

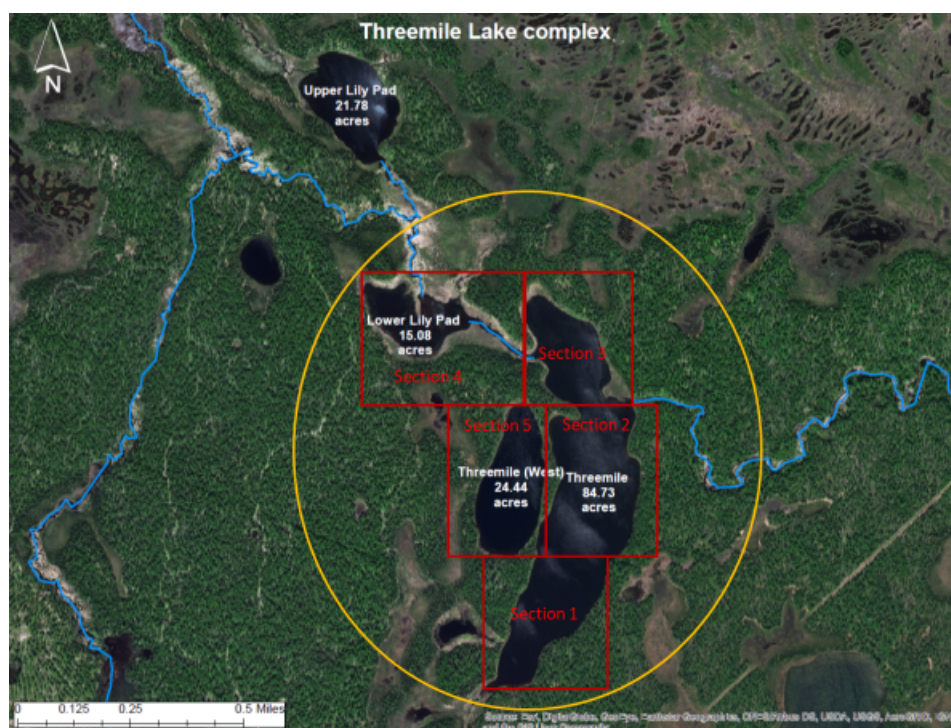
Threemile Mark-Recapture Analysis

Ben Buzzee, Biometrician, ADFG

August 2, 2018

Background

ADFG and the Tyonek Tribal Conservation District conducted a mark-recapture study on the Threemile Lake complex in Beluga, AK during June of 2018. We are interested in estimating the number of northern pike $\geq 300\text{mm}$ present at the time of our study. The lake complex was broken down into 6 sections in order to ensure uniform sampling effort and help check the assumptions. Note: Upply Lilly is section 6 in the analysis.



Assumptions

In order to our estimate to be unbiased, certain assumptions must be met:

- 1) the population is closed (northern pike do not enter the population via growth or immigration, or leave the population via death or emigration during the experiment)
- 2) all pike have a similar probability of capture during the first event, or during the second event, or marked and unmarked fish will mix completely between events
- 3) marking of pike will not affect the probability of capture during the second event
- 4) pike will not lose their marks between events and tagged fish will be correctly identified during the second event

There are no diagnostic tests available for assumptions 1, 3 and 4. We designed the study to ensure those assumptions would be met as best we could and believe they are reasonable to assume going forward.

The relevant aspects of design for assumptions 1, 3, and 4 were:

1. Fyke nets were used to prevent migration at the lake inlet and outlets. We also limited the time between the mark and recapture events to two weeks to minimize the effects of death and growth recruitment.
2. Pike that seemed overly stressed due to marking were culled. Otherwise pike were tagged and released as quickly as possible. We are making the assumption that the fishing techniques used (hook and line, gillnets), and the tag itself, did not change the probability of a pike being recaptured.
3. All marked pike were double tagged with a unique tag number and fin clip. Because of this, we know tag loss was minimal. Pike were also tagged in a standard location and thoroughly inspected for both types of tags.

Assumption 2 Diagnostics

Assumption 2 states: $P(\text{capture})$ is the same for all fish during the first event, OR $P(\text{capture})$ is the same for all fish during the second event, OR fish mix completely between events.

