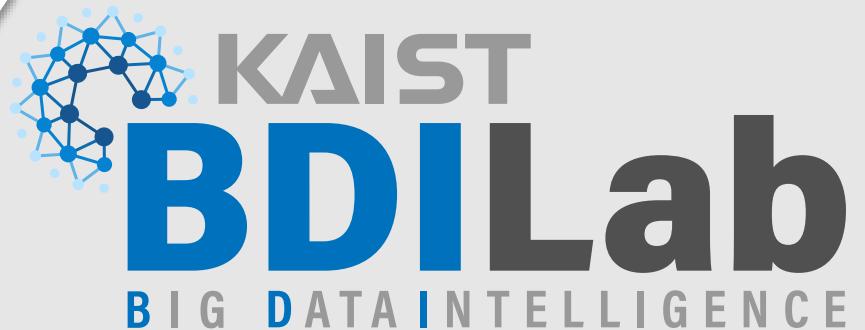


# Lecture#4: Representation Learning on Hyper-relational Knowledge Graphs

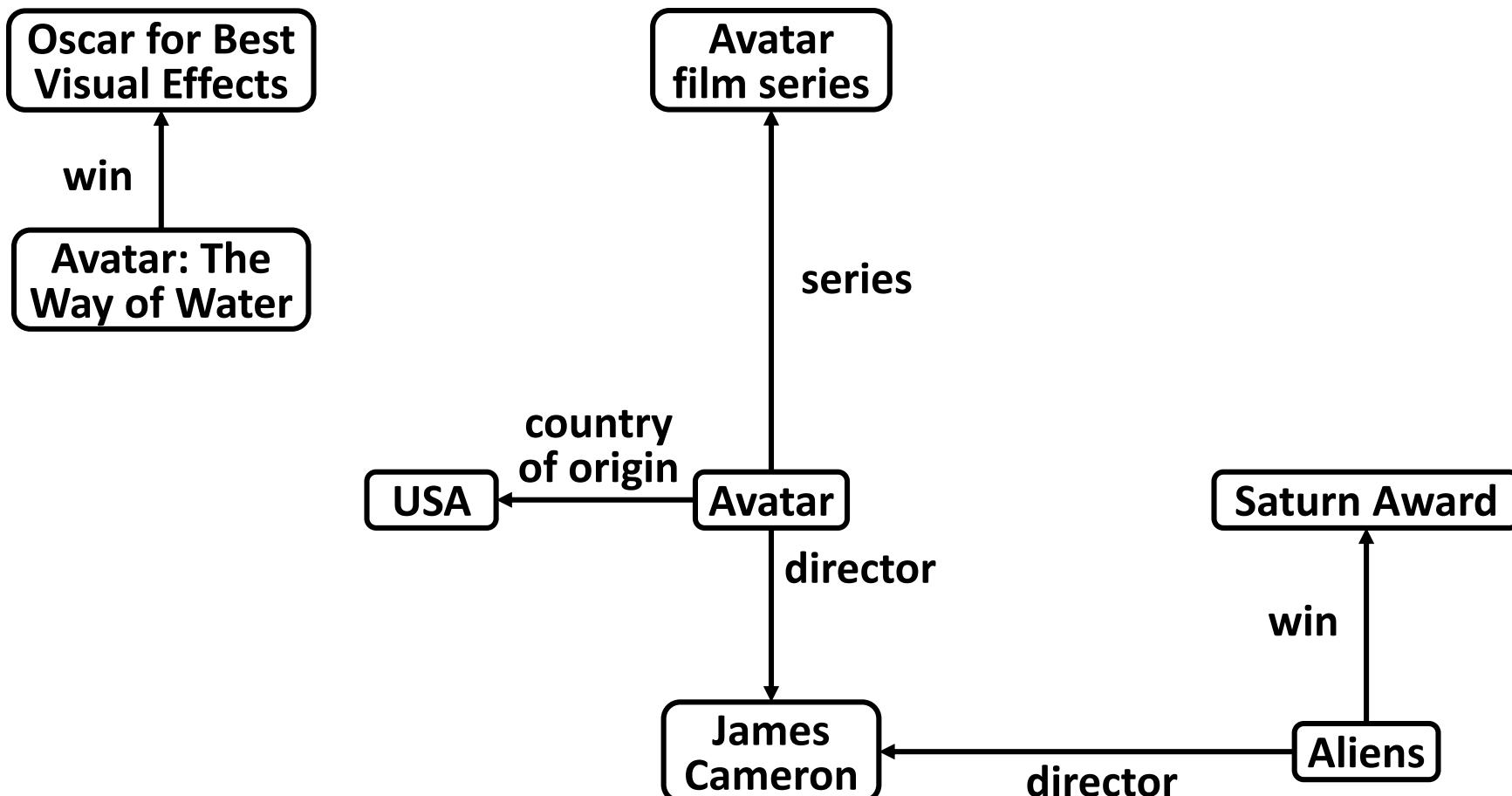
**Joyce Jiyoung Whang**  
School of Computing, KAIST

Key Facets in Modern Knowledge Graph Representation Learning  
([KeyKGRL](#)), ISWC 2025 Tutorial

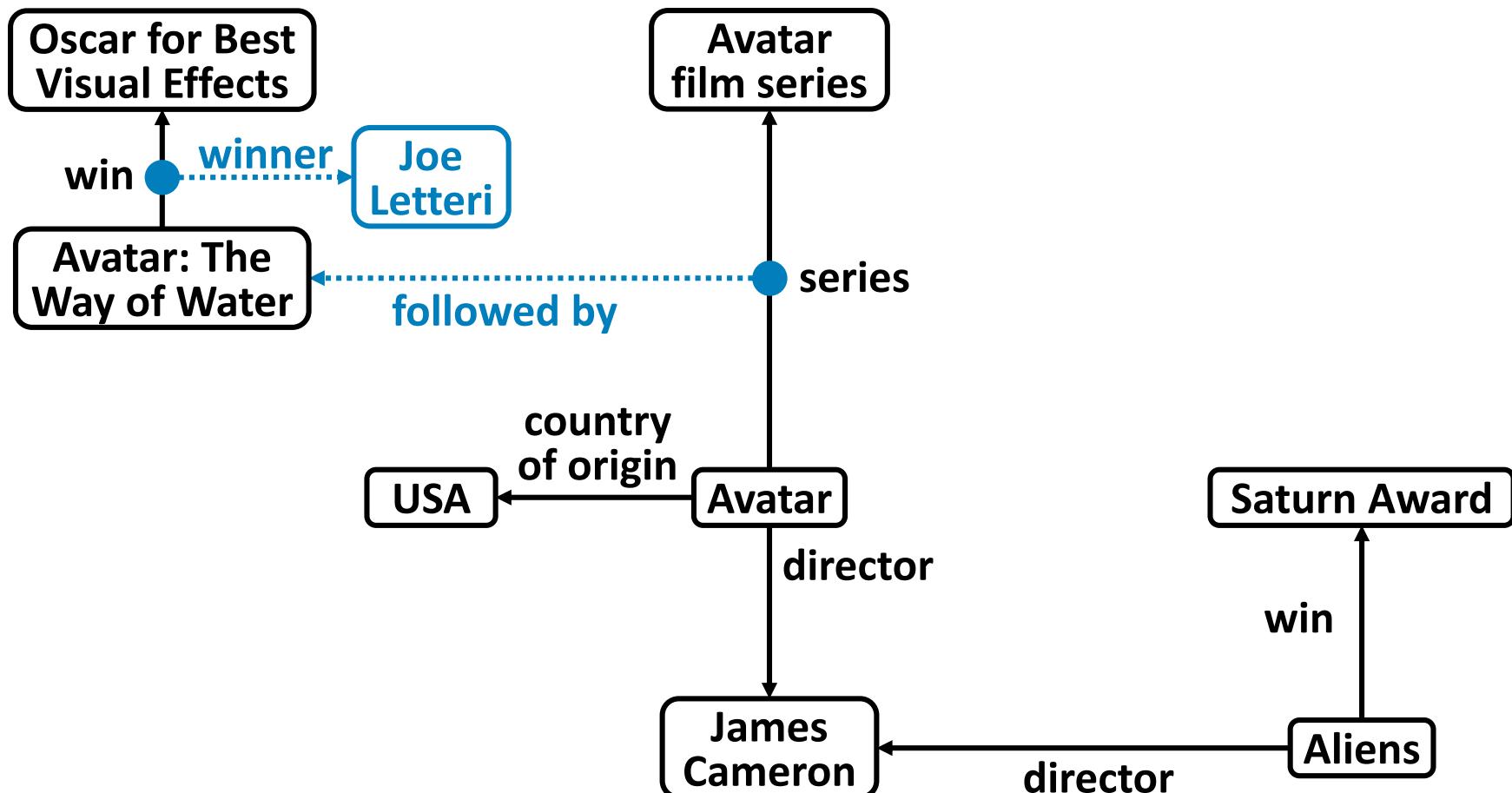
<https://bdi-lab.kaist.ac.kr>



# Knowledge Graphs



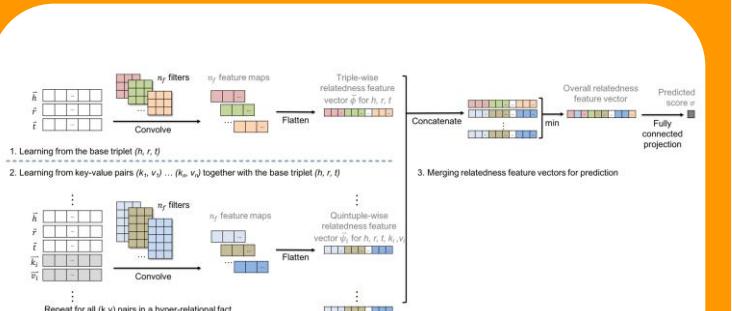
# Hyper-relational Knowledge Graphs (HKGs)



# Representation Learning on HKGs

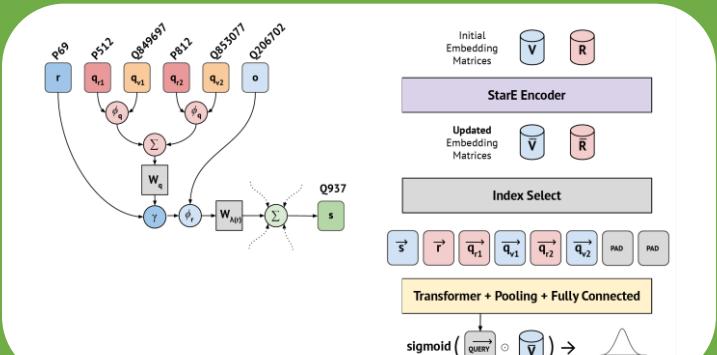
## HINGE (TheWebConf 2020)

- A hyper-relational KG embedding model that directly learns from hyper-relational facts in a KG
- Captures the structural information of the KG encoded in the triplets
  - Also captures the correlation between each triplet and its associated qualifiers



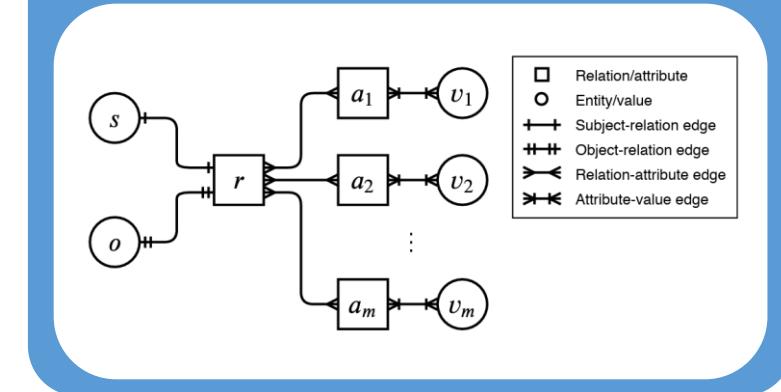
## StarE (EMNLP 2020)

- A message passing based graph encoder that is capable of modeling hyper-relational KGs
- Can encode qualifiers along with the main triplet
- Demonstrates that existing benchmarks for evaluating LP on HKGs suffer from flaws



## GRAN (ACL 2021 Findings)

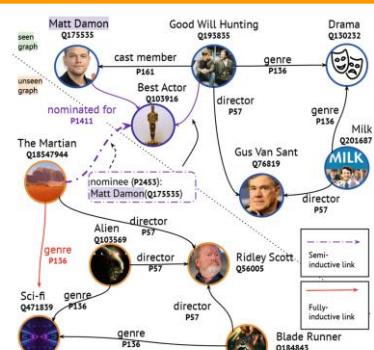
- Represents the structure of a hyper-relational fact as a small heterogeneous graph
  - Models the heterogeneous graph with edge-biased fully-connected attention
- Can fully model global and local dependencies in each fact



# Representation Learning on HKGs

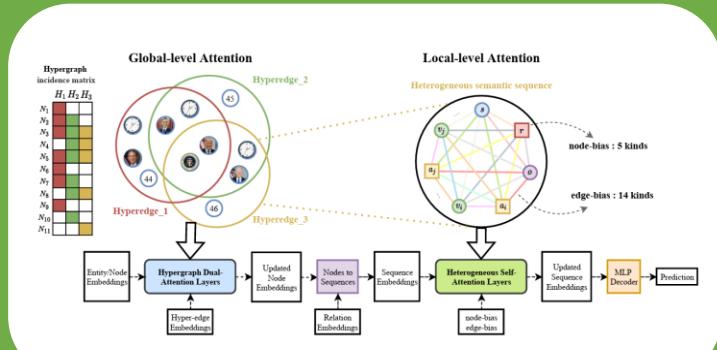
## QBLP (ISWC 2021)

- Proposes a classification of inductive LP scenarios that describes the settings formally
- Adapts two existing baseline models for the inductive LP tasks and probes them into HKGs
- Shows that using hyper-relational facts can improve inductive KGC



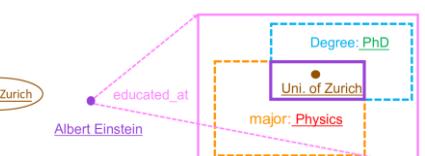
## HAHE (ACL 2023)

- Represents the global structure of HKG as a hypergraph and the local structure as a semantic sequence
- Separately models the graphical structure of HKGs and sequential structure inside facts
- Performs multi-position prediction in hyper-relational KGs



## ShrinkE (ACL 2023)

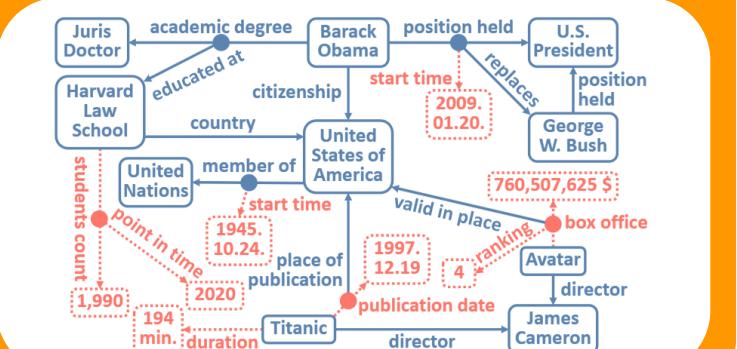
- A geometric HKG embedding method aiming to explicitly model essential inference patterns of facts
- Models a primary triplet as a spatial-functional transformation from the head into a relation-specific box
  - Each qualifier shrinks the box to narrow down the answer set



# Representation Learning on HKGs

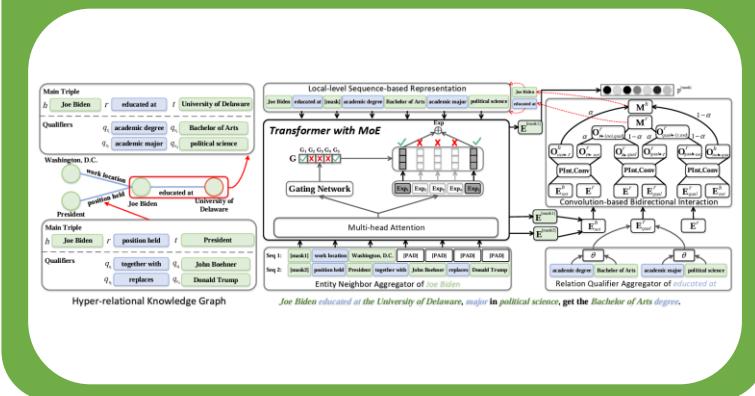
## HyNT (KDD 2023)

- A unified framework that learns representations of a HKG containing numeric literals in triplets/qualifiers
- Reduces the cost of transformers by learning compact representations of triplets and qualifiers
- Predicts missing entities, relations, and numeric values in a HKG



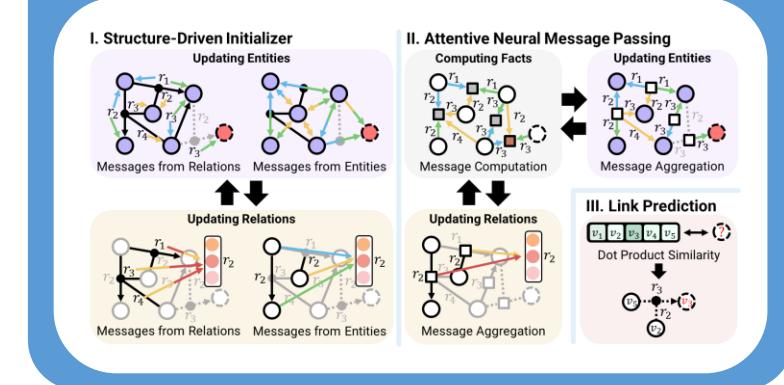
## HyperFormer (CIKM 2023)

- A model that considers local-level sequential information
  - Encodes the content of the entities, relations, and qualifiers of a triplet
- Introduces a Mixture-of-Experts strategy to strengthen the representation capabilities



## MAYPL (ICML 2025)

- Demonstrates that thoroughly leveraging the structure of an HKG is crucial for reasoning on HKGs
- The first structural representation learning method for HKGs that can be applied in both transductive and inductive learning settings

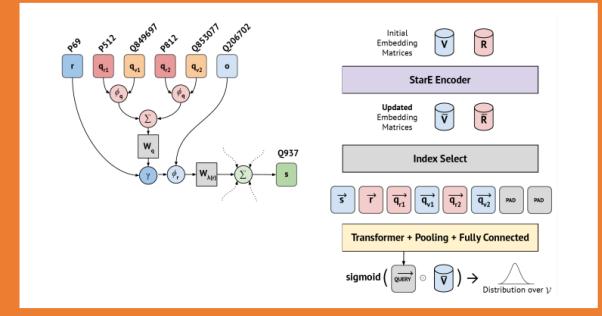




## Message Passing for Hyper-Relational Knowledge Graphs

Mikhail Galkin, Priyansh Trivedi, Gaurav Maheshwari,  
Ricardo Usbeck, and Jens Lehmann

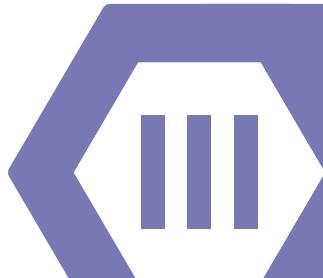
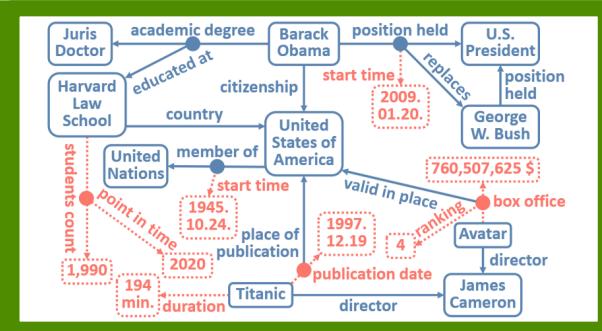
EMNLP 2020



## Representation Learning on Hyper-Relational and Numeric Knowledge Graphs with Transformers

Chanyoung Chung‡, Jaejun Lee‡, and Joyce Jiyoung Whang\*

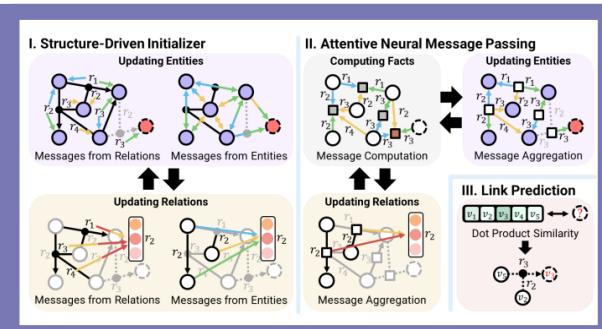
KDD 2023



## Structure Is All You Need: Structural Representation Learning on Hyper-Relational Knowledge Graphs

Jaejun Lee and Joyce Jiyoung Whang\*

ICML 2025

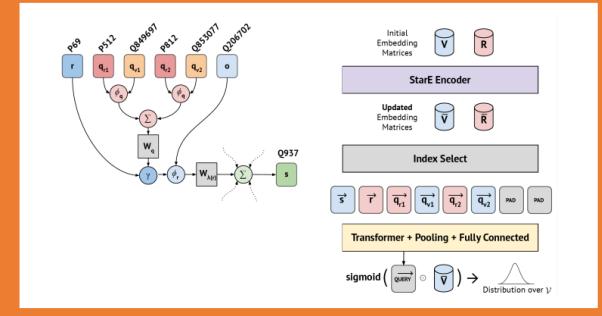




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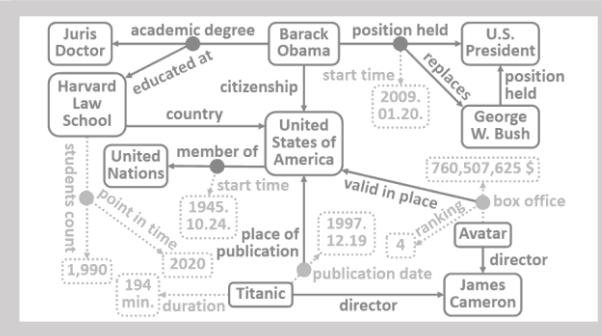
EMNLP 2020



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Chanyoung Chung<sup>†</sup>, Jaejun Lee<sup>‡</sup>, and Joyce Jiyoung Whang<sup>\*</sup>

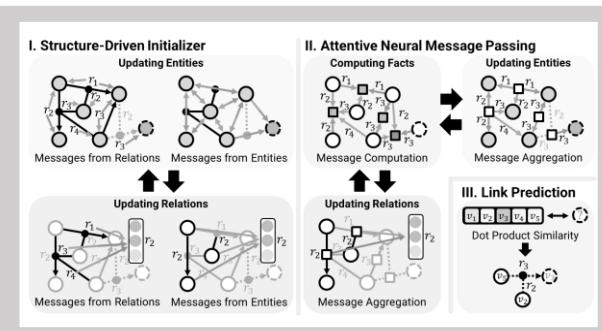
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## Structure Is All You Need: Structural Representation Learning on Hyper-Relational Knowledge Graphs

