

4.6 : Cochran's Test For related observations

$\left\{ \begin{array}{l} H_0: \text{The treatments are equally effective} \\ H_a: \text{Not all equally effective.} \end{array} \right.$

or

$H_0: p_1 = p_2 = \dots = p_c$ within each block

$H_a: \text{Not all equal}$ // // //

Test	Statistic
	$T = c(c-1) \frac{\sum_{j=1}^c (c_j - \frac{N}{c})^2}{\sum_{i=1}^r R_i (c - R_i)}$

Hand calculation

$$T = \frac{c(c-1) \sum_{j=1}^c c_j^2 - (c-1)N^2}{cN - \sum_{i=1}^r R_i^2}$$

Block	Treatment				Row total
	1	2	...	c	
1	x_{11}	x_{12}		x_{1c}	R_1
2	\vdots				\vdots
\vdots					
r	x_{r1}	x_{r2}	...	x_{rc}	R_r
	c_1	c_2	...	c_c	N

grand total \nearrow

Cont. 4.6

②

If $C = 2$ use

$$T = \frac{\sum_{i=1}^c R_i (2 - R_i)}{(c-2)^2}$$

Note: Same as McNemar's test

$$T = \frac{(c-b)^2}{b+c}$$

reject H_0 if

$$T > \chi^2_{1-\alpha}(1)$$