We will check to determine whether $P(\text{capture})$ varies according to size (KS tests), or if $P(\text{capture})$ varies according to location (chi-square tests). For the following hypothesis tests, the null hypothesis will be that the assumption is met. So a small p-value is evidence that the assumption was NOT met. First we will look at the KS tests to check for differences in $p(\text{capture})$ due to length:

Size Selectivity and Kolmogorov-Smirnov Tests

H_0 : Fish captured during the **first event** and fish that were **recaptured** share the same length distribution.

```
##  
## Two-sample Kolmogorov-Smirnov test  
##  
## data: M_len and R_len - 10  
## D = 0.12196, p-value = 0.00703  
## alternative hypothesis: two-sided
```

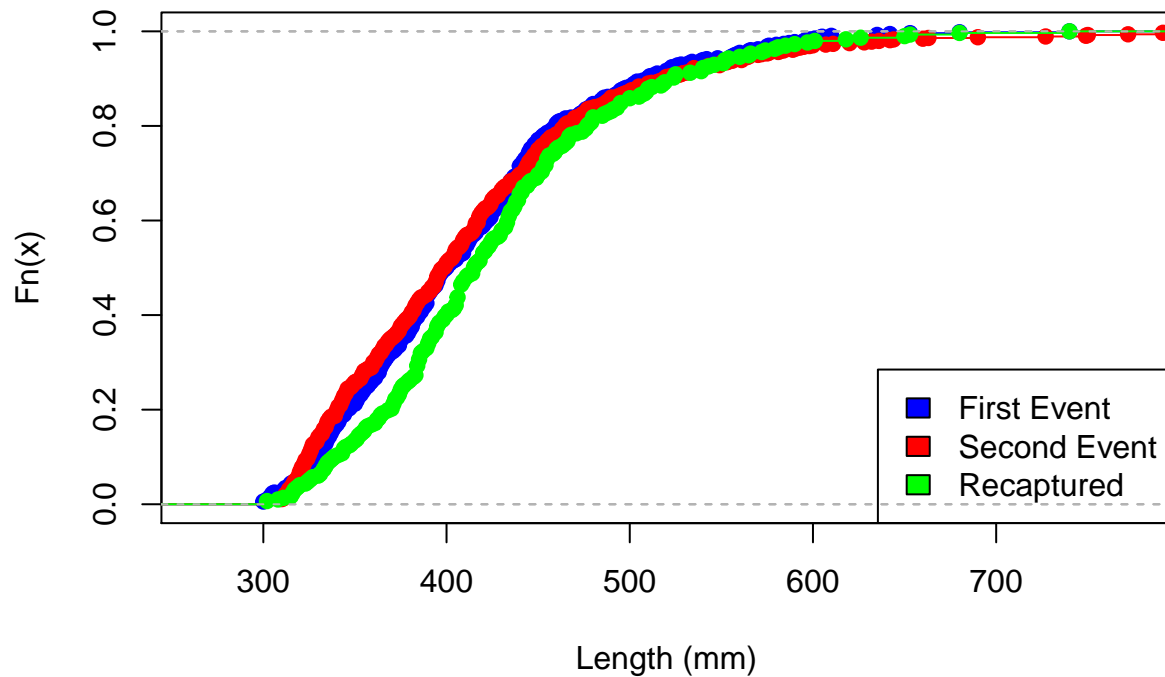
H_0 : Fish captured during the **second event** and fish that were **recaptured** share the same length distribution.

```
##  
## Two-sample Kolmogorov-Smirnov test  
##  
## data: C_len and R_len - 10  
## D = 0.14971, p-value = 0.0002217  
## alternative hypothesis: two-sided
```

H_0 : Fish captured during the **first event** and fish captured during the **second event** share the same length distribution.

```
##  
## Two-sample Kolmogorov-Smirnov test  
##  
## data: C_len and M_len  
## D = 0.046825, p-value = 0.5492  
## alternative hypothesis: two-sided
```