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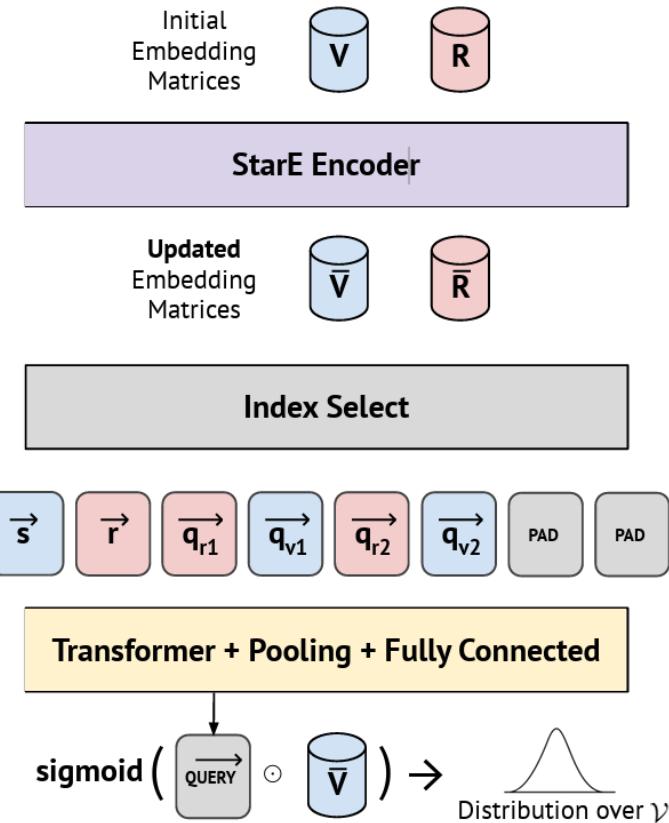
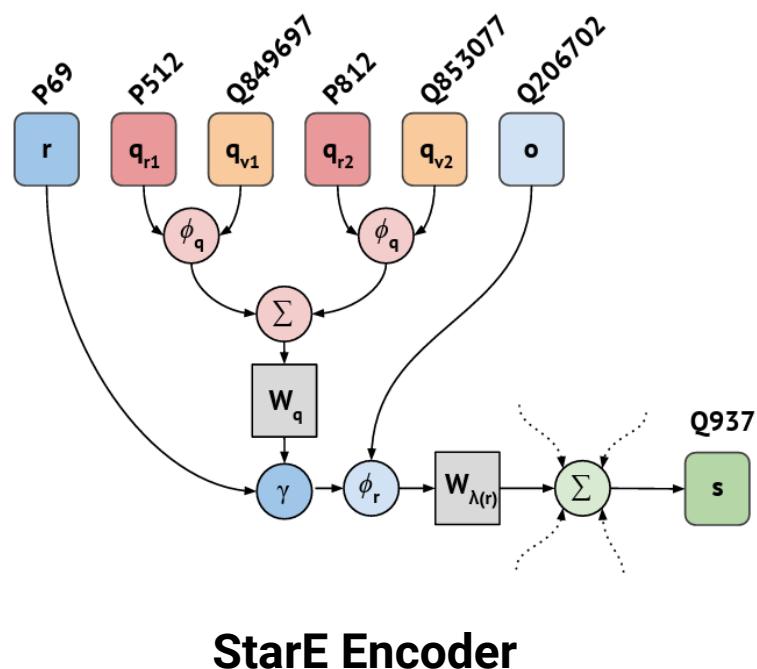
## 02 Motivation

- Existing representation learning approaches for HKGs largely treat a hyper-relational fact as a **n-ary composed relation**
- This may **lose entity-relation attribution** or **ignore the semantic difference** between a triplet relation and qualifier relation
- Some others **decompose a hyper-relational fact** into multiple quintuples comprised of a triplet and one qualifier key-value pair

# Contributions

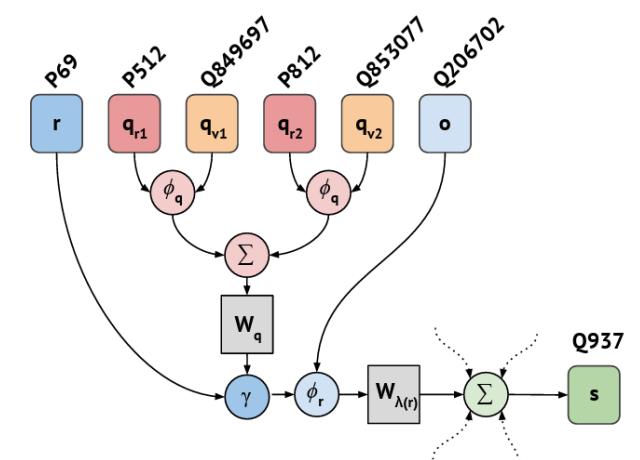
- Propose an alternate graph representation learning mechanism capable of encoding HKGs with an **arbitrary number of qualifiers**, while keeping the **semantic roles of qualifiers and triplets intact**
- Propose **StarE**, a GNN-based approach capable of handling HKGs
- Show that existing benchmarks for link prediction over hyper-relational KGs **exhibit some design flaws**
  - Propose a new hyper-relational link prediction dataset that contains facts with varying amounts of qualifiers

# Overview of StarE



**StarE-based Link  
Prediction Model**

- StarE **incorporates the qualifiers and the primary triplet** into a message passing process
  - Combines the relation embedding  $\mathbf{h}_r$  with a vector  $\mathbf{h}_q$  that represents all qualifiers in the fact
- The qualifier vector  $\mathbf{h}_q$  is obtained by **aggregating representations of the qualifiers**
  - A composition function  $\phi_q$  is used to compute a qualifier representation using the representations of the qualifier entity  $q_v$  and the qualifier relation  $q_r$



- WikiPeople and JF17K are benchmarks for learning representations on HKGs
  - 13% of facts contain a literal in WikiPeople
    - After removing literals, less than 3% of the facts contain qualifier
  - 44.5% of the facts in the test set share the same primary triplet as the facts in the training set in JF17K
- Propose a new dataset, WD50K, extracted from WikiData
  - 14% of facts have at least one qualifier

Dataset	Statements	w/ Quals (%)	Entities	Relations	E in quals	R in quals	Train	Valid	Test
WD50K	236,507	32,167 (13.6%)	47,156	532	5460	45	166,435	23,913	46,159
WikiPeople	369,866	9,482 (2.6%)	34,839	375	416	35	294,439	37,715	37,712
JF17K	100,947	46,320 (45.9%)	28,645	322	3652	180	76,379	-	24,568

# Experiments

Exp #	Method	WikiPeople				JF17K			
		MRR	H@1	H@5	H@10	MRR	H@1	H@5	H@10
1	m-TransH	0.063	0.063	-	0.300	0.206	0.206	-	0.463
1	RAE	0.059	0.059	-	0.306	0.215	0.215	-	0.469
1	NaLP-Fix	0.420	0.343	-	0.556	0.245	0.185	-	0.358
1	HINGE	0.476	<b>0.415</b>	-	0.585	0.449	0.361	-	0.624
1,4	Transformer (H)	0.469	0.403	0.538	0.586	0.512	0.434	0.593	0.665
1,4	STARE (H) + Transformer(H)	<b>0.491</b>	0.398	<b>0.592</b>	<b>0.648</b>	<b>0.574</b>	<b>0.496</b>	<b>0.658</b>	<b>0.725</b>
4	Transformer (T)	0.474	0.419	0.532	0.575	0.537	0.473	0.606	0.663
4	STARE (T) + Transformer (T)	0.493	0.400	0.592	0.648	0.562	0.493	0.637	0.702

Exp #	Dataset →	WD50K		
		Method ↓	MRR	H@1
4	Baseline (Transformer (T))	0.275	0.207	0.404
4	STARE (T) + Transformer(T)	0.308	0.228	0.465
4	NaLP-Fix	0.177	0.131	0.264
4	HINGE	0.243	0.176	0.377
1,2,4	Baseline (Transformer (H))	0.286	0.222	0.406
1,2,4	STARE (H) + Transformer(H)	<b>0.349</b>	<b>0.271</b>	<b>0.496</b>

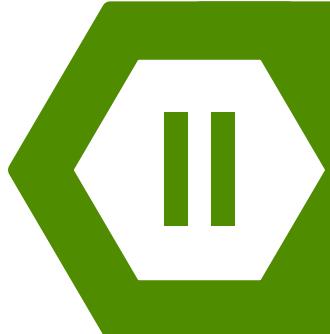
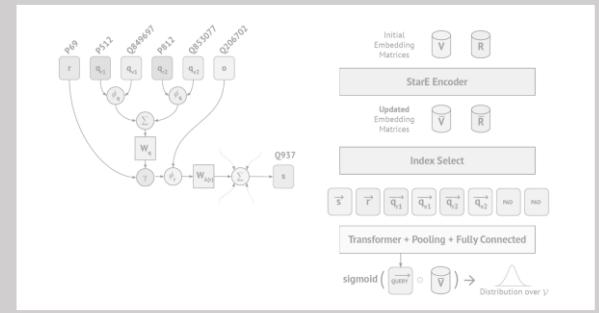
- Present **StarE**, an instance of message passing framework for representation learning over hyper-relational KGs
- StarE performs competitively on link prediction tasks over existing hyper-relational approaches and greatly outperforms triplet-only baselines
- Identify significant **flaws in existing link prediction datasets** and propose WD50K
  - WD50K: Wikidata-based hyper-relational dataset that is closer to real-world graphs and better captures the complexity of the link prediction task on HKGs



## Message Passing for Hyper-Relational Knowledge Graphs

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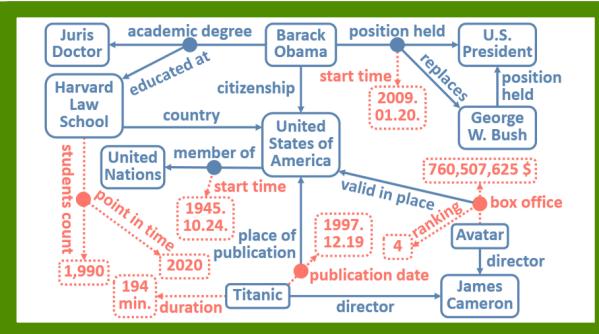
EMNLP 2020



## Representation Learning on Hyper-Relational and Numeric Knowledge Graphs with Transformers

Chanyoung Chung<sup>‡</sup>, Jaejun Lee<sup>‡</sup>, and Joyce Jiyoung Whang<sup>\*</sup>

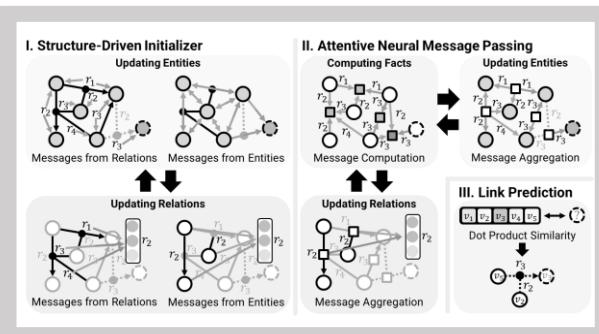
KDD 2023



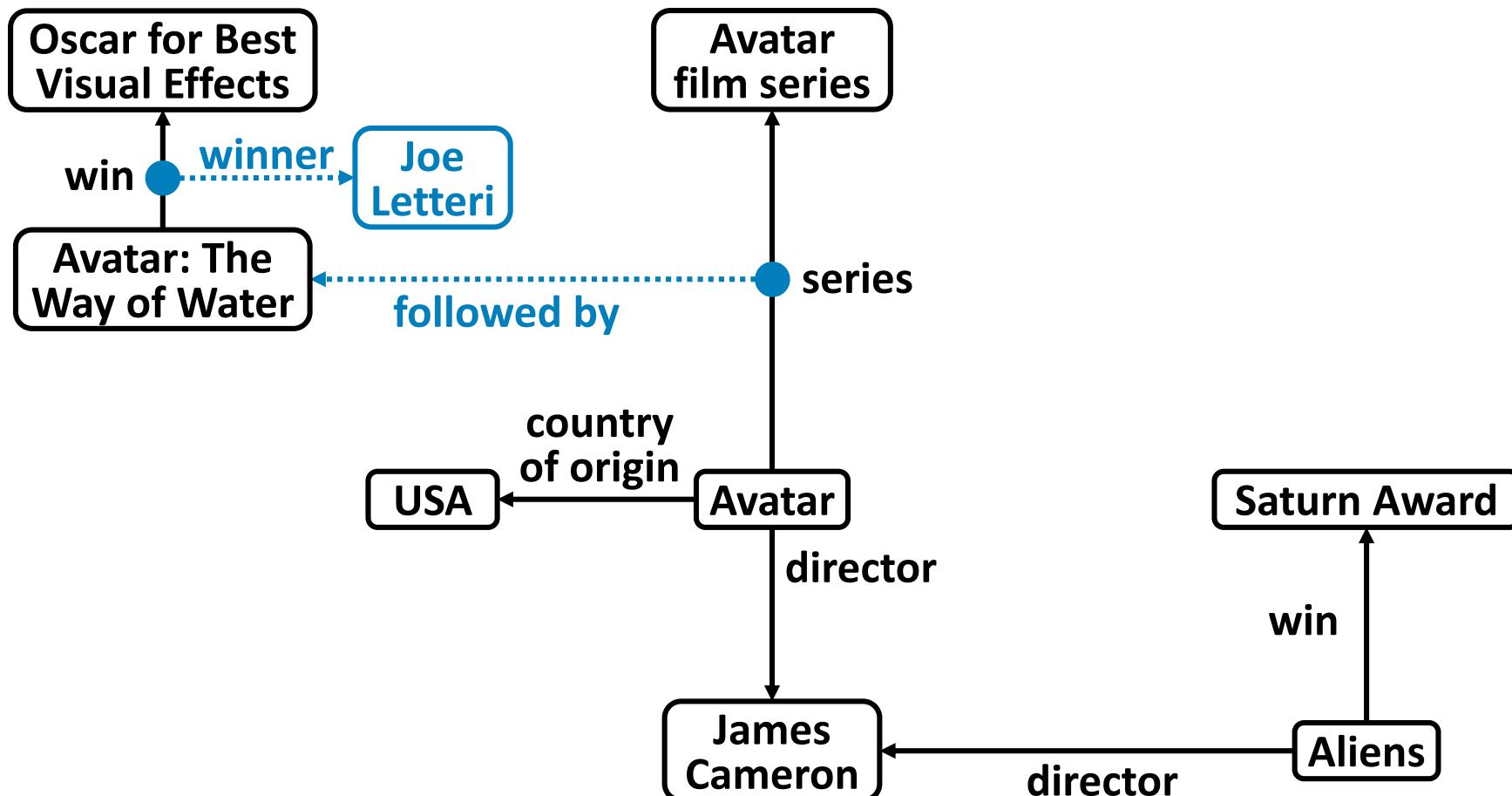
## Structure Is All You Need: Structural Representation Learning on Hyper-Relational Knowledge Graphs

Jaejun Lee and Joyce Jiyoung Whang<sup>\*</sup>

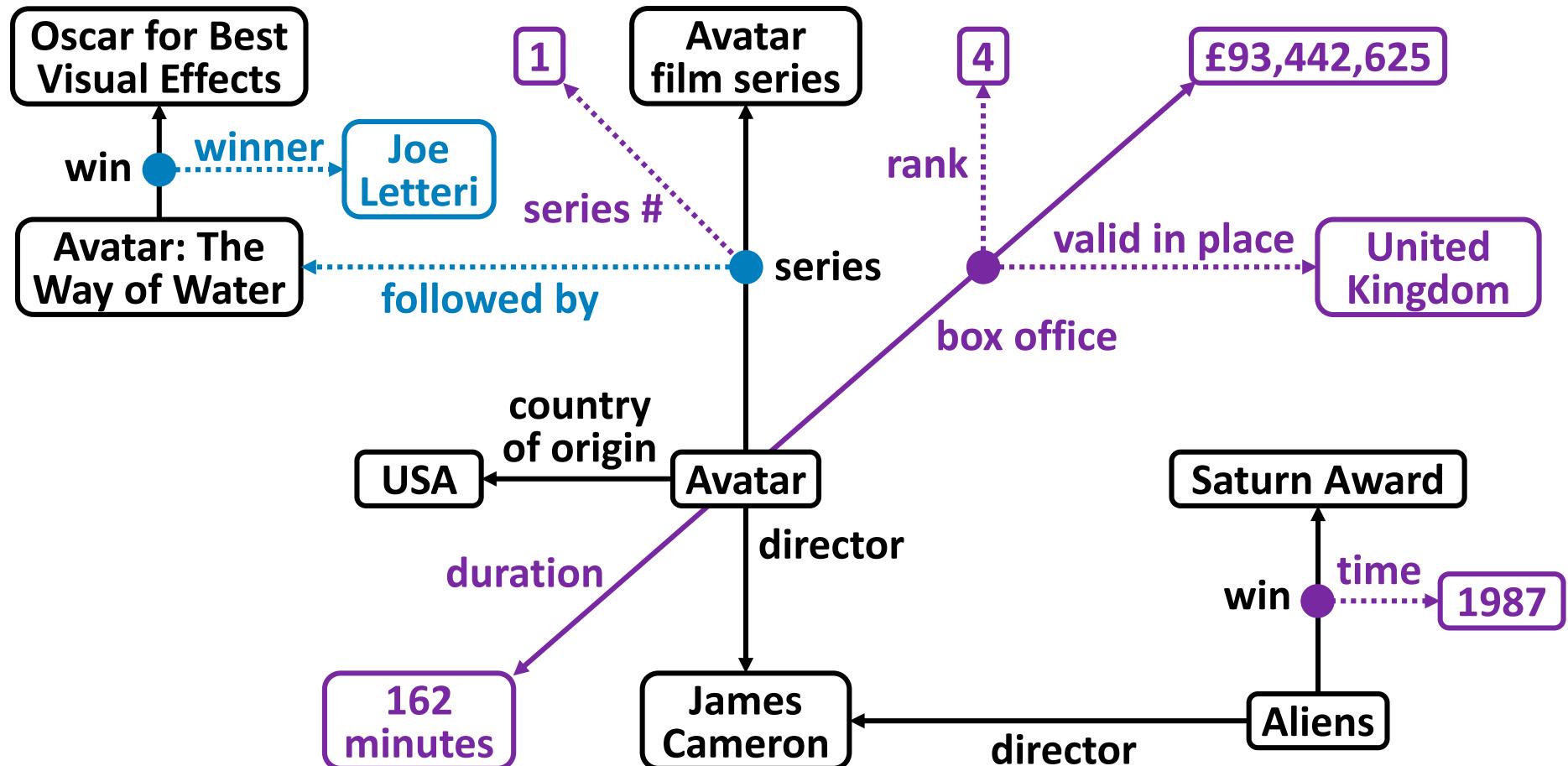
ICML 2025



# Hyper-relational Knowledge Graphs

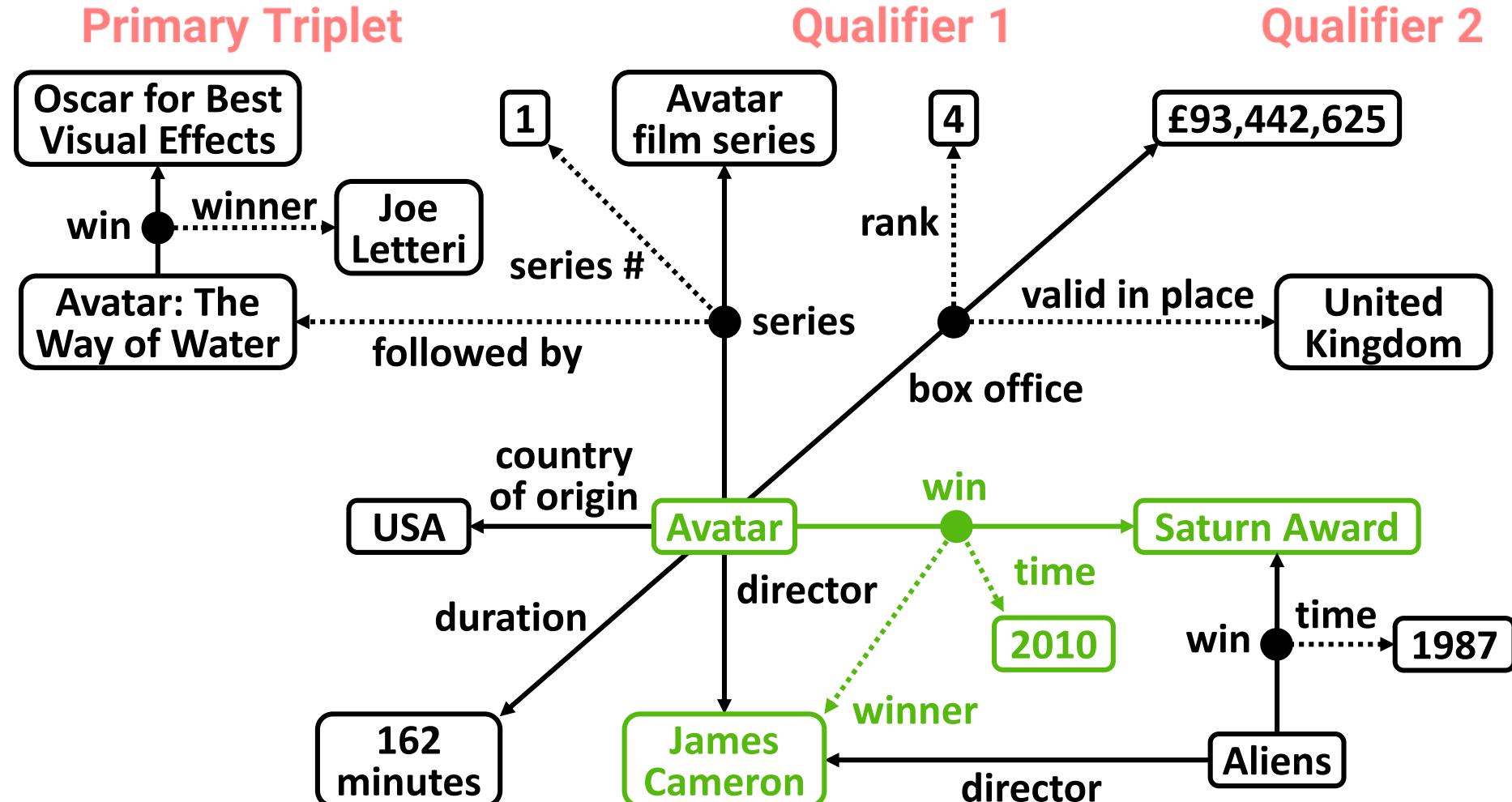


# 03 Hyper-relational and Numeric Knowledge Graphs



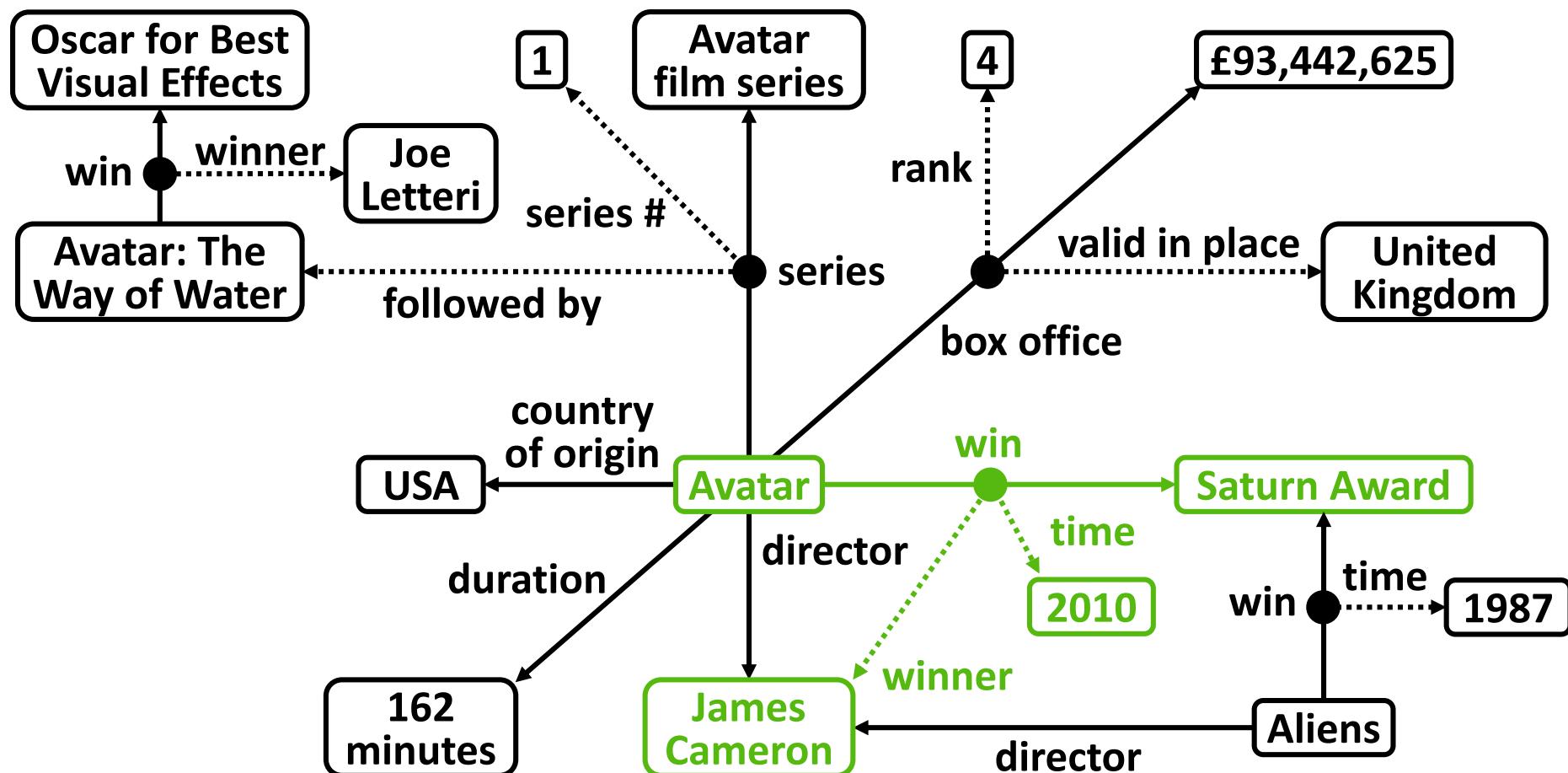
# 03 Hyper-relational and Numeric Knowledge Graphs

