
IMPROVING OUTCOME PREDICTIONS FOR PATIENTS RECEIVING MECHANICAL CIRCULATORY SUPPORT BY OPTIMIZING IMPUTATION OF MISSING VALUES

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ABSTRACT

Background Risk predictions play an important role in clinical decision making. When developing risk prediction models, practitioners often impute missing values to the mean. The purpose of this article is to evaluate the impact of applying different strategies to impute missing values on the prognostic accuracy of prediction models fitted to the imputed data. A secondary objective was to compare the accuracy of different imputation methods. To complete these objectives, we used data from the Interagency Registry for Mechanically Assisted Circulatory Support (INTERMACS).

Methods and Results We applied thirteen different strategies to impute missing values in combination with three different strategies to fit a risk prediction model for mortality and transplant after receiving mechanical circulatory support. Model performance was measured by 12-month discrimination, calibration and net reclassification index. Results indicated that multiple imputation consistently provided prediction models with greater prognostic accuracy than other missing data strategies, particularly imputation to the mean.

Conclusion Selecting an optimal strategy to handle missing values impacts the prognostic accuracy of downstream models. In the current analysis, multiple imputation emerged as an optimal strategy to handle missing values in the INTERMACS data. The current study shows that evaluation and selection of an optimal strategy to impute missing data has the potential to improve prognostic accuracy of risk predictions for other longitudinal registries.

Keywords Missing Data, · INTERMACS, · imputation, · heart failure, · mortality, · risk prediction

1 Introduction

1 Heart disease is a leading cause of death in the United States. Heart failure, a primary component of heart disease, affects
2 over 6 million Americans, and for ~10% of these patients medical management is no longer effective [1, 2]. Mechanical
3 circulatory support (MCS) is a surgical intervention in which a mechanical device is implanted in parallel to the heart to
4 improve circulation [3]. Typically, MCS is used while a patient waits for a heart transplant (bridge-to-transplant) or in
5 some cases as an alternative to transplant (destination therapy) [4]. Over 250,000 patients could benefit from MCS
6 [5]. However, less than 4,000 new patients receive a long-term MCS device each year, with widely heterogeneous

*Source code available at <https://github.com/bcjaeger/INTERMACS-missing-data>

outcomes [6]. The 2-year survival on MCS ranges from 61% for destination therapy to 78% for bridge-to-transplant [3]. Therefore, there is great need for reliable predictions of patient-specific risk to experience adverse events after receiving MCS. This information can be used to improve patient selection for MCS, inform the design of next generation pumps, and refine patient management strategies.

The Interagency Registry for Mechanically Assisted Circulatory Support (INTERMACS) was launched to improve MCS patient outcomes through the collection of patient characteristics, medical events, and long terms outcomes at a nation wide level. Currently, INTERMACS comprises over 20,000 patients who have received a MCS device. As the largest registry for data on patients receiving MCS devices, INTERMACS has been leveraged to develop numerous risk prediction models for mortality and other types of adverse events that may occur after receiving a device [7, 8, 9]. A critical step for developing risk prediction models is handling missing data, which is common in a “real world” database that is not designed for the rigor of data completeness found in a clinical trial. While some missing values are related to data entry error, others may relate to instability of a patient’s circulatory status at the time of implant. For instance, hemodynamic laboratory values are missing for patients in whom invasive catheterizations were not performed. Patients without invasive catheterizations may be too ill (unstable) to tolerate the procedure. Instead, such patients may, after determination of basic hemodynamics, proceed directly to device placement.

The primary aim of this article is to quantify how much the prognostic value of a risk prediction model developed from the INTERMACS registry depends on the strategy that was applied to impute missing data prior to developing the model. A secondary aim is to measure imputation accuracy of each strategy by introducing varying levels of artificial missing data and then imputing it. Because imputation to the mean has been a standard method for multiple annual summaries of the INTERMACS data, we measure the potential improvement in prognostic value of a risk prediction model when other strategies are applied to impute missing data *instead of imputation to the mean*. The over-arching aim is to clarify which imputation strategies are most likely to improve risk prediction (and by extension, quality of care) for patients who receive MCS devices. This investigation can directly inform future analyses of INTERMACS data and provide evidence quantifying the benefit of imputing missing data with sound methodology.

2 Methods

In this section, we describe the INTERMACS Registry in Section 2.1 and provide a broad overview of general objectives for imputation of missing data in the context of statistical inference and supervised statistical learning in Section 2.2. We then describe thirteen strategies to handle missing values (Section 2.3) and three strategies to develop risk prediction models after missing data have been imputed (Section 2.5). Next, we describe how risk prediction models and by extension the imputation strategy applied before training the model were evaluated in Section 2.6. We outline an internal validation procedure that was applied to compare combinations of imputation and modeling strategies using hierarchical Bayesian models in Section 2.7. Last, details on computation and software packages used for the current analysis are described in Section 2.9

2.1 INTERMACS Registry

The INTERMACS data is publicly available on biolincc at <https://biolincc.nhlbi.nih.gov/studies/intermacs/>. INTERMACS is a North American observational registry for patients receiving MCS devices that began as a partnership between the National Heart, Lung, and Blood Institute, US Food and Drug Administration, the Centers for Medicaid and Medicare Services, industry, and individual hospitals with the mission of improving MCS outcomes. In 2018, INTERMACS became an official Society of Thoracic Surgeons database.

The current analysis was conducted using publicly available data provided by the National Heart, Lung, and Blood Institute. We included a contemporary cohort of 14,738 patients who received continuous flow LVAD from 2012-2017. Patient follow-up begins after implantation of a durable, long term MCS device and continues while the device is in place. Registry endpoints include death on a device, heart transplantation, or cessation of support (for recovery and non-recovery reasons). INTERMACS collects pre-implant patient characteristics, medical status, laboratory values, and many other variables. Data is collected at regularly scheduled follow-up as well as during adverse events such as re-hospitalization. This is a secondary analysis of de-identified data obtained from the National Heart Lung and Blood Institute. Primary data collection is approved through University of Alabama Institutional Review Board and at individual sites.

2.2 Statistical Inference and Learning with Missing data

Statistical Inference Previous research has thoroughly investigated statistical inference in the context of missing data. In this setting, analysts often create multiple imputed datasets, replicate an analysis in each of them, and then pool their results to obtain valid test statistics for hypothesis testing [10]. Imputation strategies that create a single imputed dataset (*e.g.*, imputation to the mean) have been shown to increase type I errors (*i.e.*, rejecting a true null hypothesis) for inferential statistics by artificially reducing the variance of observed data and ignoring the uncertainty attributed to missing values [11]. To ensure valid inference, imputation models should leverage outcome variables to predict missing predictors [12]. When very few data are missing, analysts may apply listwise deletion, *i.e.*, removing any observation with at least one missing value. However, listwise deletion can easily lead to biased inference [13].

Statistical Learning In the presence of missing data, the goal of supervised statistical learning is to develop a prediction function for an outcome variable that accurately generalizes to testing data, which may or may not contain missing values [14]. Because testing data may contain missing values, listwise deletion is not a feasible strategy for statistical learning tasks. In contrast to statistical inference, strategies that create a single imputed dataset are often used for statistical learning [15]. Previous work has emphasized the importance of imputation strategies with greater accuracy, suggesting that more accurate imputation strategies lead to better performance of downstream models (*i.e.*, models fitted to the imputed data) [16]. Others have shown that imputation to the mean, model-based imputation, and multiple imputation can provide Bayes-optimal prediction models provided certain assumptions are true, but these assumptions are difficult to validate in applied settings [17].

Using outcomes during imputation The outcome variable should be used to impute predictor values for statistical inference, but using outcome variables for this purpose in supervised learning can have unintended consequences in model implementation. For instance, suppose we seek to predict an outcome Y for a patient in the clinical setting. If the patient is missing information for a predictor X and our model’s strategy to impute missing values of X leverages the observed value of Y , how should we impute X ? If we do not already know Y , then we cannot impute X and hence cannot generate a valid prediction. On the other hand, if we already know Y , then we do not need to predict it. Due to these practical considerations and because INTERMACS is often leveraged to create prediction models for clinical practice [18], we did not leverage outcome variables to impute missing values of predictors in the current analysis.

2.3 Missing Data Strategies

Single and multiple imputation Several of the imputation methods we considered allowed for creation of one or many imputed datasets. For downstream models fitted to multiple sets of imputed data, we applied the modeling technique to each imputed training set, separately, and then used a pooling technique to generate a single set of predictions based on multiple imputed testing data. Specifically, we created 10 imputed training and testing sets, then applied a modeling procedure to each imputed training set and computed model predictions on the corresponding imputed testing set, which led to 10 sets of predictions. To aggregate these predictions, we computed the median for each observation. Informal experiments where the mean was used instead of the median to aggregate predictions showed little or no difference in the model’s prediction accuracy.

Imputation to the mean Imputing data to the mean involves three steps. First, numeric and nominal variables are identified. Second, for each numeric variable, the mean is computed and used to impute missing values in the corresponding variable. Third, for each nominal variable, the mode is computed (because one cannot compute a mean for categorical variables) and used to impute missing values in the corresponding variable. The computed means and modes are then stored for future imputation of testing data. Because imputation to the mean is frequently used in practice, we use it as a reference for comparison of all other strategies to impute missing values,

Bayesian Regression Imputation with Bayesian regression draws imputed values from the posterior distribution of model parameters, accounting for uncertainty in both model error and estimation [10]. Multiple imputation with chained equations (MICE), a well known technique for generating multiply imputed data [19, 11, 20]. In each iteration of MICE, each specified variable in the dataset is imputed using the other variables in the dataset. These iterations are run until convergence criteria have been met.

