

CSCE 515 Midterm Exam Prep

Brad Burkman

Last Edit: November 19, 2018

1 Checklist

- To Do: Exercise #9, 17, 18
- To Expand/Fix: Exercise #13, 20
- Not Sure: #1, 3
- Review Hard: #10
- Done: #2, 4, 5, 6, 7, 8, 11, 12, 14, 15, 16

2 Topics to Solidify

- Lighting
- Perspective

Contents

1	Checklist	1
2	Topics to Solidify	1
3	Study Guide Questions	3
3.1	Question 1: Confused	3
3.1.1	First Punt, Brad Burkman, 11/17 7:41pm	3
3.1.2	Marcus Shannon's Answer	3
3.2	Question 2: Done	3
3.2.1	First guess, Brad Burkman, 11/14 7:44pm	4
3.2.2	Second Attttempt, informed by notes, Brad Burkman, 11/14 7:58pm	4
3.2.3	Midpoint Line (Besenham) Algorithm	4
3.2.4	Making it Faster	5

3.3	Question 3: Unsure	5
3.3.1	Information from Class Notes, Brad Burkman, 17 November 10:11pm	5
3.4	Question 4: Done	6
3.4.1	What kind of question could it be?	6
3.5	Question 5: Done	6
3.5.1	Rotation Matrices	7
3.5.2	Z-rotation matrix	7
3.5.3	Y-rotation matrix	7
3.5.4	X-rotation matrix	7
3.6	Question 6: Done	8
3.6.1	Brad's answer, 18 November 6:44 am	8
3.7	Question 7: Done	8
3.8	Question 8: Done	9
3.8.1	First guess for #8, Brad Burkman, 7:58pm, 11 November	9
3.8.2	Dr. Borst's Discussion	9
3.9	Question 9: To Do	10
3.9.1	Marcus Shannon's Answer	10
3.10	Question 10: Review	10
3.10.1	Dr. Borst's Answer	11
3.10.2	Marcus Shannon's Answer	11
3.11	Question 11: Done	11
3.11.1	First Guess, Brad Burkman, 8:26pm 14 November	11
3.12	Question 12: Done	12
3.12.1	Dr. Borst's Answer	12
3.13	Question 13: Expand and Review	12
3.13.1	Orthographic Projection from Simple Example	12
3.13.2	Extended Orthographic Projection Matrix	12
3.13.3	Perspective Matrix	12
3.14	Question 14: Done	13
3.14.1	Dr. Borst's Answer	13
3.15	Question 15: Done	13
3.15.1	Note from Marcus Shannon for #15 and #16	13
3.16	Question 16: Done	13
3.16.1	First Guess, Brad Burkman, 9:03pm 14 November	13
3.17	Question 17: To Do	13
3.17.1	Marcus Shannon's Answer	14
3.18	Question 18: To Do	14
3.18.1	Marcus Shannon's Solution	14
3.19	Question 19: Not on Exam	15
3.20	Question 20: To Fix	15

3.20.1 First Guess, Brad Burkman, 9:23pm 14 November	15
3.20.2 Changes based on Dr. Borst's Discussion	16
3.20.3 Marcus Shannon's Reply to Brad's Solution	16

3 Study Guide Questions

3.1 Question 1: Confused

1. Both raster and vector displays use a refresh buffer. What is the difference between the two in terms of refresh buffer contents?

3.1.1 First Punt, Brad Burkman, 11/17 7:41pm

I have no idea. I do not have a vector display refresh buffer in my notes, and I can't find it online.

Here's what I do know.

Raster displays have a bitmap of the color and intensity of each pixel. Their refresh buffer holds the next screen to be displayed. It may have two layers so that the swap between the displays doesn't happen in the middle of an update. If it's a CRT monitor, it paints the pixels in rows, not following the contours of each object. Raster displays have a constant refresh rate.