((Avatar, win, Saturn\_Award), {winner, James\_Cameron}, (time, 2010))



# Link Prediction on HN-KGs

((Avatar, win, Saturn\_Award), {(winner, James\_Cameron), (time, 2010)})

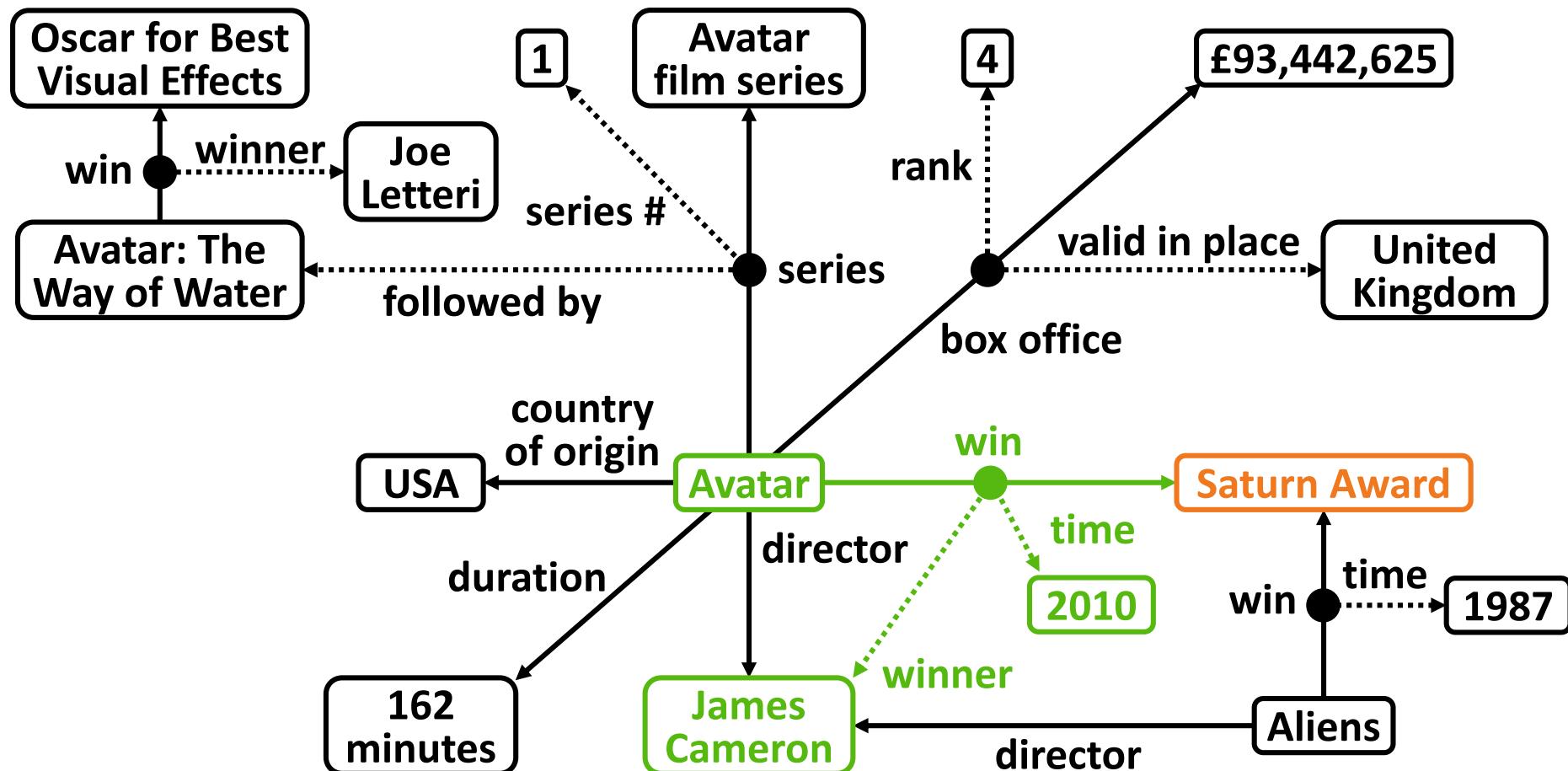


# Link Prediction on HN-KGs

((Avatar, win,

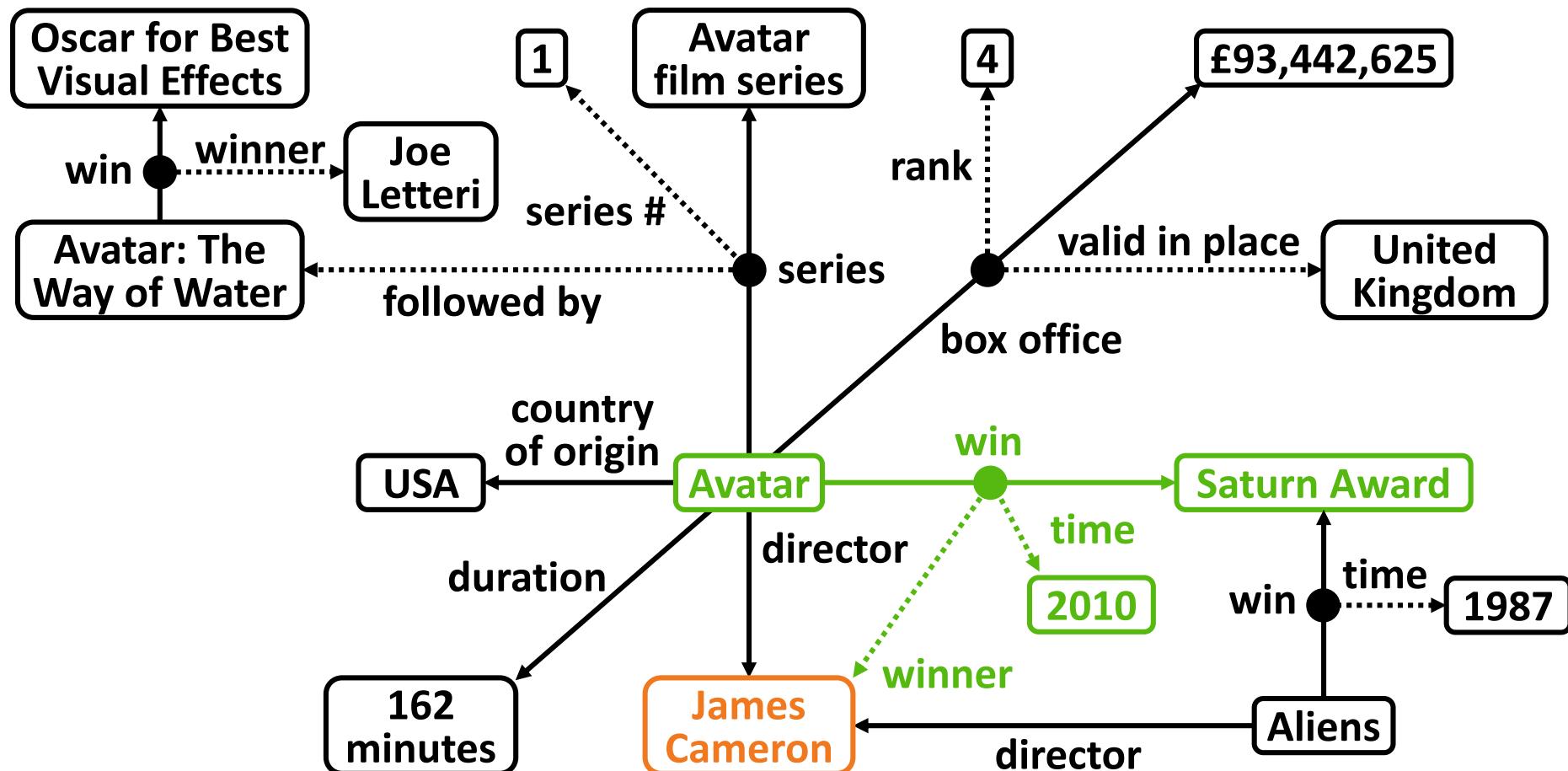
?)

), {((winner, James\_Cameron), (time, 2010))}



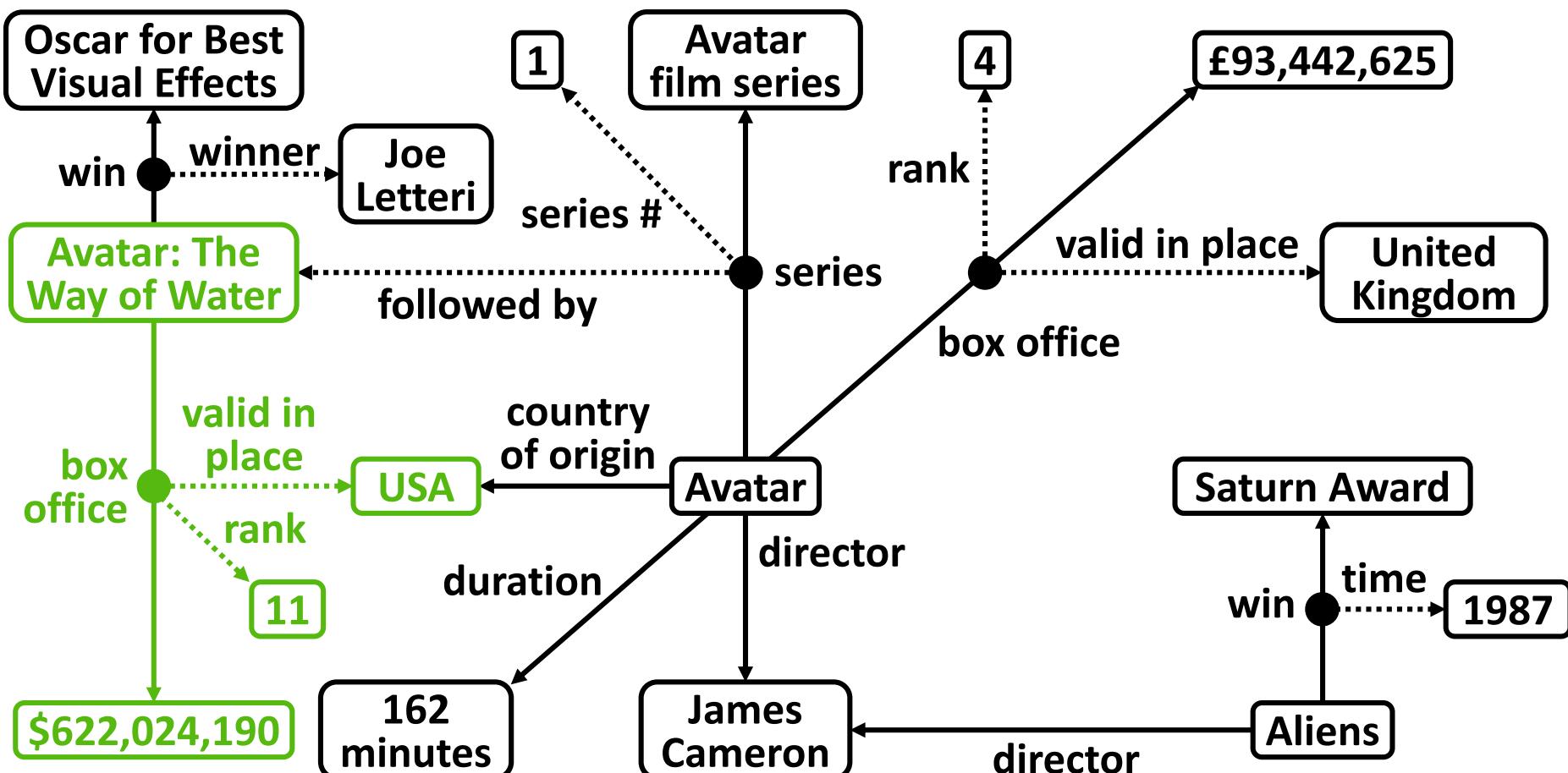
# Link Prediction on HN-KGs

((Avatar, win, Saturn\_Award), {(winner, ?, ), (time, 2010)})



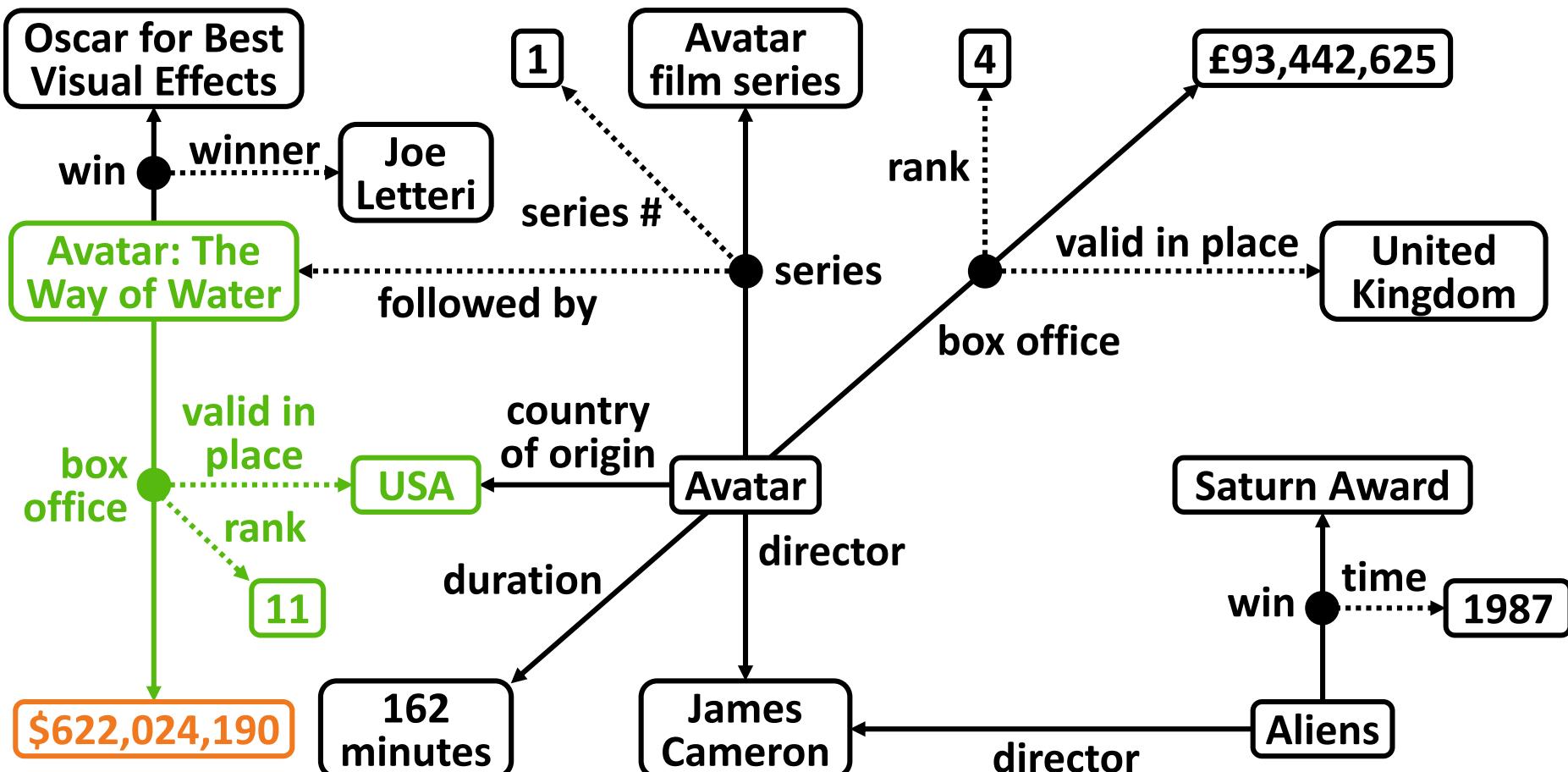
# Numeric Value Prediction on HN-KGs

((Avatar:The\_Way\_of\_Water, box\_office, \$622,024,190), {((rank, 11), (valid\_in\_place, USA))})



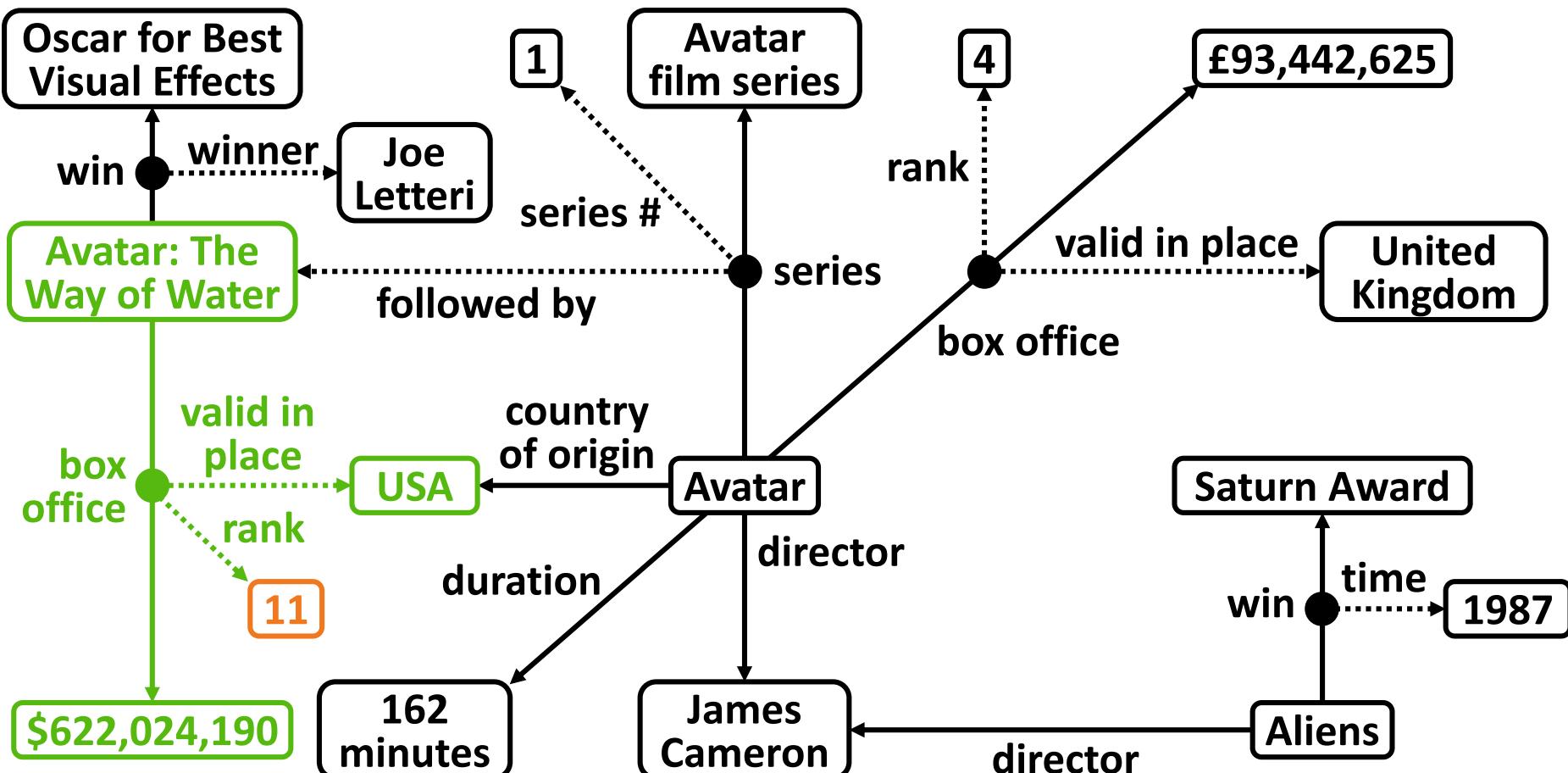
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# Numeric Value Prediction on HN-KGs

