IS 622 Week 11 Homework

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9.3.1

Figure 9.8 is a utility matrix, representing the ratings, on a 1–5 star scale, of eight items, a through h, by three users A, B, and C. Compute the following from the data of this matrix.

	a	\boldsymbol{b}	\boldsymbol{c}	d	e	f	\boldsymbol{g}	h
\boldsymbol{A}	4	5		5	1		3	2
B		3	4	3	1	2	1	
$egin{array}{c} A \ B \ C \end{array}$	2		1	3		4	5	3

(a) Treating the utility matrix as boolean, compute the Jaccard distance between each pair of users.

```
df \leftarrow data.frame(a = c(4, NA, 2),
                  b = c(5, 3, NA),
                   c = c(NA, 4, 1),
                   d = c(5, 3, 3),
                   e = c(1, 1, NA),
                   f = c(NA, 2, 4),
                   g = c(3, 1, 5),
                   h = c(2, NA, 3))
rownames(df) <- c("A", "B", "C")
cn <- colnames(df)</pre>
user.pairs <- as.data.frame(t(combn(rownames(df), 2)))</pre>
colnames(user.pairs) <- c("User1", "User2")</pre>
jaccard <- function(v1, v2) {</pre>
  length(intersect(v1, v2)) / length(union(v1, v2))
inset <- function(j) {!is.na(j) & as.logical(j)}</pre>
jd <- user.pairs</pre>
jd["Jaccard.Distance"] <-</pre>
  apply(user.pairs, 1, function(i) {
    s1 <- cn[sapply(df[i[1], ], inset)]</pre>
    s2 <- cn[sapply(df[i[2], ], inset)]</pre>
    jaccard(s1, s2)
})
jd
```

User1 User2 Jaccard.Distance

```
## 1 A B 0.5
## 2 A C 0.5
## 3 B C 0.5
```

(b) Repeat Part (a), but use the cosine distance.

```
len <- function(v) { sqrt(sum(v**2)) }
cosine.dist <- function(v1, v2) {
  v1[is.na(v1)] <- 0
  v2[is.na(v2)] <- 0
  (as.numeric(v1) %*% as.numeric(v2)) / (len(v1) * len(v2))
}

# Apply distance function
cd <- user.pairs
cd["Cosine.Distance"] <-
  apply(user.pairs, 1, function(i) {
    cosine.dist(df[i[1], ], df[i[2], ])
})

# Format output
cd</pre>
```

```
## User1 User2 Cosine.Distance
## 1 A B 0.6010408
## 2 A C 0.6149187
## 3 B C 0.5138701
```

(c) Treat ratings of 3, 4, and 5 as 1 and 1, 2, and blank as 0. Compute the Jaccard distance between each pair of users.

```
binrating <- function(i) {ifelse(i %in% c(3, 4, 5), TRUE, FALSE)}

# Apply distance function
jd.c <- user.pairs
jd.c["Jaccard.Distance"] <-
    apply(user.pairs, 1, function(i) {
    s1 <- cn[sapply(df[i[1], ], binrating)]
    s2 <- cn[sapply(df[i[2], ], binrating)]
    jaccard(s1, s2)
})

jd.c</pre>
```

```
## User1 User2 Jaccard.Distance
## 1 A B 0.4000000
## 2 A C 0.3333333
## 3 B C 0.1666667
```

(d) Repeat Part (c), but use the cosine distance.

```
cd.d <- user.pairs</pre>
cd.d["Cosine.Distance"] <-</pre>
  apply(user.pairs, 1, function(i) {
    v1 <- binrating(df[i[1], ])</pre>
    v2 <- binrating(df[i[2], ])</pre>
    cosine.dist(v1, v2)
  })
# Format output
cd.d
     User1 User2 Cosine.Distance
## 1
                В
                         0.5773503
          Α
                С
## 2
          Α
                         0.5000000
## 3
          В
                С
                         0.2886751
 (e) Normalize the matrix by subtracting from each nonblank entry the average value for its user.
df.normalized <- t(apply(df, 1, function(i) {</pre>
  i - mean(i, na.rm=TRUE)
}))
df.normalized
##
                          b
                                     С
                                                           е
                                                                        f
## A 0.6666667 1.6666667
                                    NA 1.6666667 -2.333333
                                                                      NA -0.3333333
              NA 0.6666667 1.666667 0.6666667 -1.333333 -0.3333333 -1.3333333
## C -1.0000000
                        NA -2.000000 0.0000000
                                                          NA 1.0000000 2.0000000
##
## A -1.333333
## B
## C 0.000000
  (f) Using the normalized matrix from Part (e), compute the cosine distance between each pair of users.
df.normalized[is.na(df.normalized)] <- 0</pre>
# Apply distance function
cd.f <- user.pairs</pre>
cd.f["Cosine.Distance"] <-</pre>
  apply(user.pairs, 1, function(i) {
    v1 <- df.normalized[i[1], ]</pre>
    v2 <- df.normalized[i[2], ]</pre>
    cosine.dist(v1, v2)
  })
# Format output
cd.f
##
     User1 User2 Cosine.Distance
## 1
          Α
                В
                       0.5843065
                С
## 2
          Α
                        -0.1154701
```

3

С

-0.7395740