Predictive Mean Matching (PMM) PMM computes predicted values from a pre-specified model that treats one incomplete column in the data, X , as a dependent variable. For each missing value in X , PMM identifies a set of candidate donors based on distance in predicted values of X [21]. One donor is randomly drawn from the candidates, and the observed value of the donor is taken to replace the missing value. When missing values were imputed using

PMM, we applied MICE to form multiple imputed datasets. For consistency with other approaches, we also generated a single imputed dataset using PMM by randomly selecting one of the multiple datasets imputed.

K-Nearest-Neighbors (KNN) KNN imputation identifies k ‘similar’ observations (*i.e.*, neighbors) for each observation with a missing value in a given variable [22]. A donor value for the current missing value is generated by sampling or aggregating the values from the k nearest neighbors. In the current analysis, we identified 10 nearest neighbors using Gower’s distance [23]. When imputing a single dataset using KNN, we aggregated values from 10 nearest neighbors using the median for numeric variables and the mode for categorical variables. When imputing multiple datasets using KNN, we aggregated values from 2, 6, 11, 16, and 20 neighbors, separately, to create 5 imputed datasets.

Hot Deck Similar to KNN, hot deck imputation finds k similar observations for each observation with a missing value in a given variable [24]. However, hot deck imputation uses a less computationally intensive approach, either identifying neighbors at random or using a subset of variables to find similar observations. When imputing a single dataset using hot deck imputation, we used a selection of 5 variables simultaneously to identify nearest neighbors. When imputing multiple datasets using hot deck imputation, we used a separate numeric variable for each dataset.

Random forests Random forests grow an ensemble of de-correlated decision trees, where each tree is grown using a bootstrapped replicate of the original training data [25, 26, 27, 28, 29, 30]. A particularly helpful feature of random forests is their ability to estimate testing error by aggregating each decision tree’s prediction error on data outside of their bootstrapped sample (*i.e.*, out-of-bag error). In the current analysis, we conduct MICE using one random forest to impute each variable, separately. For each imputed dataset, we allowed random forests to be re-fitted until out-of-bag error stabilized or a maximum number of iterations was completed. When imputing a single dataset, we used 250 trees per forest and a maximum of 10 iterations. When imputing multiple datasets, we used 50 trees per forest and applied PMM using the random forest’s predicted values to impute missing data by sampling one value from a pool of 10 potential donors.

Missingness incorporated as an attribute (MIA) MIA is a technique that uses missing status as a predictor rather than explicitly imputing missing values [31, 32]. MIA adds another category to nominal variables: “Missing”. For numeric variables, MIA creates two columns: one where missing values are imputed with positive infinity and the other with negative infinity. Since PH models are not compatible with infinite values, we only use MIA in boosting models. When a decision tree uses a finite cut-point to split a given numeric variable, it will assess the cut-point using both the positive and negative infinite imputed columns, and utilize whichever column provides the best split of the current data. This procedure translates to sending all missing values to the left or to the right when forming two new nodes of the decision tree, using whichever direction results in a better split.

Assumptions Each missing data strategy poses different assumptions regarding the data and the mechanisms that lead to missing values in the data. Imputation using Bayesian regression makes the same distributional assumptions as

the Bayesian models that are applied. The `mi ceRanger` algorithm does not make any formal distributional assumptions, as random forests are non-parametric and can thus handle skewed and multi-modal data as well as categorical data that are ordinal or non-ordinal. Hot deck and KNN imputation also do not make distributional assumptions, but implicitly assume that a missing value for a given observation can be approximated by aggregating observed values from the k most similar observations. PMM makes a similar implicit assumption, but is slightly more robust to skewed or multi-modal data because imputed values are sampled directly from observed ones. MIA operates based on an implicit assumption that missingness itself is informative. It is difficult to validate these assumptions in applied settings and also likely that downstream models will perform poorly if an imputation technique’s assumptions are invalid.

2.4 Evaluating imputation accuracy

Imputation accuracy was computed for each numerical and nominal variable, separately. Numeric variable imputation accuracy was measured using a re-scaled mean-squared error:

$$1 - \frac{\text{MSE}(\text{current imputation method})}{\text{MSE}(\text{imputation to the mean})}.$$

This score is greater than 0 if $\text{MSE}(\text{current imputation method})$ is smaller than $\text{MSE}(\text{imputation to the mean})$, equal to 0 if the two MSEs are equal, and less than 0 if $\text{MSE}(\text{current imputation method})$ is greater than $\text{MSE}(\text{imputation to the mean})$. Nominal variable imputation accuracy was measured using a re-scaled classification accuracy:

$$1 - \frac{\text{Classification error}(\text{current imputation method})}{\text{Classification error}(\text{imputation to the mean})}.$$

This score is greater than 0 if the classification error of the current imputation method is less than that of imputation to the mean, equal to 0 if the two classification errors are equal, and less than 0 if the classification error of the current imputation method is worse than imputation to the mean. These numeric and nominal scores are analogous to the more well known R^2 and Kappa statistics, respectively, but are modified slightly in the current analysis so that imputation to the mean will always have a score of 0. This modification makes it easier to compare the accuracy of each imputation strategy directly with imputation to the mean.

2.5 Risk Prediction Models

We applied two modeling strategies after imputing missing values:

- Cox proportional hazards (PH) model with forward stepwise variable selection
- Gradient boosted decision trees (hereafter referred to as ‘boosting’)

A thorough description of stepwise variable selection and boosting can be found in Sections 6.1.2 and 8.2.2, respectively, of *Introduction to Statistical Learning* [33]. Sir David Cox’s PH model is one of the most frequently applied methods for the analysis of right-censored time-to-event outcomes [34]. According to the PH assumption, the effect of a unit

increase in a predictor is multiplicative with respect to a baseline hazard function. Boosting grows a sequence of decision trees, each using information from the previous trees in an attempt to correct their errors [35, 36].

2.6 Evaluation of Predictions

The Brier score The prognostic value of each risk prediction model was primarily assessed using the Brier score, which depends on both the discrimination and calibration of predicted risk values [37, 38]. Let $\tilde{Y}_i(t)$ represent the observed status of individual i at time $t > 0$ in a testing set of M observations. Suppose $\tilde{Y}_i(t) = 1$ if there is an observed event at or before t and $\tilde{Y}_i(t) = 0$ otherwise. The Brier score is computed with

$$\widehat{\text{BS}}(t) = \frac{1}{M} \sum_{i=1}^M \widehat{W}_i(t) \left\{ \tilde{Y}_i(t) - \widehat{S}(t | \mathbf{x}_i) \right\}^2, \quad (1)$$

where, for the i^{th} observation, $\widehat{S}(t | \mathbf{x}_i)$ is the estimated probability of survival at time t according to a given risk prediction model, \mathbf{x}_i is the set of input values for predictor variables in the model, and $\widehat{W}_i(t)$ is the inverse proportional censoring weight at time t [39]. Thus, the Brier score is the mean squared difference between observed event status and expected event status according to a RPE at time t . Throughout the current analysis, we set $t = 6$ months after receiving MCS to focus on short term risk prediction. Models have been developed to simultaneously predict short term and long term mortality risk after receiving MCS, but these are beyond the scope of the current study [40].

The scaled Brier score The Brier score is dependent on the rate of observed events, which can make it a difficult metric to interpret. It is often more informative to scale the Brier score based on the Brier score of a naive model. More specifically, for a given risk prediction model, the scaled Brier score is computed as

$$\text{Scaled } \widehat{\text{BS}}(t) \text{ of model} = 1 - \frac{\widehat{\text{BS}}(t) \text{ of model}}{\widehat{\text{BS}}(t) \text{ of naive model}}.$$

As the Brier score for risk prediction is analogous to mean-squared error for prediction of a continuous outcome, the scaled Brier score is analogous to the R^2 statistic. Similar to the R^2 statistic, a scaled $\widehat{\text{BS}}(t)$ of 1.00 and 0.00 indicate a perfect and worthless model, respectively. In our analyses, a Kaplan-Meier estimate based on the training data (*i.e.*, a risk prediction model that did not use any predictor variables) provided the naive prediction. In the current analysis, we multiply scaled Brier score values by 100 for ease of interpretation.

Discrimination and calibration The discrimination of a risk prediction model measures the probability that the model will successfully identify which of two observations is at higher risk for the event of interest. We estimated discrimination using a time-dependent concordance (C-) index that accounted for covariate-dependent censoring. A C-index of 0.50 and 1.00 correspond to worthless and perfect discrimination, respectively. Similar to the scaled Brier score, we multiply C-index values by 100 for ease of interpretation. Calibration slope plots measure a risk prediction model's absolute accuracy. We estimated calibration error by averaging the squared distance between expected and observed event rates according to a calibration plot. Full description of these evaluation metrics are available [41, 42].

2.7 Internal Validation via Monte-Carlo Cross-Validation (MCCV)

To assess the prognostic value of each missing data strategy, we internally validated a total of 23 modeling algorithm based on combinations of imputation strategies and modeling strategies described in Sections 2.3 and 2.5. For convenience, we use the term ‘modeling algorithm’ to denote the combination of a missing data strategy and a modeling strategy (*e.g.*, imputation using mean/mode values followed by fitting the PH model with stepwise variable selection) [43]. We conducted internal validation using 200 replicates of Monte-Carlo cross validation, a resampling technique for internal validation.

