# Package 'brittnu'

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Title Britt's Nu and Euclidean Krippendorff's Alpha

Version 0.2.0

**Description** This package computes two reliability coefficients. Britt's nu is used to assess reliability for data sets composed of multiple Dirichlet-distributed samples. Euclidean Krippendorff's alpha is used to assess reliability for Euclidean and compositional data that do not necessarily adhere to a Dirichlet distribution. These measures are especially useful for the cross-validation of topic models.

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brittnu

Britt's Nu

# **Description**

This function computes the Britt's nu reliability coefficient for data sets composed of multiple Dirichlet-distributed deviates, as described by Britt (under review).

## Usage

```
brittnu(
  Х,
  type = NA,
  alpha = NA,
  symmetric_alpha = FALSE,
  pairwise = TRUE,
  estimate_pairwise_alpha_from_joint = TRUE,
  force_bootstrapping = FALSE,
  shuffle = FALSE,
  shuffle_method = "rotational",
  shuffle_dimension = NA,
  clustering_method = "average",
  slow_clustering = FALSE,
  samples = 1000,
  sampling_method = "parametric",
  lower_bound = FALSE,
  convcrit = 1e-05,
  maxit = 1000,
  progress = FALSE,
  verbose = FALSE,
  different_documents = FALSE,
  zero = (10^{(-16)}),
  tol = 1e-04
```

# **Arguments**

Х

A list such that each element is either the output from a LDA function call or a 2D double vector with observations as the rows and each category within each observation as the columns (such that each row in the vector sums to 1)

type A string indicating the type of reliability being assessed, with permitted values

of "wt" (word-topic reliability), "td" (topic-document reliability), and NA; if x contains the output from multiple LDA function calls, this must be set to either

"wt" (word-topic reliability) or "td" (topic-document reliability)

alpha A list whose length is equal to the number of observations, with each list element

representing a vector comprising the concentration parameters for the categories in the corresponding observation; if this is NA and sampling\_method=="parametric",

the concentration parameters will be estimated from x

symmetric\_alpha

A boolean value indicating whether concentration parameters should be assumed to be unchanged between observations, which is common in many topic modeling procedures; this parameter only has an effect when alpha=NA

pairwise A boolean value indicating whether pairwise reliability between individual raters

should be computed; if FALSE, pairwise reliability will be ignored in order to re-

duce the time and memory complexity of the computation

estimate\_pairwise\_alpha\_from\_joint

A boolean value indicating, when estimating reliability for pairs of raters, whether each pair of raters should use the concentration parameters estimated across all raters (TRUE) or whether separate sets of concentration parameters should be estimated for each pair of raters (FALSE); this argument only has an effect when alpha==NA, and it is strongly suggested that the default value of TRUE be used

for this argument when possible

force\_bootstrapping

A boolean value indicating whether bootstrapping should be used to estimate expected differences rather than exactly computing them even if shuffle==FALSE

shuffle

A boolean value indicating whether or not the topics may have been shuffled into different sequences by each rater; if this is TRUE and shuffle\_dimension="rows", then the observations (rows) corresponding to each rater will be reordered to achieve a (local) optimal fit, whereas if this is TRUE and shuffle\_dimension="columns",

the categories (columns) will be reordered instead

shuffle\_method A string indicating what method ("rotational", "agglomerative", or "divisive") will be used to reorder topics

shuffle\_dimension

A string indicating whether "rows" or "columns" should be reordered; this argument only has an effect if shuffle==TRUE and type==NA

clustering\_method

A string indicating the criterion that will be used to merge or divide clusters if shuffle==TRUE and either shuffle\_method=="agglomerative" or shuffle\_method=="divisive permitted values are "average", "minimum", "maximum", "median", "centroid",

and "wald"

slow\_clustering

samples

A boolean value indicating whether the distances between clusters should be recalculated after each individual observation is added to the new cluster (TRUE), which can improve the cohesiveness of the resulting cluster, or whether all observations should be added to the new cluster without recomputing the distances between clusters after every addition (FALSE); this argument only has an effect

if shuffle==TRUE and shuffle\_method=="divisive"

An integer value indicating how many samples to use to estimate expected dif-

ferences when shuffle==TRUE

sampling\_method

A string indicating whether bootstrapped sampling should be performed using a "parametric" or "nonparametric" approach when shuffle==TRUE

lower\_bound

A boolean value indicating whether the lower bound of the expected differences (based on i.i.d. beta distributions) should be used rather than shuffling Dirichlet distributions to estimate the exact difference in every sample when

shuffle==TRUE

convcrit A numeric value indicating the threshold for convergence used to estimate con-

> centration parameters when alpha==NA, sampling\_method=="parametric", and concentration parameters could not be directly obtained from the output

of a LDA object provided as x

A numeric value indicating the maximum number of iterations used to estimate maxit

> concentration parameters when alpha==NA, sampling\_method=="parametric", and concentration parameters could not be directly obtained from the output of

a LDA object provided as x

progress A boolean value indicating whether progress updates should be provided when

estimating concentration parameters, if doing so is necessary

A boolean value indicating whether brittnu and its helper functions should proverbose

vide progress updates beyond the estimation of concentration parameters

different\_documents

A boolean value indicating, if each list element in x represents the output from an LDA function call, whether some raters used different sets of documents than

A numeric value; if type=="wt" and different\_documents==TRUE, then whenzero

ever a word appears in the portion of the corpus evaluated by some raters but not others, this value is assigned as its allocation to all topics for any rater that did

not evaluate that word

A numeric value representing the tolerance for observations whose sums are tol

greater than or less than 1; a warning message appears if the sum of the values

for any observation is further from 1 than this value

#### **Details**

One of the most important uses for Britt's nu is to assess the reliability of the allocations of words to topics or of topics to documents via topic modeling techniques such as latent Dirichlet allocation (LDA). When the results of multiple LDA cross-validation iterations obtained via LDA are provided as x, the type parameter should be set to either "wt" or "td" to indicate whether word-topic or topic-document reliability, respectively, should be assessed.

