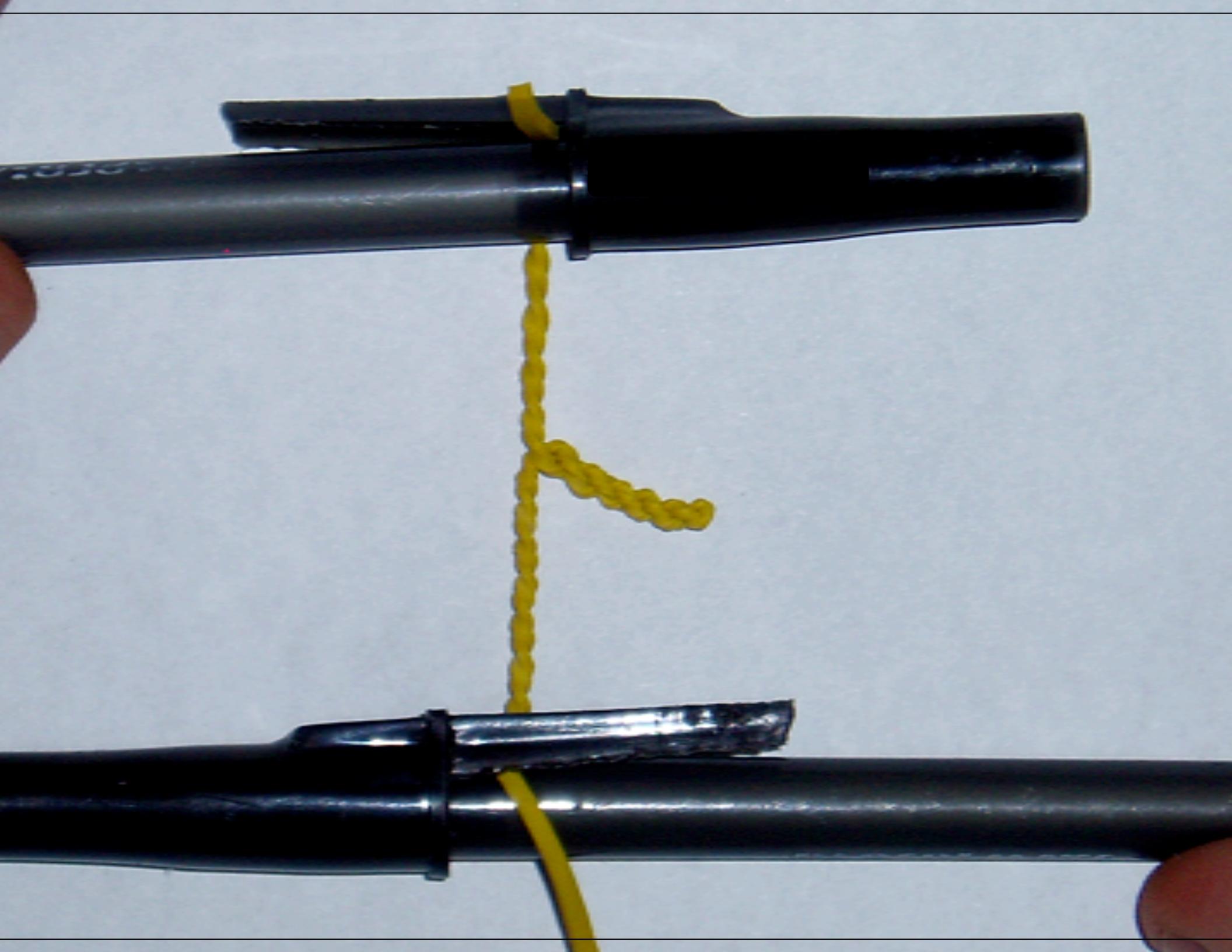


Discontinuities at the DNA supercoiling transition

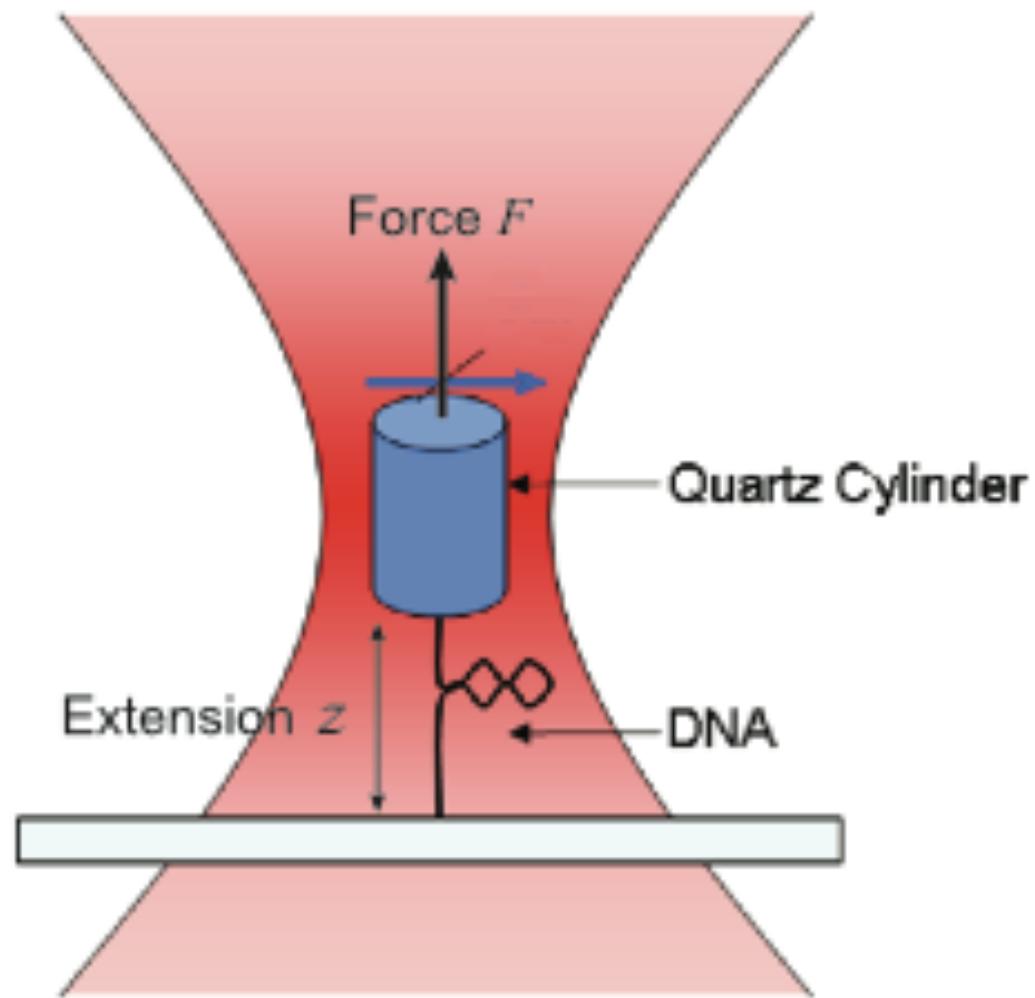


Bryan Daniels
Cornell University

