Comparisons of surface wave amplitude decay for colocated rotation and translation measurements

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SUMMARY

The broad-band surface wave magnitude equation assigns magnitude based on station-receiver distance and peak waveform amplitude; it is standard practice to use the vertical component of peak ground velocity, so that only contributions from the vertical component of Rayleigh waves are present in the recorded surface wave train. With the advent of rotational ground motion data from instruments such as ring laser gyroscopes and fiber-optic gyroscopes, it is possible to consistently measure peak amplitudes of rotations about the vertical axis for transient seismic waves. In the surface wave train, these observations are theoretically sensitive to the transverse direction of Love waves, unaffected by the horizontal component of Rayleigh waves. We use this concept to study the amplitude decay of rotations versus translations, and determine the necessity of separate surface wave magnitude equations for Love and Rayleigh waves. Utilizing a large database of recorded seismic events of colocated translations and rotations, collected in Wettzell, Germany, we empirically define new magnitude scales for multiple measured observables: rotation rate, rotation, vertical velocity and transverse velocity. Results indicate that rotation amplitudes decay faster over distance compared to velocity amplitudes for the same events, and that the current surface wave magnitude equation is insufficient for predicting the amplitudes of either observable. Synthetic seismograms were produced using Specfem3D Globe on a full scale 3D global model with realistic crustal structuring to compare against observations. Findings suggest that the current global models available for forward simulation are inadequate for accurately recreating the observed amplitude decay of both translations and rotations.

Key words: magnitude, rotational ground motions, seismic instrumentation, amplitude decay

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1 INTRODUCTION

For over a decade, the application of ring laser gyroscope technology to the field of seismology has allowed for near-continuous,
direct, measurements of rotational ground motions. An ever growing number of observations from seismic events of varying size,
distance and source mechanism, has been collected in an expansive catalog of waveform recordings for both direct rotation, and
colocated translation measurements. Previous work on this unique
waveform dataset includes phase comparisons of translations and
rotations with estimations of horizontal phase velocities (7), automatic standardized processing of rotation and translation data (9),
variations of surface wave energy in oceanic microseisms (15).

Much of this preceding work however, focuses on single events, or collections of non-earthquake sources.

In this paper, we aim to characterize and understand the differences in amplitude decay behavior of rotational and translational ground motion for a large number of seismic events. To do this, we make use of a sizeable catalog of earthquake data, as measured by an observatory based ring laser gyroscope, and colocated broadband translation sensor. By processing rotation and translation observations in a near identical manner, we hope to directly compare results over a large set of event magnitudes, epicentral distances and azimuths. We additionally seek to use this information to better understand decay characteristics of Love and Rayleigh waves.

This paper builds on work previously addressed by Igel et al. (6), where the question was posed: whether observed peak rotation amplitudes matched with expected values given by the surface wave magnitude equation. At the time, a limited number of recorded events lead to a small sample size. With a much larger number of events now currently available, we attempt to readdress

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2 Bryant Chow

this question, while also approaching the problem from the unique perspective of deriving magnitude scales to quantify and compare the decay characteristics of rotations and translations. Due to the uniqueness of our instrumental setup, we are restricted to single station observations. In order to provide comparisons to our observations, global 3D synthetic simulations were run with the wave propagation code Specfem 3D Globe [citation needed?]. Real seismic event locations, source parameters, and station locations are used, in order to provide the most comparable synthetic setup to observations.

With these observations, we aim to make quantitative statements on surface wave amplitude decay, as well as to provide magnitude scale equations that may prove useful in determining expected rotation amplitudes from seismic events.

1.1 Rotational Ground Motions

Rotational ground motions induced by seismic events can currently be observed through direct measurement, and through array analysis of translation sensors (13). In the latter, spatial gradients are taken for measurements in an adequately spaced array of translation sensors, in order to derive components of the strain tensor. One shortcoming of array based methods, however, is the necessity for multiple instruments with optimal array spacing and geometry, such that spatial gradients can be derived. With unique instrument designs, however, direct gradient measurements are possible (10).

Observations for this study were recorded by the Großring (G-ring) (10) (11), a 4x4m helium-neon ring laser gyroscope, located at the Geodetic Fundamentalstation in Wettzell, Germany (49.144°N, 12.87°E). The G-ring operates on the principle of Sagnac interferometry (14), which relates interference of counter propagating light beams to absolute rotation rate, through the following equation,

$$\delta f = \frac{4A}{\lambda P} \mathbf{n} \cdot \mathbf{\Omega},\tag{1}$$

where the constants are given by instrument area A, perimeter P and operating light wavelength λ . Equation 1 relates an observable beat frequency δf [Hz] to absolute rotation rate Ω [rad/s].

It is important to note that given stable instrument geometry and lasing, changes to the beat frequency δf , can only be introduced by changes to the inner product of the plane normal ${\bf n}$ with the rotation rate direction $\hat{\Omega}$ (e.g. through instrumental tilt), and through externally induced rotations (e.g. the passing of seismic waves). It has been shown that changes to the inner product as produced by tilt are one to two orders of magnitude smaller than rotations produced by passing seismic waves (8) (10) (11), this provides the unique benefit that the G-ring (and other instruments operating on this principle) is theoretically insensitive to translations, only sensitive to externally induced rotations.

