

Sahakar Maharshi Bhausaheb Santuji Thorat

College Sangamner

DEPARTMENT OF COMPUTER SCIENCE

Sub : Mathematics

Remark

Demonstrator's

Signature

Date:- / /20

Name:- Gorde Yash Somnath

Roll.No:- 21

Date:-

Title of the expt:- Slip no 18

Page.no:-

Class:-

BCS

Q1) Attempt any TWO of the following

A) Write a python program to draw polygon with vertices [3,3],[4,6],[2,5],[2,2] and its translation in X and Y direction using the factors 3,5 respectively

->

```
import matplotlib.pyplot as plt
```

```
import numpy as np
```

```
vertices = np.array([[3, 3], [4, 6], [2, 5], [2, 2]])
```

```
tx = 3
```

```
ty = 5
```

```
fig, axs = plt.subplots(1, 2)
```

```
axs[0].plot(vertices[:, 0], vertices[:, 1])
```

```
axs[0].set_title('Original Polygon')
```

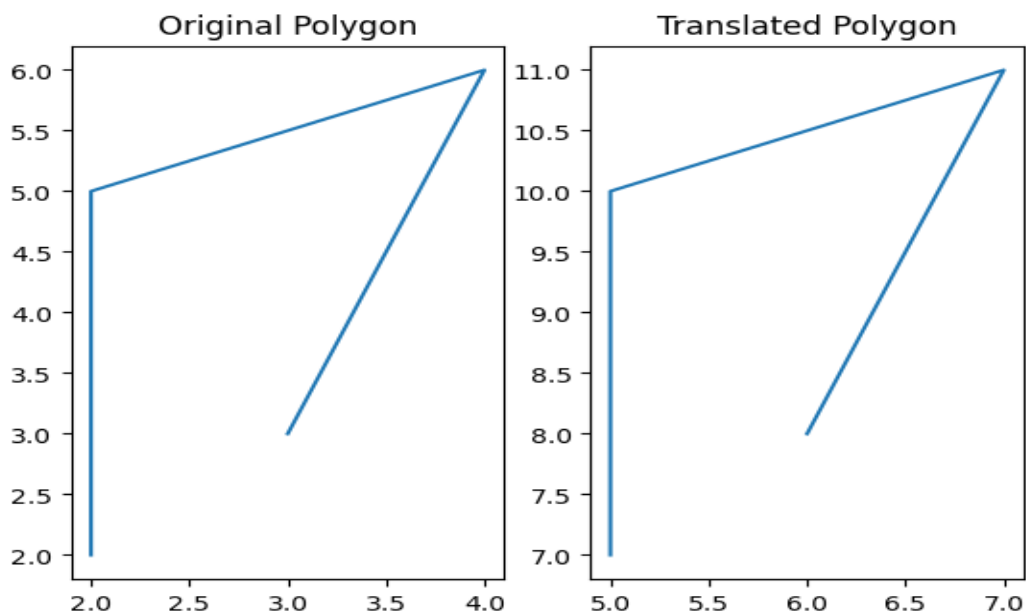
```
translation_matrix = np.array([[1, 0, tx], [0, 1, ty], [0, 0, 1]])
```

```
translated_vertices = np.dot(translation_matrix, np.hstack((vertices, np.ones((len(vertices), 1)))).T).T[:, :-1]
```

```
axs[1].plot(translated_vertices[:, 0], translated_vertices[:, 1])
```

```
axs[1].set_title('Translated Polygon')
```

```
plt.show()
```



