

For discussion

# How to Apportion Blame for a Queue with Arrivals in Bursts?

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# Roadmap

- Question
- Explanation of approach
- Explanation of parameter space
- Results
- Evaluation
- Interpretation
- Implications & Next steps

# Question

- How to apportion blame for a queue with arrivals in bursts?
- Only marking packets, with no flow state
- Arrivals in bursts can lead to a queue
  - even if they can be served on average
- Subsequent smoother arrivals sit behind the burst
  - with knock-on impact on the next arrivals
  - even after the initial burst has all departed

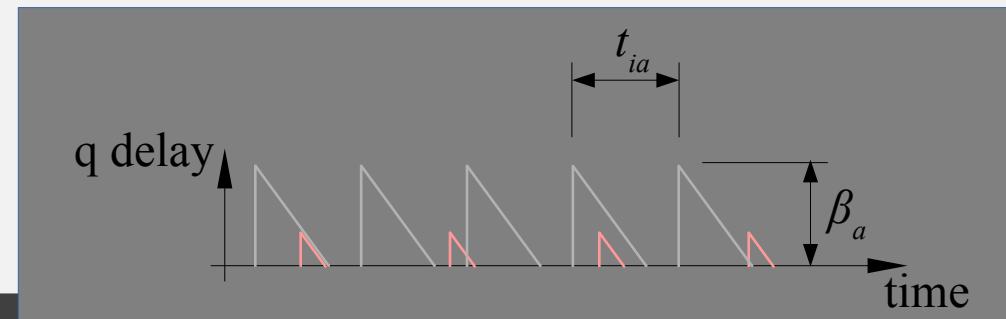
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\* may use flow state

# Approach

- Model? Simulate? Testbed?
  - model first: initial goal is understanding
  - noise of reality (packet sizing, timing dither, sync effects) could otherwise obstruct
- Unresponsive? Responsive?
  - unresponsive: cannot assume a response, so marking might solely drive policing\*
- Simplest sufficient scenario; 2 flows,  $a$  &  $b$ , with:
  - constant but different burst sizes,  $\beta$
  - constant but different capacity shares,  $\lambda$
  - No need for either to vary (understand bursts first, not bursts of bursts)
- Reduces to 2 (sawtooth) waves with different amplitude  $\beta$  & wavelength (interval  $t_i$ )
  - capacity share,  $\lambda = \beta / t_i$
  - any 1 of these 3 variables depends on the other 2

\* might use flow state



# Approach Normalized metrics

Goal: results applicable to any link rate and any step marking threshold delay

- Burst size  $\beta$  is in units of time (queue delay)
  - normalized to: marking threshold = 1 unit of time
- On time series plots, time is also normalized
  - queue delay at marking threshold = 1 unit of time
- Marking rate,  $\lambda p$ , is marked bits per unit time
  - normalized as a dimensionless fraction of link bit rate = 1
- Marking probability,  $p$ , and capacity share,  $\lambda$ 
  - both dimensionless and bounded within [0,1]
  - so normalized marking rate,  $\lambda p$ , also bounded within [0,1]
- Comparison metrics use difference,  $p_a - p_b = \Delta p$ , not ratio  $p_a/p_b$ 
  - not inflated as  $p_b \rightarrow 0$
  - for visualization, and irrespective of any congestion control assumptions

# Approach Parameter space

- A full scan of all 4 dimensions:

$$\beta_a, \lambda_a, \beta_b, \lambda_b$$

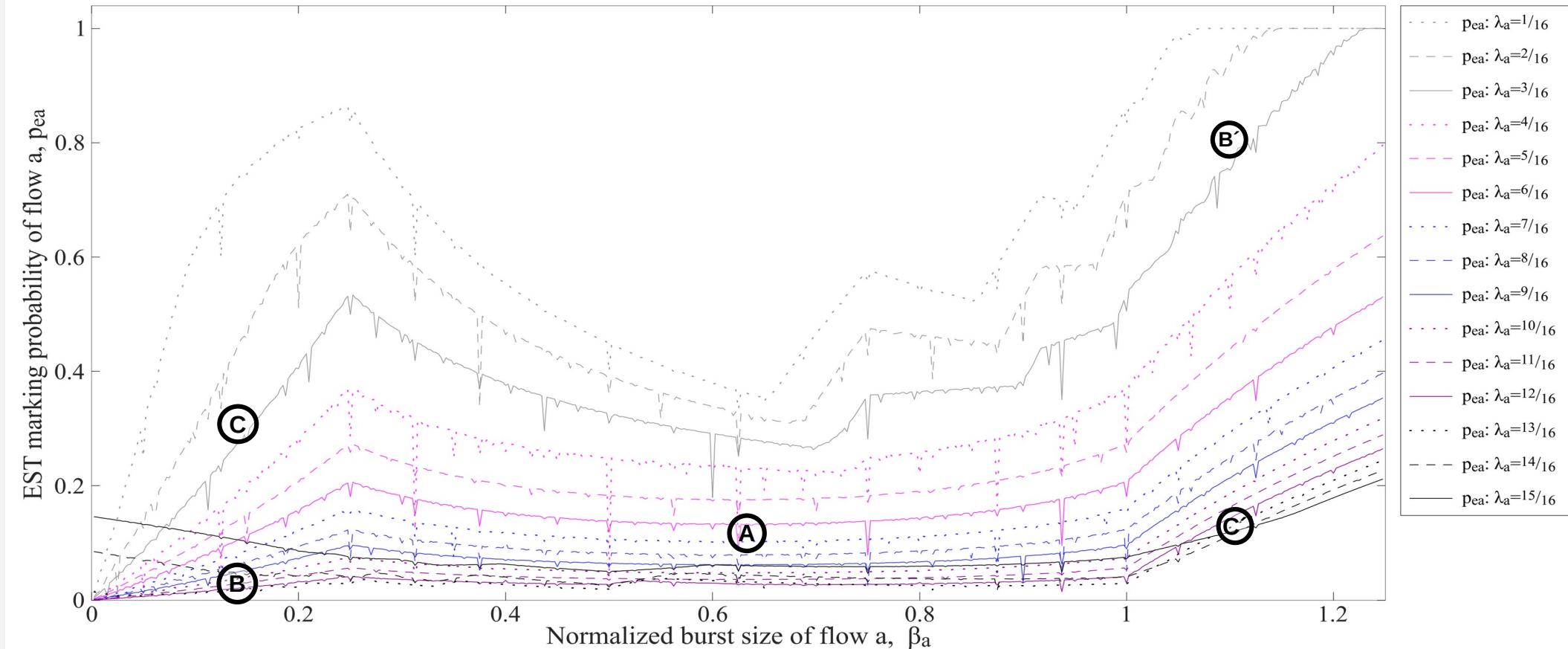
would generate more heat than light

- To focus on apportioning blame, scan the parameter space of one flow ( $\beta_a, \lambda_a$ ), while trying to keep the whole system constant, i.e.
  - constrain  $\Sigma\lambda$  (utilization) to a small selection of constants (assume  $\Sigma\lambda \leq 1$ )
  - constrain  $\Sigma\beta$  (max total burst) to a small selection of constants
- Compare two marking approaches, based on the q delay...
  - ...a packet itself experiences (the queue ahead at enqueue)
  - ...a packet causes to others (the queue behind at dequeue)

