

## Problem 1:

Let's compare some basic math functions to refresh our memory. For each of the following, just write which function is *asymptotically greater* (So, you should be thinking about your asymptotic notations!). Show your reasoning for the same.

1.  $10000000000n^2$  vs  $n^3$  in the long run  $n^3$  will be greater because "10000000000" is a finite number.
2.  $n^2 \log(n)$  vs  $n(\log(n))^{10}$  the  $n^2 \log(n)$  is greater than  $n(\log(n))^{10}$  because it is a quadratic function and the  $n(\log(n))^{10}$  is linear.
3.  $N^{\log n}$  vs  $2^{\sqrt{n}}$  the  $2^{\sqrt{n}}$  function will be greater than  $N^{\log n}$  for sufficiently large values of  $n$  because the logarithmic exponent causes the growth to be sub-exponential.
4.  $2^n$  vs  $2^{2n}$  The  $2^{2n}$  is greater because it is double the exponential growth.

## Problem 2:

Now let's examine some [pseudo]code and apply asymptotic notation to it.

```
isPrime(n) :  
    for(i = 2, i*i <= n; i++) {  
        if(n % i == 0) {  
            return false  
        }  
    }  
    return true
```

What is the

1. Best Case:  $O(1)$
2. Worst Case:  $O(\sqrt{n})$
3. Average Case:  $O(\sqrt{n})$

Time complexity for the above function? Time complexity is  $O(\sqrt{n})$ .