1.1.1 Phase velocity relation

It has been shown previously (7), that for a simple plane wave, the amplitudes of vertical rotation rate Ω_z and transverse acceleration \ddot{u}_t can be related through the equation

$$\frac{\ddot{u}_t}{\Omega_z} = -2c,\tag{2}$$

where c represents an apparent horizontal phase velocity. This re- 119

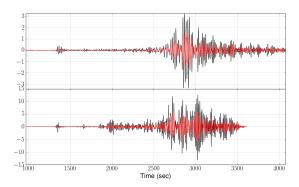


Figure 1. Teleseismic event filtered at dominant period 20s. Note the phase matching of transverse acceleration and rotation rate, as well as the calculated value of horizontal phase velocity, c=3.81 km/s.

lationship shows that, given a sufficient event-receiver distance (allowing a plane wave assumption), measured rotations are sensitive to the transverse component of translation, represented in teleseismic waves by surface horizontal waves (i.e. SH or Love waves). It also shows that waveforms of transverse acceleration and vertical rotation rate should theoretically be in phase, with oppositely polarized amplitudes, for passing horizontal waves. This can be seen in Figure 1, showing two superimposed traces of rotation rate and transverse acceleration (filtered at T=20 s) for G and a colocated broad band seismometer (top) and synthetically generated seismograms (bottom). For the observations, following Equation 2, a value of 3.81 km/s is calculated for the horizontal phase velocity, which matches well with previous findings of phase velocity from rotational studies for this area (6).

1.1.2 Peak correlation coefficient

Correlations are a useful measure of similarity between two signals. It has been shown previously that for collocated measurements of vertical rotation rate and transverse acceleration, high values (> 0.9) of zero lag correlations can be obtained in time windows centered around surface wave arrivals. Zero lag correlation coefficients are routinely computed for events measured by G (9), and are used in this study as a filtering tool to highlight "bad" events that exhibit low signal to noise ratios, or dissimilar waveforms which may arise due to non-physical effects (e.g. instrumental effects). Here, the largest correlation coefficient obtained for a seismogram is labeled the peak correlation coefficient (PCC), and is used as a representation of data quality.

1.2 Magnitude scales

Here we discuss the common magnitude scale equation, and propose using a modified version as a method for comparing amplitude decay of various observables. Amplitude based magnitude scales provide empirically derived relationships between maximum trace amplitudes and source-receiver distances. Magnitude scales offer useful and quick estimates of relative sizes of earthquakes in a simple, standard manner. The International Association of Planets Seismology and Earths Interior (IASPEI) Working Group on Magnitudes proposed a modified version of the original surface wave magnitude equation, known as the Prague formula, proposed by (@warning Citation 'karnik1962standardization' on page 2 unde-

fined). This new formula, named the broad band surface wave magnitude equation is compatible for use with modern day broadband seismic instruments (2).

In this work, we adhere strictly to the standard procedures provided by IASPEI as an outline for defining our own empirical magnitude scales. In turn, we use these derived scales as a tool for quantifying amplitude decay for different measured observables.

1.2.1 Standard Procedures

The Working Group on Magnitudes' standard procedures gives the revised surface wave magnitude equation for broad-band instruments as.

$$M_S^{BB} = log_{10}(V/2\pi) + B \cdot log_{10}(\Delta) + C,$$
 (3)

where the constants B=1.66 and C=0.3 control amplitude decay and order of magnitude, respectively. The parameter V should be the maximum trace amplitude (in nanometers second $^{-1}$) in the surface wave train, for a seismogram proportional to velocity, measured on the vertical component.

Further criteria given by IASPEI posit that the period of the surface wave should lie within 3 s $\leq T \leq 60$ s, while epicentral distances should be between $2^{\circ} \leq \Delta \leq 160^{\circ}$. It is further recommended that only shallow focus earthquakes should be considered, as medium to deep events are less capable of generating strong surface waves [citation needed?]. Maximum trace amplitudes are described as one half the largest peak to adjacent trough deflection, and associated period are given as two times the temporal difference between peak and adjacent trough. All events and processing steps in this paper adhere to these guidelines.

1.2.2 Instrumental proxies for Love and Rayleigh waves

A standard procedure for determining surface wave magnitude scales is to take amplitudes measured on the vertical component of translation. This is because vertical translation should only be sensitive to the vertical motions of Rayleigh waves, whereas vector sums of horizontal components can be influenced by both Love and Rayleigh waves. In the same vein, velocity measured on the transverse component should only show sensitivity to Love waves (and radial components should only be sensitive to the horizontal component of Rayleigh waves). This is however not common practice, due to the necessity of rotating horizontal components to the correct azimuth, which can be affected by ray paths and local site effects and epicenter location. The G-ring, which is 1) insensitive to translations and 2) proportional in phase and amplitude to transverse acceleration, should only be sensitive to Love waves in the surface wave train, irrespective of azimuth.

In this study we use our instruments as physical wave-filters, in order to study individual phases in the surface wave train. This allows us to analyze the influences of Love waves and Rayleigh waves separately. By comparing the vertical and transverse components of translations, to the vertical component of rotation, we can understand, by proxy, the wave types they are sensitive to.