Empirical Cumulative Distributions



KS Tests Results

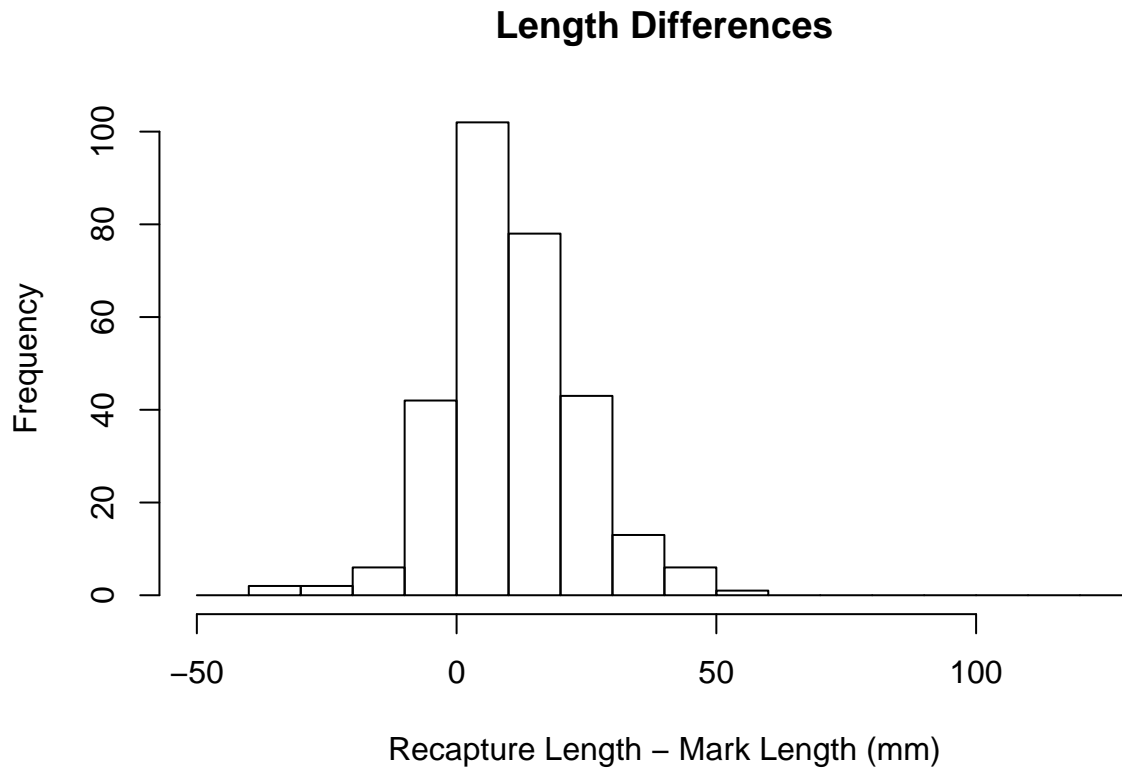
From the tests and the graph, we see that recaptured fish had a tendency to be larger than fish capture during either individual event.

The Problem of Growth

One issue that could skew the results of our KS tests is fish growth between events. If the fish grew a substantial amount between sampling periods, then there might be fish that were recaptured at 300mm that were not 300mm during the initial mark event. Additionally, the entire population of fish present during the recapture event would be larger than during the initial event.

We can look at differences in the lengths of recaptured fish to determine whether there was significant growth.

```
## [1] 10
```



Spatial Selectivity and Chi-Square Tests

The other way assumption 2 could be violated is if $p(\text{capture})$ varies according to location during each event. We will compare the number of fish caught during both events and the number recaptured across locations to check for this violation. The null hypothesis' are:

- The probability of a fish moving from stratum i to stratum j is the same or all i and j (complete mixing).
- The probability of capture was the same for each section during the first event.
- The probability of capture was the same for each section during the second event.

Again, for these tests, a low p -value is evidence that the assumption was NOT met.

```
## MIXING TEST
## H0: Movement probabilities from stratum i to stratum j are the same among sections (all theta_ij = t)
##
##      1  2  3  4  5  6 not recaptured
## 1 24  7  0  1  0  0                  11
## 2 19 42 27  6  0  0                  40
## 3  8 17 47  1  0  0                  65
## 4  3  3  4 65  0  0                  87
## 5  0  0  0  0 12  0                  14
## 6  0  0  0  2  0  9                  15
##
## X-squared:  767.3002   df:  30   p-val:  4.301984e-142
##
```

```

## EQUAL PROPORTIONS TEST
## H0: Equal probability of capture among n1 strata (all p_i equal)
##
##           1  2  3  4  5  6
## recaptured 54 69 78 75 12  9
## unmarked   38 63 89 92  9 56
##
## X-squared: 36.2602  df:  5  p-val: 8.425101e-07
##
## COMPLETE MIXING TEST
## H0: Equal probability of recapture among n2 strata (all p_j equal)
##
##           1  2  3  4  5  6
## recaptured   32 94 73 75 12 11
## not recaptured 11 40 65 87 14 15
##
## X-squared: 26.55302  df:  5  p-val: 6.968881e-05
##

```

Chi-Square Test Results

From the above tests, we have good evidence that assumption 2 was not met. But given the layout of the lake, this was to be expected. Some areas of the lake complex are isolated from other areas.