Steps taken in each replicate In each replicate of Monte-Carlo cross validation, 50% of the available data were used for model training and testing. All predictor variables with $< 50\%$ missing values were considered for imputation and subsequent model development. Among these variables, artificial missingness (0%, 15%, or 30% additional missing values) was induced based on patient age, with younger and older patients more likely to have missing data compared to patients who were between 40 and 65 years of age. Prior to imputation, 50 predictor variables were selected using a boosting model that quantified variable importance as the fractional contribution of each predictor to the model based on the total gain attributed to using the predictor while growing decision trees. Imputation was conducted in the training and testing sets, separately, for each imputation strategy. Although some imputation strategies (*e.g.*, KNN and random forests) can impute data in the testing set using models fitted to the training set, others (*e.g.*, Bayesian regression, PMM, and hot deck) cannot. Therefore, to ensure fair comparisons in our experiment, each imputation procedure imputed data in the training set using models fitted to the training set and then imputed data in the testing set using models fitted to the testing set. After imputation, Cox PH and boosting models were applied to each imputed dataset, separately. Last, model predictions for death and transplant were computed at 6 months following MCS surgery.

Bayesian analysis of model performance To determine whether any of the imputation methods described above had improved upon imputation to the mean, we applied Bayesian hierarchical models to analyze differences in scaled Brier score [44]. This strategy provides a flexible framework to conduct hypothesis testing and also accounts for correlation occurring within each replicate of Monte-Carlo cross validation. Specifically, within each replicate of Monte-Carlo cross validation, the performance of different modeling algorithms are correlated because they are trained and tested using the same data.

2.8 Statistical analysis

Participant characteristics were tabulated for the overall population and stratified by event status. Continuous and categorical variables were summarized as mean (standard deviation) and percent, respectively. The number and proportion of missing values were also tabulated for the overall population and stratified by event status. Missing data patterns were visualized for the overall population using an UpSet plot [45]. All of the proceeding analyses were conducted using resampling results from Monte-Carlo cross validation. Imputation accuracy was aggregated for all numeric and nominal variables to create two overall scores for each imputed dataset. For imputation methods that

created multiple datasets, scores were aggregated over each dataset to provide a single summary score. The distribution (*i.e.*, 25th, 50th, and 75th percentile) of the scaled Brier score was estimated for each modeling algorithm.

We split our results from Monte-carlo cross validation into four datasets based on outcome (mortality or transplant) and modeling procedure (Cox PH or boosting). For each dataset, we fit one hierarchical Bayesian model where the dependent variable was scaled Brier score and independent variables included the imputation strategy applied and the amount of artificially missing data (0%, 15%, or 30%) induced before imputation. With each model, we estimated the difference in scaled Brier score of downstream models when random forests, Bayesian regression, PMM, hot deck, MIA, or KNN imputation were applied to impute missing values instead of imputation to the mean.

2.9 Computational details

Our source code is available on GitHub (see <https://github.com/bcjaeger/INTERMACS-missing-data>).

3 Results

Patient Characteristics During the first 6 months after receiving MCS, the number (% of overall population) of deaths, transplants, and loss-to-follow-up events was 1,897 (13%), 1,067 (7.2%), and 981 (6.7%), respectively. The mean (standard deviation) age of patients was 57 (13) years, 66% of patients identified as white and 79% were male (Table 1).

Missing data Many predictor variables exhibited similar proportions of missing values in different outcome groups (Table 2). However, the number (percent) of missing values for surgery time was an exception, with 6,125 (41.6%) in the overall population, 2,246 (53.4%) among patients who died, and 1,713 (27.2%) among patients who were censored. Additionally, missing values for surgery time were frequently accompanied by missing values for CV pressure (Figure 1).

Imputation accuracy Single imputation strategies were more accurate than their counterparts using multiple imputation in 8 out of 10 comparisons of nominal scores and 10 out of 10 comparisons of numeric scores (Table 3). When an additional 15% of data were missing, single imputation KNN obtained the highest nominal accuracy (score: +0.02, 95% CI -0.05, 0.15) and single imputation with random forests obtained the highest numeric accuracy (score: +0.05, 95% CI 0.03, 0.08). When an additional 30% of data were missing, imputation to the mean obtained the highest numeric and nominal scores.

3.1 Scaled Brier score

Mortality risk prediction When no additional data were amputated and imputation to the mean was applied before fitting risk prediction models, the median (25th, 75th percentile) scaled Brier score was 6.09 (5.71, 6.54) for Cox PH and 7.27 (6.83, 7.77) for boosting models (Table 4; top panel). Multiple imputation strategies universally obtained higher

scaled Brier scores versus their single imputation counterparts. Multiple imputation using random forests provided the highest scaled Brier score compared to other strategies, leading to a median (25th, 75th percentile) increase in the scaled Brier score of 0.34 (0.12, 0.54) for Cox PH and 0.34 (0.14, 0.58) for boosting models. These performance increments improved when an additional 15% and 30% of data were amputed (Table 4; middle and bottom panel).

Transplant risk prediction When no additional data were amputed and imputation to the mean was applied before fitting risk prediction models, the median (25th, 75th percentile) scaled Brier score was 9.35 (8.80, 9.71) for Cox PH and 9.00 (8.55, 9.41) for boosting models (Table 5; top panel). For Cox PH models, imputation to the mean provided the lowest scaled Brier score, and random forest imputation led to a median (25th, 75th percentile) increase of 0.13 (0.03, 0.29) versus imputation to the mean. For boosting models, surprisingly, imputation to the mean provided a higher scaled Brier score than all imputation methods except for multiple imputation using Bayesian regression. When an additional 15% and 30% of data were amputed, the performance increments corresponding to the use of multiple imputation increased for both Cox PH and boosting models (Table 5; middle and bottom panel).

3.2 Discrimination and calibration

Mortality risk prediction Regardless of how much additional data were amputed, boosting models obtained higher median C-indices than PH models for prediction of 6-month mortality risk (Table 6). In addition, all models that used multiple imputation consistently obtained higher median C-indices compared to their counterparts using single imputation. When 0 and 15% additional data were amputed, median calibration error was lower for PH models compared to boosting models, but boosting models obtained lower median calibration error when 30% additional data were amputed (Table 7). Almost all imputation strategies provided lower median calibration error compared with imputation to the mean.

Transplant risk prediction For all amounts of additional data amputed, PH models obtained higher median C-indices than boosting models for prediction of 6-month transplant risk (Table 8). Similar to mortality risk prediction, multiple imputation strategies generally provided higher C-indices than their counterparts using single imputation strategy. For boosting models, MIA provided higher C-indices compared to all other single imputation strategies and had similar or superior performance compared to several multiple imputation strategies. Differences in calibration error were minor when no additional missing data were amputed (Table 9). When an additional 30% of data were amputed, boosting models using MIA obtained lower calibration error than any other strategy.

Bayesian analysis of model performance Adjusting for the amount of additional missing data amputed and the outcome variable, the posterior probability that an imputation strategy would improve the scaled Brier score of a downstream model relative to imputation to the mean was maximized by using multiple imputation with random forests (probability of improvement: 0.998; Figure 2). Similarly, multiple imputation using random forests was estimated to have the highest posterior probability of improving the C-index in comparison to using imputation to the mean (probability of improvement: 0.962; Figure 3). However, the estimated posterior probability of a reduction in calibration

was 1 when using either single or multiple imputation with random forests compared with imputation to the mean (Figure 4). Although imputation using random forest was estimated to be the best overall option, there was moderate to strong evidence that MIA and each multiple imputation strategy we applied would improve prognostic accuracy of downstream models compared with imputation to the mean.

4 Discussion

In this article, we leveraged data from the INTERMACS registry to evaluate how the use of different imputation strategies prior to fitting a risk prediction model would impact the external prognostic accuracy of the model. External prognostic accuracy was measured at 6 months after receiving MCS to focus on short term risk prediction, and the primary measure of accuracy was the scaled Brier score. We evaluated the performance of 12 imputation strategies in a broad range of settings by varying the type of modeling algorithm, the outcome variable, and the amount of additional missing data amputated prior to performing imputation. Our resampling experiment indicated that conducting multiple imputation has a high likelihood of increasing the downstream scaled Brier score and C-index of risk prediction models compared with imputation to the mean. Additionally, multiple imputation with random forests emerged as the imputation strategy that maximized the probability of developing a more prognostic model compared with imputation to the mean.

In previous studies involving the INTERMACS data registry, imputation to the mean has been applied prior to developing a mortality risk prediction model [46, 47, 48, 7, 8]. The current analysis has shown that the prognostic accuracy of these models can be increased by implementing a different strategy to impute missing values, particularly if multiple imputation is applied. However, few studies have investigated best practices on the use of multiple imputation for prediction models, and few software packages allow users to implement multiple imputation procedures that adhere to best practices for prediction model development (*e.g.*, using only the training data to impute missing values). Further development of open source software that allows investigators to safely and succinctly implement multiple imputation for prediction models (*e.g.*, the *mi ceRanger* package) may increase the presence of multiple imputation in published risk prediction models.

Table 1: Participant characteristics stratified by event status.