Crucially, different topic modeling cross-validation iterations (whether LDA or otherwise), which effectively represent distinct raters of the same data set, may result in the same topics appearing in a different sequence. As such, those topics, which may represent either the rows or the columns of the data set, often need to be reordered in order to yield an optimal fit.

In practice, it is generally infeasible to assess every possible combination of topics across all raters. As such, brittnu provides three methods of converging toward an optimal topic order for each rater. The default, shuffle\_method="rotational", takes the provided sequence and swaps pairs of categories until no further swaps would further improve the fit. shuffle\_method="agglomerative" and shuffle\_method="divisive" instead perform hierarchical cluster analyses of all topics, with the added restriction that two topics constructed by the same rater may not appear in the same cluster. Notably, the "agglomerative" option can take excessive time in some cases, while the

"divisive" option forms clusters based on the macro-level dynamics of the data and may therefore yield weakly matched sets of individual topics compared to the other available options.

Regardless of whether the rows or columns of the data set must be reordered, when estimating Britt's nu, it is common to compute four separate coefficients in this family: Britt's single-observation nu for all raters, Britt's single-observation nu for pairs of raters, Britt's omnibus nu for all raters, and Britt's single-observation nu for pairs of raters. For example, when assessing the reliability of multiple latent Dirichlet allocation cross-validation folds that each used the same data set and number of topics, single-observation reliability can be used to assess the reliability of the allocations of words to each individual topic, while multiple-observation reliability indicates the reliability of the allocations of words to the set of all topics. Likewise, the coefficients that take all raters into account generally more valuable for the summative assessment of reliability, but the pairwise coefficients are sometimes useful for diagnostic purposes.

By default, brittnu provides all four reliability coefficients. To reduce the time and memory required, the pairwise versions may optionally be omitted from the computation by specifying pairwise=FALSE.

Also by default, the expected difference component of Britt's nu is estimated using parametric bootstrapping based on the distribution of the original data. This process can sometimes become computationally intensive. In such cases, it may be advisable to set sampling\_method="nonparametric" in order to use nonparametric bootstrapping rather than parametric bootstrapping. You may also consider setting lower\_bound=TRUE to use i.i.d. beta distributions to estimate the lower bound of the expected differences between observations, ultimately yielding an estimated lower bound for Britt's nu itself. This method may be faster than some methods of reordering rows or columns in some cases, although this is not always true.

## Additional usage notes:

- 1. When x is a list of 2D double vectors (rather than a list of objects outputted from LDA), each row of each list element should be a single observation from a Dirichlet distribution (e.g., an LDA topic), and each column should be a category within that distribution (e.g., a word).
- 2. It is generally recommended that estimate\_pairwise\_alpha\_from\_joint be set to TRUE, which is the default setting. If concentration parameters must be estimated from x, and if all elements were generated via LDA from the same corpus or are otherwise assumed to have emerged from the same underlying distribution, then there is little reason to expect different sets of concentration parameters to be necessary across iterations. You should only consider setting estimate\_pairwise\_alpha\_from\_joint different data sets that may not have come from the same underlying distribution were used to generate different elements of x. Doing so, however, may substantially slow the procedure, so it is generally not recommended unless essential.
- 3. If you are assessing the reliability of the allocations of words to topics different set of documents. In such cases, different\_documents must be set to TRUE. For instance, if mydata1, mydata2, mydata3, mydata4, and mydata5 each contain 80 documents from a single data set, then you could run

```
cv1 <- LDA(mydata1, k=15)
cv2 <- LDA(mydata2, k=15)
cv3 <- LDA(mydata3, k=15)
cv4 <- LDA(mydata4, k=15)
cv5 <- LDA(mydata5, k=15)
cv <- list(cv1, cv2, cv3, cv4, cv5)
rel <- brittnu(cv, type="wt", shuffle=TRUE, different_documents=TRUE)
summary(rel)</pre>
```

to assess the word-topic allocation reliability for a 15-topic model. Any words that appear in some cross-validation iterations but not others will automatically be set to an allocation near 0 for any

iterations in which they are absent from the data set. If you are instead assessing the reliability of the allocations of topics to documents, then if different\_documents==TRUE, any iteration in which a given document does not appear will simply be excluded from the reliability computation for that document. Thus, fewer cross-validation iterations will be used to assess reliability for each individual document. This will weaken the stability of the reliability computation. Therefore, unless you are specifically assessing whether your topic model is stable regardless of what subset of documents was used to generate it, it is advised that all documents be included in all cross-validation iterations.