We do know that the main lake complex was comprised of 4 interconnected subsections, so lets test if the probability of capture was similar among the four main sections.

```

## MIXING TEST
## H0: Movement probabilities from stratum i to stratum j are the same among sections (all theta_ij = t)
##
##   1  2  3  4 not recaptured
## 1 24  7  0  1              11
## 2 19 42 27  6              40
## 3  8 17 47  1              65
## 4  3  3  4 65              87
##
## X-squared: 303.9818  df: 12  p-val: 6.847442e-58
##
## EQUAL PROPORTIONS TEST
## H0: Equal probability of capture among n1 strata (all p_i equal)
##
##           1  2  3  4
## recaptured 54 69 78 73
## unmarked   38 63 89 92
##
## X-squared: 5.85387  df:  3  p-val: 0.1189403
##
## COMPLETE MIXING TEST
## H0: Equal probability of recapture among n2 strata (all p_j equal)
##
##           1  2  3  4
## recaptured   32 94 73 75
## not recaptured 11 40 65 87
##

```

```
## X-squared: 23.31815 df: 3 p-val: 3.466302e-05
##
```

Chi-Square Tests for 4 Main Lake Sections

From the above tests, we could reasonably conclude that the probability of capture was similar among the main 4 sections of the lake during the first sampling event. That leaves size stratification as the only issue.

But if, we limit our focus to the four main sections, is size selectivity still an issue? To find out, we will retest for size selectivity, only looking at pike caught in one of the main 4 sections.

```
##
## Two-sample Kolmogorov-Smirnov test
##
## data: M_len4 and R_len4
## D = 0.20459, p-value = 9.621e-07
## alternative hypothesis: two-sided

##
## Two-sample Kolmogorov-Smirnov test
##
## data: C_len4 and R_len4
## D = 0.15593, p-value = 0.0002672
## alternative hypothesis: two-sided
```

So even when looking only at the 4 main sections, there is still an issue of size selectivity.

To solve this issue, we will group fish into three size categories – small, medium, and large fish. For each of these size groups we will estimate abundance and the variance.

APPLY GROWTH CORRECTION to strata

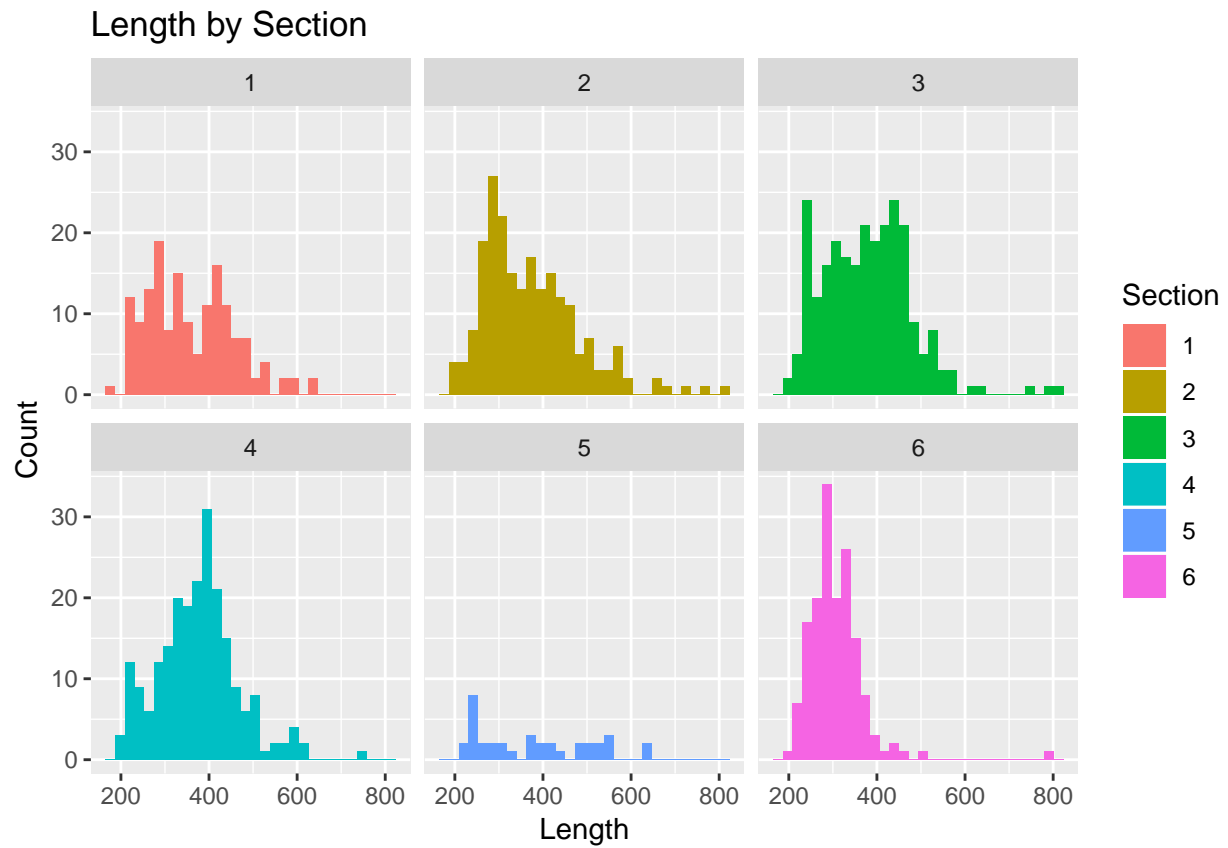
Final Estimates

```
## section      N      var      se
## 1      1-4 1063.4693 2634.00578 51.322566
## 2        5   45.5000   31.63314  5.624334
## 3        6  173.3333 1260.00000 35.496479
```

