# Comparisons of surface wave amplitude decays as measured by rotation and translation sensors

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#### **SUMMARY**

Current broad-band surface wave magnitude equations relate magnitude with station-receiver distance and the vertical component of peak ground velocity, such that only contributions from the vertical component of Rayleigh waves are present. With the advent of rotational ground motion data from instruments such as ring laser gyroscopes and fiber-optic gyroscopes, it is possible to determine peak amplitudes of rotations about the vertical axis, which is theoretically only sensitive to the transverse nature of Love waves, unaffected by the horizontal component of Rayleigh waves. We use this concept to study the amplitude decay of rotations versus translations, and determine the necessity of a separate surface wave magnitude equation for Love waves. Utilizing a large database of rotation ground motion events, collected in Wettzell, Germany, we empirically define decay constants for measured observables: rotation rate, rotation, vertical velocity and transverse velocity. Results indicate that measured rotation amplitudes decay faster over distance compared to velocity amplitudes, both on vertical and transverse components. Observations are corroborated with synthetic seismograms produced on a full scale 3D global model with crustal and Moho topography models. Synthetics were created with the spectral-element method Salvus, and suggest that ...

Key words: magnitude, rotational ground motions, seismic instrumentation, amplitude decay

## 1 INTRODUCTION

For over a decade, the application of ring laser gyroscope technology to the field of seismology has allowed for near-continuous, direct, measurements of rotational ground motions. An ever growing number of observations from seismic events of varying size, distance and source mechanism, has been collected in an expansive catalog of waveform recordings for both direct rotation, and collocated translation measurements. Previous work on this unique waveform dataset includes phase comparisons of translations and rotations [Igel 2005] and estimations of local horizontal phase velocities. [include more previous work?] Much of this preceding work however, focuses on single events, or collections of nonearthquake sources.

In this paper, we aim to characterize and understand the differences in amplitude decay behavior of rotational and translational ground motion for a large number of seismic events. To do this, we make use of a sizable catalog of event data, as measured by an observatory based ring laser gyroscope, and collocated broadband translation sensor. By processing rotation and translation observations in a near identical manner, we can directly compare results over a large set of event magnitudes, epicentral distances and back azimuths. We additionally seek to use this information to better understand decay characteristics of Love and Rayleigh waves.

This paper builds on work previously addressed by [Igel 2007], where the question was posed: whether observed peak rotation amplitudes matched with expected values given by the surface wave magnitude equation. At the time, a lack of events lead to a limited study size, however a much larger number of events is now currently available. In this work, we attempt to readdress this question, while also approaching the problem from the unique perspective of deriving magnitude scales for peak amplitudes over distance, in an attempt to similarly quantify the decay characteristics of rotations and translations.

Due to the uniqueness of our instrumental setup, we are restricted to observations at a single point of measurement. In order to provide comparisons to our observations, global 3D synthetic simulations were run with the wave propagation code Specfem3D Globe. Real seismic event locations, source parameters, as well as real station locations are used, in order to provide the most comparable synthetic setup to observations. We then fit amplitude decay of synthetic rotations and translations with a power law decay, that acn be compared to the decay found in analysis of observations.

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#### 1.1 Rotational Ground Motions

In this section we discuss the measurement and analysis of rotational ground motions in relation to the field of seismology. Rotational ground motions induced by seismic events can currently be determined through array analysis of translation sensors, and through direct measurement. In the former, spatial gradients are taken for measurements in an adequately spaced array of translation sensors, in order to derive components of the strain tensor [Spudich?]. In the latter, unique instrument designs allow for direct gradient measurements [Schreiber? Others?].

In this study, data was recorded by the Großring (G-ring) [Schreiber 2005, 2006], a 4x4m helium-neon ring laser gyroscope, located in Wettzell, Germany (49.144°N, 12.87°E). The G-ring operates on the principle of Sagnac interferometry [Stedman, 1997], which relates interference of counter propagating light beams to absolute rotation rate, through the following equation,

$$\delta f = \frac{4A}{\lambda P} \mathbf{n} \cdot \mathbf{\Omega},\tag{1}$$

where the constants are given by instrument area A, perimeter P and operating light wavelength  $\lambda$ . Equation 1 relates an observable beat frequency  $\delta f$  [Hz] to rotation rate [rad/s]  $\Omega$ .

