set_ylim(ymin=0)
axes.set_title("Google trends for two search terms in January,\n ↴2007-2022\n(Missing values for 2010 and 2011 clearly shown)")
axes.set_ylabel("Frequency of the term, monthly average")
```

```
axes.tick_params(axis='x', labelrotation = 45)
pass
```



1.4.9 Summary of time series

Typical goals are to observe and study:

- overall trend (increasing / decreasing / flat; rate of change),
- seasonality (daily / weekly / yearly cycles),
- noise (general variability / outliers)

Useful techniques:

- smoothing by aggregation and sliding window
- overlapping timescales
- relative scales
- showing uncertainty and missing values

1 Lecture 7: More statistics

Data Visualization · 1-DAV-105

Lecture by Broňa Brejová

1.1 Importing libraries and data

As usual, we start by importing libraries. We add `scipy.stats` library for working with probability distributions. One more library will be added at the end of the lecture.

```
[29]: import numpy as np
import pandas as pd
import matplotlib.pyplot as plt
import seaborn as sns
import plotly.express as px
from IPython.display import Markdown

import scipy.stats
```

In this lecture, we will use the World bank dataset from Lecture 03b (table `countries`) downloaded from WorldBank <https://databank.worldbank.org/home> under CC BY 4.0 license.

We will also work with an informal survey of preferences and opinions of young people done in 2013 among students of FSEV UK and their friends. Datatset was downloaded from <https://www.kaggle.com/miroslavsb/young-people-survey>. Columns correspond to survey questions, rows to respondents. The list of questions and meaning of responses is given in [this document](#).

```
[30]: url = 'https://bbrejova.github.io/viz/data/fsev-responses.csv'
fsev = pd.read_csv(url)
display(Markdown("## Size of fsev table:"), fsev.shape)
```

Size of fsev table:

(1010, 150)

```
[31]: url = 'https://bbrejova.github.io/viz/data/World_bank.csv'
countries = pd.read_csv(url).set_index('Country')
display(countries.describe())
```

| | Population2000 | Population2010 | Population2020 | Area | \ |
|-------|----------------|----------------|----------------|--------------|---|
| count | 2.170000e+02 | 2.170000e+02 | 2.170000e+02 | 2.160000e+02 | |
| mean | 2.821267e+07 | 3.201312e+07 | 3.592913e+07 | 6.235930e+05 | |
| std | 1.157060e+08 | 1.282292e+08 | 1.398323e+08 | 1.828856e+06 | |
| min | 9.638000e+03 | 1.024100e+04 | 1.106900e+04 | 1.000000e+01 | |
| 25% | 6.049510e+05 | 7.055170e+05 | 7.972020e+05 | 1.122250e+04 | |
| 50% | 5.056174e+06 | 5.768613e+06 | 6.579900e+06 | 1.017050e+05 | |
| 75% | 1.639406e+07 | 2.112004e+07 | 2.564925e+07 | 4.786050e+05 | |
| max | 1.262645e+09 | 1.337705e+09 | 1.411100e+09 | 1.709825e+07 | |

| | GDP2000 | GDP2010 | GDP2020 | Expectancy2000 | \ |
|-------|--------------|---------------|---------------|----------------|---|
| count | 199.000000 | 209.000000 | 210.000000 | 211.000000 | |
| mean | 8292.850729 | 16135.528397 | 17547.135072 | 67.358588 | |
| std | 13036.320032 | 24118.156125 | 26171.548454 | 9.795515 | |
| min | 122.961660 | 222.660583 | 216.827417 | 44.518000 | |
| 25% | 654.638840 | 1706.414917 | 2262.246896 | 61.362000 | |
| 50% | 1996.515578 | 5735.422857 | 6370.903532 | 70.417073 | |
| 75% | 10721.262761 | 21447.858255 | 22805.261142 | 74.505000 | |
| max | 81763.827669 | 161780.745361 | 182537.387370 | 81.370000 | |

| | Expectancy2010 | Expectancy2020 | Fertility2000 | Fertility2010 | \ |
|-------|----------------|----------------|---------------|---------------|---|
| count | 210.000000 | 209.000000 | 211.000000 | 211.000000 | |
| mean | 70.580052 | 72.309699 | 3.211021 | 2.890908 | |
| std | 8.831970 | 7.482700 | 1.716951 | 1.490287 | |
| min | 45.596000 | 52.777000 | 0.912000 | 1.042000 | |
| 25% | 64.480750 | 66.797000 | 1.840000 | 1.765000 | |
| 50% | 72.810500 | 72.889000 | 2.660000 | 2.340000 | |
| 75% | 77.578598 | 78.041000 | 4.395000 | 3.827000 | |
| max | 83.109000 | 85.497561 | 7.732000 | 7.485000 | |

| | Fertility2020 |
|-------|---------------|
| count | 211.000000 |
| mean | 2.525145 |
| std | 1.273400 |
| min | 0.837000 |
| 25% | 1.557500 |
| 50% | 2.040000 |
| 75% | 3.257000 |
| max | 6.892000 |

```
[32]: display(Markdown("**Values of life expectancy in 2020 in individual countries:  
↳**"))  
display(countries['Expectancy2020'].dropna())
```

Values of life expectancy in 2020 in individual countries:

| Country | |
|---------------------|-----------|
| Afghanistan | 62.575000 |
| Albania | 76.989000 |
| Algeria | 74.453000 |
| Angola | 62.261000 |
| Antigua and Barbuda | 78.841000 |
| | ... |
| Virgin Islands | 79.819512 |
| West Bank and Gaza | 74.403000 |
| Yemen | 64.650000 |
| Zambia | 62.380000 |
| Zimbabwe | 61.124000 |

```
Name: Expectancy2020, Length: 209, dtype: float64
```

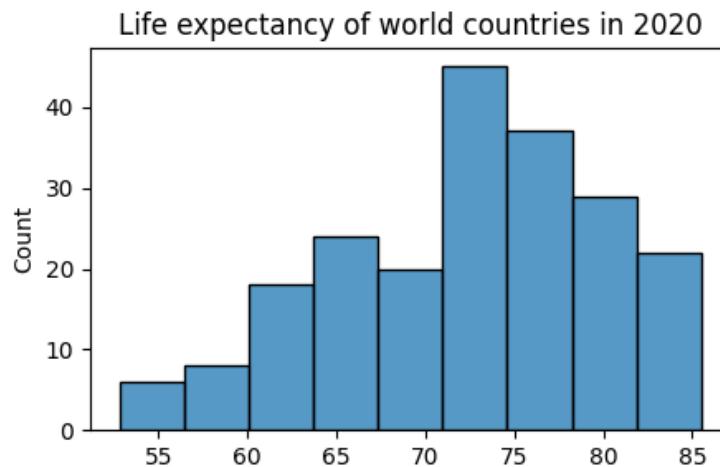
1.2 Histograms

Histograms are well known, and we have seen them in Lecture 03. We split the range of a variable into equally sized bins, count the number of data points in each bin and plot the counts as a bar graph.

Histograms allow us to observe many aspects of distribution of values of a variable:

- range of values, outliers
- central tendency
- unimodality / multimodality
- variance
- symmetry / skewness (šíkmost)

```
[33]: axes = sns.histplot(data=countries, x='Expectancy2020')
axes.set_title('Life expectancy of world countries in 2020')
axes.set_xlabel(None)
axes.figure.set_size_inches(5, 3)
pass
```



1.2.1 Custom bins

- Seaborn library makes bins by splitting the range into equally sized intervals, but perhaps a more meaningful plot uses round values at bin boundaries, e.g. intervals of 5 years 50-55, 55-60, 60-65,...
- We can use manually created bin boundaries in Seaborn.
- Plotly library tries to create more meaningful bins by default.

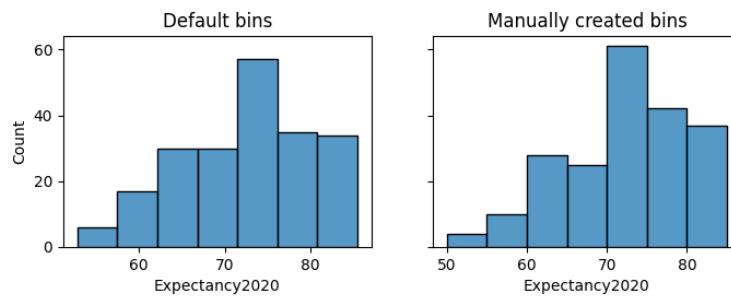
```
[34]: # create a figure with two plots
figure, axes = plt.subplots(1, 2, figsize=(8,2.5), sharey=True)
```

```

# the first plot has histogram with default bins of width 5
sns.histplot(data=countries, x='Expectancy2020', binwidth=5, ax=axes[0])
axes[0].set_title('Default bins')

# the second plot has manually set bin boundaries 50,55,60,...,85
sns.histplot(data=countries, x='Expectancy2020',
             bins=range(50, 90, 5), ax=axes[1])
axes[1].set_title('Manually created bins')
pass

```

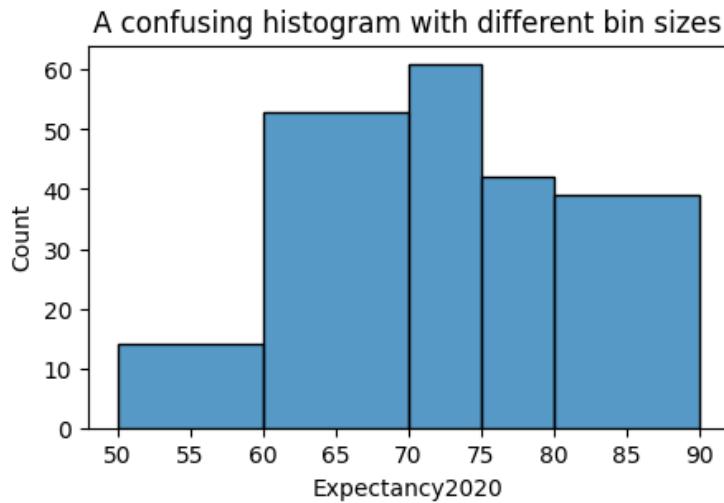


```
[35]: # in Plotly, we specify the maximum number of bins,
# library may choose a lower number to get "nice" bin boundaries
fig = px.histogram(countries, x="Expectancy2020",
                    nbins=8, width=500, height=350)
fig.show()
```

1.2.2 Use equally-sized bins

- Manually created bin boundaries can be arbitrary, but if bin width is unequal, the resulting plot is confusing.
- If you really need special bins (e.g. age <18 years, 18-65 years, >65 years), make a categorical variable, then plot it as a bar graph (typically displayed as bars with equal width, spaces between bars), clearly mark the meaning of each bar.

```
[36]: axes = sns.histplot(data=countries, x='Expectancy2020',
                      bins=[50, 60, 70, 75, 80, 90])
axes.set_title('A confusing histogram with different bin sizes')
axes.figure.set_size_inches(5, 3)
pass
```



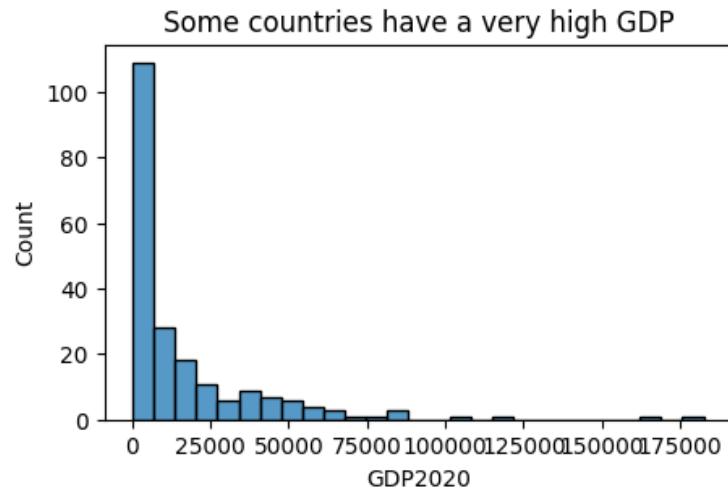
1.2.3 Removing outliers

- Histograms are great for spotting outliers.
- But extreme values reduce the space given to more regular values, so perhaps we want to remove them in subsequent analysis.

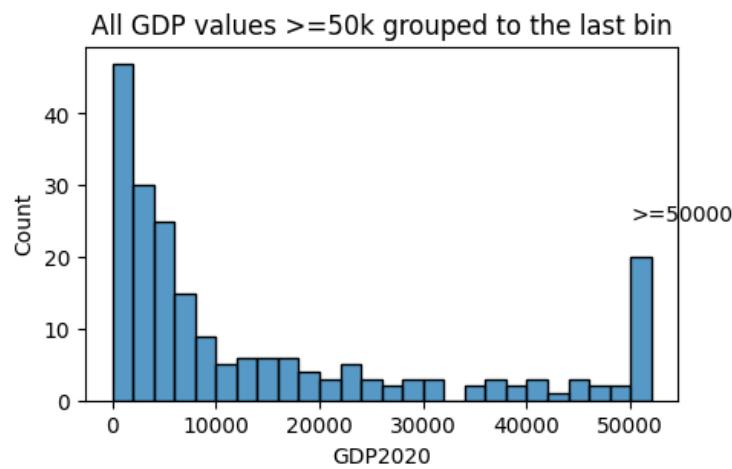
We have several options:

- Remove them from the dataset if we believe them to be errors.
- Or remove them from the plot only, e.g. by `set_xlim` or by using custom bins with a smaller range.
- Or clip values: replace values above some threshold with the threshold value (function `clip` in Pandas). Thus they will be present in the last bin. This bin should be then clearly marked.

```
[37]: axes = sns.histplot(data=countries, x='GDP2020')
axes.set_title('Some countries have a very high GDP')
axes.figure.set_size_inches(5, 3)
pass
```



```
[38]: # replace values larger than 51k with 51k
gdp_clipped = countries['GDP2020'].clip(0, 51000)
# make histogram with manual bins, with last bin 50k-52k
axes = sns.histplot(x=gdp_clipped, bins=np.arange(0, 53000, 2000))
axes.figure.set_size_inches(5, 3)
# mention clipping in plot title
axes.set_title('All GDP values >=50k grouped to the last bin')
# also add a text label to the bin with clipped values
axes.text(x=50000, y=25, s='>=50000')
pass
```



1.2.4 Problems with precision

When working with integers or even real numbers given with a small number of decimal points, we can get artifacts related to different number of possible values falling to different bins.

To illustrate this, we uniformly sample million points from the set $\{0, 0.01, 0.02, \dots, 0.99\}$.

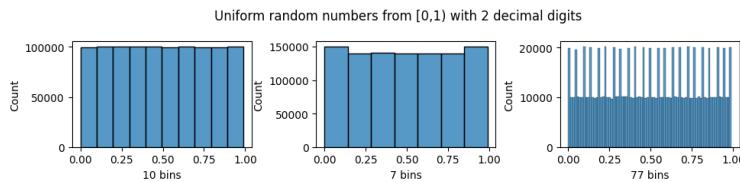
- There will be a similar number of samples for each possible value from this set.
- We show histograms with 10, 7 and 77 equally sized bins.
- For 10 bins, each bin summarizes 10 of the possible values and the sizes are approximately the same.
- For 7 bins, the first and the last bin summarize 15 possible values each and remaining bins summarize 14 possible values each. The first and last bin are thus slightly higher.
- For 77 bins, some bins summarize 2 different values, others only 1. We see clear differences in bar height.

If we are unaware of this, we may draw incorrect conclusions from the second and third plot.

```
[39]: sample_uniform = np.random.randint(0, 100, 1000000) / 100
display(Markdown('**Example of data (first values):**'), sample_uniform[0:5])
figure, axes = plt.subplots(1, 3, figsize=(10,2.5))
figure.tight_layout(pad=3)
for (i, bin) in enumerate([10, 7, 77]):
    sns.histplot(x=sample_uniform, bins=bin, ax=axes[i])
    axes[i].set_xlabel(f"{bin} bins")
figure.suptitle("Uniform random numbers from [0,1) with 2 decimal digits")
pass
```

Example of data (first values):

```
array([0.44, 0.65, 0.72, 0.14, 0.46])
```



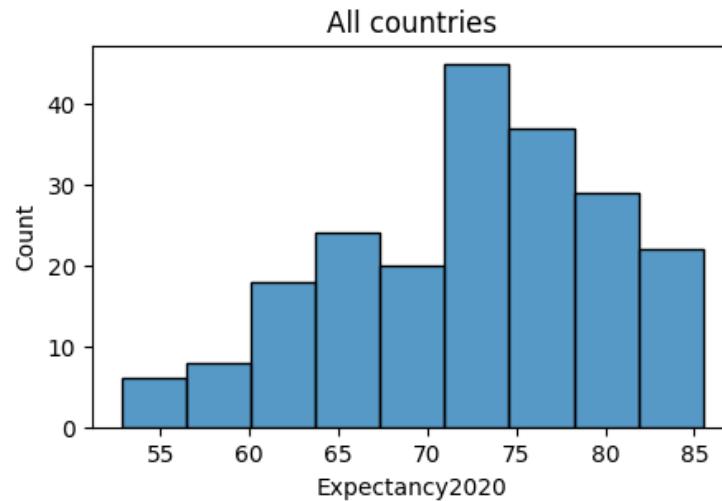
1.2.5 Small samples

Beware drawing strong conclusions from small samples.

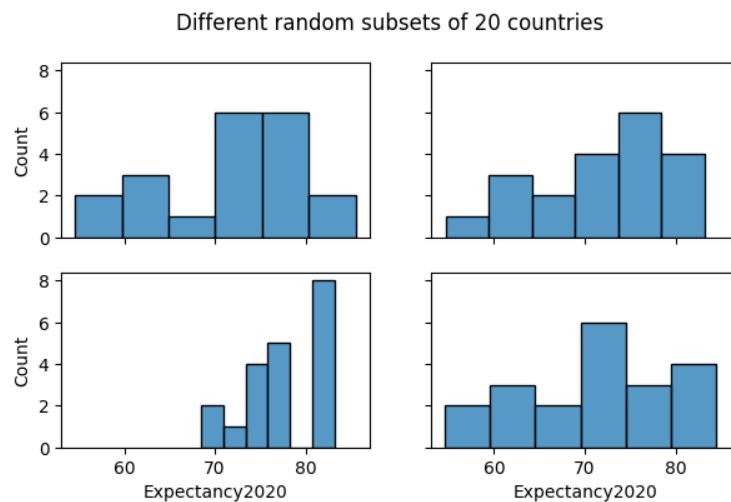
- Below we again first show the histogram of life expectancy over all countries.
- Then we show histograms of four random subsets of 20 countries each.
- Any estimates (including histograms) from small samples are subject to random noise.

```
[40]: axes = sns.histplot(data=countries, x='Expectancy2020')
axes.set_title('All countries')
axes.figure.set_size_inches(5, 3)
```

```
pass
```



```
[41]: figure, axes = plt.subplots(2, 2, sharex=True, sharey=True, figsize=(7,4))
for row in axes:
    for subplot in row:
        expectancy_sample = countries['Expectancy2020'].dropna().sample(20)
        sns.histplot(x=expectancy_sample, ax=subplot)
figure.suptitle("Different random subsets of 20 countries")
pass
```



1.2.6 Summary: Histogram bin size

To summarize, the tricky part of using histograms is to choose the bin size or the number of bins.

Smaller bins mean more details are visible, but some of those details may be artefacts:

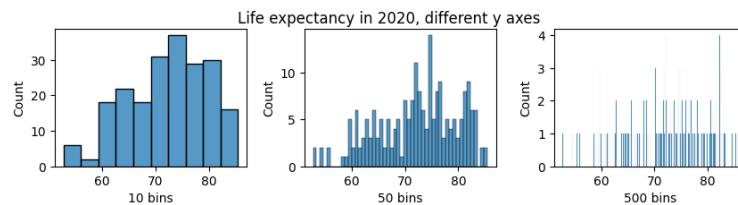
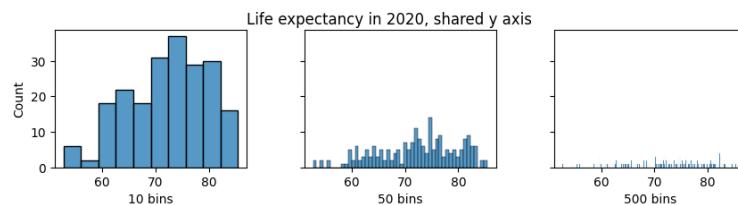
- random fluctuations due to small number of points in the bin, or
- effects related to insufficient resolution of the data.

Thus choose bin size based on:

- the amount of data,
- the precision of input values,
- the meaningful resolution of the results.

In the example below we show the life expectancy data with different number of bins. Do 50 or 500 bins show more meaningful information than 10 bins?

```
[42]: # one set of plots has share y axis, one has not
figure1, axes1 = plt.subplots(1, 3, figsize=(10,2), sharey=True)
figure2, axes2 = plt.subplots(1, 3, figsize=(10,2))
# plot the same plots for each set
for (figure, axes, title) in [(figure1, axes1, 'shared y axis'),
                               (figure2, axes2, 'different y axes')]:
    # iterate over different numbers of bins
    for (i, bin) in enumerate([10, 50, 500]):
        sns.histplot(data=countries, x='Expectancy2020', bins=bin, ax=axes[i])
        axes[i].set_xlabel(f"{bin} bins")
    # title of the whole figure
    figure.suptitle(f"Life expectancy in 2020, {title}")
    figure.subplots_adjust(wspace=0.3)
pass
```



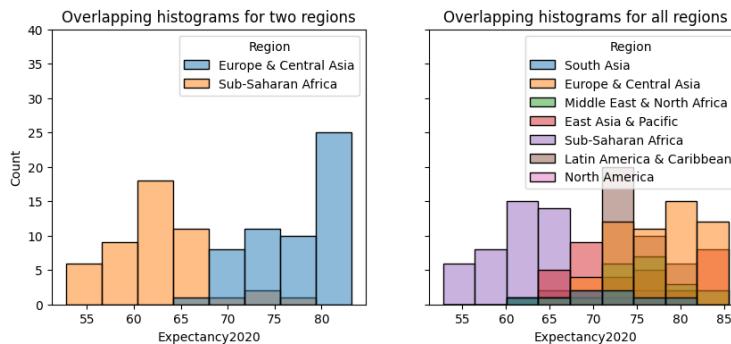
1.2.7 Comparing distributions with histograms

- We can compare distributions of a numerical variable split into groups by a categorical variable.
- For example in our `countries` table, we can compare life expectancy in different regions of the world.
- Seaborn provides [several options](#) for doing so.

The first two plots use semi-transparent overlapping histograms, which work well for two regions (left), but are a mess for many regions (right).

```
[43]: # select two regions
countries_subset = countries.query('Region == "Europe & Central Asia" '
+ 'or Region == "Sub-Saharan Africa"')

# create figure with 2 plots
figures, axes = plt.subplots(1, 2, figsize=(10,4), sharey=True)
# plot both histograms
sns.histplot(data=countries_subset, x='Expectancy2020', hue='Region', ax=axes[0])
sns.histplot(data=countries, x='Expectancy2020', hue='Region', ax=axes[1])
# make bigger y-axis to accomodate legend
axes[0].set_ylim(0,40)
# titles
axes[0].set_title('Overlapping histograms for two regions')
axes[1].set_title('Overlapping histograms for all regions')
pass
```



The next two plots attempt to improve the situation.

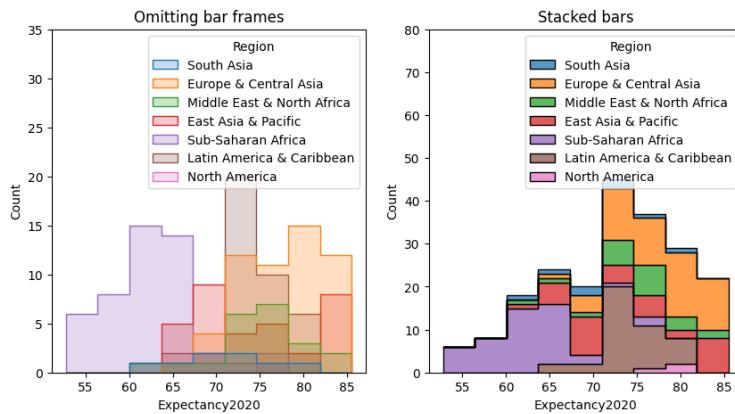
- On the left we omit bar outlines to simplify the plot.
- On the right we use stacked bars, showing contribution of each region to the whole.