Jim Sethna, Michelle Wang, Scott Forth, Maxim Sheinin



Twisting DNA

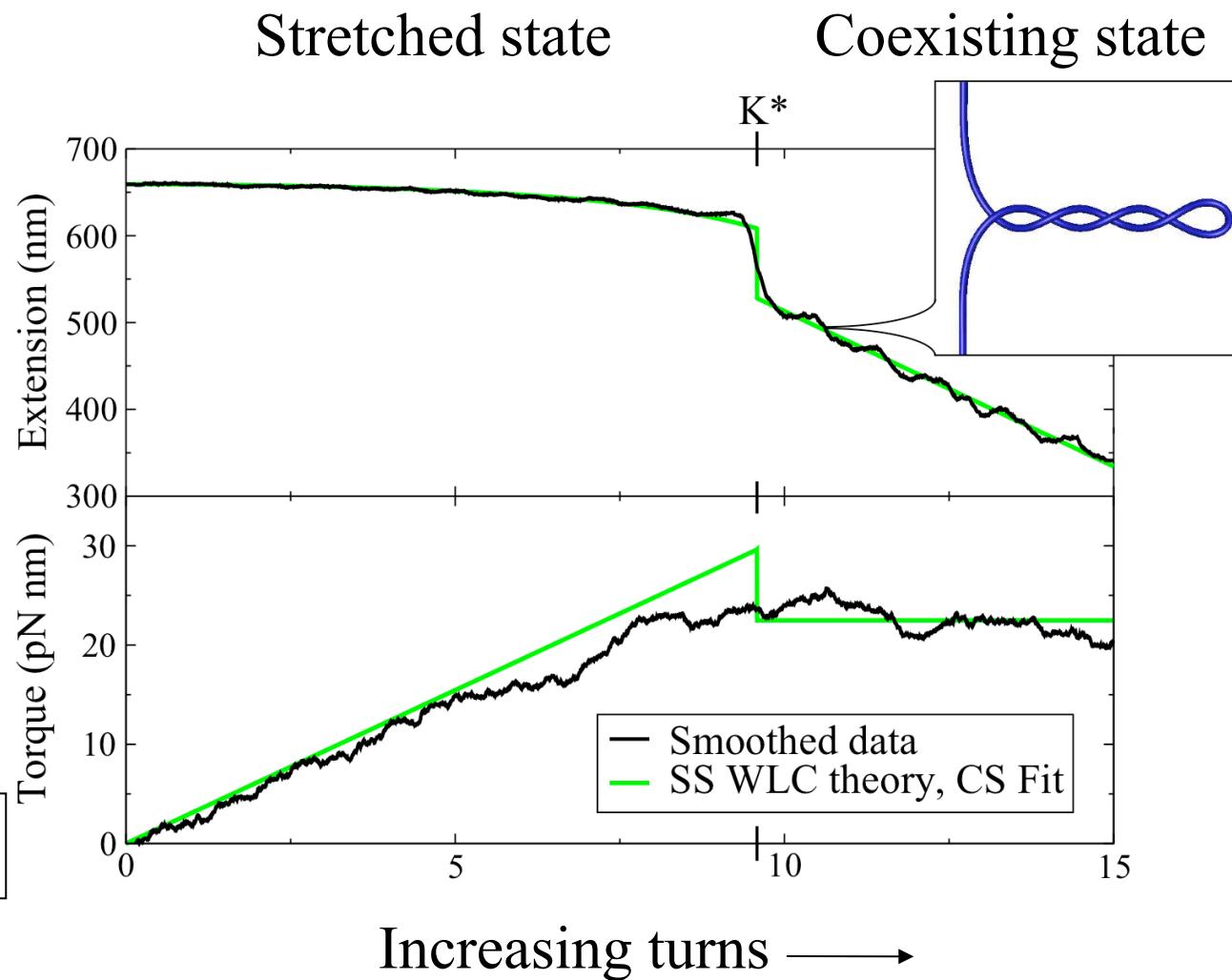


Discontinuities at the transition

