particle. physics





kinematics, accelerators particle interactions, detector response

A simple shower model

Simple shower model: [from Heitler]

Only two dominant interactions: Pair production and Bremsstrahlung ...

γ + Nucleus → Nucleus + e⁺ + e⁻ [Photons absorbed via pair production]

e + Nucleus → Nucleus + e + γ [Energy loss of electrons via Bremsstrahlung]

Shower development governed by X₀ ...

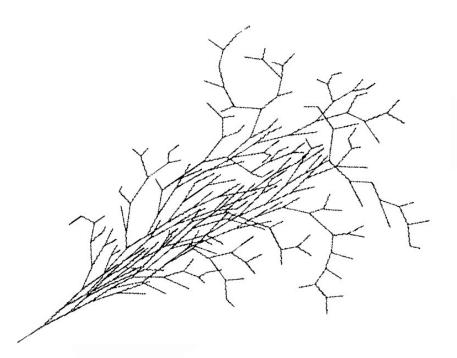
After a distance X_0 electrons remain with only $(1/e)^{th}$ of their primary energy ...

Photon produces e^+e^- -pair after $9/7X_0 \approx X_0 \dots$

Assume:

 $E > E_c$: no energy loss by ionization/excitation

 $\mathsf{E} < \mathsf{E}_{\mathtt{c}}$: energy loss only via ionization/excitation



Use Simplification:

 $E_{\Upsilon} = E_e \approx E_0/2$ [E_e looses half the energy]

 $E_e \approx E_0/2$ [Energy shared by e^+/e^-]

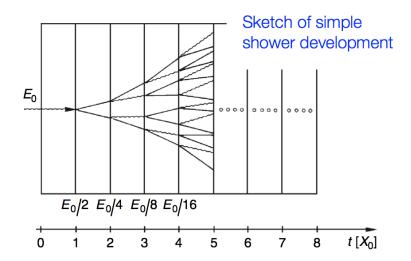
... with initial particle energy E₀

A simple shower model

Simple shower model: [continued]

Shower characterized by:

Number of particles in shower Location of shower maximum Longitudinal shower distribution Transverse shower distribution



Longitudinal components; measured in radiation length ...

... use:
$$t = \frac{x}{X_0}$$

Number of shower particles after depth t:

$$N(t) = 2^t$$

Energy per particle after depth t:

$$E = \frac{E_0}{N(t)} = E_0 \cdot 2^{-t}$$

$$\rightarrow$$
 $t = \log_2(E_0/E)$

Total number of shower particles with energy E₁:

$$N(E_0, E_1) = 2^{t_1} = 2^{\log_2(E_0/E_1)} = \frac{E_0}{E_1}$$

Number of shower particles at shower maximum:

$$N(E_0,E_c)=N_{
m max}=2^{t_{
m max}}=rac{E_0}{E_c}$$
 Shower maximum at: $\propto E_0$

$$t_{
m max} \propto \ln(E_0/E_c)$$

A simple shower model

Simple shower model: [continued]

Longitudinal shower distribution increases only logarithmically with the primary energy of the incident particle ...

Some numbers:
$$E_c \approx 10$$
 MeV, $E_0 = 1$ GeV \rightarrow $t_{max} = ln \ 100 \approx 4.5; N_{max} = 100$ $E_0 = 100$ GeV \rightarrow $t_{max} = ln \ 10000 \approx 9.2; N_{max} = 10000$

$$t_{\max}[X_0] \sim \ln \frac{E_0}{E_c}$$

Muon lifetime and acceleration

- How long muon lifetime be in a muon beam of 200 GeV momentum?
- If we inject 10¹⁰ of such muons in a storage ring of R = 100 m, how many rounds would they do before beam intensity get reduced by a 10⁶ factor?

Cosmic rays

 Protons with energy above the pion production threshold can produce them interacting with photons from relic cosmic radiation:

$$\checkmark$$
 E _{γ} ~ 10⁻³ eV

$$p + \gamma \rightarrow \Delta^+ \rightarrow p + \pi^0$$

What is the maximum energy for a proton in the cosmic rays?

This energy is called the GZK (Greisen–Zatsepin–Kuzmin) cut-off: protons above this energy see the space as a opaque medium, and decelerate...

Read this: <u>First Observation of the Greisen-Zatsepin-Kuzmin Suppression</u>

Did we observed any extremely high-energetic cosmic rays above the GKZ cut-off?

Read this: The Particle That Broke a Cosmic Speed Limit

Cosmic Ray Spectra of Various Experiments

Cosmic Ray Spectra of Various Experiments