```
[44]: # create figure with 2 plots
figures, axes = plt.subplots(1, 2, figsize=(10, 5))
# plot both histograms
sns.histplot(data=countries, x='Expectancy2020', hue='Region',
```

```

        element='step', ax = axes[0])
sns.histplot(data=countries, x='Expectancy2020', hue='Region', element='step',
             multiple="stack", ax=axes[1])
# make bigger y-axis to accomodate legend
axes[0].set_ylim(0,35)
axes[1].set_ylim(0,80)
# titles
axes[0].set_title('Omitting bar frames')
axes[1].set_title('Stacked bars')
pass

```



- Regions contain different number of countries.
- To better compare distribution of the expectancy within region, we should normalize the count to probabilities.
- Use `common_norm=False` to normalize each region separately.

```
[45]: display(Markdown("**Countries in regions:**"))
display(countries.groupby('Region').size().sort_values())

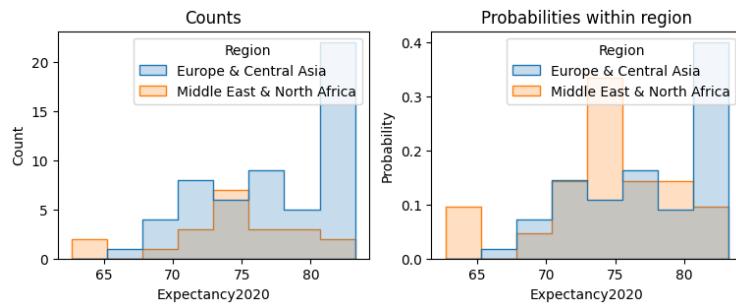
# select two regions of very different sizes
countries_subset2 = countries.query('Region == "Europe & Central Asia" '
+ 'or Region == "Middle East & North Africa"')

# plot counts and probabilities
figure, axes = plt.subplots(1, 2, figsize=(9,3))
sns.histplot(data=countries_subset2, x='Expectancy2020', hue='Region', element='step', ax=axes[0])
sns.histplot(data=countries_subset2, x='Expectancy2020', hue='Region', element='step',
             stat="probability", common_norm=False, ax=axes[1])
axes[0].set_title('Counts')
axes[1].set_title('Probabilities within region')
```

```
pass
```

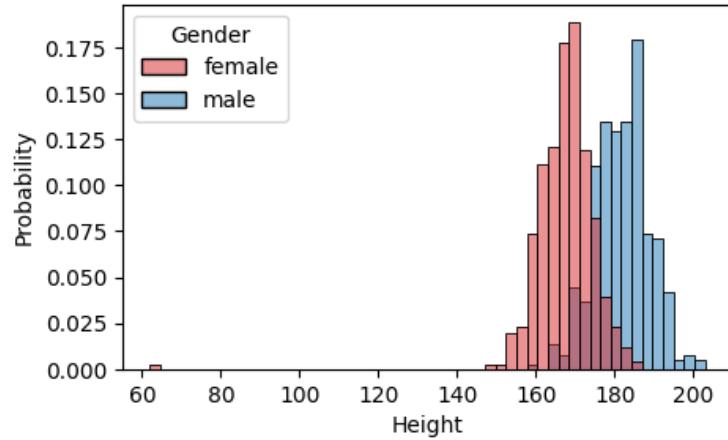
Countries in regions:

```
Region
North America           3
South Asia              8
Middle East & North Africa 21
East Asia & Pacific      37
Latin America & Caribbean 42
Sub-Saharan Africa       48
Europe & Central Asia     58
dtype: int64
```



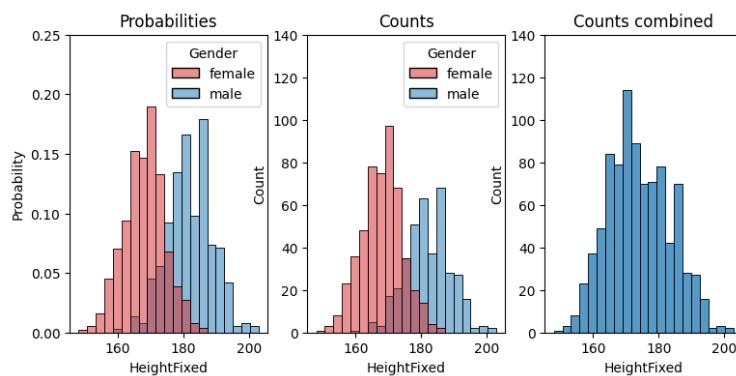
- Using FSEV survey, we can compare self-reported heights of women and men.
- We will use only values of adults above 18 years of age.
- Besides the expected trend, we also see a clear outlier, perhaps an error (although people of such heights exist, the cases are extremely rare).
- We will replace it with NaN.

```
[46]: fsev.iloc[:,144].value_counts()
adults = fsev.query("Age >= 18").copy(deep=True)
axes = sns.histplot(data=adults, x='Height', hue='Gender',
                     hue_order=['female', 'male'], palette=['C3', 'CO'],
                     stat="probability", common_norm=False)
axes.figure.set_size_inches(5, 3)
pass
```



Below we see histograms after removal of the extreme value.

```
[47]: # replace all values lower than 100cm by NaN, in a new column HeightFixed
adults['HeightFixed']=adults['Height'].mask(adults['Height']<100, np.nan)
figure, axes = plt.subplots(1, 3, figsize=(9,4))
sns.histplot(data = adults, x='HeightFixed', hue='Gender',
              hue_order=['female', 'male'], palette=['C3', 'C0'],
              stat="probability", common_norm=False, ax=axes[0])
sns.histplot(data = adults, x='HeightFixed', hue='Gender',
              hue_order=['female', 'male'], palette=['C3', 'C0'],
              ax=axes[1])
sns.histplot(data = adults, x='HeightFixed', ax=axes[2])
axes[0].set_ylim(0,0.25)
axes[1].set_ylim(0,140)
axes[2].set_ylim(0,140)
axes[0].set_title('Probabilities')
axes[1].set_title('Counts')
axes[2].set_title('Counts combined')
pass
```



1.3 Probability distributions

- For a continuous variable, we can imagine having infinitely many data points and making histogram with infinitely small bins, keeping the area under the histogram equal to one.
- Thus we obtain **probability density function** (PDF) (hustota rozdelenia pravdepodobnosti).
- We often assume that our data are a small sample from one of the well-characterized probability distributions (rozdelenie pravdepodobnosti).

1.3.1 Normal (Gaussian) distribution

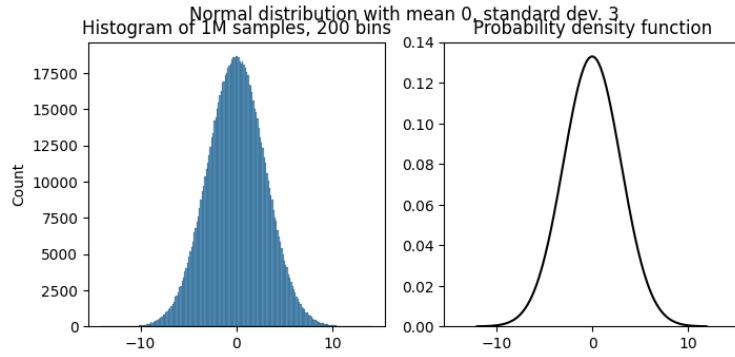
- The normal (or Gaussian) distribution has two parameters: mean μ and standard deviation σ .
- Its density is $f(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-\frac{1}{2}(\frac{x-\mu}{\sigma})^2}$.
- This is the well-known bell shape.
- Below we plot both histogram of a million samples from this distribution and the density given by the function above.
- These two plots are very similar.

```
[48]: figure, axes = plt.subplots(1, 2, sharex=True, figsize=(8, 3.5))

# sample million points from the normal distrib. with mean 0 and std. dev. 3
sample_normal = np.random.normal(0, 3, 1000000)
# create histogram of the sampled points
sns.histplot(x=sample_normal, bins=200, ax=axes[0])
axes[0].set_title('Histogram of 1M samples, 200 bins')

# create an object representing normal distrib. with mean 0 and std. dev. 3
normal = scipy.stats.norm(0, 3)
# create equally-spaced points
x = np.arange(-12, 12, 0.1)
# compute values of pdf in these points
y = normal.pdf(x)
# plot the function
axes[1].plot(x, y, 'k-')
axes[1].set_title('Probability density function')
axes[1].set_ylim(0, 0.14)

figure.suptitle("Normal distribution with mean 0, standard dev. 3")
pass
```



- Normal distribution often arises in situations where a variable is a result of many small influences.
- One example is the height of a person within one gender and population.
- Below we fit the normal distribution to the histogram of the adult male heights from the FSEV survey.

```
[49]: # select male height, drop missing values
male_heights = adults.query("Gender=='male'")['Height'].dropna()
# compute the characteristics (means, stdev)
display(Markdown(""),
        male_heights.mean(),
        Markdown(""),
        male_heights.std())

# compute the best fit
parameters = scipy.stats.norm.fit(male_heights)
display(Markdown(""), parameters)

# get function values for regularly distributed x values
x = np.arange(150, 200, 1)
pdf_fitted = scipy.stats.norm.pdf(x, loc=parameters[0], scale=parameters[1])

# plot histogram, normalized as density (area=1)
figure, axes = plt.subplots(figsize=(5,3))
sns.histplot(x=male_heights, stat='density', ax=axes)
# add a line for fitted density
axes.plot(x, pdf_fitted, 'k-')
axes.set_title('Male heights with normal distribution fit')
pass
```

Mean male height:

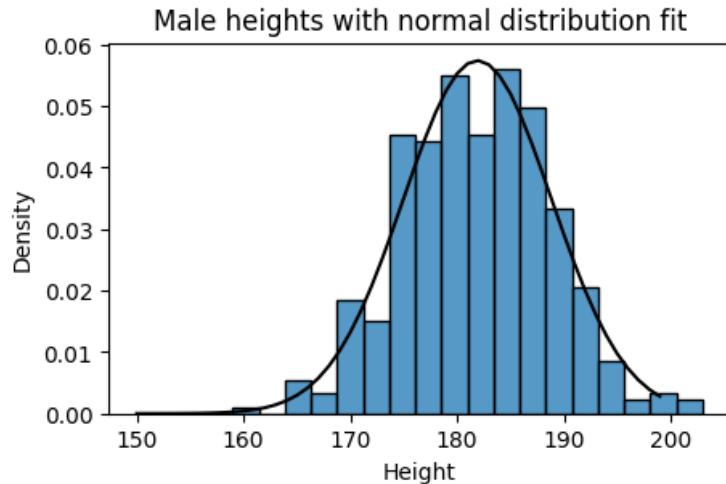
181.91820580474933

Std. dev. male height:

6.957251247475206

Best fit:

(181.91820580474933, 6.948066753375318)



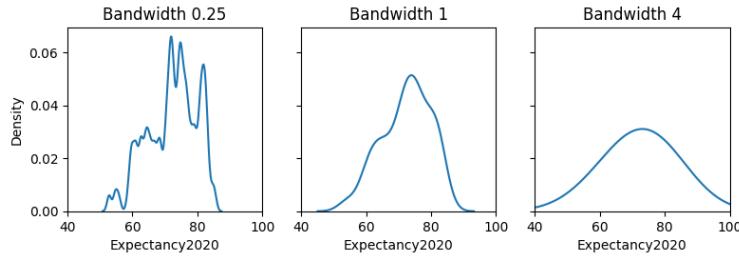
1.4 Kernel Density Estimation (KDE)

- KDE creates a smoothed version of a histogram.
- We choose a kernel function. e.g. the normal distribution.
- For each point in the dataset, the method creates a “kernel” centered at that point.
- It then adds up the heights of all kernel copies.
- The amount of smoothing is controlled by the bandwidth parameter (standard deviation for the normal distribution).
- More information is in the [scikit-learn documentation](#).

https://commons.wikimedia.org/wiki/File:Comparison_of_1D_histogram_and_KDE.png Drleft at English Wikipedia, CC BY-SA 3.0

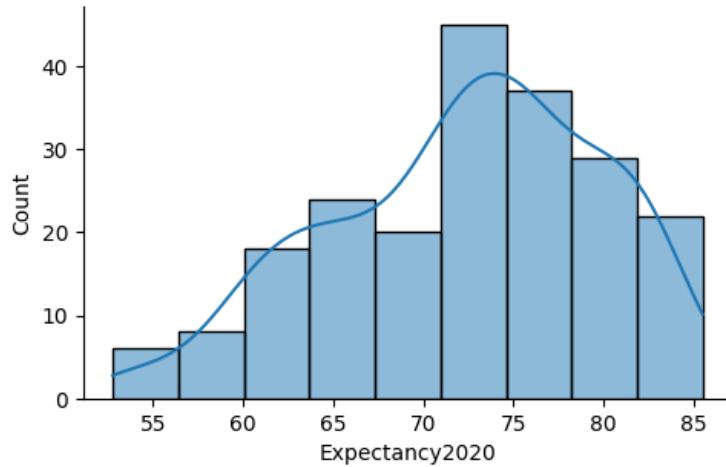
- KDE can be conveniently computed directly in Seaborn’s [displot/kdeplot function](#).
- The bandwidth is adjusted by `bw_adjust`, with default 1.
- A small bandwidth leads to a bumpy plot not representing real trends.
- A large bandwidth can obscure real trends.

```
[50]: figure, axes = plt.subplots(1, 3, sharex=True, sharey=True, figsize=(9,2.5))
for axes, bandwidth in [(axes[0], 0.25), (axes[1], 1), (axes[2], 4)]:
    sns.kdeplot(x=countries["Expectancy2020"], ax=axes, bw_adjust=bandwidth)
    axes.set_title(f'Bandwidth {bandwidth}')
    axes.set_xlim(40,100)
pass
```



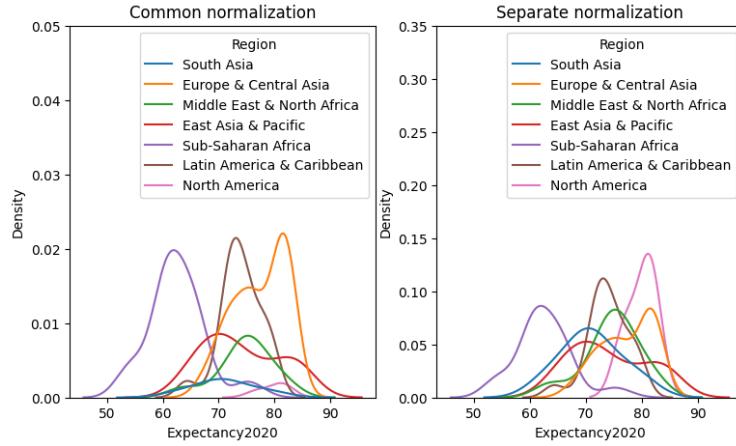
We can display combined histogram and KDE.

```
[51]: axes = sns.displot(countries, x="Expectancy2020", kde=True)
axes.figure.set_size_inches(5, 3)
pass
```



KDE plots can be also better for comparing multiple distributions, as their smooth curves are easier to follow than histograms.

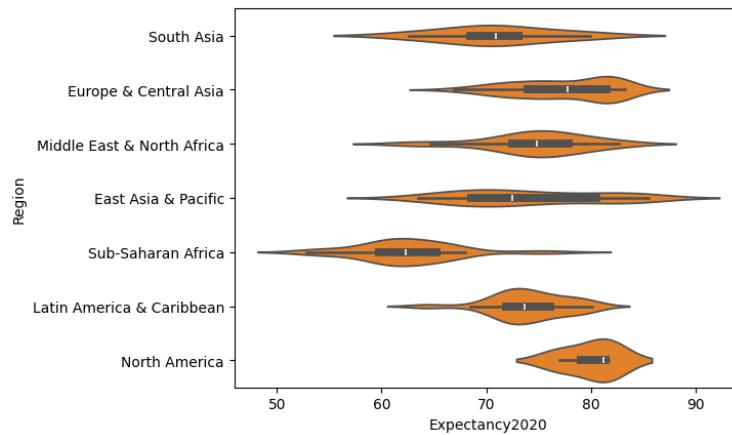
```
[52]: figure, axes = plt.subplots(1, 2, sharex=True, figsize=(9,5))
sns.kdeplot(x=countries["Expectancy2020"], hue=countries["Region"], ax=axes[0])
axes[0].set_ylim(0, 0.05)
axes[0].set_title('Common normalization')
sns.kdeplot(x=countries["Expectancy2020"], hue=countries["Region"],
            common_norm=False, ax=axes[1])
axes[1].set_title('Separate normalization')
axes[1].set_ylim(0, 0.35)
pass
```



1.5 Violin plots

- **Violin plots** are often used instead of boxplots to compare distributions for different values of a categorical variable.
- Each violin consist of two symmetric KDE plots.
- They can be accompanied by a boxplot or strip plot.
- More variants can be found in the [Seaborn tutorial](#).

```
[53]: sns.violinplot(data=countries, y="Region", x="Expectancy2020", color="C1")
      pass
```



1.6 Cumulative distribution function

For a probability density function $f(x)$:

- Its cumulative distribution function (CDF) (distribučná funkcia) is the area under the curve from left up to point x .

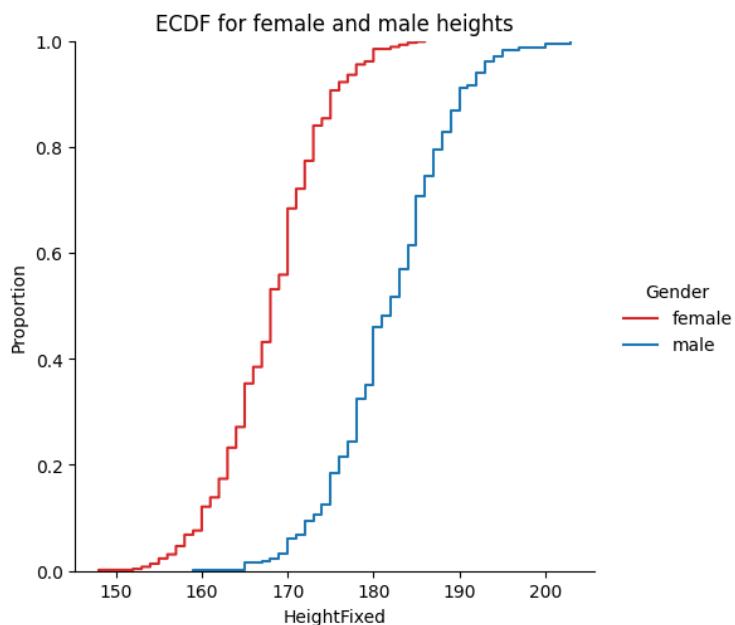
- $F(x) = \int_{-\infty}^x f(t) dt$.
- CDF is non-decreasing.
- $\lim_{x \rightarrow -\infty} F(x) = 0$ and $\lim_{x \rightarrow \infty} F(x) = 1$.
- $F(x)$ is the probability that the random point from the distribution is $\leq x$.

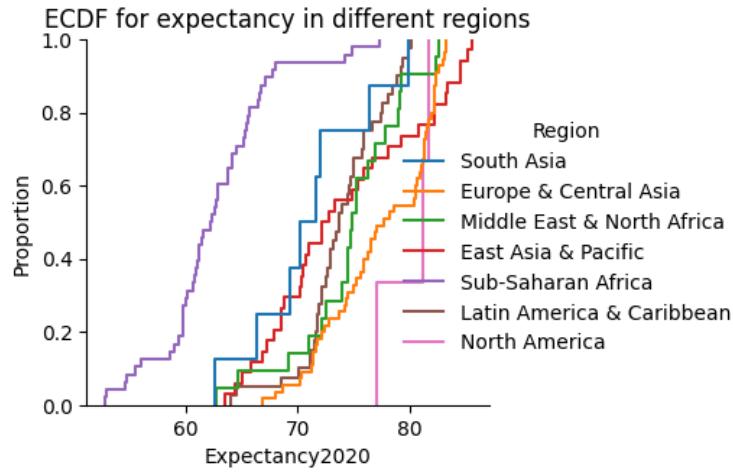
https://commons.wikimedia.org/wiki/File:Normal_Distribution_CDF.svg Inductiveload, Public domain

1.6.1 Empirical cumulative distribution function (ECDF)

- This is a similar concept for a finite sample.
- For each x , $F(x)$ is the fraction of the sample which is $\leq x$.
- This gives us a step-wise function which can be visualized.
- Unlike histograms and KDE, no parameters need to be set (bins, bandwidth).
- Allows comparison of multiple distributions and their quantiles (how?).
- But harder to interpret than histogram in terms of shape.

