$$||\dot{\vec{r}}(t)||_{2} \hat{t} = \dot{\vec{r}}(t) \neq \frac{d||\dot{\vec{r}}(t)||_{2}}{dt} \hat{t}$$
where,  $\hat{t} = \frac{1}{\sqrt{1 + f'(x)^{2}}} \begin{pmatrix} 1 \\ f'(x) \end{pmatrix}$