# Testing for Network Effects in Field Experiments: Examples from Legislative Studies

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### Research Objectives

- Model spillover of treatment effect via network structures.
- Examine how different types of networks interact with various specifications of treatment spillover.
- Evaluate the models using data from field experiments on US State legislatures.

### **Motivation**

- Conventional causal inference methods rely on SUTVA (Stable Unit Treatment Value Unit Assumption)
- Use individual-level micro attributes & context-dependent macro attributes to estimate treatment effect
- However, most social processes involve complex interaction and dependence among networked units
- Interpersonal interactions propagate treatment effect to control units and
- Various factors impact how and how much the treatment effect spreads
- Must account for the interference structure to correctly estimate the treatment effect
- Understanding the propagation of treatment itself of interest in policy planning or marketing strategy
- Generally not possible to identify the causal effects that map onto the process of social influence in observational data (Shalizi and Thomas, 2011), and randomized experiments not always feasible
- Look at methods suitable for identifying and estimating causal effect using field experiments

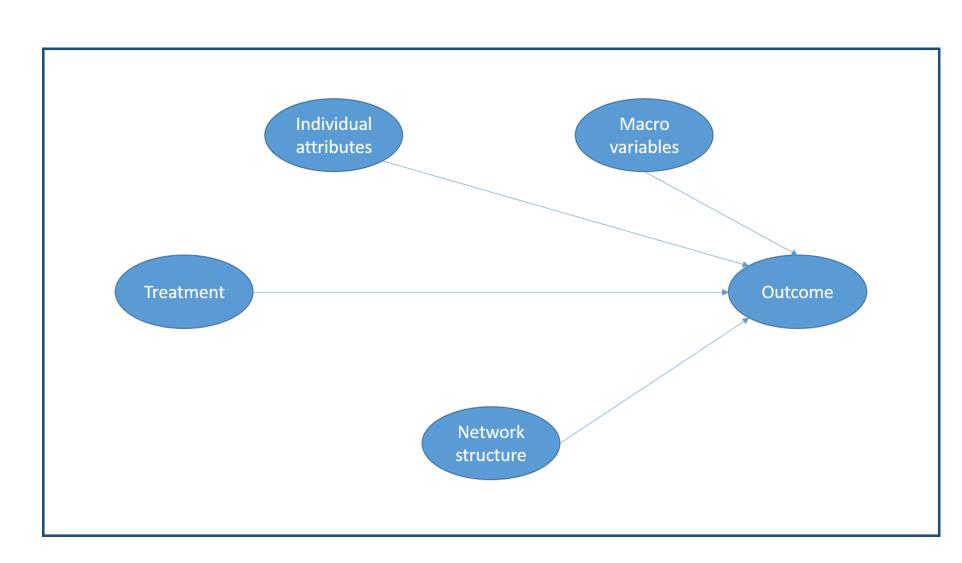


Figure: Individual causal diagram: In addition to the unit's treatment status, the network structure and treatment assignments within it are also important in determining its outcome