- Sudden and reversible formation of twisted structure
- What determines the magnitudes of jumps?

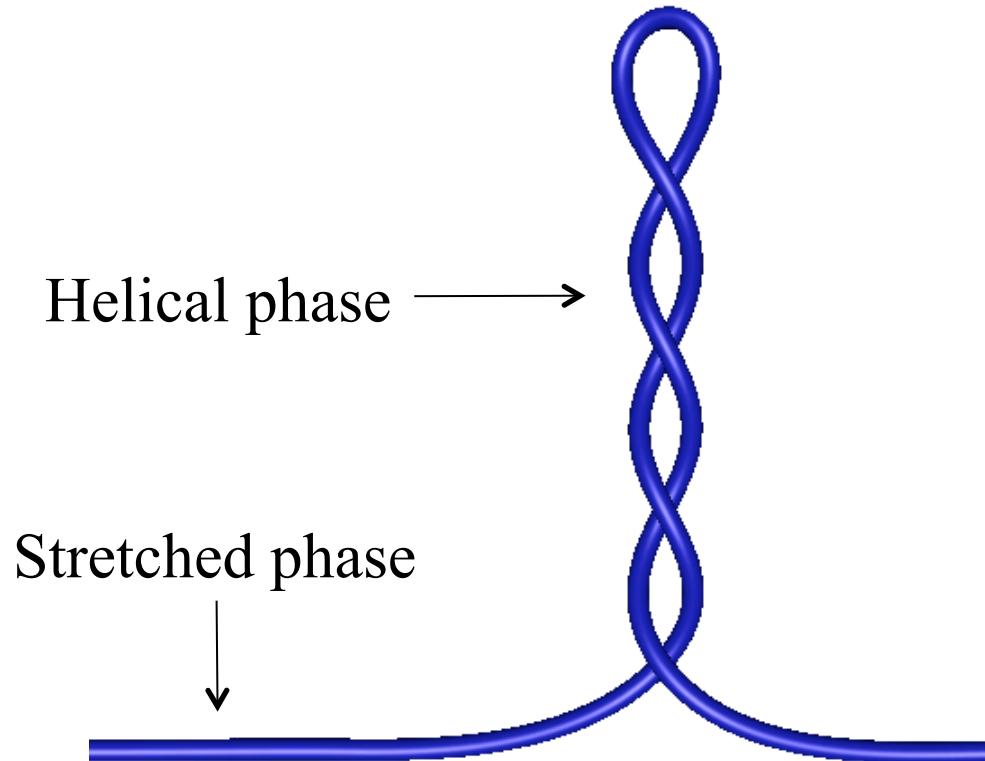
Length-dependence ?

Torque jump ?