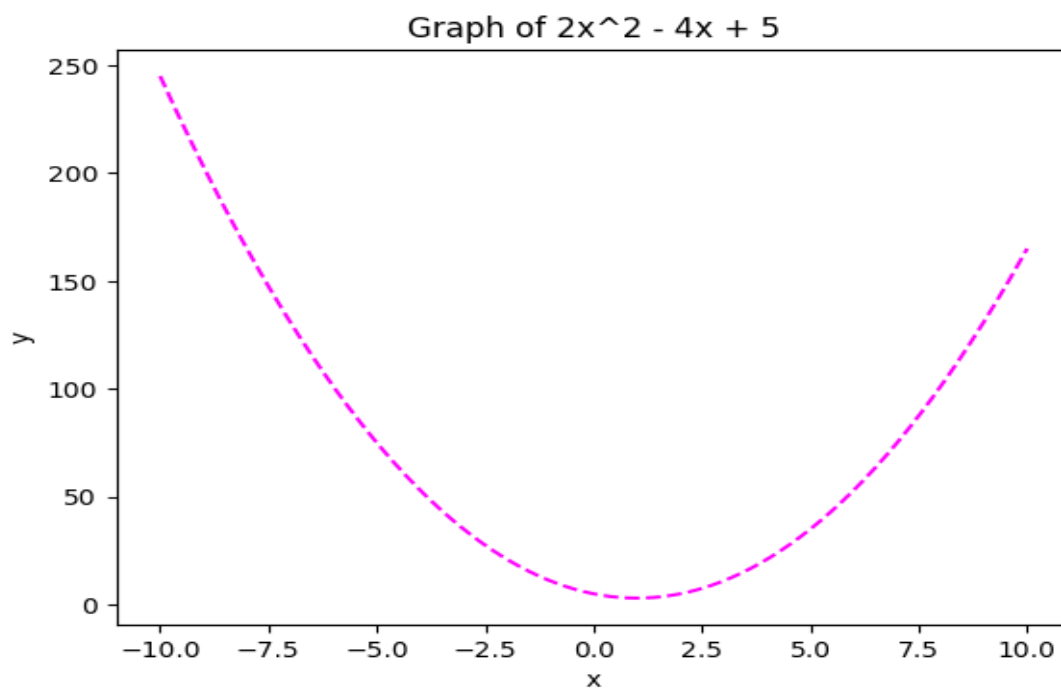
B) Write a python program to plot the graph $2x^2-4x+5$ in $[-10,10]$ in magenta colored dashed pattern

->

```
import matplotlib.pyplot as plt
import numpy as np
def f(x):
    return 2*x**2 - 4*x + 5
```

```
x = np.linspace(-10, 10, 1000)
y = f(x)
```

```
plt.plot(x, y, color='magenta', linestyle='--')
plt.xlabel('x')
plt.ylabel('y')
plt.title('Graph of  $2x^2 - 4x + 5$ ')
plt.show()
```



C) Write a python program to generate 3D plot of the function $z=x^2+y^2$ in $-5<x,y<5$

->

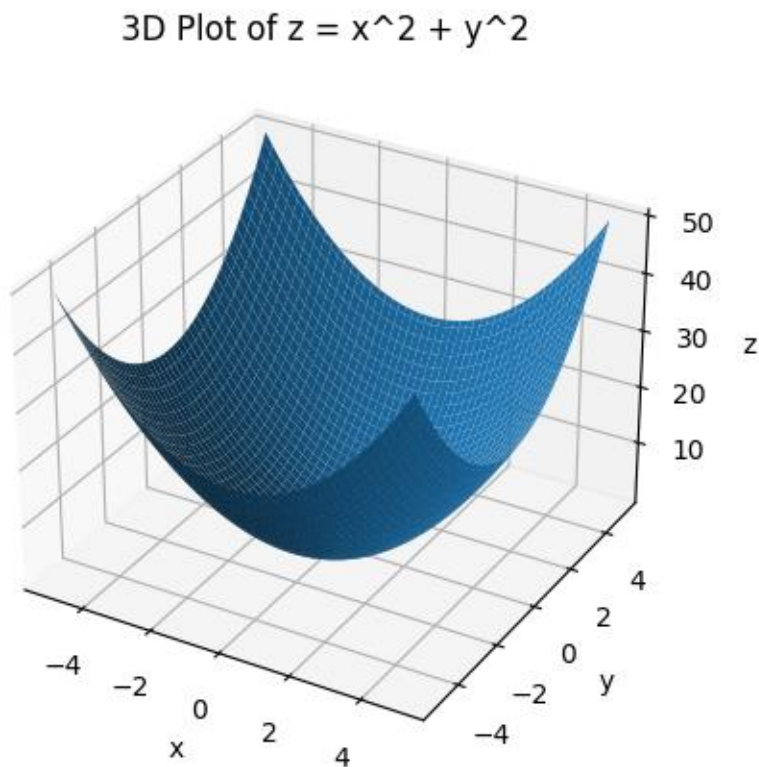
```
import matplotlib.pyplot as plt
from mpl_toolkits import mplot3d
import numpy as np
def f(x, y):
    return x**2 + y**2
```

```
x = np.linspace(-5, 5, 100)
y = np.linspace(-5, 5, 100)
X, Y = np.meshgrid(x, y)
Z = f(X, Y)
```

```

fig = plt.figure()
ax = fig.add_subplot(111, projection='3d')
ax.plot_surface(X, Y, Z)
ax.set_xlabel('x')
ax.set_ylabel('y')
ax.set_zlabel('z')
ax.set_title('3D Plot of  $z = x^2 + y^2$ ')
plt.show()