- 4. When shuffle==TRUE, each element in x comprises a large number of topics, and/or samples is large, setting lower\_bound=TRUE may sometimes be useful in order to eliminate the need to reorder a large number of topics in numerous bootstrapped samples. Additionally, for Dirichlet distributions with many categories, precise estimates of the concentration parameters may require excessive time, so whenever possible, a priori known concentration parameters should be provided via the alpha parameter rather than estimating them from the data. This is also useful to ensure the validity of Britt's nu. When this is not possible, consider setting sampling\_method="nonparametric" in order to avoid the use of concentration parameters altogether. Alternatively, the procedure may be expedited by changing converit from its default value (0.00001) to a larger number. You may also wish to set progress=TRUE and verbose=TRUE to receive periodic progress updates and ensure that the computation is proceeding as expected.
- 5. When shuffle==TRUE, the topics in x are reordered. This is described in the matrix of reordered topics, which is provided as one of the elements of the list returned by brittnu and can be viewed using summary() on that object. Each row of this matrix indicates the manner in which the topics were reordered. For instance, if the first row is c(3,1,2), that means that for the first rater, the third topic was moved to the first position, the first topic was moved to the second position, and the second topic was moved to the third position.

### Value

A list of class brittnu\_rel containing seven elements: Britt's single-observation nu for all raters (as a numeric vector indicating the reliability for each observation), Britt's single-observation nu for pairs of raters (as a list containing lists containing numeric vectors indicating the reliability of each observation for each pair of raters, e.g., the second element of the first list contains the reliability for raters 1 and 2), Britt's multiple-observation nu for all raters (as a numeric value), Britt's multiple-observation nu for pairs of raters (as a list containing lists containing numeric values, e.g., the second element of the first list contains the reliability for raters 1 and 2), the matrix of reordered topics for each rater (if shuffle==TRUE), any warnings raised, and the value of the type argument

# References

Britt, B. C. (under review). Interrater reliability for compositional, Euclidean, and Dirichlet Data.

#### **Examples**

```
shuffle=TRUE, samples=1000, verbose=TRUE)
summary(reliability_ap_td)
summary(reliability_ap_td, element="all")
summary(reliability_ap_wt)
summary(reliability_ap_wt, element="all")
#Example 2: Manually inputted data with known concentration parameters
require(gtools)
data_with_known_alpha1 <- rbind(gtools::rdirichlet(1,alpha1),</pre>
                             gtools::rdirichlet(1,alpha2),
                             gtools::rdirichlet(1,alpha3))
data_with_known_alpha2 <- rbind(gtools::rdirichlet(1,alpha1),</pre>
                             gtools::rdirichlet(1,alpha2),
                             gtools::rdirichlet(1,alpha3))
data_with_known_alpha3 <- rbind(gtools::rdirichlet(1,alpha1),</pre>
                             gtools::rdirichlet(1,alpha2),
                             gtools::rdirichlet(1,alpha3))
data_with_known_alpha4 <- rbind(gtools::rdirichlet(1,alpha1),</pre>
                             gtools::rdirichlet(1,alpha2),
                             gtools::rdirichlet(1,alpha3))
data_with_known_alpha5 <- rbind(gtools::rdirichlet(1,alpha1),</pre>
                             gtools::rdirichlet(1,alpha2),
                             gtools::rdirichlet(1,alpha3))
data_with_known_alpha <- list(data_with_known_alpha1, data_with_known_alpha2,</pre>
                           data_with_known_alpha3, data_with_known_alpha4,
                           data_with_known_alpha5)
reliability_known <- brittnu(data_with_known_alpha,</pre>
                          alpha=list(alpha1, alpha2, alpha3))
summary(reliability_known, element="all")
```

clustering\_determine\_difference

Distance Between Clusters

# **Description**

This helper function computes the distance between two clusters based on a specified metric.

# Usage

```
clustering_determine_difference(
  x_obs,
  y_obs,
  alldiff = NA,
  x_restructured = NA,
  clustering_method = NA
)
```

## **Arguments**

x_obs	A vector of indices representing the observations in the first cluster	
y_obs	A vector of indices representing the observations in the second cluster	
alldiff	A 2D array indicating the distance between each pair of observations across all raters	
x_restructured	A 2D array containing the original data set, restructured to facilitate more straightforward references in this function	
clustering_method		
	A string indicating the criterion that will be used to evaluate the distance between clusters; permitted values are "average", "minimum", "maximum", "median", "centroid", and "wald"	

## Value

A numeric value indicating the distance between clusters

```
compute\_expected\_joint\_differences\_lower\_bound \\ Compute\ Expected\ Joint\ Differences\ (Lower\ Bound)
```

# Description

This helper function estimates the lower bound of the expected differences among all raters.

# Usage

```
compute_expected_joint_differences_lower_bound(x, shuffle_dimension, verbose)
```

# **Arguments**

x A list such that each element is a 2D double vector with observations as the rows and each category within each observation as the columns shuffle\_dimension

A string indicating whether "rows" or "columns" were shuffled in the original data set

verbose A boolean value indicating whether to provide progress updates

#### Value

A list of lists containing numeric vectors indicating the lower bound of the expected differences between all raters

# **Description**

This helper function estimates the lower bound of the expected differences between pairs of raters.

## Usage

```
compute_expected_pairwise_differences_lower_bound(
    x,
    shuffle_dimension,
    verbose
)
```

#### **Arguments**

x A list such that each element is a 2D double vector with observations as the rows and each category within each observation as the columns

shuffle\_dimension

A string indicating whether "rows" or "columns" were shuffled in the original

data set

verbose A boolean value indicating whether to provide progress updates

### Value

A list of lists containing numeric vectors indicating the lower bound of the expected differences between pairs of raters

```
compute_observed_differences
```

Compute Observed Differences

# Description

This helper function computes the differences between all raters and between all pairs of raters in a given real or bootstrapped data set.

