

ACM ICPC Reference

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1 Data Structures

Treap (balanced binary search tree)

```
struct node {
    int v, key, size;
    node *c[2];
    void resize() { size = c[0]->size + c[1]->size + 1; }
};

node *newNode(int _v, node *n) {
    ++ref;
    pool[ref].v = _v, pool[ref].c[0] = pool[ref].c[1] = n, pool[ref].size = 1,
    pool[ref].key = rand();
    return &pool[ref];
}

struct Treap {
    node *root, *nil;
    void rotate(node *&t, int d) {
        node *c = t->c[d];
        t->c[d] = c->c[!d];
        c->c[!d] = t;
        t->resize(); c->resize();
        t = c;
    }
    void insert(node *&t, int x) {
        if (t == nil) t = newNode(x, nil);
        else {
            if (x == t->v) return;
            int d = x > t->v;
            insert(t->c[d], x);
            if (t->c[d]->key < t->key) rotate(t, d);
            else t->resize();
        }
    }
    void remove(node *&t, int x) {
```

```
        if (t == nil) return;
        if (t->v == x) {
            int d = t->c[1]->key < t->c[0]->key;
            if (t->c[d] == nil) {
                t = nil;
                return;
            }
            rotate(t, d);
            remove(t->c[!d], x);
        } else {
            int d = x > t->v;
            remove(t->c[d], x);
        }
        t->resize();
    }

    int rank(node *t, int x) {
        if (t == nil) return 0;
        int r = t->c[0]->size;
        if (x == t->v) return r + 1;
        if (x < t->v) return rank(t->c[0], x);
        return r + 1 + rank(t->c[1], x);
    }

    int select(node *t, int k) {
        int r = t->c[0]->size;
        if (k == r + 1) return t->v;
        if (k <= r) return select(t->c[0], k);
        return select(t->c[1], k - r - 1);
    }

    int size() {
        return root->size;
    }

    void init(int *a, int n) {
        nil = newNode(0, 0);
        nil->size = 0, nil->key = ~0U >> 1;
        root = nil;
    }
}
```

```
};
```

2 Geometry

Welzl's algorithm (minimum enclosing circle)

```
// Minimum enclosing circle, Welzl's algorithm
// Expected linear time.
// If there are any duplicate points in the input, be sure to remove them
// first.
struct point {
    double x;
    double y;
};
struct circle {
    double x;
    double y;
    double r;
    circle() {}
    circle(double x, double y, double r): x(x), y(y), r(r) {}
};
circle b_md(vector<point> R) {
    if (R.size() == 0) {
        return circle(0, 0, -1);
    } else if (R.size() == 1) {
        return circle(R[0].x, R[0].y, 0);
    } else if (R.size() == 2) {
        return circle((R[0].x+R[1].x)/2.0,
                      (R[0].y+R[1].y)/2.0,
                      hypot(R[0].x-R[1].x, R[0].y-R[1].y)/2.0);
    } else {
        double D = (R[0].x - R[2].x)*(R[1].y - R[2].y) - (R[1].x - R[2].x)*(R[0].y - R[2].y);
        double p0 = (((R[0].x - R[2].x)*(R[0].x + R[2].x) + (R[0].y - R[2].y)*(R[0].y + R[2].y)) / 2 * (R[1].y - R[2].y) - ((R[1].x - R[2].x)*(R[1].x + R[2].x) + (R[1].y - R[2].y)*(R[1].y + R[2].y)) / 2 * (R[0].y - R[2].y))/D;
        double p1 = (((R[1].x - R[2].x)*(R[1].x + R[2].x) + (R[1].y - R[2].y)*(R[1].y + R[2].y)) / 2 * (R[0].x - R[2].x) - ((R[0].x - R[2].x)*(R[0].x + R[2].x) + (R[0].y - R[2].y)*(R[0].y + R[2].y)) / 2 * (R[1].x - R[2].x))/D;
        return circle(p0, p1, hypot(R[0].x - p0, R[0].y - p1));
    }
}
```

```
}
circle b_minidisk(vector<point>& P, int i, vector<point> R) {
    if (i == P.size() || R.size() == 3) {
        return b_md(R);
    } else {
        circle D = b_minidisk(P, i+1, R);
        if (hypot(P[i].x-D.x, P[i].y-D.y) > D.r) {
            R.push_back(P[i]);
            D = b_minidisk(P, i+1, R);
        }
        return D;
    }
}

// Call this function.
circle minidisk(vector<point> P) {
    random_shuffle(P.begin(), P.end());
    return b_minidisk(P, 0, vector<point>());
}
```