```



Q2) Attempt any TWO of the following

A) Write a python program to generate vector x in the interval [-22,22] using numpy package with 80 subintervals

->

```

import numpy as np
n = 80
x = np.linspace(-22, 22, n+1)
print(x)

```

outuput :

```

[-22.  -21.45 -20.9  -20.35 -19.8  -19.25 -18.7  -18.15 -17.6  -17.05
 -16.5  -15.95 -15.4  -14.85 -14.3  -13.75 -13.2  -12.65 -12.1  -11.55
 -11.   -10.45 -9.9   -9.35  -8.8   -8.25  -7.7   -7.15  -6.6   -6.05
 -5.5   -4.95  -4.4   -3.85  -3.3   -2.75  -2.2   -1.65  -1.1   -0.55]

```

```

0.  0.55  1.1  1.65  2.2  2.75  3.3  3.85  4.4  4.95
5.5  6.05  6.6  7.15  7.7  8.25  8.8  9.35  9.9  10.45
11. 11.55 12.1  12.65 13.2  13.75 14.3  14.85 15.4  15.95
16.5 17.05 17.6  18.15 18.7  19.25 19.8  20.35 20.9  21.45
22. ]

```

B) Write a python program to rotate the triangle ABC by 90 degree where A[1,2],B[2,-2] and C[-1,2]

->

```

import numpy as np
A = np.array([1, 2])
B = np.array([2, -2])
C = np.array([-1, 2])
theta = np.pi/2
rot_mat = np.array([[np.cos(theta), -np.sin(theta)],
                    [np.sin(theta), np.cos(theta)]])

A_rot = np.dot(rot_mat, A)
B_rot = np.dot(rot_mat, B)
C_rot = np.dot(rot_mat, C)

print("Rotated triangle:")
print("A':", A_rot)
print("B':", B_rot)
print("C':", C_rot)

```

output :

```

Rotated triangle:
A': [-2.  1.]
B': [2.  2.]
C': [-2. -1.]

```

C) Write a python program to plot the rectangle with vertices at [2,1],[2,4],[5,4],[5,1] and its uniform expansion by factor 4

->

```

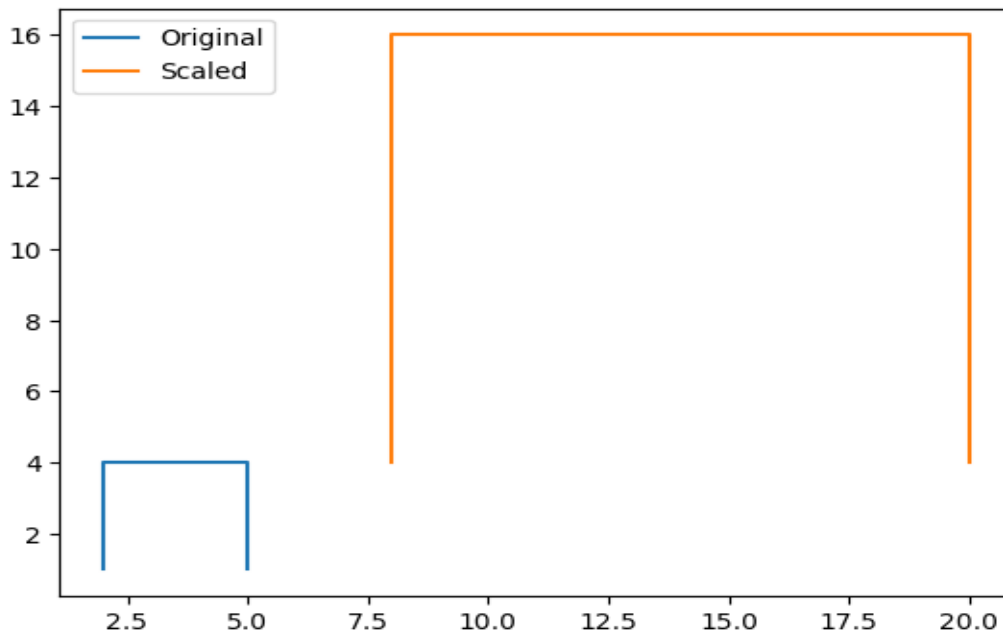
import matplotlib.pyplot as plt
import numpy as np
rectangle = np.array([[2, 1], [2, 4], [5, 4], [5, 1]])
scale_factor = 4
scale_mat = np.array([[scale_factor, 0],
                    [0, scale_factor]])
rectangle_scaled = np.dot(scale_mat, rectangle.T).T