1.2.3 Application of rotations to magnitude scales

In order to give a fair comparison to translations using derived magnitude scales, a rotation parameter complementary to velocity is 223 necessary. In Section 1.1.1, an equation is given that relates rotation rates Ω with accelerations \ddot{u} . It would make the most sense, 225

then, to compare velocities \dot{u} with rotations ω (by integrating both sides). However, without previous work to draw precedence from, and for completeness, we present observations of both rotations and rotation rates in this study.

2 EVENT CHOICE

The G-ring has been continuously recording at its current resolution since May, 2009 [citation needed]. The time range for events used in this study spans June 1, 2009 to September 1, 2016. An initial earthquake catalog was fetched from the Harvard Global Centroid Moment Tensor (GCMT) (4), with events filtered by acceptable magnitude, source depth and epicentral distance from Wettzell, Germany. At this point we imposed the restriction that the derived "magnitude" as given by our magnitude equations, should fall as close to the given surface wave magnitude as possible. This ensures that our derived scales do not stray too far from established scales. This meant that only events with centroid moment magnitude values of $6 \le M_{\rm wc} < 8$ (as published in the GCMT catalog), were considered; surface wave magnitude and moment magnitude are approximately equal in this range (12). Zero-lag cross correlations of transverse acceleration and rotation rate were taken in order to calculate peak correlation coefficients (Section 3.1). Events were not considered if their peak correlation coefficient did not meet the criterion PCC < 0.7.

These choices for event criteria narrowed the catalog down to roughly 500 events in the given time period. Each event was appropriately filtered and processed (Section 3.1), and waveforms were individually inspected. Waveforms that exhibited anomalous behavior (e.g. unexpected high amplitude peaks outside the surface wave train, high signal-to-noise ratio etc.) were rejected. A final event catalog of 243 events was reached, shown in Figure 2.

3 METHODS

3.1 Data Processing

Events were processed in a similar fashion as the processing outlined in Salvermoser et al. (9). Raw, continuous translation data in North, East and vertical components, as well as vertical rotation rate data, was fetched based on event origin time. Instrument response correction produced translation seismograms proportional to units of velocity (nm s $^{-1}$). Epicentral distances (Δ) and theoretical backazimuth values were calculated from station-receiver latitude longitude pairs, and events were separated into categories of close ($\Delta < 3^{\circ}$), local ($\Delta < 100^{\circ}$) and far ($\Delta \geq 100^{\circ}$). Translations were rotated into the transverse, radial, vertical coordinate system by the appropriate theoretical backazimuth. Measurements from ring laser gyroscope instruments do not require frequency dependent instrument correction [citation needed?], therefore only a simple scale factor was necessary to retrieve seismograms proportional to rotation rate (nrad s $^{-1}$).

Rotation rate traces, in units of nanoradians second⁻¹ were integrated to provide measurements of rotation (nanoradians), and transverse velocity was integrated to retrieve transverse acceleration, which was subsequently used to calculate correlations with vertical rotation rates. A bandpass filter was applied to all traces for periods between $3 \text{ s} \leq T \leq 60 \text{ s}$, in accordance to the IASPEI standard procedures. Peak amplitudes were chosen by finding minimum and maximum trace values and the largest associated peak or trough, respectively. The larger of the two was recorded, alongside

4 Bryant Chow

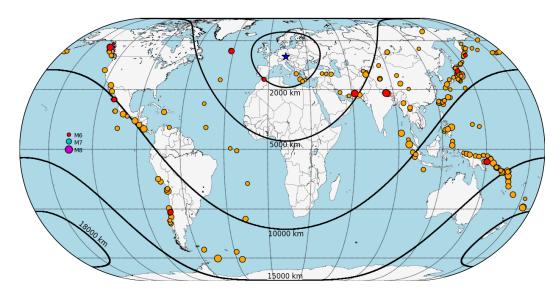


Figure 2. Event map. Size represents moment magnitude (M_{wc}). Orange dots show observed earthquakes used in magnitude scale derivation. Red dots show the ten events chosen for generation of synthetic seismograms. Black lines are equidistant points from the blue star, which represents the location of G in Wettzell, Germany (49.144°N,12.87°E).

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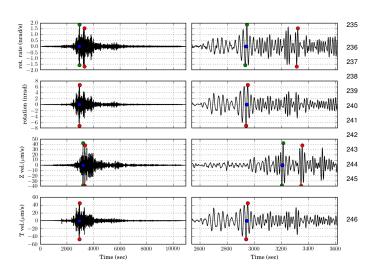


Figure 3. Left: Seismograms of [event information here]. From top to bottom: rotation rate, rotation, vertical velocity and transverse velocity. Red and green dots show largest peak to adjacent trough distance and largest trough to adjacent peak distance, respectively. The blue dot shows the zero crossing for the chosen peak to peak amplitude.

Right: Zoomed in section of seismograms, showing the visible difference in arrival times of the Love wave (as seen on rotation and transverse components), and the later arriving Rayleigh wave (as seen on the vertical component).

the associated arrival time and dominant period, taken as two times the distance between peak and adjacent trough.

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Theoretical considerations used to restrict search to the sur- 252 face wave train proved inconsistent over a large number of events, 253 so maximum amplitudes in the entire trace were considered. 254 Through manual inspection, picked amplitudes that fell outside 255 the surface wave train (which occurred very infrequently) were 256 rejected. An example of the waveforms and amplitude picking is 257 shown in Figure 3.

