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DEPARTMENT OF COMPUTER SCIENCE

Sub : Mathematics

Remark

Demonstrator's

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BCS

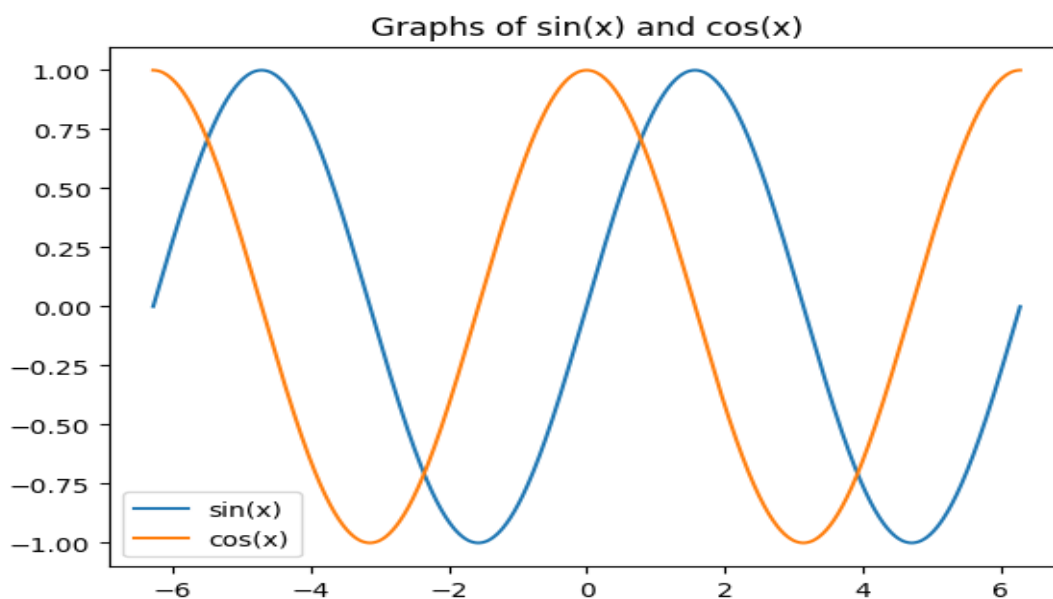
**Q1. Attempt any TWO of the following**

**A ) Write a python program to plot 2D graph of the function  $f(x)=\sin x$  and  $g(x)=\cos x$  in  $[-2\pi, 2\pi]$**

**->**

```
import numpy as np
import matplotlib.pyplot as plt
def f(x):
    return np.sin(x)
def g(x):
    return np.cos(x)
```

```
x = np.linspace(-2*np.pi, 2*np.pi, 1000)
plt.plot(x, f(x), label='sin(x)')
plt.plot(x, g(x), label='cos(x)')
plt.legend()
plt.title('Graphs of sin(x) and cos(x)')
plt.show()
```



