# BenPrescott\_Assignment3\_Part1

# February 22, 2021

Ben Prescott, Assignment 3 - Part 1, MSDS422, WI2021 Importing libraries

citations

[82]: | jupyter nbconvert --to PDF "BenPrescott\_Assignment3\_Part1.ipynb"

```
[NbConvertApp] Converting notebook BenPrescott_Assignment3_Part1.ipynb to PDF
[NbConvertApp] Support files will be in BenPrescott_Assignment3_Part1_files/
[NbConvertApp] Making directory ./BenPrescott_Assignment3_Part1_files
[NbConvertApp] Making directory ./BenPrescott_Assignment3_Part1_files
[NbConvertApp] Writing 80055 bytes to ./notebook.tex
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[NbConvertApp] Running xelatex 3 times: [u'xelatex', u'./notebook.tex', '-quiet']
[NbConvertApp] Running bibtex 1 time: [u'bibtex', u'./notebook']
[NbConvertApp] WARNING | bibtex had problems, most likely because there were no
```

[NbConvertApp] PDF successfully created [NbConvertApp] Writing 138990 bytes to BenPrescott\_Assignment3\_Part1.pdf

```
[10]: import os
     import re
     import dill
     import numpy as np
     import pandas as pd
     import matplotlib.pyplot as plt
     from matplotlib.pyplot import figure
     import matplotlib.cm as cm
     import seaborn as sns
     import tensorflow as tf
     from tensorflow import keras
     import tensorboard
     from pickleshare import *
     from sklearn.model_selection import train_test_split
     from sklearn.preprocessing import MinMaxScaler
     from timeit import default_timer as timer
     from IPython.core.interactiveshell import InteractiveShell
     InteractiveShell.ast_node_interactivity = "all"
```

The tensorboard extension is already loaded. To reload it, use: %reload\_ext tensorboard

# 0.1 Objective 0: Data Input, Verification, Transformation

In this section I'll be importing the data from the Pickle file, reviewing shape, reviewing frequency of labels, rescaling the data using MinMaxScaler, separated the labels and features into new arrays, then creating a 60/20/20 train/test/validation split.

### 0.1.1 Importing, Reviewing & Verifying

Data Shape: (40320, 786)

```
[]: df.head #excluding output due to PDF export issues/length requirements
```

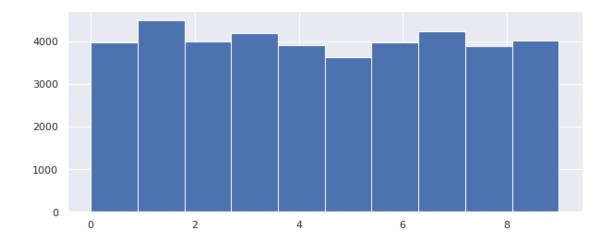
Visually reviewing the different label values and their counts. Also helps to ensure there aren't any weird values out there.

```
[13]: #Verifying image label values to ensure none are incorrect values

df['label'].unique()

#Histogram to visually verify
plt.hist(df['label'])
```

```
[13]: array([2, 1, 0, 4, 6, 3, 9, 7, 5, 8])
```



Creating a quick loop to check the Pixel features for incorrect values. Nothing is returned which shows there are no pixel values above 255 or below 0, which is accurate.

```
[14]: #Determine which columns have minimum values below 0 or maximum values above

→255

for col in df:
    if (col.startswith('pixel')) & (df[col].max() > 255):
        print('Columns with values above 255:',col)
    if (col.startswith('pixel')) & (df[col].min() < 0):
        print('Columns with values below 0:',col)
```

# 0.1.2 Rescaling Data w/ MinMaxScaler

Next I'll be rescaling the pixel features only with the MinMaxScaler. This can also be done by dividing each value by 255 (the max pixel value), but using the SKlearn algo for practice/familiarity.

```
[23]: #Loading MinMaxScaler algorithm
scaler = MinMaxScaler()
#Fitting the data to the algorithm
scaler.fit(df.iloc[:,1:785])
#Assigning the scaled data to a new variable named scaled_data
scaled_data = scaler.transform(df.iloc[:,1:785])
#Generating a new dataframe with the transformed pixels
dfscaled = pd.DataFrame(scaled_data, columns = df.iloc[:,1:785].columns)
dfscaled.iloc[0:2,153:157].head() #Reducing returned subset for PDF output

[23]: MinMaxScaler(copy=True, feature_range=(0, 1))
```

```
[23]: pixel153 pixel154 pixel155 pixel156
0 0.988235 0.988235 0.580392 0.043137
1 0.529412 0.968627 0.988235 0.909804
```