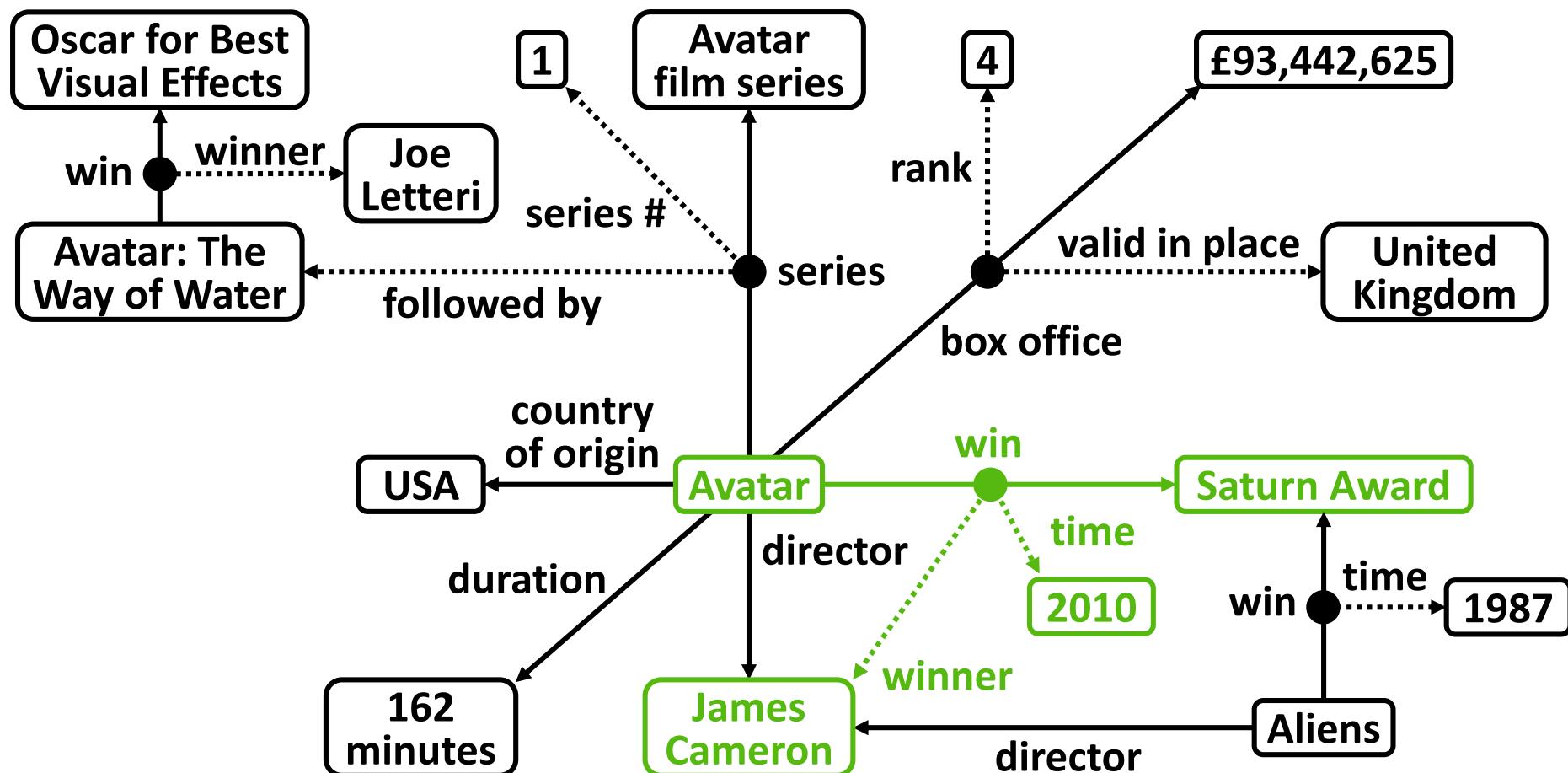
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03

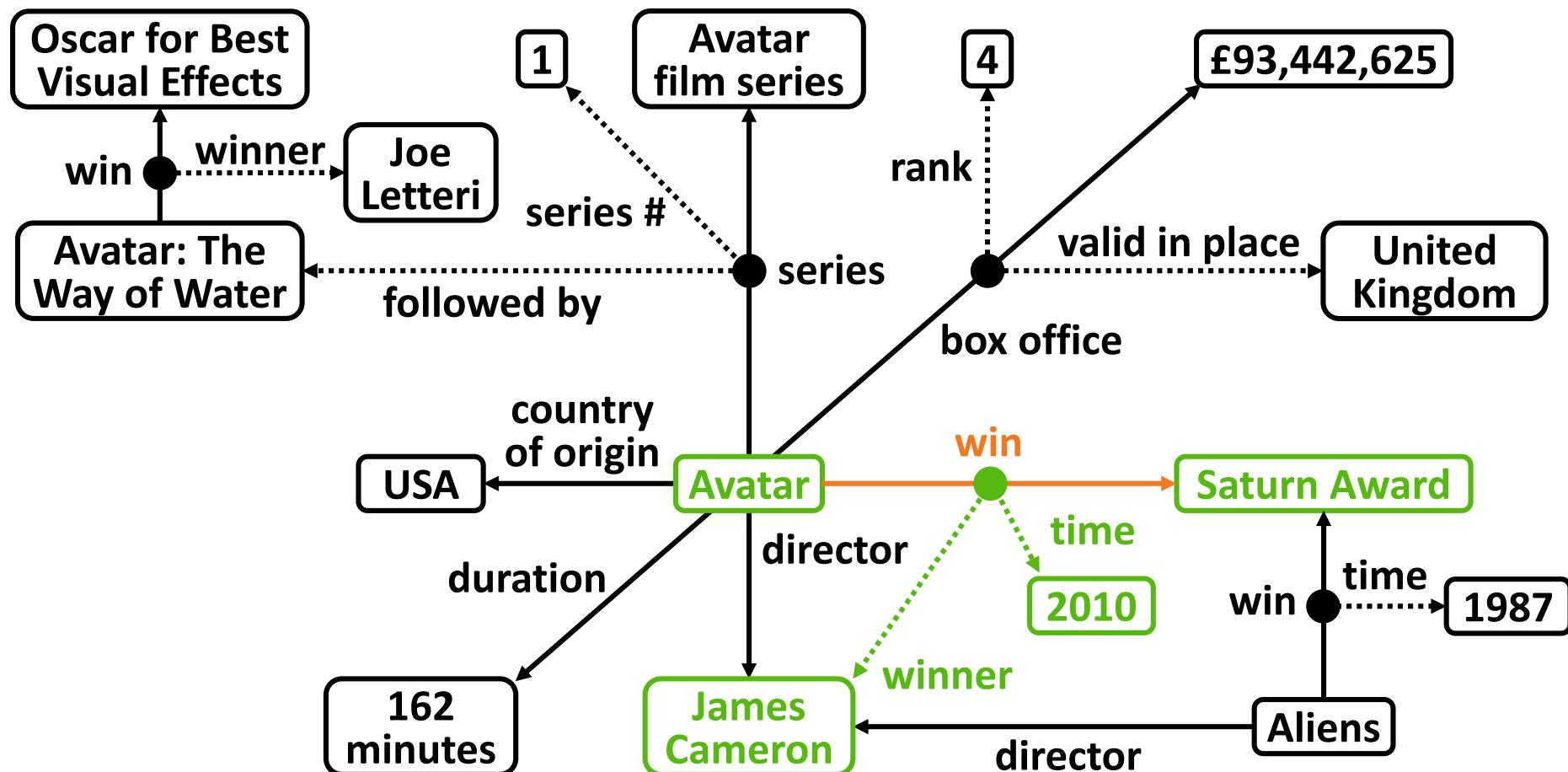
# Relation Prediction on HN-KGs

((Avatar, win, Saturn\_Award), {(winner, James\_Cameron), (time, 2010)})



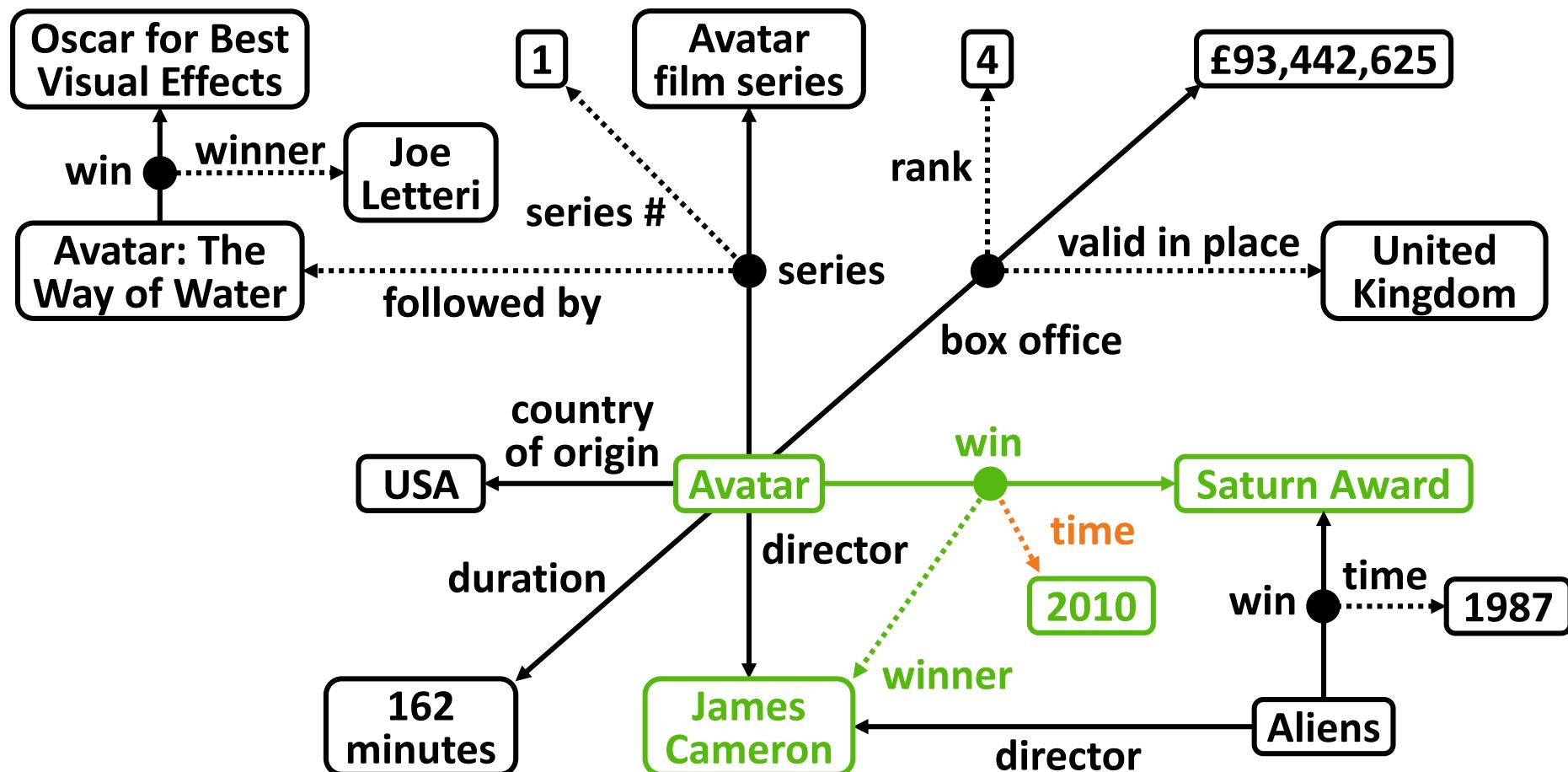
# Relation Prediction on HN-KGs

((Avatar, ?, Saturn\_Award), {(winner, James\_Cameron), (time, 2010)})



# Relation Prediction on HN-KGs

((Avatar, win, Saturn\_Award), {(winner, James\_Cameron), ( ? , 2010)})

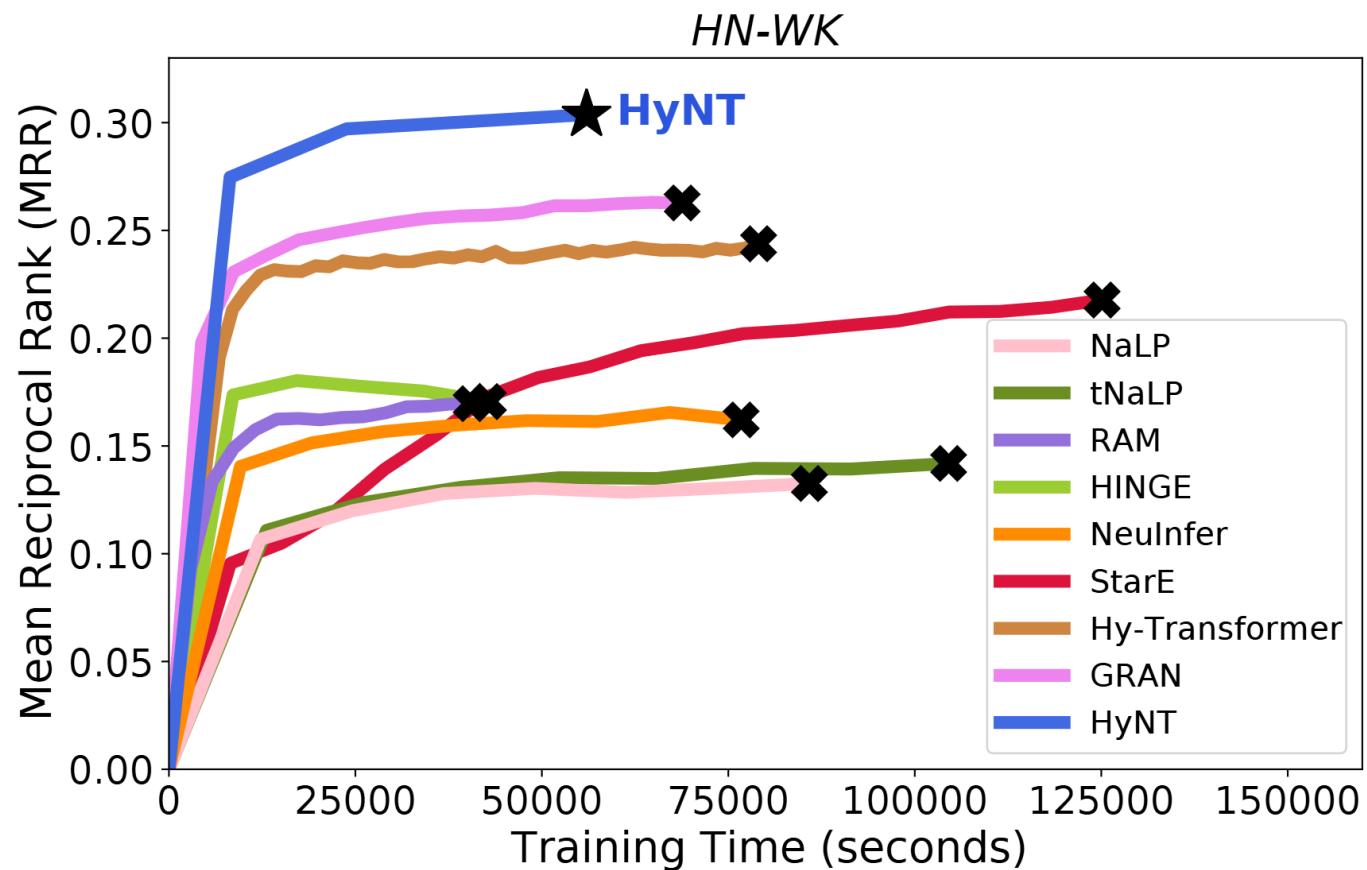


## 03 Contributions

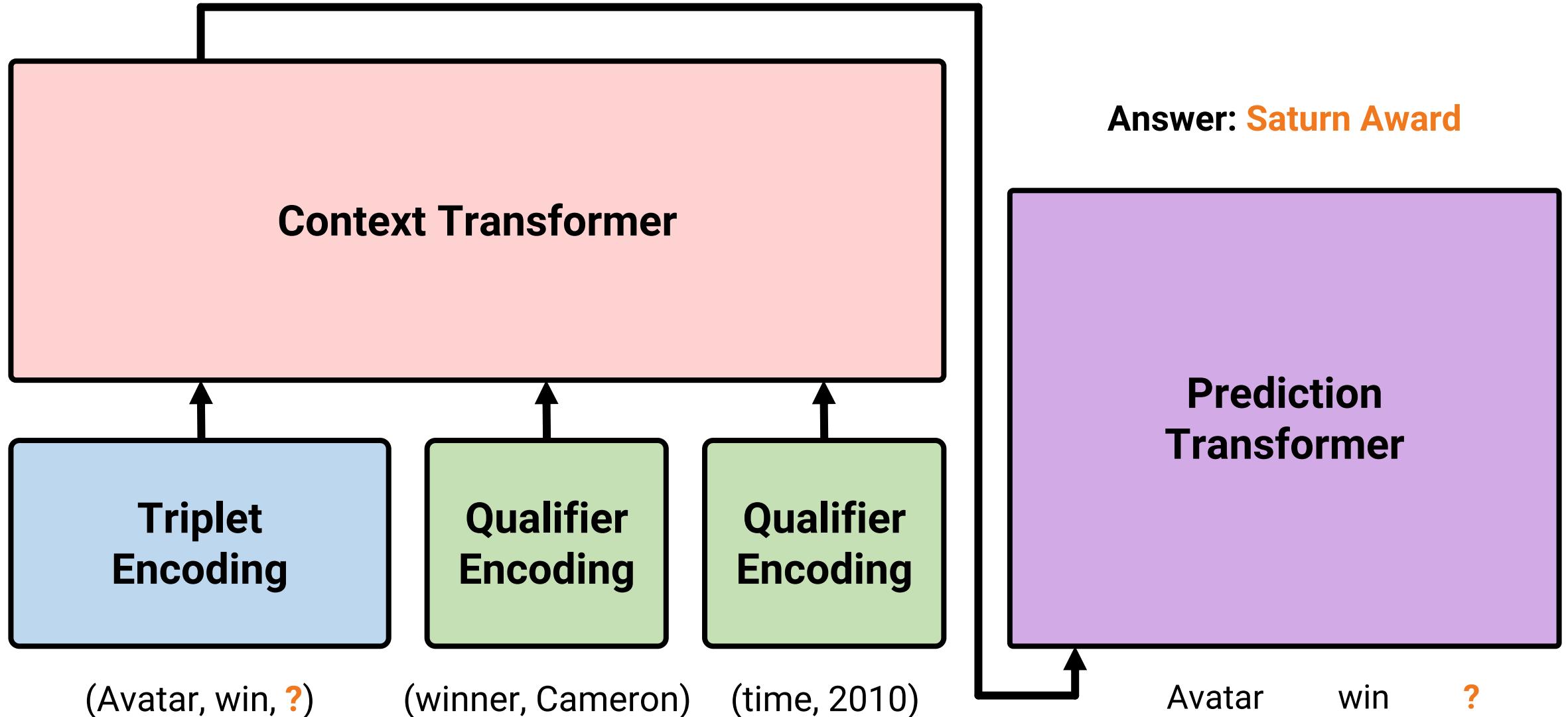
- Define **Hyper-relational and Numeric Knowledge Graphs**
  - Create 4 real-world HN-KG datasets
- Propose **HyNT**, Hyper-relational knowledge graph embedding with Numeric literals using **Transformers**
  - Define a context transformer and a prediction transformer
  - Reduce the cost by learning compact representations of triplets and qualifiers
- HyNT significantly outperforms 12 different state-of-the-art methods for **link prediction**, **numeric value prediction**, and **relation prediction**

# Contributions

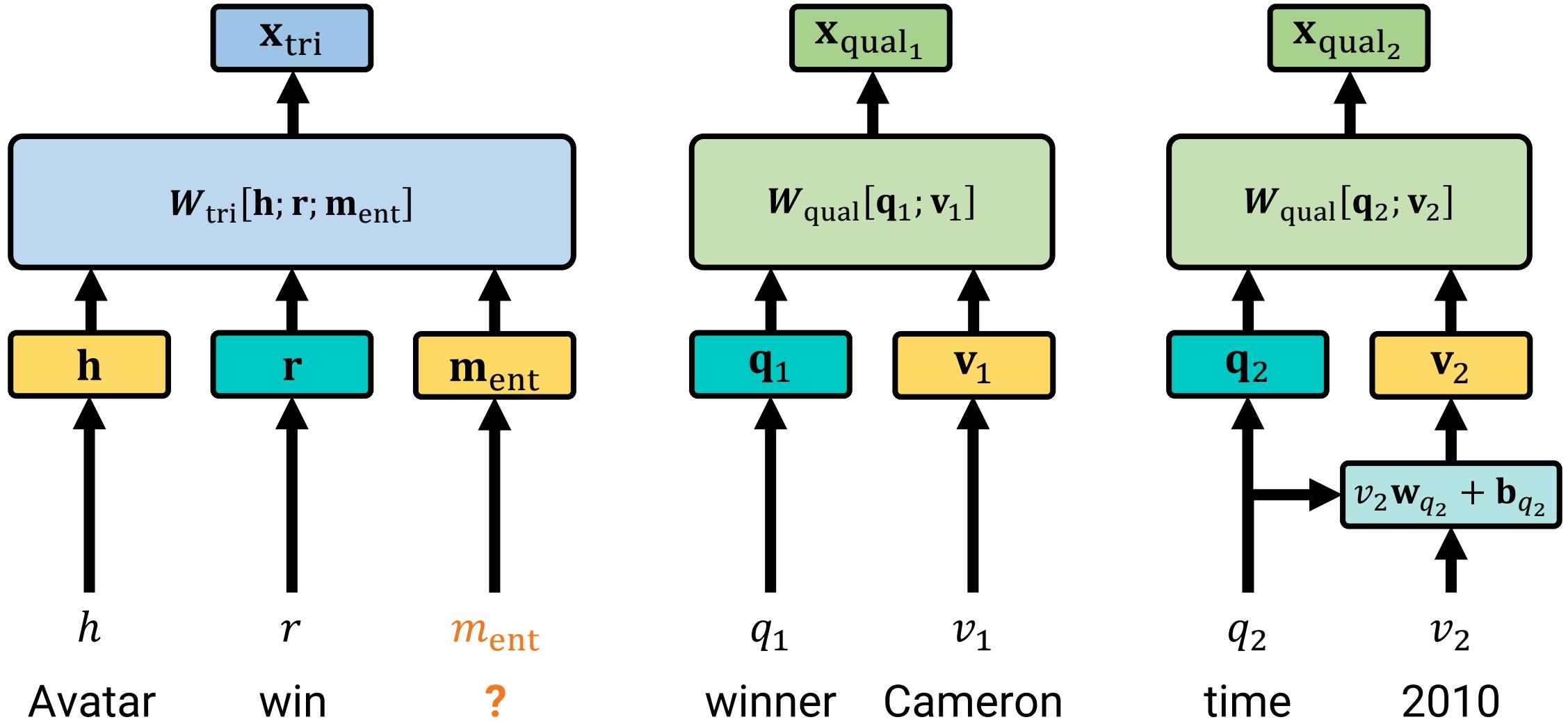
- Link Prediction Performance vs. Training Time