```
[54]: grid = sns.displot(adults, x="HeightFixed", hue="Gender", kind="ecdf",
                      hue_order=['female', 'male'], palette=['C3', 'C0'])
grid.axes[0,0].set_title('ECDF for female and male heights')
grid = sns.displot(countries, x="Expectancy2020", hue="Region", kind="ecdf")
grid.axes[0,0].set_title('ECDF for expectancy in different regions')
grid.figure.set_size_inches(5, 3)
pass
```

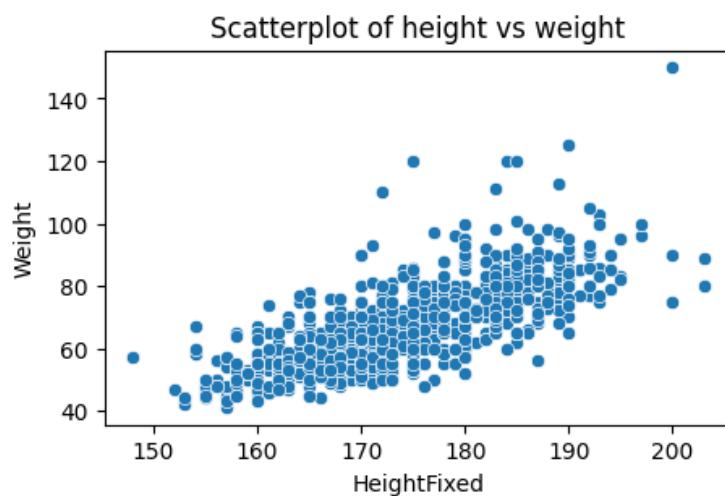




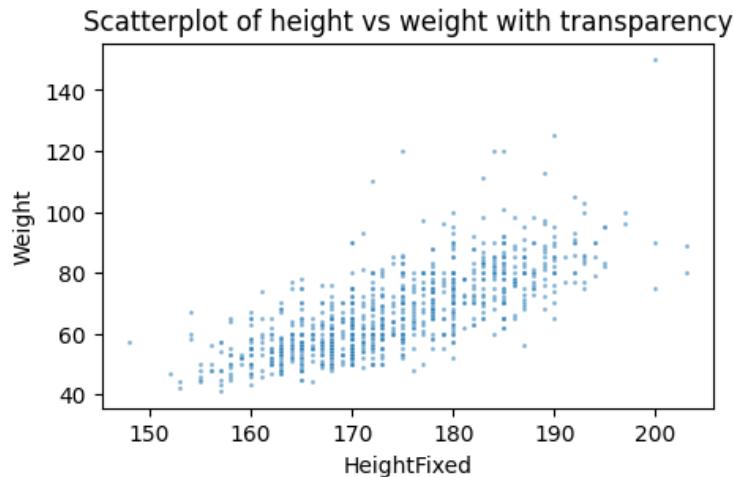
1.7 Two-dimensional histograms / KDE

- Instead of scatterplots, we can compute 2D histograms or smooth them by KDE.
- This works well if we have many overlapping points.
- Below we show several variants for the plot height vs. weight of adults in the FSEV survey (with the height outlier removed).
- In scatterplot there is a cloud of overlapping points and it is not clear which parts of it are denser. This can be somewhat improved with smaller points and transparency.

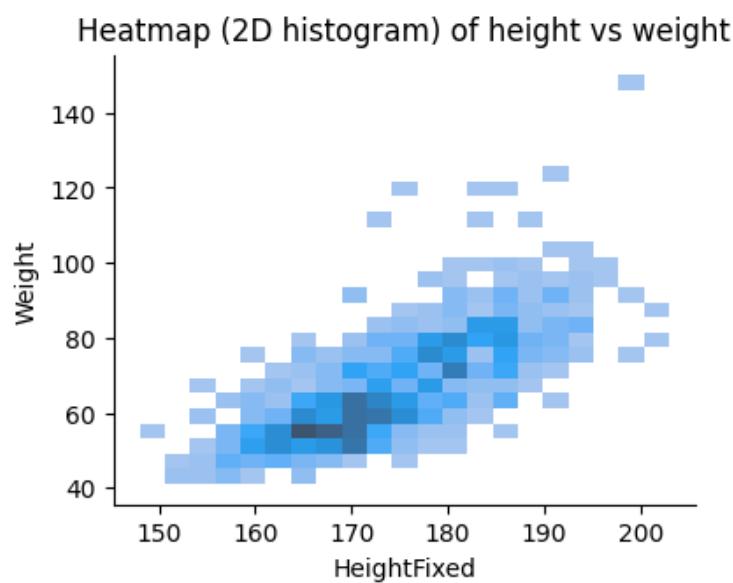
```
[55]: axes = sns.scatterplot(data=adults, x='HeightFixed', y='Weight')
axes.figure.set_size_inches(5, 3)
axes.set_title('Scatterplot of height vs weight')
pass
```



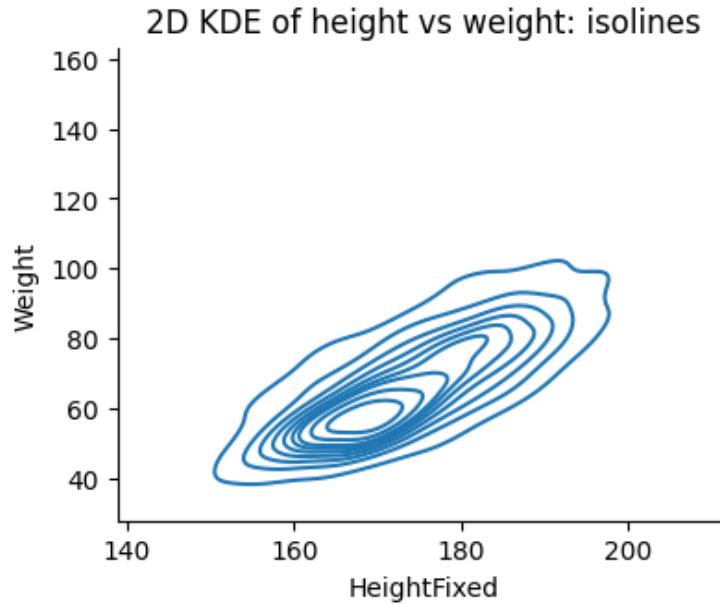
```
[56]: # plot with smaller points (s=4) and transparency (alpha=0.6)
axes = sns.scatterplot(data=adults, x='HeightFixed', y='Weight', s=4, alpha=0.6)
axes.figure.set_size_inches(5, 3)
axes.set_title('Scatterplot of height vs weight with transparency')
pass
```



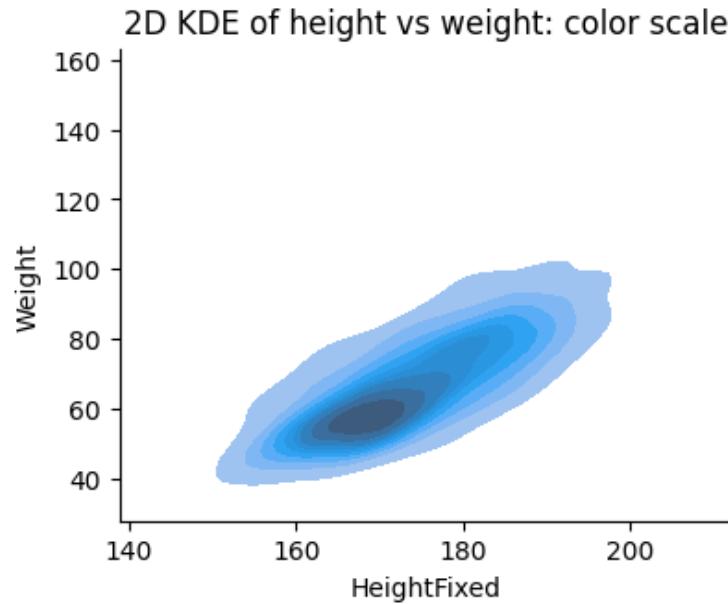
```
[57]: grid = sns.displot(data=adults, x='HeightFixed', y='Weight')
grid.figure.set_size_inches(4, 3)
grid.ax.set_title('Heatmap (2D histogram) of height vs weight')
pass
```



```
[58]: grid = sns.displot(data=adults, x='HeightFixed', y='Weight', kind="kde")
grid.figure.set_size_inches(4, 3)
grid.ax.set_title('2D KDE of height vs weight: isolines')
pass
```



```
[59]: grid = sns.displot(data=adults, x='HeightFixed', y='Weight', kind="kde", fill=True)
grid.figure.set_size_inches(4, 3)
grid.ax.set_title('2D KDE of height vs weight: color scale')
pass
```



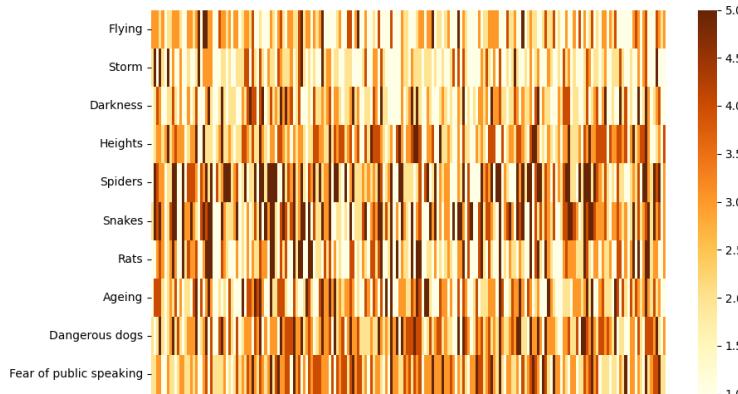
1.8 Clustering multi-dimensional data

- The FSEV survey contains questions about phobias and fears, each with answers 1-5 (5 means highest fear).
- We will first randomly select 200 participants without missing values.
- We will display them as a heatmap.

```
[60]: # columns 63-72 are fears, drop rows with missing values, sample 200 people
fsev_sample = fsev.iloc[:, 63:73].dropna().sample(200)
# show sample of the data
display(fsev_sample.head())
```

| | Flying | Storm | Darkness | Heights | Spiders | Snakes | Rats | Ageing | \ |
|-----|----------------|-------------------------|----------|---------|---------|--------|------|--------|---|
| 995 | 3.0 | 2.0 | 1.0 | 1.0 | 1.0 | 2 | 1.0 | 1.0 | |
| 27 | 3.0 | 5.0 | 2.0 | 2.0 | 5.0 | 5 | 1.0 | 4.0 | |
| 978 | 3.0 | 1.0 | 4.0 | 3.0 | 4.0 | 4 | 3.0 | 4.0 | |
| 568 | 2.0 | 5.0 | 3.0 | 3.0 | 3.0 | 5 | 4.0 | 4.0 | |
| 206 | 3.0 | 2.0 | 1.0 | 2.0 | 3.0 | 3 | 3.0 | 2.0 | |
| | | | | | | | | | |
| | Dangerous dogs | Fear of public speaking | | | | | | | |
| 995 | | 2.0 | | | | | | | |
| 27 | | 1.0 | | | | | | | |
| 978 | | 2.0 | | | | | | | |
| 568 | | 5.0 | | | | | | | |
| 206 | | 2.0 | | | | | | | |

```
[61]: figure, axes = plt.subplots(figsize=(10,6))
sns.heatmap(fsev_sample.transpose(), xticklabels=False, ax=axes, cmap="YlOrBr")
pass
```



- Heatmap does not show clear trends, but we see that some phobias have higher values than others.
- We display this more explicitly by sorted means.
- Then we “standardize” values for individual phobias by subtracting the mean and dividing by the standard deviation.
- After this change, each phobia has mean 0 and standard deviation 1.
- People with positive scores fear that subject more than average, with negative scores less than average.

```
[62]: display(Markdown("**Phobias sorted by mean score in the survey:**"))
display(fsev_sample.mean().sort_values())
```

Phobias sorted by mean score in the survey:

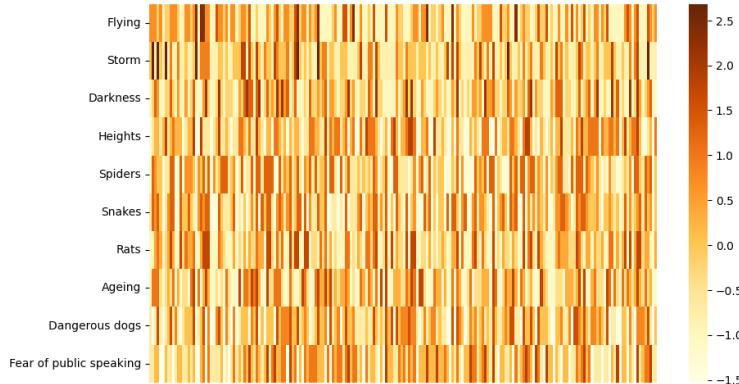
| | |
|-------------------------|-------|
| Storm | 1.970 |
| Flying | 2.180 |
| Darkness | 2.310 |
| Rats | 2.475 |
| Ageing | 2.575 |
| Heights | 2.740 |
| Fear of public speaking | 2.815 |
| Dangerous dogs | 2.920 |
| Spiders | 2.975 |
| Snakes | 3.015 |

dtype: float64

```
[63]: fsev_sample_standardized = (fsev_sample - fsev_sample.mean()) / fsev_sample.
    ↵std()
display(fsev_sample_standardized.head())
```

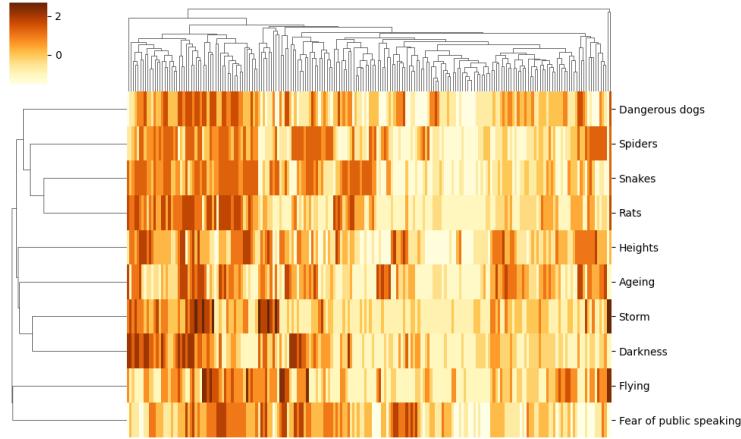
| | Flying | Storm | Darkness | Heights | Spiders | Snakes | Rats | \ |
|-----|-----------|----------------|-------------------------|-----------|-----------|-----------|-----------|---|
| 995 | 0.694374 | 0.026563 | -1.019166 | -1.411326 | -1.281210 | -0.675758 | -1.022784 | |
| 27 | 0.694374 | 2.682911 | -0.241177 | -0.600219 | 1.313646 | 1.321556 | -1.022784 | |
| 978 | 0.694374 | -0.858886 | 1.314803 | 0.210888 | 0.664932 | 0.655785 | 0.364042 | |
| 568 | -0.152423 | 2.682911 | 0.536813 | 0.210888 | 0.016218 | 1.321556 | 1.057455 | |
| 206 | 0.694374 | 0.026563 | -1.019166 | -0.600219 | 0.016218 | -0.009987 | 0.364042 | |
| | Ageing | Dangerous dogs | Fear of public speaking | | | | | |
| 995 | -1.147529 | | -0.709371 | | -0.686886 | | | |
| 27 | 1.038241 | | -1.480427 | | -0.686886 | | | |
| 978 | 1.038241 | | -0.709371 | | 0.155919 | | | |
| 568 | 1.038241 | | 1.603796 | | 0.155919 | | | |
| 206 | -0.418939 | | -0.709371 | | -1.529692 | | | |

```
[64]: figure,axes = plt.subplots(figsize=(10,6))
sns.heatmap(fsev_sample_standardized.transpose(), xticklabels=False,□
            cmap="YlOrBr")
pass
```



- Heatmap now does not show much.
- Below we reorder its rows and columns by [clustering](#) (zhlukovanie), which puts similar rows and similar columns together.
- The degree of similarity is reflected also in the trees (recall last lecture about hierarchies).
- Some areas of dark and light colors now appear.

```
[65]: sns.clustermap(fsev_sample_standardized.transpose(),
                    xticklabels=False, figsize=(10,6), cmap="YlOrBr")
pass
```



1.9 Dimensionality reduction

Methods for dimensionality reduction project high-dimensional data into lower-dimensional (usually 2D) space, while trying to preserve some structure in the original data.

- **Principal component analysis** (PCA) uses a linear projection: each new dimension is a linear combination (weighted sum) of the original dimensions. Weights are chosen to maximize variance.

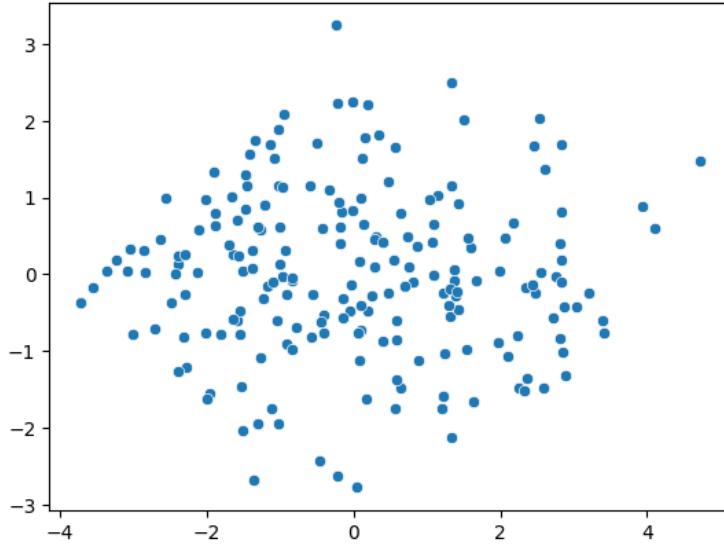
Some methods do not use linear projections, but try to preserve distances between points, for example: * Multidimensional scaling (MDS), * T-distributed Stochastic Neighbor Embedding (t-SNE).

We will use PCA from the [scikit-learn library](#) for machine learning in Python.

```
[66]: from sklearn.decomposition import PCA
# compute PCA of our standardized data with 2 dimensions
fsev_pca = PCA(n_components=2).fit_transform(fsev_sample_standardized)
display(Markdown("**PCA transformed values** (first five lines):"))
display(fsev_pca[0:5, :])
axes = sns.scatterplot(x=fsev_pca[:, 0], y=fsev_pca[:, 1])
```

PCA transformed values (first five lines):

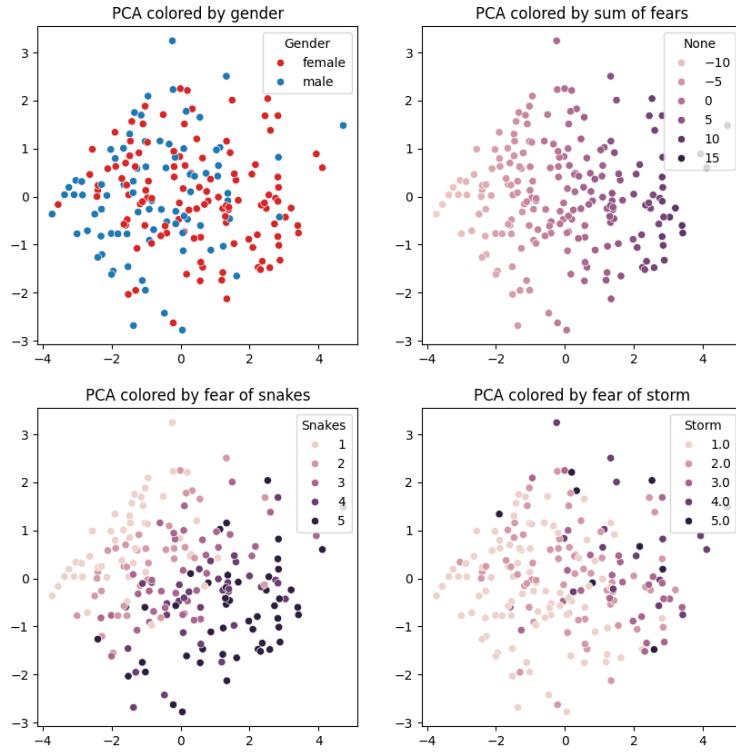
```
array([[-2.40005395,  0.13763973],
       [ 0.79985413, -0.09193566],
       [ 1.09446725, -0.01171503],
       [ 2.83751212,  0.19095389],
       [-0.90658354, -0.90915457]])
```



The scatterplot starts to be interesting if we can color points by some known factors.

- Below we see that men and women are quite mixed but women are shifted to the left.
- It seems that the first dimension strongly correlates with the overall fearlessness of a person.
- Fears of snakes and storms are strongly related to the overall fearfulness, but they also have trends along the y-axis.