Monotone chain (convex hull) and rotating calipers (farthest pair)

```
typedef long double gtype;
const gtype pi = M_PI;
typedef complex<gtype> point;
#define x real()
#define y imag()
#define polar(r, t) polar((gtype) (r), (t))
// vector
#define rot(v, t) ( (v) * polar(1, t) )
#define crs(a, b) ( (conj(a) * (b)).y )
#define dot(a, b) ( (conj(a) * (b)).x )
#define pntLinDist(a, b, p) ( abs(crs((b)-(a), (p)-(a)) / abs((b)-(a))) )
bool cmp_point(point const& p1, point const& p2) {
    return p1.x == p2.x ? (p1.y < p2.y) : (p1.x < p2.x);
}

// O(n.log(n)) - monotone chain
vector<point> mcH;
void monotoneChain(vector<point> &ps) {
    vector<point> p(ps.begin(), ps.end() - 1);
    int n = p.size(), k = 0;
    mcH = vector<point>(2 * n);
```

```

sort(p.begin(), p.end(), cmp_point);
for (int i = 0; i < n; i++) {
    while (k >= 2 && crs(mch[k - 1] - mch[k - 2], p[i] - mch[k - 2]) <= 0)
        k--;
    mch[k++] = p[i];
}
for (int i = n - 2, t = k + 1; i >= 0; i--) {
    while (k >= t && crs(mch[k - 1] - mch[k - 2], p[i] - mch[k - 2]) <= 0)
        k--;
    mch[k++] = p[i];
}
mch.resize(k);
}
// O(n) - rotating calipers (works on a ccw closed convex hull)
gtype rotatingCalipers(vector<point> &ps) {
    int aI = 0, bI = 0;
    for (size_t i = 1; i < ps.size(); ++i)
        aI = (ps[i].y < ps[aI].y ? i : aI), bI = (ps[i].y > ps[bI].y ? i : bI);
    ;
    gtype minWidth = ps[bI].y - ps[aI].y, aAng, bAng;
    point aV = point(1, 0), bV = point(-1, 0);
    for (gtype ang = 0; ang < pi; ang += min(aAng, bAng)) {
        aAng = acos(dot(ps[aI + 1] - ps[aI], aV)
            / abs(aV) / abs(ps[aI + 1] - ps[aI]));
        bAng = acos(dot(ps[bI + 1] - ps[bI], bV)
            / abs(bV) / abs(ps[bI + 1] - ps[bI]));
        aV = rot(aV, min(aAng, bAng)), bV = rot(bV, min(aAng, bAng));
        if (aAng < bAng)
            minWidth = min(minWidth, pntLinDist(ps[aI], ps[aI] + aV, ps[bI]))
            , aI = (aI + 1) % (ps.size() - 1);
        else
            minWidth = min(minWidth, pntLinDist(ps[bI], ps[bI] + bV, ps[aI]))
            , bI = (bI + 1) % (ps.size() - 1);
    }
    return minWidth;
}

```

3d Convex Hull

```

int n, bf[maxn][maxn], fcnt;
point3_t pt[maxn];
struct face_t {
    int a, b, c;

```

```

    bool vis;
} fc[maxn << 5]; /* Number of Faces(Unknown) */

bool remove(int p, int b, int a) {
    int f = bf[b][a];
    face_t ff;
    if (fc[f].vis) {
        if (dblcmp(volume(pt[p], pt[fc[f].a], pt[fc[f].b], pt[fc[f].c])) >= 0) {
            return true;
        } else {
            ff.a = a, ff.b = b, ff.c = p;
            bf[ff.a][ff.b] = bf[ff.b][ff.c] = bf[ff.c][ff.a] = ++fcnt;
            ff.vis = true;
            fc[fcnt] = ff;
        }
    }
    return false;
}

void dfs(int p, int f) {
    fc[f].vis = false;
    if (remove(p, fc[f].b, fc[f].a)) dfs(p, bf[fc[f].b][fc[f].a]);
    if (remove(p, fc[f].c, fc[f].b)) dfs(p, bf[fc[f].c][fc[f].b]);
    if (remove(p, fc[f].a, fc[f].c)) dfs(p, bf[fc[f].a][fc[f].c]);
}

void hull3d() {
    for (int i = 2; i <= n; ++i) {
        if (dblcmp((pt[i] - pt[1]).length()) > 0) swap(pt[i], pt[2]);
    }
    for (int i = 3; i <= n; ++i) {
        if (dblcmp(fabs(area(pt[1], pt[2], pt[i]))) > 0) swap(pt[i], pt[3]);
    }
    for (int i = 4; i <= n; ++i) {
        if (dblcmp(fabs(volume(pt[1], pt[2], pt[3], pt[i]))) > 0) swap(pt[i], pt[4]);
    }
    zm(fc), fcnt = 0, zm(bf);
    for (int i = 1; i <= 4; ++i) {
        face_t f;
        f.a = i + 1, f.b = i + 2, f.c = i + 3;
        if (f.a > 4) f.a -= 4;
        if (f.b > 4) f.b -= 4;
        if (f.c > 4) f.c -= 4;
        if (dblcmp(volume(pt[i], pt[f.a], pt[f.b], pt[f.c])) > 0) swap(f.a, f.b);
        f.vis = true;
    }
}