3.1.1 Zero-lag correlations

To calculate peak correlations, traces of transverse acceleration and vertical rotation rate were segmented into small time windows based on the event-station distance. In each time window, a zero-lag correlation was performed, and a single value of correlation produced. From the entire trace, the max value was taken to represent the peak correlation coefficient. For most waveforms, the peak correlation coefficient lie in the surface wave train. As mentioned previously, these peak correlation values are used extensively as a ranking system for events, providing a quickly attainable measure of waveform quality.

3.2 Curve fitting

To quantify amplitude decay, magnitude scale coefficients were fit to the data using a simple linear regression. Equation 3 represents a relationship between magnitude and amplitude for a single event. Using Equation 3, a collection of n events can be represented in the form.

$$\begin{pmatrix} log_{10}(\Delta_1) & 1\\ log_{10}(\Delta_2) & 1\\ \vdots & \vdots\\ log_{10}(\Delta_n) & 1 \end{pmatrix} \begin{pmatrix} B\\ C \end{pmatrix} = \begin{pmatrix} M_{\text{wc}_1} - log_{10}(V_1/2\pi)_{\text{max}}\\ M_{\text{wc}_2} - log_{10}(V_2/2\pi)_{\text{max}}\\ \vdots\\ M_{\text{wc}_n} - log_{10}(V_n/2\pi)_{\text{max}} \end{pmatrix},$$
(4)

which can be further condensed to the matrix-vector form, $\mathbf{Gm} = \mathbf{d}$. The unknowns B and C are represented in the vector \mathbf{m} , and can be solved for through the normal equation $\mathbf{m} = (\mathbf{G}^T\mathbf{G})^{-1}\mathbf{G}^T\mathbf{d}$. By determining values of B and C, we create an empirical magnitude scale that best describes the amplitude decay behavior of our events. In Equation 4, we impose that our derived magnitude value should be as close to an events given moment magnitude as possible, by setting M_S^{BB} equal to the value of M_{wc} retrieved from our event catalog.

95% confidence intervals were constructed for each parameter of the vector \mathbf{m} . These were calculated with the variance of estimates of the jth parameter of \mathbf{m} by the equation $\hat{m}_j \pm c \sqrt{v \hat{a} r(\hat{m}_j)}$,

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where the value of c is given as 1.96 for a confidence interval of 315 $\alpha = 0.95$.

SYNTHETIC SEISMOGRAMS

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Due to the unique instrumental setup of the G-ring, there are currently no other rotational instruments with as much temporal coverage to draw comparisons from. It should be mentioned that there 323 are other available rotation instruments which allow for single event 324 case study analyses (3) [more citations needed?], however large catalogs like that available from the G-ring are currently unavailable. One possibility for gathering more observations would be through array derived rotations as a substitute for direct rotation measurements; this option was noted during analysis, however it proved difficult finding sufficient long-term arrays with the optimal station spacing. In the future if this type of data became available, it would provide a very useful addition of information to this study. In lieu of observations, we instead turn to waveform modeling to generate synthetic seismograms, with which we recreate our experimental setup and provide a comparable set of synthetic observations.

The seismic wave propagation code Specfem3D Globe was employed. A realistic global model featuring 3D crust and mantle models was used, and the simulation featured effects that might have potential influence on surface waves at the periods of interest. These effects include: ocean loading, Earth's ellipticity, topography, self gravitation, Earth's rotation and 1-D attenuation. Event locations and moment tensors were taken from 10 real seismic events present in the observation catalogs. Events were chosen based on observation data quality, as well as event location and depth, so as to provide a varied distribution of source-receiver pairings. Table 1 provides detailed information on the chosen events.

In each simulation, events were initiated as point sources. The simulation corner frequency was set to 10 seconds, and simulations were run for one hour simulation time. As computational cost is independent of number of stations, more than one hundred stations were included; Global Seismic Network (GSN) locations were used, as well as location of the G-ring, and the German observatory station Fürstenfeldbruck. The number of simulated stations was X, and the number of station-receiver pairs X (with some station-receiver pairs falling outside the distance bounds specified in Section 1.2.1).

The direct outputs of Specfem3D were adjusted to produce displacement (in units of meters) in the transverse, radial and vertical components, by rotation with respect to the theoretical backazimuth. Direct rotation (in units of radians) in the same coordinate system was also outputted. During processing, translation seismograms were differentiated to retrieve velocity waveforms, and rotation was differentiated to produce rotation rate waveforms. A work flow identical to that used for observations was employed to calculate peak trace amplitudes, and a magnitude equation was fit to the 365 data for comparison.

RESULTS

Derived magnitude scales

Decay characteristics of rotations and translations were derived by solving for constants B and C in Equation 4. The values for each scale are presented in Table 2. For an additional check 372 on site-dependent data quality, the same analysis was performed 373 on translation observations taken at the geophysical observatory 374 Fürstenfeldbruck, Germany (FUR; 48.163°N, 11.275°E), located roughly 200 km south-west of Wettzell. Though a smaller subset of events was used due to data availability, the results confirmed those given at Wettzell.