Characteristic	Overall	Censored	Cessation of support	Dead	Transplant
No. of patients	14,738	6,308	310	4,204	3,916
months_post_implant	18 (16)	25 (18)	16 (11)	13 (14)	13 (10)
Age, years	57 (13)	57 (13)	48 (14)	61 (12)	53 (12)
Sex					
Female	21	22	41	22	19
Male	79	78	59	78	81
Race					
White	66	63	64	71	67
Black	25	28	27	21	23
Other	9.2	9.6	9.4	7.4	10
Body mass index	29 (7)	29 (7)	29 (8)	29 (7)	28 (6)
Device strategy					
Other	0.6	0.6	2.6	0.5	0.6
Bridge to transplant	52	43	51	40	81
Destination therapy	47	56	46	60	18
LVEDD	6.83 (1.10)	6.85 (1.07)	6.49 (0.93)	6.69 (1.12)	6.95 (1.12)
Urinary albumin, g/dl	3.41 (0.64)	3.42 (0.61)	3.41 (0.64)	3.33 (0.66)	3.49 (0.65)
Urinary creatinine, mg/dl	1.39 (0.68)	1.36 (0.62)	1.17 (0.53)	1.49 (0.77)	1.35 (0.67)
CV pressure	10.8 (6.2)	10.4 (6.1)	9.9 (6.0)	11.6 (6.5)	10.7 (6.0)
Periphal edema	35	33	37	44	31
BUN, mg/dl	29 (18)	28 (17)	22 (13)	32 (19)	28 (18)
Bilirubin levels, mg/dl	1.37 (1.84)	1.25 (1.14)	1.28 (1.95)	1.52 (2.46)	1.41 (1.97)
Device type					
Bi-ventricular assistance device	3.5	2.1	0.3	5.8	3.4
Left-ventricular assistance device	97	98	100	94	97
Surgery time, minutes	292 (113)	289 (110)	272 (96)	320 (128)	272 (98)
CPB time, minutes	95 (49)	93 (45)	88 (38)	103 (56)	90 (44)

Note:

Table values are mean (standard deviation) or %

Table 2: Number (percent) of missing values for a selection of predictor variables in the overall population and in subgroups based on event status.

	Overall	Dead	Transplant	Censored	Cessation of support
CV pressure	7,415 (50.3%)	2,156 (51.3%)	2,006 (51.2%)	3,108 (49.3%)	145 (46.8%)
Surgery time, minutes	6,125 (41.6%)	2,246 (53.4%)	2,007 (51.3%)	1,713 (27.2%)	159 (51.3%)
Periphal edema	5,093 (34.6%)	1,543 (36.7%)	1,470 (37.5%)	1,952 (30.9%)	128 (41.3%)
LVEDD	3,155 (21.4%)	1,000 (23.8%)	866 (22.1%)	1,233 (19.5%)	56 (18.1%)
Urinary albumin, g/dl	1,014 (6.88%)	326 (7.75%)	309 (7.89%)	359 (5.69%)	20 (6.45%)
CPB time, minutes	1,010 (6.85%)	287 (6.83%)	274 (7.00%)	421 (6.67%)	28 (9.03%)
Bilirubin levels, mg/dl	850 (5.77%)	291 (6.92%)	237 (6.05%)	304 (4.82%)	18 (5.81%)
Body mass index	77 (0.52%)	26 (0.62%)	19 (0.49%)	31 (0.49%)	1 (0.32%)
BUN, mg/dl	50 (0.34%)	10 (0.24%)	8 (0.20%)	32 (0.51%)	0 (0.00%)
Sex	24 (0.16%)	9 (0.21%)	4 (0.10%)	11 (0.17%)	0 (0.00%)
Urinary creatinine, mg/dl	20 (0.14%)	8 (0.19%)	4 (0.10%)	8 (0.13%)	0 (0.00%)
Age, years	0 (0.00%)	0 (0.00%)	0 (0.00%)	0 (0.00%)	0 (0.00%)
Race	0 (0.00%)	0 (0.00%)	0 (0.00%)	0 (0.00%)	0 (0.00%)
Device strategy	0 (0.00%)	0 (0.00%)	0 (0.00%)	0 (0.00%)	0 (0.00%)
Device type	0 (0.00%)	0 (0.00%)	0 (0.00%)	0 (0.00%)	0 (0.00%)

Table 3: Accuracy of strategies to impute artificial missing data

	Nominal variables		Numeric variables	
	Single imputation	Multiple imputation	Single imputation	Multiple imputation
+15% additional missing data				
Imputation to the mean	0 (reference)	—	0 (reference)	—
Hot deck	-0.24 (-0.34, -0.16)	-0.25 (-0.37, -0.18)	-0.35 (-0.53, -0.29)	-0.42 (-0.54, -0.36)
K-nearest-neighbors	+0.02 (-0.05, 0.15)	-0.01 (-0.09, 0.11)	+0.01 (-0.01, 0.03)	-0.02 (-0.05, 0.00)
Predictive mean matching	-0.15 (-0.34, 0.00)	-0.15 (-0.35, 0.00)	-0.25 (-0.40, -0.20)	-0.26 (-0.35, -0.21)
Random forest	-0.15 (-0.26, -0.03)	-0.15 (-0.26, -0.03)	+0.05 (0.03, 0.08)	+0.02 (-0.01, 0.04)
Bayesian regression	-0.14 (-0.26, 0.01)	-0.14 (-0.27, 0.01)	-0.30 (-0.41, -0.23)	-0.30 (-0.41, -0.23)
+30% additional missing data				
Imputation to the mean	0 (reference)	—	0 (reference)	—
Hot deck	-0.25 (-0.34, -0.18)	-0.26 (-0.36, -0.18)	-0.34 (-0.46, -0.30)	-0.40 (-0.53, -0.36)
K-nearest-neighbors	-0.04 (-0.09, 0.03)	-0.07 (-0.13, 0.00)	-0.02 (-0.03, -0.01)	-0.05 (-0.07, -0.04)
Predictive mean matching	-0.18 (-0.38, -0.04)	-0.18 (-0.37, -0.04)	-0.29 (-0.46, -0.24)	-0.29 (-0.40, -0.25)
Random forest	-0.18 (-0.28, -0.07)	-0.18 (-0.28, -0.08)	-0.01 (-0.03, 0.01)	-0.03 (-0.06, -0.01)
Bayesian regression	-0.17 (-0.29, -0.04)	-0.17 (-0.29, -0.05)	-0.31 (-0.43, -0.27)	-0.31 (-0.43, -0.27)

Table 4: Median (25th, 75th percentile) change in scaled Brier score when different imputation strategies are applied to training and testing sets instead of imputation to the mean prior to developing a risk prediction model for mortality. Table values show the scaled Brier score for imputation to the mean. For other imputation strategies, table values show the change in scaled Brier score relative to the scaled Brier score when imputation to the mean was applied. All table values are multiplied by 100 for ease of interpretability

Imputation method	Proportional hazards		Gradient boosted decision trees	
	Single Imputation	Multiple Imputation	Single Imputation	Multiple Imputation
No additional missing data				
Imputation to the mean	6.09 (5.71, 6.54)	–	7.27 (6.83, 7.77)	–
Missingness as an attribute	–	–	+0.09 (-0.16, 0.31)	–
Hot deck	-0.25 (-0.47, 0.01)	+0.05 (-0.15, 0.24)	-0.24 (-0.46, 0.03)	+0.25 (0.08, 0.45)
K-nearest-neighbors	+0.09 (-0.06, 0.23)	+0.18 (0.04, 0.34)	-0.06 (-0.27, 0.18)	+0.28 (0.06, 0.46)
Predictive mean matching	-0.30 (-0.53, -0.03)	+0.15 (-0.01, 0.37)	-0.22 (-0.43, 0.14)	+0.34 (0.13, 0.54)
Random forest	+0.05 (-0.24, 0.33)	+0.34 (0.12, 0.54)	-0.08 (-0.32, 0.21)	+0.34 (0.14, 0.58)
Bayesian regression	-0.35 (-0.61, -0.10)	+0.07 (-0.10, 0.29)	-0.25 (-0.52, 0.05)	+0.29 (0.08, 0.52)
+15% additional missing data				
Imputation to the mean	5.56 (4.95, 6.03)	–	6.72 (6.13, 7.33)	–
Missingness as an attribute	–	–	+0.52 (0.21, 0.77)	–
Hot deck	+0.10 (-0.22, 0.46)	+0.49 (0.21, 0.78)	+0.02 (-0.28, 0.33)	+0.58 (0.29, 0.92)
K-nearest-neighbors	+0.36 (0.10, 0.65)	+0.53 (0.25, 0.79)	+0.04 (-0.23, 0.36)	+0.42 (0.16, 0.68)
Predictive mean matching	+0.03 (-0.32, 0.41)	+0.54 (0.20, 0.90)	+0.21 (-0.25, 0.64)	+0.66 (0.32, 1.12)
Random forest	+0.39 (-0.05, 0.75)	+0.76 (0.37, 1.12)	+0.35 (0.01, 0.76)	+0.73 (0.41, 1.06)
Bayesian regression	+0.05 (-0.44, 0.44)	+0.49 (0.10, 0.85)	+0.19 (-0.21, 0.59)	+0.58 (0.29, 1.06)
+30% additional missing data				
Imputation to the mean	4.79 (4.11, 5.55)	–	6.29 (5.67, 7.02)	–
Missingness as an attribute	–	–	+0.40 (0.11, 0.75)	–
Hot deck	+0.47 (0.03, 0.99)	+0.73 (0.22, 1.38)	+0.10 (-0.24, 0.44)	+0.51 (0.05, 0.99)
K-nearest-neighbors	+0.57 (0.23, 0.97)	+0.77 (0.47, 1.18)	-0.09 (-0.44, 0.23)	+0.36 (0.09, 0.67)
Predictive mean matching	+0.25 (-0.36, 0.82)	+0.71 (0.16, 1.36)	+0.09 (-0.33, 0.64)	+0.58 (0.06, 1.05)
Random forest	+0.62 (0.08, 1.22)	+1.04 (0.39, 1.83)	+0.39 (-0.19, 0.77)	+0.69 (0.27, 1.12)
Bayesian regression	+0.22 (-0.40, 0.82)	+0.68 (0.10, 1.28)	+0.10 (-0.44, 0.62)	+0.43 (-0.03, 0.93)