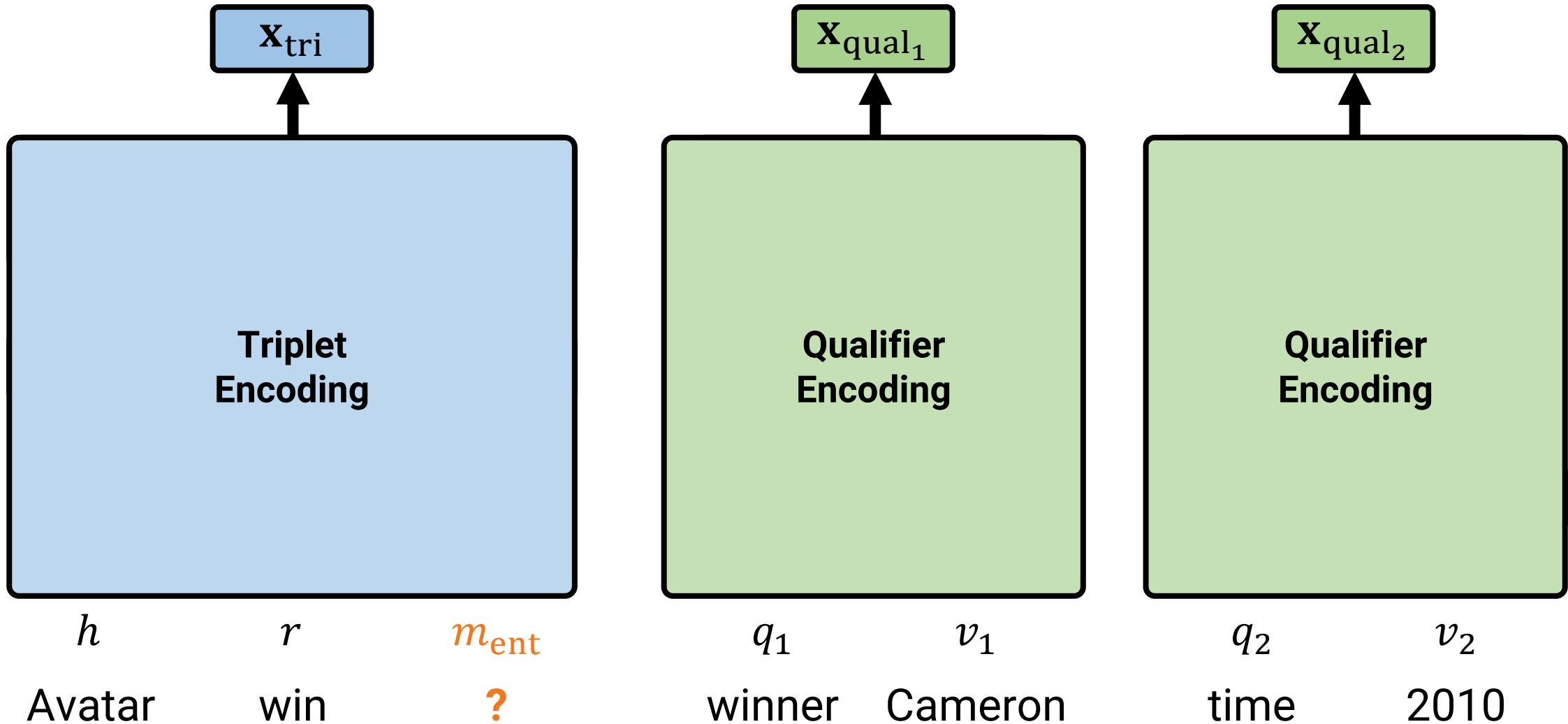
# Overview of HyNT



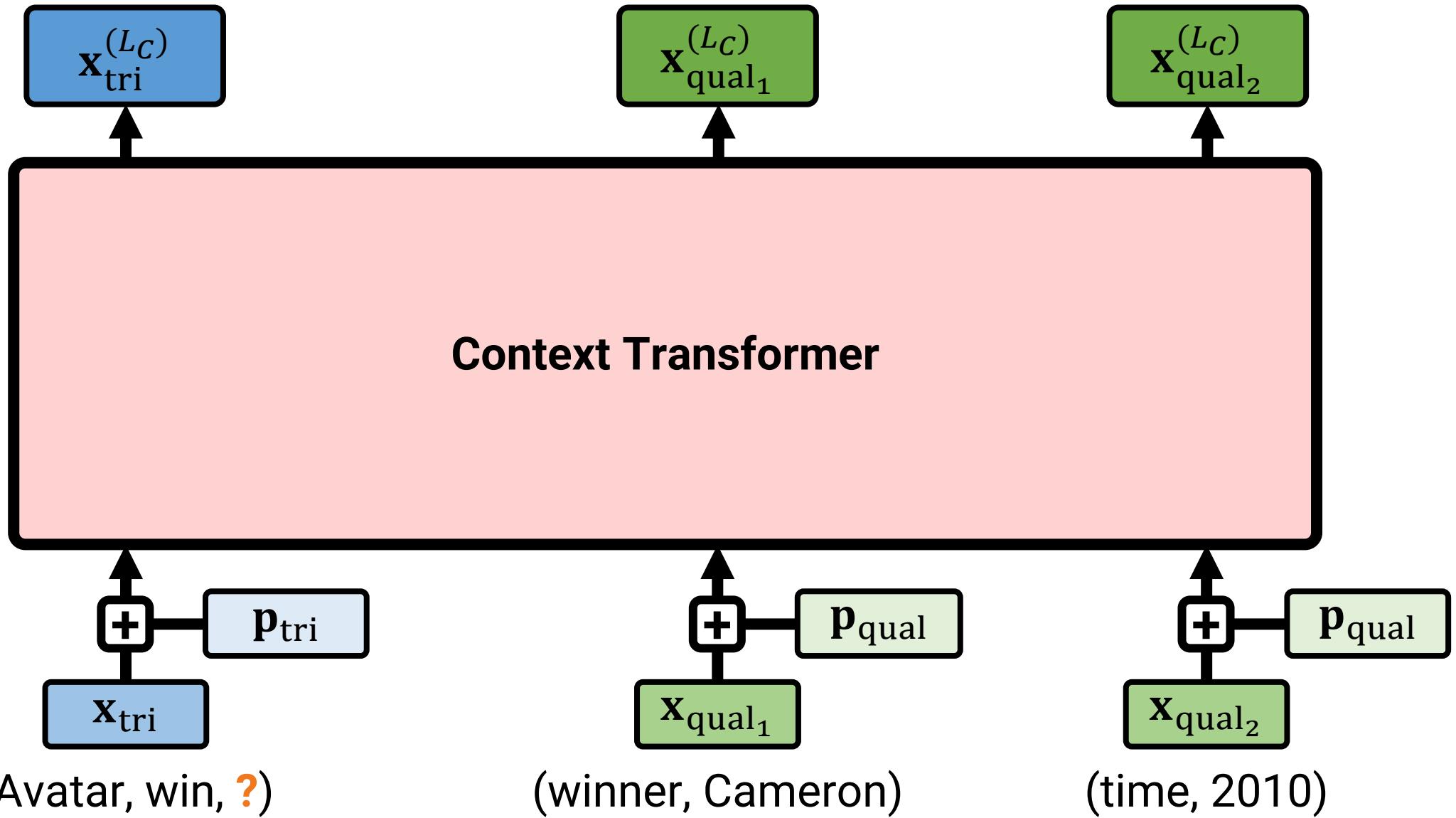
# Triplet/Qualifier Encoding



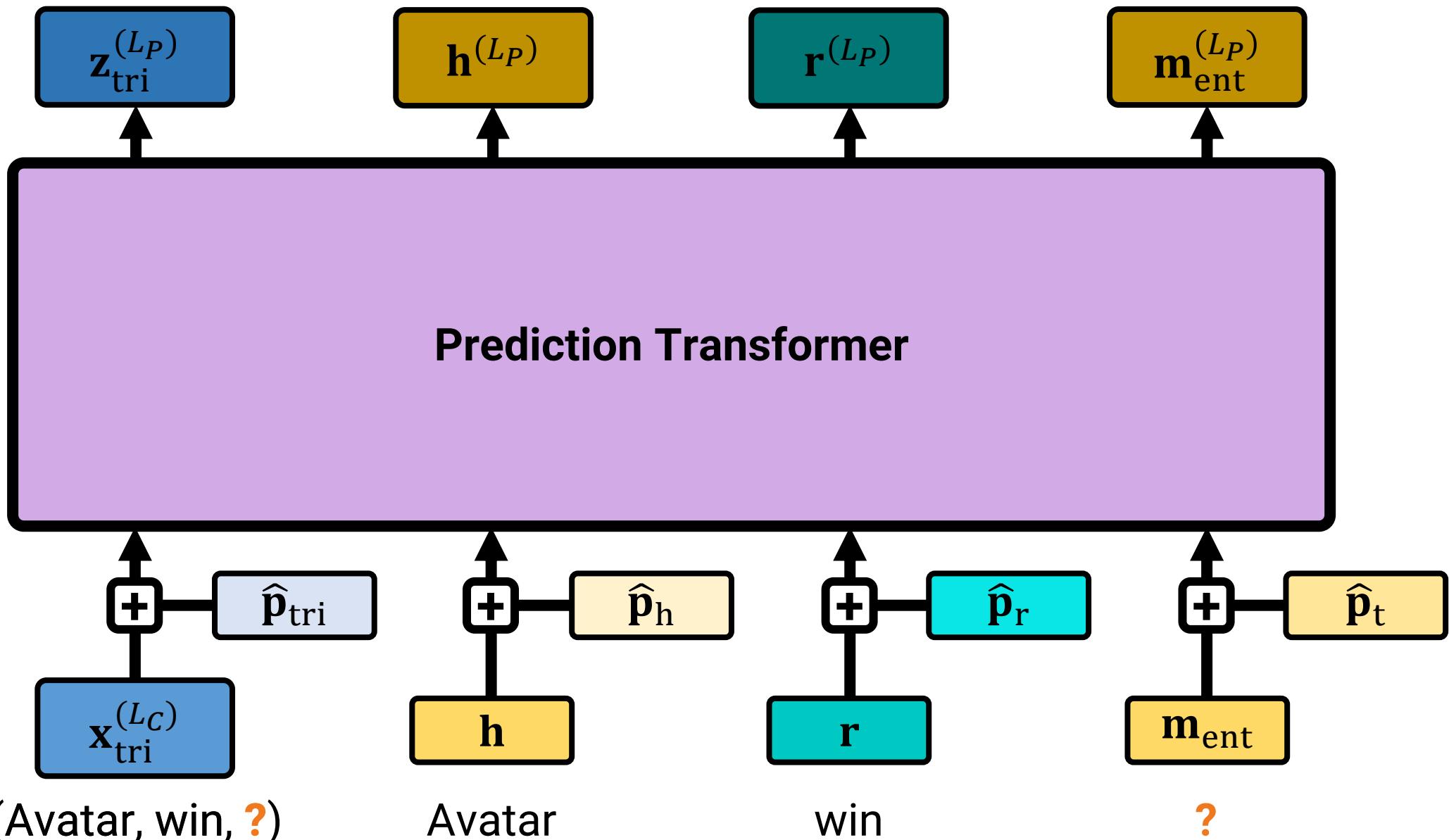
# Triplet/Qualifier Encoding



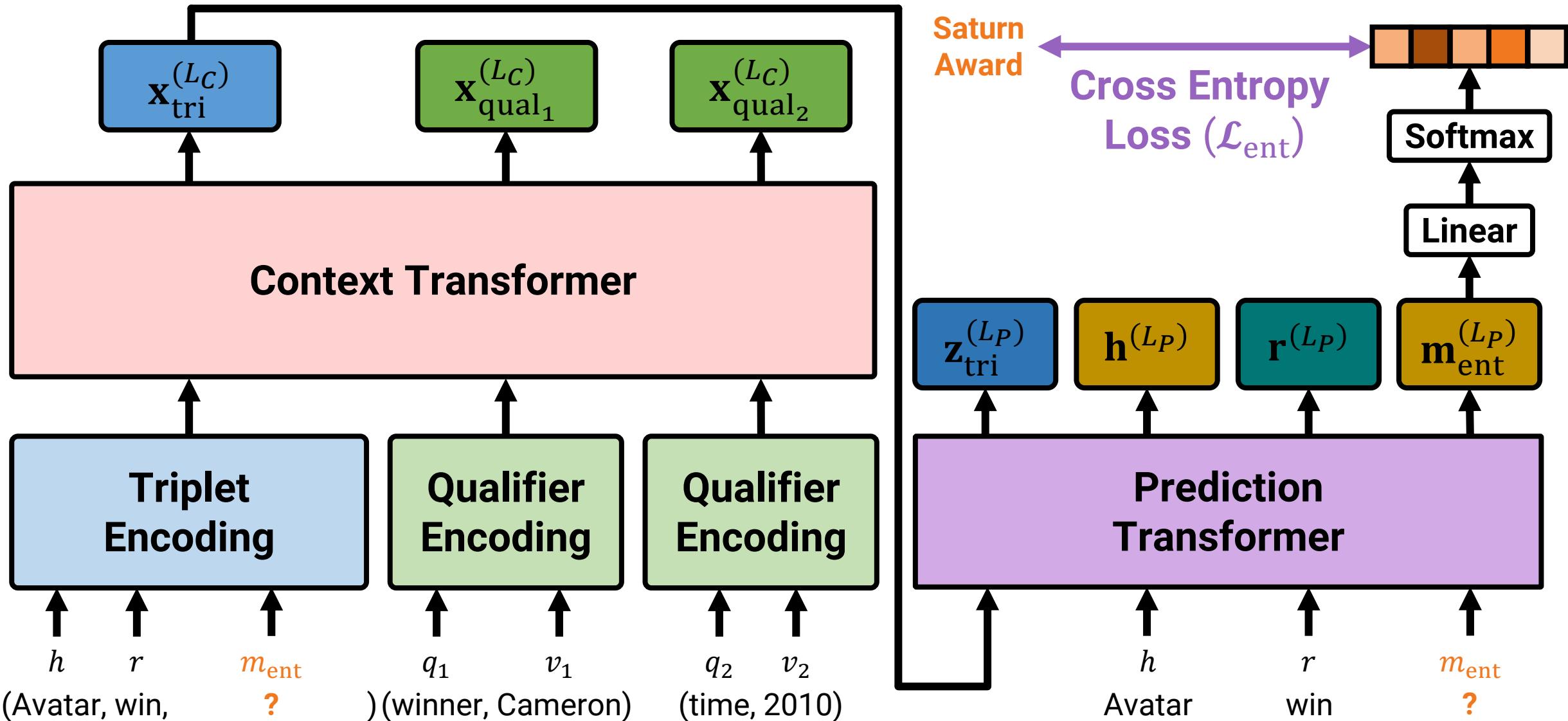
# Context Transformer



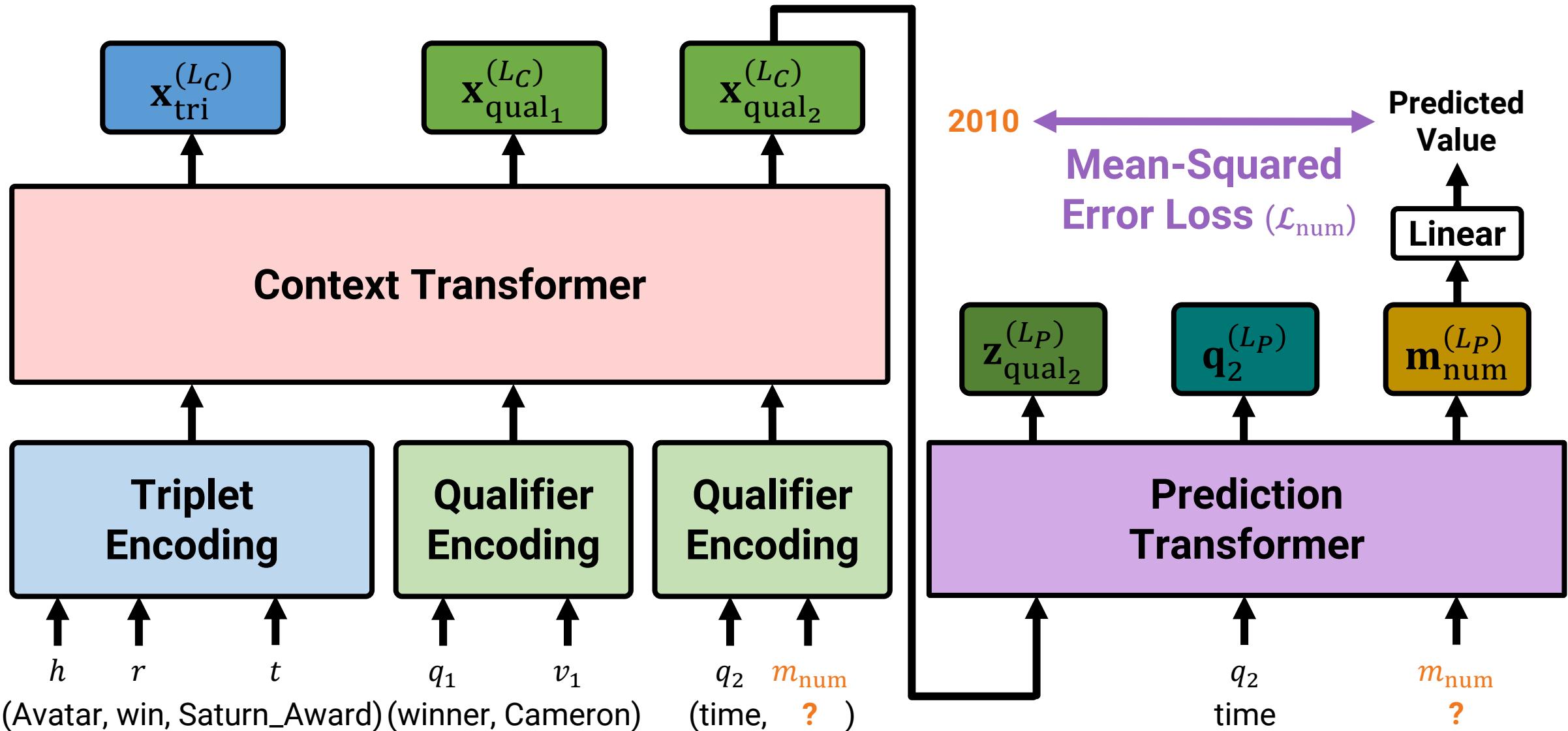
# Prediction Transformer



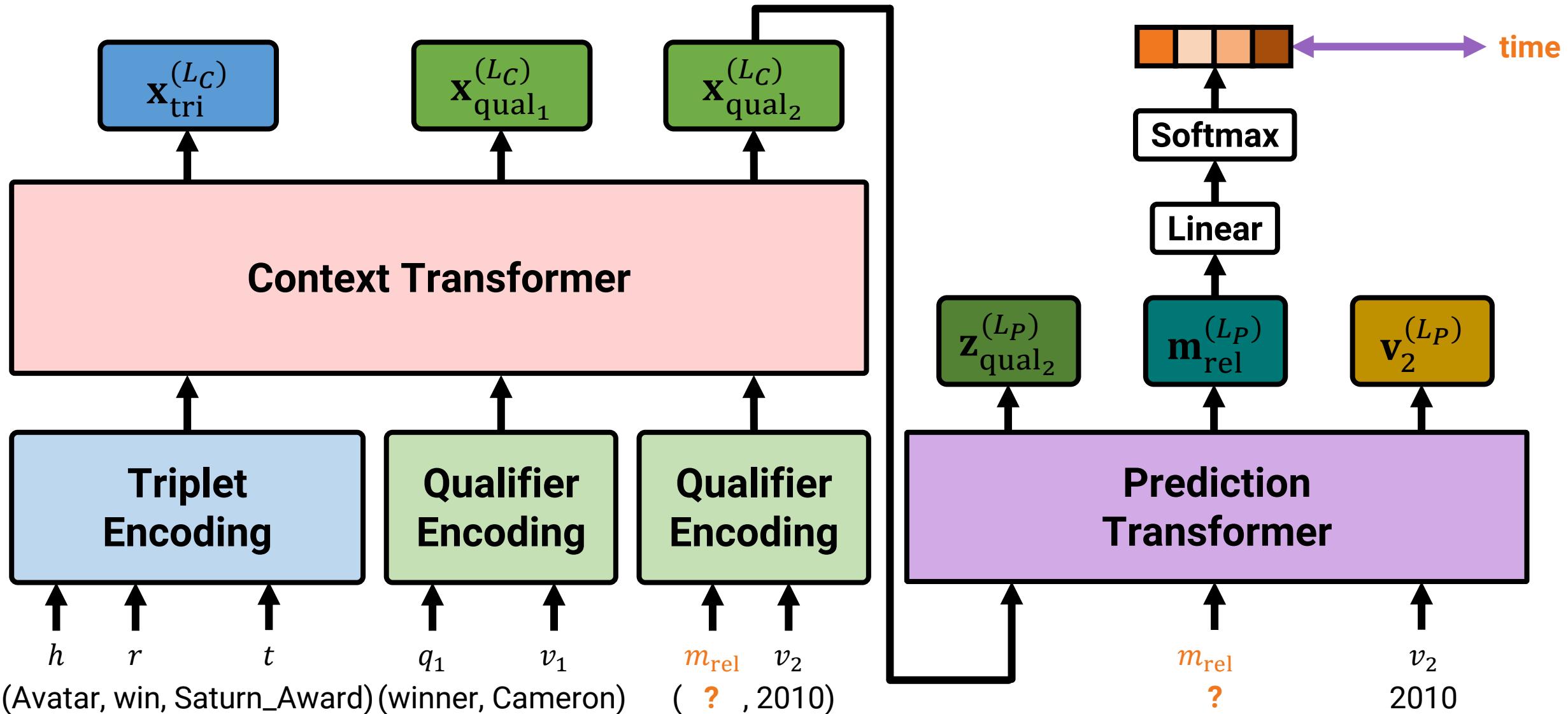
# Link Prediction using HyNT



# Numeric Value Prediction using HyNT

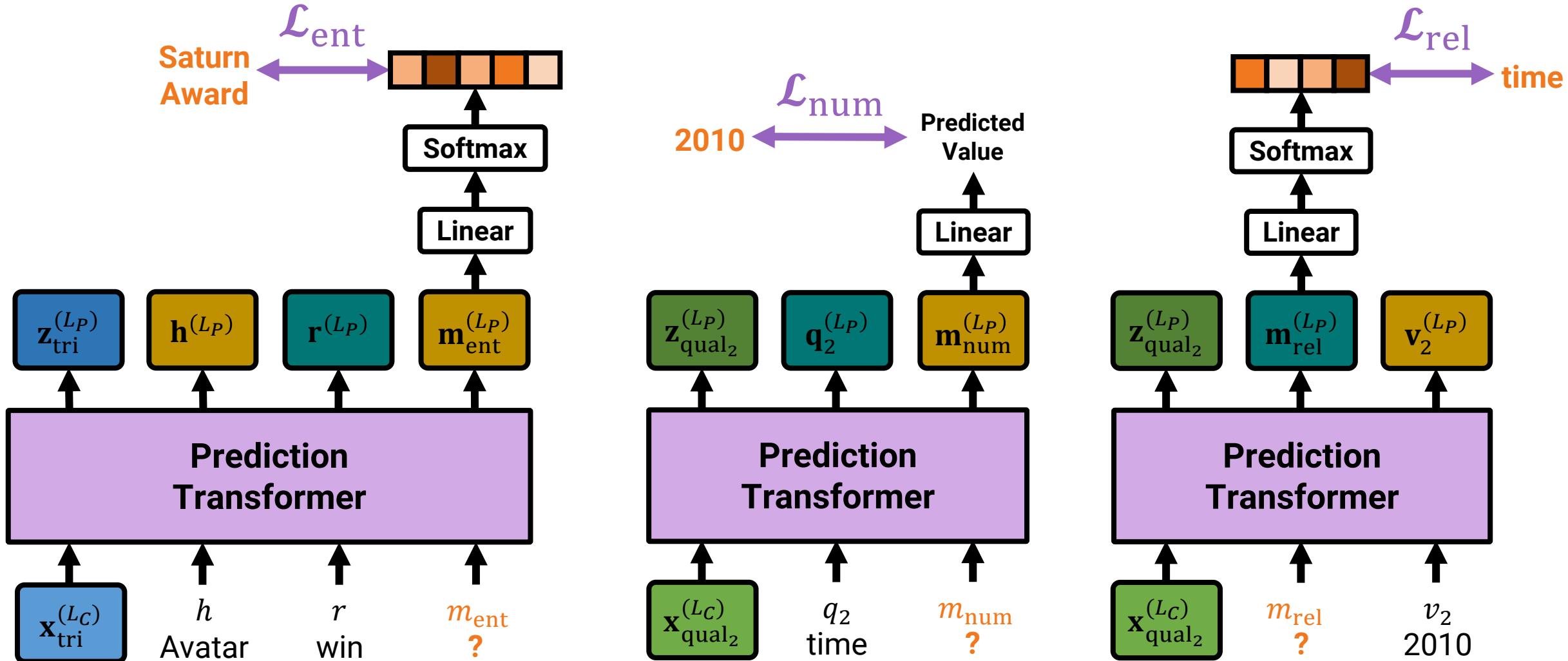


# Relation Prediction using HyNT



# Loss of HyNT

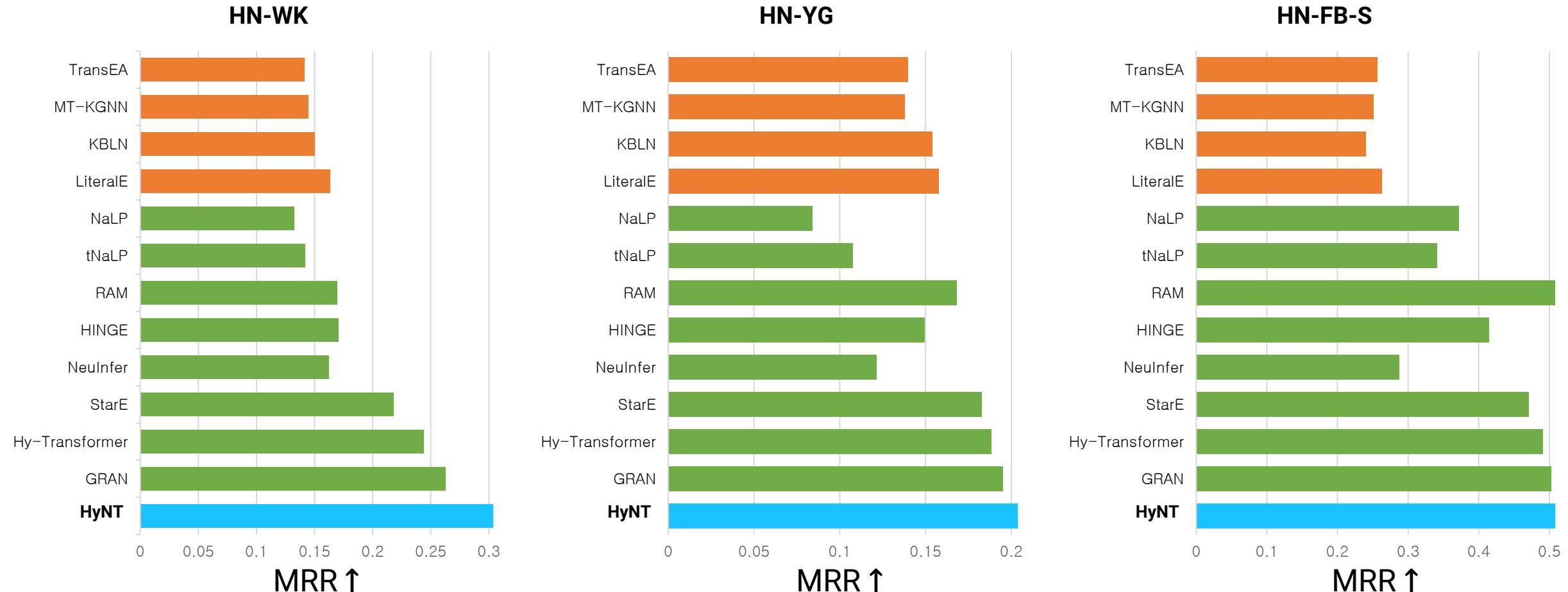
$$\mathcal{L} := \mathcal{L}_{\text{ent}} + \lambda_1 \cdot \mathcal{L}_{\text{rel}} + \lambda_2 \cdot \mathcal{L}_{\text{num}}$$