```
[67]: # all columns for our sample to select gender and all data
fsev_sample_all = fsev.loc[fsev_sample.index,]
figure, axes = plt.subplots(2, 2, figsize=(10,10))
sns.scatterplot(x=fsev_pca[:, 0], y=fsev_pca[:, 1],
                 hue=fsev_sample_all['Gender'],
                 hue_order=['female', 'male'], palette=['C3', 'C0'],
                 ax=axes[0,0])
axes[0,0].set_title('PCA colored by gender')
sns.scatterplot(x=fsev_pca[:, 0], y=fsev_pca[:, 1],
                 hue=fsev_sample_standardized.sum(axis=1), ax=axes[0,1])
axes[0,1].set_title('PCA colored by sum of fears')
sns.scatterplot(x=fsev_pca[:, 0], y=fsev_pca[:, 1],
                 hue=fsev_sample_all['Snakes'], ax=axes[1,0])
axes[1,0].set_title('PCA colored by fear of snakes')
sns.scatterplot(x=fsev_pca[:, 0], y=fsev_pca[:, 1],
                 hue=fsev_sample_all['Storm'], ax=axes[1,1])
axes[1,1].set_title('PCA colored by fear of storm')
pass
```



1.10 Conclusion and other courses

We briefly covered several statistical concepts often used in visualization:

- histogram,
- kernel density estimation,
- empirical cumulative distribution function,
- clustering,
- dimensionality reduction.

You will learn more in the next years of your study:

- [Fundamentals of Probability and Statistics](#), 2W (DAV) or 3W (BIN)
- [Principles of Data Science](#) 3W (DAV)
- [Linear Algebra](#) this semester

Lecture 8

Visual perception and colors

Data visualization · 1-DAV-105

Lecture by Broňa Brejová

Acknowledgement: materials inspired by lectures from Martina Bátorová in 2021

Aside: data analysis / visualization project phases

- Obtaining data
- Data preprocessing, **checking**, cleaning
- **Exploratory** analysis (many tables and graphs for your use)
- Formation of **hypotheses**
- Testing hypotheses (careful reanalysis, new data, other sources)
- **Explanatory** visualizations for the final report / presentation (best views selected for the audience)

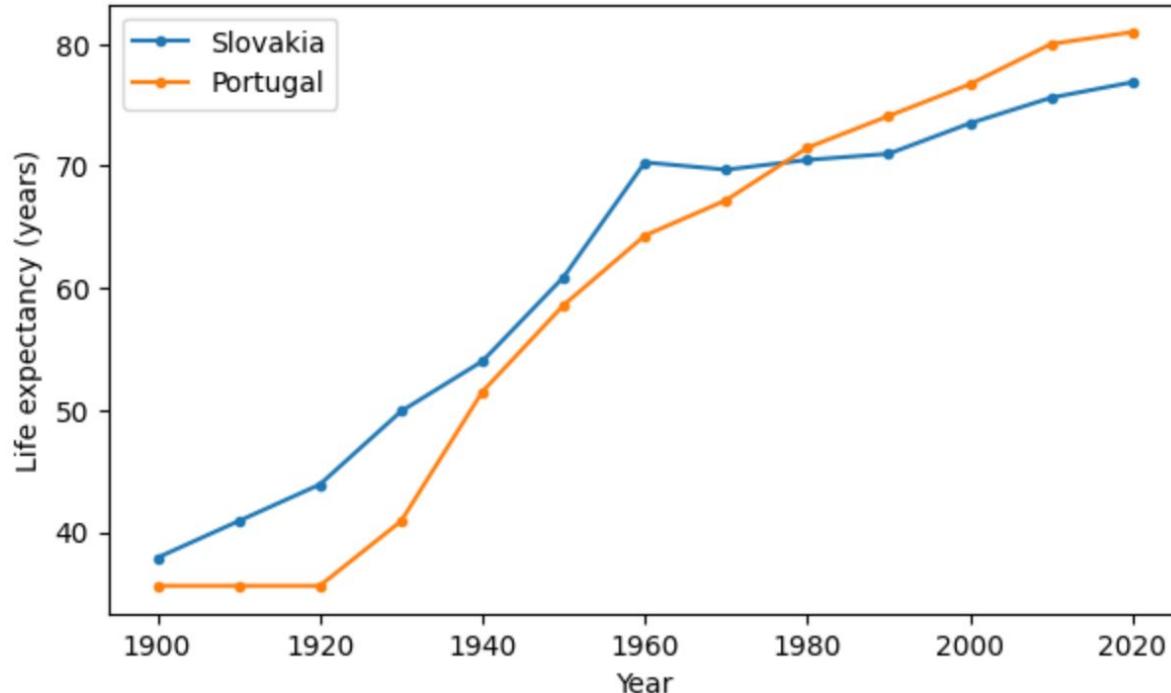
More in two weeks

Why talk about visual perception
in visualization?

In which period of time was life expectancy higher in Slovakia than in Portugal?

| | 1900 | 1910 | 1920 | 1930 | 1940 | 1950 | 1960 | 1970 | 1980 | 1990 | 2000 | 2010 | 2020 |
|-----------------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| Country | | | | | | | | | | | | | |
| Slovak Republic | 37.9 | 40.9 | 43.9 | 49.9 | 54.0 | 60.9 | 70.3 | 69.7 | 70.5 | 71.0 | 73.5 | 75.6 | 76.9 |
| Portugal | 35.6 | 35.6 | 35.6 | 40.9 | 51.5 | 58.6 | 64.3 | 67.2 | 71.5 | 74.1 | 76.7 | 80.0 | 81.0 |

In which period of time was life expectancy higher in Slovakia than in Portugal?



Visual brain, table vs. graph

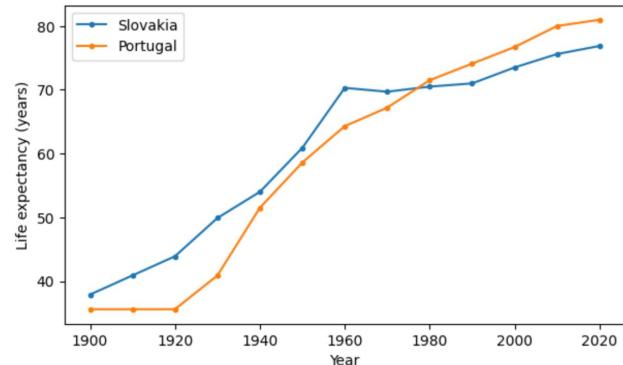
We "read" tables, verbal processing

We "see" plots, visual processing

Visual processing is very parallel and fast, evolved to spot predators

In which situations is a table preferable to a plot?

| Country | 1900 | 1910 | 1920 | 1930 | 1940 | 1950 | 1960 | 1970 | 1980 | 1990 | 2000 | 2010 | 2020 |
|-----------------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| Slovak Republic | 37.9 | 40.9 | 43.9 | 49.9 | 54.0 | 60.9 | 70.3 | 69.7 | 70.5 | 71.0 | 73.5 | 75.6 | 76.9 |
| Portugal | 35.6 | 35.6 | 35.6 | 40.9 | 51.5 | 58.6 | 64.3 | 67.2 | 71.5 | 74.1 | 76.7 | 80.0 | 81.0 |



Human visual perception

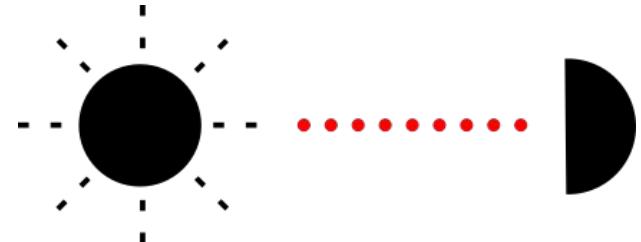
What happens when we look at the figure below?



Human visual perception

Human visual perception

What happens when we look at the figure?

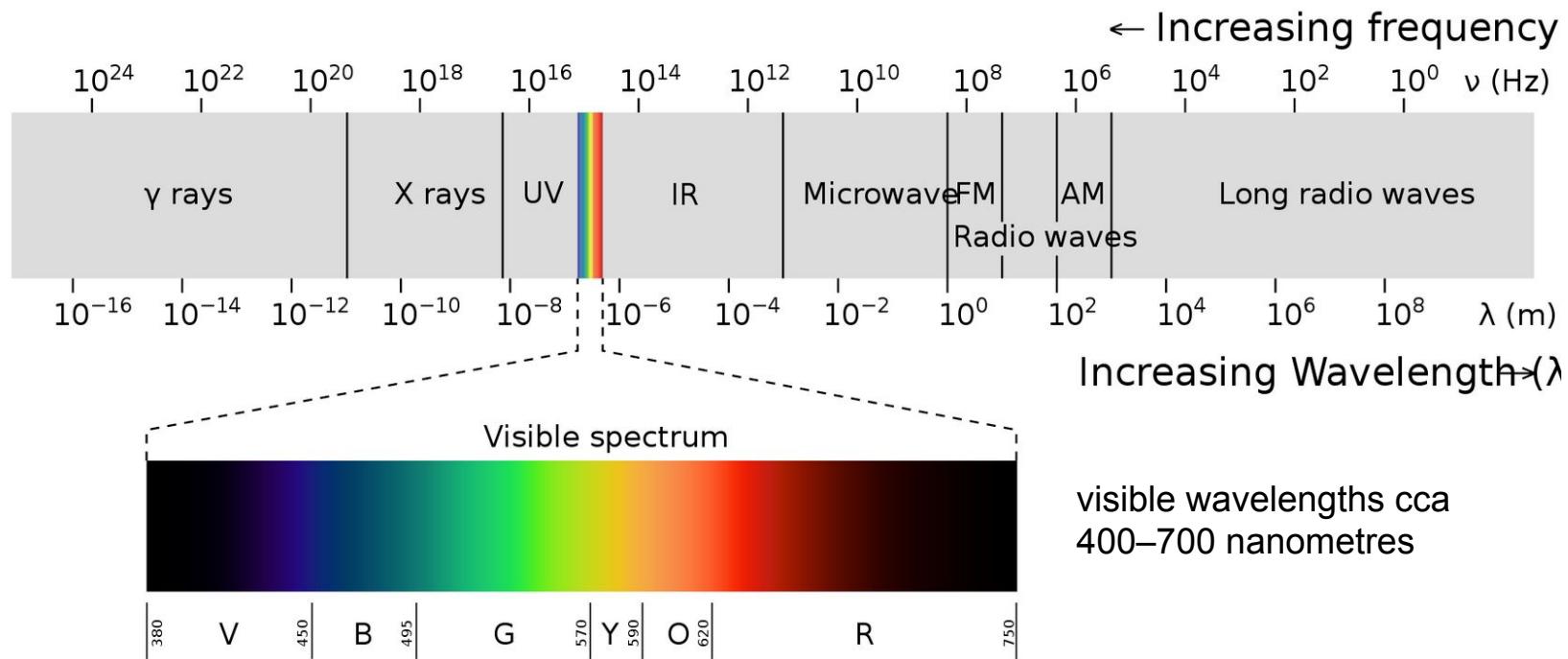


- The **light** from the screen / projector hits the retinas of our **eyes**
- Photoreceptor cells **transduce** (convert) this signal into nerve impulses
- In the brain:
 - detection of **basic features**
 - recognition of **patterns**
 - interpretation, assignment of **meaning**

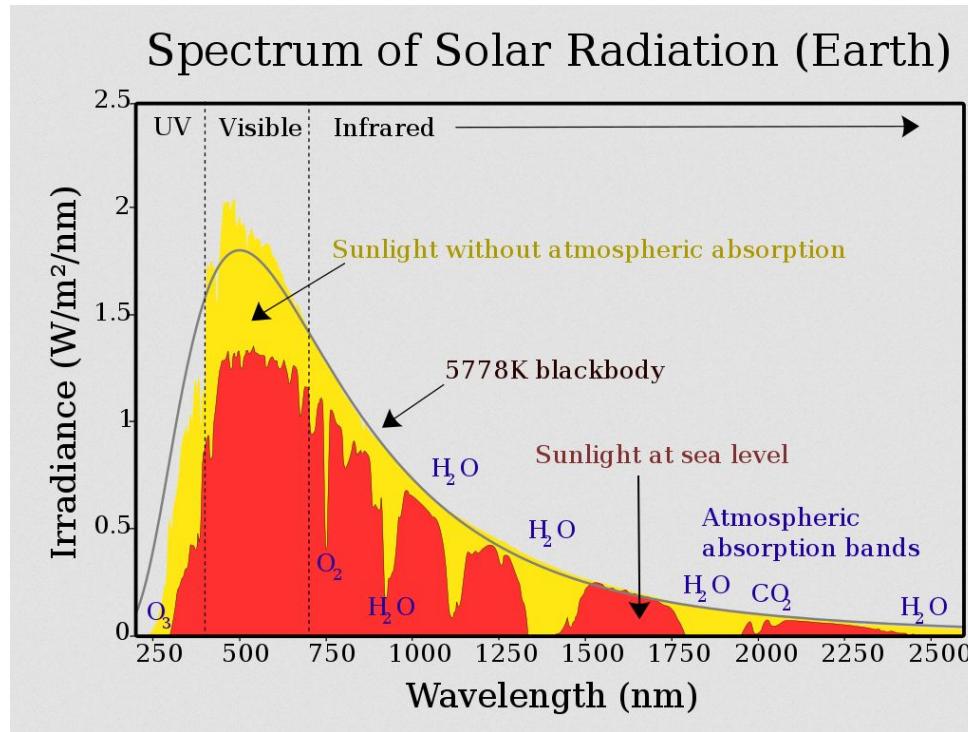
Today: Focus on the light, eyes and colors, later stages next week

Light

Visible light as a part of electromagnetic spectrum



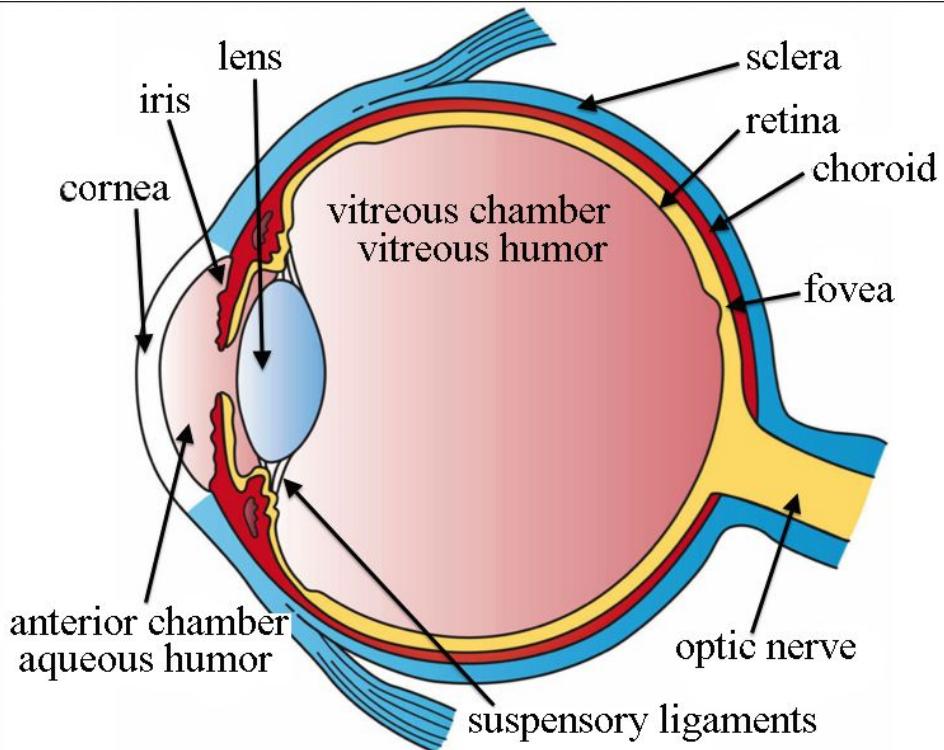
Sunlight is a mixture of different wavelengths



https://commons.wikimedia.org/wiki/File:Solar_spectrum_en.svg
<https://commons.wikimedia.org/wiki/File:WhereRainbowRises.jpg>

Human eye

Human eye

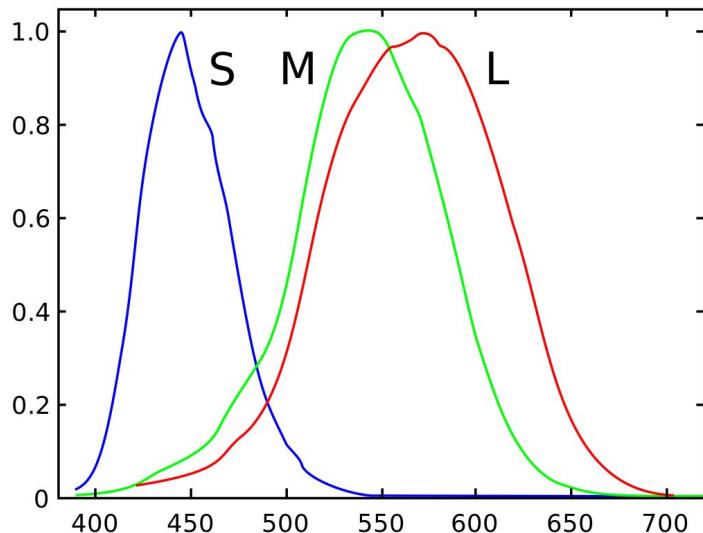


Retina (sietnica): light-sensitive layer

Lens (šošovka): focus light to retina

Pupil (zrenica): hole in iris (dúhovka) where light enters the eye, its size regulated by the amount of light

Photoreceptor cells in the retina

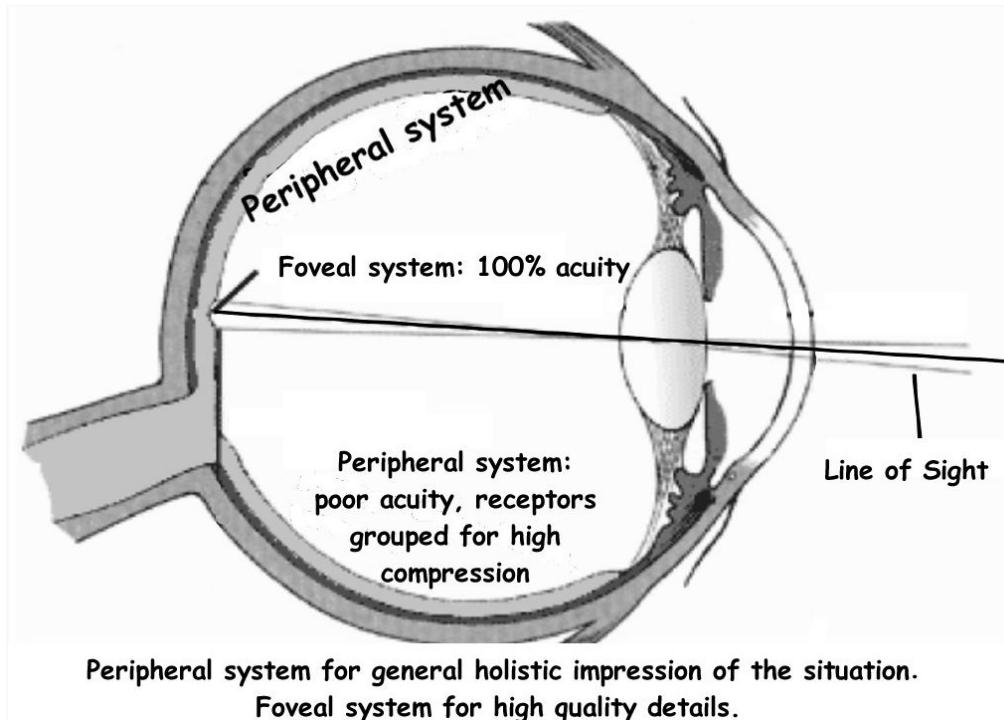


Rods (tyčinky): more sensitive to low light, not used for color vision

Cones (čapíky): color vision, three different types sensitive to different wavelengths (blue, green, red)

https://commons.wikimedia.org/wiki/File:Cones_SMJ2_E.svg

Foveal vs peripheral vision



Fovea: central zone with many cones, sharp color vision, only about 1-2°

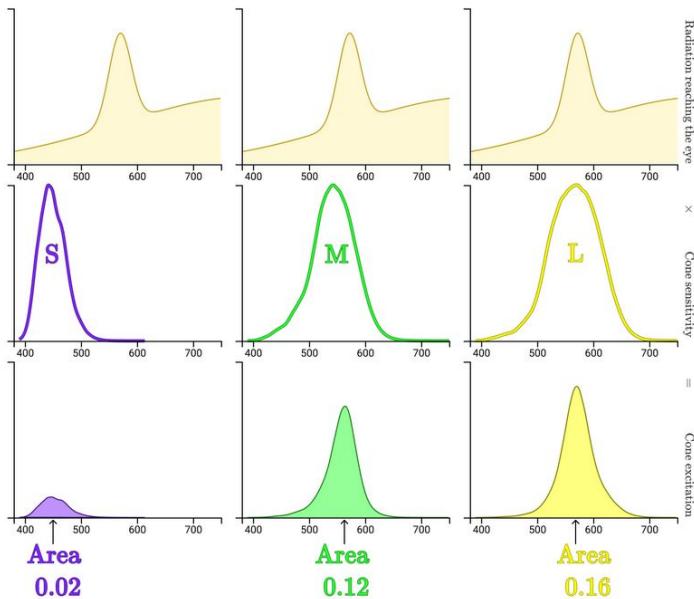
Peripheral vision: mostly rods, fast monochrome vision

The eyes make fast **movements** (saccades) between fixations on different points of interest to create a composite image

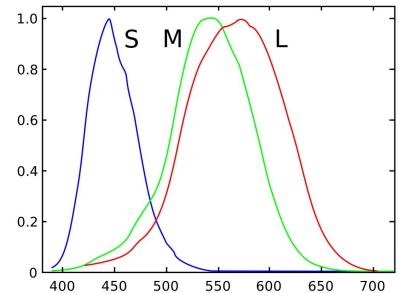
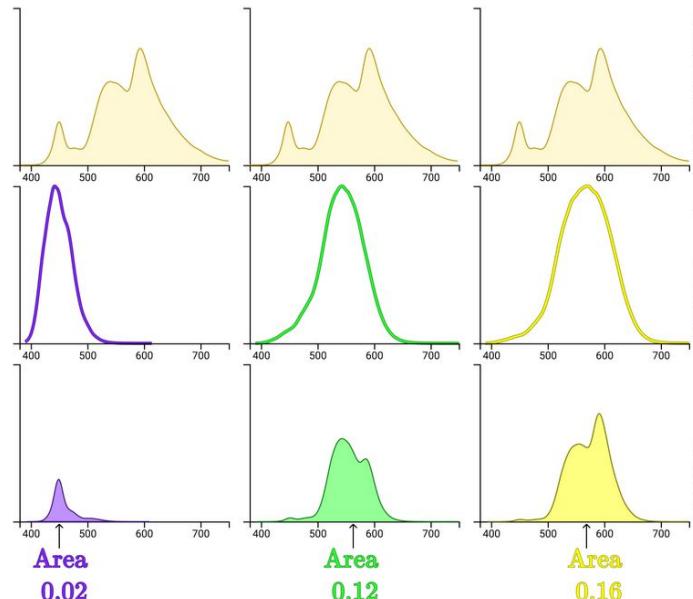
Colors and color spaces

Metamers: light with different spectra that appear the same (to typical humans)

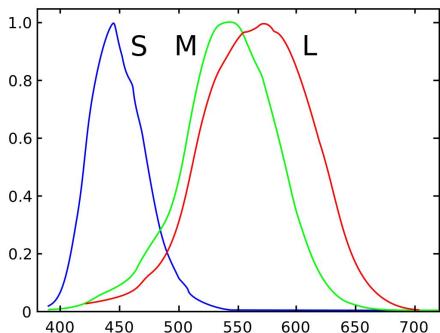
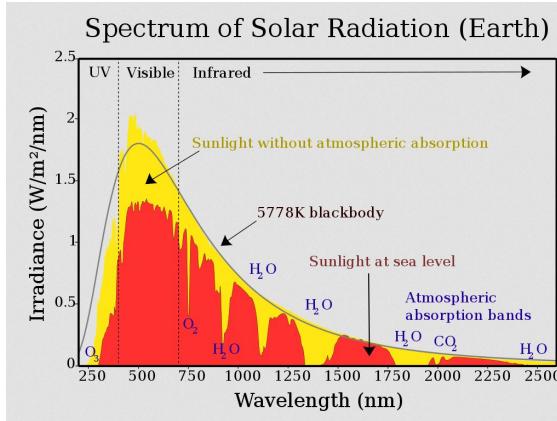
Cone excitation by a point on a lemon



Cone excitation by a pixel of a lemon on a screen



Color spaces, LMS



A **color space** is an organization of colors.

Our eye projects a full light spectrum into three values: response of the three types of cones.

S (short), M (medium), L (large) wavelength

LMS color space uses these three values to represent a color.

Metameric colors have the same values.

Derived models, e.g. CIE with better properties.

https://commons.wikimedia.org/wiki/File:Solar_spectrum_en.svg

https://commons.wikimedia.org/wiki/File:Cones_SMJ2_E.svg

Do you know some other color spaces?

Additive color models, RGB

Monitors, projectors etc.

Component lights in **primary colors**,
other colors mixtures of these (adding up light).

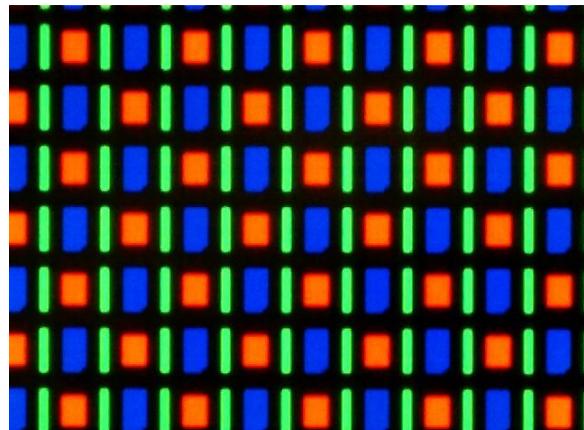
White can be achieved by combining colors.

RGB uses **red, green, blue** as primary
(corresponds to LMS peaks).

The **gamut** is the set of colors representable by a device, usually a subset of the visible spectrum.

https://commons.wikimedia.org/wiki/File:RGB_illumination.jpg

https://commons.wikimedia.org/wiki/File:Nexus_one_screen_microscope.jpg



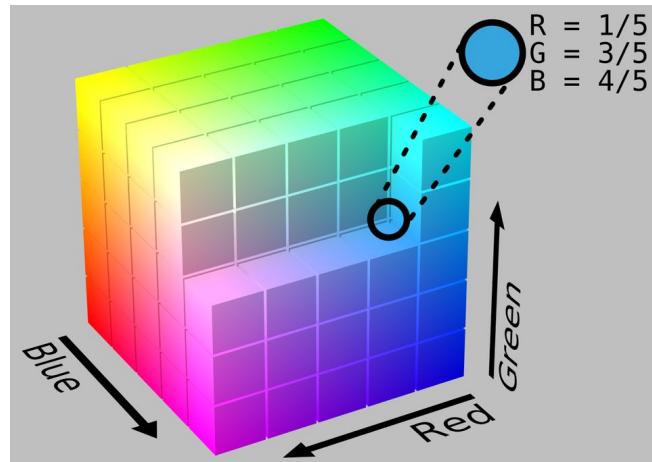
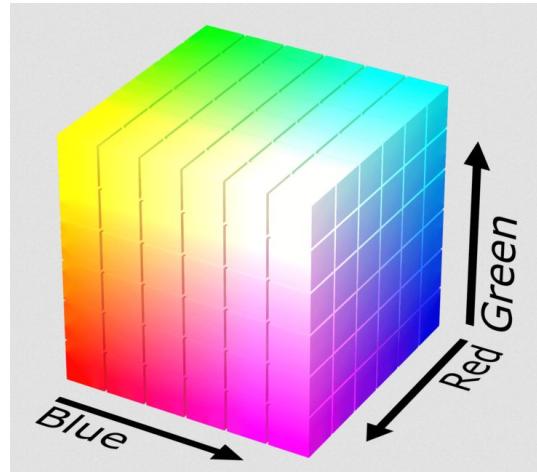
Colors in RGB space (RGB cube)

RGB is often used to specify colors.

Each coordinate e.g. a real number between 0 and 1 or integer between 0 and 255.

Also hexadecimal notation, e.g. #ff0000 is pure red.

Greytones on the main diagonal (x,x,x).



https://commons.wikimedia.org/wiki/File:RGB_color_solid_cube.png

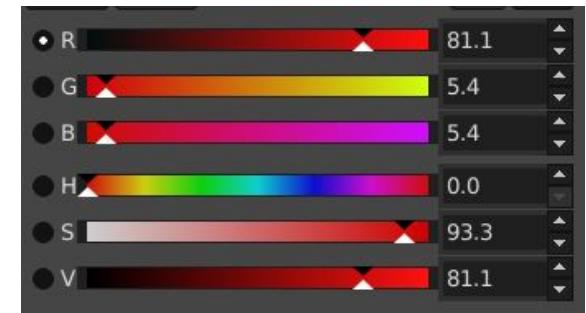
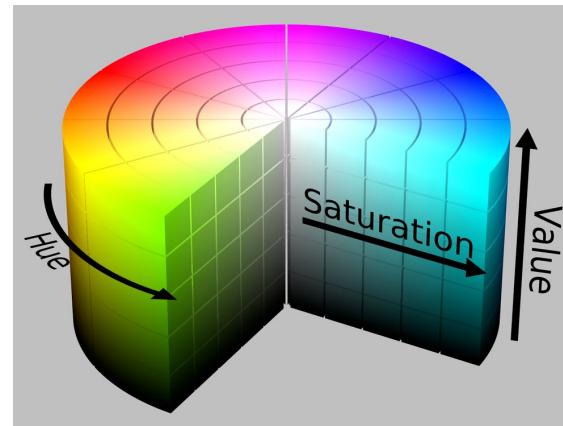
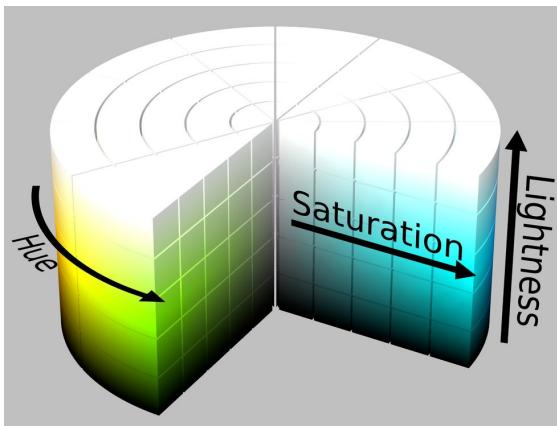
https://commons.wikimedia.org/wiki/File:RGB_Cube_Show_lowgamma_cutout_b.png

HSL and HSV color models

Transformations of RGB model with more intuitive coordinates.

Useful for color pickers, color palettes, image transformations etc.

Hue, saturation, lightness / hue, saturation, value.



https://commons.wikimedia.org/wiki/File:HSL_color_solid_cylinder_saturation_gray.png
https://commons.wikimedia.org/wiki/File:HSV_color_solid_cylinder_saturation_gray.png

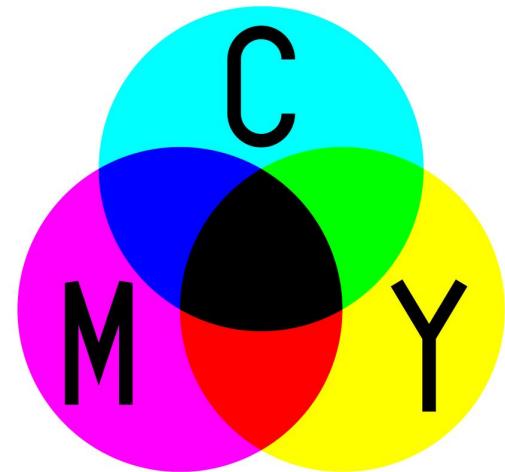
Subtractive models, pigments

Pigments block part of the light spectrum.

Adding more pigments blocks (subtracts) more light.

Black can be achieved by combining colors.

Example: CMY(K) color model used in **printing**.



<https://commons.wikimedia.org/wiki/File:SubtractiveColor.svg>

CMY(K) color model

Primary colors cyan, magenta and yellow

- **cyan** absorbs red
- **magenta** absorbs green
- **yellow** absorbs blue

Black (K) added because

- it is cheaper
- it hides artifacts in dark colors



Conversion from RGB to CMYK is difficult,
device-dependent.

https://commons.wikimedia.org/wiki/File:Barns_grand_tetons.jpg

https://commons.wikimedia.org/wiki/File:CMY_separation_%E2%80%93_no_black.jpg

https://commons.wikimedia.org/wiki/File:CMYK_separation_%E2%80%93_maximum_black.jpg

Color wheel, RYB model

Subtractive model developed in art,
for mixing pigments

Dates back to 17th century

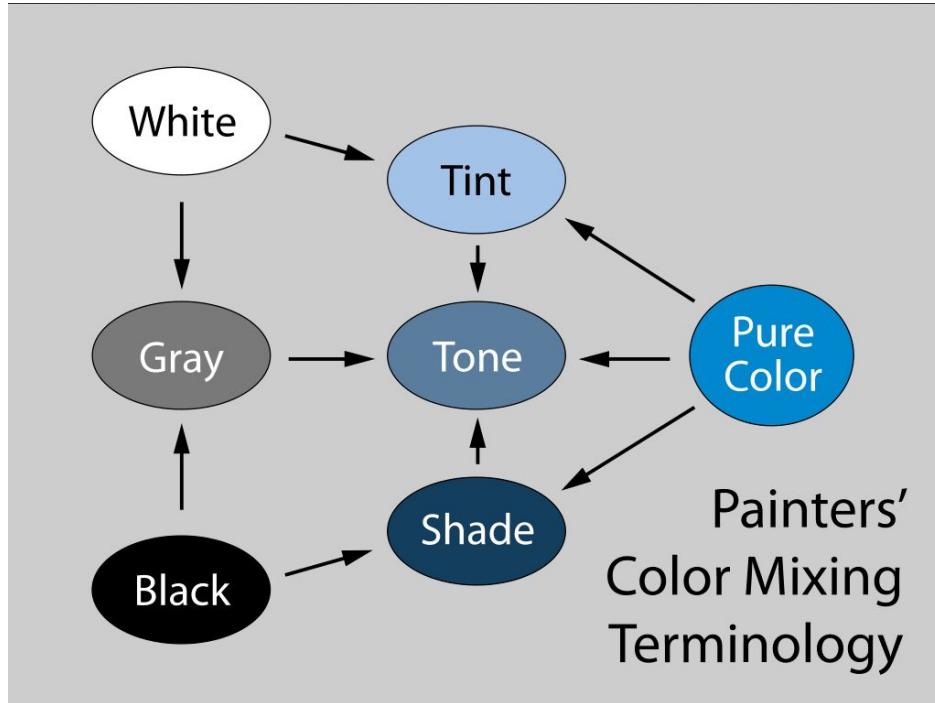
Primary colors red, yellow, blue

Secondary orange, green, purple
(each a mix of two primaries)



https://www.w3schools.com/colors/colors_wheels.asp

Tint, tone, shade - more painter terminology



<https://commons.wikimedia.org/wiki/File:Tint-tone-shade.svg>

Examples of color schemes

Monochromatic: tints / tones / shades of the same hue

Complementary: 2 colors opposite on the color wheel
(e.g. orange and blue)

Split complementary: color and 2 neighbors
of its complement (e.g. orange and blue-green, blue-purple)

Analogous: 3-5 adjacent colors on the wheel

Each of these can be desaturated (tints / tones / shades)

See also <https://color.adobe.com/create/color-wheel>



Color and meaning, cultural differences

Colors often symbolize different things both within and between cultures:

- for example red: blood, love, passion, life, anger, violence, danger, emergency, speed, heat ...
 - China: good luck, prosperity vs. Europe: warning
 - "in the red" mean losses in English, what about China?
- mourning color is black in Europe, white in the East

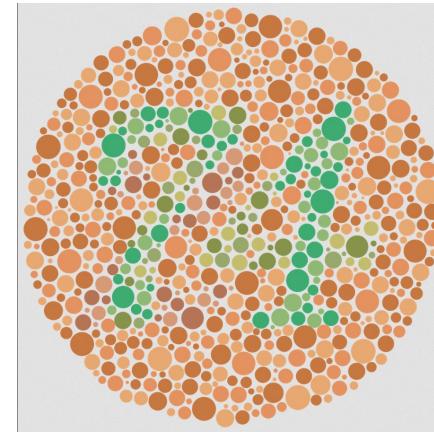
Colors in data visualization

Not everybody will be able to see your colors

Color blindness or color vision deficiency

Various forms and causes

Most often genetic red–green color blindness,
