

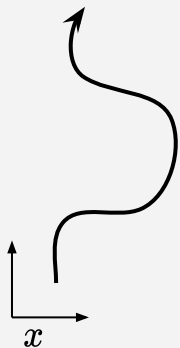
Computational motor control and learning: *a game theoretic approach*

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Motivation: Multi-agent Dynamics

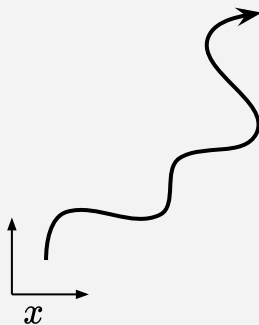
Dynamical system $\dot{x} = f(x, u_1, u_2)$

Player 1's optimal trajectory



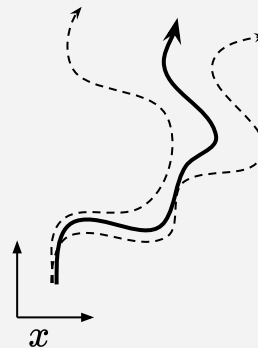
+

Player 2's optimal trajectory



?

Coupled dynamics?



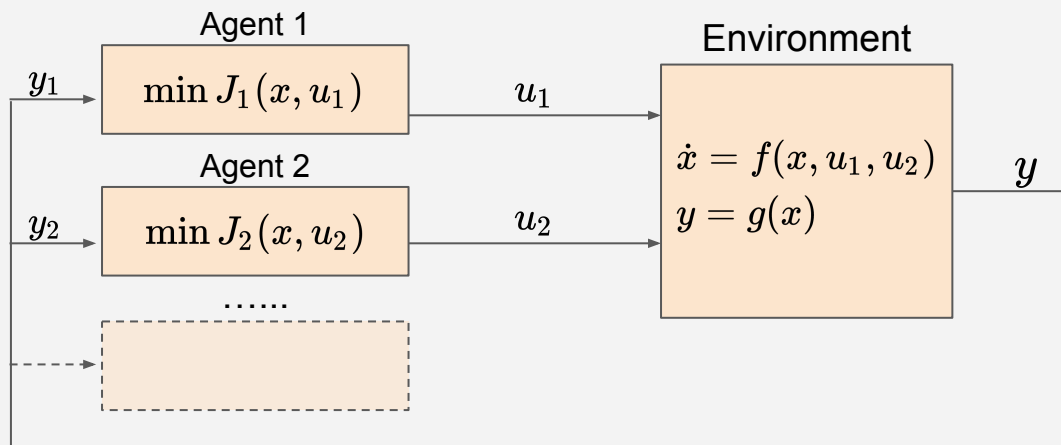
Mathematical Model

State: $x \in \mathcal{X} = \mathbb{R}^n$

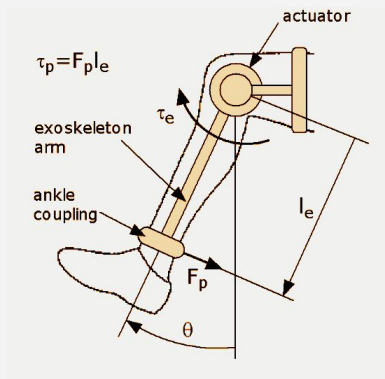
Actions: $u_i \in \mathcal{U}_i = \mathbb{R}^{m_i}$