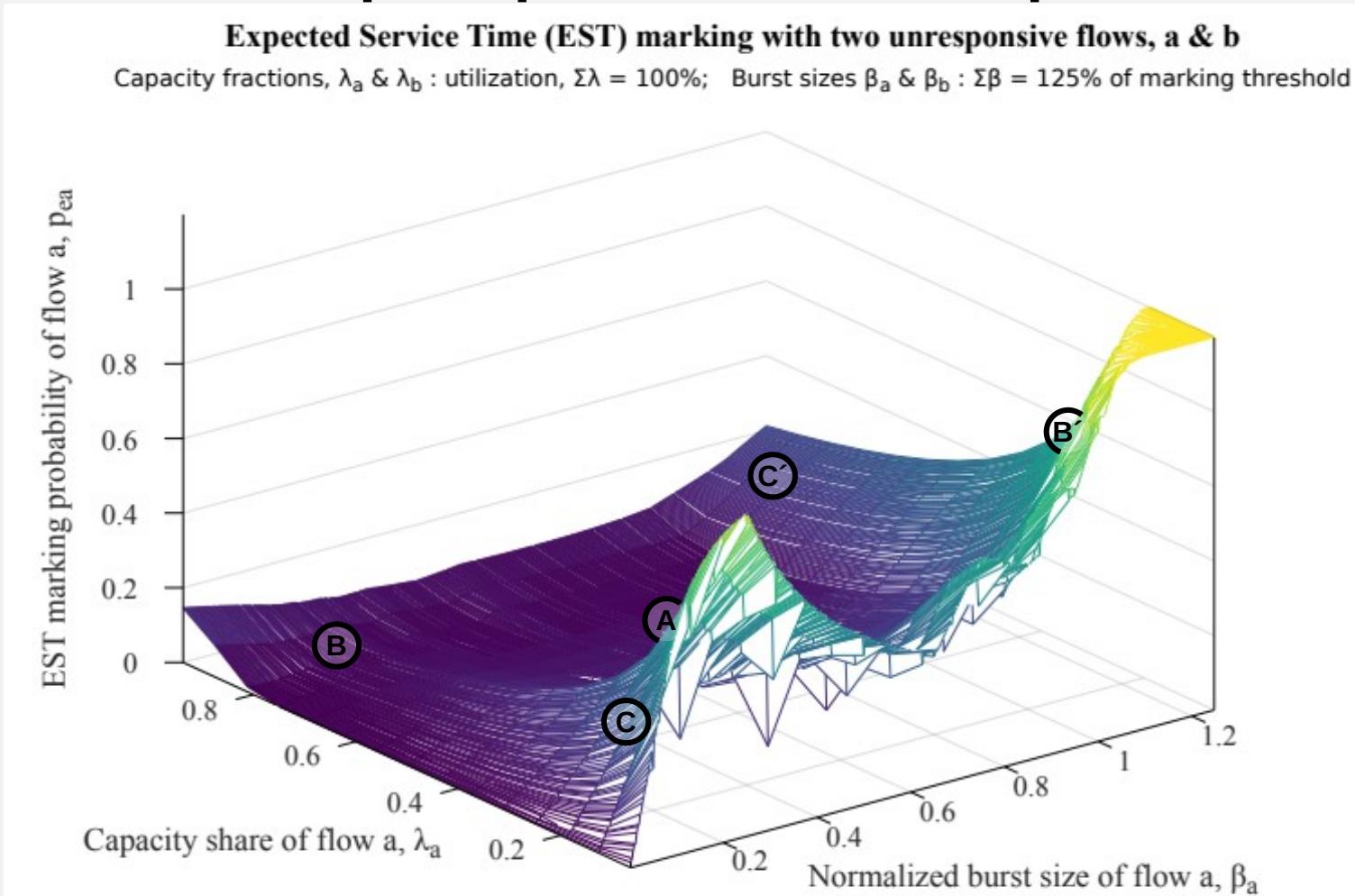
# How to Interpret the Parameter Space

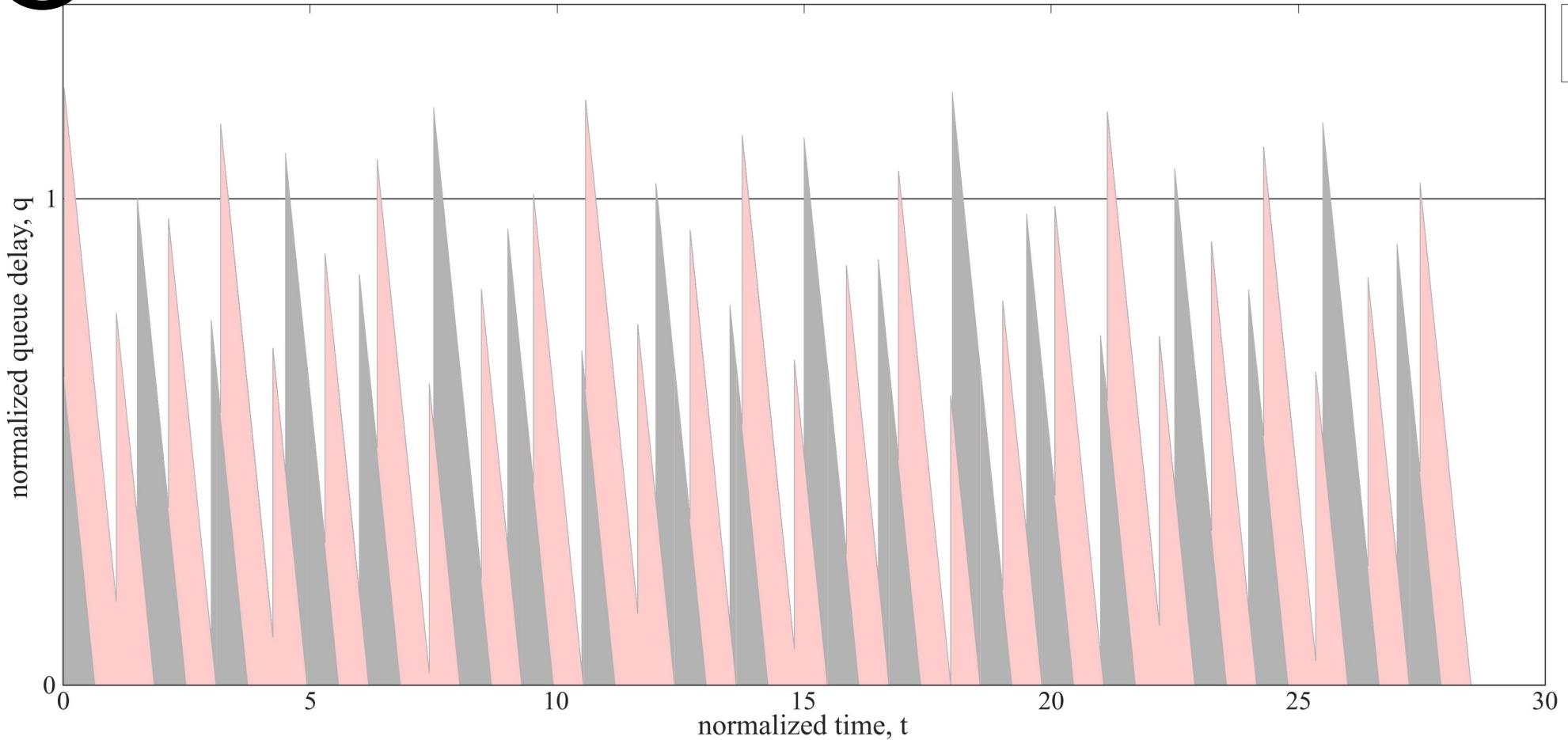
Expected Service Time (EST) marking with two unresponsive flows, a & b

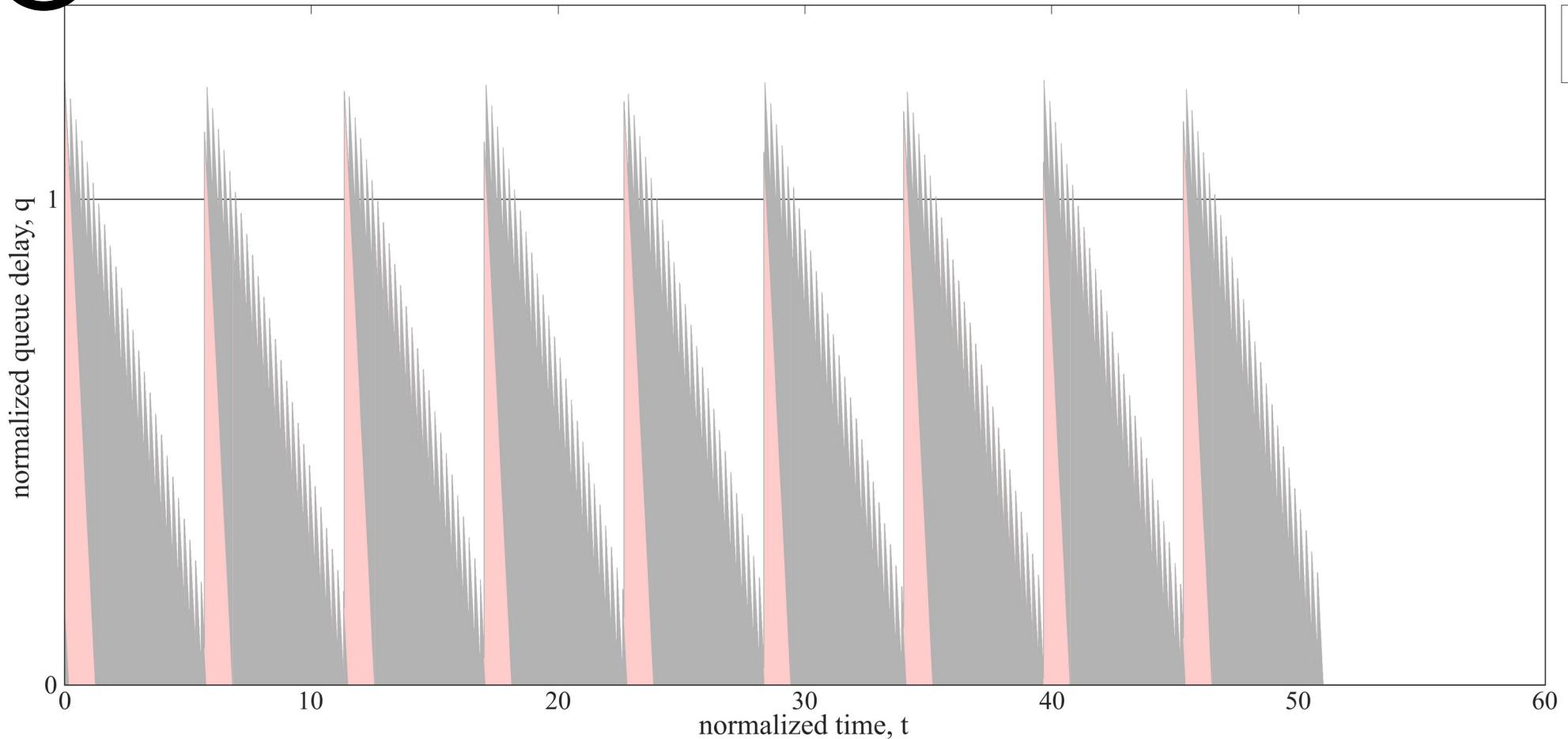
Capacity fractions,  $\lambda_a$  &  $\lambda_b$  : utilization,  $\Sigma\lambda = 100\%$ ; Burst sizes  $\beta_a$  &  $\beta_b$  :  $\Sigma\beta = 125\%$  of marking threshold

