

## STA 477 Concept Problems 1

1. What is the difference between a stochastic process and a time series realization?
2. Why is it useful to build up a large dictionary of models prior to fitting models to data?
3. Let  $\widehat{X}_{t+1}$ , which is a function of  $X_1, \dots, X_t$ , be a predictor of  $X_{t+1}$ . Under what conditions is  $\widehat{X}_{t+1}$  equal to  $X_{t+1}$ ?
4. For a time series having both trend and seasonal components, does it matter whether or not the trend or seasonal component is addressed first? Please explain.
5. Is the sample correlation between  $X_t$  and  $X_{t+1}$ , for  $t = 1, \dots, N$ , the same as  $r_1 = \widehat{\rho}(1)$ ? Please explain.
6. Explain the difference between weakly and strictly stationary processes.
7. Under what conditions is a  $MA(q)$  process equivalent to a  $AR(\infty)$  process?