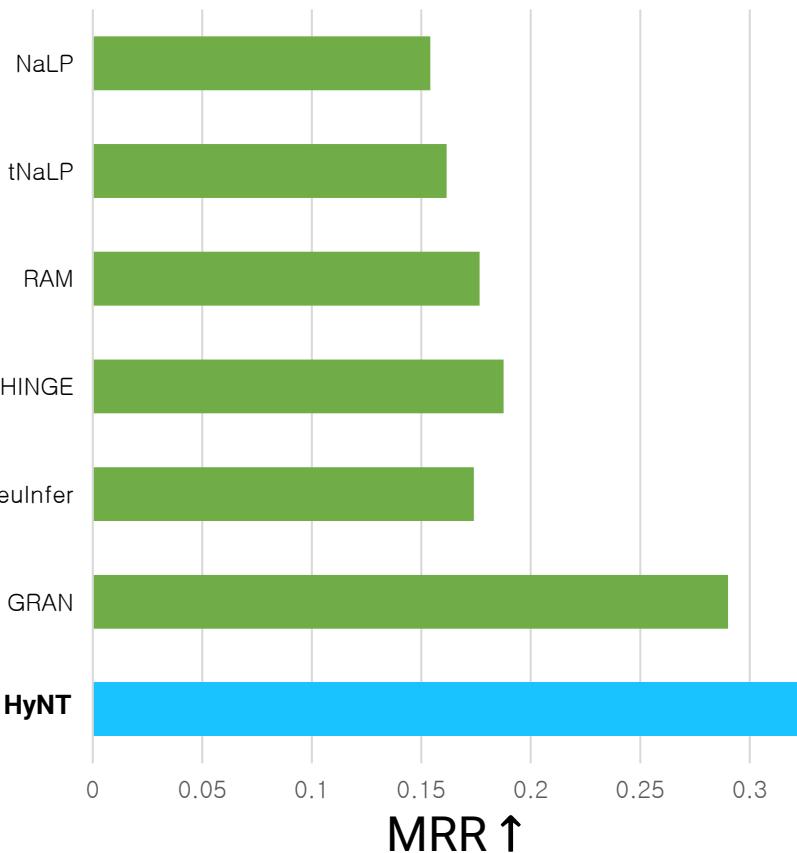
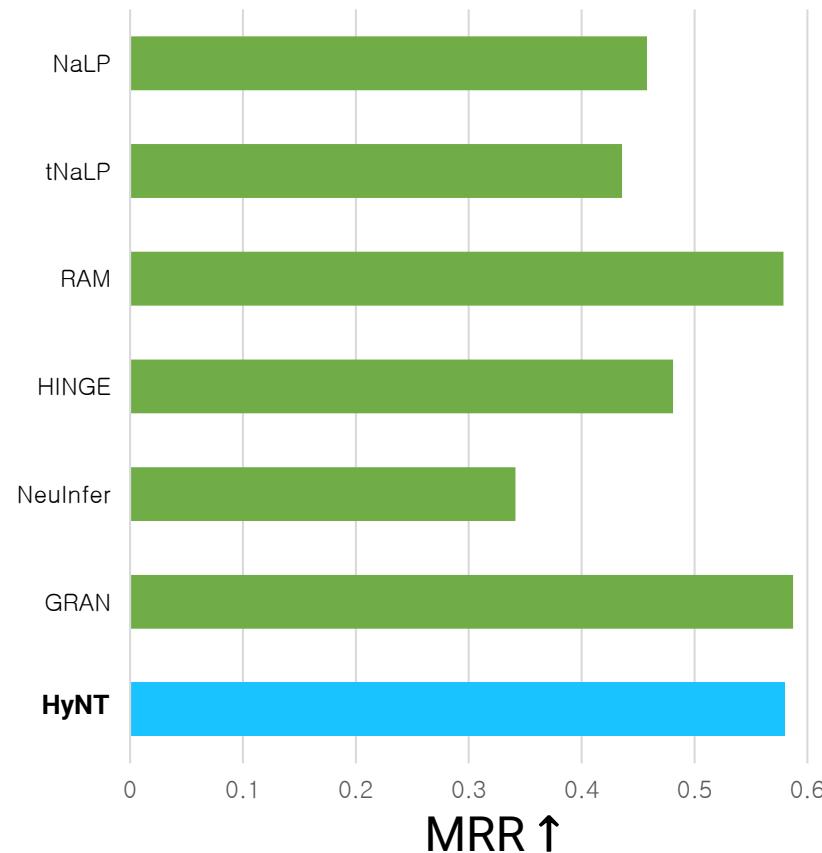
# Experimental Results

- Datasets
  - Based on Wikidata, YAGO, and Freebase
  - Create **4 Hyper-relational and Numeric Knowledge Graph (HN-KG)** datasets
    - HN-WK, HN-YG, HN-FB, HN-FB-S
- Comparison with **12 baseline methods**
  - Methods for handling numeric literals
    - TransEA, MT-KGNN, KBLN, LiteralE
  - Methods for handling hyper-relational facts
    - NaLP, tNaLP, RAM, HINGE, NeuInfer, StarE, Hy-Transformer, GRAN

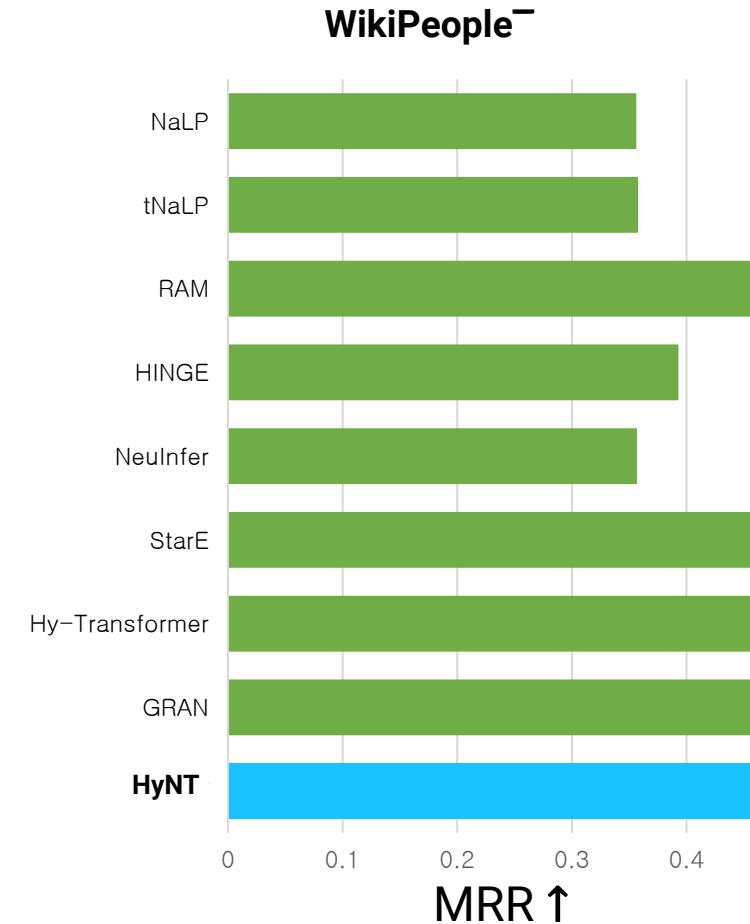
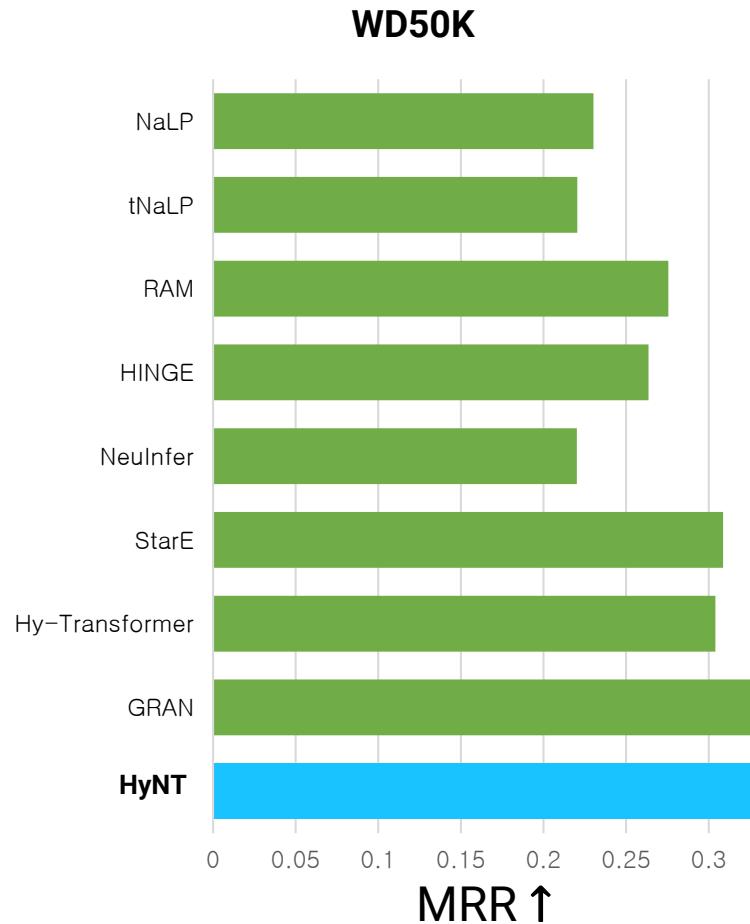
# Link Prediction Results – Primary



# Link Prediction Results – All

**HN-WK****HN-FB-S**

# Link Prediction Results – Primary (Benchmark Datasets)



# Link Prediction Results of HyNT

(( ? , nominated\_for, Best\_Actor), { (for\_work, Moneyball), (subject\_of, 84<sup>th</sup>\_Oscars) })

(( ? , nominated\_for, Best\_Actor), { (for\_work, Forrest\_Gump), (subject\_of, 67<sup>th</sup>\_Oscars) })

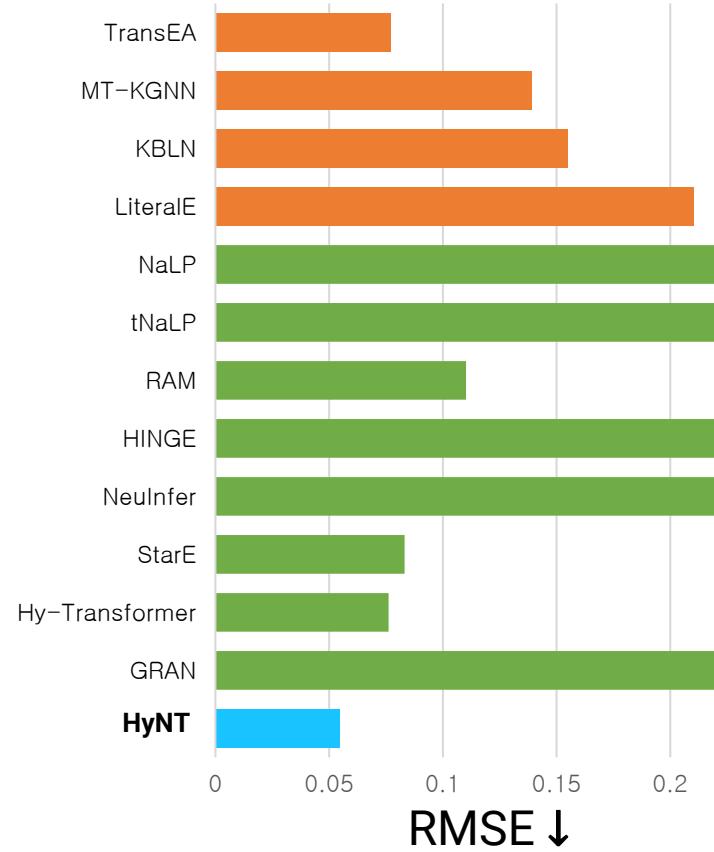
# Link Prediction Results of HyNT

((**Brad\_Pitt**, nominated\_for, Best\_Actor), {(for\_work, **Moneyball**), (subject\_of, **84<sup>th</sup>\_Oscars**)})

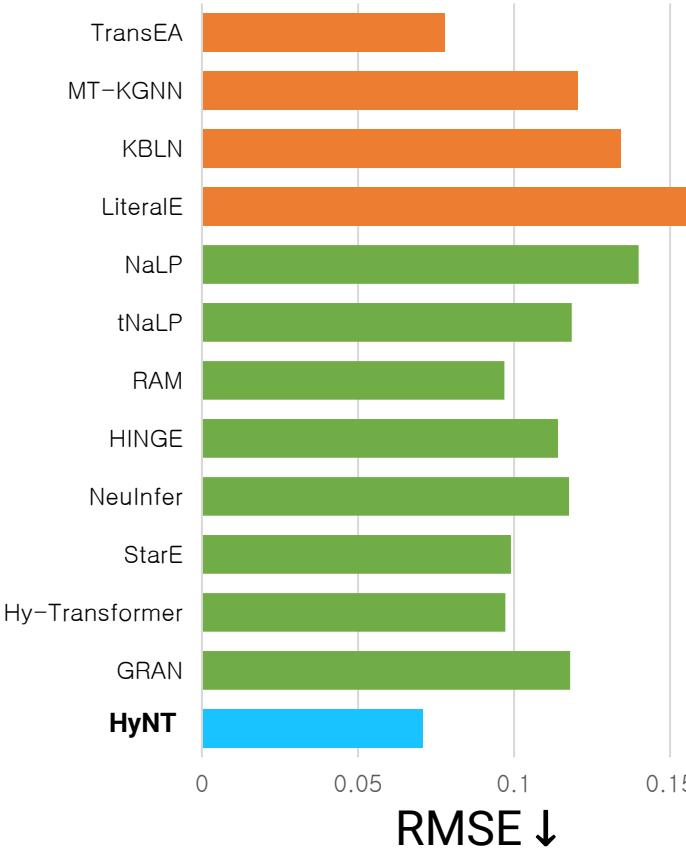
((**Tom\_Hanks**, nominated\_for, Best\_Actor), {(for\_work, **Forrest\_Gump**), (subject\_of, **67<sup>th</sup>\_Oscars**)})