It is important to note that given stable instrument geometry and lasing, changes to the beat frequency  $\delta f$ , can only be introduced by changes to the inner product of the plane normal  ${\bf n}$  with the rotation rate direction  $\hat{\Omega}$  (e.g. through instrumental tilt), and through externally induced rotations (e.g. the passing of seismic waves). It has been shown that changes to the inner product as produced by tilt are one to two orders of magnitude smaller than rotations produced by passing seismic waves [Igel? Schreiber?]. This gives instruments that operate on Sagnac interferometry the very unique benefit that they are theoretically insensitive to translations, and only sensitive to externally induced rotations.

#### 1.1.1 Phase velocity relation

As shown in [Igel 2005], for a simple plane wave assumption, the amplitudes of vertical rotation rate  $\Omega_z$  and transverse acceleration  $\ddot{u}_t$  can be related through the equation

$$\frac{\ddot{u}_t}{\Omega_z} = -2c,\tag{2}$$

where c represents an apparent horizontal phase velocity. This relationship shows that given a sufficient event-receiver distance allowing a plane wave assumption, measured rotations are sensitive to the transverse component of translation, represented by surface horizontal waves (i.e. SH or Love waves). It also states that waveforms of transverse acceleration and vertical rotation rate are theoretically in phase, with oppositely polarized amplitudes, for passing horizontal waves.

## 1.1.2 Peak correlation coefficient

Correlations are a useful measure of similarity between two signals. It has been shown previously that for collocated measurements of vertical rotation rate and transverse acceleration, high values (> 0.9) of zero lag correlations can be obtained in time windows centered around surface wave arrivals. Zero lag correlation coefficients are routinely computed for new events measured by the G ring [Salvermoser 2017], and are used in this study as a filtering

tool to highlight events with low signal to noise ratios, or dissimilar waveforms which may arise due to non-physical effects (e.g. instrumental effects). Here, the largest correlation coefficient obtained for a seismogram is labelled the peak correlation coefficient, and is used as a representation of data quality for an event.

#### 1.2 Magnitude scales

Here we discuss the common magnitude scale equation, and propose using a modified version as a method for comparing amplitude decay of various observables. Amplitude based magnitude scales provide empirically derived relationships between maximum trace amplitudes and source-receiver distances. Magnitude scales offer useful and quick estimates of relative sizes of earthquakes in a standard and easily-understandable manner. The International Association of Planets Seismology and Earths Interior (IASPEI) Working Group on Magnitudes has proposed a modified version of the original surface wave magnitude equation proposed by Karnik et al. and Vanek et al., which is compatible for use with modern day broadband seismic instruments [Borrmann and Bergman 2000].

In this work, we adhere strictly to the standard procedures provided by IASPEI as an outline for defining our own empirical magnitude scales. We use these derived scales as a tool for quantifying amplitude decay for different measured observables, in a standard fashion

## 1.2.1 Standard Procedures

The Working Group on Magnitudes' standard procedures gives the revised surface wave magnitude equation for broad-band instruments as,

$$M_S^{BB} = log_{10}(V/2\pi) + B \cdot log_{10}(\Delta) + C,$$
 (3)

where the constants B=1.66 and C=0.3 control amplitude decay and order of magnitude, respectively. The parameter V should be the maximum trace amplitude (nm s $^{-1}$ ) in the surface wave train, for a seismogram proportional to velocity, measured on the vertical component.

Further criteria given by IASPEI posit that the period of the surface wave should lie within 3 s  $\leq T \leq 60$  s, while epicentral distances should be between  $2^{\circ} \leq \Delta \leq 160^{\circ}$ . It is further recommended that only shallow focus earthquakes should be considered, as medium to deep events are less capable of generating strong surface waves. Maximum trace amplitudes are described as one half the largest peak to adjacent trough deflection, and associated period are given as two times the temporal difference between peak and adjacent trough. All events and processing steps in this paper adhere to these guidelines.

## 1.2.2 Instrumental proxies for Love and Rayleigh waves

A standard procedure for determining surface wave magnitude scales is taking amplitudes measured on the vertical component of translation. The reason given is that vertical translation should only be sensitive to the vertical motions of Rayleigh waves, whereas vector sums of horizontal components can be influenced by both Love and Rayleigh waves. In the same vein, velocity measured on the transverse component should only show sensitivity to Love waves. This is, however not common in practice, most likely due to the necessity of rotating horizontal components to the correct backazimuth. The G-ring, which is 1) insensitive to translations and 2) proportional in phase and amplitude to transverse acceleration, should

also only be sensitive to Love waves in the surface wave train, irrespective of backazimuth.

