

Sahakar Maharshi Bhausaheb Santuji Thorat

College Sangamner

DEPARTMENT OF COMPUTER SCIENCE

Sub : Mathematics

Remark

Demonstrator's

Signature

Date:- / /20

Name:- Gorde Yash Somnath

Roll.No:- 21

Date:-

Title of the expt:- Slip no 13

Page.no:-

Class:-

BCS

### Q1. Attempt any two of the following

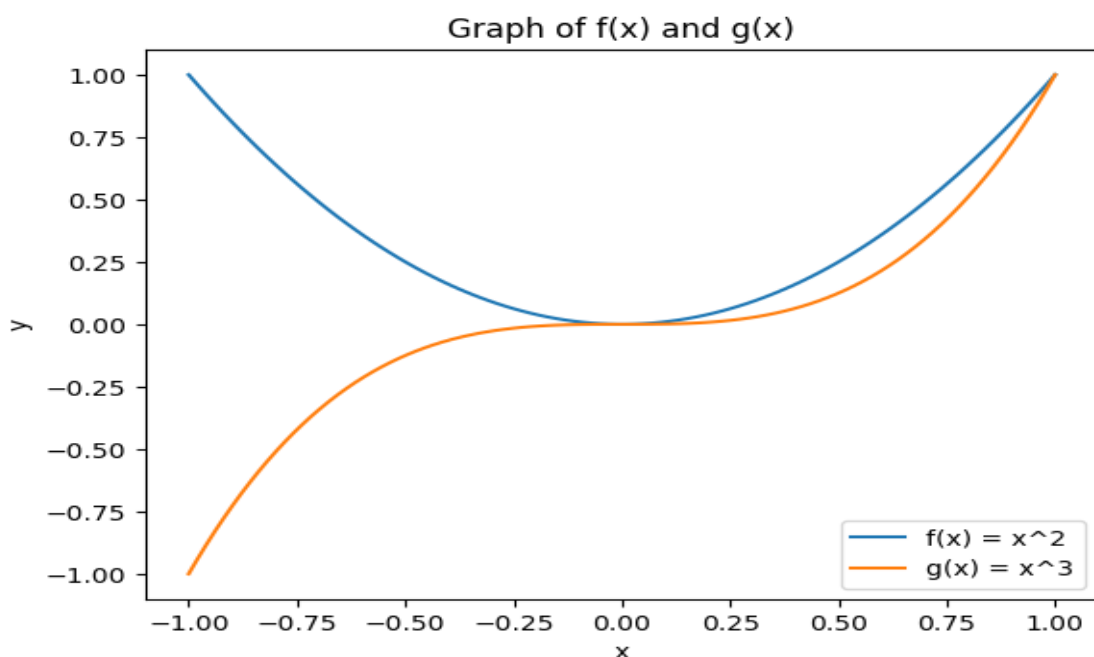
A ) Write a python program to plot 2D graph of the function  $f(x)=x^2$  and  $g(x)=x^3$  in  $[-1,1]$

->

```
import matplotlib.pyplot as plt
import numpy as np
```

```
# Define the x values
x = np.linspace(-1, 1, 100)
```

```
# Define the functions
f = x**2
g = x**3
plt.plot(x, f, label='f(x) = x^2')
plt.plot(x, g, label='g(x) = x^3')
plt.xlabel('x')
plt.ylabel('y')
plt.title('Graph of f(x) and g(x)')
plt.legend()
plt.show()
```

