

Project n.3

Final report due November 29

- ❖ Generate a vector of N random numbers distributed according to a power-law probability density function between $x=x_{\min}$ and $x=\infty$, with index α . (use quantile function). (e.g. a Salpeter mass function for $m > 1 M_{\odot}$). Compare the estimates of α obtained with the following methods
 - ❖ Linear least square (histogram)
 - ❖ Linear least square (histogram; weighted by the counts of each bin; try different binnings see Maiz-Apellaniz & Ubeda 2005)
 - ❖ Linear least square of the empirical cumulative distribution function.
 - ❖ MLE estimator.
 - ❖ Moments
 - ❖ Non-linear least square.
- ❖ Find the distribution of α from n (e.g. $n=100$) different random realizations
- ❖ Explore the dependence of the results on N

or
- ❖ Explore the dependence of the results on α
- ❖ Python and R

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- ❖ Repeat homework n.2 (powerlaw.dat) using
 - ❖ Linear least square (histogram; e.g. weighted by the counts of each bin; try different binnings: e.g. equal-count binning see Maiz-Apellaniz & Ubeda 2005)
 - ❖ Linear least square of the empirical cumulative distribution function.
 - ❖ MLE estimator.
 - ❖ Moments
- ❖ Find one example of a power-law distribution in the astronomy literature: how was the distribution calculated? How was the index of the power-law calculated?

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Progress report due November 15

- ❖ Find one example of a power-law distribution in the astronomy literature: how was the distribution calculated? How was the index of the power-law calculated? Summarize what you found in one figure.
- ❖ Project progress report

Power-law

- ❖ p.d.f. $f(x) = \alpha b^\alpha / x^{(\alpha+1)}$ For $x \geq b$
- ❖ c.d.f. $F(x) = 1 - b^\alpha / x^\alpha$
- ❖ Quantile function $q(r) = b / (1-r)^{1/\alpha}$ $r \in [0, 1)$