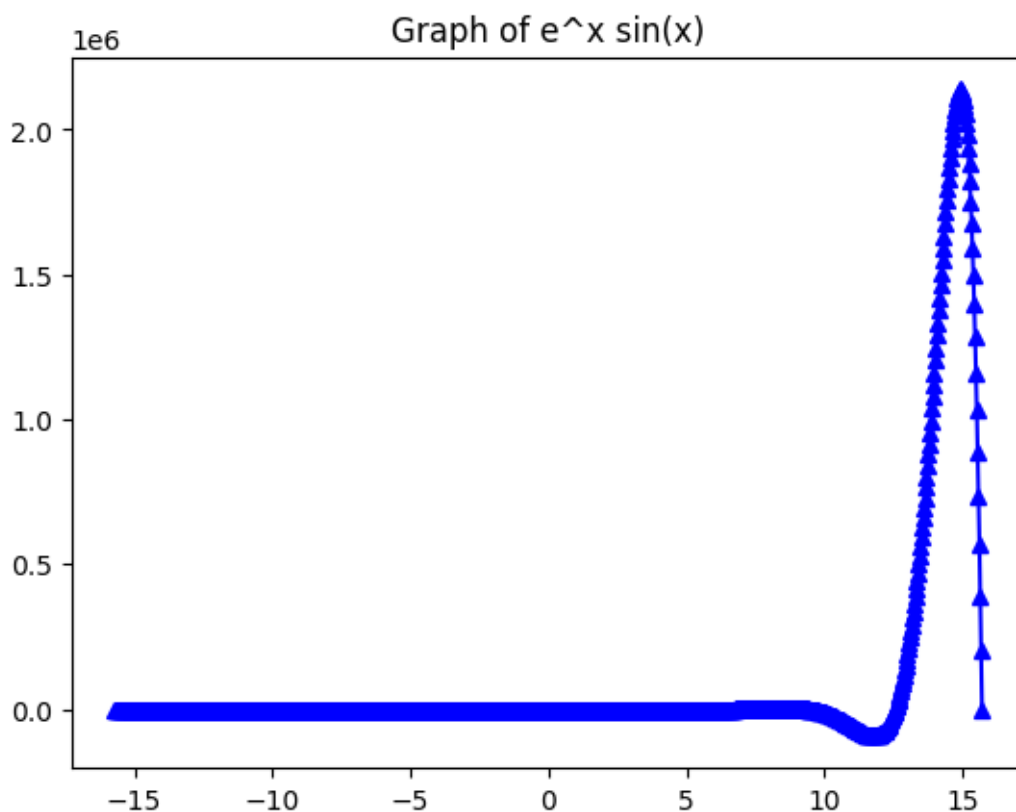
**B ) Write a python program to plot the 2D graph of the function  $f(x)=e^x \sin x$  in  $[-5\pi, 5\pi]$  with blue points line with upward pointing triangle**

**->**

```
import numpy as np
import matplotlib.pyplot as plt
def f(x):
    return np.exp(x) * np.sin(x)

x = np.linspace(-5*np.pi, 5*np.pi, 1000)

y = f(x)
plt.plot(x, y, 'b^-')
plt.title('Graph of e^x sin(x)')
plt.show()
```



**C )Write a python program to plot the 3D graph of the function  $f(x)=\sin(x^2+y^2)$   $-6 < x, y < 6$**

**->**

```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits import mplot3d
def f(x, y):
```

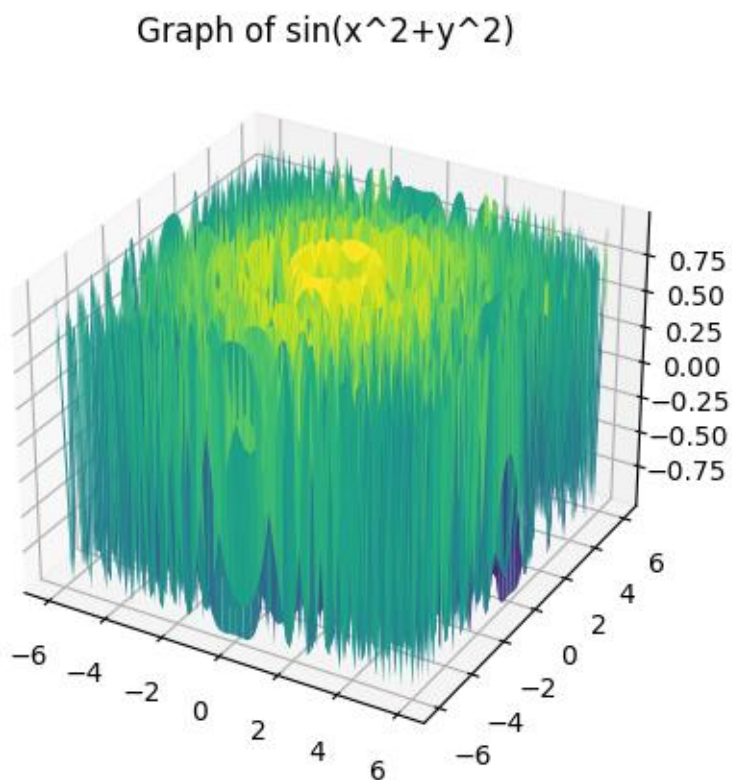
```

return np.sin(x**2+y**2)

x = np.linspace(-6, 6, 100)
y = np.linspace(-6, 6, 100)
X, Y = np.meshgrid(x, y)
Z = f(X, Y)

fig = plt.figure()
ax = plt.axes(projection='3d')
ax.plot_surface(X, Y, Z, cmap='viridis')
ax.set_title('Graph of sin(x^2+y^2)')
plt.show()