Table 5: Median (25th, 75th percentile) change in scaled Brier score when different imputation strategies are applied to training and testing sets instead of imputation to the mean prior to developing a risk prediction model for transplant. Table values show the scaled Brier score for imputation to the mean. For other imputation strategies, table values show the change in scaled Brier score relative to the scaled Brier score when imputation to the mean was applied. All table values are multiplied by 100 for ease of interpretability

Imputation method	Proportional hazards		Gradient boosted decision trees	
	Single Imputation	Multiple Imputation	Single Imputation	Multiple Imputation
No additional missing data				
Imputation to the mean	9.35 (8.80, 9.71)	–	9.00 (8.55, 9.41)	–
Missingness as an attribute	–	–	-0.07 (-0.28, 0.13)	–
Hot deck	+0.01 (-0.12, 0.15)	+0.06 (-0.04, 0.23)	-0.24 (-0.43, 0.04)	-0.01 (-0.20, 0.17)
K-nearest-neighbors	+0.06 (-0.04, 0.17)	+0.08 (0.00, 0.19)	-0.27 (-0.50, -0.05)	-0.05 (-0.20, 0.10)
Predictive mean matching	+0.04 (-0.12, 0.19)	+0.14 (0.02, 0.29)	-0.34 (-0.60, -0.10)	-0.06 (-0.23, 0.15)
Random forest	+0.03 (-0.10, 0.19)	+0.13 (0.03, 0.29)	-0.32 (-0.50, -0.07)	-0.05 (-0.21, 0.14)
Bayesian regression	+0.03 (-0.13, 0.16)	+0.10 (0.00, 0.26)	-0.32 (-0.58, -0.05)	+0.02 (-0.13, 0.25)
+15% additional missing data				
Imputation to the mean	8.76 (8.20, 9.21)	–	8.01 (7.57, 8.54)	–
Missingness as an attribute	–	–	+0.50 (0.27, 0.78)	–
Hot deck	+0.25 (-0.04, 0.55)	+0.42 (0.20, 0.78)	-0.10 (-0.34, 0.23)	+0.21 (-0.02, 0.52)
K-nearest-neighbors	+0.46 (0.20, 0.73)	+0.54 (0.28, 0.79)	-0.10 (-0.41, 0.20)	+0.12 (-0.12, 0.38)
Predictive mean matching	+0.45 (0.10, 0.76)	+0.65 (0.34, 0.94)	-0.03 (-0.34, 0.21)	+0.25 (0.02, 0.62)
Random forest	+0.44 (0.12, 0.76)	+0.60 (0.32, 0.95)	-0.07 (-0.35, 0.26)	+0.16 (-0.09, 0.47)
Bayesian regression	+0.53 (0.21, 0.79)	+0.74 (0.37, 0.94)	-0.07 (-0.39, 0.24)	+0.24 (-0.09, 0.56)
+30% additional missing data				
Imputation to the mean	7.96 (7.26, 8.63)	–	7.09 (6.45, 7.68)	–
Missingness as an attribute	–	–	+0.83 (0.55, 1.10)	–
Hot deck	+0.45 (-0.02, 0.90)	+0.60 (0.15, 1.11)	-0.01 (-0.34, 0.41)	+0.19 (-0.17, 0.65)
K-nearest-neighbors	+0.42 (0.00, 0.79)	+0.61 (0.18, 0.90)	-0.21 (-0.54, 0.19)	+0.09 (-0.22, 0.46)
Predictive mean matching	+0.70 (0.21, 1.21)	+0.90 (0.46, 1.46)	+0.09 (-0.32, 0.54)	+0.34 (-0.04, 0.85)
Random forest	+0.70 (0.14, 1.27)	+0.93 (0.49, 1.45)	-0.13 (-0.46, 0.43)	+0.25 (-0.12, 0.66)
Bayesian regression	+0.77 (0.32, 1.40)	+1.00 (0.44, 1.53)	0.00 (-0.45, 0.52)	+0.24 (-0.17, 0.80)

Table 6: Median (25th, 75th percentile) change in concordance index when different imputation strategies are applied to training and testing sets instead of imputation to the mean prior to developing a risk prediction model for mortality. Table values show the concordance index for imputation to the mean. For other imputation strategies, table values show the change in concordance index relative to the concordance index when imputation to the mean was applied. All table values are multiplied by 100 for ease of interpretability

Imputation method	Proportional hazards		Gradient boosted decision trees	
	Single Imputation	Multiple Imputation	Single Imputation	Multiple Imputation
No additional missing data				
Imputation to the mean	69.3 (68.9, 69.8)	–	70.7 (70.3, 71.0)	–
Missingness as an attribute	–	–	0.00 (-0.20, 0.19)	–
Hot deck	-0.20 (-0.44, 0.05)	+0.04 (-0.13, 0.27)	-0.19 (-0.36, 0.00)	+0.13 (-0.04, 0.28)
K-nearest-neighbors	+0.03 (-0.10, 0.23)	+0.14 (-0.02, 0.36)	-0.10 (-0.30, 0.13)	+0.14 (-0.03, 0.30)
Predictive mean matching	-0.34 (-0.56, -0.03)	+0.11 (-0.05, 0.37)	-0.21 (-0.44, 0.05)	+0.21 (0.06, 0.39)
Random forest	+0.04 (-0.24, 0.29)	+0.30 (0.08, 0.52)	-0.02 (-0.26, 0.18)	+0.24 (0.07, 0.41)
Bayesian regression	-0.39 (-0.69, -0.10)	+0.09 (-0.16, 0.28)	-0.21 (-0.44, -0.02)	+0.22 (0.06, 0.41)
+15% additional missing data				
Imputation to the mean	69.2 (68.8, 69.7)	–	70.5 (70.1, 71.0)	–
Missingness as an attribute	–	–	+0.10 (-0.11, 0.31)	–
Hot deck	-0.18 (-0.52, 0.19)	+0.25 (-0.07, 0.58)	-0.23 (-0.50, 0.03)	+0.12 (-0.07, 0.32)
K-nearest-neighbors	+0.16 (-0.17, 0.42)	+0.30 (0.05, 0.56)	-0.16 (-0.33, 0.10)	+0.10 (-0.07, 0.31)
Predictive mean matching	-0.42 (-0.83, 0.02)	+0.24 (-0.07, 0.53)	-0.26 (-0.54, 0.00)	+0.26 (0.06, 0.43)
Random forest	-0.04 (-0.39, 0.26)	+0.41 (0.05, 0.64)	-0.08 (-0.29, 0.19)	+0.27 (0.04, 0.43)
Bayesian regression	-0.50 (-0.95, -0.06)	+0.20 (-0.11, 0.47)	-0.29 (-0.48, -0.03)	+0.23 (0.07, 0.43)
+30% additional missing data				
Imputation to the mean	68.9 (68.4, 69.4)	–	70.2 (69.8, 70.7)	–
Missingness as an attribute	–	–	+0.12 (-0.08, 0.31)	–
Hot deck	-0.15 (-0.52, 0.30)	+0.12 (-0.23, 0.51)	-0.22 (-0.47, 0.02)	+0.10 (-0.17, 0.32)
K-nearest-neighbors	+0.17 (-0.11, 0.49)	+0.33 (0.09, 0.65)	-0.08 (-0.27, 0.16)	+0.19 (-0.01, 0.38)
Predictive mean matching	-0.75 (-1.15, -0.34)	+0.06 (-0.29, 0.52)	-0.36 (-0.67, -0.04)	+0.27 (0.04, 0.48)
Random forest	-0.29 (-0.80, 0.23)	+0.26 (-0.10, 0.64)	-0.16 (-0.47, 0.11)	+0.29 (0.07, 0.52)
Bayesian regression	-0.75 (-1.28, -0.22)	+0.12 (-0.29, 0.48)	-0.36 (-0.70, -0.07)	+0.19 (-0.01, 0.44)

Table 7: Median (25th, 75th percentile) change in calibration error when different imputation strategies are applied to training and testing sets instead of imputation to the mean prior to developing a risk prediction model for mortality. Table values show the calibration error for imputation to the mean. For other imputation strategies, table values show the change in calibration error relative to the calibration error when imputation to the mean was applied. All table values are multiplied by 100 for ease of interpretability