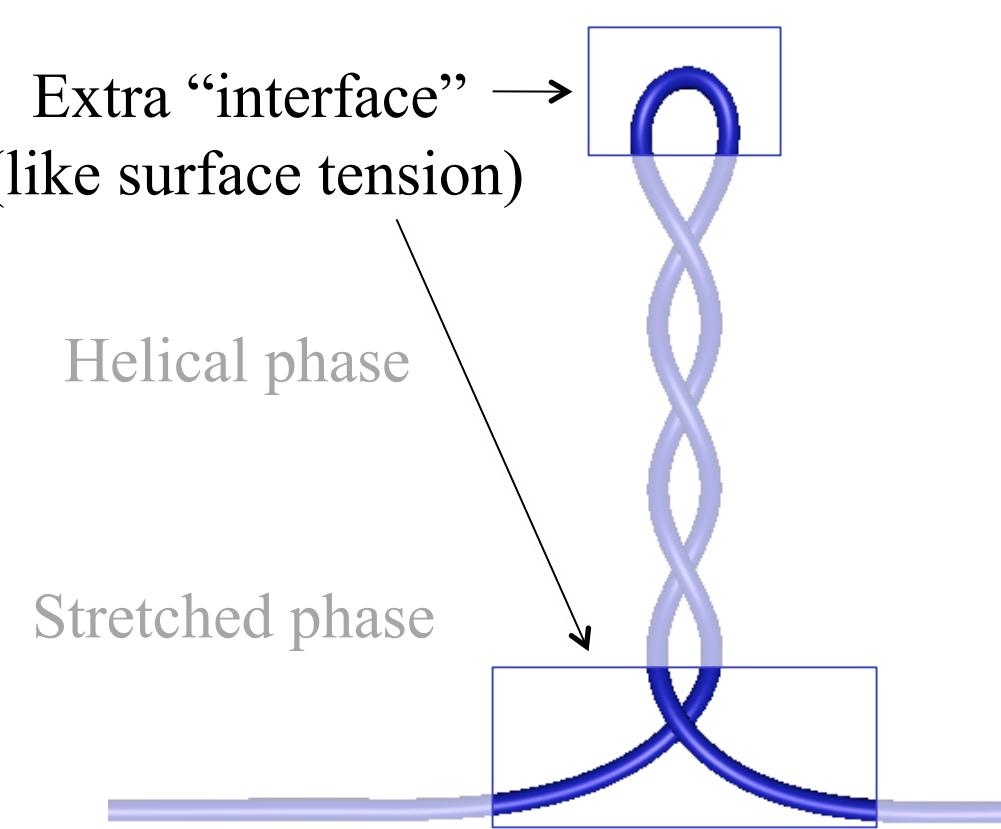
Two-phase coexistence \Rightarrow Linearity

- In coexisting state, increasing twist linearly converts stretched to helical DNA (Marko model)
- Like liquid-gas coexistence
- Extra parts create a nucleation barrier (our model): “first order phase transition” with discontinuities