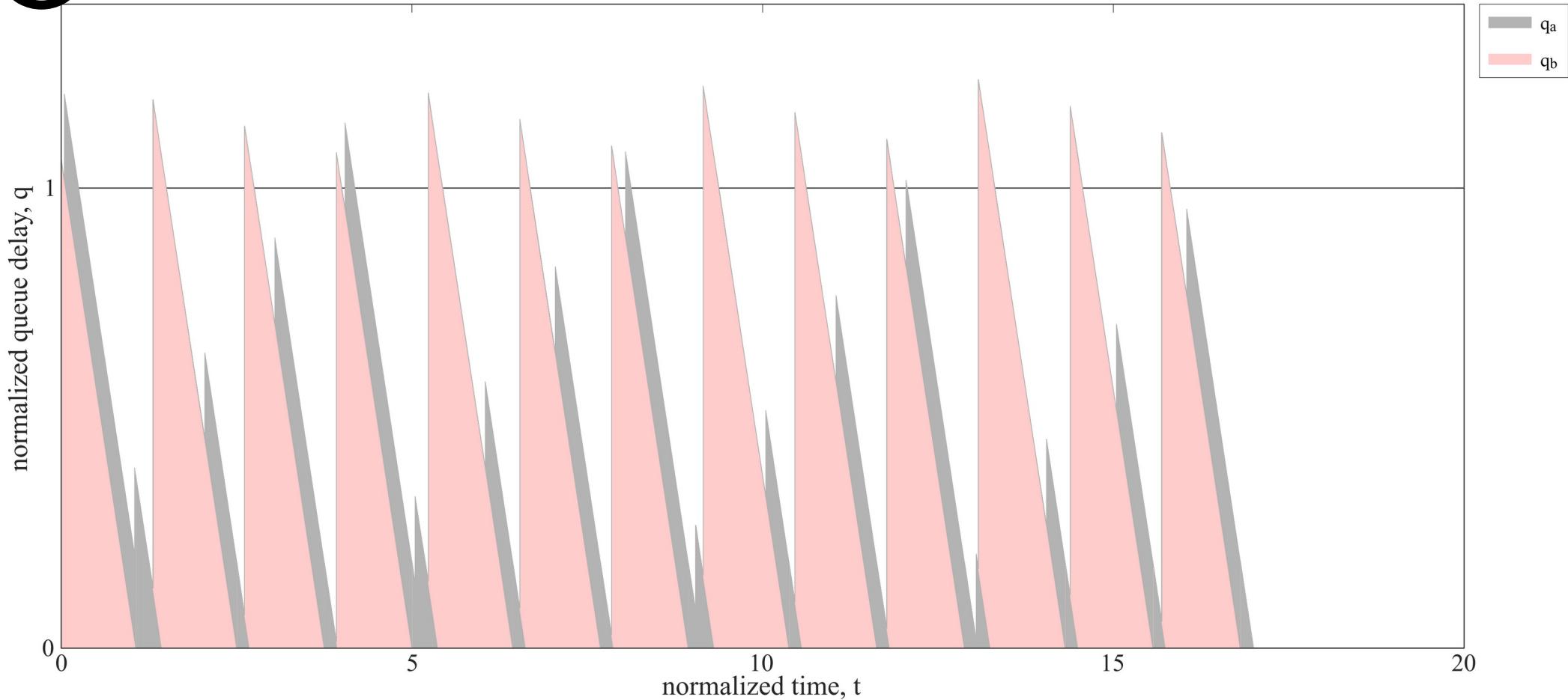


# Same example parameter space in 3-D



**A****Two unresponsive flows, a & b;**Phase shift,  $\phi = 3.0864\%$ Capacity fractions,  $\lambda_a = 7/16$ ,  $\lambda_b = 9/16$  ( $\Sigma \lambda = 100\%$ );      Burst queue delays  $\beta_a = 65.625\%$ ,  $\beta_b = 59.375\%$  ( $\Sigma \beta = 125\%$ )

**B****Two unresponsive flows, a & b;**Phase shift,  $\phi = 3.0864\%$ Capacity fractions,  $\lambda_a = 13/16$ ,  $\lambda_b = 3/16$  ( $\Sigma \lambda = 100\%$ );      Burst queue delays  $\beta_a = 18.75\%$ ,  $\beta_b = 106.25\%$  ( $\Sigma \beta = 125\%$ )

**C****Two unresponsive flows, a & b;**Phase shift,  $\phi = 3.0864\%$ Capacity fractions,  $\lambda_a = 3/16$ ,  $\lambda_b = 13/16$  ( $\Sigma \lambda = 100\%$ );      Burst queue delays  $\beta_a = 18.75\%$ ,  $\beta_b = 106.25\%$  ( $\Sigma \beta = 125\%$ )