Imputation method	Proportional hazards		Gradient boosted decision trees	
	Single Imputation	Multiple Imputation	Single Imputation	Multiple Imputation
No additional missing data				
Imputation to the mean	2.41 (1.71, 3.44)	–	3.29 (2.24, 4.80)	–
Missingness as an attribute	–	–	-0.09 (-1.07, 0.65)	–
Hot deck	-0.04 (-0.68, 0.58)	-0.45 (-1.25, 0.25)	-0.13 (-1.12, 0.65)	-0.90 (-1.98, 0.01)
K-nearest-neighbors	+0.04 (-0.59, 0.65)	-0.29 (-0.80, 0.39)	-0.30 (-1.14, 0.61)	-0.75 (-1.59, 0.14)
Predictive mean matching	-0.18 (-0.69, 0.47)	-0.69 (-1.36, -0.03)	-0.11 (-1.27, 0.89)	-1.02 (-2.08, -0.12)
Random forest	-0.07 (-0.58, 0.65)	-0.46 (-1.10, 0.17)	-0.56 (-1.38, 0.46)	-1.10 (-2.08, -0.14)
Bayesian regression	-0.08 (-0.75, 0.53)	-0.57 (-1.43, 0.02)	-0.26 (-1.08, 0.57)	-0.85 (-1.91, 0.12)
+15% additional missing data				
Imputation to the mean	5.75 (3.74, 8.59)	–	6.28 (4.17, 9.45)	–
Missingness as an attribute	–	–	-2.83 (-4.81, -0.83)	–
Hot deck	-2.16 (-4.31, -1.08)	-3.92 (-6.23, -1.72)	-1.66 (-3.82, -0.34)	-3.44 (-5.97, -1.48)
K-nearest-neighbors	-2.01 (-3.51, -0.66)	-2.48 (-4.08, -1.14)	-0.61 (-2.28, 0.84)	-2.04 (-3.32, -0.63)
Predictive mean matching	-3.83 (-6.40, -1.87)	-3.76 (-6.66, -1.04)	-3.52 (-6.43, -1.67)	-3.50 (-7.09, -1.00)
Random forest	-3.80 (-5.75, -2.07)	-4.35 (-6.60, -1.53)	-3.74 (-6.34, -1.34)	-3.92 (-6.29, -1.50)
Bayesian regression	-3.76 (-6.45, -1.81)	-3.80 (-6.61, -1.04)	-3.79 (-6.80, -1.39)	-3.27 (-6.40, -0.46)
+30% additional missing data				
Imputation to the mean	9.48 (5.50, 15.3)	–	7.02 (4.32, 11.3)	–
Missingness as an attribute	–	–	-1.61 (-5.29, 0.68)	–
Hot deck	-4.95 (-9.18, -2.49)	-6.69 (-12.8, -1.56)	-2.48 (-5.46, -0.31)	-2.48 (-7.18, 0.58)
K-nearest-neighbors	-3.47 (-6.42, -1.53)	-4.49 (-7.49, -2.39)	+0.73 (-1.56, 3.27)	-1.47 (-3.59, 0.59)
Predictive mean matching	-7.33 (-13.0, -2.61)	-6.09 (-12.3, -0.22)	-2.58 (-7.90, 0.10)	-1.30 (-6.86, 2.29)
Random forest	-7.81 (-13.1, -3.63)	-7.39 (-13.4, -2.37)	-3.53 (-7.87, -0.29)	-2.58 (-7.27, 0.44)
Bayesian regression	-7.27 (-13.2, -2.44)	-5.91 (-12.8, -0.47)	-3.00 (-7.60, 0.97)	-0.54 (-6.60, 3.08)

Table 8: Median (25th, 75th percentile) change in concordance index when different imputation strategies are applied to training and testing sets instead of imputation to the mean prior to developing a risk prediction model for transplant. Table values show the concordance index for imputation to the mean. For other imputation strategies, table values show the change in concordance index relative to the concordance index when imputation to the mean was applied. All table values are multiplied by 100 for ease of interpretability

Imputation method	Proportional hazards		Gradient boosted decision trees	
	Single Imputation	Multiple Imputation	Single Imputation	Multiple Imputation
No additional missing data				
Imputation to the mean	79.4 (79.0, 79.8)	–	79.2 (78.9, 79.7)	–
Missingness as an attribute	–	–	-0.03 (-0.22, 0.14)	–
Hot deck	+0.01 (-0.12, 0.17)	+0.07 (-0.05, 0.23)	-0.24 (-0.40, -0.02)	-0.04 (-0.20, 0.15)
K-nearest-neighbors	+0.08 (-0.02, 0.16)	+0.08 (0.01, 0.17)	-0.21 (-0.40, -0.04)	-0.04 (-0.18, 0.10)
Predictive mean matching	+0.03 (-0.11, 0.16)	+0.13 (0.01, 0.24)	-0.34 (-0.57, -0.12)	-0.06 (-0.19, 0.16)
Random forest	+0.03 (-0.09, 0.17)	+0.15 (0.06, 0.24)	-0.26 (-0.46, -0.08)	-0.02 (-0.16, 0.14)
Bayesian regression	+0.01 (-0.15, 0.16)	+0.10 (0.01, 0.22)	-0.32 (-0.54, -0.10)	+0.02 (-0.13, 0.22)
+15% additional missing data				
Imputation to the mean	78.9 (78.5, 79.4)	–	78.4 (77.9, 78.9)	–
Missingness as an attribute	–	–	+0.47 (0.26, 0.71)	–
Hot deck	+0.24 (0.04, 0.51)	+0.47 (0.26, 0.76)	-0.13 (-0.40, 0.22)	+0.29 (0.07, 0.58)
K-nearest-neighbors	+0.36 (0.21, 0.54)	+0.46 (0.29, 0.62)	-0.13 (-0.39, 0.17)	+0.17 (-0.06, 0.39)
Predictive mean matching	+0.32 (0.11, 0.58)	+0.56 (0.37, 0.82)	-0.12 (-0.38, 0.25)	+0.32 (0.14, 0.61)
Random forest	+0.32 (0.13, 0.64)	+0.59 (0.36, 0.82)	-0.11 (-0.40, 0.24)	+0.22 (-0.03, 0.51)
Bayesian regression	+0.39 (0.17, 0.63)	+0.60 (0.40, 0.83)	-0.15 (-0.46, 0.27)	+0.27 (-0.01, 0.64)
+30% additional missing data				
Imputation to the mean	78.4 (77.7, 78.8)	–	77.4 (76.8, 78.0)	–
Missingness as an attribute	–	–	+0.91 (0.52, 1.24)	–
Hot deck	+0.34 (-0.03, 0.72)	+0.74 (0.48, 1.11)	-0.19 (-0.53, 0.34)	+0.55 (0.19, 0.86)
K-nearest-neighbors	+0.28 (-0.02, 0.47)	+0.43 (0.21, 0.66)	-0.32 (-0.78, -0.04)	-0.01 (-0.33, 0.31)
Predictive mean matching	+0.62 (0.29, 0.98)	+1.02 (0.74, 1.34)	+0.03 (-0.31, 0.44)	+0.65 (0.29, 0.95)
Random forest	+0.59 (0.22, 1.00)	+1.04 (0.76, 1.30)	-0.21 (-0.58, 0.15)	+0.36 (0.01, 0.68)
Bayesian regression	+0.81 (0.41, 1.08)	+1.10 (0.80, 1.39)	-0.04 (-0.54, 0.37)	+0.47 (0.10, 0.91)

Table 9: Median (25th, 75th percentile) change in calibration error when different imputation strategies are applied to training and testing sets instead of imputation to the mean prior to developing a risk prediction model for transplant. Table values show the calibration error for imputation to the mean. For other imputation strategies, table values show the change in calibration error relative to the calibration error when imputation to the mean was applied. All table values are multiplied by 100 for ease of interpretability

