

```
1 %load_ext autoreload
2 %autoreload 2
3 %matplotlib inline
4
5 from google.colab import drive
6 drive.mount('/content/drive')
```

```
1 import os, sys
2
3 DATAPATH = '/content/drive/My Drive/Coursera/EDHEC/investment-portfolio/data'
4 print(f"DATAPATH:{DATAPATH} contents:{os.listdir(DATAPATH)}")
5
6 MODULEPATH = '/content/drive/My Drive/Coursera/EDHEC/investment-portfolio/nb'
7 print(f"MODULEPATH:{MODULEPATH} contents:{os.listdir(MODULEPATH)}")
8
9 sys.path.append(MODULEPATH)
10 print(f"sys.path:{sys.path}")
11
12 import numpy as np
13 import pandas as pd
14
15 import edhec_risk_kit_108_BBI as erk
```

▼ The Efficient Frontier - Part II

Let's start by loading the returns and generating the expected returns vector and the covariance matrix

```
1 %load_ext autoreload
2 %autoreload 2
3 %matplotlib inline
```

```

4 #import edhec_risk_kit as erk
5
6 ind = erk.get_ind_returns(DATAPATH)
7 er = erk.annualize_rets(ind["1996":"2000"], 12)
8 cov = ind["1996":"2000"].cov()

```

As a first exercise, let's assume we have some weights, and let's try and compute the returns and volatilities from the weights, returns, and a covariance matrix.

The returns are easy, so let's add this to our toolkit

```

def portfolio_return(weights, returns):
    """
    Computes the return on a portfolio from constituent returns and weights
    weights are a numpy array or Nx1 matrix and returns are a numpy array or Nx1 matrix
    """
    return weights.T @ returns

```

The volatility is just as easy in matrix form:

```

def portfolio_vol(weights, covmat):
    """
    Computes the vol of a portfolio from a covariance matrix and constituent weights
    weights are a numpy array or N x 1 matrix and covmat is an N x N matrix
    """
    return (weights.T @ covmat @ weights)**0.5

```

```

1 l = ["Food", "Beer", "Smoke", "Coal"]

```

```

1 er[l]

```

```
1 cov.loc[1,1]
```

```
1 import pandas as pd
2 import numpy as np
3 ew = np.repeat(0.25, 4)
4 erk.portfolio_return(ew, er[1])
```

```
1 erk.portfolio_vol(ew, cov.loc[1,1])
```

▼ The 2-Asset Case

In the case of 2 assets, the problem is somewhat simplified, since the weight of the second asset is

Let's write a function that draws the efficient frontier for a simple 2 asset case.

Start by generating a sequence of weights in a list of tuples. Python makes it easy to generate a list using *comprehension* ... which you can think of as an efficient way to generate a list of values instead of v

```
1 import numpy as np
2
3 n_points = 20
```

```
4 weights = [np.array([w, 1-w]) for w in np.linspace(0, 1, n_points)]  
5
```

```
1 type(weights)
```

```
1 len(weights)
```

```
1 weights[0]
```

```
1 weights[4]
```

```
1 weights[19]
```

```
1 l = ["Games", "Fin"]  
2 rets = [erk.portfolio_return(w, er[l]) for w in weights]  
3 vols = [erk.portfolio_vol(w, cov.loc[l,l]) for w in weights]
```

```
4 ef = pd.DataFrame({"R": rets, "V": vols})  
5 ef.plot.scatter(x="V", y="R", figsize = (12, 6))
```

```
DATAPATH:/content/drive/My Drive/Coursera/EDHEC/investment-portfolio/data cont  
MODULEPATH:/content/drive/My Drive/Coursera/EDHEC/investment-portfolio/nb cont  
sys.path:['', '/env/python', '/usr/lib/python36.zip', '/usr/lib/python3.6', '/
```

We can create function that plots the frontier:

```

def plot_ef2(n_points, er, cov):
    """
    Plots the 2-asset efficient frontier
    """
    if er.shape[0] != 2 or er.shape[1] != 2:
        raise ValueError("plot_ef2 can only plot 2-asset frontiers")
    weights = [np.array([w, 1-w]) for w in np.linspace(0, 1, n_points)]
    rets = [portfolio_return(w, er) for w in weights]
    vols = [portfolio_vol(w, cov) for w in weights]
    ef = pd.DataFrame({
        "Returns": rets,
        "Volatility": vols
    })
    return ef.plot.line(x="Volatility", y="Returns", style=".-")

```

A useful summary of the visualization features in pandas is [here](#)

```

1 l = ["Fin", "Beer"]
2 erk.plot_ef2(25, er[l].values, cov.loc[l,l])

```



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▼ The 2-Asset Case

In the case of 2 assets, the problem is somewhat simplified, since the weight of the second asset is 1-the weight of the first asset.

Let's write a function that draws the efficient frontier for a simple 2 asset case.

Start by generating a sequence of weights in a list of tuples. Python makes it easy to generate a list by using something called a *list comprehension* ... which you can think of as an efficient way to generate a list of values instead of writing a for loop.

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