### 0.1.3 Separating Features & Labels

Now I'll be separating the features and original dataframe labels into two separate variables to prepare for train/test/validation split. I've also set the features dtype to float32 and labels to integer per the instructions.

```
[24]: features = dfscaled
  labels = df['label']
  X = features.to_numpy(copy=True, dtype = 'float32')
  y = labels.to_numpy(copy=True, dtype = 'int')
  X.shape
  y.shape
[24]: (40320, 784)
[24]: (40320,)
```

# 0.1.4 Train/Test/Validation Split (60/20/20)

Train/test/validation split. The goal is 60/20/20 train/test/validation. First train\_test\_split splits into a donor train pair and the test pair, with an initial 80/20 split. We now use the donor training set in the second train\_test\_split to create our validation set. We also decrease the ratio to 75/25 to provide us with the original 60/20/20 need.

```
X_train: (24192, 784)
y_train: (24192,)
X_test: (8064, 784)
y_test: (8064,)
X_valid: (8064, 784)
y_valid: (8064,)
```

# 0.2 Objective 1: Train & Evaluate Four Version of a MLP That Predicts Digit Labels

In this section I'll be creating four different versions of MLPs. The goal is to predict the labels of different input digits.

To start I'm going to be creating the model checkpoint save location, as well as a callback for timing the model runtime. These will be used for each model moving forward.

Common hyperparameters that will be used are the callbacks, the optimizer (Adam), the loss function (sparse\_categorical\_crossentropy), the metric returned (accuracy), the number of epochs (10), batch size (32) and the activation types (selu / softmax).

The hyperparameters that will be varied are the number of hidden layers, the number of nodes in each layer, and the kernel initializer.

```
[28]: #Model Checkpoint location
cploc = '/content/drive/MyDrive/MSDS422/Assignment3/'
class TimingCallback(keras.callbacks.Callback):
    def __init__(self, logs={}):
        self.logs=[]
    def on_epoch_begin(self, epoch, logs={}):
        self.starttime = timer()
    def on_epoch_end(self, epoch, logs={}):
        self.logs.append(timer()-self.starttime)
```

### 0.2.1 Model 1

Training the first MLP. Providing comments to help provide context, but will remove comments to save space for future models, as they will follow the same format.

```
[]: #Adding checkpoint to save the best model based on validation accuracy
   model_cp_save = keras.callbacks.ModelCheckpoint(cploc + 'model1.hdf5',_
    →save_best_only=True, monitor='val_accuracy')
   model_stop = keras.callbacks.EarlyStopping(monitor='loss', patience=3)
   model_time = TimingCallback()
   optimizer = keras.optimizers.Adam()
   #Creating the sequential model with 1 input layer, 2 hiden layers and 1 output
    \rightarrow layer
   #Leveraging SeLU to provide a layer of internal normalization
   model1 = keras.models.Sequential([
       keras.layers.Flatten(input shape = X_train.shape[1:], name = 'InputLayer'),
       keras.layers.Dense(30, activation="selu", name = 'Layer1', L
    →kernel_initializer='lecun_normal'),
       keras.layers.Dense(20, activation="selu", name = 'Layer2', __
    →kernel_initializer='lecun_normal'),
       keras.layers.Dense(10, activation="softmax", name = 'OutputLayer')
   #Compiling the model. Using sparse categorical crossentropy due to digits being \Box
    \rightarrow from 0 - 9.
   model1.compile(loss="sparse_categorical_crossentropy",
                  optimizer=optimizer,
                  metrics=["accuracy"])
   #Generating model summary
   model1.summary()
   #Fitting the model. Sticking with 20 epochs and a batch size of 32.
```

```
model1output = model1.fit(X_train, y_train, epochs=10, validation_data =__
     →(X_valid, y_valid), callbacks=[model_cp_save, model_time, model_stop],
     →batch_size=32)
    #Saving model training duration for later use
    model1time = round(sum(model_time.logs),2)
[30]: #Predicting the first 5 rows of the test data using the newly trained model
    y_proba = model1.predict(X_test[:5])
    predicted = pd.DataFrame(y proba.round(2))
    actuals = pd.DataFrame(y_test[:5])
    predicted['predicted_label'] = predicted.idxmax(axis=1)
    predicted['actual_label'] = actuals
    predicted
[30]:
                          3
                                   5
                                         6
                                                           predicted_label
       0.0 0.00 0.00 0.00 0.0 0.0 1.00
                                           0.0
                                                0.00 0.0
                                                                        6
    1 0.0 0.01 0.15 0.01 0.0 0.0 0.82 0.0 0.00
                                                                        6
                                                      0.0
    2 0.0 0.00 0.00 0.55 0.0 0.0 0.00 0.0 0.45
                                                     0.0
                                                                        3
    3 1.0 0.00 0.00 0.00 0.0 0.0 0.00 0.0
                                                      0.0
                                                                        0
                                                0.00
    5
       actual_label
    0
                 6
    1
    2
                 3
    3
                 0
[68]: #Creating a dataframe from the output history. Will be displaying a combined
     \rightarrow dataframe later.
    t1 = pd.DataFrame(model1output.history)
    t1 = t1.loc[t1['val_accuracy'][::-1].idxmax()]
```