Imputation method	Proportional hazards		Gradient boosted decision trees	
	Single Imputation	Multiple Imputation	Single Imputation	Multiple Imputation
No additional missing data				
Imputation to the mean	1.36 (0.92, 2.07)	–	1.79 (1.34, 2.50)	–
Missingness as an attribute	–	–	+0.01 (-0.53, 0.54)	–
Hot deck	-0.01 (-0.37, 0.29)	0.00 (-0.39, 0.26)	+0.11 (-0.56, 0.68)	-0.07 (-0.67, 0.67)
K-nearest-neighbors	+0.00 (-0.25, 0.24)	-0.02 (-0.25, 0.21)	+0.09 (-0.40, 0.61)	-0.03 (-0.52, 0.67)
Predictive mean matching	-0.04 (-0.34, 0.32)	-0.08 (-0.41, 0.26)	+0.09 (-0.49, 0.63)	-0.04 (-0.63, 0.70)
Random forest	-0.06 (-0.39, 0.29)	-0.06 (-0.35, 0.29)	-0.02 (-0.49, 0.63)	+0.02 (-0.54, 0.56)
Bayesian regression	-0.01 (-0.40, 0.27)	-0.13 (-0.38, 0.18)	+0.12 (-0.46, 0.78)	+0.24 (-0.46, 1.04)
+15% additional missing data				
Imputation to the mean	2.48 (1.79, 3.93)	–	2.51 (1.81, 3.29)	–
Missingness as an attribute	–	–	-0.50 (-1.38, 0.16)	–
Hot deck	-0.76 (-1.95, 0.21)	-0.51 (-2.14, 0.89)	-0.01 (-1.00, 0.66)	+0.69 (-0.47, 1.97)
K-nearest-neighbors	-0.82 (-2.01, 0.21)	-0.78 (-1.96, 0.26)	+0.20 (-0.59, 1.01)	+0.23 (-0.73, 1.02)
Predictive mean matching	-1.01 (-2.15, 0.27)	-0.46 (-2.16, 0.94)	+0.15 (-0.91, 1.02)	+0.72 (-0.81, 1.87)
Random forest	-0.80 (-2.32, 0.51)	-0.59 (-2.03, 0.81)	-0.10 (-1.15, 0.66)	+0.42 (-0.93, 1.34)
Bayesian regression	-0.94 (-2.32, 0.58)	-0.64 (-2.04, 0.89)	+0.19 (-0.76, 1.16)	+0.99 (-0.50, 2.27)
+30% additional missing data				
Imputation to the mean	4.98 (3.42, 7.00)	–	3.99 (2.74, 6.22)	–
Missingness as an attribute	–	–	-1.52 (-2.62, -0.35)	–
Hot deck	-2.17 (-4.65, 0.10)	-0.49 (-3.74, 2.34)	-0.53 (-2.79, 1.05)	+1.89 (-0.93, 4.76)
K-nearest-neighbors	-1.88 (-3.34, -0.22)	-1.88 (-3.70, -0.14)	-0.41 (-1.72, 0.68)	-0.54 (-2.26, 0.88)
Predictive mean matching	-1.30 (-4.52, 1.28)	+0.04 (-3.48, 2.70)	-0.05 (-2.54, 2.53)	+1.36 (-1.26, 4.01)
Random forest	-1.80 (-4.34, 0.79)	-0.58 (-3.95, 2.18)	-0.55 (-2.64, 1.53)	+0.33 (-2.27, 2.77)
Bayesian regression	-1.34 (-4.22, 1.59)	-0.23 (-3.15, 2.61)	-0.16 (-2.47, 1.94)	+0.89 (-1.89, 3.67)

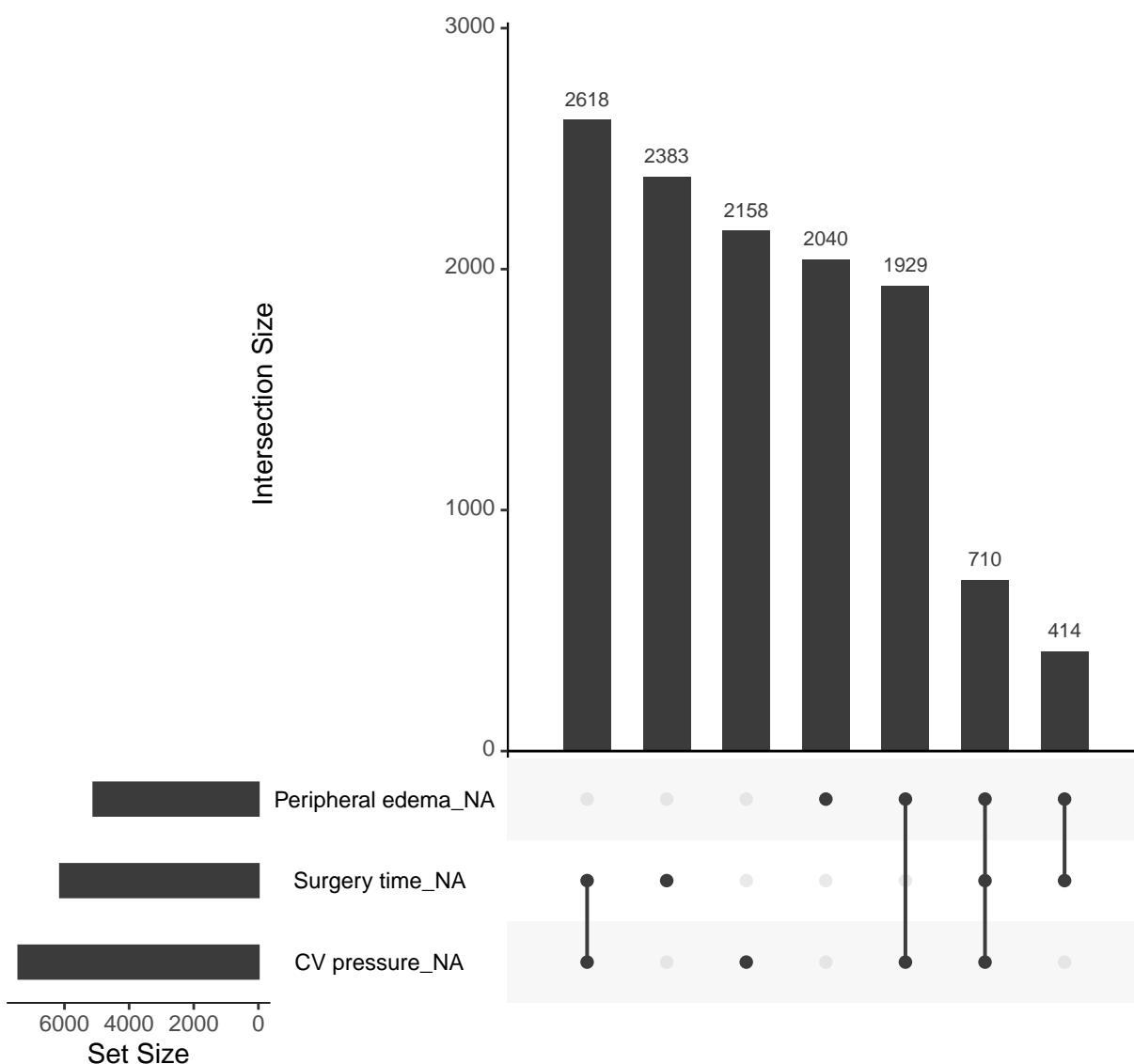


Figure 1: An upset plot showing three variables from the INTERMACS registry and all combinations of missing patterns. The bottom left plot shows the number of missing values for each variable, separately. The top right plot shows the number of missing values for each combination of the three variables. For example, there were 2,618 rows in the overall INTERMACS data where both CV pressure and surgery time were missing.

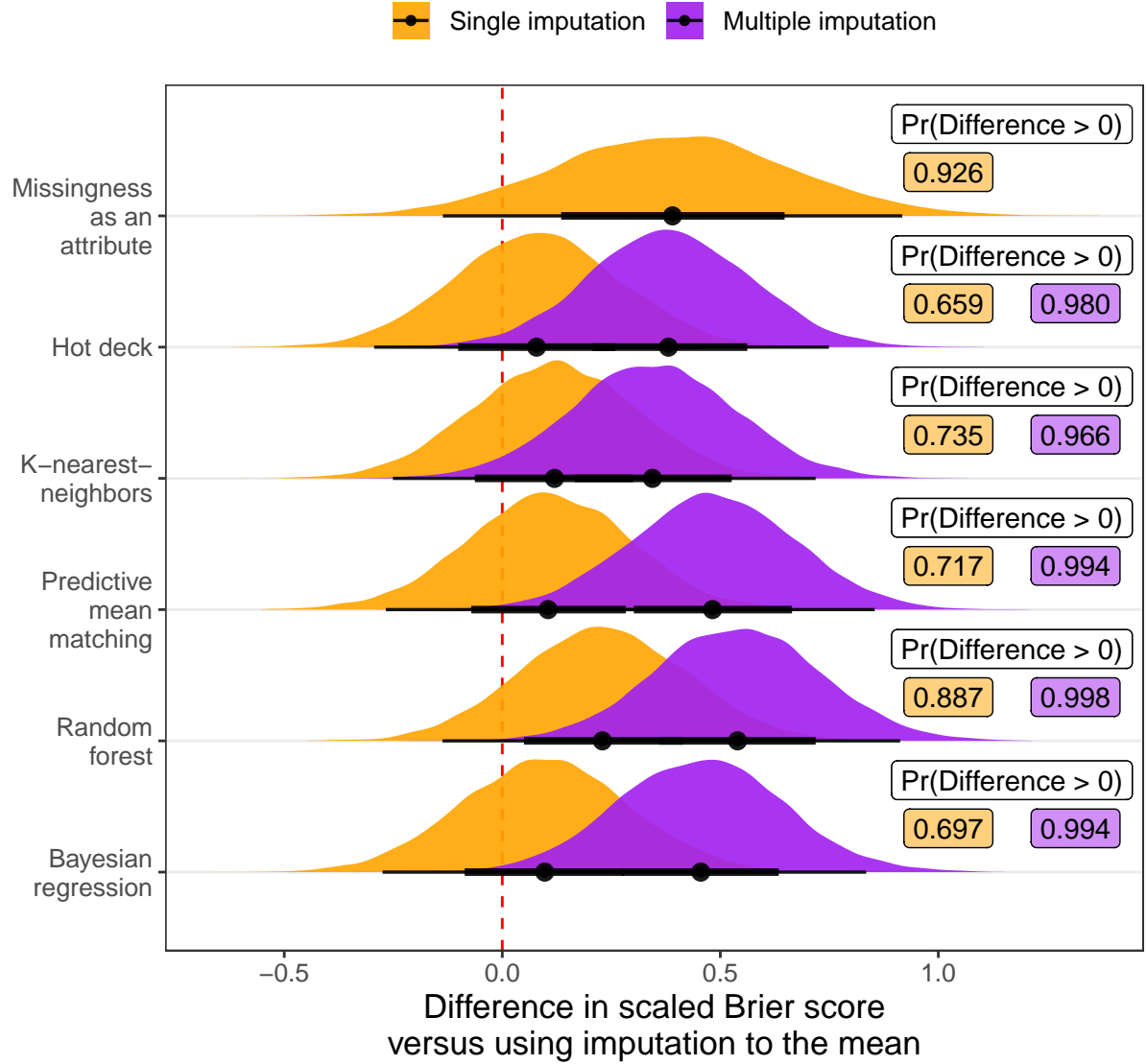


Figure 2: Posterior distribution of differences in scaled Brier score values relative to imputation to the mean when different imputation strategies are applied before fitting a risk prediction model. Results are aggregated over scenarios where the outcome is mortality and transplant and the amount of additional missing data is 0%, 15%, or 30%. Posterior probability that the difference in scaled Brier score exceeds 0, indicating an improvement in overall model accuracy for the current imputation strategy, is printed to the right of each distribution.