Vector displays, like an oscilloscope, move a laser or electron beam over the screen following the contours of each object, drawing it smoothly. It starts redrawing the screen after it has finished drawing the screen.

3.1.2 Marcus Shannon's Answer

Q1: According to my class notes

- Vector Display Refresh Buffers contain a series of commands directing how the electron gun is controlled by the deflection plates, organizing an effective way to draw lines onto the display.
- Raster Display Refresh Buffers contain a 2-dimensional bitmap/pixmap which is then used to render per-pixel data via the video controller onto the display.

3.2 Question 2: Done

2. For the midpoint line algorithm, how were floating point operations converted to integer operations for the main loop? (Be as specific as possible.)

3.2.1 First guess, Brad Burkman, 11/14 7:44pm

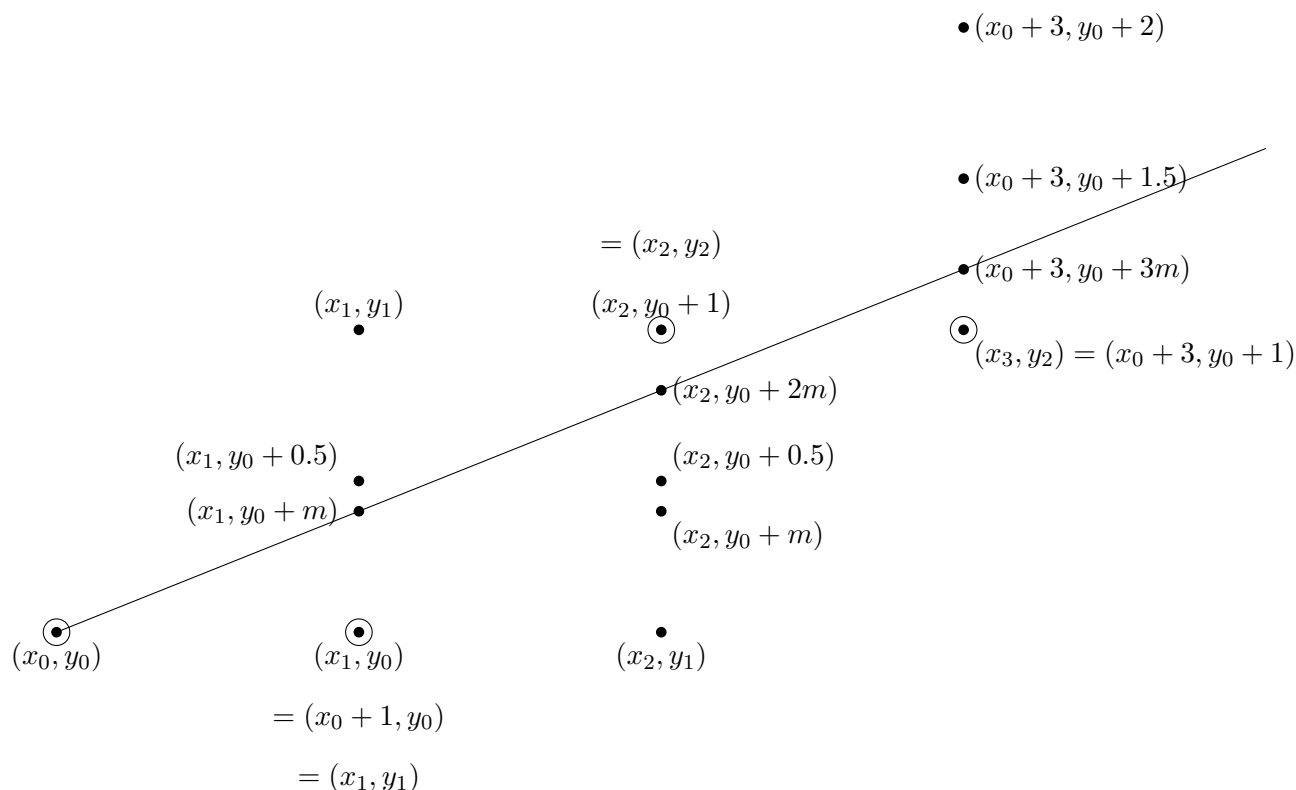
The floating point operations were multiplied by [something like] the number of pixels that each integer represented, then rounded, because we don't care about being between two pixels; we have to pick one.