# Usage

```
compute_observed_differences(x)
```

#### **Arguments**

x A list such that each element is a 2D double vector with observations as the rows and each category within each observation as the columns

#### Value

A two-element list indicating the observed differences between observations for all raters and for each pair of raters, respectively

# **Description**

This helper function computes the expected squared difference between deviates from the same underlying Dirichlet distribution when the categories in each distribution are not allowed to be reordered.

# Usage

```
compute_single_expectation(
    x,
    joint_alpha,
    pairwise_alpha,
    pairwise,
    samples = 1000,
    sampling_method = "nonparametric",
    verbose = FALSE
)
```

# Arguments

Х	A list such that each element is a 2D double vector with observations as the rows and each category within each observation as the columns	
joint_alpha	A vector of concentration parameters representing all raters	
pairwise_alpha	A list of lists of vectors of concentration parameters representing all pairs of raters	
pairwise	A boolean value indicating whether pairwise differences between individual raters should be computed; if FALSE, pairwise differences will be ignored in order to reduce the time and memory complexity of the computation	
samples	An integer value indicating how many samples to use to estimate expected differences	
sampling_method		
	A string indicating whether bootstrapped sampling should be performed using a "parametric" or "nonparametric" approach	
verbose	A boolean value indicating whether to provide progress updates	

# Value

A two-element list indicating the expected differences between observations for all raters and for each pair of raters, respectively

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dirichlet.mle	Estimate Concentration Parameters	

# Description

This helper function estimates the concentration parameters of the Dirichlet distribution underlying multiple observations, with no restrictions placed on the values of those concentration parameters. This function is heavily based on dirichlet.mle, with modifications to avoid potential singularities in the estimation procedure.

# Usage

```
dirichlet.mle(
   x,
   weights = NULL,
   eps = 10^(-5),
   convcrit = 1e-05,
   maxit = 1000,
   oldfac = 0.3,
   progress = FALSE
)
```

# **Arguments**

X	A list such that each element is a 2D double vector with observations as the rows and each category within each observation as the columns
weights	A numeric vector used to calibrate the initial estimates of concentration parameters
eps	A numeric value used as a tolerance parameter to prevent logarithms of zero
convcrit	A numeric value indicating the threshold for convergence used to estimate concentration parameters
maxit	A numeric value indicating the maximum number of iterations used to estimate concentration parameters
oldfac	A numeric value between 0 and 1 used as the convergence acceleration factor
progress	A boolean value indicating whether progress updates should be provided

## Value

A list of the estimated concentration parameters, the sum of those estimated concentration parameters, and the ratio between each estimated concentration parameter and the sum of those parameters

```
estimate_alpha_from_data

*Estimate Alpha from Data*
```

### **Description**

This helper function estimates the expected concentration parameters of the Dirichlet distribution underlying multiple observations.

# Usage

```
estimate_alpha_from_data(
    x,
    pairwise,
    estimate_pairwise_alpha_from_joint,
    symmetric_alpha = FALSE,
    convcrit = 1e-05,
    maxit = 1000,
    progress = FALSE
)
```

#### **Arguments**

х

A list such that each element is a 2D double vector with observations as the rows and each category within each observation as the columns

pairwise

A boolean value indicating whether pairwise differences between individual raters should be computed; if FALSE, pairwise differences will be ignored in order to reduce the time and memory complexity of the computation

estimate\_pairwise\_alpha\_from\_joint

A boolean value indicating, when estimating reliability for pairs of raters, whether each pair of raters should use the concentration parameters estimated across all raters (TRUE) or whether separate sets of concentration parameters should be estimated for each pair of raters (FALSE); this argument only has an effect when alpha==NA, and it is strongly suggested that the default value of TRUE be used for this argument when possible

symmetric\_alpha

A boolean value indicating whether concentration parameters should be assumed to be unchanged between observations, which is common in many topic modeling procedures

convcrit

A numeric value indicating the threshold for convergence used to estimate concentration parameters

maxit

A numeric value indicating the maximum number of iterations used to estimate

concentration parameters

progress

A boolean value indicating whether to provide progress updates

# Value

A two-element list indicating the estimated concentration parameters for all raters and for each pair of raters, respectively

```
estimate_single_expectation
```

Estimate Single Expectation

# Description

This helper function uses bootstrapping to estimate the expected squared difference between observations from the same underlying distribution.

### Usage

```
estimate_single_expectation(
    x,
    joint_alpha,
    pairwise_alpha,
    pairwise,
    shuffle = TRUE,
    shuffle_method = "rotational",
    shuffle_dimension = "rows",
    clustering_method = "average",
    slow_clustering = FALSE,
    samples = 1000,
    sampling_method = "nonparametric",
    lower_bound = TRUE,
    verbose = FALSE
)
```

# **Arguments**

clustering\_method

X	A list such that each element is a 2D double vector with observations as the rows and each category within each observation as the columns
joint_alpha	A vector of concentration parameters representing all raters
pairwise_alpha	A list of lists of vectors of concentration parameters representing all pairs of raters
pairwise	A boolean value indicating whether pairwise differences between individual raters should be computed; if FALSE, pairwise differences will be ignored in order to reduce the time and memory complexity of the computation
shuffle	A boolean value indicating whether or not the topics may have been shuffled into different sequences by each rater
shuffle_method	A string indicating what method ("rotational", "agglomerative", or "divisive") will be used to reorder topics
shuffle_dimension	
	A string indicating whether "rows" or "columns" should be reordered; this

argument only has an effect if shuffle==TRUE and type==NA

A string indicating the criterion that will be used to merge or divide clusters if shuffle==TRUE and either shuffle\_method=="agglomerative" or shuffle\_method=="divisive permitted values are "average", "minimum", "maximum", "median", "centroid", and "wald"