#### 0.2.2 Model 2

Added an additional 2 hidden layers and modified the number of nodes per layer. All other hyperparameters remain the same.

```
keras.layers.Dense(40,activation="selu", name = 'Layer3',__
      →kernel_initializer='lecun_normal'),
        keras.layers.Dense(30, activation="selu", name = 'Layer4', __
      →kernel initializer='lecun normal'),
        keras.layers.Dense(10, activation="softmax", name = 'OutputLayer')
    ])
    model2.compile(loss="sparse_categorical_crossentropy",
                  optimizer=optimizer,
                  metrics=["accuracy"])
    model2.summary()
    model2output = model2.fit(X_train, y_train, epochs=10, validation_data =_u
     →(X_valid, y_valid), callbacks = [model_cp_save, model_time, model_stop], __
     →batch_size = 32)
    model2time = round(sum(model_time.logs),2)
[65]: y_proba = model2.predict(X_test[:5])
    predicted = pd.DataFrame(y_proba.round(2))
    actuals = pd.DataFrame(y_test[:5])
    predicted['predicted_label'] = predicted.idxmax(axis=1)
    predicted['actual_label'] = actuals
    predicted
[65]:
         0
                    2
                               4
                                    5
                                               7
                                                         9 predicted_label
                                          6
                                                    8
    0 0.0 0.0 0.00 0.0 0.03 0.0 0.97 0.0 0.0 0.0
                                                                         6
    1 0.0 0.0 0.02 0.0 0.00 0.0 0.97
                                             0.0 0.0 0.0
                                                                         6
                                 0.0 0.00
    2 0.0 0.0 0.00 1.0 0.00
                                                                         3
                                            0.0 0.0 0.0
    3 1.0 0.0 0.00 0.0 0.00
                                 0.0 0.00
                                            0.0 0.0 0.0
                                                                         0
    4 0.0 0.0 0.00 0.0 0.00 1.0 0.00 0.0 0.0
                                                                         5
       actual label
    0
    1
                  6
    2
                  3
    3
                  5
[67]: #Creating a dataframe from the output history
    t2 = pd.DataFrame(model2output.history)
    t2 = t2.loc[t2['val_accuracy'][::-1].idxmax()]
```

### 0.2.3 Model 3

Keeping the number of hidden layers the same but adjusting the number of nodes per layer to examine the change.

```
optimizer = keras.optimizers.Adam()
    model3 = keras.models.Sequential([
        keras.layers.Flatten(input_shape = X_train.shape[1:], name = 'InputLayer'),
        keras.layers.Dense(500,activation="selu", name = 'Layer1', u
      →kernel_initializer='lecun_normal'),
        keras.layers.Dense(200,activation="selu", name = 'Layer2',
      →kernel_initializer='lecun_normal'),
        keras.layers.Dense(200,activation="selu", name = 'Layer3', u
      →kernel_initializer='lecun_normal'),
        keras.layers.Dense(50, activation="selu", name = 'Layer4', __
      →kernel_initializer='lecun_normal'),
        keras.layers.Dense(10, activation="softmax", name = 'OutputLayer')
    ])
    model3.compile(loss="sparse_categorical_crossentropy",
                  optimizer=optimizer,
                  metrics=["accuracy"])
    model3.summary()
    model3output = model3.fit(X_train, y_train, epochs=10, validation_data =__
     →(X valid, y valid), callbacks = [model cp save, model time, model stop],
     →batch_size = 32)
    model3time = round(sum(model_time.logs),2)
[69]: X_{new} = X_{test}[:5]
    y_proba = model3.predict(X_new)
    predicted = pd.DataFrame(y_proba.round(2))
    actuals = pd.DataFrame(y_test[:5])
    predicted['predicted_label'] = predicted.idxmax(axis=1)
    predicted['actual_label'] = actuals
    predicted
[69]:
                                                       9 predicted_label
         0
                   2
                         3
                              4
                                   5
                                        6
                                             7
                                                  8
       0.0 \quad 0.0 \quad 0.0 \quad 0.00 \quad 0.0 \quad 0.0 \quad 1.0 \quad 0.0 \quad 0.0
    1 0.0 0.0 0.0 0.00 0.0 0.0 1.0 0.0 0.0
                                                                       6
    2 0.0 0.0 0.0 0.89 0.0 0.0 0.0 0.0 0.1 0.0
                                                                       3
    0
    4 0.0 0.0 0.0 0.00 0.0 1.0 0.0 0.0 0.0
                                                                       5
       actual_label
    0
                  6
    1
                  6
                  3
    2
    3
                  0
                  5
```

```
[70]: #Creating a dataframe from the output history
t3 = pd.DataFrame(model3output.history)
t3 = t3.loc[t3['val_accuracy'][::-1].idxmax()]
```