```

```

fig, ax = plt.subplots()
ax.plot(rectangle[:, 0], rectangle[:, 1], label='Original')
ax.plot(rectangle_scaled[:, 0], rectangle_scaled[:, 1], label='Scaled')
ax.legend()
plt.show()

```



Q3) Attempt the following

A) Attempt any ONE of the following

I) Write a python program to solve the following LPP :

Min $Z=x+y$
Subject to $x \geq 6$
 $y \geq 6$
 $x+y \leq 11$
 $x, y \geq 0$

->

```

from scipy.optimize import linprog
c = [1, 1]
A = [[-1, 0], [0, -1], [1, 1]]
b = [-6, -6, 11]

```

```

x_bounds = (0, None)
y_bounds = (0, None)
res = linprog(c=c, A_ub=A, b_ub=b, bounds=[x_bounds, y_bounds])

```

if res.success:

Print the results

```

print('Optimal value:', res.fun)
print('x:', res.x[0])
print('y:', res.x[1])
else:
    print('No solution found.')

```

output :

No solution found.

II) Write a python program to solve the following LPP

Max $Z=2x+3y$
Subject to $5x-y \geq 0$
 $X+y \geq 6$
 $X,y \geq 0$

->

```

from scipy.optimize import linprog
c = [-2, -3]
A = [[5, -1], [-1, 1]]
b = [0, 6]
x_bounds = (0, None)
y_bounds = (0, None)
res = linprog(c=c, A_ub=A, b_ub=b, bounds=[x_bounds, y_bounds])

print('Optimal value:', -res.fun)
print('x:', res.x[0])
print('y:', res.x[1])

```

output :

Optimal value: 25.5
x: 1.5
y: 7.5

B) Attempt any ONE of the following

I) Write a python program to find the combined transformation of the line segment between the points A[3,2] and B[2,-3] for the following sequence of transformation

A) First rotation about origin through an angle $\pi/6$

B) Followed by scaling in y coordination by 4 units respectively

C) Followed by reflection through the origin

->

```
import numpy as np
```

```
A = np.array([3, 2])
```

```
B = np.array([2, -3])
```

```
theta = np.pi/6
```

```
R = np.array([[np.cos(theta), -np.sin(theta)], [np.sin(theta), np.cos(theta)]])
```

```
S = np.array([[1, 0], [0, 4]])
```

```
F = np.array([[-1, 0], [0, -1]])
```

```
T = F @ S @ R
```

```
A_transformed = T @ A
```

```
B_transformed = T @ B
```

```
print(f"A': {A_transformed}")
```

```
print(f"B': {B_transformed}")
```

output :

```
A': [-1.59807621 -12.92820323]
```

```
B': [-3.23205081  6.39230485]
```

II) Apply each of the following transformation on the point P[3,-1]

A) Reflection through Y-axis

B) Scaling in X and Y direction by $\frac{1}{2}$ and 3 units respectively

C) Shearing in both X and Y direction by -2 and 4 units respectively

D) Rotation about origin by an angle 60 degrees

->

```
import numpy as np
```

```
P = np.array([3, -1])
```

```
F = np.array([[-1, 0], [0, 1]])
```

```
P_transformed = F @ P
```

```
print("After Reflection through Y-axis: ", P_transformed)
```

```
S = np.array([[0.5, 0], [0, 3]])
```

```
P_transformed = S @ P
```

```
print("After Scaling in X and Y direction by  $\frac{1}{2}$  and 3 units respectively: ",  
P_transformed)
```

```
H = np.array([[1, -2], [4, 1]])
P_transformed = H @ P
print("After Shearing in both X and Y direction by -2 and 4 units respectively: ",
P_transformed)
```

```
theta = np.pi/3 # 60 degrees in radians
R = np.array([[np.cos(theta), -np.sin(theta)], [np.sin(theta), np.cos(theta)]])
P_transformed = R @ P
```

```
print("After Rotation about origin by an angle 60 degrees: ", P_transformed)
```

output :

After Reflection through Y-axis: [-3 -1]

After Scaling in X and Y direction by $\frac{1}{2}$ and 3 units respectively: [1.5 -3.]

After Shearing in both X and Y direction by -2 and 4 units respectively: [5 11]

After Rotation about origin by an angle 60 degrees: [2.3660254 2.09807621]