The value of B covers a large range, from 1.084 to 1.823 for vertical velocity \mathbf{M}_Z^{WET} and rotation rate \mathbf{M}_{RR}^{RLAS} , respectively. Rotation \mathbf{M}_{RT}^{RLAS} falls closest to the standard IASPEI value of B=1.66. Velocity values match quite consistently between Wettzell and Fürstenfeldbruck, with FFB showing slightly higher amplitudes, as seen in the value of C, which controls the order of magnitude of expected amplitudes. In comparing these two stations, consideration should be given to the subsurface composition; the geodetic observatory in Wettzell overlies granitic bedrock, while Fürstenfeldbruck sits atop a sedimentary basin [citation needed?], which are known to amplify passing seismic waves [citations of papers for basin amplification effects?]. It is therefore not surprising, and perhaps expected, that we observe on-average larger amplitudes at Fürstenfeldbruck. This is visible in the transverse component, sensitive to Love waves, in Figure ??, however the vertical component, sensitive to the vertical component of Rayleigh waves, does not reflect this.

Variations of velocity based scales from the surface wave magnitude equation are large, but not as unsurprising as they first appear. It has been proposed that the modern surface wave magnitude equation has a systematic distance bias, which tends to under predict amplitudes at greater distances (5). Previous works have proposed corrected values of the coefficients B and C, using a global catalog (5) and a European regional dataset (1). These corrections match well with the vertical velocity scales derived in this work; the values (adjusted for the change of units in the IASPEI scale) are presented in Table 2 as ${\cal M}_S^{HH}$ and ${\cal M}_S^{AF}$ for scales proposed in Herak & Herak (5) and Ambraseys & Free (1), respectively.

There exists a noticeable difference between values of B for transverse and vertical velocities. The vertical velocity scale is expected to present an identical setup to the broadband surface wave magnitude equation, however it gives with the largest discrepancy, for both stations WET and FUR. Transverse velocity, which should sample Love waves, same as rotations (see 1.2.2), shows a larger value for B as compared to vertical velocity.

It is to be expected that rotation rate shows a larger value for B as compared to rotation, as rotation is being compared with its time derivative, which contains amplified high frequency components and should exhibit faster decay with distance as the wave path filters out this high frequency energy.

Confidence intervals, which can be viewed as a quantification of misfit between the fitted magnitude equation and the observations, shows the uncertainty of the observations due to the limitation of spatial coverage; in Figure 4, the red shaded area shows the confidence interval of the M6 decay line. It should be noted that the magnitude scale is heavily controlled by its end members. Due to a lack of events at very close epicentral distances, it is difficult to constrain the decay here, and the few events at distances less than 20° have a strong influence on the derived value of B. It can also be seen that more than one third of the events used in this study fall around 80° epicentral distance, due to geographic constraints; many of these events occur around Japan.

5.2 Observed and synthetic waveforms

For each of the simulated events, synthetic seismograms were generated for all stations mentioned previously. Waveforms for station WET were compared for all possible components of translation and 375

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Date	Time (UTC)	Lat(°)	Lon(°)	Depth(km)	$\mathbf{M}_{\mathbf{wc}}$	Flinn-Engdahl Region	Peak Corr. Coeff.
2010-07-18	13:34:59	-5.93	150.59	35.0	7.32	New Britain Region, P.N.G.	0.98
2011-09-16	19:26:41	40.27	142.78	35.0	6.67	Off East Coast Of Honshu, Japan	0.99
2013-01-05	08:58:19	55.39	-134.65	10.0	7.53	Southeastern Alaska	0.95
2013-04-16	10:44:20	28.03	62.0	80.0	7.74	Southern Iran	0.98
2013-04-19	19:58:40	49.97	157.65	15.0	6.06	East Of Kuril Islands	0.99
2015-02-13	18:59:12	52.65	-31.9	16.7	7.07	Reykjanes Ridge	0.99
2015-04-25	06:11:26	28.15	84.71	15.0	7.88	Nepal	0.99
2015-09-13	08:14:12	25.14	-109.43	10.0	6.6	Gulf Of California	0.98
2015-09-16	23:18:41	-31.56	-71.43	28.4	7.1	Near Coast Of Central Chile	0.99
2016-01-25	04:22:02	35.65	-3.68	12.0	6.38	Strait Of Gibraltar	0.99

Table 1. List of events used as synthetic sources in Specfem3D. Peak correlations are used as a measure of waveform quality, and only events with the highest values were used, in order to provide the best comparisons of synthetics with observations. Events were also chosen based on a diverse coverage of magnitudes and epicentral distances from the ring laser stationed in Wettzell, Germany. Event information taken from the GCMT catalog.

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rotation. In one event (2010-07-18), a fore shock in the observations 418 went unnoticed during event choice, which prevented useful com- 419 parison. In most other cases, P-wave and S-wave arrivals matched well. Later arrivals are not in agreement with very different behavior exhibited by arriving surface waves. This can be potentially ex- 422 plained by the use of point sources for such large magnitude earthquakes; the effects of the source time function as well as the rupture 424 plane are not captured in our synthetics, and we therefore do not expect to match phases of surface wave arrivals. Consideration should also be given to the topographic and crustal models included, which 427 affect the resulting surface wave waveforms. Fortunately we focus on peak amplitude measurements in this work, and therefore are not 429 deterred by the misfit of waveforms. The broad frequency range (10-60s) also present difficulties in matching waveforms. Narrow pass filters (i.e. 20 second dominant period) capture similarities better, however in this study we aim to stick to the definition of the 433 IASPEI surface wave magnitude equation, which calls for a broad frequency range.