3.2.2 Second Attempt, informed by notes, Brad Burkman, 11/14 7:58pm

Since this sample question is about a small piece of the Bresenham algorithm, I presume the actual exam question could be anything about it.

Looking at the notes from 28 August, here's how the midpoint (Bresenham) algorithm works.

3.2.3 Midpoint Line (Bresenham) Algorithm



Initialize d at $m - 0.5$.

Since in this case d is negative, choose to move E rather than NE.

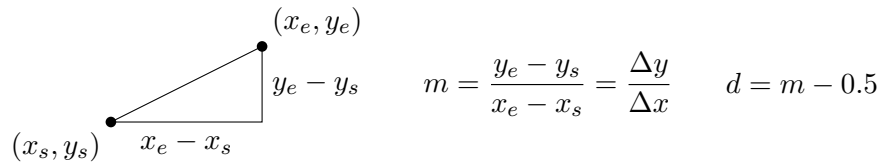
At the second step, because we moved E, $d = d + m$, so $d = 2m - 0.5$.

Since d is positive, move NE.

Now since we moved NE, $d = d + m - 1 = (2m - 0.5) + m - 1 = 3m - 1.5$

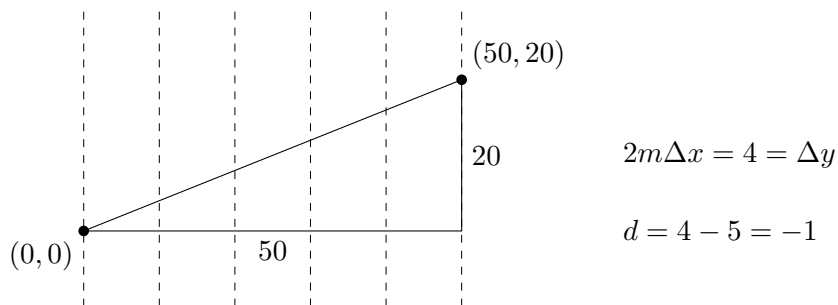
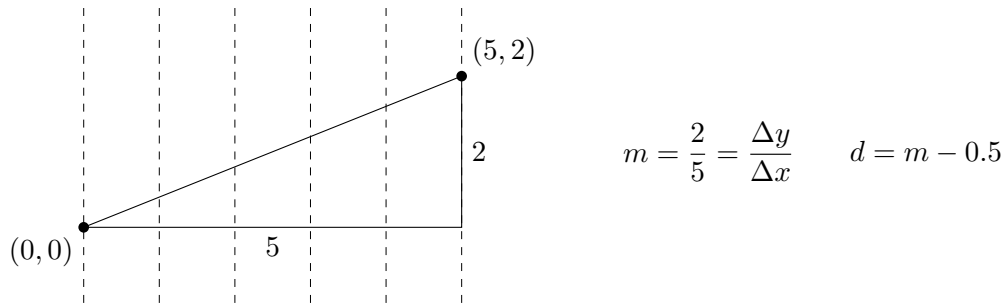
Since $d = 3m - 1.5$ is negative, move E.

3.2.4 Making it Faster



Scale everything by $2\Delta x$, so that $m = 2\Delta y$ and $d = 2\Delta y - \Delta x$.

Same example as above:



Initialize d at $2\Delta y - \Delta x = 4 - 5 = -1$

Since in this case d is negative, choose to move E rather than NE.

At the second step, because we moved E, $d = d + 2\Delta y$, so $d = -1 + 4 = 3$.