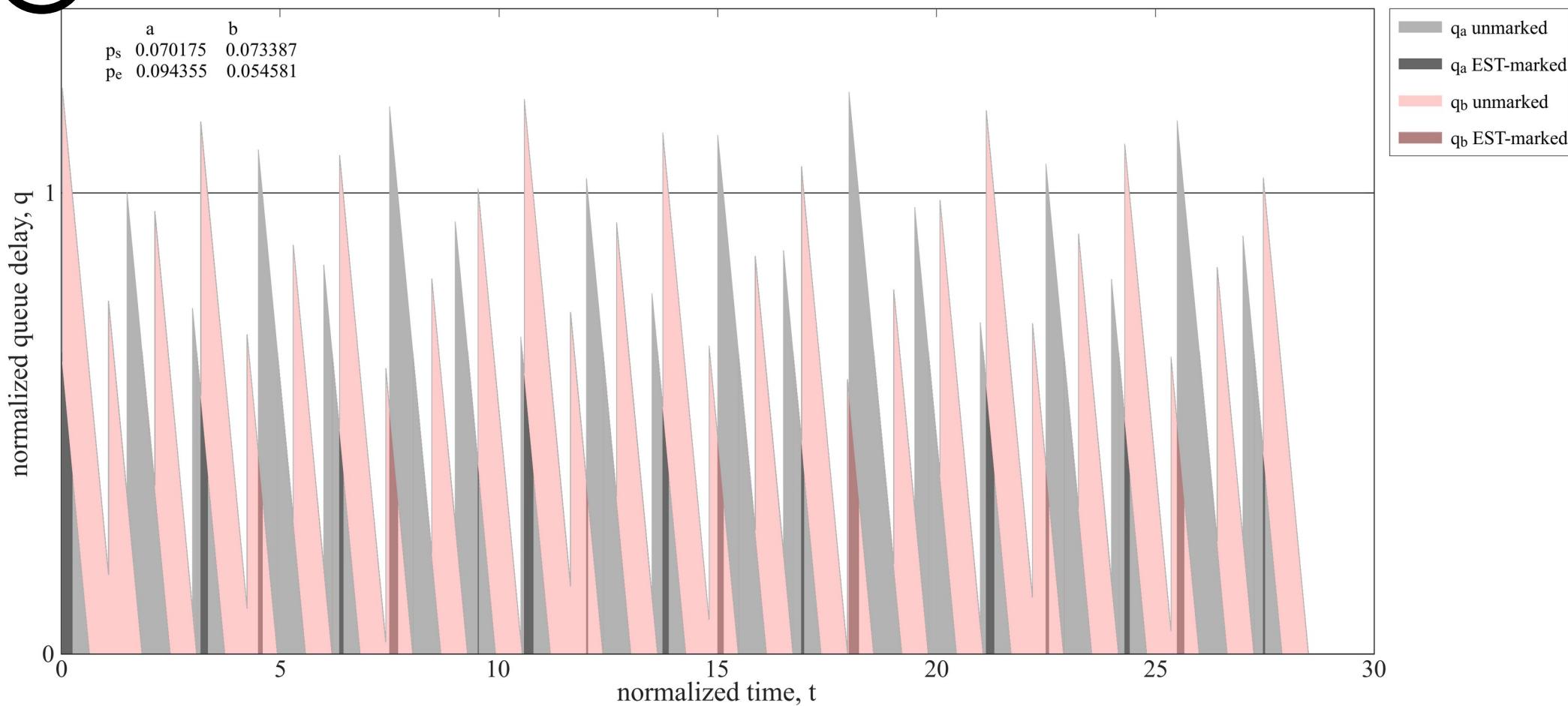
# Ideals for apportioning blame

- Marking probability of one flow,  $p_a$ 
  - 1) should monotonically increase with its burst size,  $\beta_a$
  - 2) should not decrease with its capacity share,  $\lambda_a$

assuming the whole system is otherwise constant
- Satisfying both ideals would be robust but probably unattainable, e.g.
  - would fail on #1 if marking saturates, e.g. v large bursts
  - unsure if #2 is even satisfied with equal constant burstiness (see control expt later)
- Some scope to relax either ideal,
  - but unable to quantify precisely, so far

# Compare 2 marking approaches

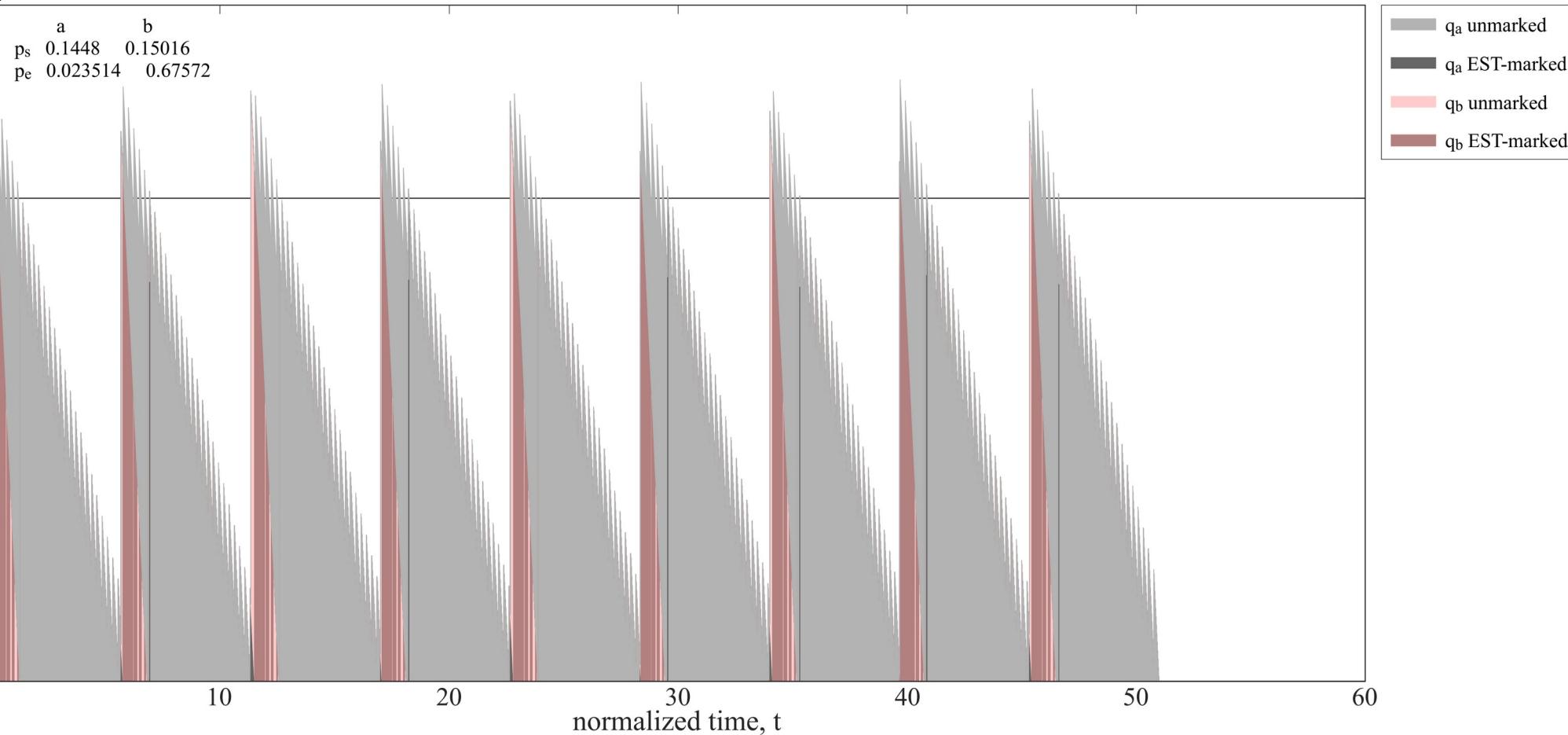
- based on delay to self,  $q_s$ 
  - sojourn-based marking (subscript  $s$ )
  - queue delay ahead at enqueue
  - visualization: the amount and flow colour of the  $q$  over the threshold
- based on delay to others,  $q_e$ 
  - expected service time (subscript  $e$ )
  - queue delay behind at dequeue
  - visualization: colour of flow being dequeued when the  $q$  is over threshold

**A****Two unresponsive flows, a & b;****Phase shift,  $\varphi = 3.0864\%$** Capacity fractions,  $\lambda_a = 7/16$ ,  $\lambda_b = 9/16$  ( $\Sigma\lambda = 100\%$ );      Burst queue delays  $\beta_a = 65.625\%$ ,  $\beta_b = 59.375\%$  ( $\Sigma\beta = 125\%$ )

**B**

Two unresponsive flows, a & b; Phase shift,  $\varphi = 3.0864\%$

Capacity fractions,  $\lambda_a = 13/16$ ,  $\lambda_b = 3/16$  ( $\Sigma \lambda = 100\%$ ); Burst queue delays  $\beta_a = 18.75\%$ ,  $\beta_b = 106.25\%$  ( $\Sigma \beta = 125\%$ )