In this study we use instruments as physical wave-filters, in order to separate phases in the surface wave train. This allows us to study the influences of Love waves and Rayleigh waves individually. By comparing the vertical and transverse components of translations, to the vertical component of rotation, we can understand, by proxy, the wave types they are sensitive to.

## 1.2.3 Application of rotations to magnitude scales

The surface wave magnitude equation is defined for peak vertical velocity amplitudes in the surface wave train. In order to give a fair comparison using derived magnitude scales, a complementary rotation parameter is necessary. In Section 1.1.1, an equation is given that relates rotation rates  $\Omega$  with accelerations  $\dot{u}$ . It would make the most sense, then, to compare velocities  $\dot{u}$  with rotations  $\omega$  (by integrating both sides). However, without previous work to draw precedence from, and for completeness, we present observations of both rotations and rotation rates in this study.

## 2 EVENT CHOICE

The G-ring has been continuously recording at its current resolution since May, 2009. The time range for events used in this study spans from June, 2009 until September, 2016. An initial catalog was fetched from the Harvard Global Centroid Moment Tensor (GCMT) [Ekström et al. 2012 ?], with events initially filtered by acceptable magnitude, source depth and epicentral distance from Wettzell, Germany. At this point we imposed the restriction that the derived 'magnitude' as given by our magnitude equations, should fall as close to the given surface wave magnitude as possible. This ensures that our derived scales do not stray too far from established scales. This meant only events with centroid moment magnitude values of  $6 \le M_{\rm wc} < 8$  (as published in the GCMT catalog), were considered; surface wave magnitude and moment magnitude are approximately equal in this range [Shearer 2009]. Zero-lag cross correlations were taken in order to calculate peak correlation coefficients between rotation and acceleration traces (Section 3.1). Events were not considered if their peak correlation coefficient was below PCC < 0.7.

These event choice criteria narrowed the catalog down to less than 500 events in the given time period. Each event was appropriately filtered and processed (Section 3.1), and waveforms were individually inspected. Waveforms that exhibited anomalous behavior (i.e. unexpected high amplitude peaks outside the surface wave train, high signal-to-noise ratio etc.) were rejected. Examples of accepted and rejected waveforms are given in Figure (put a figure here). A final event catalog of 243 events was reached.

## 3 METHODS

## 3.1 Data Processing

Events were processed in a similar fashion as the steps outlined in [Salvermoser 2017]. Raw continuous translation data in North, East and up components, as well as vertical rotation data, was fetched based on event origin time. Instrument response correction produced translation seismograms proportional to units of velocity (nm s<sup>-1</sup>). Epicentral distances and theoretical backazimuth values were calculated from station-receiver latitude longitude pairs,

and events were separated into categories of close ( $\Delta < 3^{\circ}$ ), local  $(\Delta < 100^{\circ})$  and far  $(\Delta > 100^{\circ})$ . Horizontal components were rotated into the transverse, radial coordinate system by the appropriate theoretical backazimuth. Measurements from ring laser gyroscope instruments do not require frequency dependent instrument correction [Sagnac?], therefore only a simple scale factor was necessary to retrieve seismograms proportional to rotation rate (nrad  $\mathrm{s}^{-1}$ ). Rotation rate traces were integrated to provide measurements of rotation (nrad), and transverse velocity was integrated to retrieve transverse acceleration, which was subsequently used to calculate correlations with vertical rotation rates. but? A bandpass filter was applied to all traces for periods between 3 s < T < 60 s, in accordance to the IASPEI standard procedures. Peak amplitudes were chosen by finding minimum and maximum trace values and the largest associated peak or trough, respectively. The larger of the two was taken, alongside the associated arrival time and dominant period. Theoretical considerations used to restrict search to the surface wave train proved inconsistent over a large number of events, so maximum amplitudes in the entire trace were considered. Through manual inspection, picked amplitudes that fell outside the surface wave train were rejected.

## 3.1.1 Zero-lag correlations

To calculate peak correlations, traces of transverse acceleration and vertical rotation rate were segmented into small time windows based on the event-station distance. In each time window, a zero-lag correlation was performed, and a single value of correlation produced. From the entire trace, the max value was taken to represent the peak correlation coefficient. For most waveforms, the peak correlation coefficient lie in the surface wave train. As mentioned previously, these peak correlation values are used extensively as a ranking system for events, providing a quickly attainable measure of waveform quality.

