

# Portland State University

## Department of Physics

PH 624: Classical Mechanics

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### Problem Set 3 (Chapters 6,8,9)

H. Goldstein, C.Poole and J.Safko, Classical Mechanics, (Addison Wesley, N.Y., 2002)

#### Chapter 6: Small Oscillations

**Cooper:** 6.4 - Double Pendulum and Beats - 2. Start with solution to 1.22

**Crawford:** 6.8 - Triangular Molecule - 2. Uses standard procedure

**Fowler:** 6.12a - Normal Modes of Vibration - 2. This and the next problem are modified forms of problem 6-12 in Goldstein. In 12a start by writing the T and V matrices for the general case where all 3 k's are different and the two masses are different. Do not solve this; it is tedious and not very instructive. For this part, take  $K_1=K_3=K$ ,  $K_2=\alpha K$  and  $m=M$  (the two masses).  $K_1$  and  $K_3$  refer to the springs at the ends Now find the normal modes of vibration and solve for the motion. Take the limits  $\alpha \rightarrow 0$  and  $\alpha \rightarrow \infty$ , and discuss the resulting frequencies and their physical significance.

**Grist:** 6.12b Same set-up as above except take the case  $K_1=K_2=K_3=K$  and  $m=\beta M$ . Find the normal modes. Take the limits  $\beta \rightarrow 0$  and  $\beta \rightarrow \infty$  and discuss the frequencies and their physical interpretation.

**Hopkins:** 6.16 - Steep potential oscillations -2. A thought provoking problem about when motion is simple harmonic.

#### Chapter 8: Hamiltonian Formulation of Classical Mechanics

**Hudson:** 8.1 - Legendre transformation -1

**Illyas:** 8.8 - Hamilton's Principle and Hamilton's Equations -1. Deriving Hamilton's equations without explicitly using the Lagrangian.

**Karmaker:** 8.13 - Double Pendulum -3. A bit tedious.

**Keating:** 8.14 - Hamiltonian and Conservation Laws - 3. Straightforward but rough algebra.

**Kozell:** 8.19 Complex Pendulum -3.

#### Chapter 9: Canonical Transformations

**Kuperman:** 9.2 Canonical Transformations and Generating Functions -2

**Lankow:** 9.6 More Canonical Transformations - 3