Since d is positive, move NE.

Now since we moved NE, $d = d + 2\Delta y - 10 = 3 + 2(2) - 10 = -3$

Since $d = -3$ is negative, move E.

3.3 Question 3: Unsure

3. What is meant by each of the three terms geometry, topology, and attributes for a polygonal surface model?

3.3.1 Information from Class Notes, Brad Burkman, 17 November 10:11pm

- Vertex list gives the geometry, the shape.
- Index list gives the topology, the relationships between neighbors.

- Attributes are colors and normal vectors, perhaps the texture?

3.4 Question 4: Done

~~4. Give an example of an operation that would normally be faster with pointers to a vertex list mesh representation than with an explicit representation. Justify your answer.~~

Replace with:

Triangle Strips Question

3.4.1 What kind of question could it be?

- Primitive restart index
- Vertices 0,1,2 define first triangle, 1,2,3 define second.
- First triangle in the strip determines winding order. Default is counterclockwise for the exterior, clockwise for the interior.
- Given a rotated surface with np number of points to be rotated and nm steps of rotation, how many vertices, cells, triangles, triangles, triangle strips, elements in the vertex list, elements in the index list ... are there?

3.5 Question 5: Done

5. Answer true or false for each item below.

For transforms as discussed in class:

- Any two rotations are commutative.
False. See example below.
- Any two translations are commutative.
True.
- The inverse of a rotation matrix is its transpose.
True
- The inverse of a translation matrix is its transpose.
False
- For any composite sequence of translations and rotations, there exists a single rotation and translation pair that would have the same net effect. [Dr. Borst says it's true.]

3.5.1 Rotation Matrices

What do we know about rotation matrices?

- Each row, and each column, is a unit vector, because we're not changing scale.
- The determinant of the matrix is 1.
- They are orthogonal; i.e. $R^{-1} = R^T$.

3.5.2 Z-rotation matrix

$$\begin{bmatrix} \cos \theta & -\sin \theta & 0 & 0 \\ \sin \theta & \cos \theta & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

3.5.3 Y-rotation matrix

$$\begin{bmatrix} \cos \theta & 0 & \sin \theta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \theta & 0 & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

3.5.4 X-rotation matrix

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \theta & -\sin \theta & 0 \\ 0 & \sin \theta & \cos \theta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Let's multiply two of them together and see whether it's commutative.

$$YX = \begin{bmatrix} \cos \beta & 0 & \sin \beta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \beta & 0 & \cos \beta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \alpha & -\sin \alpha & 0 \\ 0 & \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \cos \beta & \sin \alpha \sin \beta & \cos \alpha \sin \beta & 0 \\ 0 & \cos \alpha & -\sin \alpha & 0 \\ -\sin \beta & \sin \alpha \cos \beta & \cos \alpha \cos \beta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$XY = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & \cos \alpha & -\sin \alpha & 0 \\ 0 & \sin \alpha & \cos \alpha & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos \beta & 0 & \sin \beta & 0 \\ 0 & 1 & 0 & 0 \\ -\sin \beta & 0 & \cos \beta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} \cos \beta & 0 & \sin \beta & 0 \\ \sin \alpha \sin \beta & \cos \alpha & -\sin \alpha \cos \beta & 0 \\ -\cos \alpha \sin \beta & \sin \alpha & \cos \alpha \cos \beta & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

3.6 Question 6: Done

6. Give a 4×4 homogeneous transform (sixteen numbers) for describing an object's local coordinate system with respect to the world coordinate system such that:

- The object's local origin is at world coordinate $(x, y, z) = (4, 0, 2)$,
- The object's local x -axis direction matches the world's z -axis direction, and
- The object's local z -axis direction matches the world's $-x$ (negative x) direction,

3.6.1 Brad's answer, 18 November 6:44 am

A -90° rotation in the Y gives the correct orientation.