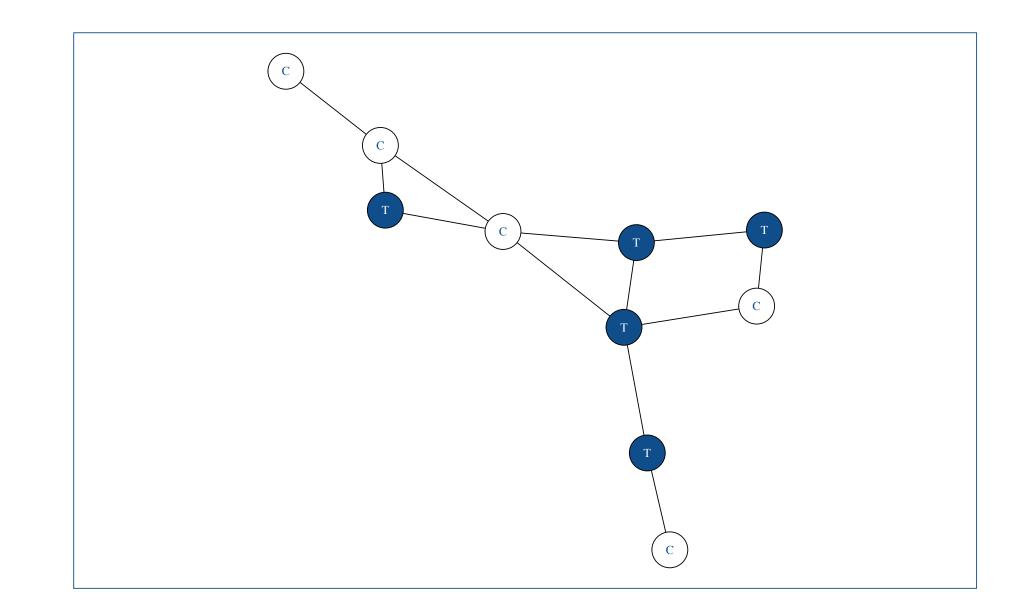


Figure: Network plot: How would we expect the treatment to affect untreated units? Simple illustration showing possible neighborhoods of control units. T: treated unit and C: control

# **Existing Approaches**

### Bowers et. al. method:

Bowers, Fredrickson and Panagopoulos 2012 proposed a non-parametric testing method for interference effects. Overall idea of this method is as follows:

- Assume the "sharp null hypothesis of no effects" i.e. treatment assignment has no effect on any unit
- Specify causal model describing the change in potential outcomes when treatment assignment changes
- Map potential outcomes from the causal model to observed outcomes
- Assume treatment only spreads along edges and spillover depends on the number of treated neighbors
- Test statistic should be a small value when distribution of treated and control outcomes in the adjusted data are similar, and a large value when distributions are dissimilar
- p-value is the proportion of permutation tests whose test statistic is lesser than the observed test statistic

### Coppock application

Coppock 2014 implements Bowers method to analyze the New Mexico Legislator experiment conducted by Butler, Nickerson et al. 2011. Uses ideological network with a different choice of diffusion model and test statistic. Bowers methodology is inadequate to handle categorical outcomes.

# Proposed extensions along various dimensions

- Neighborhood specification:
- Effect from all units

- Effect from k-nearest neighbors
- **Diffusion model specification:** Consider models varying along following dimensions:
- Distance from the nearest treated node
- Form of spread (linear or non-linear)
- Number/proportion of treated neighbors Network selection:
- Ideological network

• Committee network

Co-sponsorship network

Geographical network network

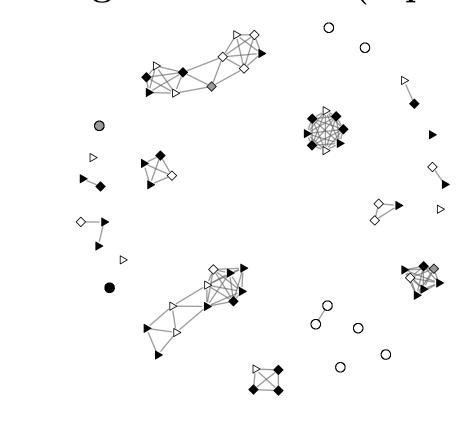
- Test statistic selection:
- Kolmogorov-Smirnov test Anderson-Darling test

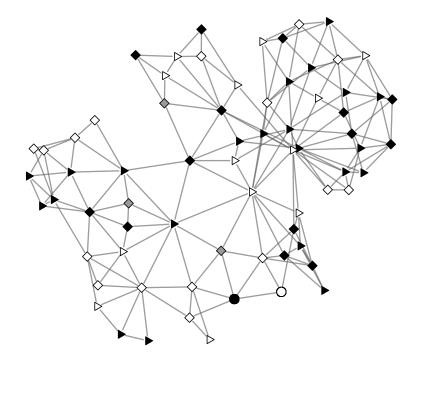
#### Mann-Whitney U test Control Median test