# 03 Numeric Value Prediction Results – Primary

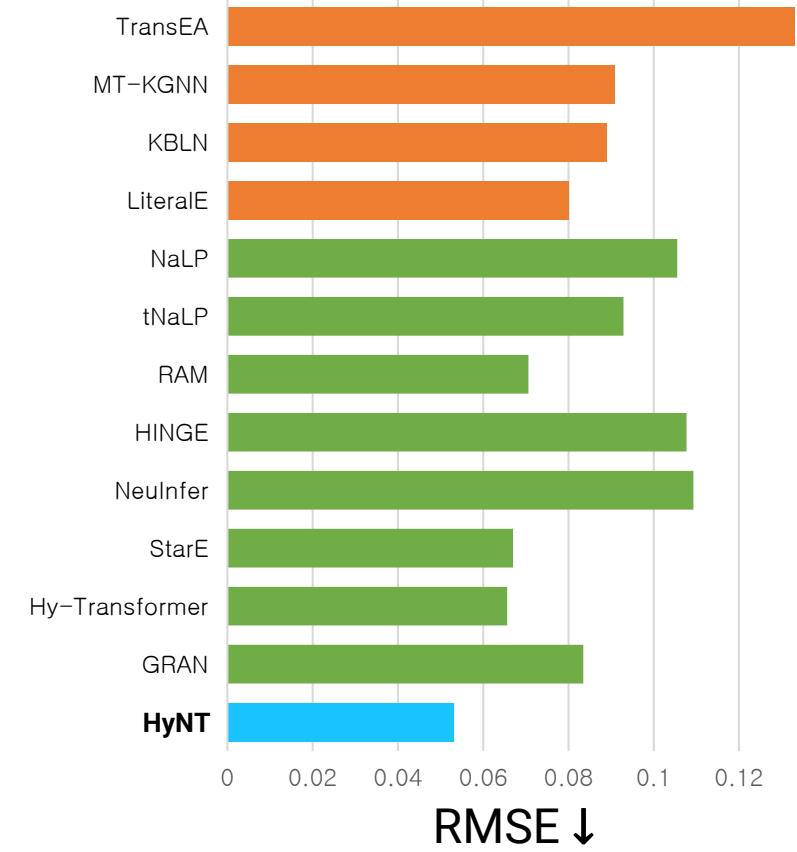
**HN-WK**



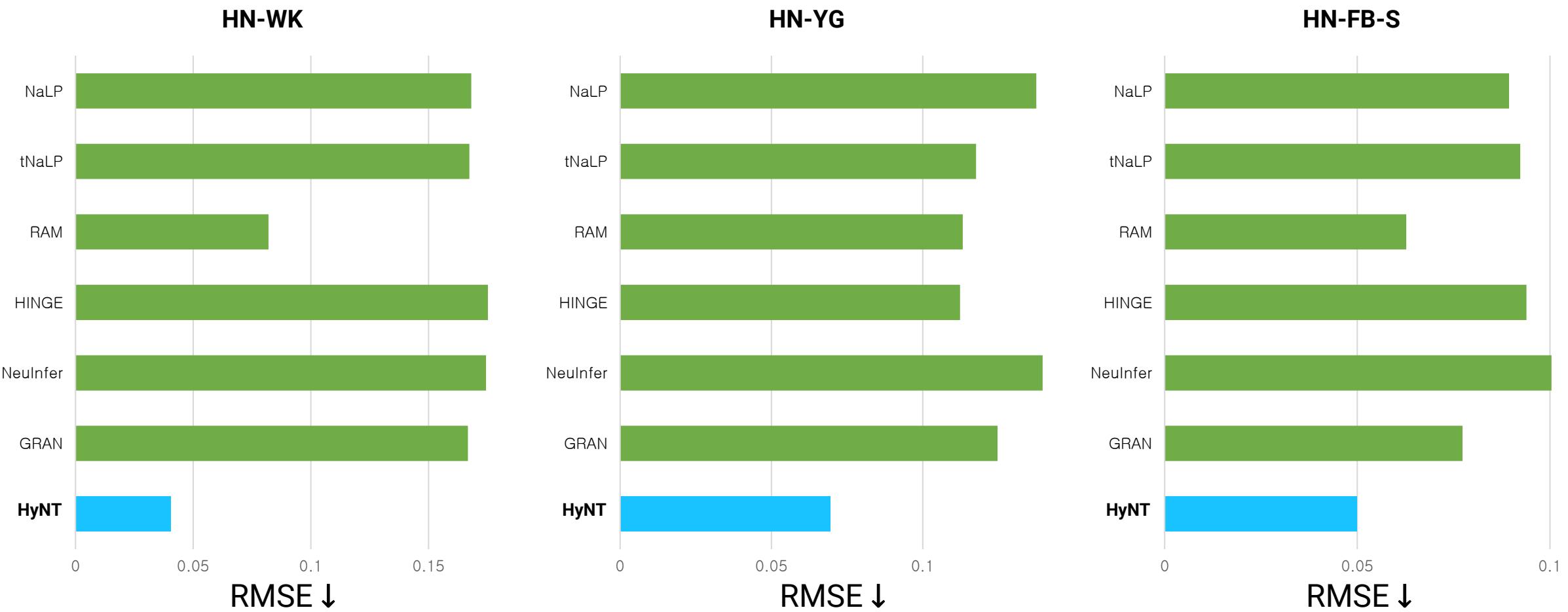
**HN-YG**



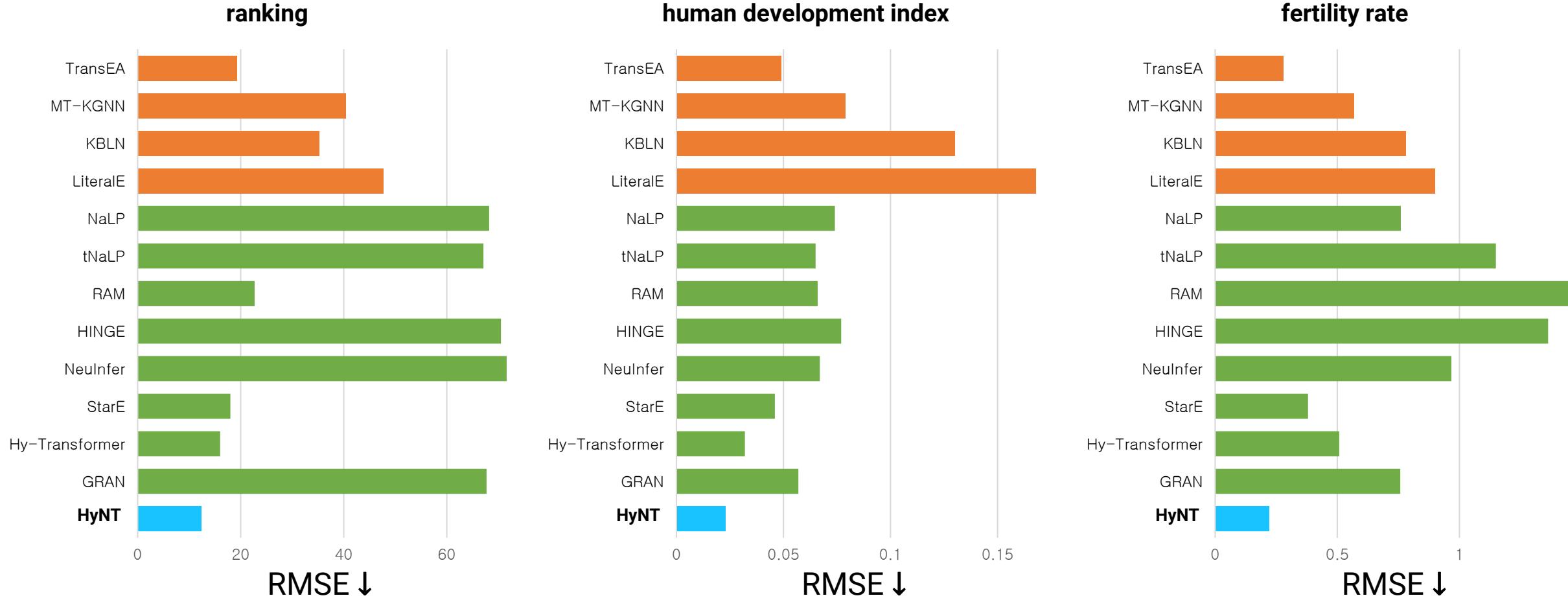
**HN-FB-S**



# Numeric Value Prediction Results – All



# Numeric Value Prediction Results per Attribute Type in HN-WK



# Visualization of the Predictions

## Target Values

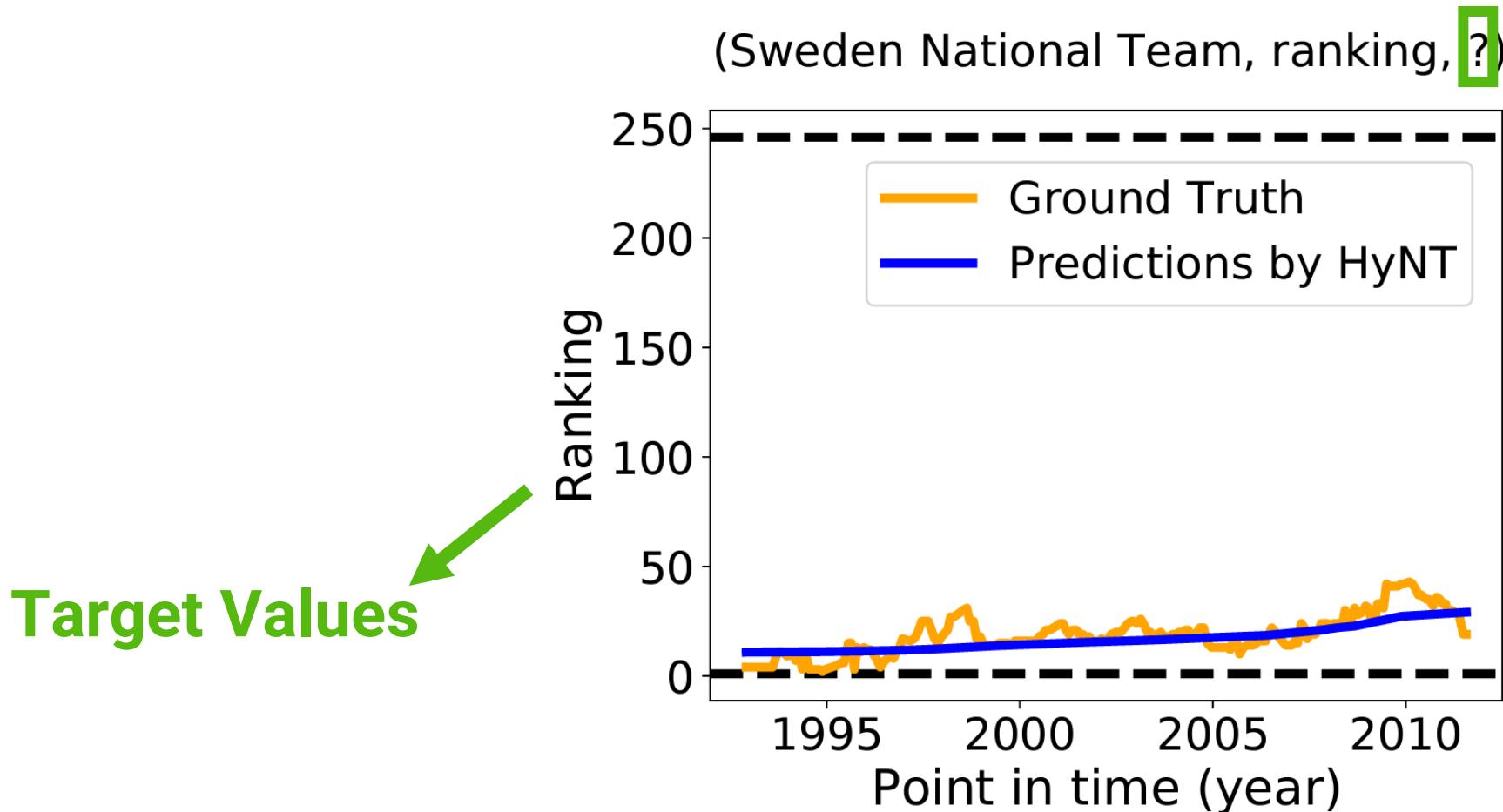
((Sweden National team, ranking, ?), {(point in time, 1995)})

((Sweden National team, ranking, ?), {(point in time, 1996)})

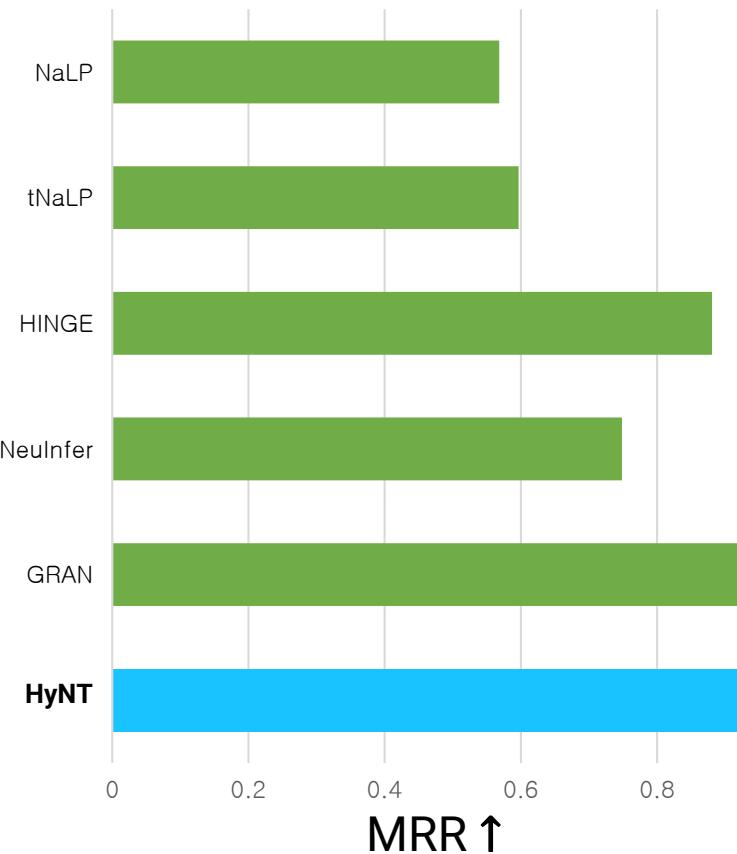
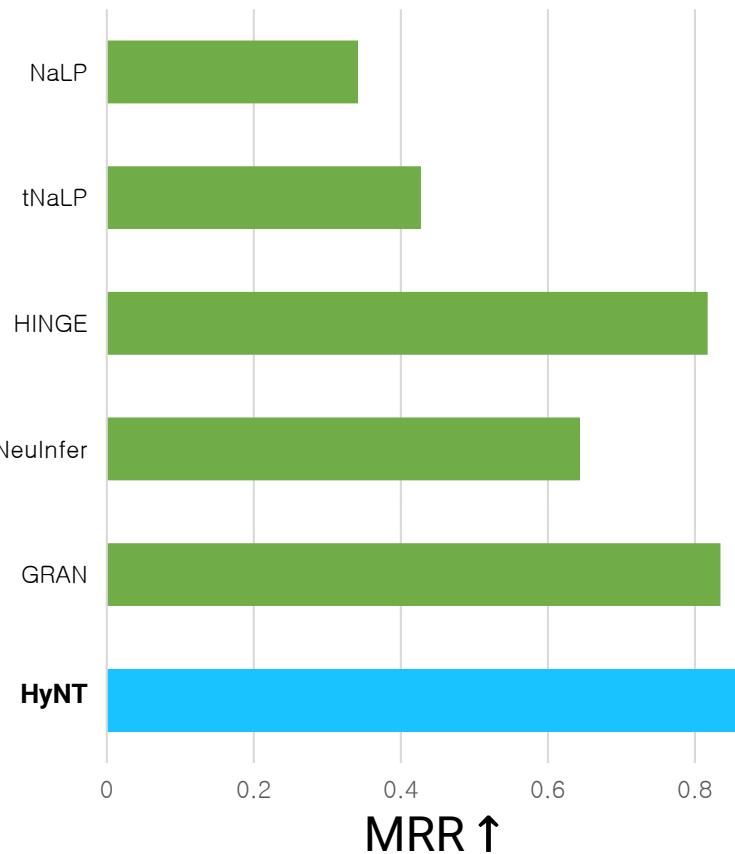
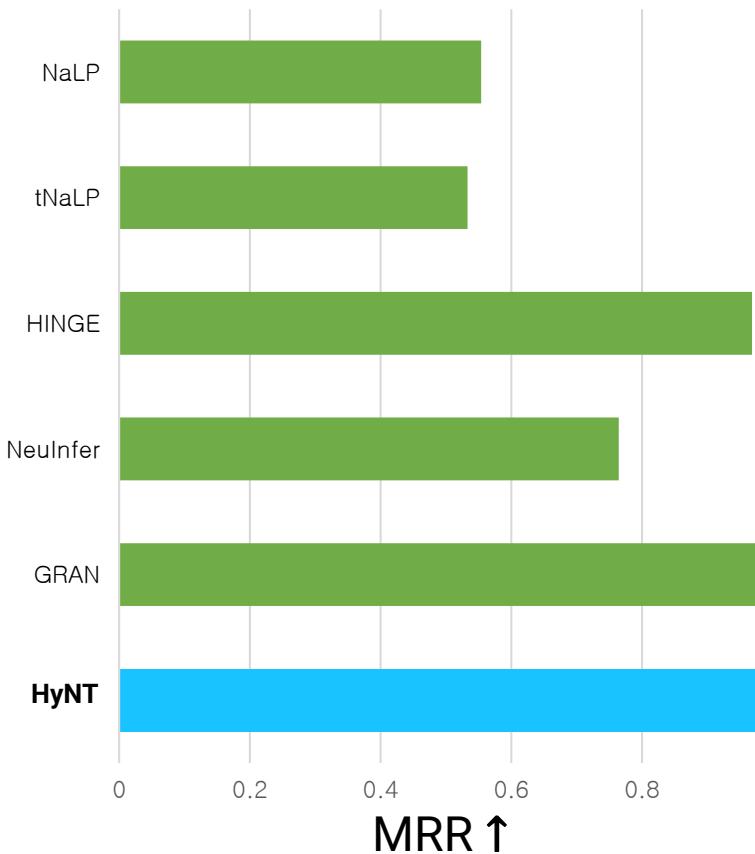
((Sweden National team, ranking, ?), {(point in time, 1997)})

:

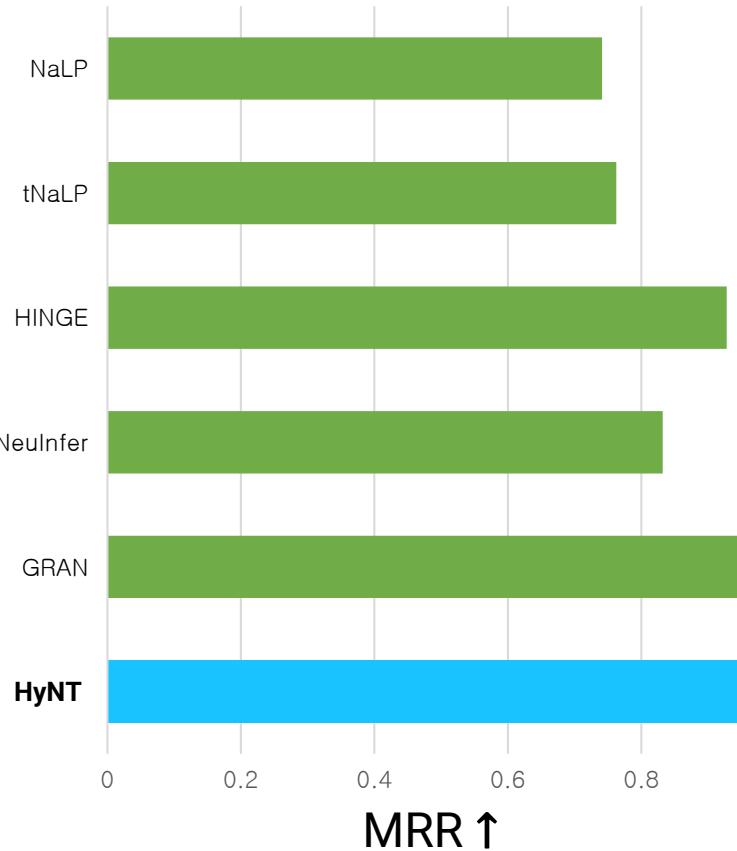
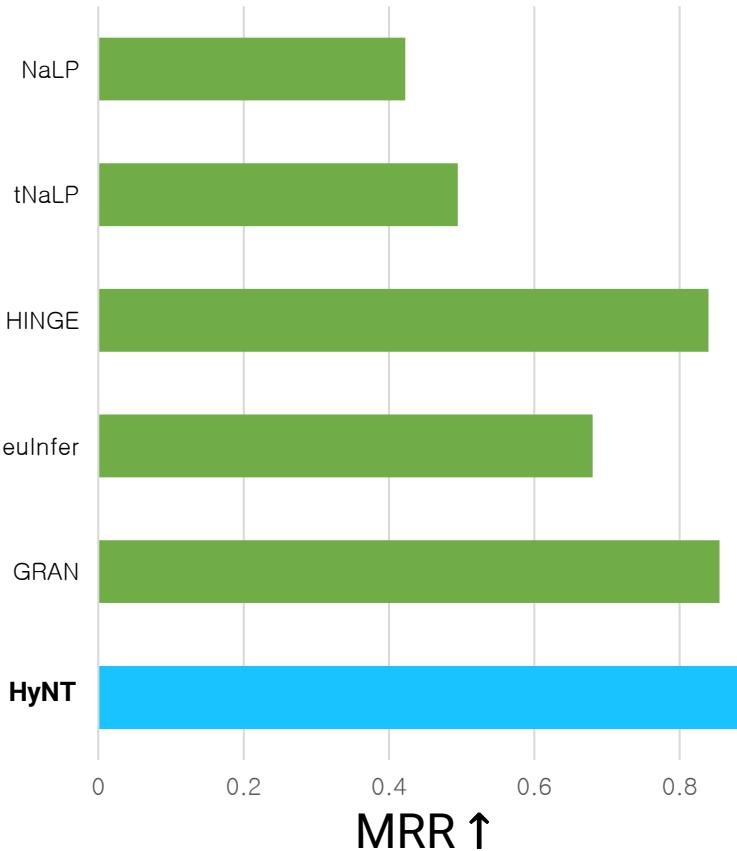
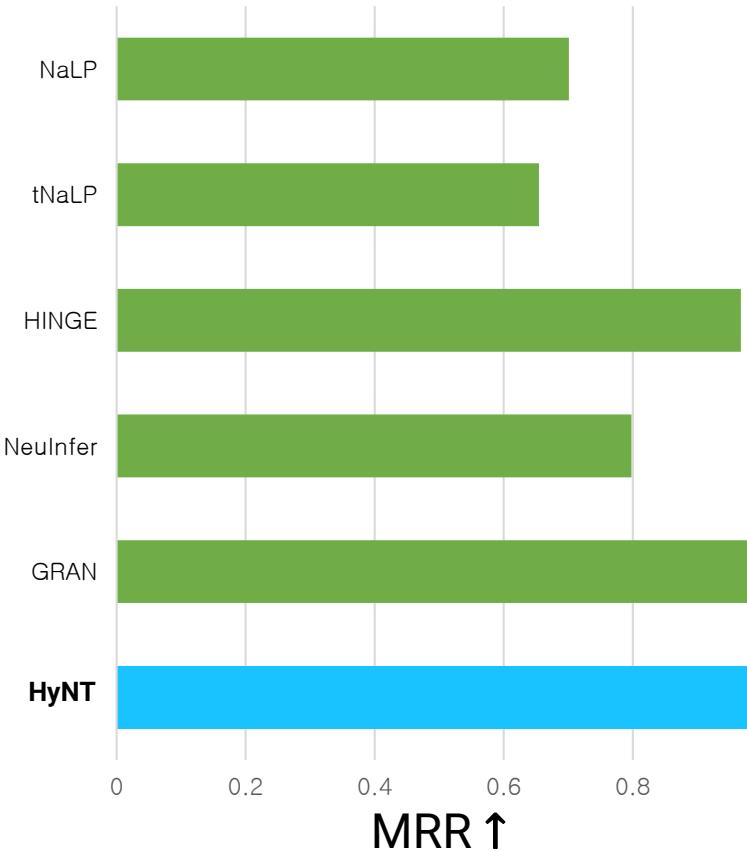
# Visualization of the Predictions



# Relation Prediction Results – Primary

**HN-WK****HN-YG****HN-FB-S**

# Relation Prediction Results – All

**HN-WK****HN-YG****HN-FB-S**

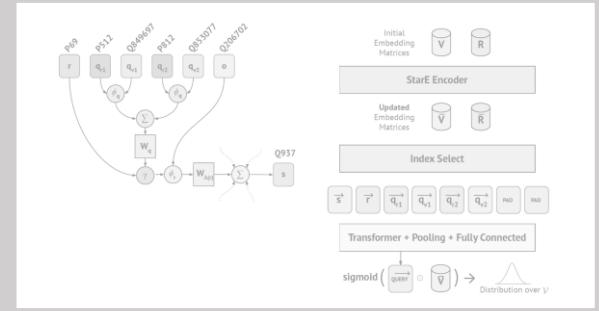
- Hyper-relational and Numeric Knowledge Graphs (**HN-KGs**)
- Propose **HyNT** to solve **link prediction**, **numeric value prediction**, and **relation prediction** on **HN-KGs**
- HyNT significantly outperforms 12 different state-of-the-art methods
- Extend HyNT to **inductive learning scenarios**
  - New entities and relations appear at test time



## Message Passing for Hyper-Relational Knowledge Graphs

Mikhail Galkin, Priyansh Trivedi, Gaurav Maheshwari,  
Ricardo Usbeck, and Jens Lehmann

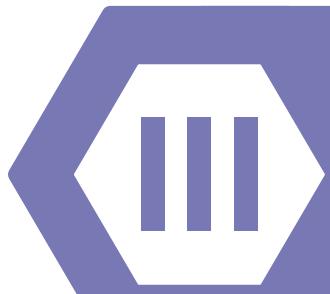
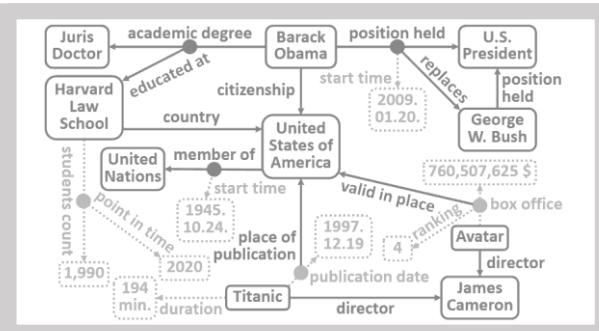
EMNLP 2020



## Representation Learning on Hyper-Relational and Numeric Knowledge Graphs with Transformers

Chanyoung Chung<sup>†</sup>, Jaejun Lee<sup>‡</sup>, and Joyce Jiyoung Whang<sup>\*</sup>

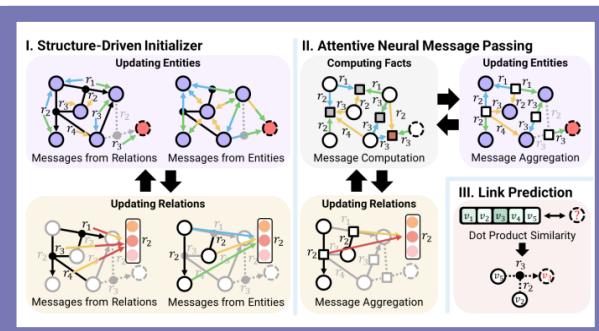
KDD 2023



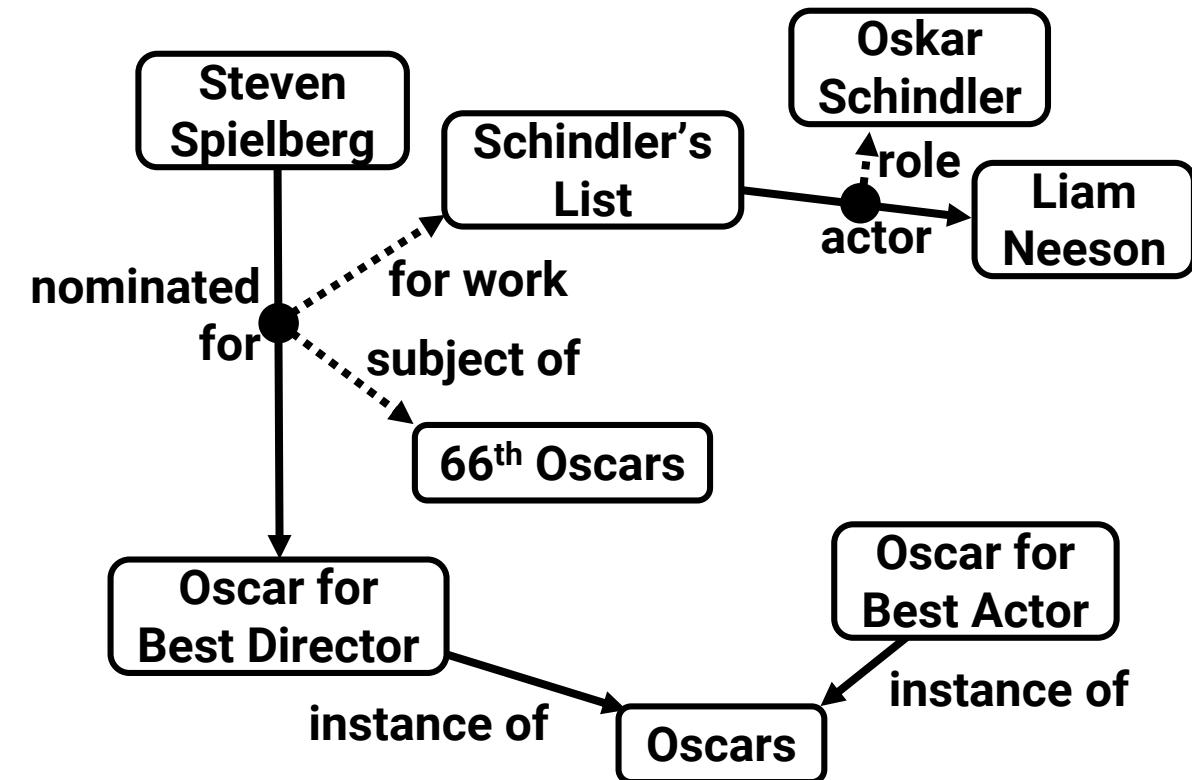
## Structure Is All You Need: Structural Representation Learning on Hyper-Relational Knowledge Graphs