```

```

    bf[f.a][f.b] = bf[f.b][f.c] = bf[f.c][f.a] = ++fcnt;
    fc[fcnt] = f;
}
random_shuffle(pt + 5, pt + 1 + n);
for (int i = 5; i <= n; ++i) {
    for (int j = 1; j <= fcnt; ++j) {
        if (!fc[j].vis) continue;
        if (dblcmp(volume(pt[i], pt[fc[j].a], pt[fc[j].b], pt[fc[j].c])) >= 0) {
            dfs(i, j);
            break;
        }
    }
}
for (int i = 1; i <= fcnt; ++i) if (!fc[i].vis) swap(fc[i--], fc[fcnt--]);
}

```

3 Graph

Min cost flow

```

/* Min cost max flow (Edmonds-Karp relabelling + fast heap Dijkstra)
 * Based on code by Frank Chu and Igor Naverniouk
 * (http://shygypsy.com/tools/mcmf4.cpp)
 *
 * COMPLEXITY:
 *   - Worst case: O(min(m*log(m)*flow, n*m*log(m)*fcost))
 * FIELD TESTING:
 *   - Valladolid 10594: Data Flow
 * REFERENCE:
 *   Edmonds, J., Karp, R. "Theoretical Improvements in Algorithmic
 *   Efficiency for Network Flow Problems".
 *   This is a slight improvement of Frank Chu's implementation.
 */

#define Inf (LLONG_MAX/2)
#define BUBL { \
    t = q[i]; q[i] = q[j]; q[j] = t; \
    t = inq[q[i]]; inq[q[i]] = inq[q[j]]; inq[q[j]] = t; }
#define Pot(u,v) (d[u] + pi[u] - pi[v])
struct MinCostMaxFlow {
    typedef long long LL;
    int n, qs;
    vector<vector<LL>> cap, cost, fnet;

```

```

    vector<vector<int>> adj;
    vector<LL> d, pi;
    vector<int> deg, par, q, inq;

    // n = number of vertices
    MinCostMaxFlow(int n): n(n), qs(0), deg(n+1), par(n+1), d(n+1), q(n+1), inq(
        n+1), pi(n+1), cap(n+1, vector<LL>(n+1)), cost(cap), fnet(cap), adj(n+1,
        vector<int>(n+1)) {}

    // call to add a directed edge. vertices are 0-based
    // ALL COSTS MUST BE NON-NEGATIVE
    void AddEdge(int from, int to, LL cap_, LL cost_) {
        cap[from][to] = cap_; cost[from][to] = cost_;
    }

    bool dijkstra( int s, int t ) {
        fill(d.begin(), d.end(), 0x3f3f3f3f3f3f3f3fLL);
        fill(par.begin(), par.end(), -1);
        fill(inq.begin(), inq.end(), -1);
        d[s] = qs = 0;
        inq[q[qs++] = s] = 0;
        par[s] = n;
        while( qs ) {
            int u = q[0]; inq[u] = -1;
            q[0] = q[--qs];
            if( qs ) inq[q[0]] = 0;
            for( int i = 0, j = 2*i + 1, t; j < qs; i = j, j = 2*i + 1 ) {
                if( j + 1 < qs && d[q[j + 1]] < d[q[j]] ) j++;
                if( d[q[j]] >= d[q[i]] ) break;
                BUBL;
            }
            for( int k = 0, v = adj[u][k]; k < deg[u]; v = adj[u][++k] ) {
                if( fnet[v][u] && d[v] > Pot(u,v) - cost[v][u] )
                    d[v] = Pot(u,v) - cost[v][par[v] = u];
                if( fnet[u][v] < cap[u][v] && d[v] > Pot(u,v) + cost[u][v] )
                    d[v] = Pot(u,v) + cost[par[v] = u][v];
                if( par[v] == u ) {
                    if( inq[v] < 0 ) { inq[q[qs] = v] = qs; qs++; }
                    for( int i = inq[v], j = ( i - 1 )/2, t;
                        d[q[i]] < d[q[j]]; i = j, j = ( i - 1 )/2 )
                        BUBL;
                }
            }
        }
        for( int i = 0; i < n; i++ ) if( pi[i] < Inf ) pi[i] += d[i];
        return par[t] >= 0;
    }

```

```

}

// Returns: (flow, total cost) between source s and sink t
// Call this once only. fnet[i][j] contains the flow from i to j. Careful,
// fnet[i][j] and fnet[j][i] could both be positive.
pair<LL, LL> mcmf4(int s, int t) {
    for( int i = 0; i < n; i++ )
        for( int j = 0; j < n; j++ )
            if( cap[i][j] || cap[j][i] ) adj[i][deg[i]++] = j;
    LL flow = 0; LL fcost = 0;
    while( dijkstra( s, t ) ) {
        LL bot = LLONG_MAX;
        for( int v = t, u = par[v]; v != s; u = par[v = u] )
            bot = min(bot, fnet[v][u] ? fnet[v][u] : ( cap[u][v] - fnet[u][v] ));
        for( int v = t, u = par[v]; v != s; u = par[v = u] )
            if( fnet[v][u] ) { fnet[v][u] -= bot; fcost -= bot * cost[v][u]; }
            else { fnet[u][v] += bot; fcost += bot * cost[u][v]; }
        flow += bot;
    }
    return make_pair(flow, fcost);
}
};