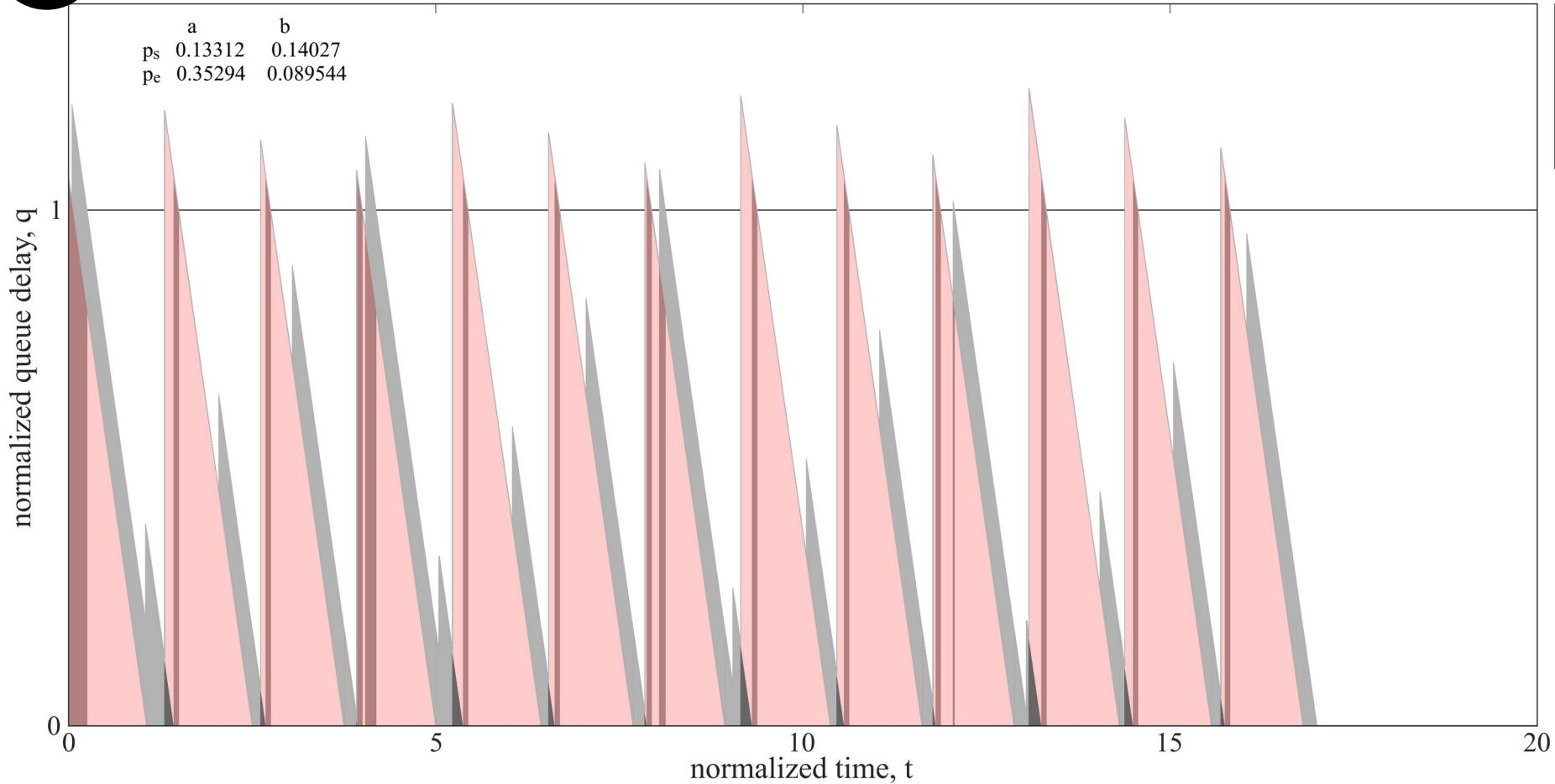


C

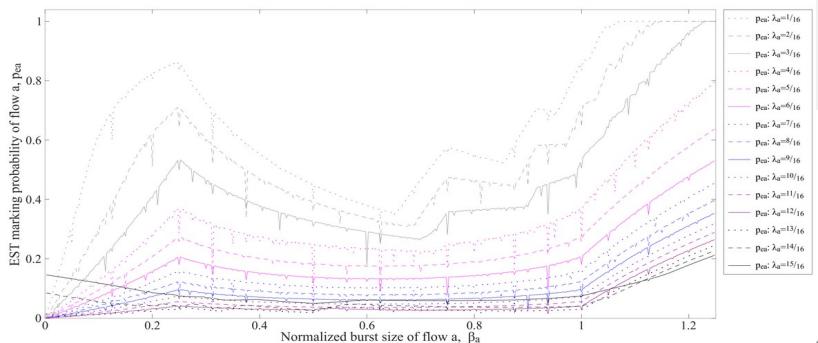
**Two unresponsive flows, a & b;****Phase shift,  $\varphi = 3.0864\%$** **Capacity fractions,  $\lambda_a = 3/16$ ,  $\lambda_b = 13/16$  ( $\Sigma\lambda = 100\%$ );      Burst queue delays  $\beta_a = 18.75\%$ ,  $\beta_b = 106.25\%$  ( $\Sigma\beta = 125\%$ )**

	a	b
$p_s$	0.13312	0.14027
$p_e$	0.35294	0.089544

- q<sub>a</sub> unmarked
- q<sub>a</sub> EST-marked
- q<sub>b</sub> unmarked
- q<sub>b</sub> EST-marked



Expected Service Time (EST) marking with two unresponsive flows, a & b  
Capacity fractions,  $\lambda_a$  &  $\lambda_b$  : utilization,  $\Sigma\lambda = 100\%$ ; Burst sizes  $\beta_a$  &  $\beta_b$  :  $\Sigma\beta = 125\%$  of marking threshold

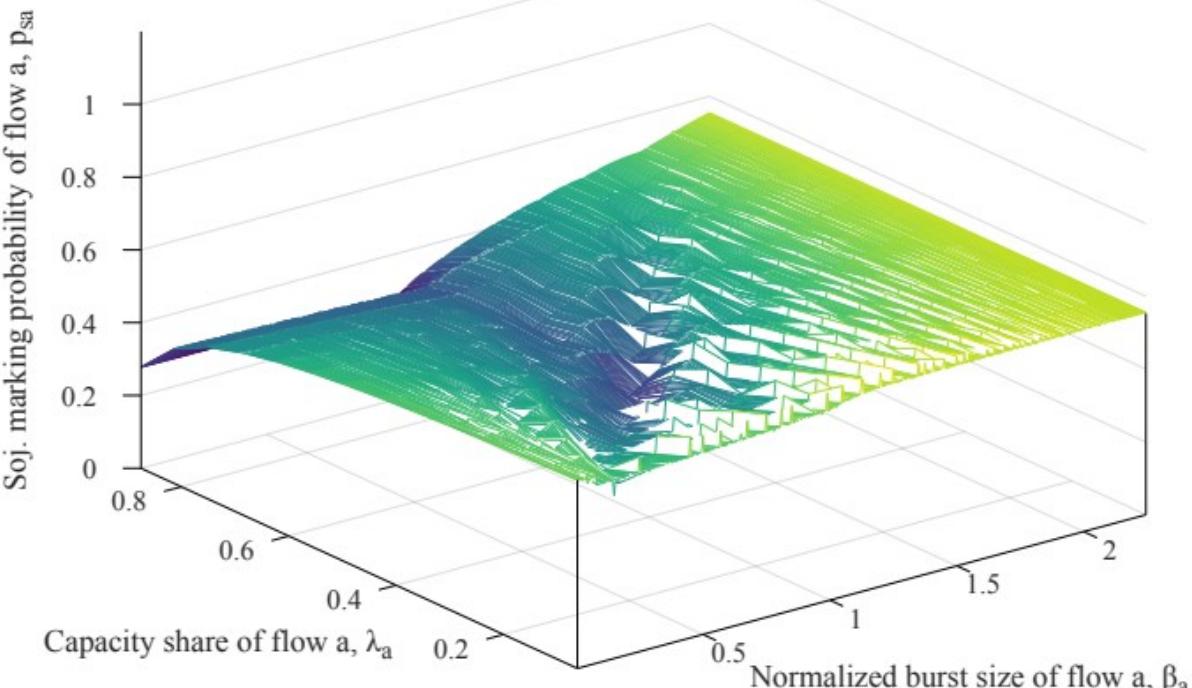


# Results – Examples

- Detailed 2-D plots (like above)
  - in 4 complementary slide packs
  - 1 for each metric
- choice of 4 metrics
  - $p_a$  : marking probability of flow a
  - $\Delta p = p_a - p_b$
  - $\lambda_a p_a$  : marking rate of flow a
  - $\Delta(\lambda p) = \lambda_a p_a - \lambda_b p_b$
- Next 2 slides: 3-D plots
  - using first metric only ( $p_a$ )
  - axes will be too small to read, but all like the example to the right

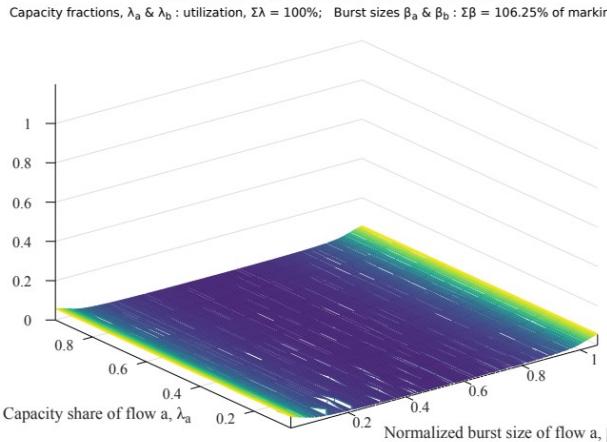
Sojourn marking with two unresponsive flows, a & b