# **Data**

Bill to return a projected budget surplus in form of a rebate proposed in the New Mexico state legislature during a special session in 2008. 35 out of the 70 legislators (matched pairs) received estimates of support within their constituencies. Below are three possible network structures connecting the legislators:

#### Ideological Network (top 5%) Geographic Network Committee Network (>1 common)





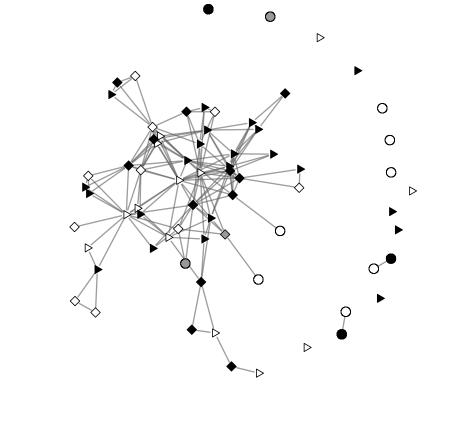


Figure: Different networks among New Mexico legislators. Colors denote outcome: black means voted with district, gray means abstained, white means voted against. Shape denotes treatment status. Triangles are treated. Squares are adjacent to treated. Circles are isolated from treatment

# Replication of Coppock analysis

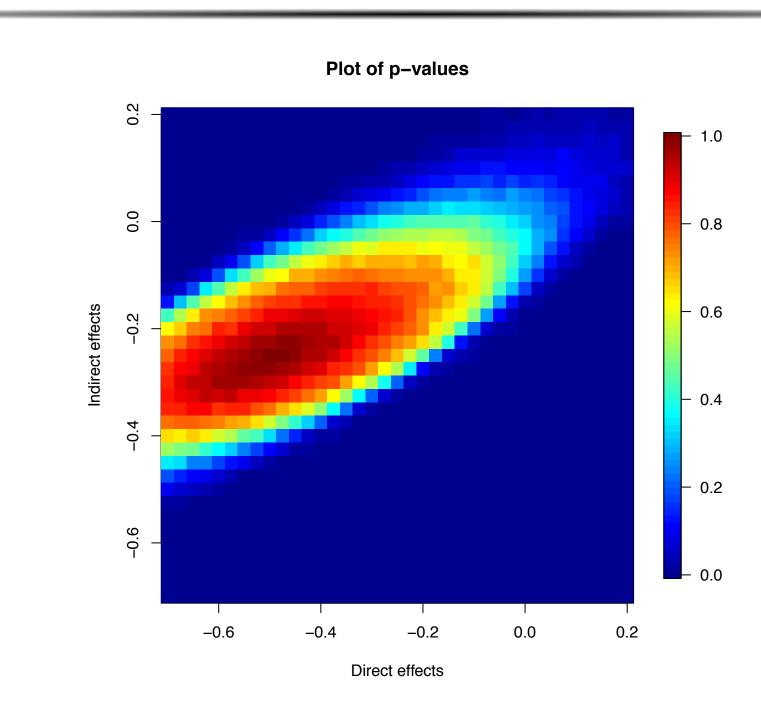


Figure: Higher values provide evidence for spillover effect

### **Extension**

Extend the Coppock analysis using a different neighborhood specification. We use ideological scores and create an adjacency matrix based on whether a particular legislator is one of the k nearest neighbors