Do the rotation, then the translation.

$$\begin{aligned} A = T_{(4,0,2)}Y_{-90} &= \begin{bmatrix} 1 & 0 & 0 & 4 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \cos(-90) & 0 & \sin(-90) & 0 \\ 0 & 1 & 0 & 0 \\ -\sin(-90) & 0 & \cos(-90) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \\ &= \begin{bmatrix} 1 & 0 & 0 & 4 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 2 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & -1 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \\ &= \begin{bmatrix} 0 & 0 & -1 & 4 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 2 \\ 0 & 0 & 0 & 1 \end{bmatrix} \end{aligned}$$

3.7 Question 7: Done

Give the inverse of the transform.

$$A^{-1} = (T_{(4,0,2)}Y_{-90})^{-1} = (Y_{-90})^{-1} (T_{(4,0,2)})^{-1} = Y_{90}T_{(-4,0,-2)}$$

$$\begin{bmatrix} \cos(90) & 0 & \sin(90) & 0 \\ 0 & 1 & 0 & 0 \\ -\sin(90) & 0 & \cos(90) & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & -4 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & -2 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

$$\begin{aligned}
&= \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & -4 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & -2 \\ 0 & 0 & 0 & 1 \end{bmatrix} \\
&= \begin{bmatrix} 0 & 0 & 1 & -2 \\ 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 4 \\ 0 & 0 & 0 & 1 \end{bmatrix}
\end{aligned}$$

Check.

$$AA^{-1} = \begin{bmatrix} 0 & 0 & -1 & 4 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 2 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 0 & 0 & 1 & -2 \\ 0 & 1 & 0 & 0 \\ -1 & 0 & 0 & 4 \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \quad \checkmark$$

3.8 Question 8: Done

8. The diagrams below show a house model. Give $\hat{\mathbf{n}}$, the unit normal vector for the right side of the roof.

3.8.1 First guess for #8, Brad Burkman, 7:58pm, 11 November

$$\hat{\mathbf{n}} = \begin{bmatrix} \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} \\ 0 \end{bmatrix}$$

3.8.2 Dr. Borst's Discussion

Create a coordinate system, make a triangle, and use the cross product to find the normal.

Front left top corner of the house at $A(1, 1, 1)$,

Back left top corner of the house at $B(1, 1, -1)$,

Front peak of house at $C(0, 2, 1)$

Vector \vec{u} from A to B: $\vec{u} = (0, 0, -2)$

Vector \vec{v} from A to C: $\vec{v} = (-1, 1, 0)$

$$\vec{u} \times \vec{v} = \mathbf{n} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 0 & 0 & -2 \\ -1 & 1 & 0 \end{vmatrix} = 2\vec{i} + 2\vec{j} + 0\vec{k}$$

$$\hat{\mathbf{n}} = \frac{\mathbf{n}}{|\mathbf{n}|} = \frac{2\vec{i} + 2\vec{j} + 0\vec{k}}{2\sqrt{2}} = \frac{\sqrt{2}}{2}\vec{i} + \frac{\sqrt{2}}{2}\vec{j} + 0\vec{k} = \begin{bmatrix} \frac{\sqrt{2}}{2} \\ \frac{\sqrt{2}}{2} \\ 0 \end{bmatrix}$$

3.9 Question 9: To Do

9. Recall the plane diagram above. Suppose plane orientation is stored as an $X - Z - Y$ fixed axis set (θ, ϕ, α) , that is, three rotations about fixed world axes in the order X, Z, Y . In terms of the composite rotation resulting from these three components and for arbitrary plane orientation:

- 1) A small change in θ (X amount) will always cause rotation about:

local x_p local y_p local z_p world x world y world z NOT A

- 2) A small change in ϕ (Z amount) will always cause rotation about:

local x_p local y_p local z_p world x world y world z NOT A

- 3) A small change in α (Y amount) will always cause rotation about:

local x_p local y_p local z_p world x world y world z NOT A

- 4) If each component rotation is expressed as a matrix and then all three are composed into a single rotation matrix, the multiplication order for this representation would be:

$R_X R_Z R_Y$ $R_Y R_Z R_X$ $R_X R_Y R_Z$ $R_Z R_Y R_X$ NOT A

3.9.1 Marcus Shannon's Answer

Q9: According to my class notes

- Fixed - Axis Angles are guaranteed a single world rotation and a single local rotation. Everything else is considered questionable.