Capacity fractions,  $\lambda_a$  &  $\lambda_b$  : utilization,  $\Sigma\lambda = 93.75\%$ ; Burst sizes  $\beta_a$  &  $\beta_b$  :  $\Sigma\beta = 225\%$  of marking threshold

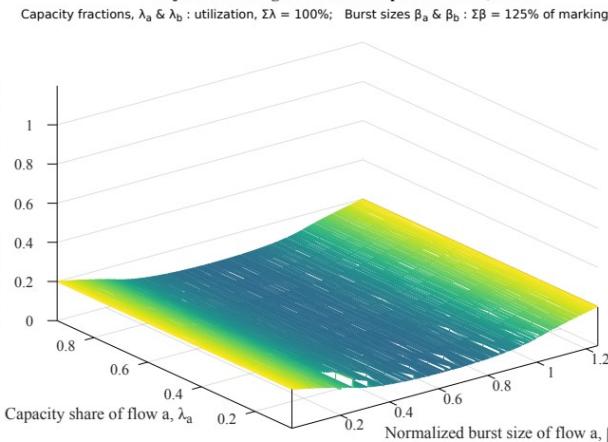


# Sojourn marking

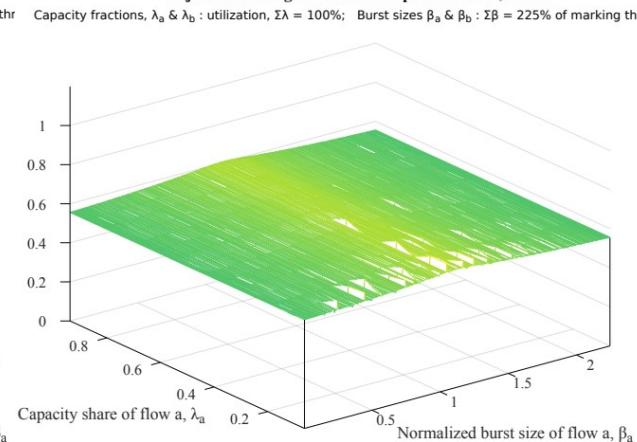
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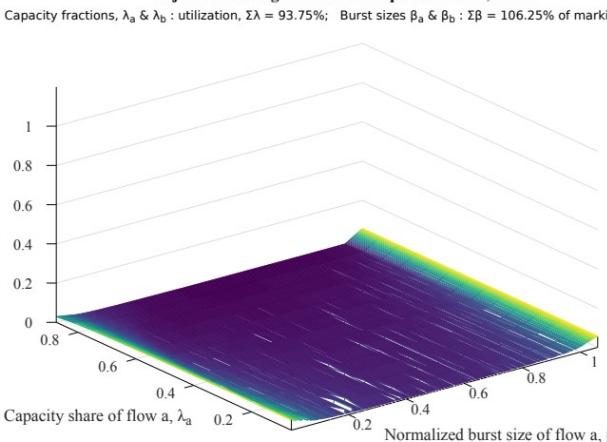
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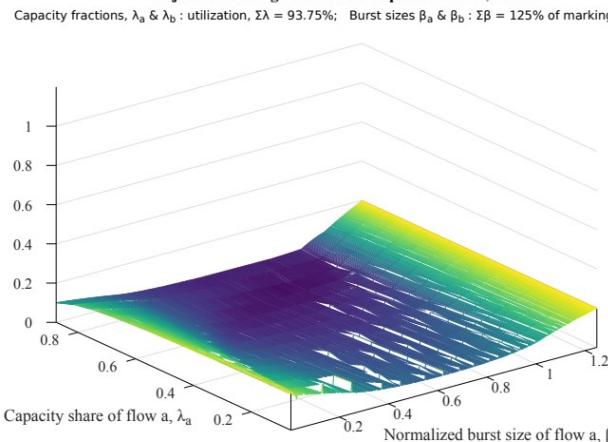
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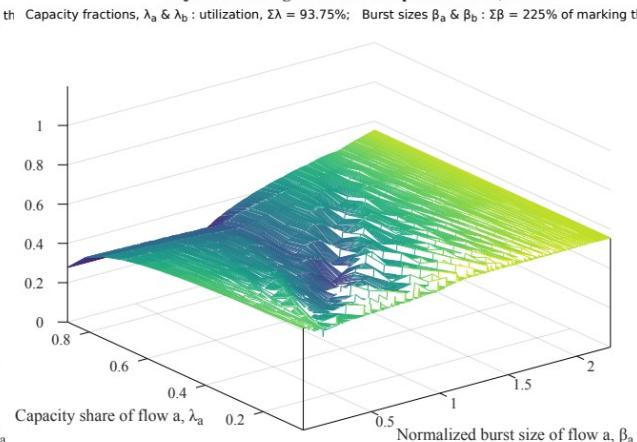
**Sojourn marking with two unresponsive flows, a & b**



**Sojourn marking with two unresponsive flows, a & b**



**Sojourn marking with two unresponsive flows, a & b**



max burst,  $\Sigma\beta$

106.25%

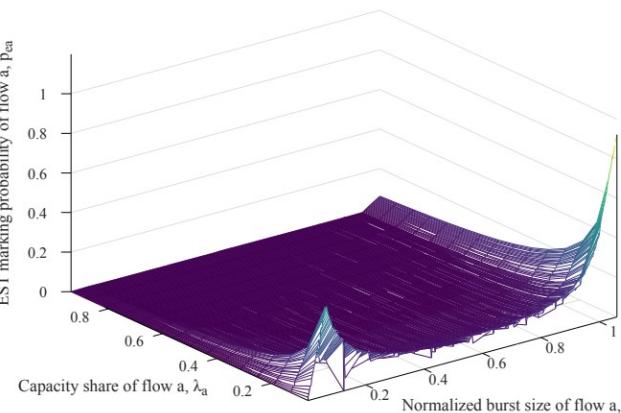
125%

225%

# EST marking

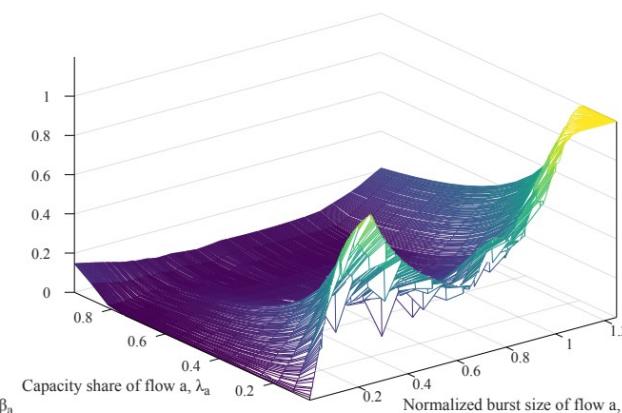
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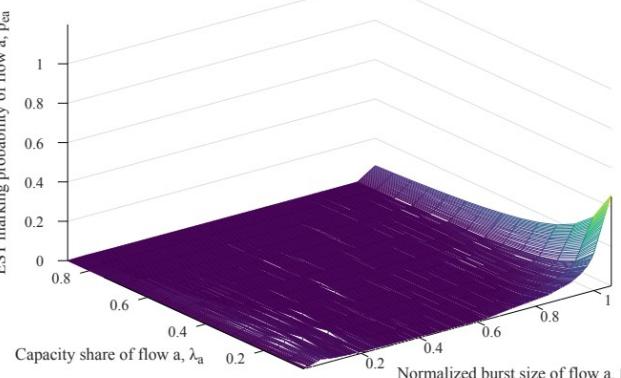
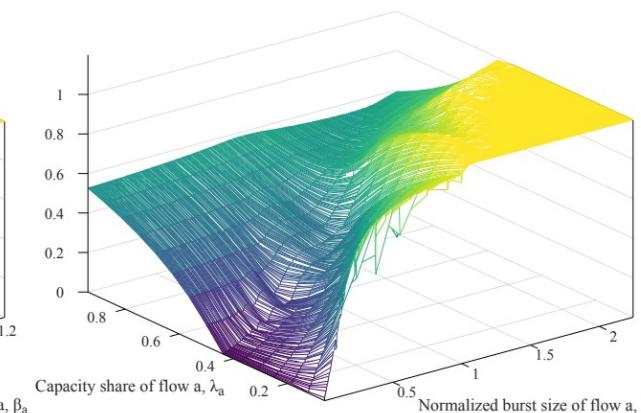
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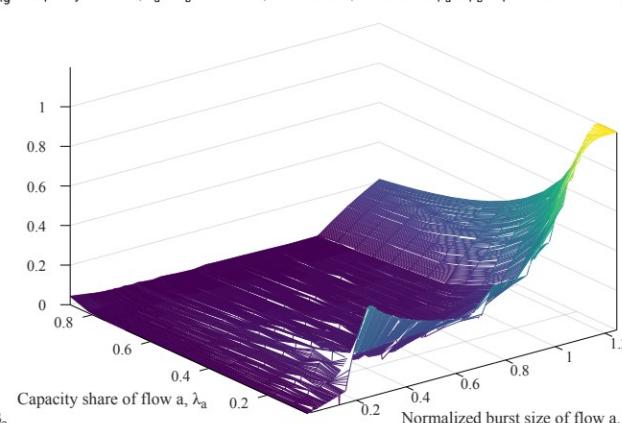
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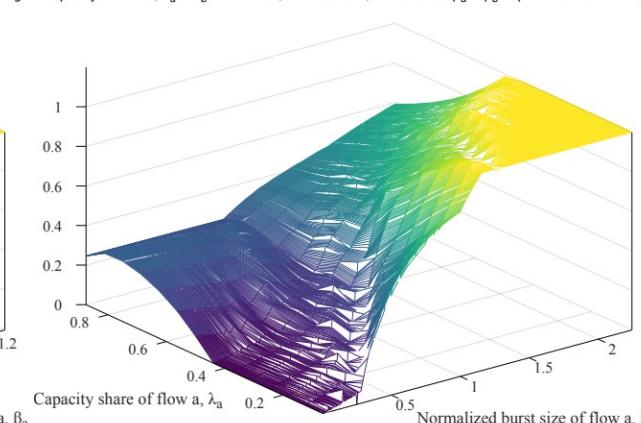
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max burst,  $\Sigma\beta$

