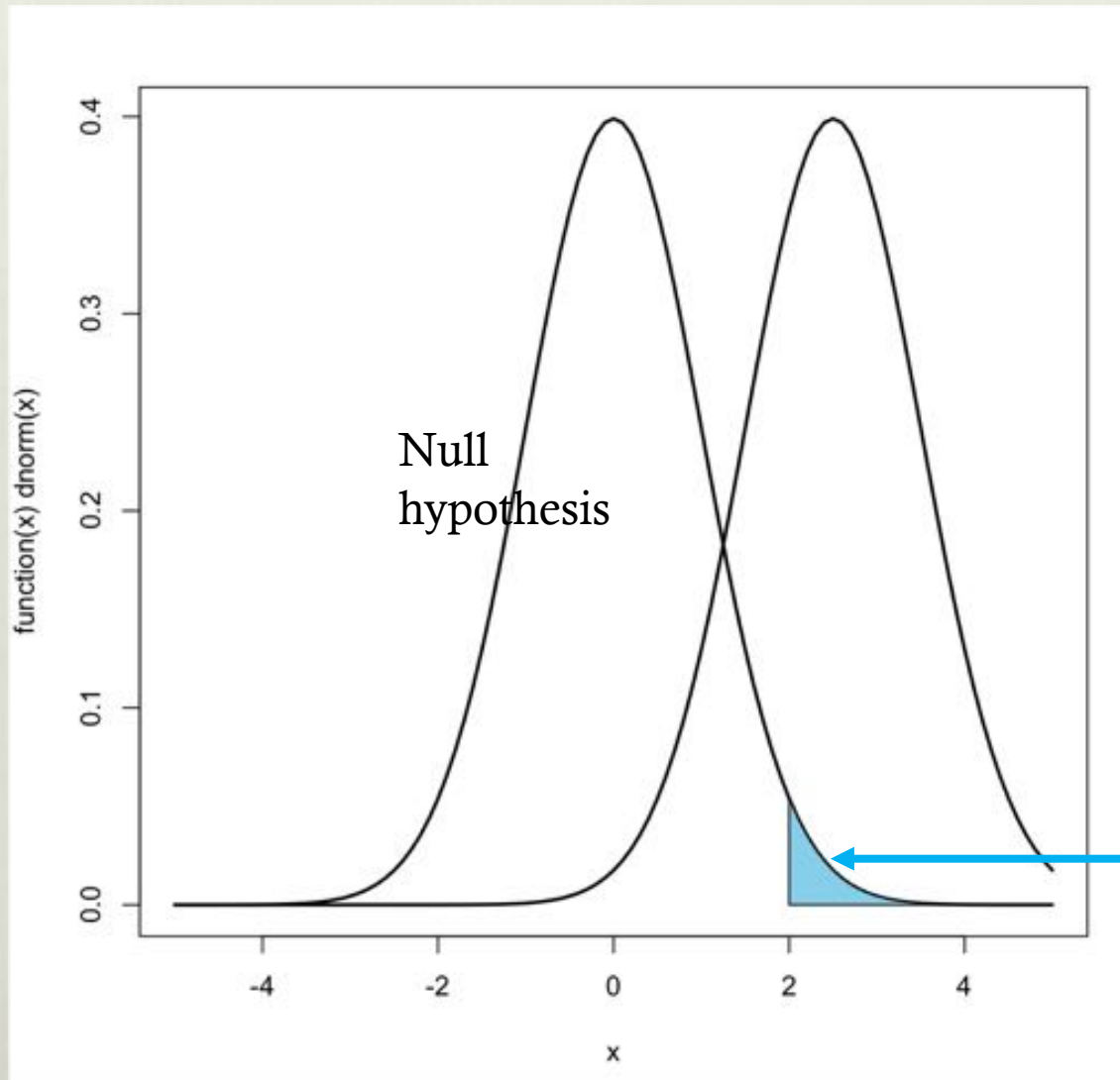


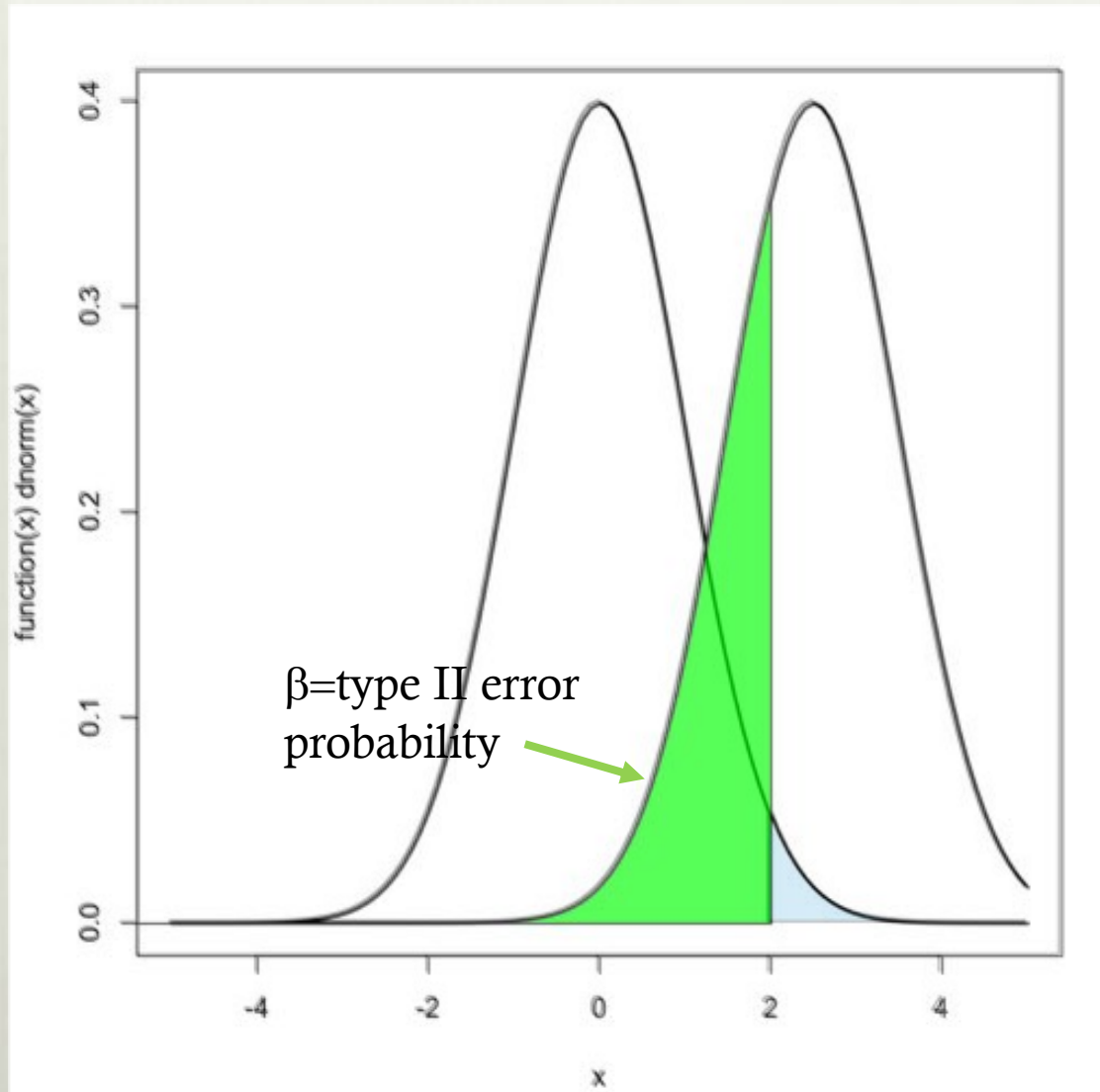
Graduate Seminar-  
A 780  
Astrostatistics and  
Scientific Computing

# Power analysis



$\alpha$ =type I error probability

# Power analysis



# Type II error

Fail to reject the null hypothesis when the alternative hypothesis is true.