## 3.2 Curve fitting

To quantify amplitude decay, magnitude scale coefficients were fit to the data using a simple linear regression. Equation 3 represents a relationship between magnitude and amplitude for a single event. A collection of n events can be represented in the form,

$$\begin{pmatrix} log_{10}(\Delta_1) & 1\\ log_{10}(\Delta_2) & 1\\ \vdots & \vdots\\ log_{10}(\Delta_n) & 1 \end{pmatrix} \begin{pmatrix} B\\ C \end{pmatrix} = \begin{pmatrix} M_{\text{wc}_1} - log_{10}(V_1/2\pi)_{\text{max}}\\ M_{\text{wc}_2} - log_{10}(V_2/2\pi)_{\text{max}}\\ \vdots\\ M_{\text{wc}_n} - log_{10}(V_n/2\pi)_{\text{max}} \end{pmatrix},$$
(4)

which can be further condensed to the form,  $\mathbf{Gm} = \mathbf{d}$ . The unknowns B and C are represented in the vector  $\mathbf{m}$ , and can be solved for through the normal equation  $\mathbf{m} = (\mathbf{G}^T\mathbf{G})^{-1}\mathbf{G}^T\mathbf{d}$ . By determining values of B and C, we create an empirical magnitude scale that best describes the amplitude decay behavior of our events. In Equation 4, we impose that our derived magnitude value should be as close to an events given moment magnitude as possible, by setting  $M_S^{BB}$  equal to the value of  $M_{\mathrm{wc}}$  retrieved from our event catalog.

95% confidence intervals were constructed for each parameter of the vector  $\mathbf{m}$ . These were calculated with the variance of estimates of the jth parameter of  $\mathbf{m}$  by the equation  $\hat{m}_j \pm c \sqrt{v \hat{a} r(\hat{m}_j)}$ , where the value of c is given as 1.96.

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#### 4 SYNTHETIC SEISMOGRAMS

Due to the unique instrumental setup of the G-ring, there are currently no other rotational instruments with as much temporal coverage to draw comparisons from. It should be mentioned that there are other available rotation instruments which allow for single event case study analyses [Donner 2017 PFO?], however the large catalogs like that available from the G-ring are currently unavailable. One possibility for gathering more observations would be through array derived rotations as a substitute for direct rotation measurements [Spudich ?]; this option was noted during analysis, however it proved difficult finding sufficient long-term arrays with the optimal station spacing. In lieu of observations, we instead turn to waveform modeling to generate synthetic seismograms, with which we can recreate our experimental setup and provide a comparable set of observations.

The seismic wave propagation code Specfem3D Globe was employed [cite specfem]. A realistic global model featuring 3D crust and mantle models was used, and the simulation featured effects that might have potential influence on surface waves at the periods of interest. These effects include: ocean loading, Earth's ellipticity, topography, self gravitation, Earth's rotation and 1-D attenuation. Event locations and moment tensors were taken from 10 real seismic events present in the observation catalogs. Events were chosen based on observation data quality, as well as event location and depth, so as to provide a varied distribution of source-receiver pairings. Table 1 provides detailed information on the chosen events.

Events were initiated as point sources. The simulation corner frequency was set to 10 seconds, and simulations were run for one hour simulation time. As computational cost is independent of number of stations, more than one hundred stations were included; Global Seismic Network (GSN) locations were used, as well as location of the G-ring, and the German observatory station Fürstenfeldbruck. The number of simulated stations was X, and the number of station-receiver pairs X (with some station-receiver pairs falling outside the distance bounds specified in Section 1.2.1).

The direct outputs of Specfem3D were adjusted to produce displacement in the transverse, radial and vertical components, by rotation with respect to the theoretical backazimuth. Direct rotation in the same coordinate system was also outputted. A work flow identical to that used for observations was employed to calculate peak trace amplitudes, and a magnitude equation was fit to the data for comparison.

## 5 RESULTS

## 5.1 Derived magnitude scales

For rotations and translations, decay characteristics were derived by solving for constants B and C in the magnitude equation. The determined values for each scale are presented in a Table 2. Because the constant C is dependent on the order of magnitude of the units, it is difficult to compare it between different observation types. For this reasons we make the decision to focus comparisons and interpretations on the relative values of B. The parameter B represents the slope of amplitude versus distance, and allows us to make comparisons of rotations and translations. As a check on the processing steps, and on site-dependent data quality, the same analysis was performed on translation observations taken at the geophysical observatory in Fürstenfeldbruck, Germany (48.163°N, 11.275°E), located roughly 200 km south-west of Wettzell. Though a smaller

subset of events was used due to data availability, the results confirmed those given by Wettzell by returning derived constants B and C within 1%

One can see in Table 2, that the decay constant B varies quite a bit, from both the standard IASPEI scale, as well as from one another. It is to be expected that rotation rate would show a larger value for B as compared to rotation, as we are comparing a unit and its time derivative. It was surprising to see, however, the drastic differences between values of B for scales derived from translation observations. As the surface wave magnitude equation is defined for vertical component observations, it was expected that vertical velocity would present a similar decay to the broadband surface wave magnitude equation, however it presents itself as the largest discrepancy.