where L or M opsin gene is mutated (8% of males)



Technical problems

- Projectors often distort colors
- Black-and-white printing

https://commons.wikimedia.org/wiki/File:Ishihara_9.svg

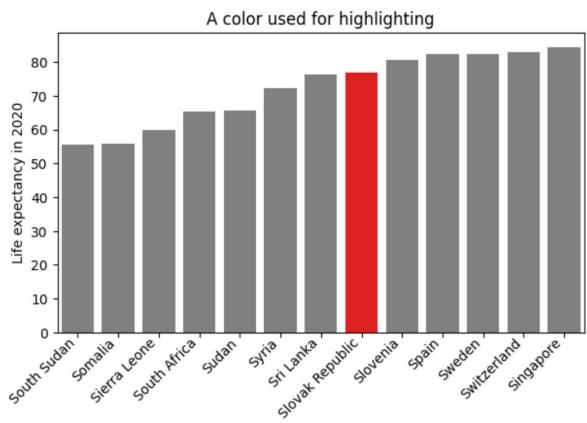
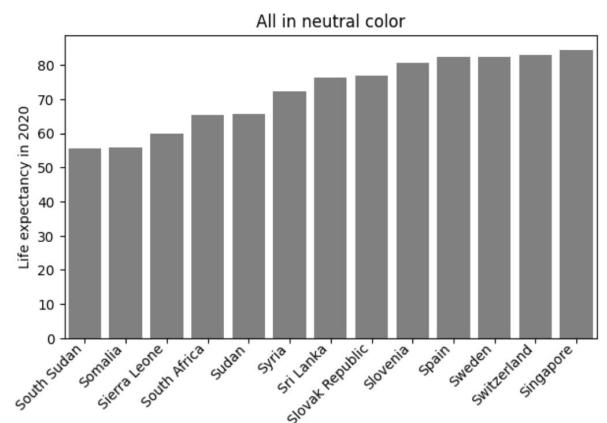
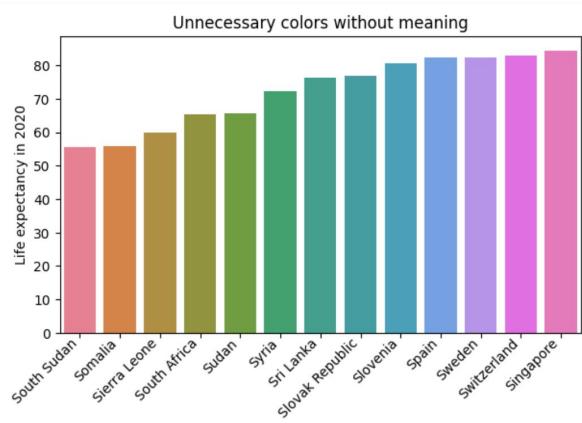
Choose your colors wisely to avoid these problems as much as possible

Color draws attention, use it sparingly

Rely on neutral tones

Use color sparingly, avoid unnecessary colors

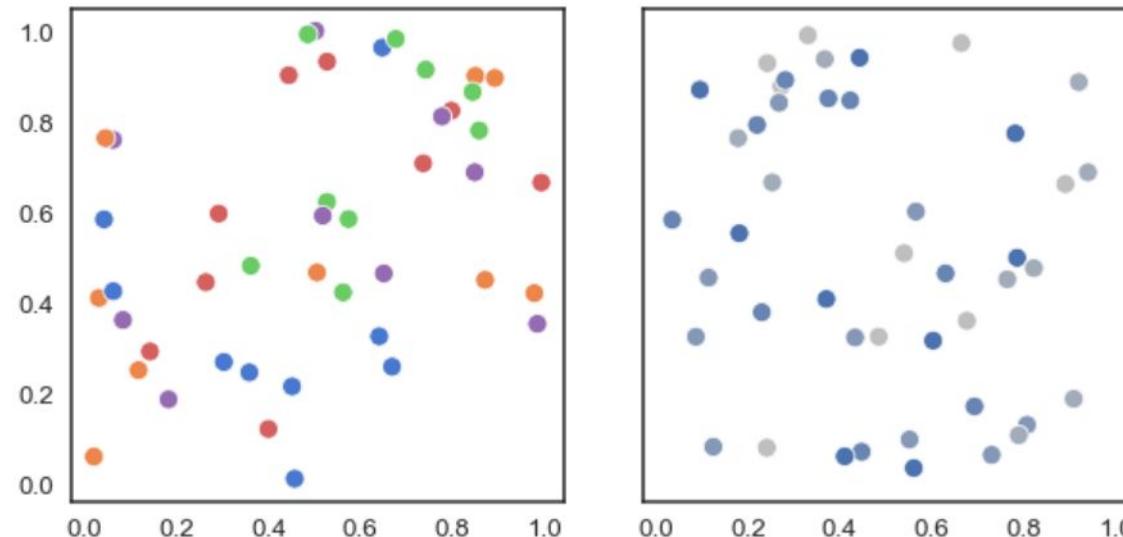
Colors are great for highlighting points of interest



Qualitative palettes (for categorical variables)

Typically vary hues, easier to distinguish than lightness of the same hue

Try to keep the number of colors low



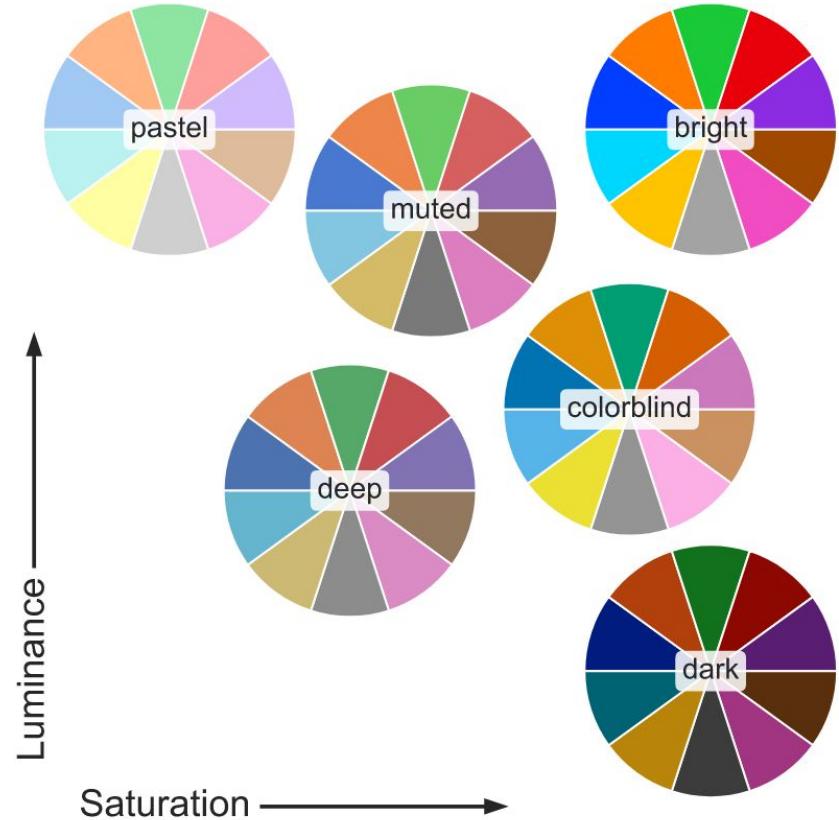
Qualitative palettes (for categorical variables)

Examples from Seaborn library
on the right:

Color Brewer tool:



https://seaborn.pydata.org/tutorial/color_palettes.html



Quantitative sequential palettes (for numerical variables)

Vary lightness rather than (just) hue (hue is circular, hard to interpret)

Discrete vs continuous:



https://seaborn.pydata.org/tutorial/color_palettes.html

Quantitative diverging palettes

For numerical variables with a special midpoint, often 0
(such as increase / decrease)

Midpoint displayed as a special neutral color, e.g. grey



https://seaborn.pydata.org/tutorial/color_palettes.html

Summary

Visual perception:

- light on the retina, transduction on photoreceptor cells
- feature detection, pattern formation, interpretation

Light and color:

- Visible light as a part of electromagnetic spectrum
- Three types of cones sensitive to different wavelengths of light

Color spaces (LMS, RGB, HSL, HSV, CMYK, RYB)

Colors in visualization (qualitative and quantitative palettes, color blindness, sparing use of colors)

Graphics file formats (for exporting graphs)

Raster formats: store your plot as pixels at some resolution

- resolution leads to tradeoff between size and quality
- prefer lossless compression (PNG rather than JPEG)
- transparent background may be also a good idea

Vector formats: store your plot as geometric objects (SVG, PDF, EPS)

- can be arbitrarily enlarged, editable
- can be large if many points / lines (subsample data?)
- vector formats usually preferable unless not supported by software
- it is a good idea to include fonts in the file
- beware that these file formats may include bitmaps

Lecture 9

Pre-attentive attributes, gestalt, illusions

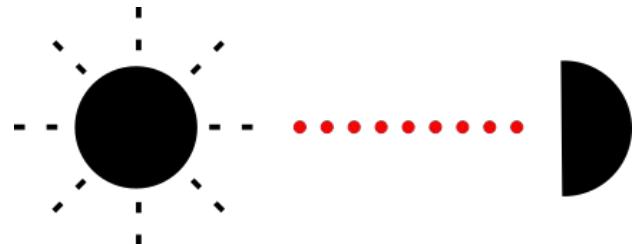
Data visualization · 1-DAV-105

Lecture by Broňa Brejová

Acknowledgement: materials inspired by lectures from Martina Bátorová in 2021

Human visual perception

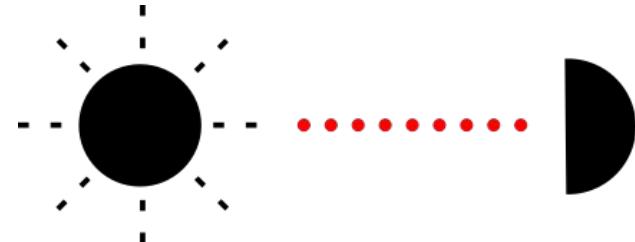
What happens when we look at the figure?



- The **light** from the screen / projector hits the retinas of our **eyes**
- Photoreceptor cells **transduce** (convert) this signal into nerve impulses
- In the brain:
 - detection of **basic features**
 - recognition of **patterns**
 - interpretation, assignment of **meaning**

Human visual perception

What happens when we look at the figure?



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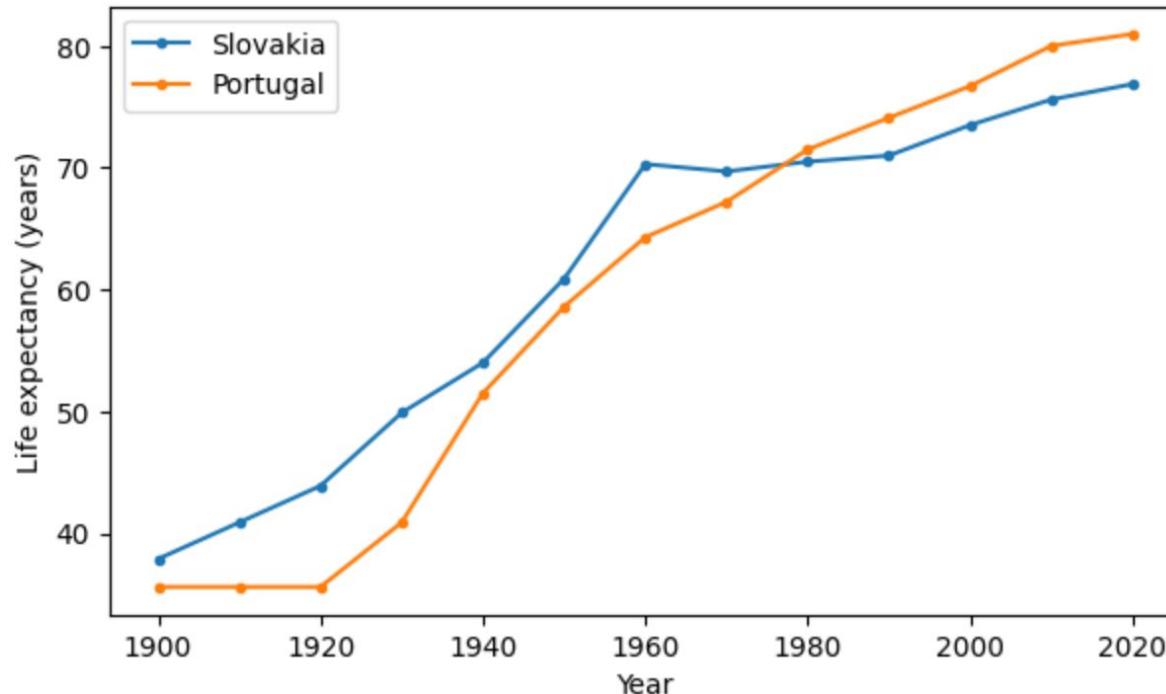
Today: Detection of features and patterns, use for visualization

Note: Human visual perception is very good for detecting **motion** (danger/prey). This is relevant for animated visualization, but not covered today.

In which period of time was life expectancy higher in Slovakia than in Portugal?

| | 1900 | 1910 | 1920 | 1930 | 1940 | 1950 | 1960 | 1970 | 1980 | 1990 | 2000 | 2010 | 2020 |
|-----------------|------|------|------|------|------|------|------|------|------|------|------|------|------|
| Country | | | | | | | | | | | | | |
| Slovak Republic | 37.9 | 40.9 | 43.9 | 49.9 | 54.0 | 60.9 | 70.3 | 69.7 | 70.5 | 71.0 | 73.5 | 75.6 | 76.9 |
| Portugal | 35.6 | 35.6 | 35.6 | 40.9 | 51.5 | 58.6 | 64.3 | 67.2 | 71.5 | 74.1 | 76.7 | 80.0 | 81.0 |

In which period of time was life expectancy higher in Slovakia than in Portugal?



How many copies of digit six do you see?

1014508

2530653

6821550

3702967

8622988

What about now?

1014508

2530**6**53

6821550

3702967

8622988

What about Slovakia vs Portugal in this table?

| | 1900 | 1910 | 1920 | 1930 | 1940 | 1950 | 1960 | 1970 | 1980 | 1990 | 2000 | 2010 | 2020 |
|----------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| Slovakia | 37.9 | 40.9 | 43.9 | 49.9 | 54.0 | 60.9 | 70.3 | 69.7 | 70.5 | 71.0 | 73.5 | 75.6 | 76.9 |
| Portugal | 35.6 | 35.6 | 35.6 | 40.9 | 51.5 | 58.6 | 64.3 | 67.2 | 71.5 | 74.1 | 76.7 | 80.0 | 81.0 |

Pre-attentive attributes

- Features of the seen objects detected by our brain very **fast**
- Prior to and **without** the need of conscious **awareness**
- Brain uses them to **guide attention** / gaze to interesting parts of the scene
- Their correct use allows fast and effortless understanding of our visualizations

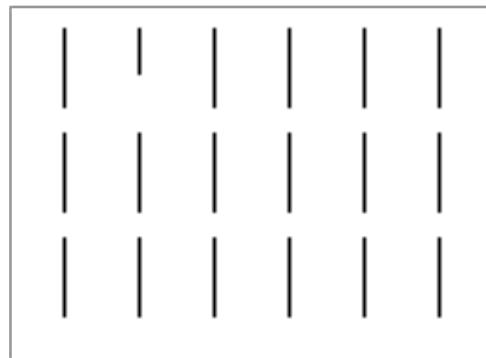
Next:

Examples of important pre-attentive attributes (form, color, position)
following Few 2009

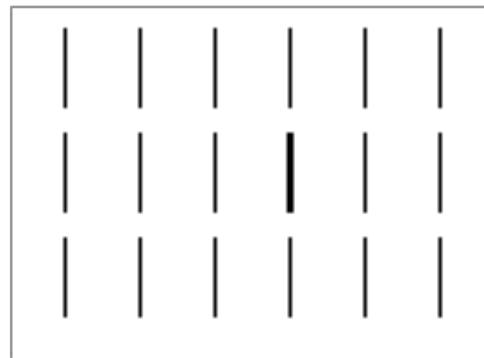
See also <https://www.csc2.ncsu.edu/faculty/healey/PP/>

Pre-attentive attributes: form

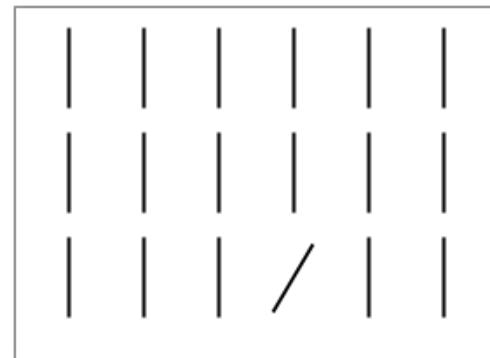
We can quickly distinguish one object that differs from the rest



Length



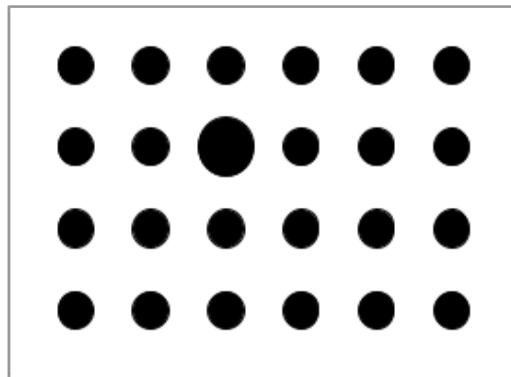
Width



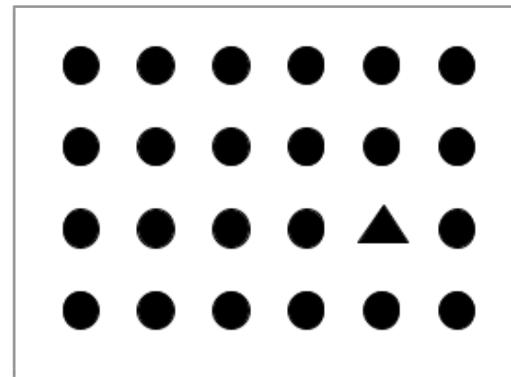
Orientation

Pre-attentive attributes: form

We can quickly distinguish one object that differs from the rest



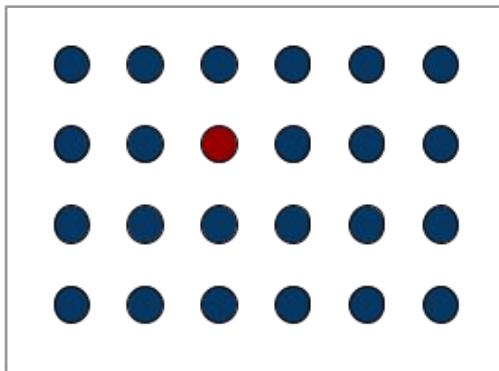
Size



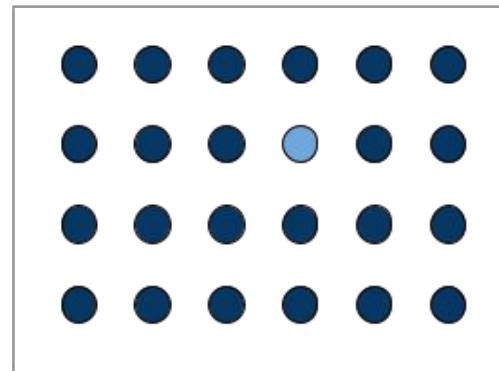
Shape

Pre-attentive attributes: color

We can quickly distinguish one object that differs from the rest

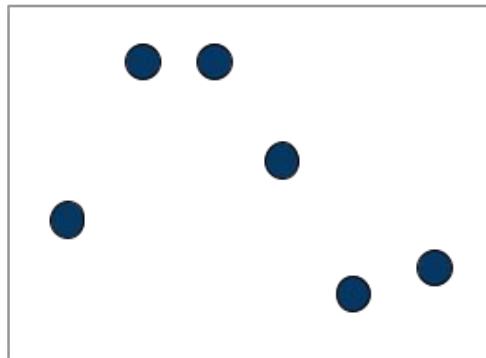


Hue

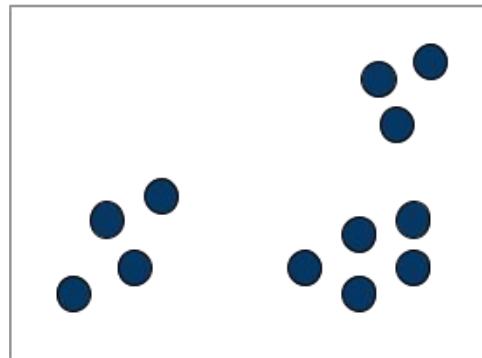


Lightness

Pre-attentive attributes: position



2D



Groups

Hierarchy of graph elements

Cleveland, McGill 1985

Experiments with volunteers of how well they **judge ratios** between values graphically encoded in different ways.

Not all pre-attentive attributes are equally good for **quantitative reasoning**.

Prefer elements on the left side for accuracy

Length (aligned)



Length



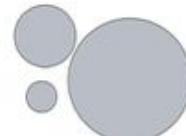
Slope



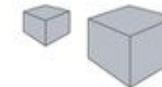
Angle



Area



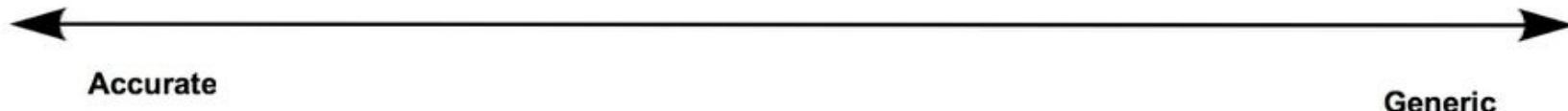
Volume



Color hue



Color intensity



The same data with length / area / color / angle

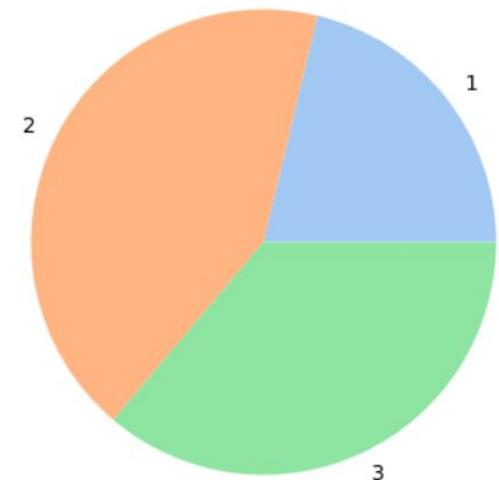
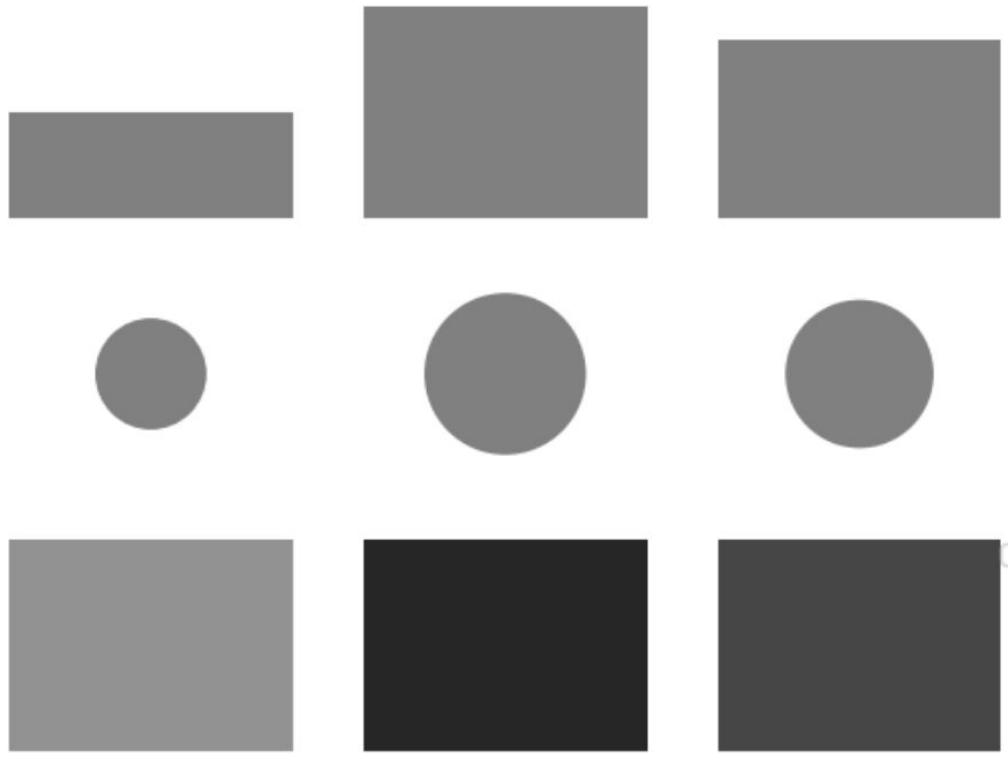


Chart selection tools

In lecture 3 and later, we have seen many types of graphs

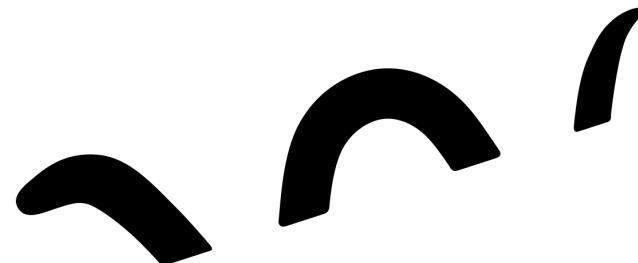
Some websites list them based on variable type and purpose for easier selection:

- <https://www.data-to-viz.com/>
- https://extremepresentation.typepad.com/blog/2006/09/choosing_a_good.html

Let us look at some the suggestions from the first website in terms of the hierarchy of graph elements

From parts to the whole: gestalt

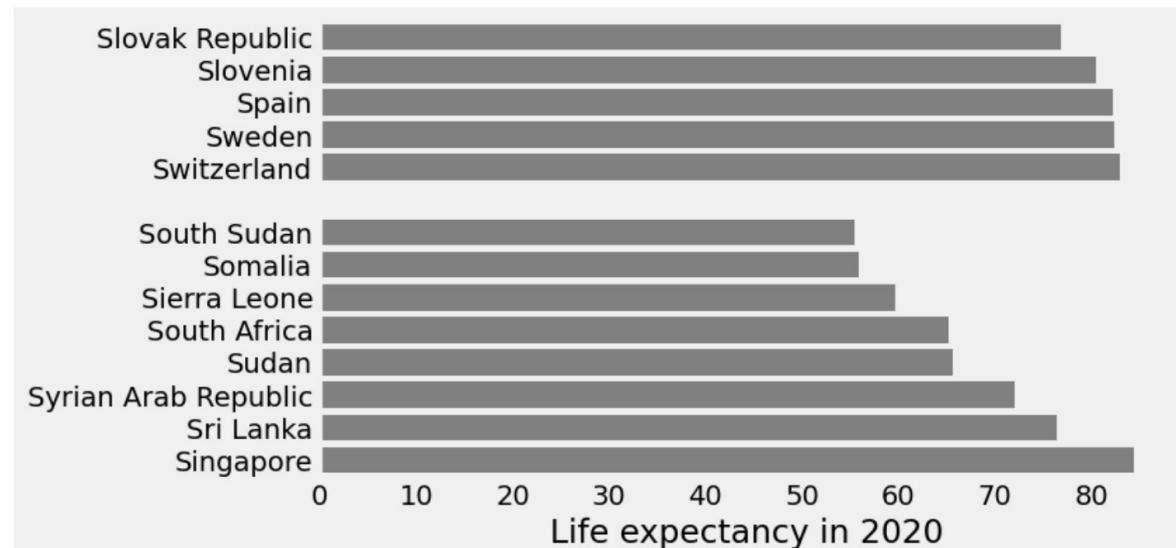
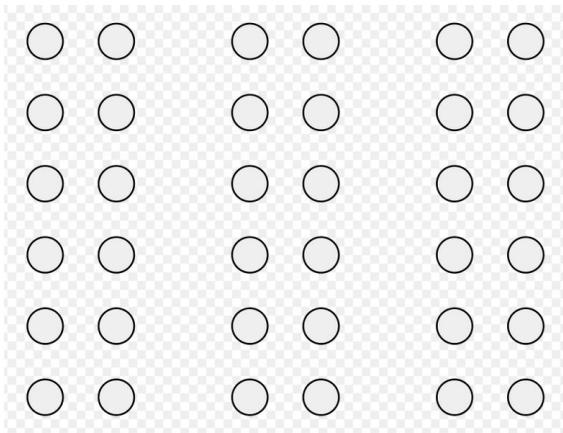
- Gestalt psychology (early 20th century, Austria and Germany)
- **Gestalt means pattern**
- Our brains group individual shapes into larger patterns
- The brain favors speed to precision (illusions, errors)
- It also favors symmetry and simplicity
- Several gestalt principles are relevant in data visualization



<https://commons.wikimedia.org/wiki/File:Reification.svg>

Principle of proximity

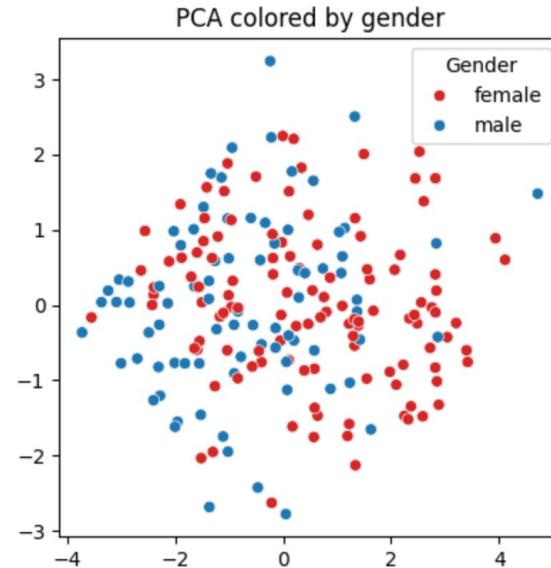
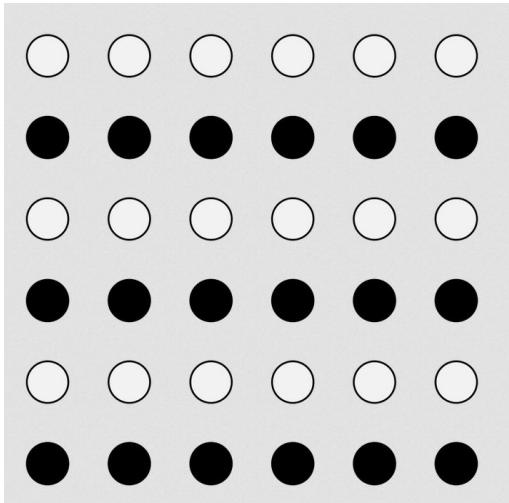
- Objects located close to each other are perceived as a group
- Good use of space in plots / tables / presentations can improve readability



https://commons.wikimedia.org/wiki/File:Gestalt_proximity.svg

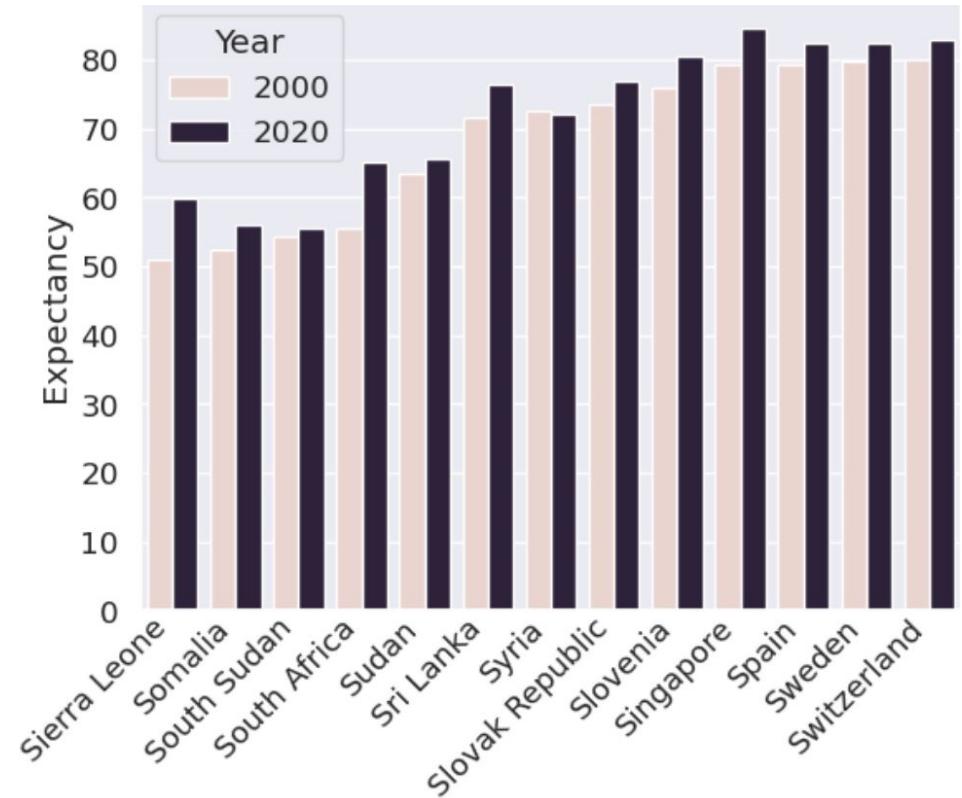
Principle of similarity

- Similar objects are perceived as a group even if not close by
- Various plots use color / shape to distinguish groups



https://commons.wikimedia.org/wiki/File:Gestalt_similarity.svg

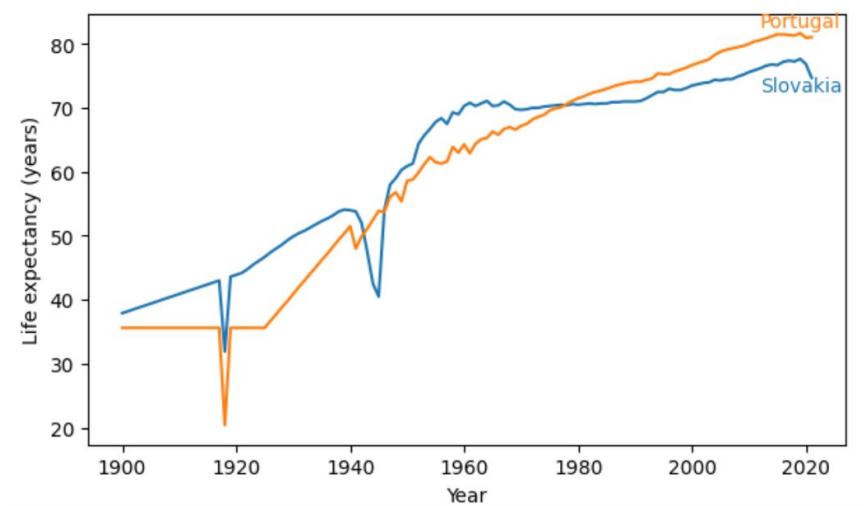
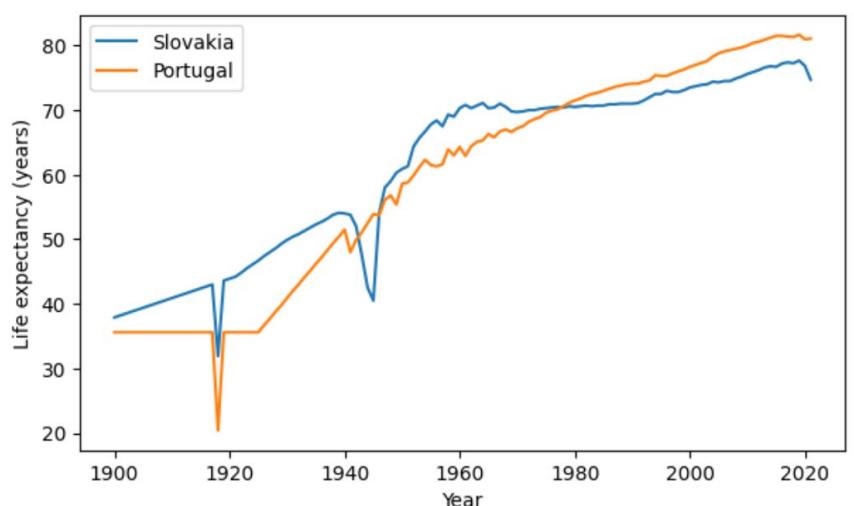
How are both principles used here?



Example

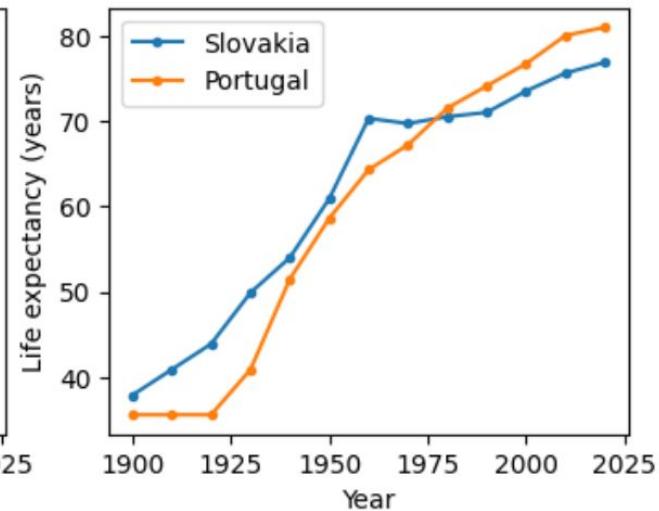
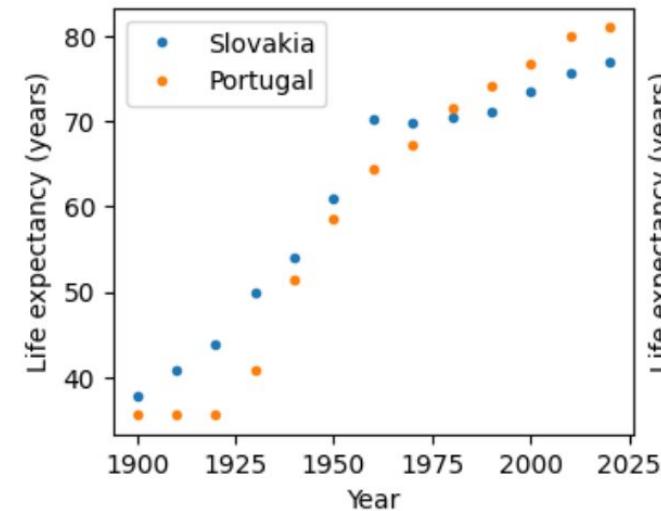
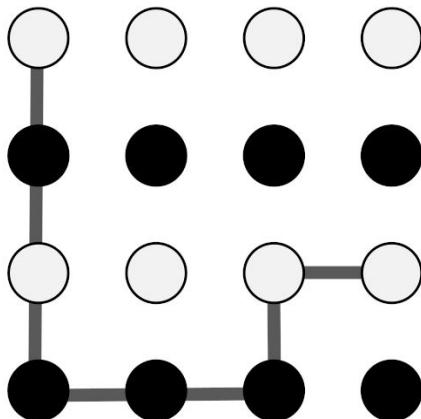
separate legend vs marking lines with text in the same color

- using principles of proximity and similarity



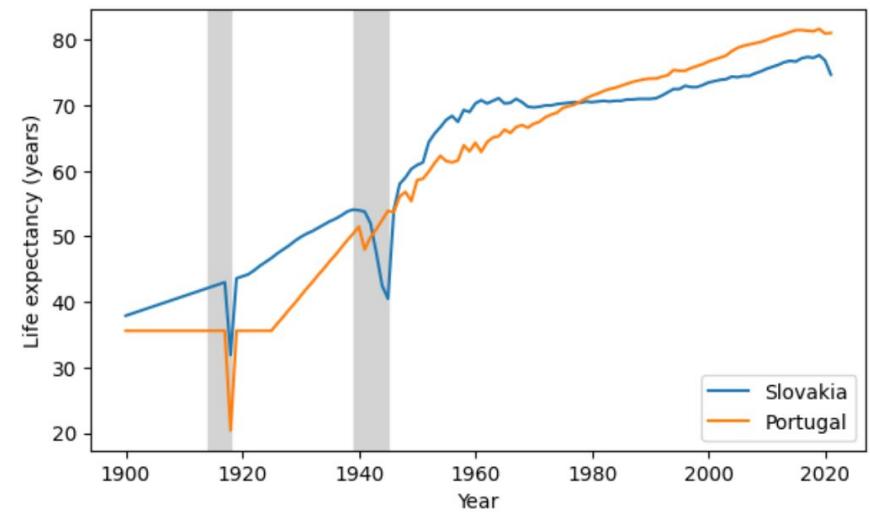
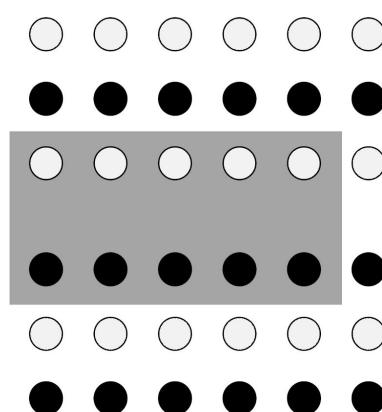
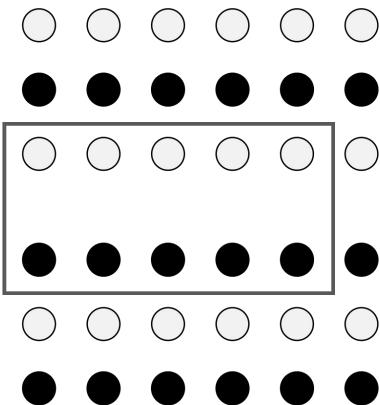
Principle of connection

- Connected objects are perceived to form a group
- Stronger than proximity and similarity
- Consider carefully when to use line graph vs. scatter plot



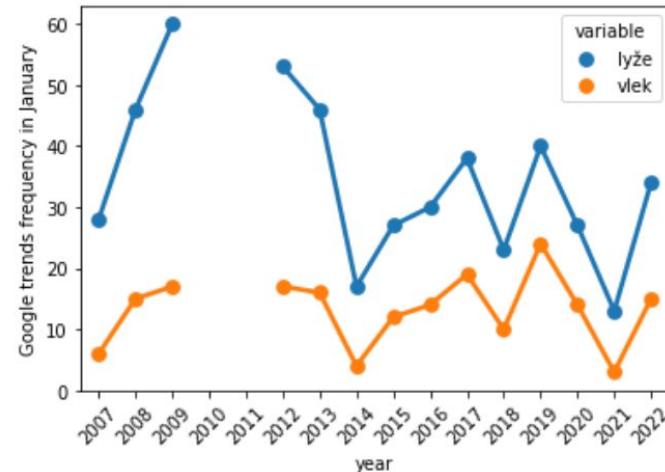
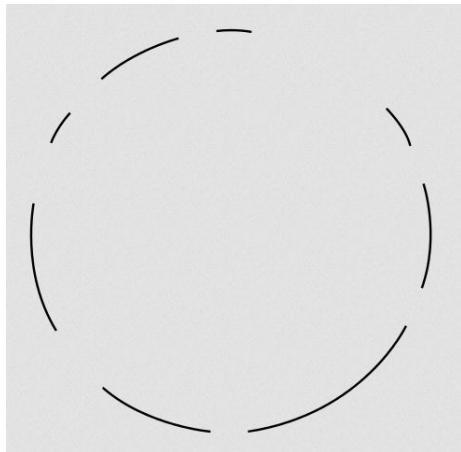
Principle of enclosure

- Enclosed objects are perceived as a member of the group
- Stronger than proximity and similarity
- Useful for highlighting in plots; little is enough (e.g. light background)



Principle of closure

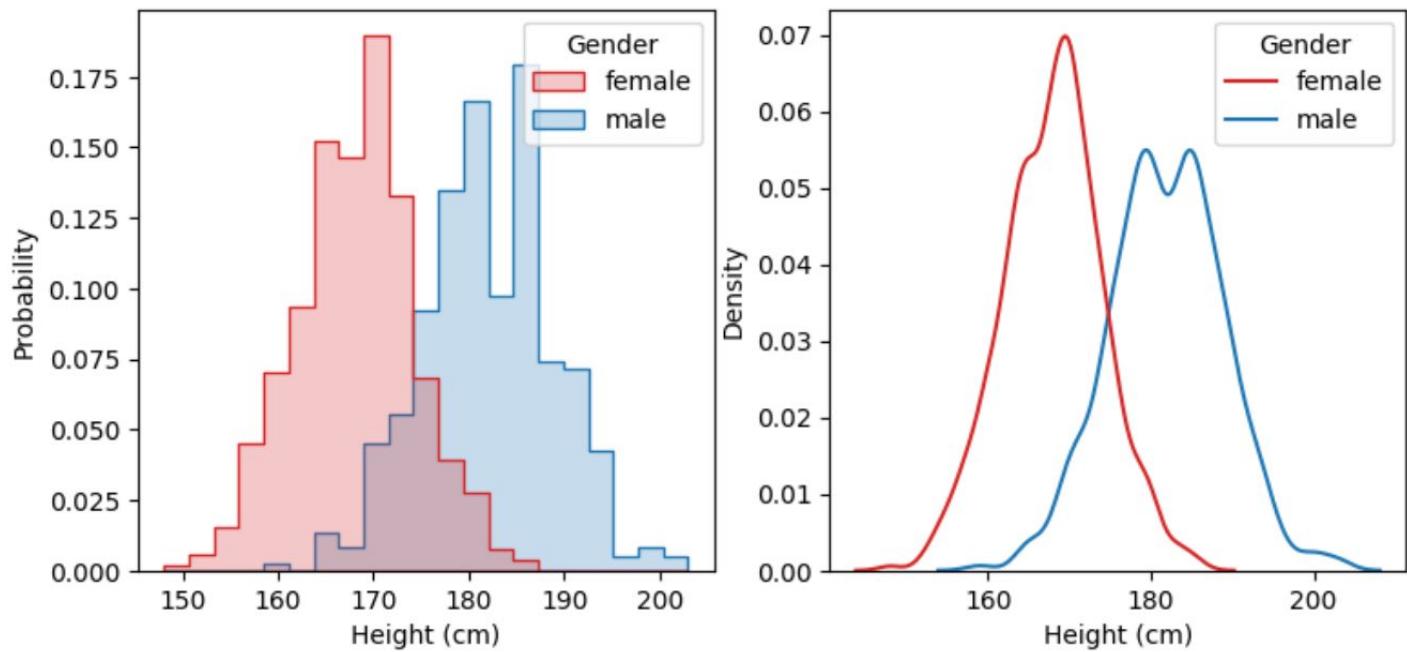
- Our brain fills gaps in figures, connects interrupted lines
- Useful / dangerous when interruptions by design



https://commons.wikimedia.org/wiki/File:Gestalt_closure.svg

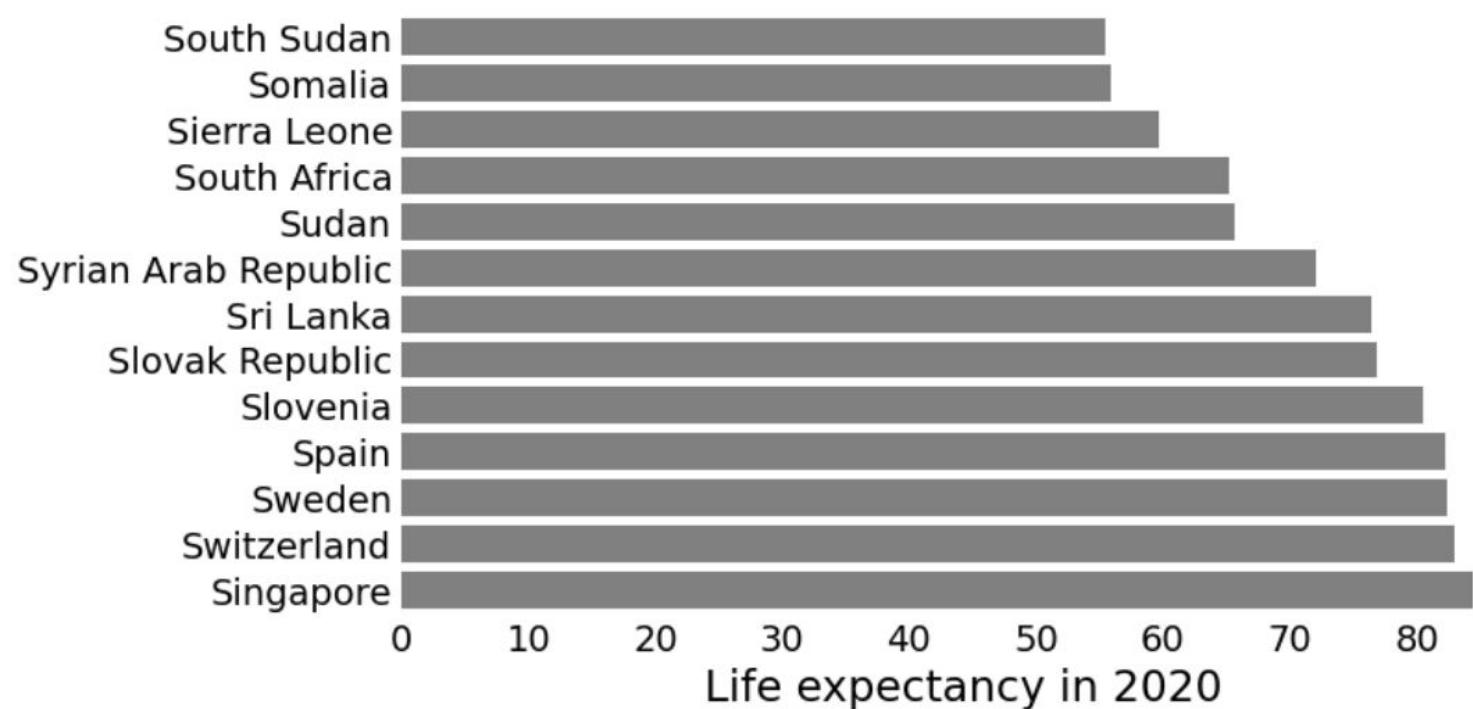
Principle of continuity

Smooth lines are easier to follow than angular and sharp



Frames not necessary, gestalt principles fills them in

(principles of closure and continuity)

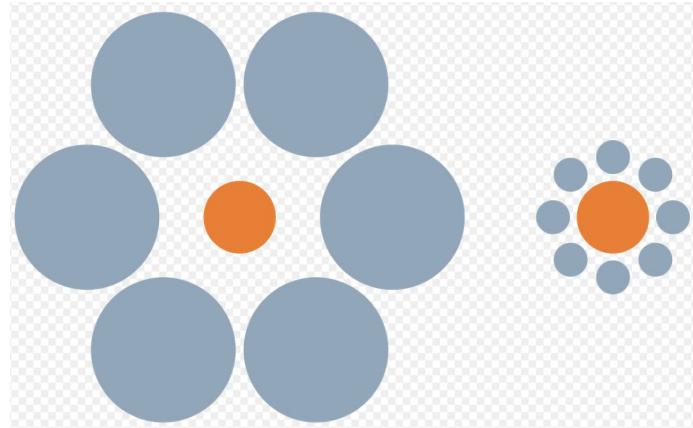
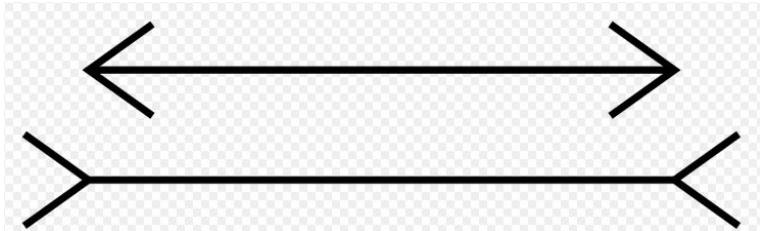


Illusions

- Fast visual processing leads to errors
- These are demonstrated by many optical illusions
- Beware not to create illusions in your plots

Illusions: length and size

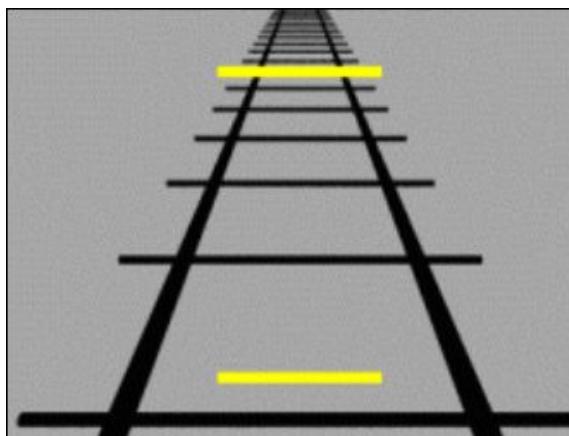