```

Dinic's (VE^2 max flow)

```

// C++ implementation of Dinic's Algorithm
#include<bits/stdc++.h>
using namespace std;

// A structure to represent an edge between
// two vertex
struct Edge
{
    int v ; // Vertex v (or "to" vertex)
            // of a directed edge u-v. "From"
            // vertex u can be obtained using
            // index in adjacent array.

    int flow ; // flow of data in edge

    int C;    // capacity

    int rev ; // To store index of reverse

```

```

            // edge in adjacency list so that
            // we can quickly find it.
};

// Residual Graph
class Graph
{
    int V; // number of vertex
    int *level ; // stores level of a node
    vector< Edge > *adj;
public :
    Graph(int V)
    {
        adj = new vector<Edge>[V];
        this->V = V;
        level = new int[V];
    }

    // add edge to the graph
    void addEdge(int u, int v, int C)
    {
        // Forward edge : 0 flow and C capacity
        Edge a{v, 0, C, adj[v].size()};

        // Back edge : 0 flow and 0 capacity
        Edge b{u, 0, 0, adj[u].size()};

        adj[u].push_back(a);
        adj[v].push_back(b); // reverse edge
    }

    bool BFS(int s, int t);
    int sendFlow(int s, int flow, int t, int ptr[]);
    int DinicMaxflow(int s, int t);
};

// Finds if more flow can be sent from s to t.
// Also assigns levels to nodes.
bool Graph::BFS(int s, int t)
{
    for (int i = 0 ; i < V ; i++)
        level[i] = -1;

    level[s] = 0; // Level of source vertex

    // Create a queue, enqueue source vertex

```

```

// and mark source vertex as visited here
// level[] array works as visited array also.
list< int > q;
q.push_back(s);

vector<Edge>::iterator i ;
while (!q.empty())
{
    int u = q.front();
    q.pop_front();
    for (i = adj[u].begin(); i != adj[u].end(); i++)
    {
        Edge &e = *i;
        if (level[e.v] < 0  && e.flow < e.C)
        {
            // Level of current vertex is,
            // level of parent + 1
            level[e.v] = level[u] + 1;

            q.push_back(e.v);
        }
    }

    // IF we can not reach to the sink we
    // return false else true
    return level[t] < 0 ? false : true ;
}

// A DFS based function to send flow after BFS has
// figured out that there is a possible flow and
// constructed levels. This function called multiple
// times for a single call of BFS.
// flow : Current flow send by parent function call
// start[] : To keep track of next edge to be explored.
//          start[i] stores count of edges explored
//          from i.
// u : Current vertex
// t : Sink
int Graph::sendFlow(int u, int flow, int t, int start[])
{
    // Sink reached
    if (u == t)
        return flow;

    // Traverse all adjacent edges one -by - one.

```

```

for ( ; start[u] < adj[u].size(); start[u]++)
{
    // Pick next edge from adjacency list of u
    Edge &e = adj[u][start[u]];

    if (level[e.v] == level[u]+1 && e.flow < e.C)
    {
        // find minimum flow from u to t
        int curr_flow = min(flow, e.C - e.flow);

        int temp_flow = sendFlow(e.v, curr_flow, t, start);

        // flow is greater than zero
        if (temp_flow > 0)
        {
            // add flow to current edge
            e.flow += temp_flow;

            // subtract flow from reverse edge
            // of current edge
            adj[e.v][e.rev].flow -= temp_flow;
            return temp_flow;
        }
    }
}

return 0;
}

// Returns maximum flow in graph
int Graph::DinicMaxflow(int s, int t)
{
    // Corner case
    if (s == t)
        return -1;

    int total = 0; // Initialize result

    // Augment the flow while there is path
    // from source to sink
    while (BFS(s, t) == true)
    {
        // store how many edges are visited
        // from V { 0 to V }
        int *start = new int[V+1];

```

```

    // while flow is not zero in graph from S to D
    while (int flow = sendFlow(s, INT_MAX, t, start))

        // Add path flow to overall flow
        total += flow;
    }

    // return maximum flow
    return total;
}

// Driver program to test above functions
int main()
{
    Graph g(6);
    g.addEdge(0, 1, 16 );
    g.addEdge(0, 2, 13 );
    g.addEdge(1, 2, 10 );
    g.addEdge(1, 3, 12 );
    g.addEdge(2, 1, 4 );
    g.addEdge(2, 4, 14);
    g.addEdge(3, 2, 9 );
    g.addEdge(3, 5, 20 );
    g.addEdge(4, 3, 7 );
    g.addEdge(4, 5, 4);

    // next exmp
    /*g.addEdge(0, 1, 3 );
    g.addEdge(0, 2, 7 );
    g.addEdge(1, 3, 9);
    g.addEdge(1, 4, 9 );
    g.addEdge(2, 1, 9 );
    g.addEdge(2, 4, 9);
    g.addEdge(2, 5, 4);
    g.addEdge(3, 5, 3);
    g.addEdge(4, 5, 7 );
    g.addEdge(0, 4, 10);

    // next exp
    g.addEdge(0, 1, 10);
    g.addEdge(0, 2, 10);
    g.addEdge(1, 3, 4 );
    g.addEdge(1, 4, 8 );
    g.addEdge(1, 2, 2 );
    g.addEdge(2, 4, 9 );
    g.addEdge(3, 5, 10 );