As to be expected, the observed waveforms present a much 436 more complicated picture of arrivals. In most of the observations, 437 noise levels are high enough that determining body wave arrivals is 438 difficult compared to the synthetic models. Even for narrow pass fil- 439 ters, as in Figure 7, observation and synthetic seismograms do not 440 exhibit high correlations. Neverthless, peak amplitude picking in all 10 events falls in the surface wave train which allows for determination of magnitude scales - this allows us to make comparisons without relying on detailed waveform information.

Comparisons of transverse acceleration and rotation rate provide solid phase matching throughout the waveform, with the strongest correlation during the surface wave train, even for relatively wide bandpass filters (i.e. 10 to 60 seconds). This is true for both observations and synthetics, and also allows for the calculation of phase velocities. Because this is not the goal of this paper, we do not delve too far into the analysis of phase velocities, however taking peak value amplitude ratios for broad bandpass filter ranges (which would average the horizontal phase velocities of each dominant period contained), we recover values ranging from 3 to 5 km/s.

5.3 Synthetic magnitude scales

Results derived from synthetic seismograms, shown in Table 2, 457 vary quite dramatically from the observed results; these results do 458 not reflect the same discrepancies that are present in the values 459 given by observations.

A visual representation for the synthetic rotation rate magnitude scale M_{RR}^{SYN} is shown in Figure 8. The distribution of points on this scale is much more uniform compared to ??, which can be attributed to the increased number of recordings for a single event due to the large number of synthetic stations. With so many station receiver pairs over a range of epicentral distances, there are roughly six times more observation points, which provides stronger coverage of epicentral distances. The number of events at very close distances is also quite low, similarly due to the imposed geographic considerations. The 95% confidence intervals provide a much narrower band, due to the larger number of events and the synthetic nature of this scale; single events providing data points over the entire distance range puts a strong constraint on the fitted decay constants.

The synthetic magnitude scales all exhibit very similar values for the decay constant B. The large variation in decay as seen in the observations is not captured here. Compared to the IASPEI magnitude scale, all the synthetic scales fall much lower in their value of B. Synthetic rotation rate gives the largest, or steepest decay constant at 1.215, by only a small margin. Transverse velocity falls in with the smallest value. Looking at the values of C, expected amplitudes are all also quite high, except for rotation rate. Vertical velocity exhibits a n

Expected rotation amplitudes

One useful aspect of magnitude scales is to provide an expected amplitude value for a given magnitude event at certain distance.

One area of interest in rotational seismology is the development of field deployable sensors. Due to the very low order of magnitudes of rotation signals (measured in nanoradian scale), it is a concern whether or not newly developed field deployable rotation sensors can reach the sensitivity necessary to capture the rotational motion amplitudes excited by regional or tele-seismic events. With the rotational magnitude scale derived here, we are able to create a list of observation based expected amplitudes. At the time of writing, the field deployable rotation sensor BlueSeis from the company iXBlue, has a noise floor of roughly 1 nrad/s/ \sqrt{Hz} [citation for ixblue?]. Referring to Table 2, the approximate maximum distance the sensor can be placed to detect a M_w5 event would be 21° epicentral distance, roughly 2300 km. This distance range would mean current day sensors could detect regional ¿M5 earthquakes. Other considerations must be taken into account before these values can be used for field deployment decisions, however it provides a useful jumping off point for future instrument deployments.

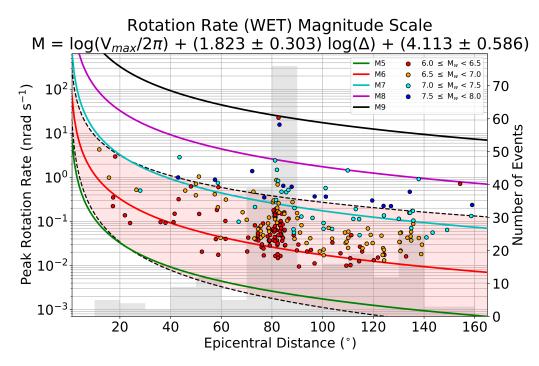


Figure 4. Rotation rate magnitude scale for observations. Event magnitudes separated by bins of 0.5 and denoted by color. Magnitude equation plotted by integer values as solid color lines. 95% confidence interval for M6 shown by the shaded red area, bordered by black dashed lines. The number of events for each epicentral distance bin shown by gray bars in the background.