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slow\_clustering

A boolean value indicating whether the distances between clusters should be recalculated after each individual observation is added to the new cluster (TRUE), which can improve the cohesiveness of the resulting cluster, or whether all observations should be added to the new cluster without recomputing the distances between clusters after every addition (FALSE); this argument only has an effect if shuffle==TRUE and shuffle\_method=="divisive"

samples

An integer value indicating how many samples to use to estimate expected differences

sampling\_method

A string indicating whether bootstrapped sampling should be performed using a "parametric" or "nonparametric" approach

lower\_bound

A boolean value indicating whether the lower bound of the expected differences (based on i.i.d. beta distributions) should be used rather than reordering Dirichlet distributions to estimate the exact difference in every sample when

shuffle==TRUE

verbose

A boolean value indicating whether to provide progress updates

#### Value

A two-element list indicating the expected differences between observations for all raters and for each pair of raters, respectively

euclidkrip

Euclidean Krippendorff's Alpha

## **Description**

This function computes Euclidean Krippendorff's alpha for data sets composed of compositional or Euclidean data, as described by Britt (under review).

# Usage

```
euclidkrip(
    x,
    pairwise = TRUE,
    force_bootstrapping = FALSE,
    shuffle = FALSE,
    shuffle_method = "rotational",
    shuffle_dimension = "rows",
    clustering_method = "average",
    slow_clustering = FALSE,
    samples = 1000,
    lower_bound = FALSE,
    verbose = FALSE
)
```

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#### **Arguments**

x A list such that each element is a 2D double vector with observations as the rows

and each category within each observation as the columns

pairwise A boolean value indicating whether pairwise reliability between individual raters

should be computed; if FALSE, pairwise reliability will be ignored in order to re-

duce the time and memory complexity of the computation

force\_bootstrapping

A boolean value indicating whether bootstrapping should be used to estimate expected differences rather than exactly computing them even if shuffle==FALSE

shuffle A boolean value indicating whether or not the topics may have been shuffled into

different sequences by each rater; if this is TRUE and shuffle\_dimension="rows", then the observations (rows) corresponding to each rater will be reordered to

 $a chieve \ a \ (local) \ optimal \ fit, \ whereas \ if this \ is \ TRUE \ and \ shuffle\_dimension="columns",$ 

the categories (columns) will be reordered instead

shuffle\_method A string indicating what method ("rotational", "agglomerative", or "divisive")

will be used to reorder topics

shuffle\_dimension

A string indicating whether "rows" or "columns" should be reordered; this argument only has an effect if shuffle==TRUE and type==NA

clustering\_method

A string indicating the criterion that will be used to merge or divide clusters if shuffle==TRUE and either shuffle\_method=="agglomerative" or shuffle\_method=="divisive permitted values are "average", "minimum", "maximum", "median", "centroid",

and "wald"

slow\_clustering

A boolean value indicating whether the distances between clusters should be recalculated after each individual observation is added to the new cluster (TRUE), which can improve the cohesiveness of the resulting cluster, or whether all observations should be added to the new cluster without recomputing the distances between clusters after every addition (FALSE); this argument only has an effect

if shuffle==TRUE and shuffle\_method=="divisive"

samples An integer value indicating how many samples to use to estimate expected dif-

ferences when shuffle==TRUE

lower\_bound A boolean value indicating whether the lower bound of the expected differ-

ences (based on i.i.d. beta distributions) should be used rather than shuffling Dirichlet distributions to estimate the exact difference in every sample when

shuffle==TRUE

verbose A boolean value indicating whether euclidkrip and its helper functions should

provide progress updates beyond the estimation of concentration parameters

#### **Details**

One of the most important uses for Euclidean Krippendorff's alpha is to assess the reliability of the allocations of words to topics or of topics to documents via topic modeling techniques that do not necessarily adhere to a Dirichlet distribution. This includes, for instance, Dirichlet multinomial mixture models, which are commonly used for short text topic modeling.

Crucially, different topic modeling cross-validation iterations, which effectively represent distinct raters of the same data set, may result in the same topics appearing in a different sequence. As such, those topics, which may represent either the rows or the columns of the data set, often need to be reordered in order to yield an optimal fit.

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In practice, it is generally infeasible to assess every possible combination of topics across all raters. As such, euclidkrip provides three methods of converging toward an optimal topic order for each rater. The default, shuffle\_method="rotational", takes the provided sequence and swaps pairs of categories until no further swaps would further improve the fit. shuffle\_method="agglomerative" and shuffle\_method="divisive" instead perform hierarchical cluster analyses of all topics, with the added restriction that two topics constructed by the same rater may not appear in the same cluster. Notably, the "agglomerative" option can take excessive time in some cases, while the "divisive" option forms clusters based on the macro-level dynamics of the data and may therefore yield weakly matched sets of individual topics compared to the other available options.