```

```

    g.addEdge(4, 3, 6 );
    g.addEdge(4, 5, 10 ); */

    cout << "Maximum flow" << g.DinicMaxflow(0, 5);
    return 0;
}

```

Edmond's algorithm (unweighted general matching)

```

// Unweighted general matching.
// Vertices are numbered from 1 to V.
// G is an adjlist.
// G[x][0] contains the number of neighbours of x.
// The neighbours are then stored in G[x][1] .. G[x][G[x][0]].
// Mate[x] will contain the matching node for x.
// V and E are the number of edges and vertices.
// Slow Version (2x on random graphs) of Gabow's implementation
// of Edmonds' algorithm ( $O(V^3)$ ).
const int MAXV = 250;
int G[MAXV][MAXV];
int VLabel[MAXV];
int Queue[MAXV];
int Mate[MAXV];
int Save[MAXV];
int Used[MAXV];
int Up, Down;
int V;

void ReMatch(int x, int y)
{
    int m = Mate[x]; Mate[x] = y;
    if (Mate[m] == x)
    {
        if (VLabel[x] <= V)
        {
            Mate[m] = VLabel[x];
            ReMatch(VLabel[x], m);
        }
    }
    else
    {
        int a = 1 + (VLabel[x] - V - 1) / V;
        int b = 1 + (VLabel[x] - V - 1) % V;
        ReMatch(a, b); ReMatch(b, a);
    }
}

```

```

    }
}

void Traverse(int x)
{
    for (int i = 1; i <= V; i++) Save[i] = Mate[i];
    ReMatch(x, x);
    for (int i = 1; i <= V; i++)
    {
        if (Mate[i] != Save[i]) Used[i]++;
        Mate[i] = Save[i];
    }
}

void ReLabel(int x, int y)
{
    for (int i = 1; i <= V; i++) Used[i] = 0;
    Traverse(x); Traverse(y);
    for (int i = 1; i <= V; i++)
    {
        if (Used[i] == 1 && VLabel[i] < 0)
        {
            VLabel[i] = V + x + (y - 1) * V;
            Queue[Up++] = i;
        }
    }
}

// Call this after constructing G
void Solve()
{
    for (int i = 1; i <= V; i++)
        if (Mate[i] == 0)
        {
            for (int j = 1; j <= V; j++) VLabel[j] = -1;
            VLabel[i] = 0; Down = 1; Up = 1; Queue[Up++] = i;
            while (Down != Up)
            {
                int x = Queue[Down++];
                for (int p = 1; p <= G[x][0]; p++)
                {
                    int y = G[x][p];
                    if (Mate[y] == 0 && i != y)
                    {
                        Mate[y] = x; ReMatch(x, y);

```

```

                        Down = Up; break;
                    }
                if (VLabel[y] >= 0)
                {
                    ReLabel(x, y);
                    continue;
                }
                if (VLabel[Mate[y]] < 0)
                {
                    VLabel[Mate[y]] = x;
                    Queue[Up++] = Mate[y];
                }
            }
        }
    }

// Call this after Solve(). Returns number of edges in matching (half the
// number of matched vertices)
int Size()
{
    int Count = 0;
    for (int i = 1; i <= V; i++)
        if (Mate[i] > i) Count++;
    return Count;
}

```

Link cut tree

```

struct node_t {
    node_t();
    node_t *ch[2], *p;
    int size, root;
    int dir() { return this == p->ch[1]; }
    void setc(node_t *c, int d) { ch[d] = c, c->p = this; }
    void update() { size = ch[0]->size + ch[1]->size + 1; }
} s[maxn], *nil = s;

node_t::node_t() {
    size = 1, root = true;
    ch[0] = ch[1] = p = nil;
}

```



```

void rotate(node_t *t) {
    node_t *p = t->p;
    int d = t->dir();
    if (!p->root) {
        p->p->setc(t, p->dir());
    } else {
        p->root = false, t->root = true;
        t->p = p->p; // Path Parent
    }
    p->setc(t->ch[!d], d);
    t->setc(p, !d);
    p->update(), t->update();
}

void splay(node_t *t) {
    // t->update(); // tag!
    while (!t->root) {
        // if (!t->p->root) t->p->p->update(); t->p->update(), t->update(); // !
        if (!t->p->root) rotate(t->dir() == t->p->dir() ? t->p : t);
        rotate(t);
    }
}

void access(node_t *x) { // Ask u, v: access(u), access(v, true), x = LCA
    node_t *y = nil;
    while (x != nil) {
        splay(x);
        // if (x->p == nil) at second call, x->ch[1](rev) + (x)_single + y
        x->ch[1]->root = true;
        x->ch[1] = y, y->root = false;
        x->update();
        y = x, x = x->p;
    }
}

void cut(node_t *x) {
    access(x);
    splay(x);
    x->ch[0]->root = true;
    x->ch[0]->p = nil;
    x->ch[0] = nil;
}

void link(node_t *x, node_t *y) {
    access(y);
    splay(y);

