

# Considering Interference in Field Experiments

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## Abstract

We plan to write a paper about how interference hypotheses can and should be used to analyze the results of field experiments in which there is a high probability that subjects interacted between the administration of treatment and the observation of outcomes.

## 1 Introduction

Networks are integral parts of human interaction and hence social science research. If one unit in a network gets treated, the effect may trickle down throughout network. The currently established framework for causal inference relies on SUTVA (Stable Unit Treatment Value Assumption). It assumes that whether or not one person/unit/node is treated, does not affect any other unit. However, SUTVA breaks down in a network setting. It is therefore imperative to take the interference structure into account. Rather, in policy planning or designing marketing campaigns, a researcher may be interested in studying the propagation of treatment effect itself.

In field experiments on social groups, interference may be substantial. In this project we intend to study interference models for randomized experiments conducted on social networks and causal inference basis this.

To understand, explain and predict social phenomena, social scientists typically look to individual actors' attributes to explain their behavior (e.g., an increase in an individual's wealth will result in a decrease in that individual's support for government spending on social welfare), or to attributes of the macro context (e.g., an increase in the unemployment rate will lead an individual's support for the party of the president to decrease). However, these two conceptual approaches to explaining individual behavior leave out a potentially powerful class of social dynamics – interpersonal influence. That is, the behavior of one individual may depend upon the behavior of one or more others (e.g., a person may decide to vote due to their friends claiming to have voted (?)). Inferences regarding influence involve the analysis of individual behaviors and the behaviors of those adjacent or nearby in some contact network. However, as in most settings, it is generally not possible to identify the causal effects that map onto the process of social influence in observational data CITE SHALIZI. As such, we need experimental methods to identify causal influence effects.

## **1.1 tasks**

- Points about why it is interesting to study propagation. (BD)
- Outline of the paper (SP)

## **2 Background**

Review of relevant methodological work and substance.

## 2.1 tasks

- **PRIORITY:** Explain the Bowers et al method in our own words (SP). Describe the algorithm in enough detail that one could implement it based on our explanation.

Below we see a description of the Fisherian inference algorithm as described in the Bowers et al paper. Here the aim is to test for a model  $\mathcal{H}$  against the data we observe. This hypothesized model can include interference effect

1. As discussed in the Method section, we assume the "sharp null hypothesis of no effects" i.e. we assume that the treatment assignment has no effect on any unit
2. We begin by specifying the causal model which describes the change in potential outcomes when treatment assignment changes from  $\mathbf{u}$  to  $\mathbf{w}$ ;  $\mathcal{H}(y_{i,\mathbf{u}}, \mathbf{w}, \theta)$ . If spillover effects are theoretically motivated, we must also specify treatment assignment for  $u_j$  and  $w_j$  where  $i \neq j$
3. The potential outcomes from the causal model must be mapped to the observed outcomes  $y_{\mathbf{z}}$ . The treatment assignment in the experiment ( $\mathbf{z}$ ) must be mapped to the uniformity trial which is based on a no-treatment assignment i.e. every unit is a control unit. In this condition, all  $z_i$ s are zero and we refer to this as the baseline condition. Uniformity trial is specified as  $\mathcal{H}(y_{\mathbf{z}}, \mathbf{0}, \theta) = \mathbf{y}_0$ . These mappings should give us the hypothesized value of  $\theta$  and a data adjusted to the model
4. The test statistic we consider is  $\mathcal{T}$  and the key characteristic is that it should be a small value when distribution of treated and control outcomes in the adjusted

data (mentioned in point 3) are similar.  $\mathcal{T}$  should be larger when distributions are dissimilar. Since we want the similarity to depend on not just the center but also higher-order moments of a distribution (spread, skewness etc.), we need a sensitive measure. Bowers et al recommend using the Kolmogorov-Smirnov (KS) test statistic.

