

# From Quantized Chern Transport to Quantum Technologies: Nonlinear Topological Pumping

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Simulations on *nonlinear bosonic* topological transport in Rice–Mele optical lattices are presented, computing *Chern number* from Zak phases of time-evolved ground states over full pump cycles to predict quantized displacement per cycle. The approach is based on soliton solutions to the Hubber model for the Thouless pump [1]. These results delineate transport/no-transport regimes versus drive frequency and interaction strength, identifying an adiabatic window with integer pumping ( $C \approx 1$ ) and degradation under stronger nonlinearity or nonadiabatic drive, in line with recent observations of nonlinear and fractional Thouless pumping of solitons [2, 3]. Framed for quantum technology, we translate design knobs into device-level metrics and emphasize two representative applications: (i) reliable qubit/state transfer via dimerized topological chains [4]; and (ii) topologically protected memory based on surface-code architectures, from foundational proposals to recent system-level demonstrations of improving logical lifetimes with increasing code size [5].

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