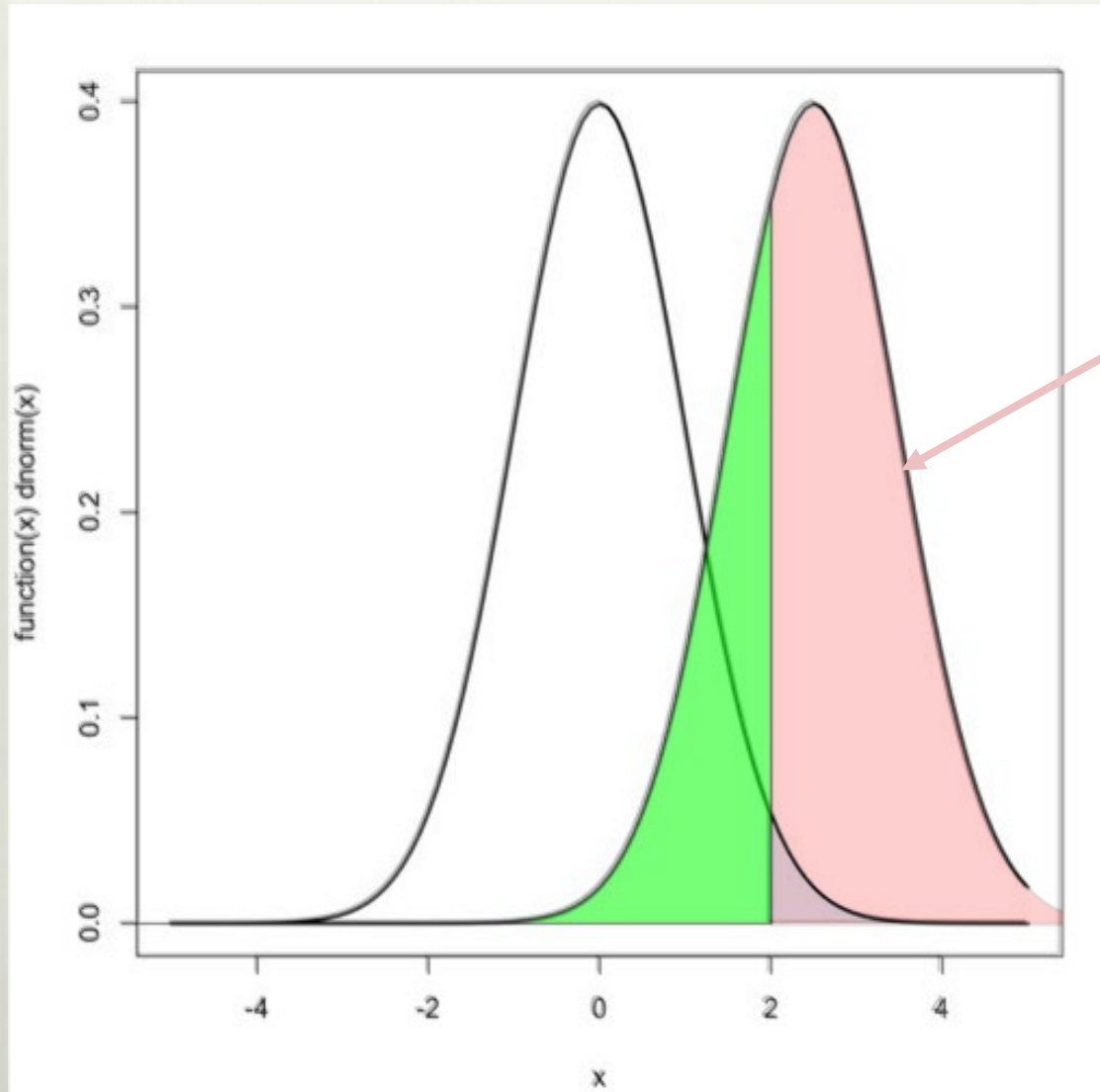
$\beta$  = Probability (type II error)

Power of hypothesis test:

Probability of rejecting the null hypothesis  
when the alternative hypothesis is true

$$= 1 - \beta$$

# Power analysis



$1-\beta$ = statistical power

# Project 1 - Appendix

- ❖ Power analysis
  - ❖ Assuming  $\text{abs}(m1-m2)=0.2$  and  $sd=1$  for  $N=50$  and for  $N=100$ . With a power analysis, calculate the expected fraction of cases in which your statistical test failed to reject the null hypothesis (for `meanfilesA.tar` and `meanfilesB.tar`).
- ❖ What fraction of the statistically significant results you found for `meanfilesE.tar` are actually not real?
  - ❖ Answer this question with a power analysis by assuming that  $\text{abs}(m1-m2)=0.25$ ,  $sd=1$  for 40 per cent of the cases.

# Project 1 - Appendix

- ❖ Generate 100 samples with  $n$  numbers from a normal distribution with mean =1 and sd=1 (subsample 1) and  $n$  numbers from a normal distribution with mean =1.2 and sd=1 (subsample 2)
- ❖ t.test for  $(m1-m2)=0$ ,  $\alpha=0.05$ , alternative m1 different from m2 (assume equal variances)
- ❖ calculate  $\text{mean}(m1-m2)$  of all the statistically significant results (i.e. of all the cases for which  $p\text{-value}<0.05$ ).
- ❖ Effect size is defined as  $d=\text{abs}(m1-m2)/sd$
- ❖ power analysis for effect size 0.2; what is the power of the test for effect size=0.2?
- ❖ Plot ' $\text{mean}(m1-m2)$  of all the statistically significant tests' vs  $n$
- ❖ Plot ' $\text{mean}(m1-m2)$  of all the statistically significant tests' vs power of the test
- ❖ For  $n=10$  to 1000 in steps of 10

# Power analysis in R

- ❖ `power.t.test`
- ❖ ..or `library(pwr) pwr.t.test, pwr.t2n.test`

Effect size needed for `pwr.t.test` =  $\text{abs}(m1 - m2) / (\text{pooled sd})$

```
library(lsr)
```

```
d = cohensD(x, y)
```

```
pwr.t.test(d, ...
```



# Python

❖ `statsmodels.stats.power.tt_ind_solve_power`