As noted in footnote 12 of the paper, KS statistic is the maximum difference between the empirical cumulative distribution functions (ECDFs) of treated ( $F_1$ ) and control ( $F_0$ ) units. So under the baseline condition,

$$\mathcal{T}_{\mathbf{y}_0, \mathbf{z}} = \max_{1 \leq i \leq n} [F_1(y_i, 0) - F_0(y_i, 0)]$$

where  $F(x) = \frac{1}{n} \sum_{i=1}^n I(x_i \leq x)$  is the proportion of  $x$  below  $x_i$

5. We must form hypothesis for interference. Here we assume that treatment only spreads through edges and the spillover effect only depends on the number of neighbours treated. The model for interference is explained in the immediately next section. However, here we note that the spillover effect is modeled using a growth curve  $\beta + (1 - \beta)e^{-\tau^2 \mathbf{z}^T \mathbf{s}}$
6. Now we generate the distribution of test statistic under our hypothesis. The exact distribution is specified by computing  $t_k = \mathcal{T}(\mathbf{y}_0, \mathbf{Z}_k)$  for each  $\mathbf{Z}_k \in \Omega$ . Essentially, we are evaluating this for every possible treatment assignment. Alternatively, we can use sampling methods and limit theorems to estimate the distribution from data.

7. Finally, the p-value for our test can be calculated using the following formula:

$$\frac{\sum_{k=1}^{abs(\Omega)} I(x_i > t_k)}{abs(\Omega)}$$

- Paragraph on each category of papers that serve as relevant background (SP)
  - Interference models (diffusion, propagation) (SP–Review)
  - Experiments on networks (applications) (SP–Review)
  - Approaches to inference or estimation with propagation (SP–Review)
  - Potential outcomes framework (SP – find papers & Review)
  - Review of political networks (SP–Review)
  - Review of field experiments (SP–Review)
  - \* (??????)

### 3 Research Design

We plan to re-analyze data from past field experimental studies to understand how conclusions regarding direct effects and interference effects depend upon

#### 3.1 tasks

Develop a list of alternative propagation models to evaluate. (SP)

The key factors that we consider important in building propagation models are:

1. Geographical proximity
2. Ideological similarity
3. Co-sponsorship

Each of these factors is such, that a treatment such as the message sent through emails in New Hampshire, would possibly spread to untreated units as well. Legislators from adjoining districts may affect each other's opinions through geographic proximity as well as potentially via common issues faced by citizens in their constituencies.

Ideological similarity is a tricky variable because it could be hard to distinguish that from party affiliation. In the New Hampshire paper, there is a need to include this effect in the model since matched pairs are created based on party affiliation. If a Republican candidate receives the treatment, the chances that through various communication channels, he/she will convey the message to the control group candidate from the same party and district, are very high.

Finally, serving on the same committee can also contribute to spreading the effect of a treatment. We must test for any dependence across these three factors before incorporating them into our model. Therefore it is important that we propose and test propagation models that consider the spread of treatment through our network.

**\*\*Notes:**

1. Ideological similarity: This should get highest priority in modeling, since I believe, it would be easiest to affect an undecided legislator's vote through similarity in ideas

and belief about citizen's issues and how to resolve them. I would propose that we model immediate neighbours to have a 50

2. Grographical proximity: An untreated legislator from adjoining district would be
3. Co-sponsorship: Serving on the same committee increases the chances of

## 4 Analysis

\*Could we use the idea of communities to model spread of treatment across the network?