#### 0.2.4 Model 4

Adding an additional 4 hidden layers to total 1 input layer, 8 hidden layers and 1 output layer. Varying the number of nodes per layer as well. Keeping all other settings the same.

```
[]: model_cp_save = keras.callbacks.ModelCheckpoint(cploc + 'model4.hdf5',u
    →save_best_only=True, monitor='val_accuracy')
   model_stop = keras.callbacks.EarlyStopping(monitor='loss', patience=3)
   model time = TimingCallback()
   optimizer = keras.optimizers.Adam()
   model4 = keras.models.Sequential([
       keras.layers.Flatten(input_shape = X_train.shape[1:], name = 'InputLayer'),
       keras.layers.Dense(600,activation="selu", name = 'Layer1',_
    →kernel_initializer='lecun_normal'),
       keras.layers.Dense(200,activation="selu", name = 'Layer2', u
    →kernel_initializer='lecun_normal'),
       keras.layers.Dense(500,activation="selu", name = 'Layer3',__
    →kernel_initializer='lecun_normal'),
       keras.layers.Dense(300,activation="selu", name = 'Layer4',__
    →kernel_initializer='lecun_normal'),
       keras.layers.Dense(400,activation="selu", name = 'Layer5',_
    →kernel_initializer='lecun_normal'),
       keras.layers.Dense(400,activation="selu", name = 'Layer6',_
    →kernel_initializer='lecun_normal'),
       keras.layers.Dense(100,activation="selu", name = 'Layer7',__
    →kernel_initializer='lecun_normal'),
       keras.layers.Dense(50, activation="selu", name = 'Layer8',
    →kernel_initializer='lecun_normal'),
       keras.layers.Dense(10, activation="softmax", name = 'OutputLayer')
   ])
   model4.compile(loss="sparse_categorical_crossentropy",
                 optimizer=optimizer,
                 metrics=["accuracy"])
   model4.summary()
   model4output = model4.fit(X_train, y_train, epochs=20, validation_data =_u
    →(X_valid, y_valid), callbacks = [model_cp_save, model_time, model_stop],
    →batch_size = 32)
   model4time = round(sum(model_time.logs),2)
```

```
[72]: X_new = X_test[:5]
     y proba = model4.predict(X new)
     predicted = pd.DataFrame(y proba.round(2))
     actuals = pd.DataFrame(y_test[:5])
     predicted['predicted label'] = predicted.idxmax(axis=1)
     predicted['actual_label'] = actuals
     predicted
[72]:
          0
                                          6
               1
                    2
                         3
                              4
                                    5
                                               7
                                                     8
                                                             predicted_label
        0.0
             0.0
                  0.0
                       0.0
                            0.0
                                 0.0
                                       1.00
                                             0.0
                                                  0.00
                                                        0.0
        0.0
             0.0
                  0.0
                       0.0
                            0.0
                                 0.0
                                       0.99
                                                  0.01
                                                                            6
     1
                                             0.0
                                                        0.0
                                                  0.00
     2
        0.0
             0.0
                  0.0
                       1.0
                            0.0
                                 0.0
                                       0.00
                                             0.0
                                                        0.0
                                                                            3
     3 1.0
             0.0
                  0.0
                       0.0
                            0.0
                                 0.0
                                       0.00
                                             0.0
                                                  0.00
                                                        0.0
                                                                            0
        0.0 0.0 0.0 0.0
                            0.0
                                 1.0
                                       0.00
                                                  0.00
                                                                            5
                                            0.0
                                                        0.0
        actual_label
     0
     1
                   6
     2
                   3
     3
                   0
     4
                   5
[75]: #Creating a dataframe from the output history
     t4 = pd.DataFrame(model3output.history)
     t4 = t4.loc[t4['val_accuracy'][::-1].idxmax()]
[75]: loss
                     0.060591
     accuracy
                     0.981605
     val_loss
                     0.147407
     val_accuracy
                     0.968626
     Name: 9, dtype: float64
```