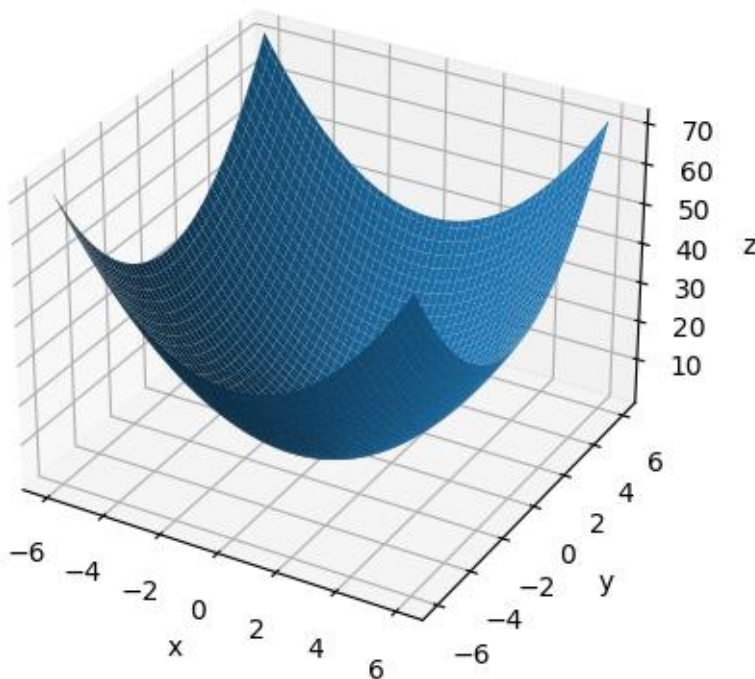


**B ) Using Python plot the surface plot of parabola  $z=x^2+y^2$  in  $-6 < x, y < 6$**

**->**

```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D
x = np.linspace(-6, 6, 100)
y = np.linspace(-6, 6, 100)
X, Y = np.meshgrid(x, y)
Z = X**2 + Y**2
```

```
fig = plt.figure()
ax = fig.add_subplot(111, projection='3d')
ax.plot_surface(X, Y, Z)
ax.set_xlabel('x')
ax.set_ylabel('y')
ax.set_zlabel('z')
plt.show()
```



**C ) Write a python program to plot the 3D line graph whose parametric equation is  $(\cos(2x), \sin(2x), x)$  for  $10 \leq x \leq 20$  (in red color) with title to the graph**

**->**

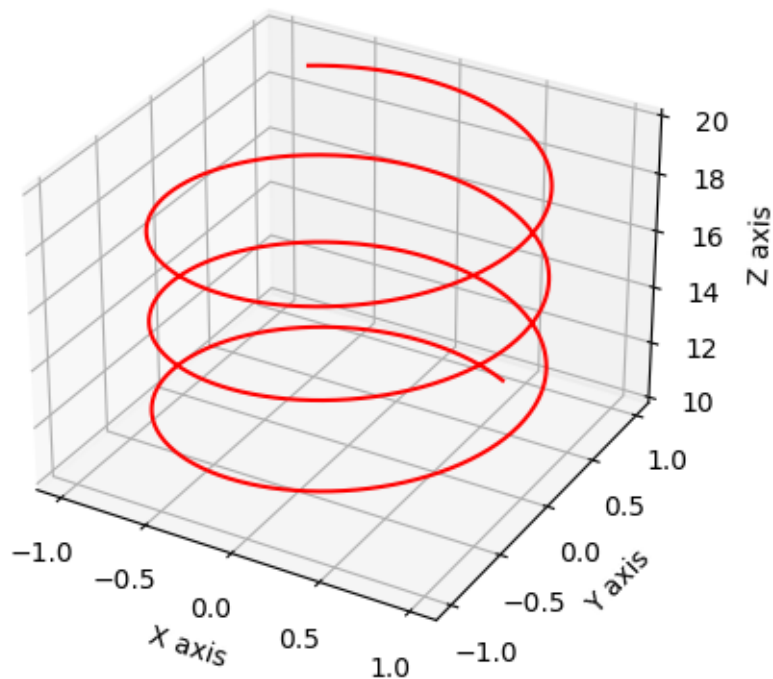
```
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D
x = np.linspace(10, 20, 1000)
y = np.cos(2*x)
z = np.sin(2*x)
w = x
```

```

fig = plt.figure()
ax = fig.add_subplot(111, projection='3d')
ax.plot(y, z, w, color='red')
ax.set_xlabel('X axis')
ax.set_ylabel('Y axis')
ax.set_zlabel('Z axis')
plt.title('3D line graph of (cos(2x), sin(2x), x)')
plt.show()

```

3D line graph of  $(\cos(2x), \sin(2x), x)$



**Q2 ) Attempt any TWO of the following**

**A ) Write a python program to reflect the  $\triangle ABC$  through the line  $y=3$  where  $A(1,0), B(2,-1), C(-1,3)$**

**->**

```

import numpy as np
import matplotlib.pyplot as plt
A = np.array([1, 0])
B = np.array([2, -1])
C = np.array([-1, 3])
x = np.linspace(-5, 5, 100)
y = np.full_like(x, 3)

plt.plot(A[0], A[1], 'o', label='A')
plt.plot(B[0], B[1], 'o', label='B')
plt.plot(C[0], C[1], 'o', label='C')
plt.plot(x, y, label='y=3')