```

```

    y->p = x;
    access(y);
}

void init() { nil->size = 0; }

```

4 Strings

KMP (linear string search)

```

typedef vector<int> VI;

void buildTable(string& w, VI& t)
{
    t = VI(w.length());
    int i = 2, j = 0;
    t[0] = -1; t[1] = 0;

    while(i < w.length())
    {
        if(w[i-1] == w[j]) { t[i] = j+1; i++; j++; }
        else if(j > 0) j = t[j];
        else { t[i] = 0; i++; }
    }
}

int KMP(string& s, string& w)
{
    int m = 0, i = 0;
    VI t;

    buildTable(w, t);
    while(m+i < s.length())
    {
        if(w[i] == s[m+i])
        {
            i++;
            if(i == w.length()) return m;
        }
        else
        {
            m += i-t[i];
            if(i > 0) i = t[i];
        }
    }
}

```

```

    }
}
return s.length();
}

```

Manacher (max palindrome substring)

```

// Manacher's algorithm: finds maximal palindrome lengths centered around each
// position in a string (including positions between characters) and returns
// them in left-to-right order of centres. Linear time.
// Ex: "opposes" -> [0, 1, 0, 1, 4, 1, 0, 1, 0, 1, 0, 3, 0, 1, 0]
vector<int> fastLongestPalindromes(string str) {
    int i=0,j,d,s,e,lLen,palLen=0;
    vector<int> res;
    while (i < str.length()) {
        if (i > palLen && str[i-palLen-1] == str[i]) {
            palLen += 2; i++; continue;
        }
        res.push_back(palLen);
        s = res.size()-2;
        e = s-palLen;
        bool b = true;
        for (j=s; j>e; j--) {
            d = j-e-1;
            if (res[j] == d) { palLen = d; b = false; break; }
            res.push_back(min(d, res[j]));
        }
        if (b) { palLen = 1; i++; }
    }
    res.push_back(palLen);
    lLen = res.size();
    s = lLen-2;
    e = s-(2*str.length()+1-lLen);
    for (i=s; i>e; i--) { d = i-e-1; res.push_back(min(d, res[i])); }
    return res;
}

```

Suffix array

// Suffix array construction in $O(L \log^2 L)$ time. Routine for

```

// computing the length of the longest common prefix of any two
// suffixes in  $O(\log L)$  time.
//
// INPUT:   string s
//
// OUTPUT:  array suffix[] such that suffix[i] = index (from 0 to L-1)
//           of substring s[i...L-1] in the list of sorted suffixes.
//           That is, if we take the inverse of the permutation suffix[],
//           we get the actual suffix array.
struct SuffixArray {
    const int L;
    string s;
    vector<vector<int> > P;
    vector<pair<pair<int,int>,int> > M;

    SuffixArray(const string &s) : L(s.length()), s(s), P(1, vector<int>(L, 0)),
        M(L) {
        for (int i = 0; i < L; i++) P[0][i] = int(s[i]);
        for (int skip = 1, level = 1; skip < L; skip *= 2, level++) {
            P.push_back(vector<int>(L, 0));
            for (int i = 0; i < L; i++)
                M[i] = make_pair(make_pair(P[level-1][i], i + skip < L ? P[level-1][i + skip] : -1000), i);
            sort(M.begin(), M.end());
            for (int i = 0; i < L; i++)
                P[level][M[i].second] = (i > 0 && M[i].first == M[i-1].first) ? P[level][M[i-1].second] : i;
        }
    }

    vector<int> GetSuffixArray() { return P.back(); }

    // returns the length of the longest common prefix of s[i...L-1] and s[j...L-1]
    int LongestCommonPrefix(int i, int j) {
        int len = 0;
        if (i == j) return L - i;
        for (int k = P.size() - 1; k >= 0 && i < L && j < L; k--) {
            if (P[k][i] == P[k][j]) {
                i += 1 << k;
                j += 1 << k;
                len += 1 << k;
            }
        }
        return len;
    }
}