Observations: $y_i \in \mathbb{R}^d$

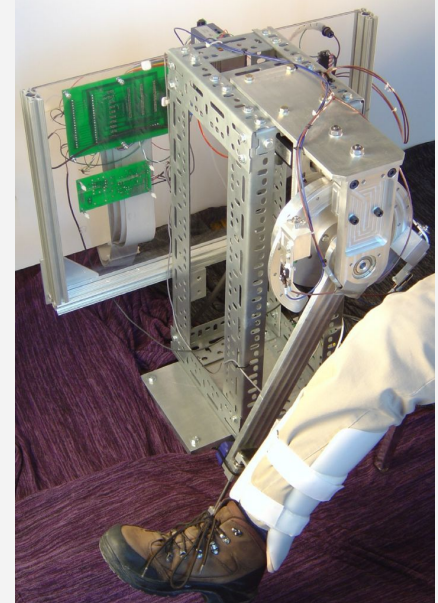
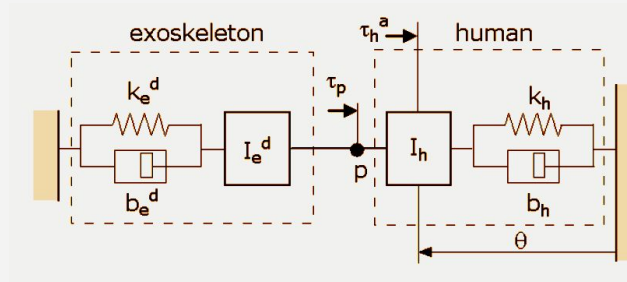
Costs: $J_i : \mathcal{X} \times \mathcal{U}_i \rightarrow \mathbb{R}$



Mechanical Human/Agent Example



$$\dot{x} = f(x, u_1, u_2)$$



Reed, Peshkin (2008)

Prior work

Adaptive Control (*Slotine, 1980s ...*)

Learns unknown system parameters

Inverse optimal control (*Levine, Abbeel, Ng, etc, 2000s ...*)

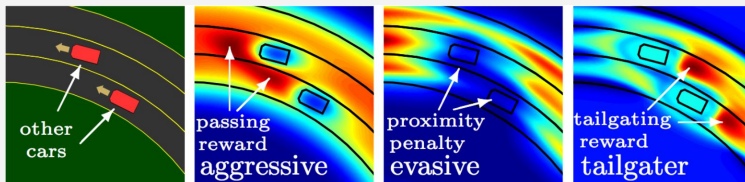
Learns control law from trajectory

Dynamic noncooperative games (*Başar, Olsner, 1999 ...*)

Theoretical framework for analyzing dynamic games

Motor games (*Wolpert, 2009 ...*)

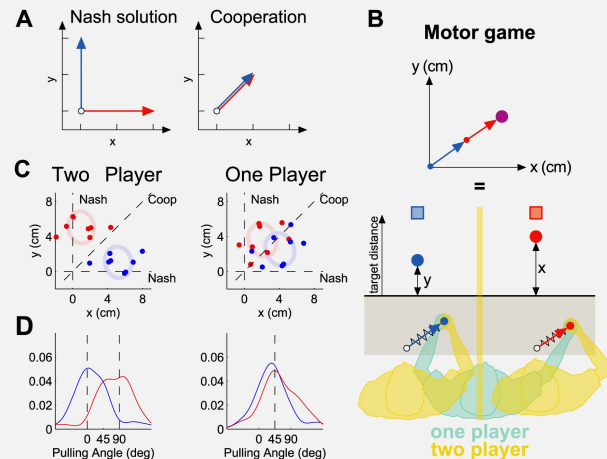
Cooperation vs nash equilibrium in motor games



Levine, Vladlen (2012)



Lavretsky et. al (2003)



Braun, Pedro, Wolpert (2009)