Replicating results from the Nickerson paper

The first table contains results of balance test for pre-treatment covariates in the analysis. The p-values are calculates using simple logit regressions. This table shows that there is covariate balance across treatment conditions

	Treatment	Control	p-value
Republican	40%	40%	1
Constituent support for spending	40.8%	41.3%	0.8
Constituent support for health care	54.2%	52.7%	0.34
Bush vote-share 04	51.3%	49.3%	0.59
Member vote-share 06	60.6%	61.2%	0.86
Running for re-election	91.4%	88.6%	0.69
Running unopposed	59.4%	58.1%	0.92
Supported prior health care bill	54.3%	51.4%	0.81

Table 1: Table 1: Randomization checks

The next two tables present regression results. We are modeling the likelihood of

voting in favor of SB 24. In the first regression, we study whether the treatment effects differ substantively across districts where support for the governor’s spending proposals was low and ones where it was not. This is our key independent variable. Each regression uses a Probit model with standard errors clustered on the 35 matched pairs on which the randomization was based. We use the Zelig program/package in R to incorporate clustered standard errors into the model. The original analysis was performed in STATA. We notice that our estimates are the same as those in the original paper and standard errors are very close as well.

	Coefficients	SEs
Constant	0.76	0.33
Treatment	0.16	0.49
Low support for spending	0.70	0.60
Low support*Treatment	-1.49	0.76

Table 2: Table 2A: Regression results without controls

In the second regression, we also control for whether the legislator was a Republican and the 2004 Presidential election results for the given district.

	Coefficients	SEs
Constant	-0.16	1.65
Treatment	-0.07	0.70
Low support for spending	1.50	0.83
Low support*Treatment	-1.86	1.04
Republican legislator	-1.61	0.68
2004 Democratic two-party presidential vote share	4.06	2.78

Present original results from studies that we replicate: Coppock

The Coppock (2014) paper builds upon the New Mexico Legislator experiment con-



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Table 3: Regression results with controls

ducted by Butler and Nickerson (2011). The next two figures replicate analysis from the original paper, as shown in the Coppock (2014) paper. Figure 1 below replicates the result under the assumption that indirect effects are exactly zero. X-axis represents the proposed values for direct treatment effect, Y-axis represents simulated p-values and the colouring is according to the p-values.

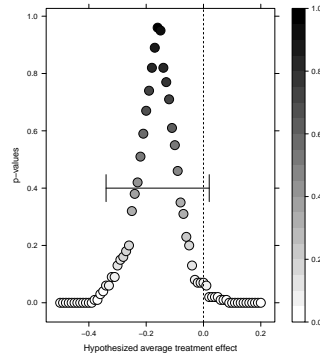


Figure 1: Figure 1

Figure 2 shows the heterogeneous effects of treatment. X-axis represents hypothesized effects in higher-support districts as against the hypothesized effects in lower-support districts on Y-axis. Once again, the colour scale indicates the p-value for each pair of hypotheses. Darker region indicates a higher p-value. We observe maximum p-value at

effect values (0.05, -0.37) in higher-support and lower-support regions respectively.

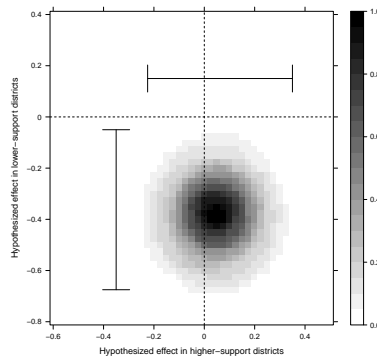


Figure 2: Figure 1

Present results when we assume some form of interference

Explore how alternative assumptions regarding interference change results

## 4.1 tasks

- Replicate Bergan. (SP)
- Find other network data for the New Mexico legislature. (BD)
- Geography and ideology data for New Hampshire (BD)
- Produce cosponsorship, ideology and geography estimates for both Bergan and Nickerson (SP & BD)
- For at least two spreading models (SP & BD)
- Replicate Nyhan (SP)

Records of standing committee membership in the 16 standing committees in place during the 2008 regular session was obtained from the New Mexico Legislative Council Service Librarian.

