$\label{lem:eq:continuous} Evaluate\ the\ following\ definite\ integrals.$

1.
$$\int_{-1}^{2} (2x - x^2) dx$$

2.
$$\int_0^{\pi} 2\cos x - 1 \, dx$$

3.
$$\int_0^2 (t-1)(t+2) dt$$

4.
$$\int_0^{\pi/4} \sec \theta \tan \theta + \sec^2 \theta \, d\theta$$

5. Find the area under the curve $y = \frac{1}{x^2}$ from x = 1 to x = 10.

6. Suppose that the voltage of a battery is decreasing at a rate of $\frac{-5}{(t+1)^2}$ volts per year. How much will the voltage of the battery decrease in 3 years?

Use u-substitution to find the following integrals.

$$7. \int (x-3)^6 dx$$

$$8. \int \frac{2x}{\sqrt{x^2 + 1}} \, dt$$

9.
$$\int \frac{1}{(4x+1)^{1/3}} \, dt$$

10.
$$\int_0^{\pi/6} 3\cos 2x \, dx$$

11. Find the average value of the function $f(x) = 2 \sin x$ on the interval from 0 to π .