For example: for the fixed axis angle set X, Z, Y ; X would be the world rotation and Y would be the local rotation. Z is considered questionable and no guarantees can be made about its axis of rotation in relation to what coordinate system.

- Fixed Axis Angle rotations are calculated right to left, for XZY you'll get $Y * Z * X$.
- Euler Angle rotations are calculated left to right, for XYZ you'll get $X * Y * Z$.

3.10 Question 10: Review

10. How could we convert an orientation expressed in a 3-angle set convention above to a single quaternion representing the same orientation? Give a concise but accurate conceptual description.

3.10.1 Dr. Borst's Answer

“Convert each of the three components into a quaternion, and multiply them.” [Dr. Borst]

$X - Z - Y$ fixed axis set is multiplied as $R_Y R_Z R_X$.

3.10.2 Marcus Shannon's Answer

Q10: From deduction and expanding on Dr. Borst explanation of "Convert each of the three components into a quaternion, and multiply them":

- To start, we have a fixed axis angle set of XZY.
- Take each rotation and convert it into three separate Angle-Axis rotations:

$$X \rightarrow x_\theta, ux^t = [1, 0, 0]$$

$$Z \rightarrow z_\theta, uz^t = [0, 1, 0]$$

$$Y \rightarrow y_\theta, uy^t = [0, 0, 1]$$

Note: t means transpose.

- We then compute these using the conversion formula provided in class for converting Angle Axis form into Quaternion form:

$$q = \cos(\theta/2) + (i)(u_x)(\sin(\theta/2)) + (j)(u_y)(\sin(\theta/2)) + (k)(u_z)(\sin(\theta/2))$$

- Composing these 3 quaternions, we now have a single quaternion composed of all rotations.

$$q_{final} = qx * qz * qy$$

- Note: I don't claim for this to be the full expansion or correct, this is merely logical meandering based on what I currently understand.

3.11 Question 11: Done

11. The graph below represents the relationships between coordinate systems (objects, if you prefer) using notation from lecture. Suppose $\{D\}$ is the camera's local frame in an OpenGL application. When rendering an object having vertices described in frame $\{E\}$, what would the value of the modelview matrix be?

3.11.1 First Guess, Brad Burkman, 8:26pm 14 November

$${}^D T \cdot {}^C T \cdot {}^A T \cdot {}^B T \cdot {}^E T = ({}^C T)^{-1} \cdot ({}^A T)^{-1} \cdot {}^A T \cdot {}^B T \cdot {}^E T$$

3.12 Question 12: Done

12. Suppose, for the above diagram, we want to rotate frame $\{B\}$ by a rotation transform R that is to act as a rotation described with respect to the current $\{B\}$ frame. How exactly should R be applied to update one of the transforms in the graph?

3.12.1 Dr. Borst's Answer

${}^A_B T$ gets modified. Multiply by R on the right to be a local change to B .

