



ST557: HOMEWORK 1

Brian Cervantes Alvarez
October 9, 2023

Question 1

```
# Set random seed for reproducibility
set.seed(503)

# Read HW1Q1 dataset in using base R
ds <- read.csv("HW1Q1.csv")
# Show first 5 rows
head(ds, 5)
```

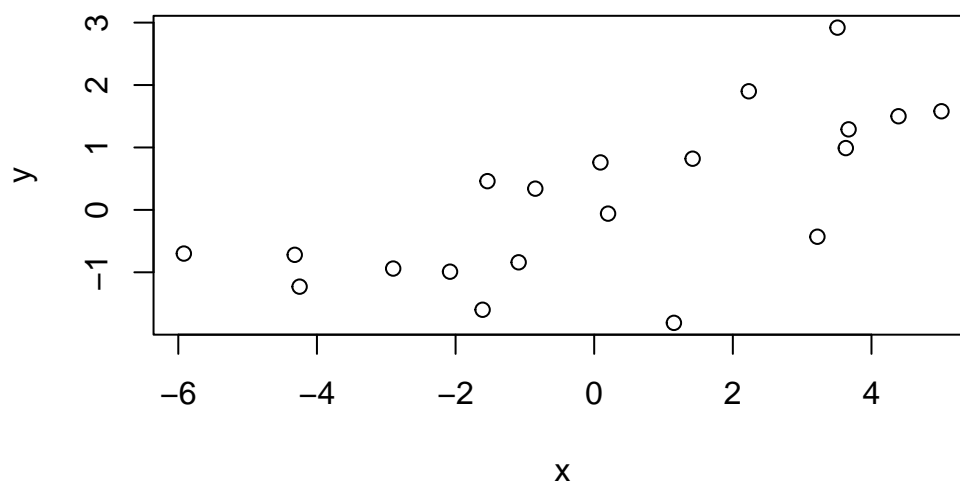
	X	Y
1	-1.54	0.46
2	-4.25	-1.23
3	-0.85	0.34
4	-2.90	-0.94
5	-1.09	-0.84

Part A

Read this data into R using `read.csv()`. Create a 2-dimensional scatter plot of the 20 observations (use `plot()` function in R).

```
# Get X and Y Components into vectors
x = ds$X
y = ds$Y

# Create scatter plot of Y ~ X
plot(x,y)
```





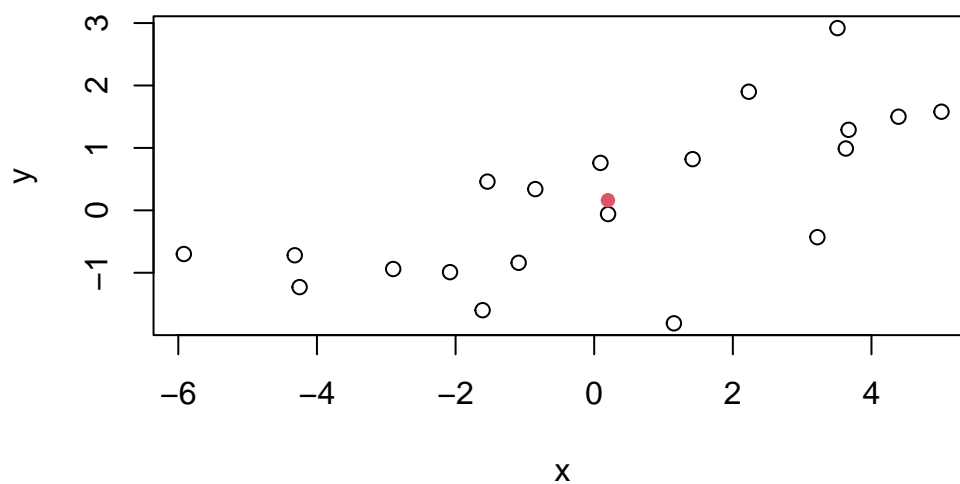
Part B

Find the sample mean vector, and add this point to the plot using `points()`. You can make this point a different color using the `col=` argument, or you can make it a different plotting character using the `pch=` argument. For example: `> points(sampMean[1], sampMean[2], pch=16, col=2)`

```
plot(x,y)

sampMeanX = mean(x)
sampMeanY = mean(y)

points(sampMeanX, sampMeanY, pch=16, col=2)
```