Regardless of whether the rows or columns of the data set must be reordered, when computing Euclidean Krippendorff's alpha, it is common to compute two separate coefficients in this family: Euclidean Krippendorff's alpha for all raters and for pairs of raters. Unlike Britt's nu, both of these Euclidean Krippendorff's alpha measures yield a single reliability score for all observations, as the formula used by Euclidean Krippendorff's alpha to compute the expected differences between raters does not produce separate results for each individual observation. However, if the reliability of each observation is desired, then nonparametric bootstrapping may be used to estimate those coefficients. This is automatically done when shuffle==TRUE, and it is also implemented when force\_bootstrapping==TRUE. In either of those cases, the single-observation reliability values will be reported alongside the multiple-observation reliability values that euclidkrip already provides.

By default, euclidkrip provides reliability coefficients for all raters and for pairs of raters. To reduce the time and memory required, the pairwise versions may optionally be omitted from the computation by specifying pairwise=FALSE.

#### Additional usage notes:

- 1. x must be a list of 2D double vectors, and each row of each list element should be a single observation from a Dirichlet distribution (e.g., an LDA topic) while each column should represent a category within that distribution (e.g., a word).
- 2. When shuffle==TRUE, each element in x comprises a large number of topics, and/or samples is large, setting lower\_bound=TRUE may sometimes be useful in order to eliminate the need to reorder a large number of topics in numerous bootstrapped samples. You may also wish to set verbose=TRUE to receive periodic progress updates and ensure that the computation is proceeding as expected.
- 3. When shuffle==TRUE, the topics in x are reordered. This is described in the matrix of reordered topics, which is provided as one of the elements of the list returned by euclidkrip and can be viewed using summary() on that object. Each row of this matrix indicates the manner in which the topics were reordered. For instance, if the first row is c(3,1,2), that means that for the first rater, the third topic was moved to the first position, the first topic was moved to the second position, and the second topic was moved to the third position.

#### Value

A list of class euclidkrip\_rel containing six elements: Euclidean Krippendorff's alpha for each observation and all raters (as a numeric vector indicating the reliability for each observation), Euclidean Krippendorff's alpha for each observation and pairs of raters (as a list containing lists containing numeric vectors indicating the reliability of each observation for each pair of raters, e.g., the second element of the first list contains the reliability for raters 1 and 2), Euclidean Krippendorff's alpha for all observations and all raters (as a numeric value), Euclidean Krippendorff's alpha for all observations and pairs of raters (as a list containing lists containing numeric values, e.g., the second element of the first list contains the reliability for raters 1 and 2), the matrix of reordered topics for each rater (if shuffle==TRUE), and any warnings raised

#### References

Britt, B. C. (under review). Interrater reliability for compositional, Euclidean, and Dirichlet Data.

#### **Examples**

#### **Description**

This helper function uses nonparametric bootstrapping to generate an artificial data set from a provided data set

### Usage

```
generate_artificial_data_nonparametric(x, shuffle, shuffle_dimension)
```

#### **Arguments**

A list such that each element is a 2D double vector with observations as the rows and each category within each observation as the columns

shuffle A boolean value indicating whether or not the topics may have been shuffled into different sequences by each rater

shuffle\_dimension

A string indicating whether "rows" or "columns" were shuffled in the original data set; this argument only has an effect if shuffle==TRUE

#### Value

A list of nonparametrically bootstrapped data such that each element is a 2D double vector with observations as the rows and each category within each observation as the columns

18 label\_assignments

```
generate_artificial_data_parametric

Generate Artificial Data (Parametric)
```

#### **Description**

This helper function uses parametric bootstrapping to generate an artificial data set from a provided data set

#### Usage

```
generate_artificial_data_parametric(x, pairwise_alpha)
```

#### **Arguments**

x A list such that each element is a 2D double vector with observations as the rows and each category within each observation as the columns

pairwise\_alpha A list of lists of vectors of concentration parameters representing all pairs of raters

#### Value

A list of parametrically bootstrapped data such that each element is a 2D double vector with observations as the rows and each category within each observation as the columns

label\_assignments Lc

Label Assignments Matrix

#### **Description**

This helper function adds labels to the assignments matrix based on whether the rows and columns represent documents and topics, topics and words, or something else, in order to facilitate more informative printing.

#### Usage

```
label_assignments(assignments, type = NA)
```

# Arguments

assignments A matrix indicating the relationship between each reordered topic and its origi-

nal position in the data

type A string indicating the type of reliability being assessed, with permitted values

of "wt" (word-topic reliability), "td" (topic-document reliability), and NA

#### Value

A matrix indicating the relationship between each reordered topic and its original position in the data, with the addition of row and column labels

print.brittnu\_rel 19

#### **Description**

This helper method calls summary() when the user attempts to print an object of class brittnu\_rel outputted from brittnu.

# Usage

```
## S3 method for class 'brittnu_rel'
print(x, element = NA, ...)
```

# **Arguments**

... Other arguments inherited from the generic print function

```
print.euclidkrip_rel Print(euclidkrip)
```

## **Description**

This helper method calls summary() when the user attempts to print an object of class euclidkrip\_rel outputted from euclidkrip.

# Usage

```
## S3 method for class 'euclidkrip_rel'
print(x, element = NA, ...)
```

# Arguments

An object of class euclidkrip\_rel outputted from euclidkrip

element The specific reliability coefficient to be printed; permitted values are "singleomnibus",
 "singlepairwise", "multipleomnibus", "multiplepairwise", "all", and
 NA

Other arguments inherited from the generic print function

rdirichlet

Generate Dirichlet Observations

## **Description**

This helper function generates a set of observations from a Dirichlet distribution with underlying concentration parameters equal to alpha. This function is heavily based on rdirichlet, with modifications to prevent concentration parameters equal to 0.

