IS622 Week 4 Homework

Ben Arancibia

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3.1.3 Suppose we have a universal set U of n elements, and we choose two subsets S and T at random, each with m of the n elements. What is the expected value of the Jaccard similarity of S and T?

Each item in T has an m / n chance of also being in S. The expected number of items common to S & T is therefore m^2 / n.

Exp. Jaccard Similarity = (No. of common items) / (Size of T + Size of S - Number of common items) = <math>m / (2n - m) after simplification.

3.3.3

(a) Compute the minhash signature for each column if we use the following three hash functions: $h1(x) = 2x + 1 \mod 6$; $h2(x) = 3x + 2 \mod 6$; $h3(x) = 5x + 2 \mod 6$.

```
s1 <- c(0,0,1,0,0,1); s2 <- c(1,1,0,0,0,0); s3 <- c(0,0,0,1,1,0)
s4 <- c(1,0,1,0,1,0); element <- c(0,1,2,3,4,5)
h1 <- function(x) { (2*x + 1) %% 6 }
h2 <- function(x) { (3*x + 2) %% 6 }
h3 <- function(x) { (5*x + 2) %% 6 }

hashlist <- list(h1,h2,h3)
setlist <- list(s1,s2,s3,s4)

results <- computeMinhashSigs(hashlist, setlist)

s1 <- c(2,5); s2 <- c(0,1); s3 <- c(3,4); s4 <- c(0,2,4)
setlist <- list(s1,s2,s3,s4)

result <- computeMinhashSigs(hashlist, setlist)
result <- computeMinhashSigs(hashlist, setlist)
result</pre>
```

```
## [,1] [,2] [,3] [,4]
## [1,] 5 1 1 1
## [2,] 2 2 2 2
## [3,] 0 1 4 0
```

identical

It looks like the h2 has believes each row is identical while h1 believes they look nearly

(b) Which of these hash functions are true permutations?

```
hashlist <- list("h1"=h1,"h2"=h2,"h3"=h3)
row_count <- 5
hashPermuteDirect(hashlist, row_count)</pre>
```

```
## [,1] [,2]
## [1,] "h1" "3"
## [2,] "h2" "2"
## [3,] "h3" "6"
```

(c) How close are the estimated Jaccard similarities for the six pairs of columns to the true Jaccard similarities?

I think they are close, but not sure on my calculations...functions might not be working correctly

3.5.5

```
Compute the cosines of the angles between each of the following pairs of vectors.
angle <- function(x,y){</pre>
  dot.prod <- x%*%y
  norm.x <- norm(x,type="2")</pre>
  norm.y <- norm(y,type="2")</pre>
  theta <- acos(dot.prod / (norm.x * norm.y))</pre>
  as.numeric(theta)
 (a) (3,-1,2) and (-2,3,1).
x \leftarrow as.matrix(c(3,-1,2))
y <- as.matrix(c(-2,3,1))
angle(t(x),y)
## [1] 2.094395
 (b) (1,2,3)and(2,4,6).
x <- as.matrix(c(1,2,3))
y <- as.matrix(c(2,4,6))</pre>
angle(t(x),y)
## [1] 2.107342e-08
 (c) (5,0,-4) and (-1,-6,2).
x <- as.matrix(c(5,0,-4))
y \leftarrow as.matrix(c(-1,-6,2))
angle(t(x),y)
## [1] 1.893438
 (d) (0,1,1,0,1,1) and (0,0,1,0,0,0).
```

```
x <- as.matrix(c(0,1,1,0,1,1))
y <- as.matrix(c(0,0,1,0,0,0))
angle(t(x),y)</pre>
```

[1] 1.047198

3.7.1

Suppose we construct the basic family of six locality-sensitive functions for vectors of length six. For each pair of the vectors 000000, 110011, 010101, and 011100, which of the six functions makes them candidates?

I don't think this question has an answer….all of the six functions have a random parameter so their output varies