Scale	Label	В	C	Wave
IASPEI	M_S^{BB}	1.66	0.3	Rayleigh
Herak Herak 1993	M_S^{HH}	1.094	1.429	Rayleigh
Ambraseys-Free 1997	M_S^{AF}	0.947	1.77	Rayleigh
Rotation	M_{RT}^{RLAS}	1.557 ± 0.295	4.186 ± 0.569	Love
Rotation Rate	M_{RR}^{RLAS}	1.823 ± 0.303	4.113 ± 0.586	Love
Transverse Velocity (Wettzell)	M_T^{WET}	1.45 ± 0.27	0.527 ± 0.521	Love
Transverse Velocity (FFB)	M_T^{FUR}	1.442 ± 0.27	0.447 ± 0.523	Love
Vertical Velocity (Wettzell)	M_Z^{WET}	1.084 ± 0.264	1.093 ± 0.511	Rayleigh
Vertical Velocity (FFB)	M_Z^{FUR}	1.095 ± 0.259	1.09 ± 0.502	Rayleigh

Table 2. Magnitude scales and derived constants with 95% confidence intervals for observations at instruments RLAS, WET (Wettzell, Germany) and FUR (Fürstenfeldbruck, Germany), for equations of the form $M = log_{10}(V/2\pi) + B \cdot log_{10}(\Delta) + C$. The final column gives consideration to the wave type that each instrument component should provide a proxy for.

Scale	Label	В	C	Wave
Synthetic Rotation	M_{RT}^{SYN}	1.204 ± 0.086	3.841 ± 0.159	Love
Synthetic Rotation Rate	M_{RR}^{SYN}	1.215 ± 0.086	4.007 ± 0.161	Love
Synthetic Transverse Velocity	M_T^{SYN}	1.094 ± 0.081	0.146 ± 0.16	Love
Synthetic Vertical Velocity	M_Z^{SYN}	1.206 ± 0.08	-0.011 ± 0.149	Rayleigh

Table 3. Synthetic magnitude scales and derived constants with 95% confidence intervals, for equations of the form $M = log_{10}(V/2\pi) + B \cdot log_{10}(\Delta) + C$. The final column gives consideration to the wave type that each instrument component should provide a proxy for.

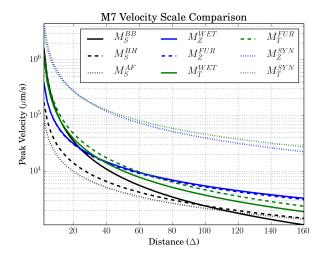


Figure 5. A comparison of velocity based scales for stations WET, FUR and synthetic scales, with the IASPEI scale used as reference. Peak amplitudes given in units of nanometers/s

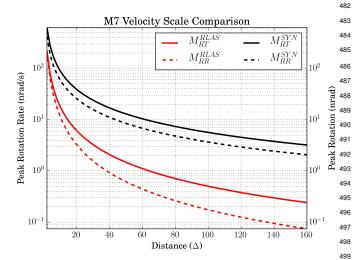


Figure 6. A comparison of rotation based scales for station WET and synthetic scales. Peak amplitudes given in units of nanoradians/s

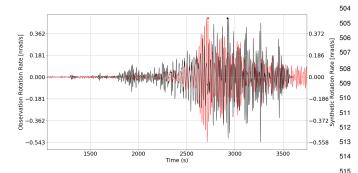


Figure 7. A comparison of synthetic and observed waveforms for an M6.1 event, East of Kuril Islands. Waveforms filtered at dominant period 20s.

6 DISCUSSION

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The long term continuous recordings of rotation and translation waveforms at Wettzell has provided us an extensive catalog of colocated observations to explore seismic signals of events with largely varying source parameters and travel paths. The motivation for addressing amplitude decays in the initial study of Igel et al. (6), was to determine whether or not decay of peak observed rotation rates was consistent with the definition of the commonly used surface wave magnitude equation. In this study we expanded our motivation to include the comparison of decay rates between rotations and translations, to see if and how these quantities might differ. Measurements of seismically induced rotation amplitudes have never been addressed on such a scale, and if rotations are to someday be incorporated into standard seismological practices, it is useful and beneficial to understand the general characteristics of their observed signals.

The rotation based magnitude scales presented in Table 2 present the idea that rotation amplitude decay is not exceedingly different from those for translation measurements; that is, values of B are not orders of magnitude different. Since rotation measurements in the surface wave train sample the horizontal nature of the Love wave, this finding is not so surprising, and of course was already shown previously by Igel et al. (6). It does prove reassuring that instruments measuring rotation, given the necessary resolution, will not face any differences in recording events at distance.

Although translation measurements exhibit lower values of B, it has been stated previously ((5)/(1)) that this result is not unexpected, and perhaps even a better representation of the surface wave amplitude decay. The stark contrast between the values of B for scales sensitive to Love waves versus Rayleigh waves is very interesting. Taking theoretical assumptions into account, we can use these results to make the statement that Love waves have a faster amplitude decay rate compared with Rayleigh waves. This statement is of course through instrumental proxies, however we can strengthen the case by taking transverse velocity into consideration, which has a value of B that lies closer to that of rotation (because we are using the same events for all scales considered, we are confident that these comparisons are made fairly); determining transverse velocity is dependent on correct rotating the North and East components, and it is possible that incorrect rotation can lead to mixing of Love waves and the radial component of Rayleigh waves. If radial and vertical components of Rayleigh waves decay at the same rate, then this would lead to the effect seen in Table 2: a slightly lower value of B than that of rotation, a scale that is instrumentally insensitive to translations. (A backazimuth value that is incorrect by 10° changes the expected amplitude of the transverse component by 75%.)