#### Usage

```
rdirichlet(n, alpha, zero2 = (10^(-255)))
```

## **Arguments**

n	A numeric value indicating the number of observations to be generated
alpha	A numeric vector indicating the concentration parameters of the Dirichlet distribution from which observations should be generated
zero2	A numeric value representing the minimum allocation permitted for any given Dirichlet category in order to prevent errors

#### Value

A numeric vector with n Dirichlet observations

```
restricted_agglomerative_clustering

*Restricted Agglomerative Clustering*
```

## **Description**

This helper function performs agglomerative hierarchical cluster analysis in order to minimize the sum of squared differences between raters.

## Usage

```
restricted_agglomerative_clustering(
   x,
   verbose = FALSE,
   clustering_method = "average"
)
```

## **Arguments**

A list such that each element is a 2D double vector, with the topics to be reordered representing the rows of each vector

 $\begin{tabular}{ll} \end{tabular} \begin{tabular}{ll} \end{tabular} \begin{tabular}{ll} \end{tabular} A boolean value indicating whether to provide progress updates clustering_method \\ \end{tabular}$ 

A string indicating the criterion that will be used to merge or divide clusters; permitted values are "average", "minimum", "maximum", "median", "centroid", and "wald"

#### **Details**

This procedure conducts a cluster analysis in order to group topics from each rater into clusters indicating optimal matches between those topics. This effectively serves to reorder the topics constructed by each such that, to the extent possible, each individual topic is matched with its best-fitting counterparts constructed by each other rater before reliability is assessed.

This cluster analysis uses an additional constraint: topics from the same rater can never be combined into the same cluster. This ensures that at the end of the process, the number of clusters will be equal to the number of topics constructed by each rater, and each rater will have yielded one topic belonging to each cluster. If two clusters would be combined such that this rule would be violated, then immediately afterward, all offending topics are removed from the newly merged cluster and each one is treated as an independent cluster to be later merged into other clusters.

Additionally, to prevent infinite loops (e.g., the same topic is repeatedly added to a larger cluster and removed afterward in accordance with the preceding procedure), two additional requirements are imposed in order to merge any pair of clusters. First, when considering any potential cluster merge operation, if executing the merge would in an identical set of clusters as any prior step, that operation is not performed, and the procedure skips to the next pair of clusters to be considered for merging. Second, when considering any potential cluster merge operation, the procedure compares the set of raters from which all topics in each of the two clusters were drawn, and if either one is a perfect subset of the other (e.g., the topics in cluster 1 came from raters 3 and 6, while the topics in cluster 2 were created by raters 1, 2, 3, 4, 6, and 8), then we cannot merge the two clusters, as all observations in one cluster would just be removed from the resulting cluster afterward. Whenever such a perfect subset is observed via this diagnostic, the procedure skips to the next pair of clusters to be considered for merging.

Notably, although infinite loops are avoided, this function still tends to get stuck in long-lasting loops. When this happens, either rotational\_shuffling or restricted\_divisive\_clustering may be a better choice.

#### Value

A two-element list containing the reordered data set and a matrix indicating the relationship between each reordered topic and its original position in the data, respectively

```
restricted_divisive_clustering

*Restricted Divisive Clustering*
```

#### **Description**

This helper function performs divisive hierarchical cluster analysis in order to minimize the sum of squared differences between raters.

#### Usage

```
restricted_divisive_clustering(
    x,
    verbose = FALSE,
    clustering_method = "average",
    slow_clustering = FALSE
)
```

22 rotational\_shuffling

#### **Arguments**

Х

A list such that each element is a 2D double vector, with the topics to be reordered representing the rows of each vector

verbose

A boolean value indicating whether to provide progress updates

clustering\_method

A string indicating the criterion that will be used to merge or divide clusters; permitted values are "average", "minimum", "maximum", "median", "centroid", and "wald"

slow\_clustering

A boolean value indicating whether the distances between clusters should be recalculated after each individual observation is added to the new cluster (TRUE), which can improve the cohesiveness of the resulting cluster, or whether all observations should be added to the new cluster without recomputing the distances between clusters after every addition (FALSE)

#### **Details**

This procedure conducts a cluster analysis in order to group topics from each rater into clusters indicating optimal matches between those topics. This effectively serves to reorder the topics constructed by each such that, to the extent possible, each individual topic is matched with its best-fitting counterparts constructed by each other rater before reliability is assessed.

This cluster analysis uses an additional constraint: all clusters resulting from dividing an existing cluster must contain a number of observations that is a multiple of the number of topics constructed by each rater, and all raters must be equally represented in each of those resulting clusters. This ensures that at the end of the process, the number of clusters will be equal to the number of topics constructed by each rater, and each rater will have yielded one topic belonging to each cluster.

However, this approach sometimes creates clusters based on macro-level dynamics rather than micro-level differences between topics, ultimately yielding weakly matched sets of categories compared with other approaches. In those cases, either rotational\_shuffling or restricted\_agglomerative\_clustering may yield superior results.

#### Value

A two-element list containing the reordered data set and a matrix indicating the relationship between each reordered topic and its original position in the data, respectively

rotational\_shuffling Rotational Shuffling

#### **Description**

This helper function reorders the rows of ratings from multiple raters in order to minimize the sum of squared differences between them.