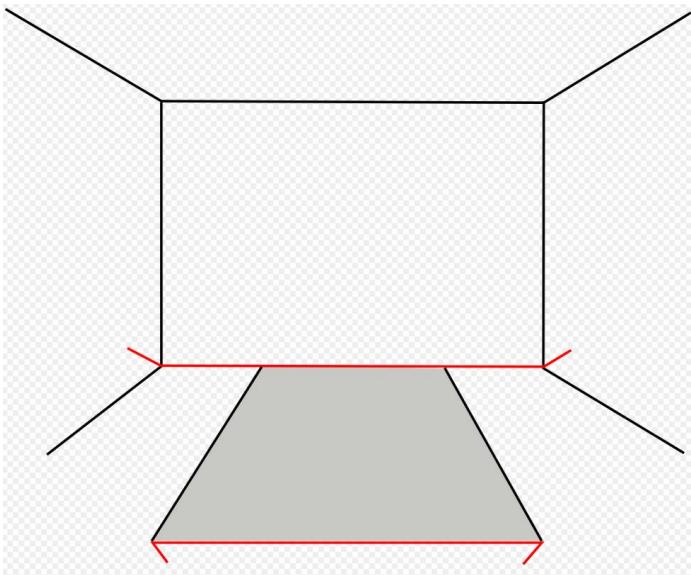
Müller-Lyer and Ebbinghaus illusions



https://commons.wikimedia.org/wiki/File:M%C3%BCller-Lyer_illusion.svg

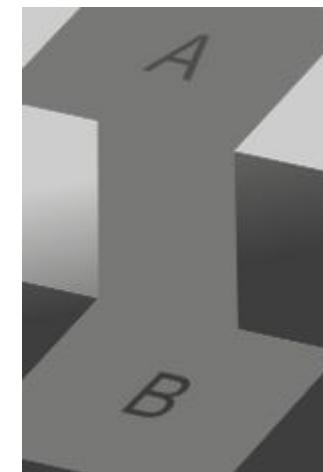
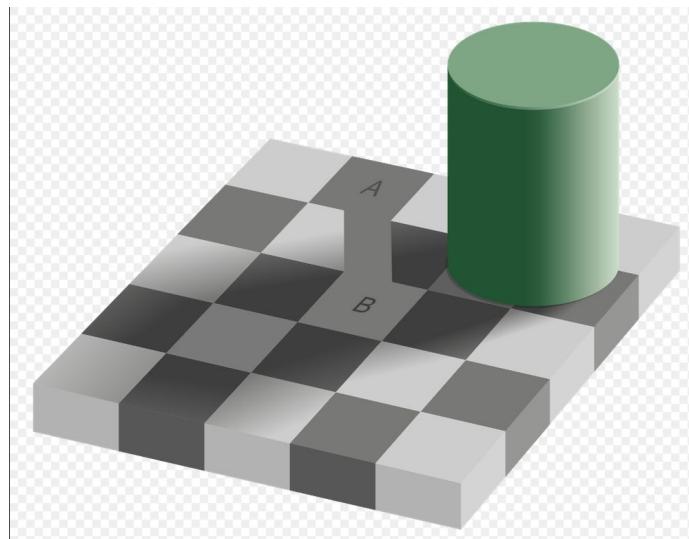
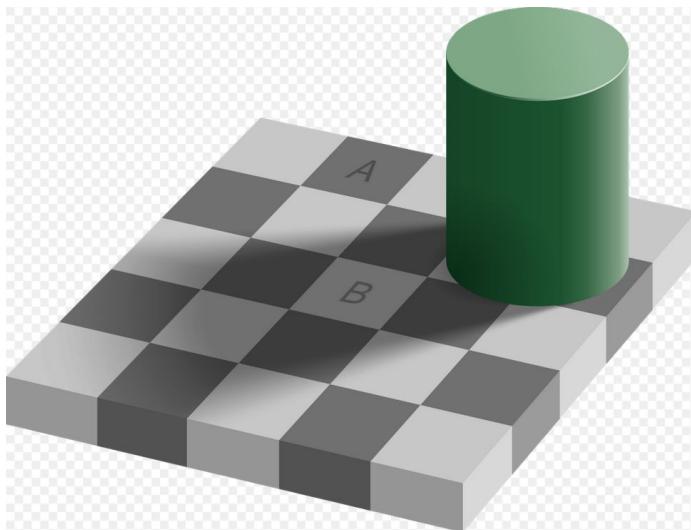
<https://commons.wikimedia.org/wiki/File:Mond-vergleich.svg>

Illusions: length, perspective, spatial compensation



https://commons.wikimedia.org/wiki/File:Mueller_Lyer.svg
https://commons.wikimedia.org/wiki/File:Ponzo_illusion.gif

Illusions: color

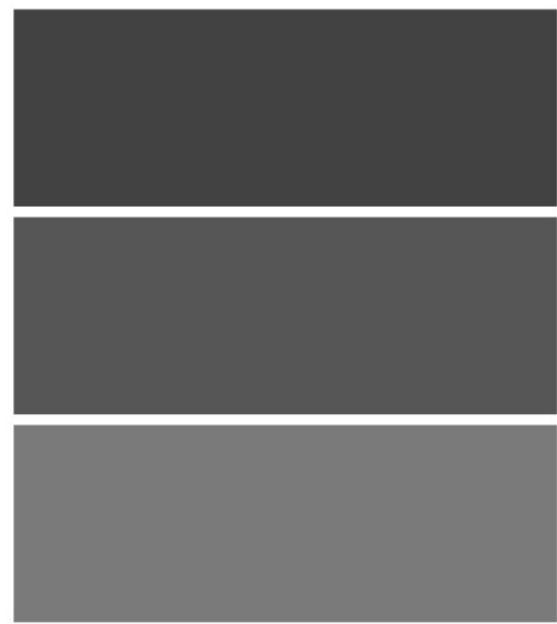


https://en.wikipedia.org/wiki/File:Checker_shadow_illusion.svg

https://commons.wikimedia.org/wiki/File:Grey_square_optical_illusion_proof2.svg

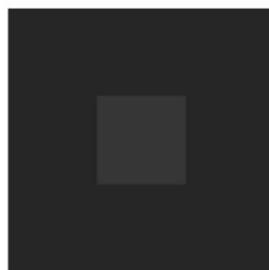
Illusions: color

Mach bands: when bands touch, the edge effect exaggerates their difference



Illusions: color

In heatmap the perception of colors influenced by their surroundings



Working memory

- **Iconic memory:** extremely short-term (<1s), simple pre-attentive processing
 - **Visual short-term memory:** many seconds, but very small capacity (only 3-5 items)
 - **Long-term memory:** store and recall selected information

Since working memory is small, looking at a plot with many colors requires back-and-forth between legend and plot

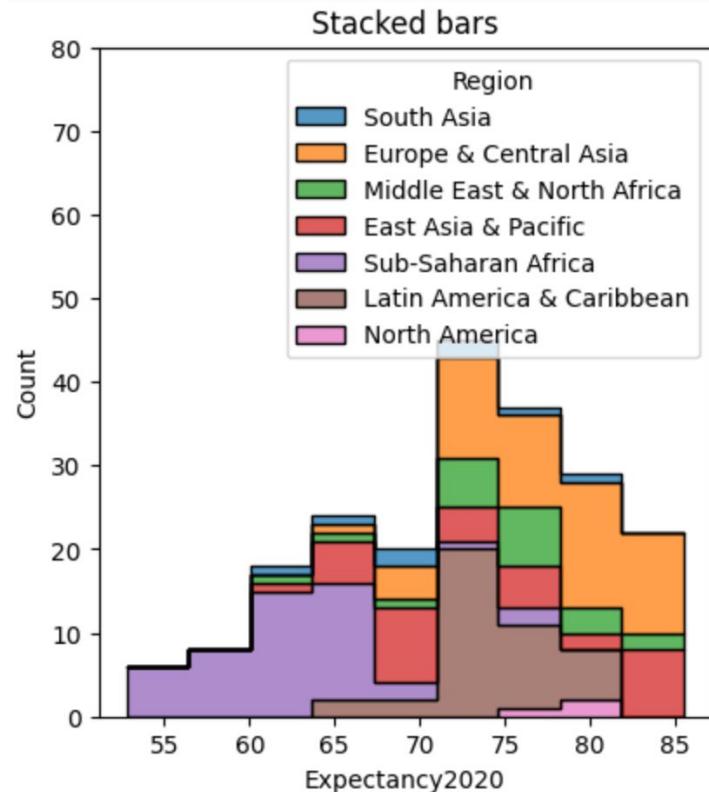


Chart and table junk

- **Chart junk:** elements of plots not necessary to convey information
- They unhelpfully catch our attention through pre-attentive attributes
- Most visualization can be improved by simplification
- Some redundancy can be useful

Nice visualizations of the simplification process:

- <https://www.darkhorseanalytics.com/blog/data-looks-better-naked>
- Also tables, maps and the unpopular pie charts

Summary

- **Pre-attentive attributes** are processed by our brains very fast
- Choosing the right attributes from the **hierarchy** allows accurate quantification
- Principles of **gestalt** describe how the brain connects part to the whole
- The brain can also make errors in visual processing as seen in **illusions**
- Removing **chart junk** concentrates our attention to the important elements

Additional sources

- [Utilizing Gestalt Principles to Improve Your Data Visualization Design](#)
- <http://daydreamingnumbers.com/blog/gestalt-laws-data-visualization/>
- Albert Cairo: The Functional Art
- C.N. Knaflc: Storytelling with Data
- Stephen Few: Now You See it

Visualizing text data

Visualizing text data

Working with natural text is difficult

- Complex grammar, ambiguous meaning, synonyms, etc.
- Lot of machine learning research
- Nonetheless sometimes simple statistics on frequencies of words or groups of words can be useful
- Usually we remove *stop words* (frequent words such as "and", "is"...) and apply *lemmatization* (convert inflected words to canonical form, such as "seen" -> "see")

Word clouds

State of the Union Address, 2002 vs. 2011



https://commons.wikimedia.org/wiki/File:State_of_the_union_word_clouds.png

President Bush, January 29, 2002

President Obama, January 25, 2011

Word clouds

- Display the most common words from a text
- Size of words grows with frequency
- Arranged to be visually pleasing
- Not the best option for understanding/comparing word frequencies
- You can also display word frequencies using **bar graphs** and other plot types

Tag cloud

- Endings of German city names typical for individual regions
 - Combination of a word cloud and map
 - Figure from [Reckziegel et al 2018](#)

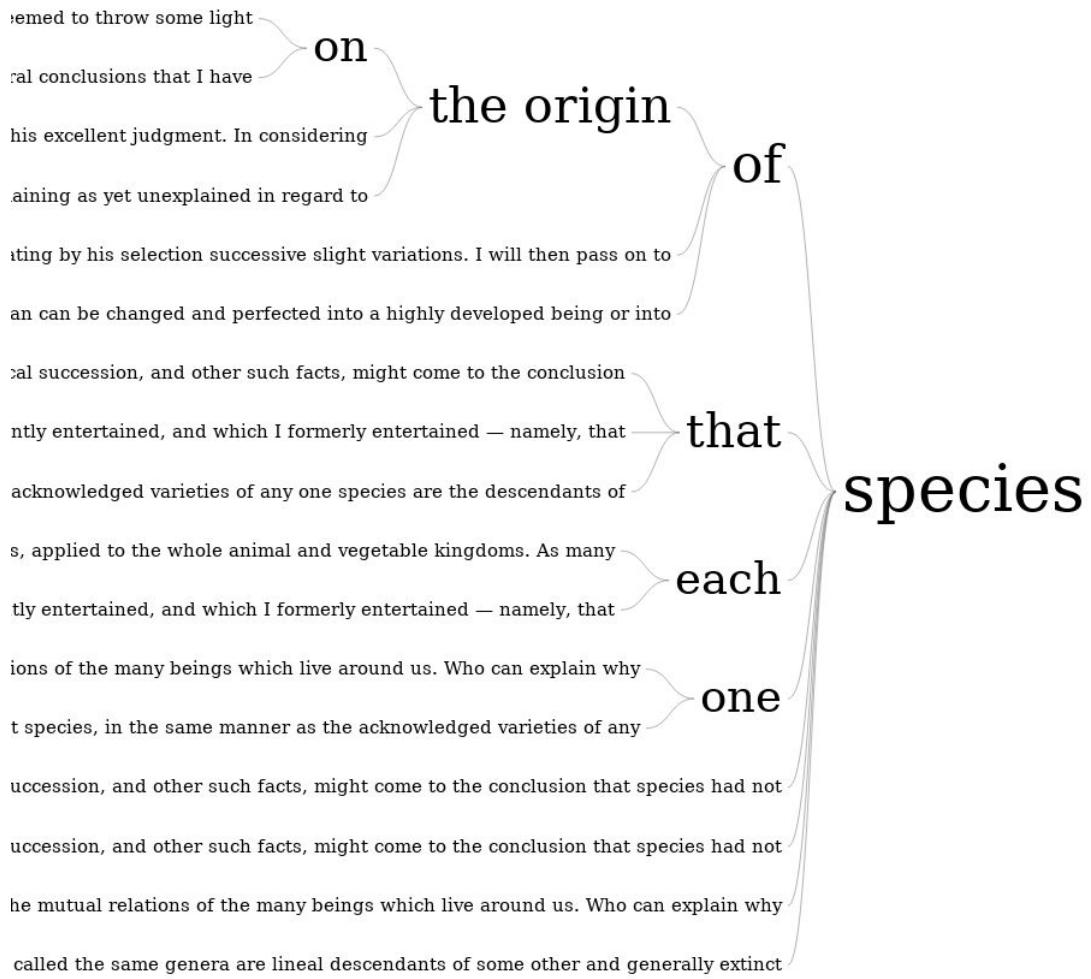


Word tree

Shows with words most often follow or precede a given word using a hierarchy

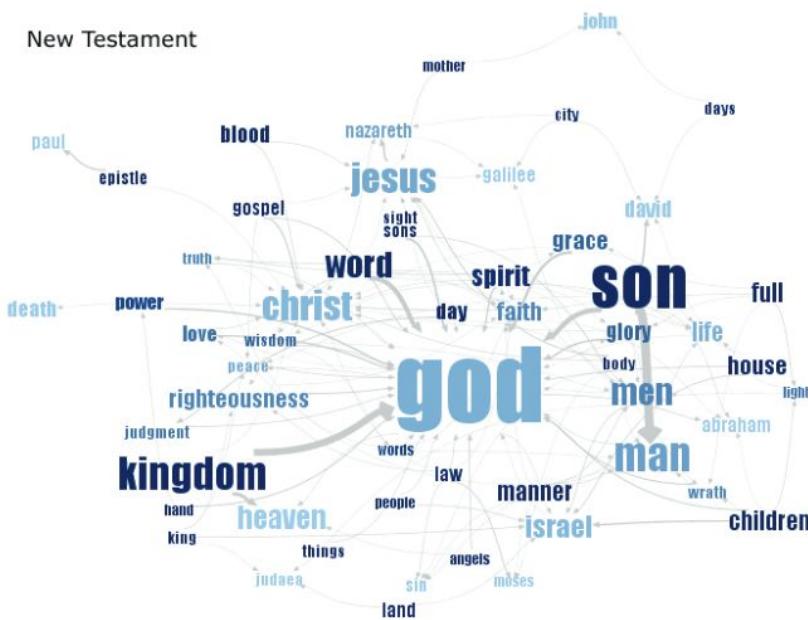
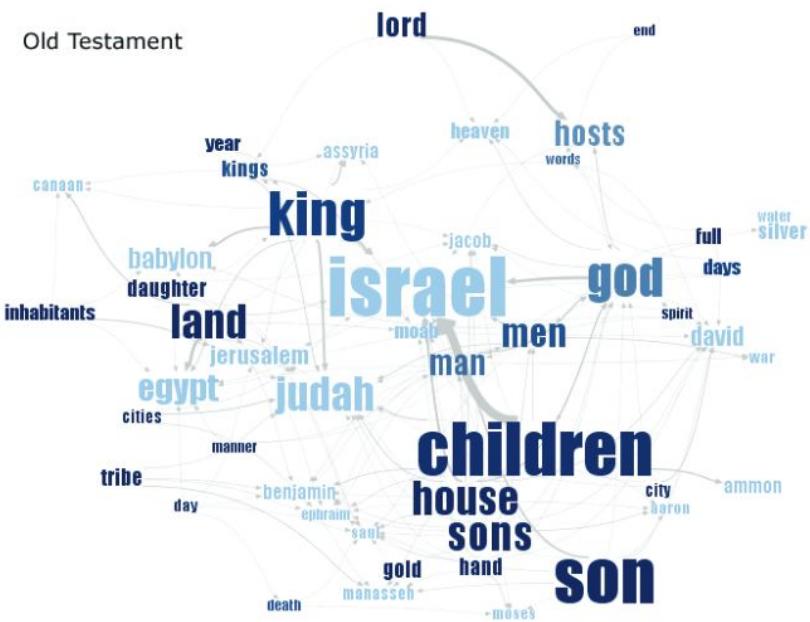
Text: [Introduction](#) to The Origin of Species by Charles Darwin, 1859, 1872

[Figure source](#)



Phrase nets

Phrases of type "X of Y", X connected to Y in a graph; source [van Ham et al 2009](#)



Text visualization: additional sources

- Courses Data management (2L), Principles of Data Science (3Z)
- Text visualization browser <https://textvis.lnu.se/>
- [Lecture from Univ. of Washington](#)
- [Drawing Elena Ferrante's Profile](#): Finding out who is Elena Ferrante, bestselling Italian author (*My Brilliant Friend*) by comparing word frequencies etc. (see e.g. page 100)

Lecture 10

Presentation of results

Data visualization · 1-DAV-105

Lecture by Broňa Brejová

Acknowledgement: materials inspired by lectures from Martina Bátorová in 2021

Data analysis project phases

Recall from L08: Data analysis project phases

- Obtaining data
- Data preprocessing, **checking**, cleaning
- **Exploratory** analysis
- Formation of **hypotheses**
- Testing hypotheses
- **Explanatory** visualizations for the final report / presentation

Details: obtaining data

- Obtaining data
 - This course: we download whole datasets in a tabular form
 - But often also web scraping, manual collection of data, measurements, surveys,...
 - Requires careful planning
- Data preprocessing, **checking**, cleaning
- **Exploratory** analysis
- Formation of **hypotheses**
- Testing hypotheses
- **Explanatory** visualizations for the final report / presentation

Details: preprocessing data

- Obtaining data
- Data preprocessing, **checking**, cleaning
 - Try to understand how (and why) the data was obtained and processed
 - Convert them to a convenient format
 - Check for missing values and suspicious outliers
 - Very important phrase: "Garbage in, garbage out"
- **Exploratory** analysis
- Formation of **hypotheses**
- Testing hypotheses
- **Explanatory** visualizations for the final report / presentation

Details: exploratory analysis

- Obtaining data
- Data preprocessing, **checking**, cleaning
- **Exploratory** analysis
 - Try many analyses
 - This course: visualizations and simple statistics
 - Later you learn advanced statistical and machine learning models
 - Less successful attempts may suggest new directions
- Formation of **hypotheses**
- Testing hypotheses
- **Explanatory** visualizations for the final report / presentation

Details: Formation of hypotheses

- Obtaining data
- Data preprocessing, **checking**, cleaning
- **Exploratory** analysis
- Formation of **hypotheses**
 - Select visualizations showing interesting trends / exceptions in the data
 - Formulate possible relationships
(but remember, correlation does not imply causation)
- Testing hypotheses
- **Explanatory** visualizations for the final report / presentation

Details: Testing hypotheses

- Obtaining data
- Data preprocessing, **checking**, cleaning
- **Exploratory** analysis
- Formation of **hypotheses**
- Testing hypotheses
 - Recheck your code and data, try other related analyses
 - Try to find other relevant data or existing analyses by other people
 - If important decisions will be based on your result,
test it particularly thoroughly
(what would happen if our plot was all wrong?)
- **Explanatory** visualizations for the final report / presentation

Details: Explanatory visualizations

- Obtaining data
- Data preprocessing, **checking**, cleaning
- **Exploratory** analysis
- Formation of **hypotheses**
- Testing hypotheses
- **Explanatory** visualizations for the final report / presentation
 - Formulate your conclusions
 - Support them with your analysis and visualizations
 - Do not include all exploratory analyses
(but do not hide data contradicting your conclusion)
 - Polish visualizations that you selected

Presentation of results

Presentation of results

- Understand **context**, audience, goals (more later)
- Tell a **story** (more later)
- Choose appropriate **visuals** (text / table / chart, appropriate type of graph, pre-attentive attributes, hierarchy of graph elements)
- Eliminate clutter, **focus attention** on the main points (pre-attentive attributes, such as color, size, spacing)
- Pay attention to **design** (accessibility due to font size and colors, aesthetics...)
- Get **feedback** and a lot of **practice**

(see Cole Nussbaumer Knaflic: Storytelling with data)

Understand the context of your presentation

Before writing any text or preparing any presentation try to find out:

- Who is your expected audience?
- What do they know and what do you need to explain?
- What might be interesting / new for them?
- What is the medium (live presentation, video, printed text, website)?
- What is the appropriate length (time, number of pages)?
- What do you want to achieve by the presentation?
(inform / entertain / inspire to take a specific action)

Examples

Try to list some examples of situations where data visualization might be presented: who are speakers and audiences, what are goals

Situations where data visualizations are presented

- A **company** presents to potential **consumers**, persuades them to **buy** their products
- A **charity** presents to general **public**, persuades them to **donate**
- A **nonprofit / government** present to general **public**, persuades them to take **action** (live healthily, protect environment, ...)
- An **employee** presents to **colleagues**, persuades them to **change** processes
- A **politician** presents to general **public**, persuades them to **vote** for something
- A **journalist** writes for general **public**, informs them about important **issues**
- A **teacher** presents to **students**, teaches them a given **topic**
- A **student** presents to a **teacher**, demonstrates his / her **achievements** and skills
- A speaker talks to general **public**, **entertains / informs** about interesting topics
- A speaker talks to **experts**, informs about **new discoveries**, technologies etc.

Presentation of results

- Understand context
- **Tell a story**
- Choose appropriate visuals
- Eliminate clutter, focus attention on the main points