3.13 Question 13: Expand and Review

13. Give any one of the perspective projection matrices, M_{per} from the lecture slides.

3.13.1 Orthographic Projection from Simple Example

$$M_{ort} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

3.13.2 Extended Orthographic Projection Matrix

$$M_{ort,norm} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} \frac{2}{r-l} & 0 & 0 & 0 \\ 0 & \frac{2}{t-b} & 0 & 0 \\ 0 & 0 & \frac{2}{f-n} & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & -\frac{l+r}{2} \\ 0 & 1 & 0 & -\frac{b+t}{2} \\ 0 & 0 & 1 & \frac{n+f}{2} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

3.13.3 Perspective Matrix

Basic perspective matrix.

$$\begin{bmatrix} X \\ Y \\ Z \\ W \end{bmatrix} = M_{per} \cdot p = \begin{bmatrix} -n & 0 & 0 & 0 \\ 0 & -n & 0 & 0 \\ 0 & 0 & -n & 0 \\ 0 & 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \\ 1 \end{bmatrix} = \begin{bmatrix} -nx \\ -ny \\ -nz \\ z \end{bmatrix} = \begin{bmatrix} -nx/z \\ -ny/z \\ -n \\ 1 \end{bmatrix} = \begin{bmatrix} x_p \\ y_p \\ z_p \\ 1 \end{bmatrix}$$

Generalized perspective matrix

$$M_{per} = \begin{bmatrix} -n & 0 & 0 & 0 \\ 0 & -n & 0 & 0 \\ 0 & 0 & -(n+f) & -nf \\ 0 & 0 & 1 & 0 \end{bmatrix}$$

Preserves some depth info (z coordinate)

Z -coordinate is unchanged at near and far boundaries
Transforms the frustum into an orthographic view volume.

3.14 Question 14: Done

14. What is meant by a normalizing transform and what two substeps can be used to build the normalizing transform for the orthographic projection case described in lecture? A good conceptual description is sufficient; exact transforms are not requested.

3.14.1 Dr. Borst's Answer

Normalizing transform takes a box in the view and transforms it to $[-1, 1] \times [-1, 1] \times [-1, 1]$. Transform the center to the origin and scale.

3.15 Question 15: Done

15. In the OpenGL pipeline, after the modelview matrix is applied to a vertex, the result is that the vertex is described with respect to which coordinate system?

ModelView Matrix is the composition of all of the transformations from the camera to the node being rendered.

Answer: Camera View

3.15.1 Note from Marcus Shannon for #15 and #16

Q15 & Q16: This is a trivial point to make but the Camera View, from my understanding, is equivalent to the Eye Coordinate System.

3.16 Question 16: Done

16. The six common parameters (near, far, left, ...) of a perspective frustum description are coordinates describing the viewing volume with respect to which coordinate system?

Answer: Camera View

3.16.1 First Guess, Brad Burkman, 9:03pm 14 November

Eye (camera) coordinate system.

3.17 Question 17: To Do

17. Below, circle all correct answers for questions about the illumination equation from lecture.

1) Which of the following vectors is (are) used in computing the ambient lighting term?

Direction to light Surface normal Direction to viewer None

2) Which of the following vectors is (are) used in computing the diffuse lighting term?

Direction to light Surface normal Direction to viewer None

3) Which of the following vectors is (are) used in computing the specular lighting term?

Direction to light Surface normal Direction to viewer None

3.17.1 Marcus Shannon's Answer

Q17: This is simply about looking at the Phong Illumination Equation and identifying what vectors come into play with what parts.

- Ambient light only considers: Reflection Coefficient (K_a), Ambient Light Intensity (I_a), & RGB of Object (O_d).
- Therefore 1) is None.
- Diffuse considers: Diffuse Coefficient (K_d), Diffuse Light Intensity (I_d), Normalized Light Normal (N with hat), & Normalized Light Direction (L with hat).
- Therefore 2) is Direction to light & Surface Normal.
- Specular considers: Specular Coefficient (K_s), Specular Object (O_s), Specular Exponent (n), Normalized Reflection (R with hat), & Direction to Viewer (V with hat).
- Initially, it looks as though the answer is the same as 2) however R (with hat) expands into using N (with hat) & L (with hat).
- Therefore 3) is Direction to light, Surface Normal, & Direction to Viewer.

3.18 Question 18: To Do

18. Describe why a triangle may look different with Phong shading than with Gouraud shading, and include a sketch of shaded triangles that illustrate the difference you discuss.