106.25%

125%

225%

# Evaluation

ideal:	increase with burst size $\beta_a$ ?	not decrease with capacity share $\lambda_a$ ?
sojourn <sup>1</sup>	N <sup>2</sup>	Y <sup>1</sup>
EST	Y & N <sup>3</sup>	N

- Sojourn is not good enough, but EST is not sufficiently better to replace it
- Not as clear-cut as the traffic light colours imply
  - see earlier: "some scope to relax either ideal"
  - but "unable to quantify precisely, so far"

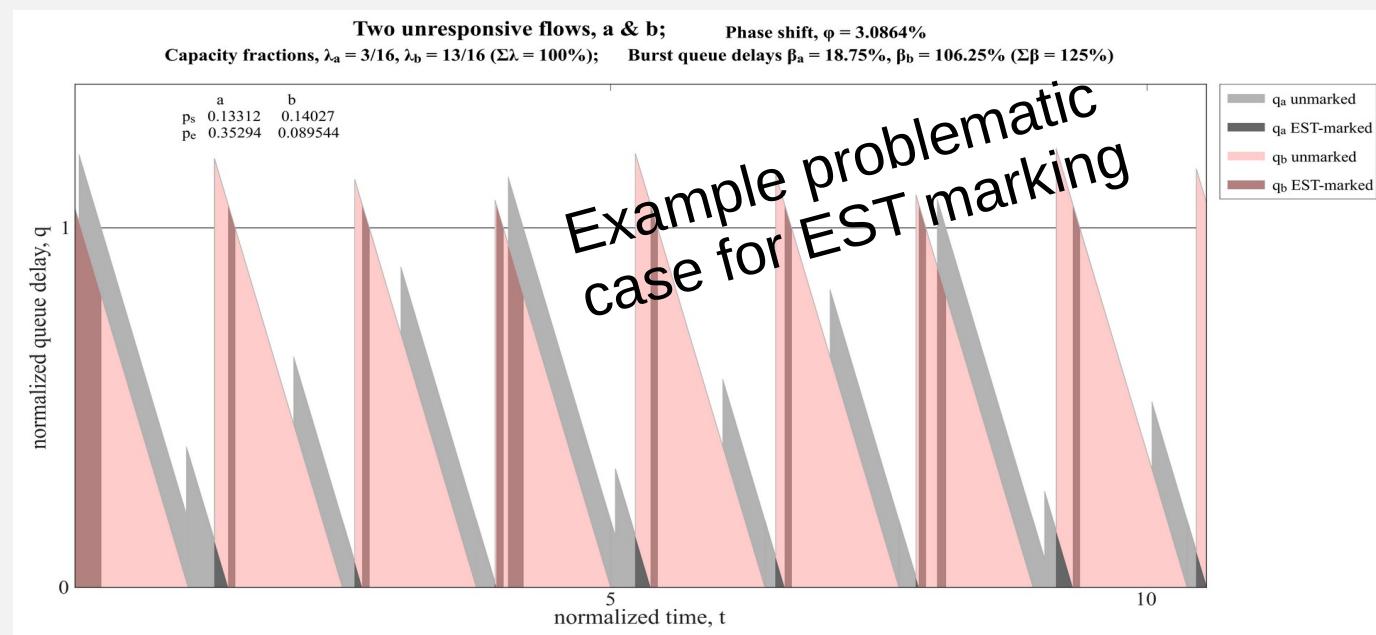
<sup>1</sup> in general, other than high max burst and low utilization

<sup>2</sup> symmetric about the avg burst size

<sup>3</sup> decreases from a peak at  $\beta_a = \sum \beta - 1$  if low capacity share

# Interpretation

- for a grey flow with low capacity share and smaller bursts than pink
- even though grey arrives smoothly, it can only depart in the gaps betw. pink bursts
- variation in these gaps and in how many grey bursts arrive between pink ones is high relative to average grey traffic
- EST marks the residual grey in the  $q$  when the next pink burst arrives
- and the pink burst gets pushed back, closing subsequent gaps
- **on average grey fits between pink bursts, but EST punishes grey for all variance**



# Next steps

- Design a better marking approach?
  - using the insights from this research
  - based on sthg like  $q_e - q_s$  . Perhaps  $2(q_e - q_s)(q_e + q_s)$  ?
- Validate model against:
  - ns3 simulation
  - testbed
- Design and evaluate an aggregate policer?

# How to Apportion Blame for a Queue with Arrivals in Bursts?

Discussion  
and spare slides

Compare 2 marking approaches: Sojourn (s) & EST (e)

Revisit  
Original  
✓

# Experiment plans

Expt 1.1:

- For a set of fixed capacity shares  $\lambda_a + \lambda_b = \Sigma\lambda$  (constant)
- burst size  $\beta$ : increase  $\beta_a$ , decrease  $\beta_b$ , with  $\beta_a + \beta_b = \Sigma\beta$  (constant)
- measure both marking probabilities,  $p_s$  &  $p_e$
- for each approach, report mean, max & min of each marking metric over a range of phase shifts

• Expt 2.1:

- Same as #1.1, except hold  $\beta_b$ , while increasing  $\beta_a$

✓ Expt 3.1:

- Same as #1.1 except increase  $\beta_a$  with  $\lambda_a$
- **(can visualize this on 3-D plots of expt 1.1)**

✓ Control expt 1.2:

- Same as #1.1, with  $\Sigma\lambda$  and  $\Sigma\beta$  constant
- but with  $\beta_a = \beta_b$  increase  $\lambda_a$
- marking should not depend on capacity share,  $\lambda$
- **(can visualize this on 3-D plots of expt 1.1)**

• Expt 4? Model packetization or use ns3

• Redesign marking?