```

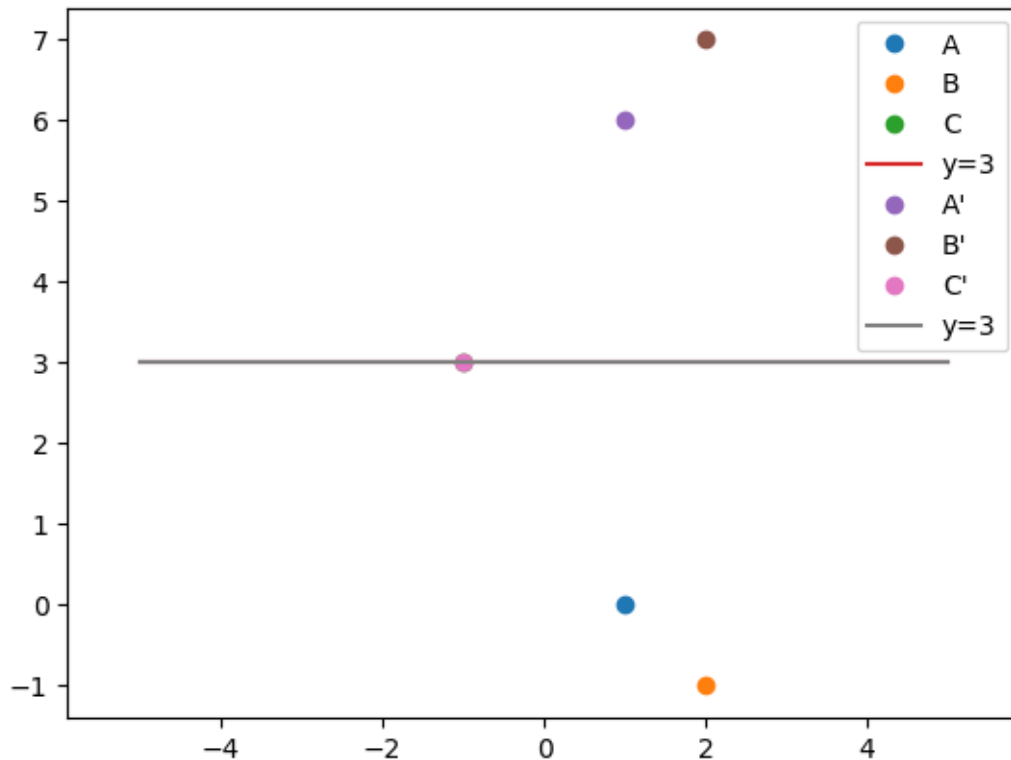
```

plt.axis('equal')
plt.grid()
plt.legend()

# Reflect the coordinates of the triangle across the line y=3
A_reflect = np.array([A[0], 2*3 - A[1]])
B_reflect = np.array([B[0], 2*3 - B[1]])
C_reflect = np.array([C[0], 2*3 - C[1]])

plt.plot(A_reflect[0], A_reflect[1], 'o', label='A\'')
plt.plot(B_reflect[0], B_reflect[1], 'o', label='B\'')
plt.plot(C_reflect[0], C_reflect[1], 'o', label='C\'')
plt.plot(x, y, label='y=3')
plt.axis('equal')
plt.grid()
plt.legend()
plt.show()

```



**B ) Find the area and perimeter of the  $\triangle ABC$  where  $A[0,0], B[5,0], C[3,3]$**

**->**

```

import numpy as np
A = np.array([0, 0])
B = np.array([5, 0])
C = np.array([3, 3])

```

```

dist_AB = np.linalg.norm(B - A)

```

```

dist_BC = np.linalg.norm(C - B)
dist_CA = np.linalg.norm(A - C)

perimeter = dist_AB + dist_BC + dist_CA
area = 0.5 * abs((A[0]*B[1] + B[0]*C[1] + C[0]*A[1]) - (A[1]*B[0] + B[1]*C[0] + C[1]*A[0]))
print("Perimeter =", perimeter)
print("Area =", area)

```

Output :

```

Perimeter = 12.848191962583275
Area = 7.5

```

**C ) Using sympy declare the points P(5,2),Q(5,-2),R(5,0) ,check whether these points are colliner.Declare the ray passing through the points P and Q , find the length of this ray between P and Q, Also find slop of this ray  
->**

```

from sympy import Point, Segment, Line
P = Point(5, 2)
Q = Point(5, -2)
R = Point(5, 0)
area = abs((Q.x - P.x)*(R.y - P.y) - (R.x - P.x)*(Q.y - P.y))/2
if area < 1e-6:
    print("The points are collinear")
else:
    print("The points are not collinear")

ray_PQ = Segment(P, Q).direction
length_PQ = Segment(P, Q).length
slope_PQ = Line(P, Q).slope

print("Length of ray PQ:", length_PQ)
print("Slope of ray PQ:", slope_PQ)

```

output :

```

The points are collinear
Length of ray PQ: 4
Slope of ray PQ: oo

```

**Q3 ) Attempt the following**

**A ) Attempt any ONE of the following**

**I ) Write a python program to solve the following LPP :**

$$\begin{array}{ll}\text{Max } Z=5x+3y \\ \text{Subject to } X+Y \leq 7 \\ \quad \quad \quad 2x+5y \leq 1 \\ \quad \quad \quad X, y \geq 0\end{array}$$