3.18.1 Marcus Shannon's Solution

Q18: Pulled from the slides (paraphrased):

- Gouraud shading will evaluate at polygon vertices & interpolate resulting color across the polygon.
- Phong shading will interpolate surface normals from vertices & then apply lighting equation per-pixel.

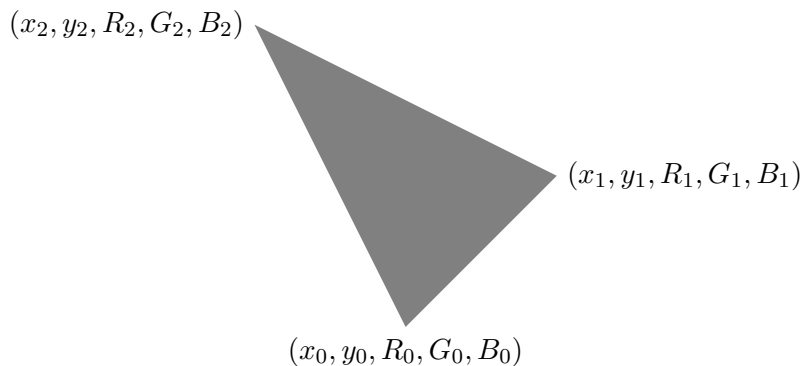
- For triangle shading, review the second set of slides provided on moodle and scroll down a bit.

3.19 Question 19: Not on Exam

19. ~~Sketch a scene with two or three polygons for which the painter's algorithm would be insufficient for visible surface determination.~~

3.20 Question 20: To Fix

20. Consider scan conversion of the illustrated triangle. Assume that scan conversion is done from the bottom up, that the triangle crosses several scan lines, and that the geometry matches the illustration.



- 1) In terms of the vertex coordinates and colors labeled on the diagram, give the coordinates and RGB color values for the first pixel to be colored.
- 2) In terms of the vertex coordinates and colors labeled on the diagram, give the coordinates and RGB values for the second pixel to be colored.

3.20.1 First Guess, Brad Burkman, 9:23pm 14 November

First pixel to be colored is the bottom.

$$(x_0, y_0, R_0, G_0, B_0)$$

Second pixel to be colored is above left of that.

$$m = \frac{y_2 - y_0}{x_2 - x_0} = \frac{\Delta y}{\Delta x}$$

Since we're going up one pixel, $\Delta y = 1$, so we're interested in Δx .

$$\Delta x = \frac{x_2 - x_0}{y_2 - y_0}$$

and we're going to round it up (on the left, down on the right), because we're talking about pixel values, which are integers.

$$\Delta x = \left\lceil \frac{x_2 - x_0}{y_2 - y_0} \right\rceil$$

Change in colors works the same way.

$$\Delta R = \frac{R_2 - R_0}{y_2 - y_0}$$

So the coordinates and colors of the second point to be colored are:

$$\left(x_0 + \left\lceil \frac{x_2 - x_0}{y_2 - y_0} \right\rceil, y_0 + 1, R_0 + \frac{R_2 - R_0}{y_2 - y_0}, G_0 + \frac{G_2 - G_0}{y_2 - y_0}, B_0 + \frac{B_2 - B_0}{y_2 - y_0} \right)$$

3.20.2 Changes based on Dr. Borst's Discussion

I realize I had forgotten about the offset between the line and the pixel.

3.20.3 Marcus Shannon's Reply to Brad's Solution

Q20: Almost got the same answer, I pulled slightly different equations from my notes:

- To give an example to show the deviation in our solution:
- I defined R for the second pixel colored to be

$$R = R_0 + \frac{R_1 - R_0}{y_1 - y_0}$$

- Almost all instances where you used a subscript of 2, I used a subscript of 1 (for the scope of this solution).
- Which of us is correct, I honestly couldn't say.