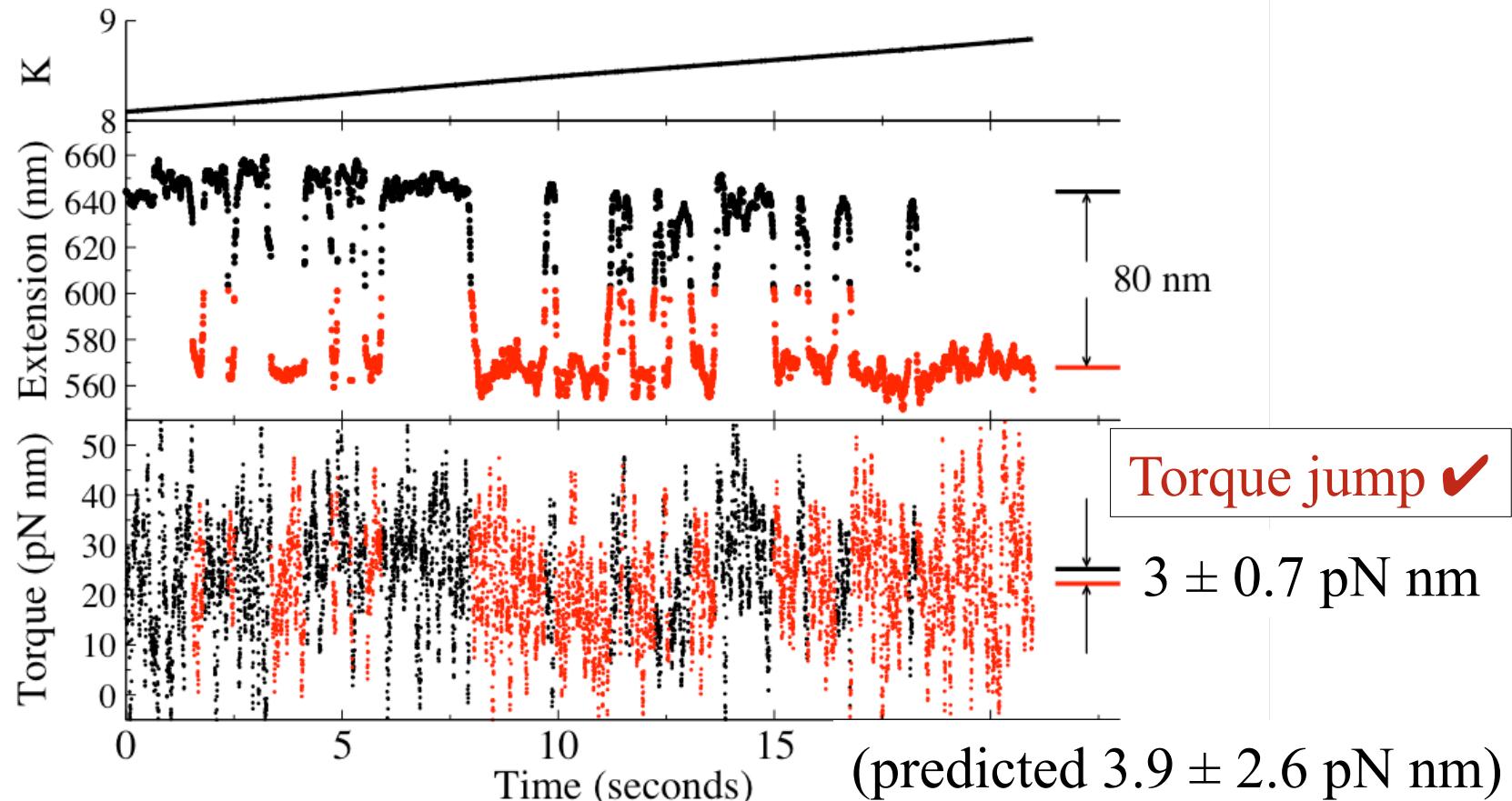
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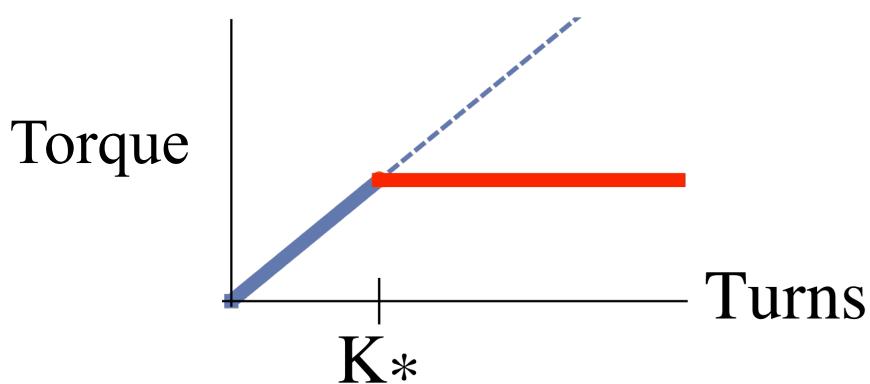
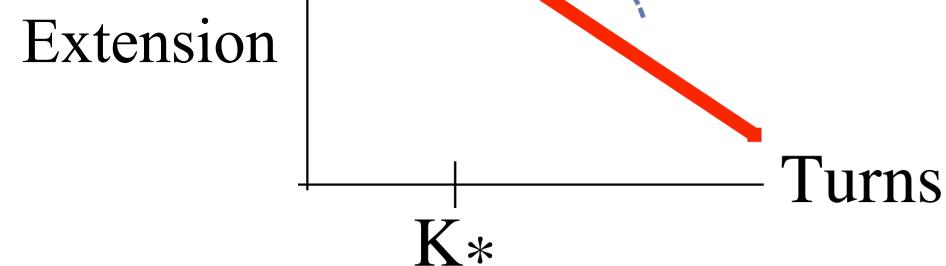
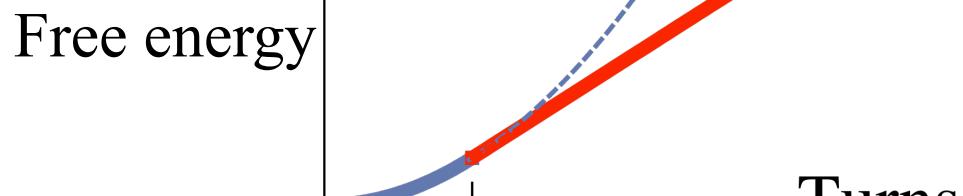
“Phase transition” smearing

- Thermal hopping smears the transition
- Can directly measure torque jump using binned averaging; agrees with prediction



