$$\int_0^{+\infty} \int_0^{\pi} \int_0^{2\pi} R^2(r) Y^2(\theta, \varphi) r^2 dr d\theta d\varphi = 1$$
$$\iiint_0^{2\pi} R^2(r) Y^2(\theta, \varphi) r^2 dr d\theta d\varphi = 1$$