## Extra Practice Questions for Midterm 1

1. (a) What would be the result from running the following code?

```
all(c(1,2,3,4,5) > 0)
```

(b) Consider the following function

```
a_function <- function(n) {
  out <- 0
  for (i in 1:n) {
    out <- out + i^2
  }
  out
}</pre>
```

If you run the following code, what will it output?

```
a_function(5)
```

- 2. Suppose there are two random variables X and Y.
  - a) If you know that X and Y are independent, do you know what their covariance is equal to? Explain. If yes, what is the covariance equal to?
  - b) If you know that cov(X,Y) = 0, are X and Y independent? Explain.
  - c) If you know that cov(X,Y) = 1, are X and Y independent? Explain.

- 3. Suppose that  $X_1$  and  $X_2$  are two random variables such that  $\mathbb{E}[X_1] = 0$ ,  $\mathbb{E}[X_2] = 5$ ,  $\text{var}(X_1) = 1$ ,  $\text{var}(X_2) = 10$  and  $\text{cov}(X_1, X_2) = -1$ . Suppose that  $Y = X_1 + X_2$ .
  - a) What is  $\mathbb{E}[Y]$ ?
  - b) What is var(Y)?

4. Consider a random variable Y that is equal to a firm's profits (in thousands of dollars) and another random variable X that is equal to firm's number of employees. Suppose you know that

$$\mathbb{E}[Y|X=x] = 50 + 10x$$

- a) Explain how to interpret  $\mathbb{E}[Y|X=x]$ .
- b) What is  $\mathbb{E}[Y|X=10]$ ?
- c) Suppose that var(Y) = 40,  $\mathbb{E}[X] = 30$ , and var(Y) = 20, calculate  $\mathbb{E}[Y]$ .

- 5. Suppose that we have a random sample of n observations of X and Y.
  - a) Suppose that you want to estimate the covariance between X and Y using the data that we have. Propose an estimator for the covariance. **Hint:** Try using the analogy principle and the expression  $cov(X,Y) = \mathbb{E}[XY] \mathbb{E}[X]\mathbb{E}[Y]$ .
  - b) Alternatively, the definition of covariance is  $cov(X,Y) = \mathbb{E}[(X \mathbb{E}[X])(Y \mathbb{E}[Y])]$ . Propose an estimator for the covariance based on this expression. Would you expect this to give you the same estimate of the covariance as in part a?