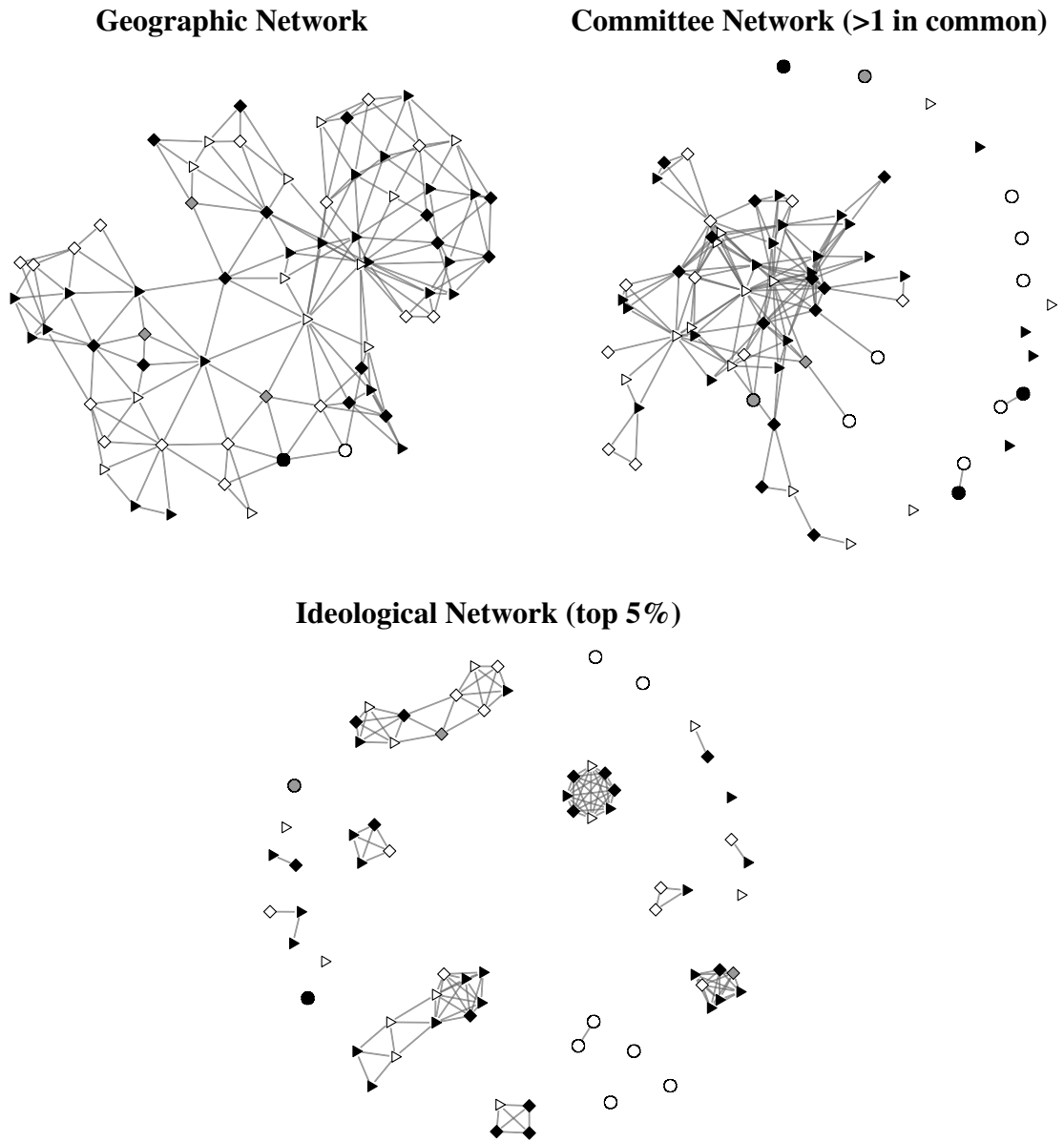


Figure 3: Different networks among New Mexico legislators. Colors denote outcome: black means voted with district, gray means abstained, white means voted against. Shape denotes treatment status. Triangles are treated. Squares are adjacent to treated. Circles are isolated from treatment

## References