# Usage

```
rotational_shuffling(x, verbose = FALSE, swap_tol = (10^{-12}))
```

shuffle\_distributions 23

#### **Arguments**

x A list such that each element is a 2D double vector, with the topics to be re-

ordered representing the rows of each vector

verbose A boolean value indicating whether to provide progress updates

swap\_tol A numeric value representing the minimum threshold by which the sum of

squared differences must be improved in order to execute a potential swap of two rows; this is necessary in order to prevent infinite loops due to minuscule

rounding errors

#### Value

A two-element list containing the reordered data set and a matrix indicating the relationship between each reordered topic and its original position in the data, respectively

```
shuffle_distributions Shuffle Distributions
```

### **Description**

This helper function reorders the categories in multiple Dirichlet deviates in order to minimize the sum of squared differences between them.

## Usage

```
shuffle_distributions(
    x,
    verbose = FALSE,
    shuffle_method = "rotational",
    clustering_method = "average",
    slow_clustering = FALSE,
    shuffle_dimension = "rows"
)
```

#### **Arguments**

A list such that each element is a 2D double vector with observations as the rows

and each category within each observation as the columns

verbose A boolean value indicating whether to provide progress updates

shuffle\_method A string indicating what method ("rotational", "agglomerative", or "divisive")

will be used to reorder topics

clustering\_method

A string indicating the criterion that will be used to merge or divide clusters if shuffle\_method=="agglomerative" or shuffle\_method=="divisive"; permitted values are "average", "minimum", "maximum", "median", "centroid",

and "wald"  $\,$ 

slow\_clustering

A boolean value indicating whether the distances between clusters should be recalculated after each individual observation is added to the new cluster (TRUE), which can improve the cohesiveness of the resulting cluster, or whether all observations should be added to the new cluster without recomputing the distances 24 squarediff

between clusters after every addition (FALSE); this argument only has an effect if shuffle\_method=="divisive"

shuffle\_dimension

A string indicating whether "rows" or "columns" should be reordered

#### Value

A two-element list containing the reordered data set and a matrix indicating the relationship between each reordered topic and its original position in the data, respectively

sirt\_digamma1

Sirt Digamma 1

#### **Description**

This helper function estimates the derivative of the digamma function. This function is directly drawn from sirt::sirt\_digamma1, as published at https://github.com/cran/sirt/blob/master/R/sirt\_digamma1.R. This function does not appear to be included in current releases of sirt and therefore cannot be directly loaded from that package.

#### Usage

```
sirt_digamma1(x, h = 0.001)
```

#### **Arguments**

x A vector of concentration parameters

h A numeric value used to define a pair of nearby observations

#### Value

A list of the estimated concentration parameters, the sum of those estimated concentration parameters, and the ratio between each estimated concentration parameter and the sum of those parameters

squarediff

Sum of Squared Differences

#### **Description**

This helper function computes the sum of squared differences between two vectors.

# Usage

```
squarediff(x, y)
```

#### **Arguments**

x A numeric vector y A numeric vector

## Value

A numeric value representing the sum of the squared differences between x and y

summary.brittnu\_rel 25

```
summary.brittnu_rel Summary(brittnu)
```

# Description

This method prints a summary of the Britt's nu reliability values using an object of class brittnu\_rel outputted from brittnu.

## Usage

```
## S3 method for class 'brittnu_rel'
summary(object, element = NA, ...)
```

## **Arguments**

object An object of class brittnu\_rel outputted from brittnu

element The specific reliability coefficient to be printed; permitted values are "singleomnibus",

"singlepairwise", "multipleomnibus", "multiplepairwise", "all", and

NA

... Other arguments inherited from the generic summary function

# Description

This method prints a summary of the Euclidean Krippendorff's alpha reliability values using an object of class euclidkrip\_rel outputted from euclidkrip.

# Usage

```
## S3 method for class 'euclidkrip_rel'
summary(object, element = NA, ...)
```

## **Arguments**

object An object of class euclidkrip\_rel outputted from euclidkrip

element The specific reliability coefficient to be printed; permitted values are "singleomnibus",

"singlepairwise", "multipleomnibus", "multiplepairwise", "all", and

NA

... Other arguments inherited from the generic summary function

```
symmetric.dirichlet.mle
```

Estimate Symmetric Concentration Parameters

## **Description**

This helper function estimates the concentration parameters of the Dirichlet distribution underlying multiple deviates, assuming that those concentration parameters are all equal. This function is heavily based on dirichlet.mle, with modifications to restrict all concentration parameters to be equal and to avoid potential singularities in the estimation procedure.

## Usage

```
symmetric.dirichlet.mle(
    x,
    weights = NULL,
    eps = 10^(-5),
    convcrit = 1e-05,
    maxit = 1000,
    oldfac = 0.3,
    progress = FALSE
)
```

# Arguments

Х	A list such that each element is a 2D double vector with observations as the rows and each category within each observation as the columns
weights	A numeric vector used to calibrate the initial estimates of concentration parameters
eps	A numeric value used as a tolerance parameter to prevent logarithms of zero
convcrit	A numeric value indicating the threshold for convergence used to estimate concentration parameters
maxit	A numeric value indicating the maximum number of iterations used to estimate concentration parameters
oldfac	A numeric value between 0 and 1 used as the convergence acceleration factor
progress	A boolean value indicating whether progress updates should be provided

# Value

A list of the estimated concentration parameters, the sum of those estimated concentration parameters, and the ratio between each estimated concentration parameter and the sum of those parameters

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