**Evaluating Model Results** Now that I have trained the four models I'll take each model's best epoch and combine them into a dataframe. I'll then decide which model to use to predict my test values.

Based on the output of the model history's best epoch (based on validation accuracy) the best model looks to be Model 3. Both Model 3 and 4 have exactly the same metric values. However, Model 4 is more complex/resource intensive and may result in a risk of overfitting with a greater number of epochs, so I'll be going with Model 3 to provide my predictions

```
[87]: tout = pd.concat([t1,t2,t3,t4], axis=1)
tout.columns = ['Model 1','Model 2','Model 3', 'Model 4']
tout.loc['training_time'] = np.

→array([model1time,model2time,model3time,model4time])
tout.loc['num_epochs'] = [len(model1output.history['loss']),len(model2output.

→history['loss']),len(model3output.history['loss']),len(model4output.

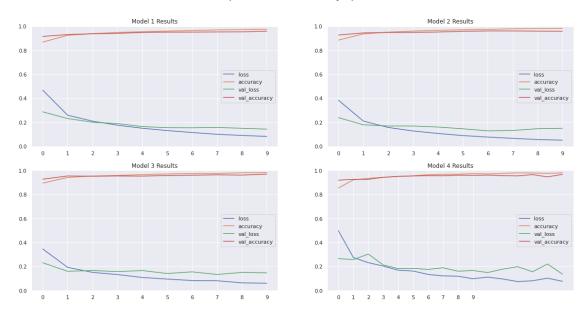
→history['loss'])]
```

```
[87]:
                         Model 1
                                       Model 2
                                                      Model 3
                                                                    Model 4
                                                     0.060591 6.059139e-02
     loss
                        0.082856
                                      0.077477
     accuracy
                                                     0.981605
                                                               9.816055e-01
                        0.974578
                                      0.974165
     val_loss
                        0.143516
                                      0.129277
                                                     0.147407
                                                               1.474069e-01
     val_accuracy
                        0.958953
                                      0.960938
                                                     0.968626
                                                               9.686260e-01
     training_time
                       18.660000
                                     19.460000
                                                    19.650000
                                                               3.581000e+01
    num_epochs
                       10.000000
                                     10.000000
                                                    10.000000
                                                               1.600000e+01
    num_layers
                        4.000000
                                      6.000000
                                                     6.000000
                                                               1.000000e+01
    num params
                    24380.000000 53730.000000 543460.000000
                                                               1.168460e+06
```

Plotting each model's metrics history to further validate the decision for model 3. Model 4 looks to be potentially increasing the loss/decreasing accuracy past epoch #9 - another reason not to use it.

```
[84]: fig, ((ax1, ax2), (ax3, ax4)) = plt.subplots(2, 2, figsize=(20,10))
     fig.suptitle('Sequential MLP Results By Epoch', fontsize = 20)
     ax1.plot(pd.DataFrame(model1output.history))
     ax1.set_title('Model 1 Results')
     ax1.set_ylim(0,1)
     ax1.set_xticks(np.arange(0,10))
     ax1.legend(pd.DataFrame(model1output.history), loc="center right")
     ax2.plot(pd.DataFrame(model2output.history))
     ax2.set title('Model 2 Results')
     ax2.set_ylim(0,1)
     ax2.set_xticks(np.arange(0,10))
     ax2.legend(pd.DataFrame(model1output.history), loc="center right")
     ax3.plot(pd.DataFrame(model3output.history))
     ax3.set_title('Model 3 Results')
     ax3.set_ylim(0,1)
     ax3.set_xticks(np.arange(0,10))
     ax3.legend(pd.DataFrame(model1output.history), loc="center right")
     ax4.plot(pd.DataFrame(model4output.history))
     ax4.set_title('Model 4 Results')
     ax4.set_ylim(0,1)
     ax4.set_xticks(np.arange(0,10))
     ax4.legend(pd.DataFrame(model1output.history), loc="center right")
     plt.show;
```

### Sequential MLP Results By Epoch



**Predicting Test Values w/ Model 3** Now that I've chosen Model 3 I'll be predicting labels using the X\_test data. I'll then take the information and add it to a dataframe so that we can see the probability of each number, as well as the overall predicted value vs the true label.