Transverse velocity, which should sample the same waves as rotations (see ??), shows a larger value for B as compared to vertical velocity, however it also exhibits lower than expected decay compared to the IASPEI scale.

#### 5.2 Observed and synthetic wave forms

For each of the 10 events, wave forms for station WET were compared for all components of translation and rotation. In most cases, onset time was within reasonable distance, however phases and amplitudes were not in agreement. Considerations should be made towards using point sources with no source time functions, and the rather broad range of frequencies included in the observations. Local site and source effects also may not have been taken into captured by the synthetic model used. Unfortunately due to limited computational resources, the synthetic traces only extend one hour, and do not capture the full extent of the waveform represented in the observations. Comparison of the wave forms, however, suggest that all of the surface wave energy has been captured in the one hour of simulation time.

## 5.3 Synthetic magnitude scales

The derived magnitude scales for synthetic results differ drastically from the observed results. The synthetic results do not reflect the same discrepancies that are present in the values given in Table 2.

Looking at Figure [SYN MAG SCALE FIG], the distribution of points on the magnitude scales is much more uniform. This can be attributed to the increased number of recordings for a single event due to the large number of synthetic stations. With so many station receiver pairs over a range of epicentral distances, it is possible for the receiver to track the earthquake. This was unfortunately not possible in the observations, and gives rise to some discrepancy in the appearance of the different magnitude scales.

The synthetic magnitude scales all exhibit very similar values for the decay constant B. The large variation in decay as seen in the observations is not at all captured here. The largest discrepancy between two scales is X!. Even between rotation and rotation rate, as well as the values of velocity.

#### 5.4 Expected rotation amplitudes

One useful aspect of magnitude scales is to provide an expected amplitude value for a given magnitude event at certain distance. This is quite helpful in areas such as seismic hazard, where one can estimate the order of magnitude of ground motion at a location some distance away from an event, given a certain event size,

Date	Time (UTC)	Lat(°)	Lon(°)	Depth(km)	$\mathbf{M}_{\mathbf{wc}}$	Flinn-Engdahl Region	Peak Corr. Coeff.
2010-07-18	13:34:59	-5.93	150.59	35.0	7.32	New Britain Region, P.N.G.	0.98
2011-09-16	19:26:41	40.27	142.78	35.0	6.67	Off East Coast Of Honshu, Japan	0.99
2013-01-05	08:58:19	55.39	-134.65	10.0	7.53	Southeastern Alaska	0.95
2013-04-16	10:44:20	28.03	62.0	80.0	7.74	Southern Iran	0.98
2013-04-19	19:58:40	49.97	157.65	15.0	6.06	East Of Kuril Islands	0.99
2015-02-13	18:59:12	52.65	-31.9	16.7	7.07	Reykjanes Ridge	0.99
2015-04-25	06:11:26	28.15	84.71	15.0	7.88	Nepal	0.99
2015-09-13	08:14:12	25.14	-109.43	10.0	6.6	Gulf Of California	0.98
2015-09-16	23:18:41	-31.56	-71.43	28.4	7.1	Near Coast Of Central Chile	0.99
2016-01-25	04:22:02	35.65	-3.68	12.0	6.38	Strait Of Gibraltar	0.99

**Table 1.** List of events used as synthetic sources in Specfem3D. Peak correlations are used as a measure of waveform quality, and only events with the highest values were used, in order to provide the best comparisons of synthetics with observations. Events were also chosen based on a diverse coverage of magnitudes and epicentral distances from the ring laser stationed in Wettzell, Germany. Event information taken from the GCMT catalog.

though this is also dependent on site effects, travel paths, and amplitude modulation due to attenuation, focusing etc. This has largely been replaced by the concept of ground motion prediction equations, however in the emerging field of rotational seismology, it provides a useful insight.