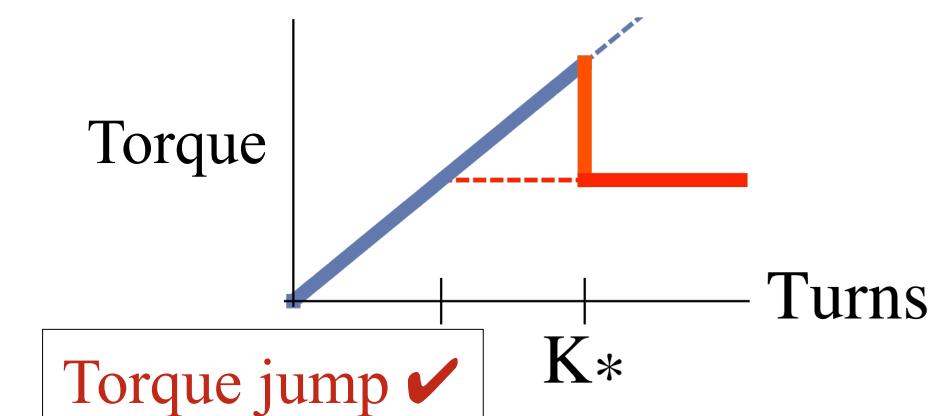
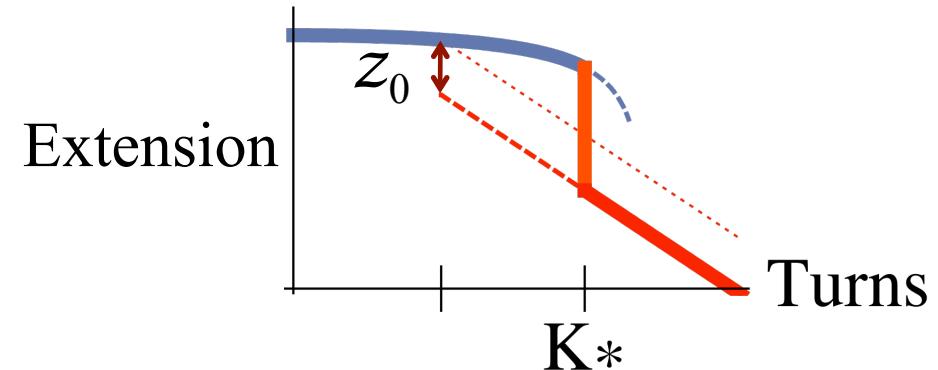
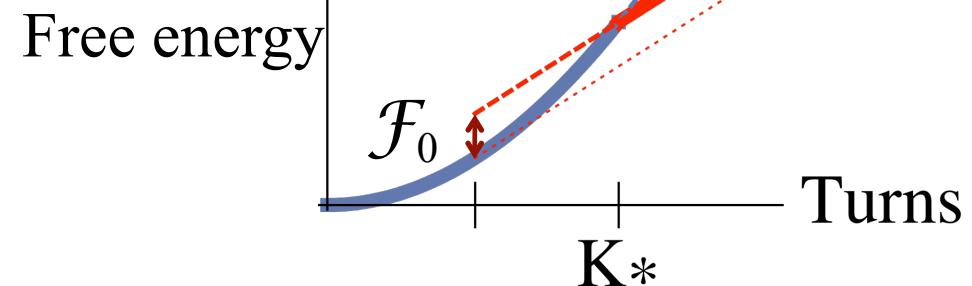
Without interface (Marko)

[Linear]