Our contribution

- Dynamical system

$$\dot{x} = f(x, u_1, u_2, \dots)$$

- Non-cooperative agents

$$\min J_1, \min J_2, \dots$$

- Online adaptive controllers

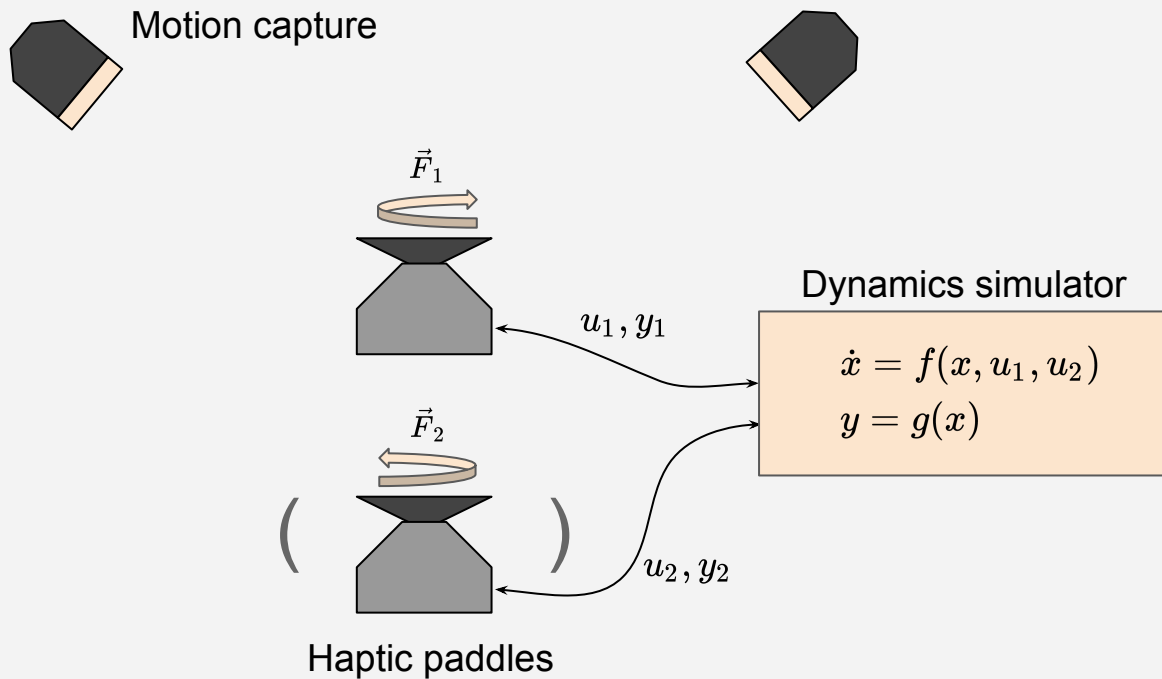
Learns unknown parameters/control law of other agents

- Game theoretic insights

Nash equilibria, stackelberg equilibria, information patterns...

- Experimental validation of theory

Experimental setup



Questions?

References

Basar, Tamer, and Geert Jan Olsder. *Dynamic noncooperative game theory*. Vol. 23. Siam, 1999.

Braun, Daniel A., Pedro A. Ortega, and Daniel M. Wolpert. "Nash equilibria in multi-agent motor interactions." *PLoS computational biology* 5, no. 8 (2009): e1000468.