```



**Q2 ) Attempt any TWO of the following**

**A ) Write a python program to reflect the line segment joining the points A[-5,2],B[3,-4] through the line  $y=2x-1$**

**->**

```

import numpy as np
import matplotlib.pyplot as plt
def given_line(x):
    return 2*x - 1

```

```

A = np.array([-5, 2])
B = np.array([3, -4])

m = 2
c = -1

x = np.linspace(-10, 10, 100)
plt.plot(x, given_line(x), 'b-', label='Given Line')
plt.plot([A[0], B[0]], [A[1], B[1]], 'r-', label='Line Segment')

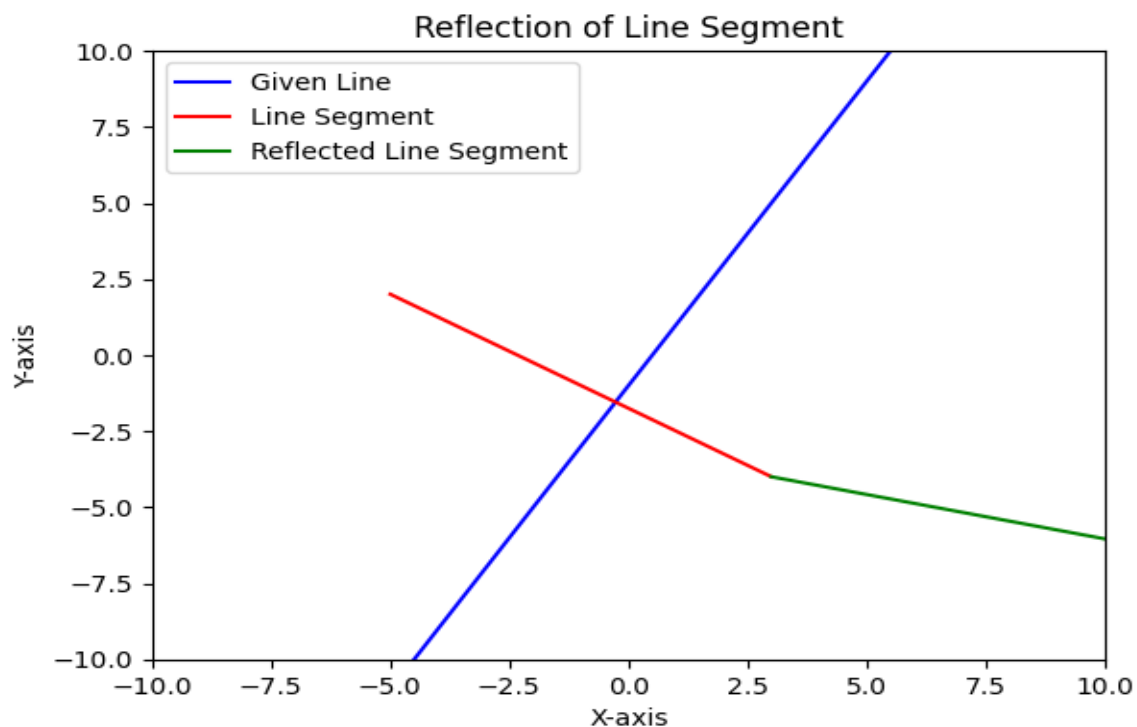
v = np.array([B[0]-A[0], B[1]-A[1]])
w = np.array([m, -1])
projection = (np.dot(v, w) / np.dot(w, w)) * w
reflection = 2*projection - v
C = B + reflection

plt.plot([B[0], C[0]], [B[1], C[1]], 'g-', label='Reflected Line Segment')
plt.legend()

plt.xlim(-10, 10)
plt.ylim(-10, 10)

plt.xlabel('X-axis')
plt.ylabel('Y-axis')
plt.title('Reflection of Line Segment')
plt.show()