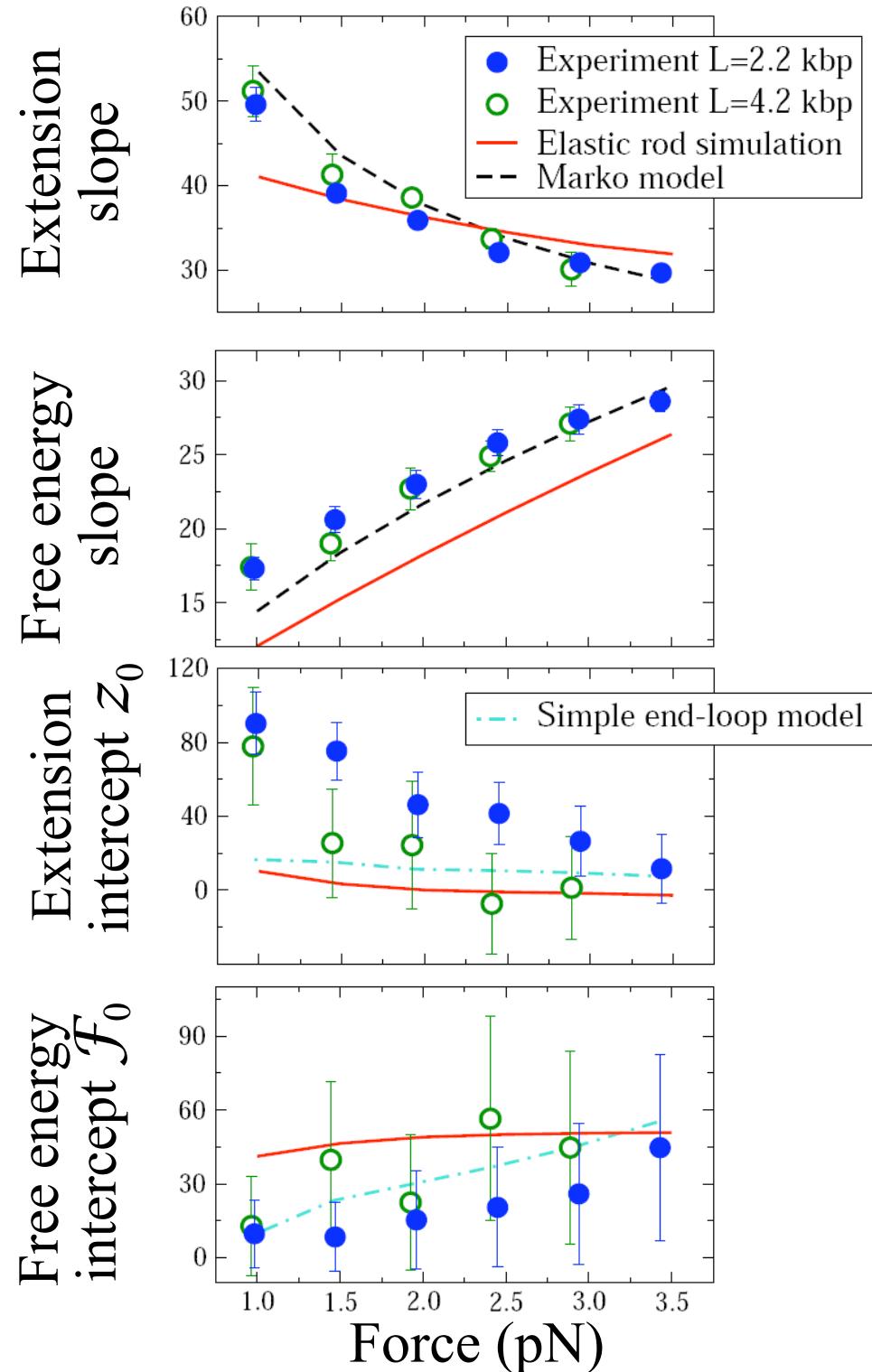
With interface (us)

[Linear + intercepts]