Part C

Find the sample covariance matrix.

```
# Sample covariance matrix  
sampCov <- cov(ds)
```

```
sampCov
```

	X	Y
X	10.140227	2.852078
Y	2.852078	1.668133



Part D

Find the eigendecomposition (spectral decomposition) of the sample covariance matrix using `eigen()`.

```
sampEigenDecomp <- eigen(sampCov)
```

```
sampEigenDecomp
```

```
eigen() decomposition
```

```
$values
```

```
[1] 11.0108859  0.7974741
```

```
$vectors
```

```
      [,1]      [,2]
```

```
[1,] -0.9564274  0.2919702
```

```
[2,] -0.2919702 -0.9564274
```



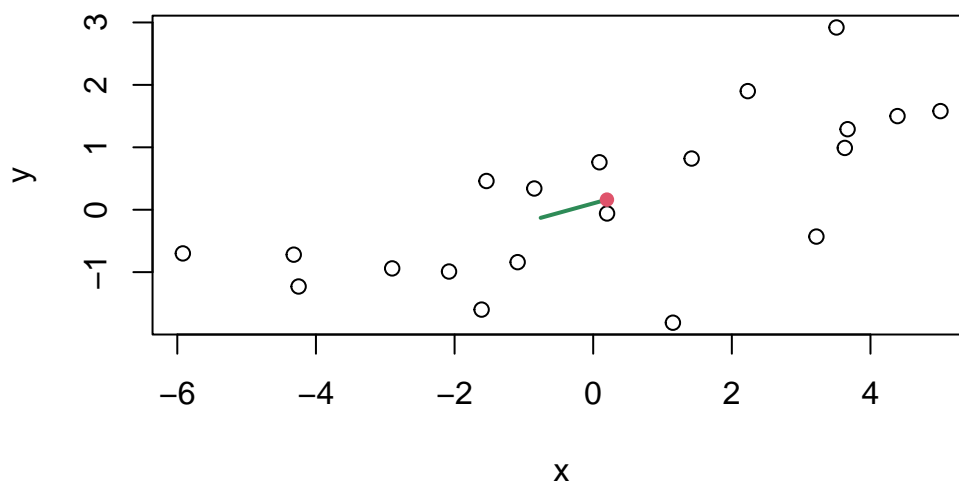
Part E

Add the eigenvector corresponding to the largest eigenvalue to the plot as a vector from the sample mean using `lines()`. Be careful here: if the first eigenvector is (v_1, v_2) and the sample mean vector is (\bar{x}_1, \bar{x}_2) , you want a line from (\bar{x}_1, \bar{x}_2) to $(\bar{x}_1 + v_1, \bar{x}_2 + v_2)$."

```
# Find the index of the largest eigenvalue
largestEigenvalue <- which.max(sampEigenDecomp$values)
# Extract the eigenvector corresponding to the largest eigenvalue
largestEigenvector <- sampEigenDecomp$vectors[, largestEigenvalue]

# Calculate the endpoints of the line segment
sampMeanX <- mean(x)
sampMeanY <- mean(y)
xend <- sampMeanX + largestEigenvector[1]
yend <- sampMeanY + largestEigenvector[2]

plot(x,y)
# Add the line segment to the plot
lines(c(sampMeanX, xend), c(sampMeanY, yend), col = "seagreen4", lwd = 2)
points(sampMeanX, sampMeanY, pch=16, col=2)
```



Discussion for Part E

Question: Describe how the direction of this eigenvector relates to the cloud of data points

The eigenvector follows the trend of the data points, which themselves are showing a positive increasing trend, and it culminates precisely at the location of the sample means for X and Y.

Question 2