- Get feedback and a lot of practice

Storytelling

- We are easily captivated by a good story (book, movie, play)
 - We do not want to interrupt reading / watching
 - We can recall the plot afterwards
 - We want to achieve similar effects by your presentation
- Traditional stories structured as basic plot - twists - ending
- This roughly corresponds to introduction, actual content, conclusion
- Repetition useful in stories as well as in presentation
- Suspense and surprise

(see Cole Nussbaumer Knaflic: Storytelling with data)

Storytelling: structuring presentation

- One option is to describe your process of discovery roughly **chronologically** (omitting some dead ends): identifying question, getting data, analyzing data, coming to conclusion, recommending action
- Another option is to **lead with the ending**: starting with a call to action, backing it up with data

(see Cole Nussbaumer Knaflic: Storytelling with data)

Cognitive biases

Cognitive bias (kognitívne skreslenie)

- Cognitive bias is a systematic deviation from rational judgement
- A brain mechanism to create shortcuts, allow fast reasoning
- Term introduced by Amos Tversky and Daniel Kahneman in 1972

Very long list of biases discovered by researchers:

[https://commons.wikimedia.org/wiki/File:The_Cognitive_Bias_Codex_-_180%2B_biases,_designed_by_John_Manooian_III_\(jm3\).png](https://commons.wikimedia.org/wiki/File:The_Cognitive_Bias_Codex_-_180%2B_biases,_designed_by_John_Manooian_III_(jm3).png)

Three cognitive biases

- **Patternicity bias:** See non-existent patterns in data, even in random noise (related to seeing faces in the clouds)
- **Storytelling bias:** Invent "stories", explanations, cause-effect relationships for these patterns
- **Confirmation bias:** It is hard to discard our beliefs. We search for evidence that back our theories and interpret contradicting evidence the opposite way.

See Alberto Cairo: The Truthful Art

Cognitive biases in analysis and presentation

- Beware of biases in yourselves during analysis and in your audience during presentation
- *"The first principle is that you must not fool yourself---and you are the easiest person to fool"* Richard Feynman

Do not oversimplify

Story from Alberto Cairo: The Truthful Art

"Study finds that more than a quarter journalism grads wish they'd chosen a different career" Poynter Institute, 2013

Storytelling bias suggests:

- A change from printed to online media leads to worse job market for journalists
- Cairo as a journalism professor starts to worry about his future

Journalism grads (cont.)

"Study finds that more than a quarter journalism grads wish they'd chosen a different career" Poynter Institute, 2013

Actual value is 28%, as found by a [survey](#)

- This value by itself is presumably correct
- However it is not put into perspective, compared with other values

Results of Cairo's investigation

- The dissatisfaction among journalism students did not change much over the years
- Decreases in the number of news reporters and their low salaries
- Survey results imply sampling error which should be considered
- (Ideally compare to grads from other fields)

He suggests reformulating the message of the story:

"Even if jobs prospects for journalists have worsened substantially and they may worsen even further in the future, the percentage of grads who wish they'd chosen a different career hasn't changed at all in more than a decade."

Properties of good visualization

- **Truthful** (based on thorough and honest research, high quality data, appropriate analysis, correct math, no bugs in code)
- **Functional** (constitutes an accurate depiction of the data, allows meaningful comparisons)
- **Beautiful** (attractive, intriguing, aesthetically pleasing for target audience)
- **Insightful** (reveals evidence hard to see otherwise)
- **Enlightening** (changes our minds for the better)

Alberto Cairo: The Truthful Art (journalist's perspective)

Back to thoughts on good visualization

Last lecture

Pre-attentive attributes are quickly recognized by our brain (size, color, position,...)

Hierarchy of graph elements: not all attributes are good for accurate quantitative reasoning

Gestalt principles: how brain connects elements into larger patterns (proximity, similarity, connection, enclosure, closure, continuity,)

Errors in visual processing lead to **illusions**

This informs our chart type choice (bars vs pies) and elimination of chart junk

Additional aspects of good plot choice

Basic setup: Selecting variables, choosing type of plot, assigning variables to x, y, color...

Data transformations: filtering (e.g. select data from one region), aggregating (e.g. summary per region) to avoid overplotting

Additional settings: sorting (e.g. bar graph columns), rescaling (log axis), re-expressing (e.g. absolute value vs relative change), zooming

Focus and explanation: highlighting, annotating (adding notes to plot)

Inspired by Stephen Few: Now you see it

Speed is not always everything

While there is a place for rapidly-understood graphs, it is too limiting to make speed a requirement in science and technology, where the use of graphs ranges from detailed in-depth data analysis to quick presentation. [...]

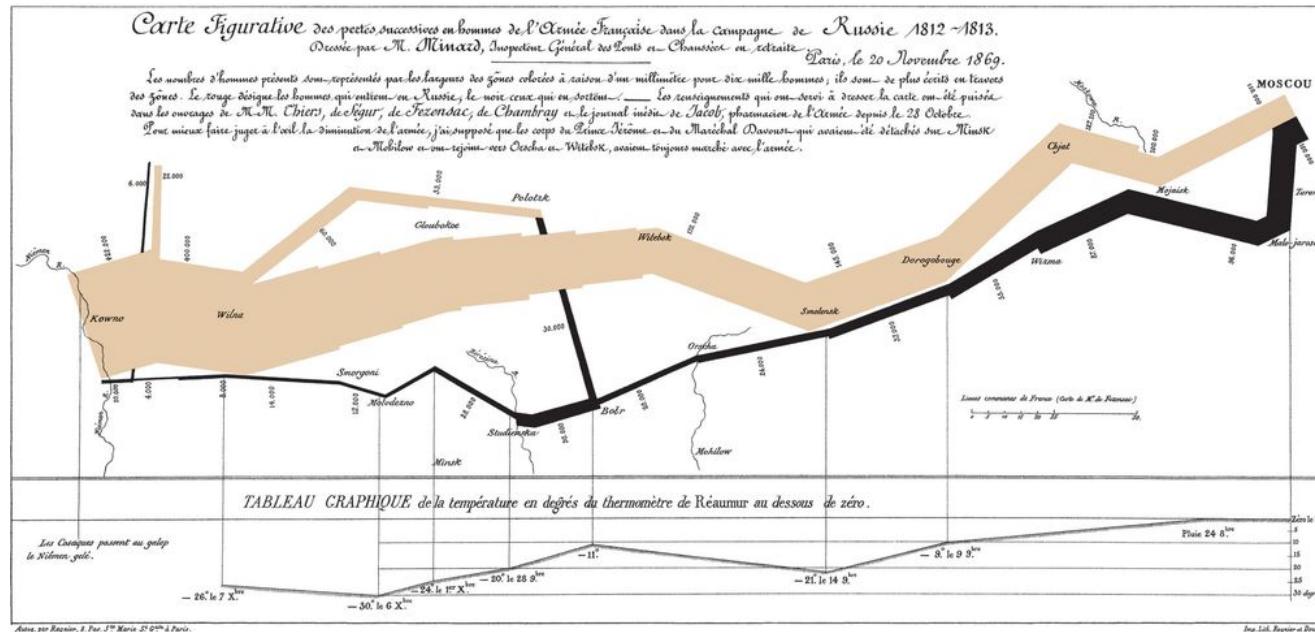
The important criterion for a graph is not simply how fast we can see a result; rather it is whether through the use of the graph we can see something that would have been harder to see otherwise or that could not have been seen at all.

William Cleveland, The Elements of Graphing Data, Chapter 2

Recall: exploratory vs. explanatory analysis, sometimes audience can explore too

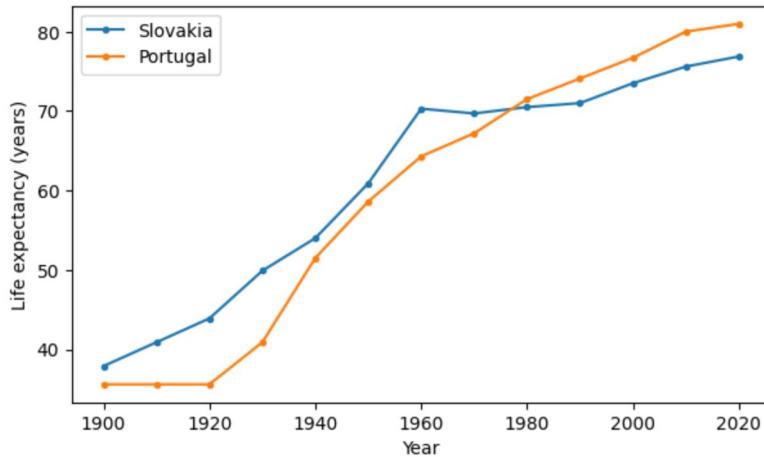
Recall Minard's plot of French army losses

Easy to see big picture but also many minute details



Tables vs. graphs

When is it good to include a table instead of / in addition to a graph?



| | 1900 | 1910 | 1920 | 1930 | 1940 | 1950 | 1960 | 1970 | 1980 | 1990 | 2000 | 2010 | 2020 |
|----------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|-------------|
| Slovakia | 37.9 | 40.9 | 43.9 | 49.9 | 54.0 | 60.9 | 70.3 | 69.7 | 70.5 | 71.0 | 73.5 | 75.6 | 76.9 |
| Portugal | 35.6 | 35.6 | 35.6 | 40.9 | 51.5 | 58.6 | 64.3 | 67.2 | 71.5 | 74.1 | 76.7 | 80.0 | 81.0 |

Tables vs. graphs

Advantages of tables:

- **Very few numbers** typically better given directly than in a graph
- In a long table, each reader can **find items** of personal interest (e.g. results of a sport competition, statistics for all countries)
- A table gives **exact values**
- Readers can **re-analyze** the same data (table preferably machine-readable)
- Numbers at very **different scales** are sometimes difficult to display even with log axes

See also

<https://www.storytellingwithdata.com/blog/2011/11/visual-battle-table-vs-graph>

Examples of bad graphs and their improvements

- <http://www.perceptualedge.com/examples.php>
- <https://eagereyes.org/pie-charts>
- <https://viz.wtf/>

Infographics

Some examples of infographics

Several examples that are close to data visualization:

- Income by religious group in US ([image](#), [website](#))
- Deadliest pandemics ([website](#))
- War casualties ([website](#))
- Game of Thrones relationships ([website](#))
- Emergency medical services in Slovakia 2019 ([website](#))

Some explain other types of information:

- Sitting and standing is bad ([website](#))

Data visualization (DV) vs infographics (IG)

- **Target audience:** IG general public, DV often experts
- **Storytelling:** often in IG, can be created from multiple DV
- **Design and aesthetics:** more elaborate in IG, includes graphics elements and clipart (considered chart junk in DV)
- **Process of creation:** many simple tools for DV, IG time consuming, often created by collaboration of data analysis, domain experts and graphic designers

<https://www.statsilk.com/blog/real-difference-between-infographics-and-data-visualizations>

1 Lecture 11: Infographics, interactivity, other tools, specialized plots

Data Visualization · 1-DAV-105

Lecture by Broňa Brejová

Acknowledgement: some materials inspired by lectures from Martina Bátorová in 2021

1.0.1 Several examples of infographics

Several examples that are close to data visualization:

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1.2 Interactivity

Interactive visualization engages audience, allows them to explore data in depth and according to their interest.

1.2.1 Examples

- PhD gender gap ([website](#))
- Making it big ([website](#))
- US cities with the same name ([website](#))

1.2.2 Techniques in interactivity visualization

Similar to decisions made in designing a static plot:

- Selecting variables (x, y, color, ...)
- Filtering data (selecting table rows)
- Highlighting points or groups

- Aggregating (display countries or region summaries)
- Zooming / panning
- Rescaling (log-scale) / reexpressing (e.g. % instead of counts)
- Sorting (e.g. bars in bargraphs)
- Displaying details (tooltips)
- Annotating
- Bookmarking

(Stephen Few)

1.2.3 Dashboard

- A display consisting of multiple plots, summarizing current state of important indicators (e.g. of a business, pandemics, ...)
- Inspired by dashboards in cars and planes
- Often interactive, but main features in default view

Two SARS-CoV-2 examples:

- [WHO](#)
- [Nextstrain](#)
 - many options: selecting color, filtering, highlighting, aggregating, zooming and panning (maps and tree), rescaling (time vs divergence), tooltips, bookmarking

1.2.4 Interactivity in Plotly Express

All Plotly plots by default have some interactivity:

- Filtering groups
- Zooming / panning
- [Details](#)
- Spike lines

Example 1: Country indicators from World Bank, <https://databank.worldbank.org/home> under CC BY 4.0 license.

Regions can be switched on and off.