```

```
};
```

5 Math

Chinese Remainder Theorem

```
/* Extended Euclidean Algorithm
 * find x, y s.t. ax+by=gcd(a,b)
 */
void eea(int a, int b, int &x, int &y) {
    int r[3] = {a, b}, s[3] = {1, 0}, t[3] = {0, 1};
    while (r[1]) {
        int q = r[0] / r[1];
        r[2] = r[0] - q * r[1];
        s[2] = s[0] - q * s[1];
        t[2] = t[0] - q * t[1];
        r[0] = r[1]; r[1] = r[2];
        s[0] = s[1]; s[1] = s[2];
        t[0] = t[1]; t[1] = t[2];
    }
    x = s[0]; y = t[0];
}

/* Chinese Remainder Theorem
 * find x s.t. x = a[i] mod b[i]
 */
int crt(int *a, int *b, int n) {
    int B = 1;
    for (int i = 0; i < n; ++i)
        B *= b[i];
    int x = 0;
    for (int i = 0; i < n; ++i) {
        int c, d;
        eea(b[i], B / b[i], c, d);
        x = (x + B / b[i] * d * a[i]) % B;
    }
    x = (x + B) % B;
    return x;
}
```

Fast Fourier Transform

```
typedef complex<double> cd;

int const NMAX = 1 << 9;
double const PI2 = atan(1.0) * 8;
cd a[NMAX], b[NMAX];

// fft(src, num, stride, dst, nth root of unity)
// e.g. fft(a, n, 1, b, polar(1.0, -PI2 / n))
void fft(cd *a, int n, int s, cd *b, cd unit) {
    if (n == 1) {
        *b = *a;
        return;
    }
    int nh = n / 2;
    fft(a, nh, s * 2, b, unit * unit);
    fft(a + s, nh, s * 2, b + nh, unit * unit);
    cd coef = 1;
    for (int i = 0; i < nh; ++i) {
        cd ofs = coef * b[i + nh];
        b[i + nh] = b[i] - ofs;
        b[i] = b[i] + ofs;
        coef *= unit;
    }
}
```

Simplex Algorithm (Linear programming)

```
// Two-phase simplex algorithm for solving linear programs of the form
//
//      maximize      c^T x
//      subject to    Ax <= b
//                   x >= 0
//
// INPUT: A -- an m x n matrix
//         b -- an m-dimensional vector
//         c -- an n-dimensional vector
//         x -- a vector where the optimal solution will be stored
//
// OUTPUT: value of the optimal solution (infinity if unbounded
//         above, nan if infeasible)
//
```

```
// To use this code, create an LPSolver object with A, b, and c as
// arguments. Then, call Solve(x).
```

```
typedef long double DOUBLE;
typedef vector<DOUBLE> VD;
typedef vector<VD> VVD;
typedef vector<int> VI;
```

```
const DOUBLE EPS = 1e-9;
```

```
struct LPSolver {
```

```
    int m, n;
    VI B, N;
    VVD D;
```

```
    LPSolver(const VVD &A, const VD &b, const VD &c) :
```

```
        m(b.size()), n(c.size()), N(n+1), B(m), D(m+2, VD(n+2)) {
        for (int i = 0; i < m; i++) for (int j = 0; j < n; j++) D[i][j] = A[i][j];
        for (int i = 0; i < m; i++) { B[i] = n+i; D[i][n] = -1; D[i][n+1] = b[i];
        }
        for (int j = 0; j < n; j++) { N[j] = j; D[m][j] = -c[j]; }
        N[n] = -1; D[m+1][n] = 1;
    }
}
```

```
void Pivot(int r, int s) {
```

```
    DOUBLE inv = 1.0 / D[r][s];
    for (int i = 0; i < m+2; i++) if (i != r)
        for (int j = 0; j < n+2; j++) if (j != s)
            D[i][j] -= D[r][j] * D[i][s] * inv;
    for (int j = 0; j < n+2; j++) if (j != s) D[r][j] *= inv;
    for (int i = 0; i < m+2; i++) if (i != r) D[i][s] *= -inv;
    D[r][s] = inv;
    swap(B[r], N[s]);
}
```

```
bool Simplex(int phase) {
```

```
    int x = phase == 1 ? m+1 : m;
    while (true) {
        int s = -1;
        for (int j = 0; j <= n; j++) {
            if (phase == 2 && N[j] == -1) continue;
            if (s == -1 || D[x][j] < D[x][s] || D[x][j] == D[x][s] && N[j] < N[s])
                s = j;
        }
        if (s < 0 || D[x][s] > -EPS) return true;
        int r = -1;
```

```
        for (int i = 0; i < m; i++) {
            if (D[i][s] < EPS) continue;
            if (r == -1 || D[i][n+1] / D[i][s] < D[r][n+1] / D[r][s] ||
                D[i][n+1] / D[i][s] == D[r][n+1] / D[r][s] && B[i] < B[r]) r = i;
        }
        if (r == -1) return false;
        Pivot(r, s);
    }
}
```

```
DOUBLE Solve(VD &x) {
```

```
    int r = 0;
    for (int i = 1; i < m; i++) if (D[i][n+1] < D[r][n+1]) r = i;
    if (D[r][n+1] <= -EPS) {
        Pivot(r, n);
        if (!Simplex(1) || D[m+1][n+1] < -EPS) return -numeric_limits<DOUBLE>::
            infinity();
        for (int i = 0; i < m; i++) if (B[i] == -1) {
            int s = -1;
            for (int j = 0; j <= n; j++)
                if (s == -1 || D[i][j] < D[i][s] || D[i][j] == D[i][s] && N[j] < N[s])
                    s = j;
            Pivot(i, s);
        }
    }
    if (!Simplex(2)) return numeric_limits<DOUBLE>::infinity();
    x = VD(n);
    for (int i = 0; i < m; i++) if (B[i] < n) x[B[i]] = D[i][n+1];
    return D[m][n+1];
}
};
```