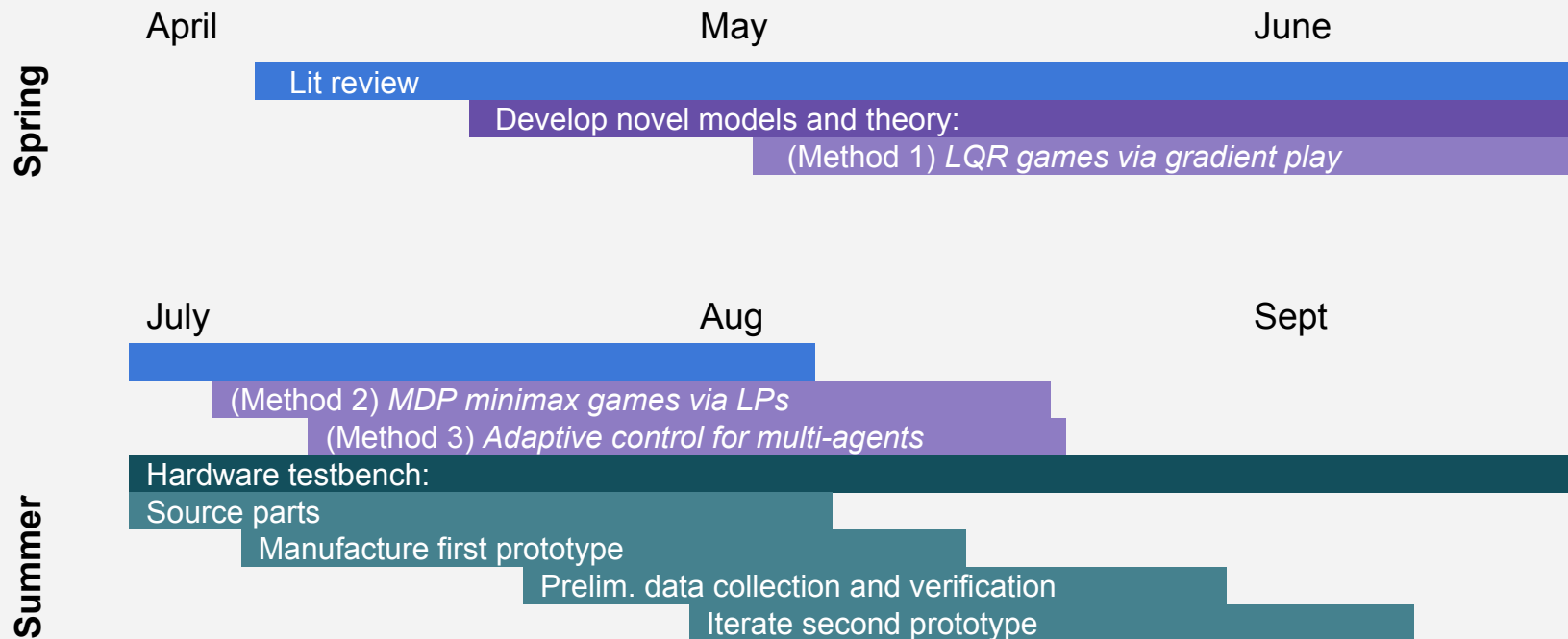
Lavretsky, E., Hovakimyan, N., Calise, A., Stepanyan, V. "Adaptive Vortex Seeking Formation Flight Neurocontrol", *AIAA-2002-4757, AIAA GN&C Conference*, St. Antonio, TX, 2003.

Levine, Sergey, and Vladlen Koltun. "Continuous inverse optimal control with locally optimal examples." *arXiv preprint arXiv:1206.4617* (2012).

Reed, Kyle B., and Michael A. Peshkin. "Physical collaboration of human-human and human-robot teams." *IEEE Transactions on Haptics* 1, no. 2 (2008): 108-120.

Slotine, Jean-Jacques E., and Weiping Li. *Applied nonlinear control*. Vol. 199, no. 1. Englewood Cliffs, NJ: Prentice hall, 1991.

Project Timeline



Summer deliverables








Completed








In progress

Theory

- **LQR games via gradient play**
 - Convergence guarantees 
 - Prelim simulations 
- **MDP minimax games**
 - Problem formulation with constraints 
 - Prelim. simulations 
- **Adaptive control with multi-agent SI**
 - *Novel* multi-agent approach 
 - Inverse optimal control
 - Shift nash of cost minimizing agents
 - Prelim. simulations

Experimental

- **Modular testbench:** series-elastic haptic paddle
 - Design first prototype 
 - Source parts 
 - Print and assemble 
 - Simple PID controller 
- **Validation experiments:**
 - Adaptive controller detects sys. params. 
 - Reproduce Wolpert motor games
- (Stretch goal) **Novel experiments**
 - Characterize nash of two-player dynamic games
 - Inverse reinforcement learning via adaptive control
- (Stretch goal) **Extend modular hardware setup**
 - Hopper games
 - Balance games