```
[1]: import plotly.express as px
import pandas as pd
url = 'http://compbio.fmph.uniba.sk/vyuka/viz/images/9/9d/World_bank.csv'
countries = pd.read_csv(url)

px.scatter(
    countries, x="GDP2018", y="Expectancy2018", color="Region",
    hover_data=['Country'],
    title="Country indicators 2018", log_x=True,
    width=800, height=500
)
```

Example 2: Life expectancy data provided free by the [Gapminder foundation](#) under the CC-BY license.

Compare data along the x coordinate.

```
[2]: url="http://compbio.fmph.uniba.sk/vyuka/viz/images/3/33/
      ↪Gapminder_life_expectancy_years.csv"
orig_expectancy = pd.read_csv(url)
expectancy = pd.melt(orig_expectancy, id_vars=["country"], var_name="year")
expectancy['year'] = expectancy['year'].astype(int)

[3]: selected = expectancy.query("country=='Slovak Republic' or country=='France'")
fig=px.line(
    selected, x="year", y="value", color="country",
    title="Life expectancy", width=800, height=500
)
fig.update_layout(hovermode="x unified")
```

1.2.5 More interaction with Dash by Plotly

- Dash library by Plotly allows adding control elements (selectors, sliders, buttons, ...)
- We have seen an example in L01

1.3 Other visualization tools

Non-programmers typically create plots in spreadsheets:

- Excel ([examples](#))
- Google sheets ([examples](#))

System R: programming language for statistical computing

- Together with Python, very popular in data science
- Built-in plots
- Also other libraries, notably `ggplot2` based on system called Grammar of Graphics ([cheat-sheet](#))

Javascript

- Programming language popular in web programming
- Google charts for Javascript ([examples](#))
- `D3.js` library (Data-Driven Documents)

Tableau

- Advanced visualization tools, commercial
- [Gallery](#)

Microsoft Power BI

- Interactive data visualization software with a focus on business intelligence
- An [example](#)

1.4 Several specialized visualization types

1.4.1 UML diagrams in computer science

- Display relationships between different classes or other components and aspects of software

https://commons.wikimedia.org/wiki/File:UML_diagrams_overview.svg Derfel73; Pmerson

1.4.2 Waterfall chart

- Used in business analysis: financial, inventory, human resources etc.
- Displays effects decreasing or increasing a given value
- The first and last columns are bars displaying starting and final value
- Intermediate columns float, displaying changes from previous total
- [Description](#)

https://commons.wikimedia.org/wiki/File:Waterfallchart_ex2.jpg FusionCharts Blog, CC BY-SA 4.0

1.4.3 Funnel charts

- Display losses within a business process, e.g. from website visit to actual purchase
- Horizontal bar chart with centered bars
- Beware: different from [funnel plot](#) in medical meta-analyses of multiple publications

```
[4]: # example from https://plotly.com/python/funnel-charts/
data = dict(
    number=[39, 27.4, 20.6, 11, 2],
    stage=["Website visit", "Downloads", "Potential customers", "Requested price", "invoice sent"])
fig = px.funnel(data, x='number', y='stage')
fig.show()
```

1.4.4 Gantt chart

- Used in management to display project schedule with different tasks and their planned duration
- Can also display current status of tasks and their dependencies

<https://commons.wikimedia.org/wiki/File:GanttChartAnatomy.svg>

1.4.5 Candlestick chart

- Similar to boxplot, used in financial data, e.g. stocks, currency exchange rates
- Line: minimum and maximum, box: opening and close, color: increase or decrease

https://commons.wikimedia.org/wiki/File:Candlestick_Chart_in_MetaTrader_5.png