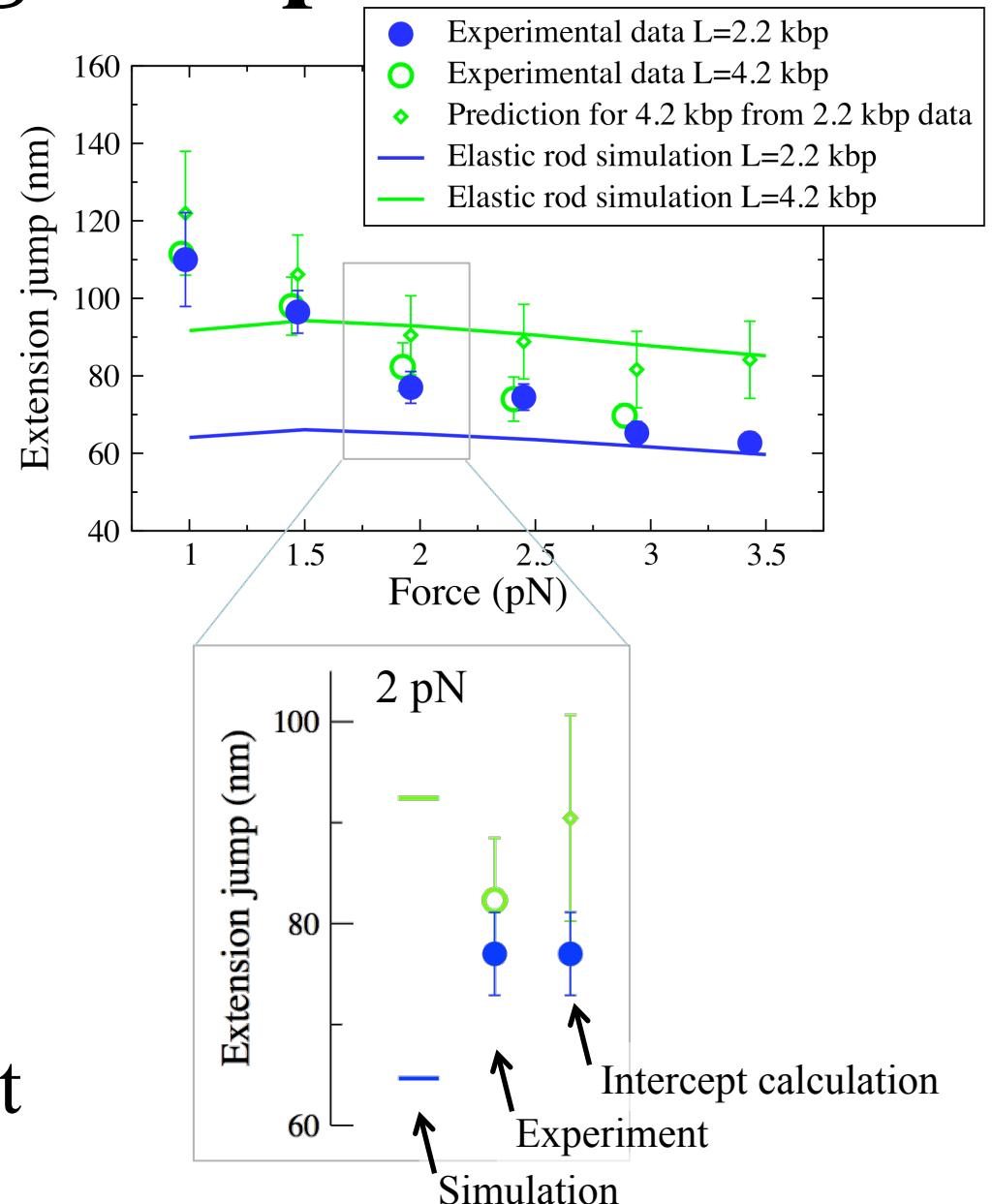
Coexisting state theory

- We can measure slopes and intercepts vs. force from experiment and simulation
- These predict extension and torque jumps
 - Experiment ⇒
 - Length-dependence ✓
 - Can also test DNA models



Predicted length-dependence

- Simulation showed large length-dependence of extension jump
- Data measured using **2.2 kbp** predict the extension jump using **4.2 kbp**
 - Gives smaller length-dependence, consistent with exp't



Conclusions

- Two-phase coexistence model \Rightarrow torque jump and length-dependence
- Predicted torque jump can be measured
- Small length-dependence of extension jump consistent with measured parameters
- Next: What is wrong with the DNA model?

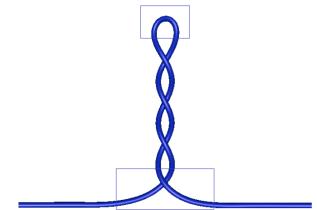


Extension and torque jumps
as a function of coexisting
state parameters

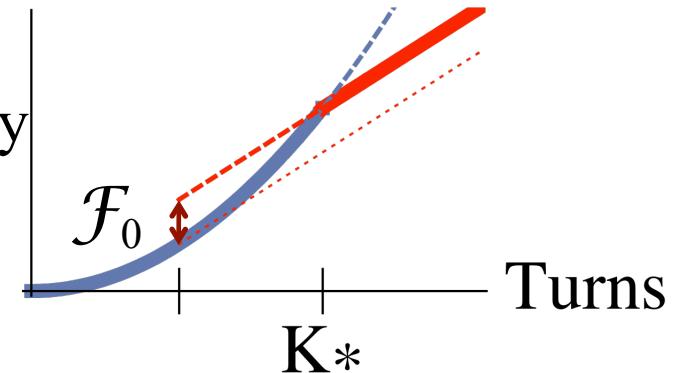
$$\Delta z = z_0 + q \sqrt{\frac{L\mathcal{F}_0}{2\pi^2 C}} - L \left(\xi(\tau) - \xi(\tau + \sqrt{2C\mathcal{F}_0/L}) \right)$$

$$\Delta\tau = \sqrt{\frac{2C}{L}\mathcal{F}_0}$$

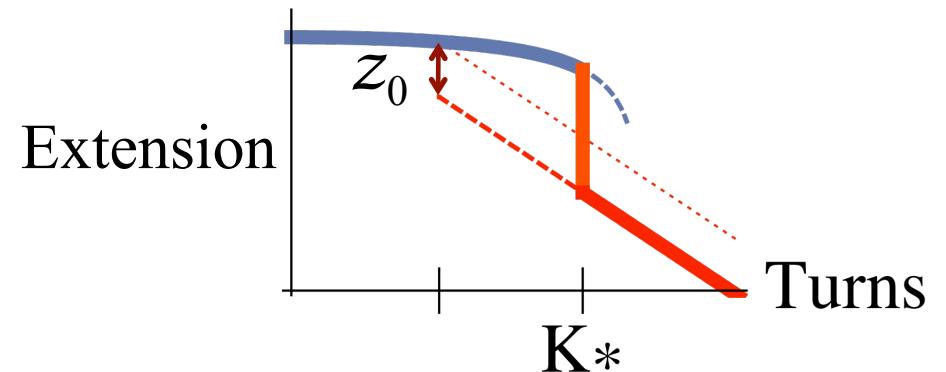
With interface (us)
[Linear + intercepts]



Free energy



Extension



Torque