```



**B ) Write a python program to find the area and perimeter of a polygon with vertices (0,0),(-2,0),(5,5),(1,-3)**

->

```
from shapely.geometry import Polygon
```

```
vertices = [(0, 0), (-2, 0), (5, 5), (1, -3)]
```

```
polygon = Polygon(vertices)
```

```
area = polygon.area
```

```
perimeter = polygon.length
```

```
print(f"Area: {area:.2f}")
```

```
print(f"Perimeter: {perimeter:.2f}")
```

output :

Area: 15.00

Perimeter: 22.71

**C )Write a python program to plot the 3D graph of the function  $f(x,y)=\sin x + \cos y$  , $x,y \in [-2\pi, 2\pi]$  using wireframe plot**

->

```
import numpy as np
```

```
import matplotlib.pyplot as plt
```

```
from mpl_toolkits.mplot3d import axes3d
```

```
def f(x, y):
```

```
    return np.sin(x) + np.cos(y)
```

```
x = np.linspace(-2*np.pi, 2*np.pi, 100)
```

```
y = np.linspace(-2*np.pi, 2*np.pi, 100)
```

```
X, Y = np.meshgrid(x, y)
```

```
Z = f(X, Y)
```

```
fig = plt.figure()
```

```
ax = fig.add_subplot(111, projection='3d')
```

```
ax.plot_wireframe(X, Y, Z)
```

```
ax.set_xlabel('X')
```

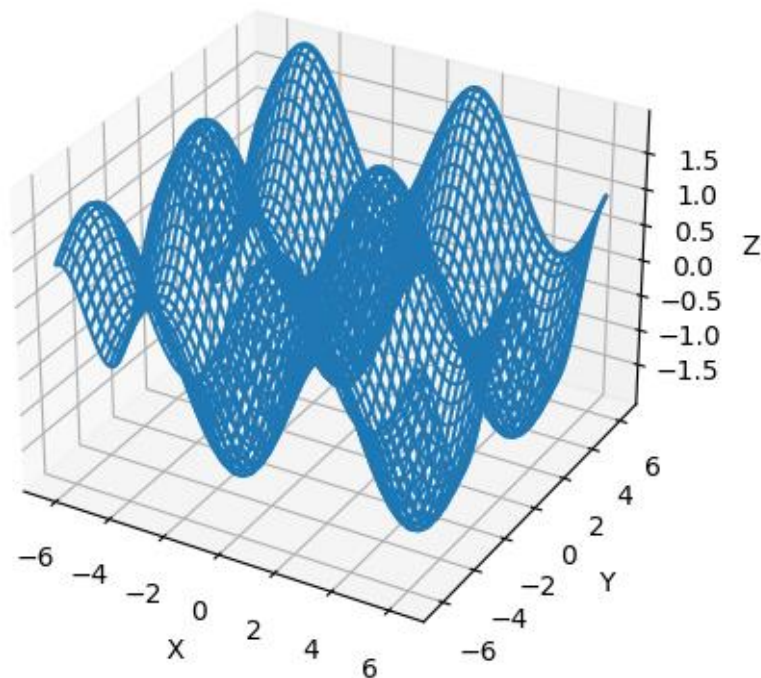
```
ax.set_ylabel('Y')
```

```
ax.set_zlabel('Z')
```

```
ax.set_title('Wireframe Plot of  $f(x,y) = \sin(x) + \cos(y)$ ')
```

```
plt.show()
```