And our final interval estimate for all six sections:

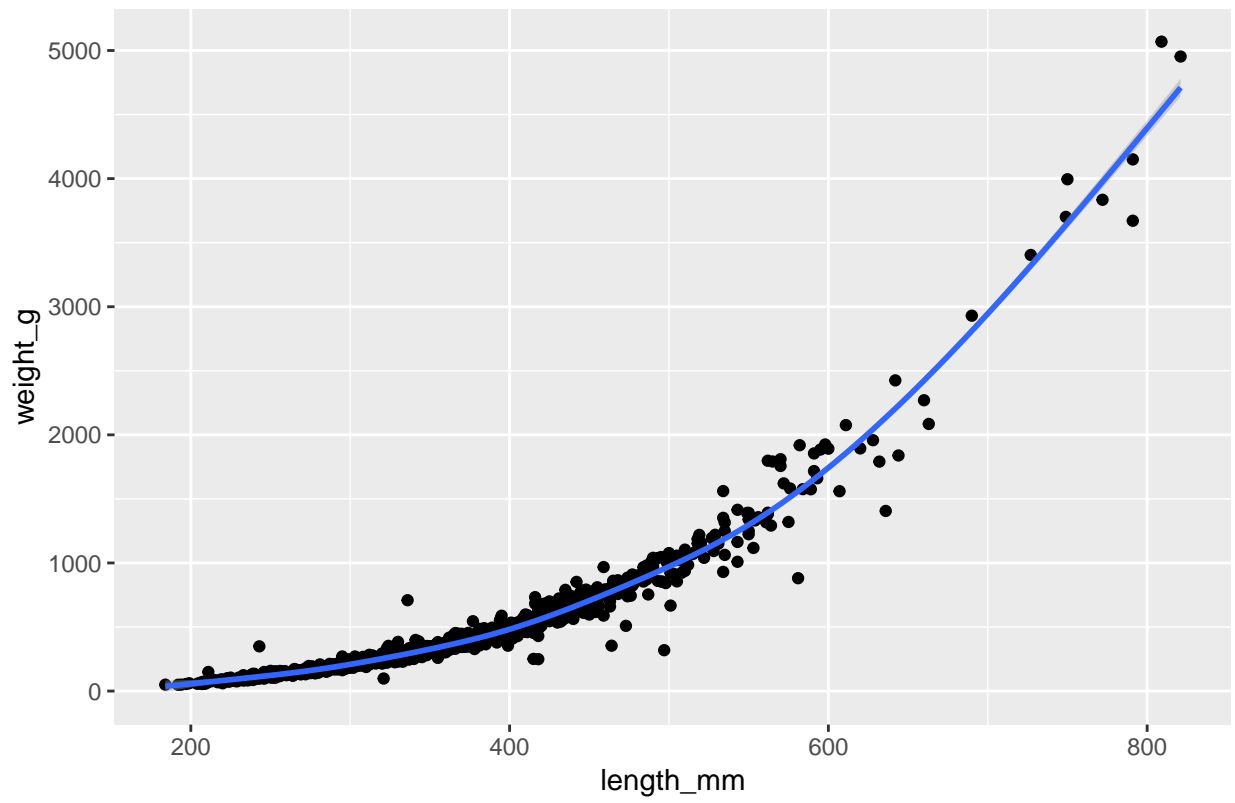
```
## [1] 1159.499 1405.106
```

Length Analysis



Assuming there is a healthy population of fish < 200 mm, an interested question is at what size does size-selectivity during sampling start? Are fish in the 200-220 mm range less likely to be caught? Or is 200 mm a hard cutoff?

Length and Weight



Diet