Although moment magnitude has proven a more grounded measure of earthquake size, surface wave magnitude is still used by agencies around the world. Previous literature has recommended that this scale should be amended in the face of having a potential distance bias. In this study we report the same findings: the current values of B and C for the surface wave magnitude scale are insufficient in predicting the magnitude based on surface wave amplitude values; both observationally and synthetically we show that values of B are systematically lower than the current value of B = 1.66.

Synthetic results prove drastically different from those predicted by observations, and warrants the doubt whether our synthetics lack the detail necessary to fully capture the reality of earth structure which strongly affects amplitudes of surface waves. 3D crust and mantel models, including topography and a host of other

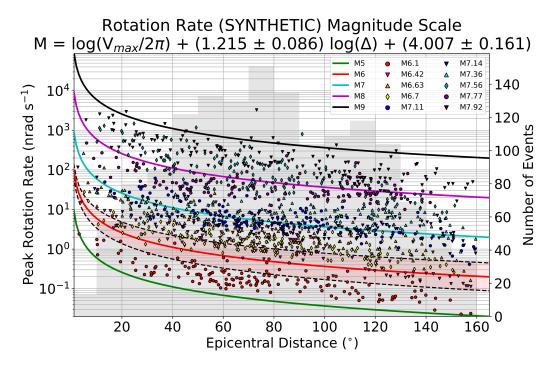


Figure 8. Rotation rate magnitude scale for synthetics. All objects similarly represented as in Figure 4. Colors of points here represent individual events simulated (for event information, see Table 1).

factors that play a role in surface wave amplitudes, still predicted amplitudes one order of magnitude larger than those observed at 557 our stations. This large discrepancy points to a need for a more detailed and realistic full earth model than what is available at the 559 time of writing, if it is to be used for this purpose of determining amplitude decays. 561

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Many questions arose from analysis of these results which would prove interesting to investigate, but fall outside the scope of this paper. One such question is understanding the cause of discrepancy between observed rotation and translation amplitude decays. If this is a detail related to the observable, would this affect still be seen if these analyses were also performed on rotation derived through array methods, or is this effect only noticeable on instruments operating on Sagnac interferometry. If, rather, this effect is a factor of the wavetypes our instruments are sensitive to: what, theoretically, causes the difference in decay rates between Love waves and Rayleigh waves? Is this detectable in other regions and tectonic settings, or only seen for stations on the European continent? 573 Perhaps this magnitude scale analysis could be performed only for tranvserse, radial and vertical components of single stations, to see if these values of B and C are recovered in other areas. In regards to the synthetics, what sort of modifications to our earth models are required to reproduce the effects we are seeing with our observations? If point sources are insufficient in producing the teleseismic amplitudes we observe, what level of complexity is required to accurately model waves at these periods and distances? In the same vein, how important is the observation setup; does number of stations, receivers and station-receiver pairs have a strong impact on the values we recover? Would an observational setup with hundreds of sensors and events provide a different perspective than what we $\,^{\,585}$ have seen here? Finally in regards to a rotation based magnitude 586 scale; if we are observing such large differences between rotation 587 and vertical velocity based magnitude scales, this might warrant 588 defining a new magnitude scale solely for Love waves. Ground mo- 589 tion from these Love and Rayleigh waves are starkly different and perhaps one single surface wave magnitude scale is insufficient. If these discrepancies show up also in previous literature, perhaps it is necessary to instead define M_S^{LOVE} and $M_S^{RAYLEIGH}$ to replace the current M_S^{BB} . At the time of writing, with the push for field deployable rotation sensors and with an increasing number of rotation observations available, it would be possible to quickly determine peak amplitudes of rotations for incoming surface waves and define some magnitude based on an instrument only sensitive to Love waves, extremely useful because it does not require the precise position of the event for determining the correct backazimuth. If this is the case, we propose in this discussion that the current rotation based magnitude scale given in Table 2 should be used as a preliminary Rotation magnitude scale for determining magnitudes of events for instruments measuring rotation on the vertical axis. We expect further observations, instruments and catalogs will be used to refine these preliminary values.

A lack of observations at epicentral distances less than 20° and greater than 140° provides large uncertainties in the accuracy of our rotation magnitude scale. Going forward, it would be immensely beneficial to collect peak amplitude values at these distances to provide further constraint on our magnitude scales. The inclusion of more stations recording the same event would also make these derived scales much more robust. Since it may be a some time before full networks of permanent six component stations are available, inclusion of array derived rotations would prove the most useful method in providing more data for determination of these magnitude scales. For synthetics, deeper exploration of individual waveforms might assist in understanding where our current global models fail in accurately recreating real world observations.

Measurements of rotations and spatial gradients has proven a very interesting theoretical aspect of a field which has become extremely proficient in stable observations of three translational components. With this new observable, we are able to revisit the-

10 Bryant Chow

ories proposed decades before with a new perspective. With the 653 590 development of translational and rotational magnitude scales, we 591 have determined some stark differences in observed amplitude de-592 cays between these two observables, and believe we can put forth 593 the idea that Love waves exhibit stronger observed amplitude de-594 cays compared to Rayleigh waves, and that perhaps it is necessary to split our current definition of surface wave magnitude into two 596 definitive definitions. Time will tell whether these results hold, as 597 rotation measurements become more readily available and accessi-598 ble, however it is exciting to see how these might change as a new 599 slew of instruments and observations become available to the field 600 of seismology. 601

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