Wireframe Plot of  $f(x,y) = \sin(x) + \cos(y)$



**Q3 ) Attempt the following**

**A ) Attempt any ONE of the following**

**I ) Write a python program to solve the following LPP :**

**Max      $Z=x+y$   
Subject to  $x-y \geq 1$   
            $x+y \geq 2$   
            $x,y \geq 0$**

**->**

```
import numpy as np
from scipy.optimize import linprog
c = np.array([1, 1])
A = np.array([[ -1, 1], [ 1, 1]])
b = np.array([1, 2])
bounds = [(0, None), (0, None)]
res = linprog(-c, A_ub=A, b_ub=b, bounds=bounds)

print(f"Optimal value of Z: {-res.fun:.2f}")
print(f"x: {res.x[0]:.2f}")
print(f"y: {res.x[1]:.2f}")
```

output :

Optimal value of Z: 2.00  
x: 2.00  
y: 0.00

**II ) Write a python program to solve the following LPP :**

**Min  $Z=3.5x + 2y$**   
**Subject to  $x-y \geq 5$**   
 **$x \geq 4$**   
 **$y \leq 2$**   
 **$x, y \geq 0$**

**->**

```
import numpy as np
from scipy.optimize import linprog
c = np.array([3.5, 2])
A = np.array([[ -1, 1], [ 1, 0], [ 0, -1]])
b = np.array([5, 4, -2])
bounds = [(4, None), (None, 2)]
res = linprog(c, A_ub=A, b_ub=b, bounds=bounds)

print(f"Optimal value of Z: {res.fun:.2f}")
print(f"x: {res.x[0]:.2f}")
print(f"y: {res.x[1]:.2f}")
```

output :

Optimal value of Z: 18.00  
x: 4.00  
y: 2.00

**B ) Attempt any ONE of the following**

**I ) Apply the following transformation on the point P[3,-2]**

- A ) Scaling in Y direction by 4 units**
- B ) Reflection through Y axis**
- C ) Rotation about origin by an angle  $45^\circ$**
- D ) Reflection through the line  $y=x$**

->

```
import numpy as np
P = np.array([3, -2])
```

```
A = np.array([[1, 0], [0, 4]])
P_A = A.dot(P)
print("After scaling in Y direction by 4 units:", P_A)
```

```
B = np.array([[-1, 0], [0, 1]])
P_B = B.dot(P)
print("After reflection through Y axis:", P_B)
```

```
theta = np.deg2rad(45)
C = np.array([[np.cos(theta), -np.sin(theta)], [np.sin(theta), np.cos(theta)]])
P_C = C.dot(P)
print("After rotation about origin by 45 degrees:", P_C)
```

```
D = np.array([[0, 1], [1, 0]])
P_D = D.dot(P)
print("After reflection through the line y=x:", P_D)
```

output :

After scaling in Y direction by 4 units: [ 3 -8]  
After reflection through Y axis: [-3 -2]  
After rotation about origin by 45 degrees: [3.53553391 0.70710678]  
After reflection through the line y=x: [-2 3]

**II ) Apply the following transformation on the point P[3,-2]**

**A ) Shering in x direction by -2 units**

**B ) Scaling in x and y direction by -3 and 2 units respectively**

**C ) reflection through x axis**

**D ) Reflection through the line  $y=-x$**

->

```
import numpy as np
P = np.array([3, -2])
```

```
A = np.array([[1, -2], [0, 1]])
P_A = A.dot(P)
print("After shering in x direction by -2 units:", P_A)
```



```
B = np.array([[ -3, 0], [0, 2]])
P_B = B.dot(P)
print("After scaling in x and y direction by -3 and 2 units respectively:", P_B)
```

```
C = np.array([[1, 0], [0, -1]])
P_C = C.dot(P)
print("After reflection through x axis:", P_C)
```

```
D = np.array([[0, -1], [-1, 0]])
P_D = D.dot(P)
print("After reflection through the line  $y=-x$ :", P_D)
```

output :

```
After shering in x direction by -2 units: [ 7 -2]
After scaling in x and y direction by -3 and 2 units respectively: [-9 -4]
After reflection through x axis: [3 2]
After reflection through the line  $y=-x$ : [ 2 -3]
```