Gaussian elimination

```
// Gauss-Jordan elimination with full pivoting.
// Uses:
// (1) solving systems of linear equations (AX=B)
// (2) inverting matrices (AX=I)
// (3) computing determinants of square matrices
//
// Running time: O(n^3)
//
// INPUT:    a[][] = an nxn matrix
```

```
//          b[][] = an nxm matrix
//          A MUST BE INVERTIBLE!
//
// OUTPUT:  X          = an nxm matrix (stored in b[][])
//          A^{-1} = an nxn matrix (stored in a[][])
//          returns determinant of a[][]

const double EPS = 1e-10;

typedef vector<int> VI;
typedef double T;
typedef vector<T> VT;
typedef vector<VT> VVT;

T GaussJordan(VVT &a, VVT &b) {
    const int n = a.size();
    const int m = b[0].size();
    VI irow(n), icol(n), ipiv(n);
    T det = 1;

    for (int i = 0; i < n; i++) {
        int pj = -1, pk = -1;
        for (int j = 0; j < n; j++) if (!ipiv[j])
            for (int k = 0; k < n; k++) if (!ipiv[k])
                if (pj == -1 || fabs(a[j][k]) > fabs(a[pj][pk])) { pj = j; pk = k; }
        if (fabs(a[pj][pk]) < EPS) { return 0; }
        ipiv[pk]++;
        swap(a[pj], a[pk]);
        swap(b[pj], b[pk]);
        if (pj != pk) det *= -1;
        irow[i] = pj;
        icol[i] = pk;

        T c = 1.0 / a[pk][pk];
        det *= a[pk][pk];
        a[pk][pk] = 1.0;
        for (int p = 0; p < n; p++) a[pk][p] *= c;
        for (int p = 0; p < m; p++) b[pk][p] *= c;
        for (int p = 0; p < n; p++) if (p != pk) {
            c = a[p][pk];
            a[p][pk] = 0;
            for (int q = 0; q < n; q++) a[p][q] -= a[pk][q] * c;
            for (int q = 0; q < m; q++) b[p][q] -= b[pk][q] * c;
        }
    }
}
```

```
for (int p = n-1; p >= 0; p--) if (irow[p] != icol[p]) {
    for (int k = 0; k < n; k++) swap(a[k][irow[p]], a[k][icol[p]]);
}

return det;
}
```

Karatsuba multiplication

```
class Karatsuba {
    typedef typename vector<T>::iterator vTi;
    int cut;
    void convolve_naive(vTi a, vTi b, vTi c, int n) {
        int n2 = n * 2;
        for (int i = 0; i < n2; ++i)
            c[i] = 0;
        for (int i = 0; i < n; ++i)
            for (int j = 0; j < n; ++j)
                c[i + j] += a[i] * b[j];
    }
    /*
    * v----d----v                                v-dh-v
    * -----
    * | a1 * b1 | ah * bh | as * bs |           |         | as | bs |
    * -----
    * ^x0  ^xh  ^x1          ^x2
    */
    void karatsuba(vTi a, vTi b, vTi c, int n) {
        if (n <= cut) {
            convolve_naive(a, b, c, n);
            return;
        }
        int nh = n / 2;
        vTi al = a, ah = a + nh, as = c + nh * 10;
        vTi bl = b, bh = b + nh, bs = c + nh * 11;
        vTi x0 = c, x1 = c + n, x2 = c + n * 2, xh = c + nh;
        for (int i = 0; i < nh; ++i) {
            as[i] = al[i] + ah[i];
            bs[i] = bl[i] + bh[i];
        }
        karatsuba(al, bl, x0, nh);
        karatsuba(ah, bh, x1, nh);
        karatsuba(as, bs, x2, nh);
    }
}
```

```
    for (int i = 0; i < n; ++i) x2[i] -= x0[i] + x1[i];
    for (int i = 0; i < n; ++i) xh[i] += x2[i];
}
public:
    Karatsuba(int _cut = 1 << 5) : cut(_cut) {}
    vector<T> convolve(vector<T> &_a, vector<T> &_b) {
        vector<T> a = _a, b = _b, c;
        int sz = max(a.size(), b.size()), sz2;
        for (sz2 = 1; sz2 < sz; sz2 *= 2);
        a.resize(sz2); b.resize(sz2); c.resize(sz2 * 6);
        karatsuba(a.begin(), b.begin(), c.begin(), sz2);
        c.resize(_a.size() + _b.size() - 1);
        return c;
    }
};
```