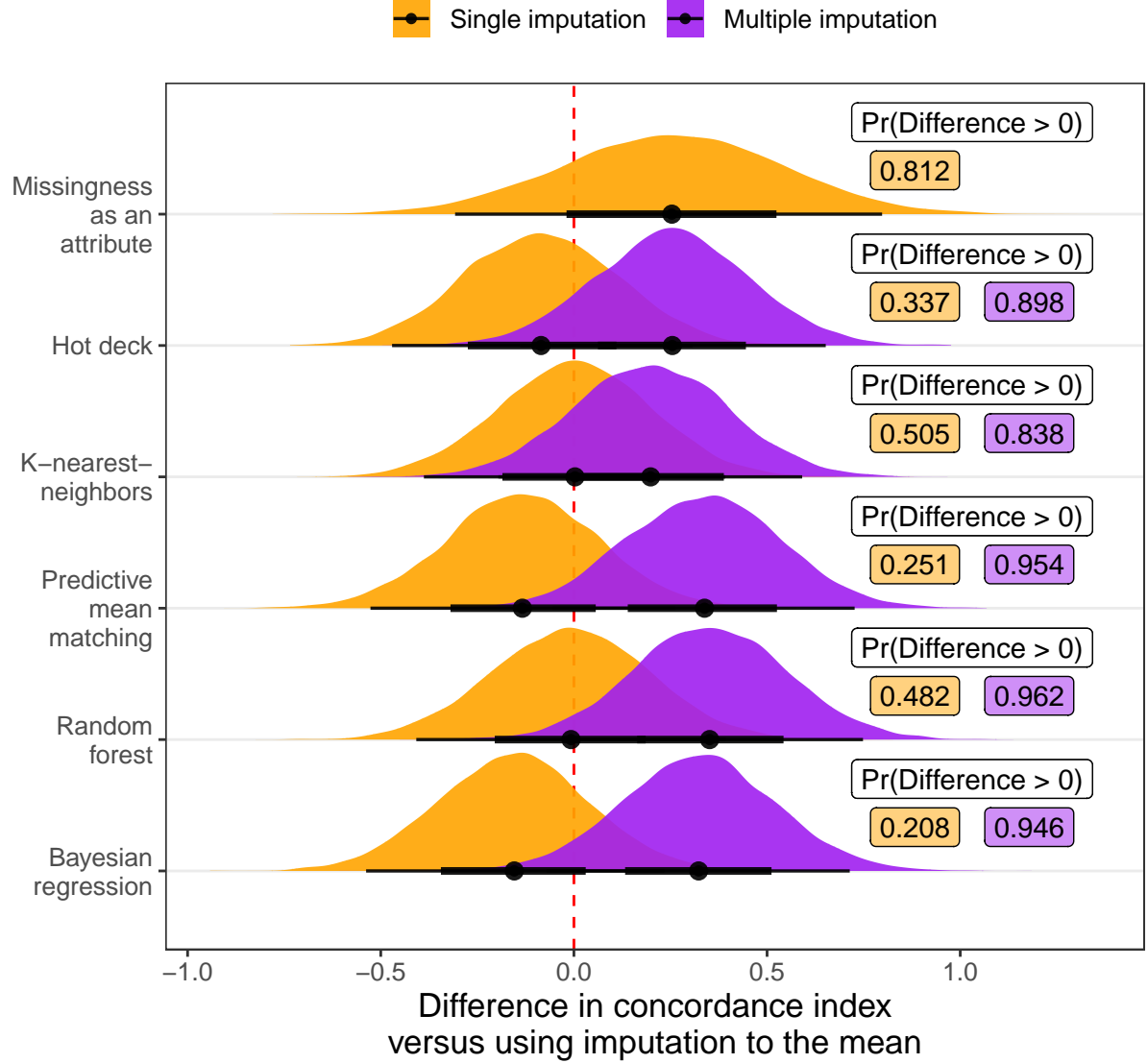


Figure 3: Posterior distribution of differences in scaled Brier score values relative to imputation to the mean when different imputation strategies are applied before fitting a risk prediction model. Results are aggregated over scenarios where the outcome is mortality and transplant and the amount of additional missing data is 0%, 15%, or 30%. Posterior probability that the difference in scaled Brier score exceeds 0, indicating an improvement in overall model accuracy for the current imputation strategy, is printed to the right of each distribution.

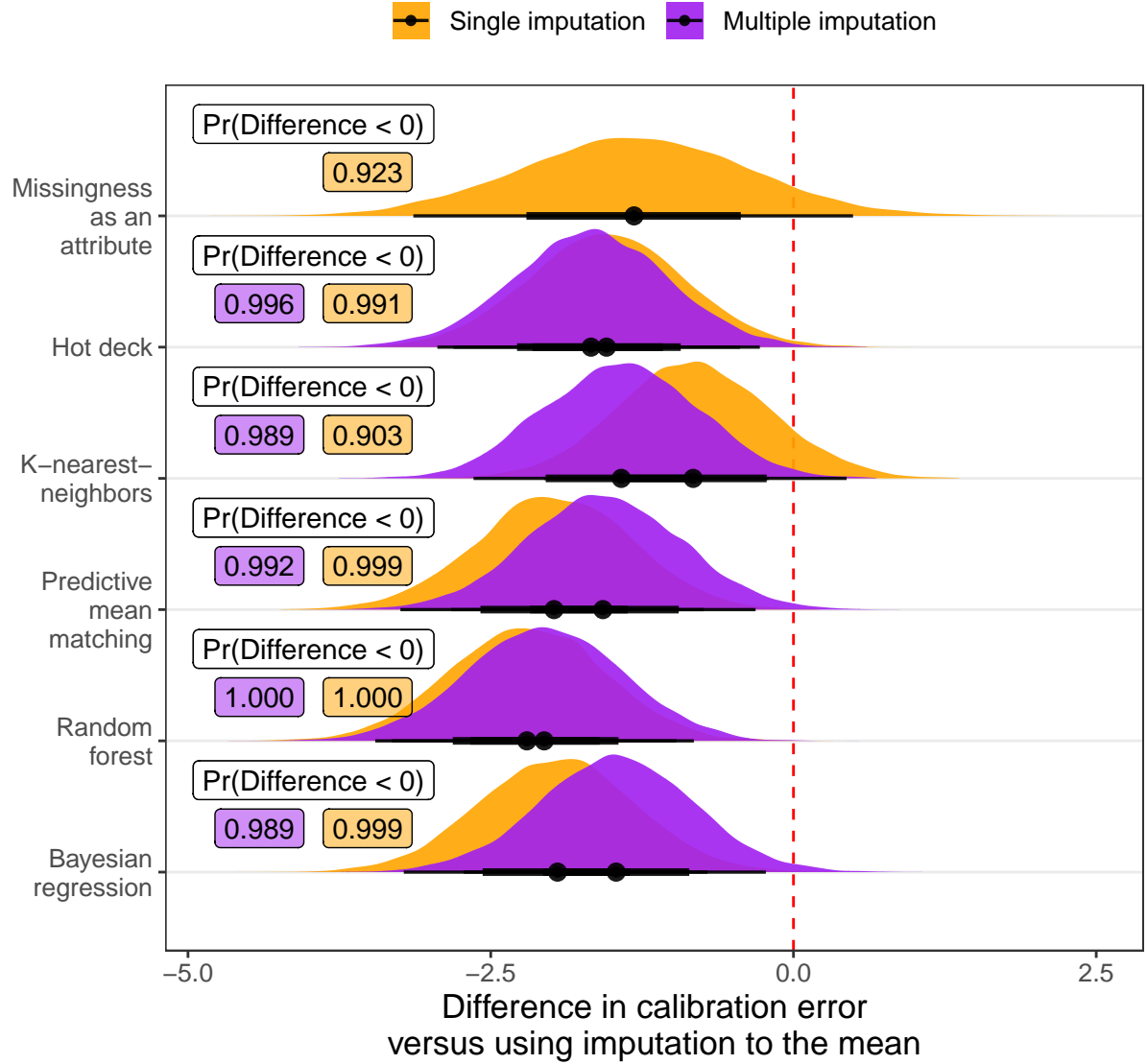


Figure 4: Posterior distribution of differences in calibration error values relative to imputation to the mean when different imputation strategies are applied before fitting a risk prediction model. Results are aggregated over scenarios where the outcome is mortality and transplant and the amount of additional missing data is 0%, 15%, or 30%. Posterior probability that the difference in calibration error exceeds 0, indicating an improvement in overall model accuracy for the current imputation strategy, is printed to the right of each distribution.

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