One concern in rotational seismology arises from whether or not newly developed field deployable rotation sensors will have the sensitivity necessary to capture the rotational motion amplitudes excited by regional or distant seismic events. With the rotational magnitude scale we derived here, we are able to create a list of expected rotational amplitudes for tele-seismic events. At the time of writing, the field deployable rotation sensor BlueSeis from the company iXBlue, has a noise floor of about (???) [Cite ???], which measures gradient information (rotation rate). Referring to the values given in Table 2, the maximum distance the sensor can be to detect a  $M_w$  event would be  $X^\circ$ . Other considerations must be taken into account before these values can be used for field deployment decisions, however it provides a jumping off point for a new area of field research.

#### 6 DISCUSSIONS AND CONCLUSIONS

Long term continuous recordings of collocated rotation and translation has now provided a superb catalog of seismic events usable in comparisons of direct translation measurements and direct measurements of spatial gradients. Phase information has proved a very fruitful venture, but the measure of amplitudes has long been sidelined. If the amplitude information can be trusted, it can prove useful in better understanding rotational motions in the context of seismology.

The results of this work show the consistency of rotation measurements for a large observatory based ring laser gyroscope, and allow very accurate and stable comparisons of rotations and translations. Since events were manually chosen to exhibit the best characteristics for their waveforms, we can be sure that the derived decay characteristics that are shown here also are stable, albeit for teleseismic waves. The results at face value show that observed rotations for the event catalog used decay faster than observed translations for the same events, and that rotation rate decays faster than the rotation, though this is to be excepted as we are simply looking at time derivative information. What is most interesting is how the rotation and rotation rate decays match much closer to the globally averaged surface wave magnitude as compared to the translation measurements which it is based off. Understandably a global aver-

age should be taken to give a more reasonable value for the decay. It should be pointed out, however, that even without global averaging, it is exciting to see the characteristics of this new observable, and by taking comparisons of direct measurements, we are gaining more understanding of the behaviors of this observable.

In this setup, multiple stations were used to record synthetic waveforms from single events, and as a result it is possible to see the amplitude decay of a single event over distance.

Since we were not capable of this in the observable results, there is a stark difference in how the magnitude scales look and are derived. One major contrast between synthetics and observations is the differences in amplitudes of both rotational and translational motions. Given the magnitude equations in Tables 2 and 3, for an example event magnitude 7 at a distance of  $100^{\circ}$ , we retrieve an expected rotation rate value of X for observations, but Y for synthetics. In the same vein, velocities show X and Y for observations and synthetics respectively.

Although amplitude differences were to be expected, these contrasts are quite strong. Possible explanations include the frequencies of interest or perhaps structural or site effects that are not modeled or captured by the synthetic mesh.

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Scale	Label	В	C	Wave
IASPEI	$M_S^{BB}$	1.66	0.3	Rayleigh
Rotation	$M_{RT}^{RLAS}$	$1.557 \pm 0.295$	$4.186 \pm 0.569$	Love
Rotation Rate	$M_{RR}^{RLAS}$	$1.823 \pm 0.303$	$4.113 \pm 0.586$	Love
Transverse Velocity	$M_T^{WET}$	$1.45 \pm 0.27$	$0.527 \pm 0.521$	Love
Vertical Velocity	$M_Z^{WET}$	$1.084 \pm 0.264$	$1.093 \pm 0.511$	Rayleigh

**Table 2.** Magnitude scales and derived constants with 95% confidence intervals for observations at station RLAS/WET, for equations of the form  $M = log_{10}(V/2\pi) + B \cdot log_{10}(\Delta) + C$ . The final column gives consideration to the wave type that each instrument component should provide a proxy for

Scale	Label	В	C	Wave
Synthetic Rotation	$M_{RT}^{SYN}$	$1.557 \pm 0.295$	$4.186 \pm 0.569$	Love
Synthetic Rotation Rate	$M_{RR}^{SYN}$	$1.823 \pm 0.303$	$4.113 \pm 0.586$	Love
Synthetic Transverse Velocity	$M_T^{SYN}$	$1.45 \pm 0.27$	$0.527 \pm 0.521$	Love
Synthetic Vertical Velocity	$M_Z^{SYN}$	$1.084 \pm 0.264$	$1.093 \pm 0.511$	Rayleigh

**Table 3.** Synthetic magnitude scales and derived constants with 95% confidence intervals, for equations of the form  $M = log_{10}(V/2\pi) + B \cdot log_{10}(\Delta) + C$ . The final column gives consideration to the wave type that each instrument component should provide a proxy for.