**->**

```
import numpy as np
from scipy.optimize import linprog
c = np.array([5, 3])
A = np.array([[1, 1], [2, 5]])
b = np.array([7, 1])
x_bounds = (0, None)
y_bounds = (0, None)
result = linprog(c, A_ub=A, b_ub=b, bounds=[x_bounds, y_bounds],
method='simplex')

print("Status:", result.message)
print("x =", result.x[0])
print("y =", result.x[1])
print("Optimal value of Z =", result.fun)
```

**output :**

```
Status: Optimization terminated successfully.
x = 0.0
y = 0.0
Optimal value of Z = 0.0
```

**II ) write a python program to display the following LPP by using pulp module and simplex method. Find its optimal solution if exist**

**Max  $Z=3x+2y+5z$   
Subject to  $x+2y+z \leq 430$   
 $3x+4z \leq 460$   
 $x+4y \leq 120$   
 $x,y,z \geq 0$**

**->**

```
from pulp import *
prob = LpProblem("LPP", LpMaximize)
x = LpVariable("x", lowBound=0)
y = LpVariable("y", lowBound=0)
z = LpVariable("z", lowBound=0)

prob += 3*x + 2*y + 5*z
prob += x + 2*y + z <= 430
prob += 3*x + 4*z <= 460
prob += x + 4*y <= 120
prob.solve()

print("Status:", LpStatus[prob.status])
print("x =", value(x))
print("y =", value(y))
print("z =", value(z))
print("Optimal value of Z =", value(prob.objective))
```

**B ) Attempt any ONE of the following**

**I ) Write a python program to apply the following transformation on the point (-2,4) :**

**A ) Shering in Y direction by 7 units**

**B ) Scaling in X and Y direction by  $\frac{7}{2}$  and 7 units respectively**

**C ) Shering in X and Y direction by 4 and 7 units respectively**

**D ) Rotation about origin by an angle  $60^\circ$**

**->**

```
import numpy as np
p = np.array([-2, 4, 1]).T
T_A = np.array([[1, 0, 0], [7, 1, 0], [0, 0, 1]])
T_B = np.array([[7/2, 0, 0], [0, 7, 0], [0, 0, 1]])
T_C = np.array([[1, 4, 0], [7, 1, 0], [0, 0, 1]])
theta = np.radians(60)
```

```
T_D = np.array([[np.cos(theta), -np.sin(theta), 0], [np.sin(theta), np.cos(theta), 0], [0, 0, 1]])
```

```
p_A = np.dot(T_A, p)
p_B = np.dot(T_B, p)
p_C = np.dot(T_C, p)
p_D = np.dot(T_D, p)
```

```
print("A) Shearing in Y direction by 7 units:", p_A)
print("B) Scaling in X and Y direction by 7/2 and 7 units respectively:", p_B)
print("C) Shearing in X and Y direction by 4 and 7 units respectively:", p_C)
print("D) Rotation about origin by an angle 60°:", p_D)
```

Output :

```
A) Shearing in Y direction by 7 units: [ -2 -10  1]
B) Scaling in X and Y direction by 7/2 and 7 units respectively: [-7. 28.  1.]
C) Shearing in X and Y direction by 4 and 7 units respectively: [ 14 -10  1]
D) Rotation about origin by an angle 60°: [-4.46410162  0.26794919  1.    ]
```

**II ) Write a python program to plot 2D x-axis and y-axis in black colour.in the same diagram plot**

**A ) Green triangle with vertices [5,4],[7,4],[6,6]**  
**B )Blue rectangle with vertices[2,2],[10,2],[10,8],[2,8]**  
**C )Red polygon with vertices[6,2],[10,4],[8,7],[4,8],[2,4]**  
**D )Isosceles triangle with vertices [0,0],[4,0],[2,4]**  
**->**

```
import matplotlib.pyplot as plt
plt.axhline(y=0, color='black')
plt.axvline(x=0, color='black')
plt.plot([5, 7, 6], [4, 4, 6], 'g')
plt.plot([2, 10, 10, 2, 2], [2, 2, 8, 8, 2], 'b')
plt.plot([6, 10, 8, 4, 2], [2, 4, 7, 8, 4], 'r')
plt.plot([0, 4, 2, 0], [0, 0, 4, 0], 'm')
```



```
plt.xlim(-2, 12)  
plt.ylim(-2, 12)
```

```
plt.title('Shapes')  
plt.xlabel('x-axis')  
plt.ylabel('y-axis')  
plt.show()
```