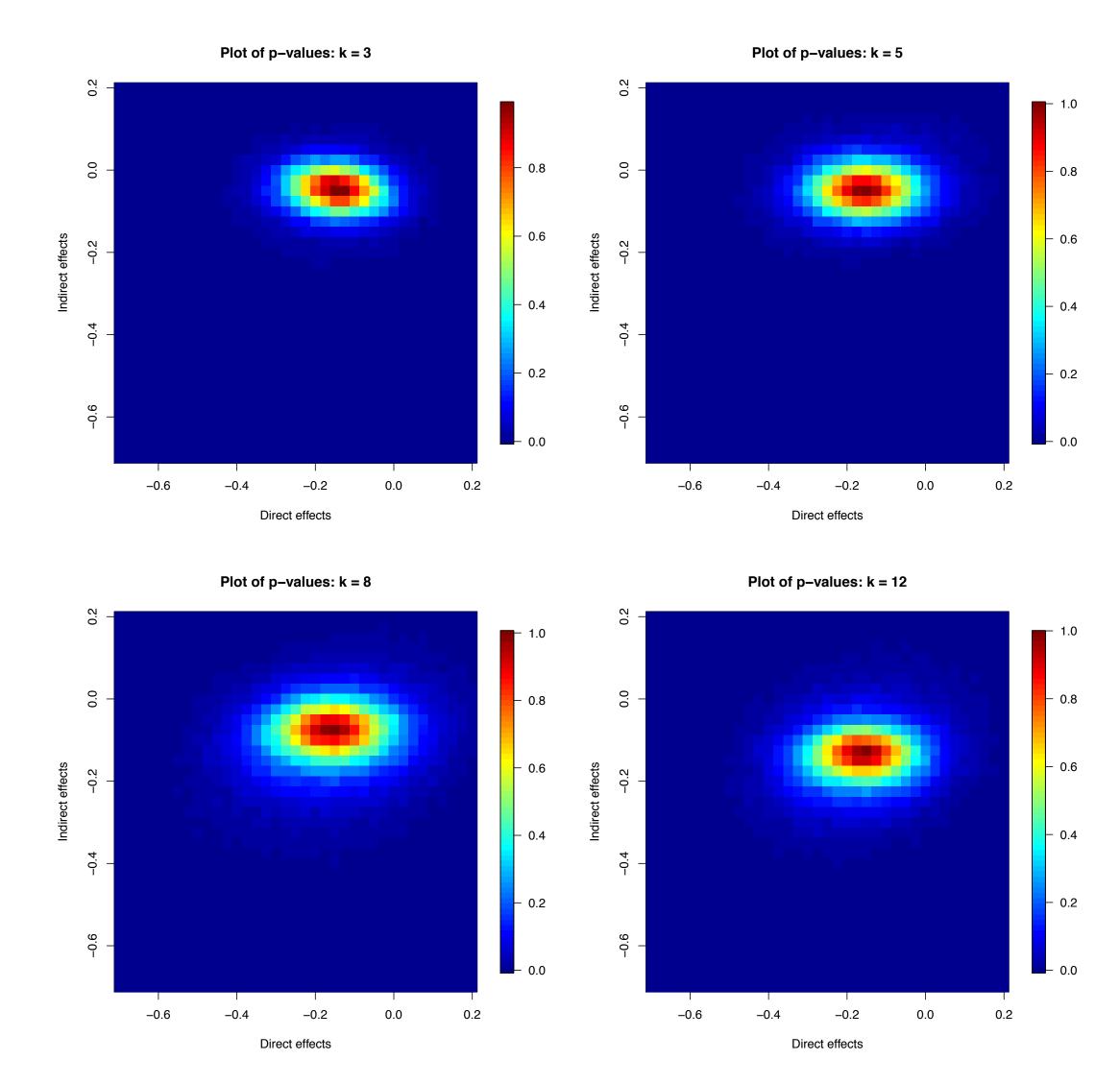


Figure: p-values: highest values move closer to zero value for both effects

# **Future direction**

- Consider another example of a field experiment on New Hampshire state legislature
- Evaluate models specified by various dimensions under the extensions



Bowers, Jake, Mark M Fredrickson and Costas Panagopoulos. 2012. "Reasoning about interference between units: A general framework." *Political Analysis* p. mps038.

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Coppock, Alexander. 2014. "Information spillovers: Another look at experimental estimates of legislator responsiveness." Journal of Experimental Political Science 1(02):159–169.

Shalizi, Cosma Rohilla and Andrew C Thomas. 2011. "Homophily and contagion are generically confounded in observational social network studies." Sociological methods & research 40(2):211–239.