I chose a mostly random subset of data to show from the dataframe, with the intention of finding one predicted label that was incorrect. Row 215 shows that it was 100% confident it was a 5, but the actual label from the y\_test data was a 9.

Overall, the model does a pretty good job of predicting the values and having a usually high confidence

```
[94]: y_proba = model3.predict(X_test)
     predicted = pd.DataFrame(y_proba.round(2))
     actuals = pd.DataFrame(y_test)
     predicted['predicted_label'] = predicted.idxmax(axis=1)
     predicted['actual_label'] = actuals
     predicted[200:220]
[94]:
                    1
                                                           7
              0
                           2
                                  3
                                        4
                                               5
                                                     6
                                                                8
                                                                       9
     200
          0.00
                 0.00
                       0.00
                              0.00
                                     0.00
                                           0.00
                                                  0.00
                                                         0.0
                                                              1.0
                                                                    0.00
     201
          0.00
                 0.00
                       0.00
                              1.00
                                     0.00
                                            0.00
                                                                    0.00
                                                  0.00
                                                         0.0
                                                              0.0
          0.00
                 0.00
     202
                       0.00
                              0.00
                                     0.00
                                           0.00
                                                  0.00
                                                         0.0
                                                              0.0
                                                                    1.00
     203
          0.00
                 1.00
                       0.00
                              0.00
                                     0.00
                                           0.00
                                                  0.00
                                                              0.0
                                                                    0.00
                                                         0.0
     204
          0.00
                 0.00
                       0.00
                              0.00
                                     0.00
                                           0.00
                                                  1.00
                                                              0.0
                                                                    0.00
                                                         0.0
                 0.00
                       0.00
                              0.00
     205
          0.00
                                     1.00
                                           0.00
                                                  0.00
                                                         0.0
                                                              0.0
                                                                    0.00
          0.00
                 1.00
                       0.00
                              0.00
                                     0.00
     206
                                           0.00
                                                  0.00
                                                         0.0
                                                              0.0
                                                                    0.00
     207
          0.00
                 0.00
                       0.00
                              0.00
                                     0.00
                                           0.00
                                                  0.00
                                                         1.0
                                                              0.0
                                                                    0.00
     208
          0.00
                 0.00
                       0.00
                              0.00
                                     1.00
                                           0.00
                                                  0.00
                                                         0.0
                                                              0.0
                                                                    0.00
     209
          0.00
                 0.00
                       0.00
                              0.00
                                     0.84
                                           0.00
                                                  0.00
                                                         0.0
                                                              0.0
                                                                    0.16
```

210	0.02	0.01	0.14	0.54	0.00	0.05	0.14	0.0	0.1	0.00
211	0.00	0.00	0.00	1.00	0.00	0.00	0.00	0.0	0.0	0.00
212	0.00	0.00	0.00	0.00	0.00	0.00	0.00	1.0	0.0	0.00
213	0.00	0.00	1.00	0.00	0.00	0.00	0.00	0.0	0.0	0.00
214	0.00	0.00	0.00	0.00	0.00	1.00	0.00	0.0	0.0	0.00
215	0.00	0.00	0.00	0.00	0.00	1.00	0.00	0.0	0.0	0.00
216	1.00	0.00	0.00	0.00	0.00	0.00	0.00	0.0	0.0	0.00
217	0.00	1.00	0.00	0.00	0.00	0.00	0.00	0.0	0.0	0.00
218	0.00	0.00	0.00	0.00	0.00	1.00	0.00	0.0	0.0	0.00
219	0.00	1.00	0.00	0.00	0.00	0.00	0.00	0.0	0.0	0.00

	<pre>predicted_label</pre>	actual_label
200	8	8
201	3	3
202	9	9
203	1	1
204	6	6
205	4	4
206	1	1
207	7	7
208	4	4
209	4	4
210	3	3
211	3	3
212	7	7
213	2	2
214	5	5
215	5	9
216	0	0
217	1	1
218	5	5
219	1	1