

Handout # 22

```
#####  
# R Code for canonical correlation analysis #  
#####  
  
# Use the iris data set and consider the entire data set (all three species)  
TX<- c( 5.1, 3.5, 1.4, 0.2, 1,  
# more rows here  
        5.9, 3.0, 5.1, 1.8, 3)  
  
X<-matrix(data=TX,ncol=5,byrow=TRUE)  
Iris <- data.frame(SepalL = X[,1],SepalW = X[,2],PetalL = X[,3], PetalW = X[,4], Group = X[,5])  
sepal.meas <- Iris[,1:2]  
petal.meas <- Iris[,3:4]  
  
# CCA  
# Find the blocks of the COVARIANCE matrix:  
S11 <- cov(sepal.meas)  
S22 <- cov(petal.meas)  
S12 <- c(cov(sepal.meas[,1], petal.meas[,1]), cov(sepal.meas[,1], petal.meas[,2]),  
          cov(sepal.meas[,2], petal.meas[,1]), cov(sepal.meas[,2], petal.meas[,2]))  
S12 <- matrix(S12, ncol=ncol(S22), byrow=T) # S12 has q2 columns, same as number of petal measurements  
S21 <- t(S12) # S21=transpose of S12  
  
# Finding the E1 and E2 matrices:  
E1 <- solve(S11) %*% S12 %*% solve(S22) %*% S21  
E2 <- solve(S22) %*% S21 %*% solve(S11) %*% S12  
eigen(E1)  
eigen(E2)  
  
# The canonical correlations are:  
canon.corr <- sqrt(eigen(E1)$values)  
canon.corr  
  
# The canonical variates are based on the eigenvectors of E1 and E2:  
# a1 = (0.78, -0.62)  
# b1 = (0.77, -0.63)  
# a2 = (0.26, 0.97)  
# b2 = (-0.37, 0.93)  
  
# Only the first canonical correlation is really substantial:  
# u1 = 0.78*Sepal.Length - 0.62*Sepal.Width  
# v1 = 0.77*Petal.Length - 0.63*Petal.Width  
  
# Plotting the first set of canonical variables:  
u1 <- as.matrix(Iris[,1:2]) %*% as.matrix(eigen(E1)$vectors[,1])  
v1 <- as.matrix(Iris[,3:4]) %*% as.matrix(eigen(E2)$vectors[,1])  
plot(u1,v1)  
cor(u1,v1)  
  
# Plotting the second set of canonical variables:  
u2 <- as.matrix(Iris[,1:2]) %*% as.matrix(eigen(E1)$vectors[,2])  
v2 <- as.matrix(Iris[,3:4]) %*% as.matrix(eigen(E2)$vectors[,2])  
plot(u2,v2)  
cor(u2,v2)
```

```
#####
> eigen(E1)
$values
[1] 0.88542265 0.01536035

$vectors
      [,1] [,2]
[1,] 0.7809378 0.2607687
[2,] -0.6246088 0.9654013

> eigen(E2)
$values
[1] 0.88542265 0.01536035

$vectors
      [,1] [,2]
[1,] 0.7743756 -0.3705408
[2,] -0.6327262 0.9288162

>
> # The canonical correlations are:
>
> canon.corr <- sqrt(eigen(E1)$values)
> canon.corr
[1] 0.9409690 0.1239369
>
> # The canonical variates are based on the eigenvectors of E1 and E2:
>
> # a1 = (0.78, -0.62)
> # b1 = (0.77, -0.63)
> # a2 = (0.26, 0.97)
> # b2 = (-0.37, 0.93)
>
> # Only the first canonical correlation is really substantial:
>
> # u1 = 0.78*Sepal.Length - 0.62*Sepal.Width
> # v1 = 0.77*Petal.Length - 0.63*Petal.Width
>
> # Plotting the first set of canonical variables:
>
> u1 <- as.matrix(Iris[,1:2]) %*% as.matrix(eigen(E1)$vectors[,1])
> v1 <- as.matrix(Iris[,3:4]) %*% as.matrix(eigen(E2)$vectors[,1])
> plot(u1,v1)
> cor(u1,v1)
      [,1]
[1,] 0.940969
>
> # Plotting the second set of canonical variables:
>
> u2 <- as.matrix(Iris[,1:2]) %*% as.matrix(eigen(E1)$vectors[,2])
> v2 <- as.matrix(Iris[,3:4]) %*% as.matrix(eigen(E2)$vectors[,2])
> plot(u2,v2)
> cor(u2,v2)
      [,1]
[1,] 0.1239369
```