• Design & Model aggregate policer

Approach – more detail

# Phase Shift

- At each point in the parameter space, start from multiple different phase shifts
- Avoid always including zero as one phase shift
- Record mean, max & min\* of marking metrics

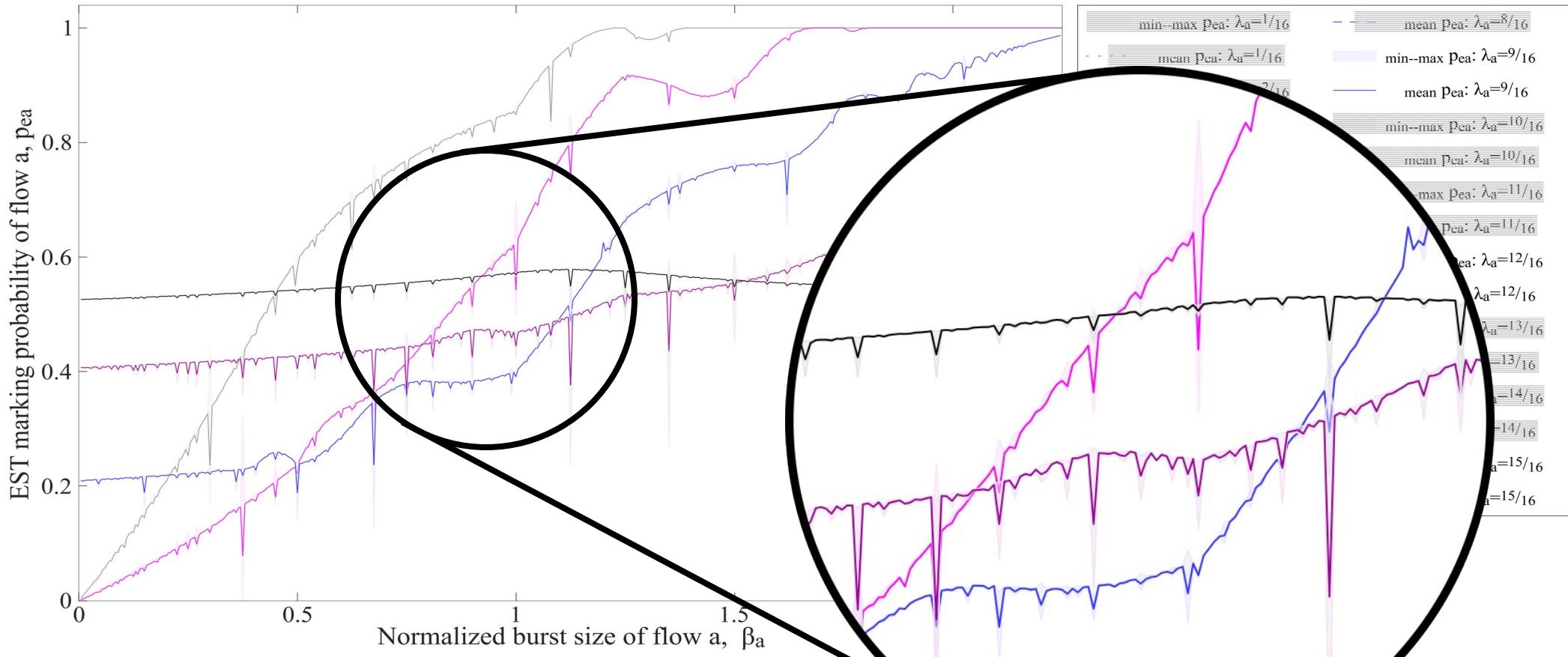
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\* variation is not symmetric, so std. dev. not applicable

# Typical Spread of Results over 8 phase samples

Expected Service Time (EST) marking with two unresponsive flows, a & b

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# Interpretation: phase shift results

- points where spread increases are where the pattern repeats after a few bursts
  - i.e. lowest common integer multiple of the two burst intervals is low
  - then "law of large numbers" doesn't apply
  - unusual coincidences more likely,  
e.g. bursts never precisely coincide
- flows are unlikely to get stuck at these points
  - lower marking causes flow to increase window
- recommend a little randomization of burst sizing – just in case

## Approach – more detail

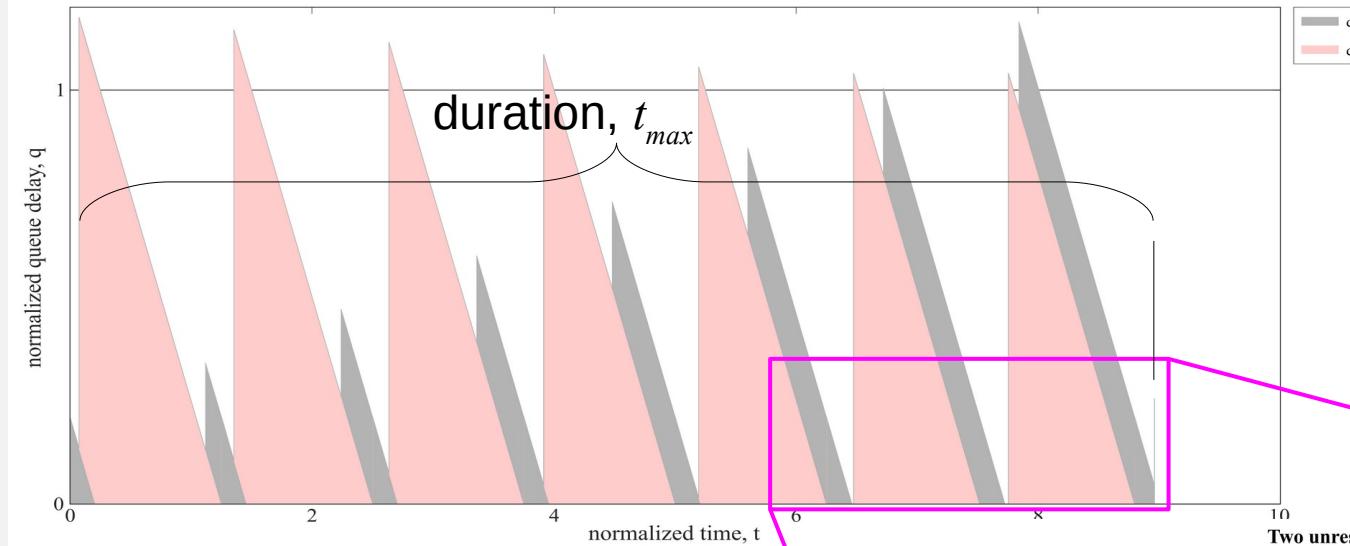
# Minimal Repeating Pattern

- Duration: lowest common integer multiple
  - of the two burst intervals (not integers themselves)
- Find where to start
  - assume a sufficient standing queue to never go idle
  - start 2<sup>nd</sup> pass where standing q is smallest
  - challenge: 2 passes without doubling the run time

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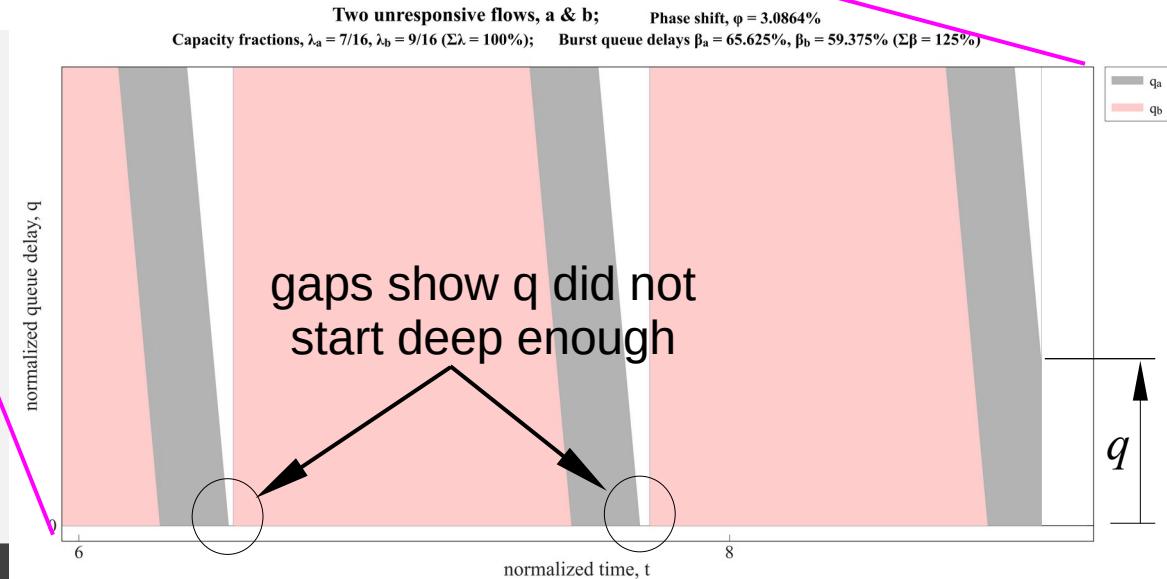
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# Example of $q=0$ at the wrong burst

- if set  $q = 0$  at wrong burst,  
 $q > 0$  at end of duration  
 and starting with a slightly larger  $q$   
 has a knock-on effect next round
- for correct approach see source  
 (after 2 subtly incorrect attempts)



# Approach What if's

- Check the validity of the approach,  
by investigating alternative avenues
  - increase burstiness of flow a,  $\beta_a$ ,  
while holding  $\beta_b$  at a small selection of const. values
  - increase  $\lambda_a$  &  $\beta_a$  together,  
related by a selection of factors, e.g.  $\Delta\lambda = k\Delta\beta$   
(different diagonal paths across the 3-D surface)
  - investigate including zero in the range of phase shifts