Jaejun Lee and Joyce Jiyoung Whang<sup>\*</sup>

ICML 2025

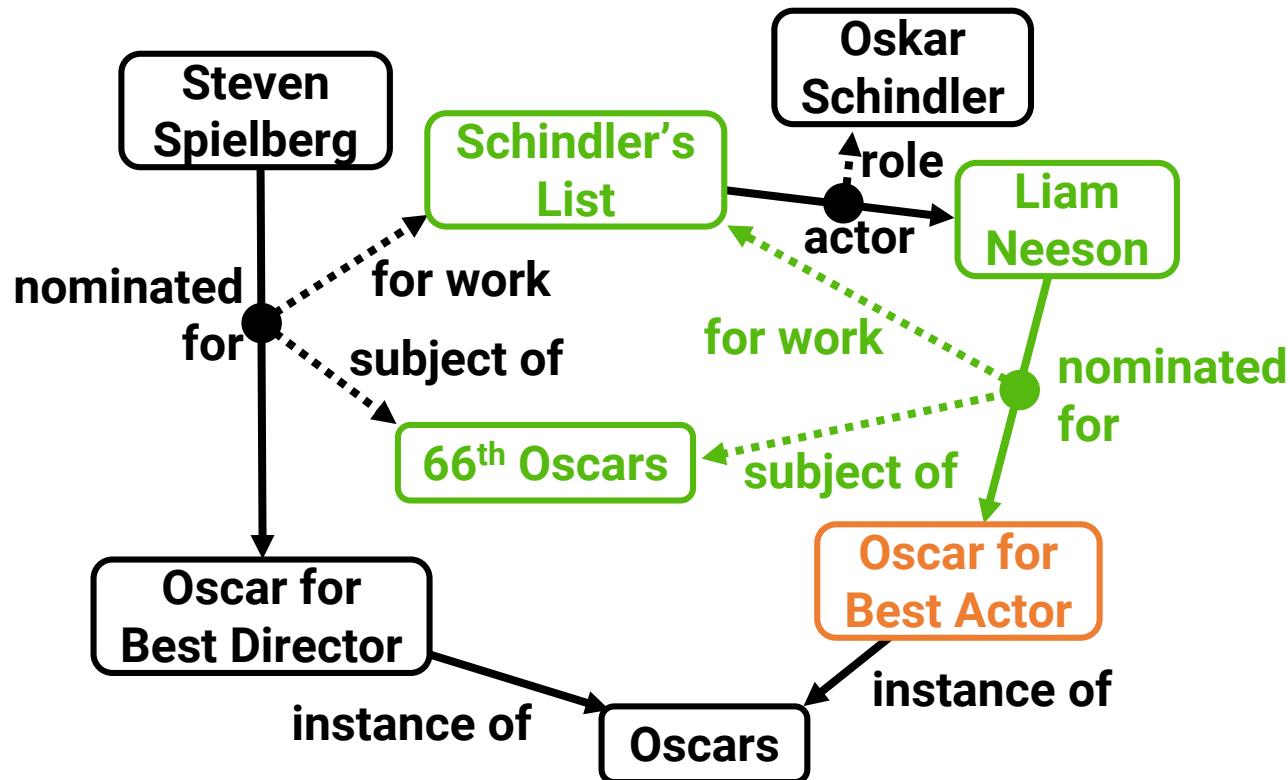


# 04 Hyper-relational Knowledge Graphs (HKGs)

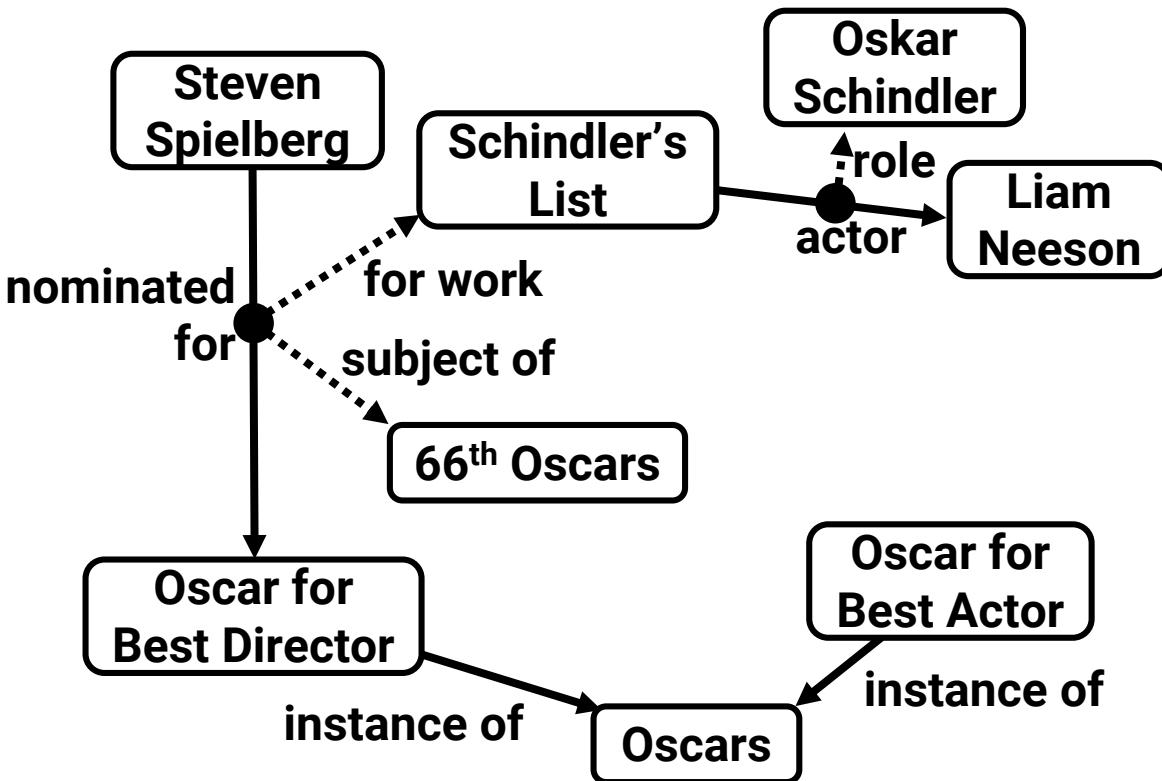


# Transductive Link Prediction on HKGs

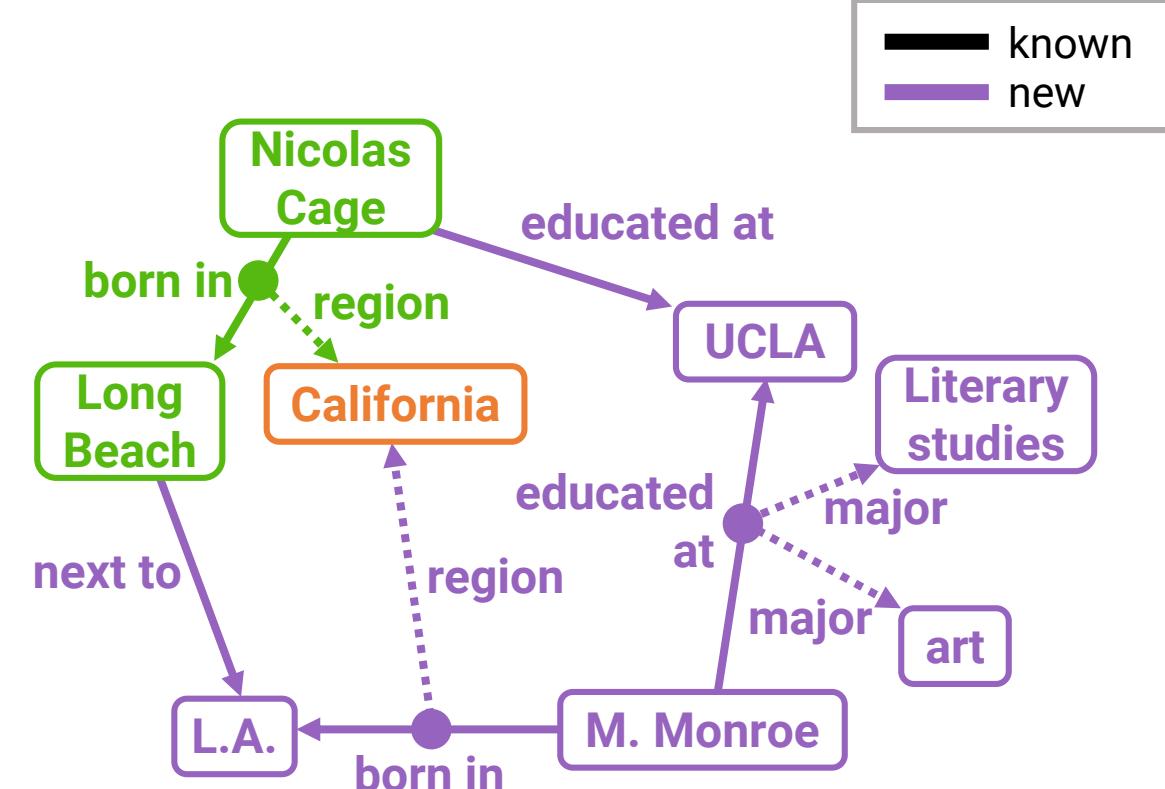
((Liam Neeson, nominated for, ? ),  
((for work, Schindler's List), (subject of, 66<sup>th</sup> Oscars)))



# Inductive Link Prediction on HKGs



Training HKG

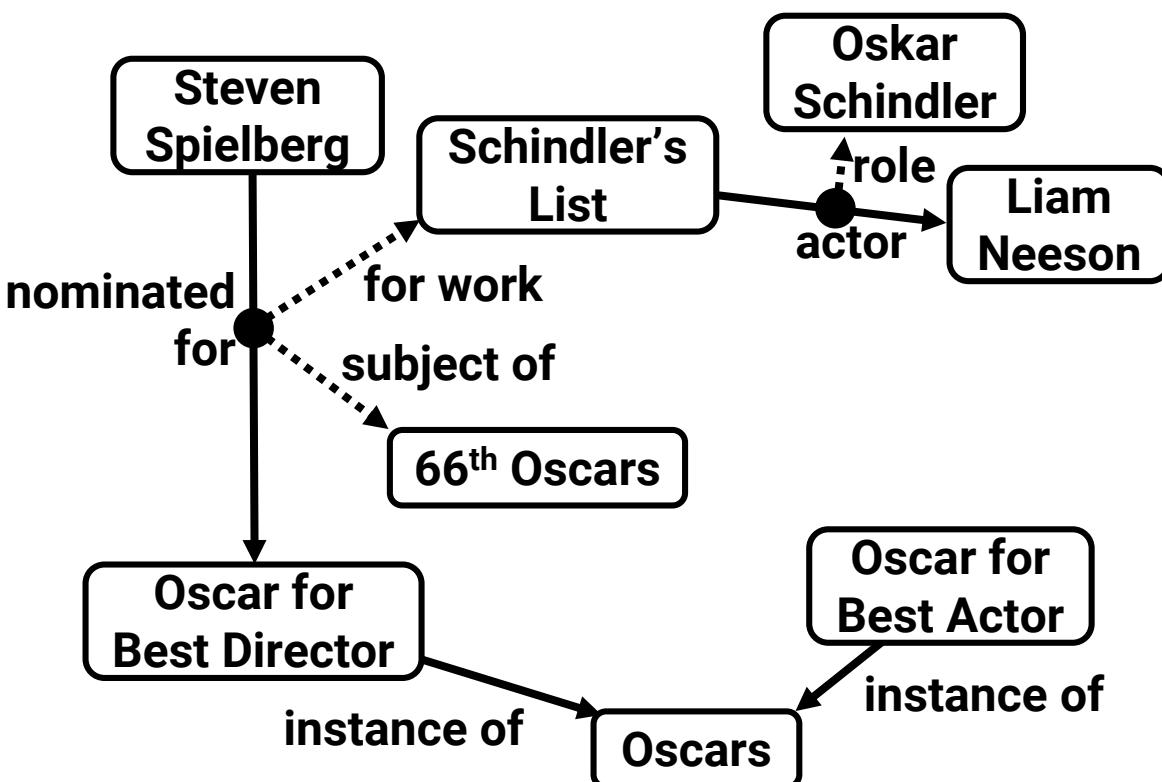


Inference HKG

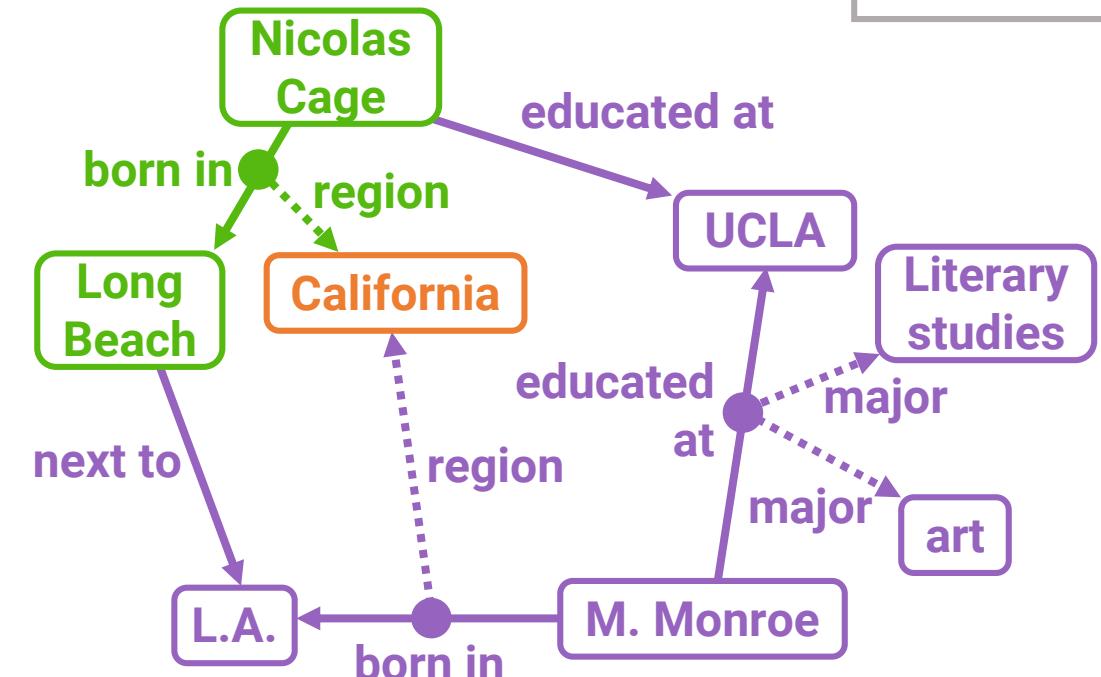
# Inductive Link Prediction on HKGs

((Nicolas Cage, born in, Long Beach),  
 {(region, ? )})

— known  
 — new



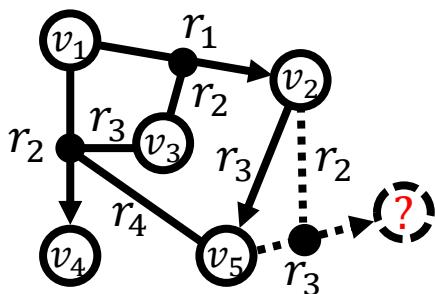
Training HKG



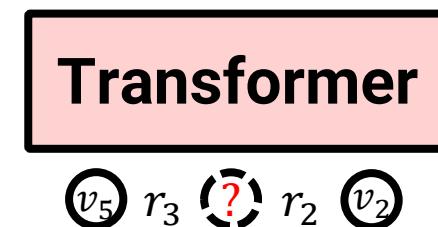
Inference HKG

# Existing HKG Methods

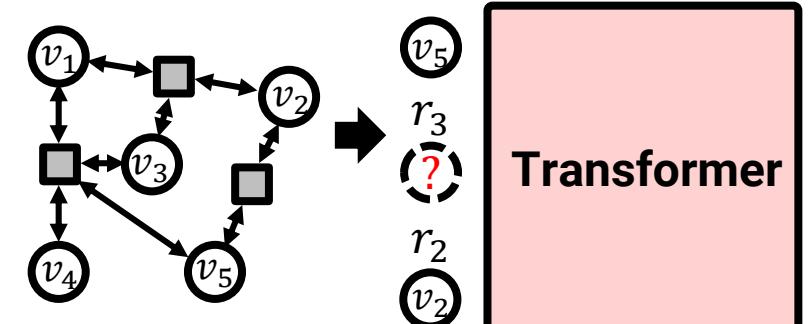
- Incorporate only limited structural information and fail to utilize HKG structures
  - Transformer-based methods: process each fact individually
  - GNN-based encoders: redundant / does not consider relations and positions of entities



Hyper-relational  
Knowledge Graph



Transformer-based Methods



Existing GNN-based Methods

Inductive Inference

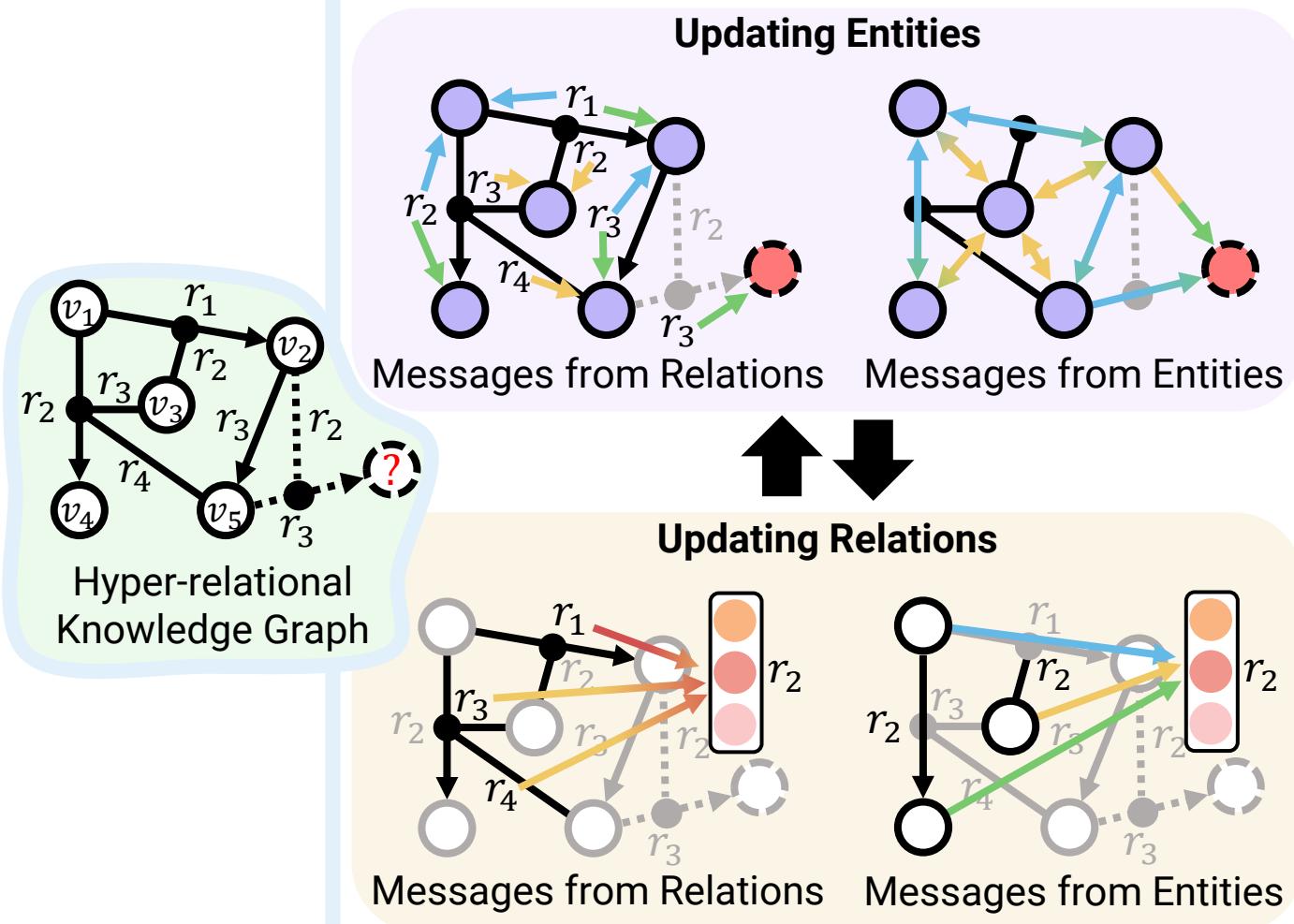


Structure Utilization



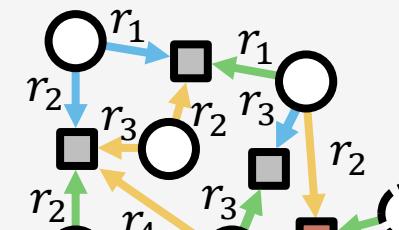
# MAYPL: Message Passing Framework for Hyper-Relational Knowledge Graph Representation Learning

## I. Structure-Driven Initializer

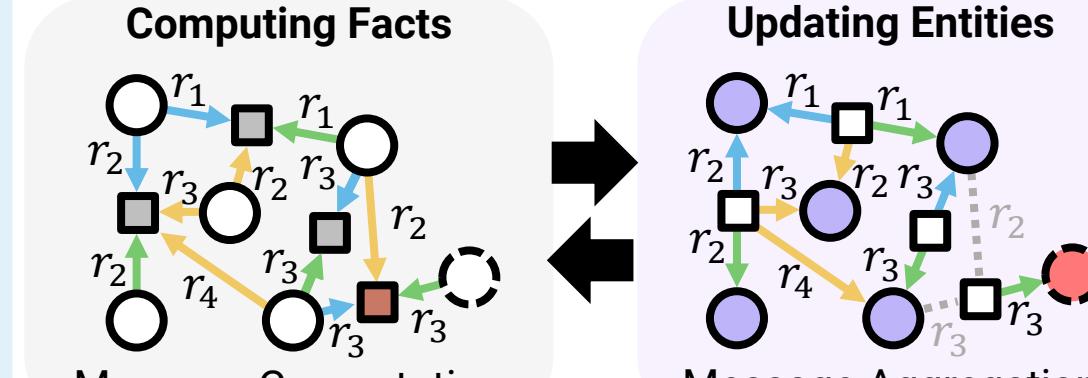


## II. Attentive Neural Message Passing

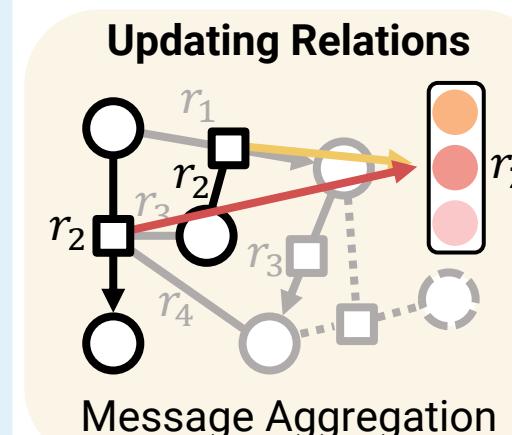
### Computing Facts



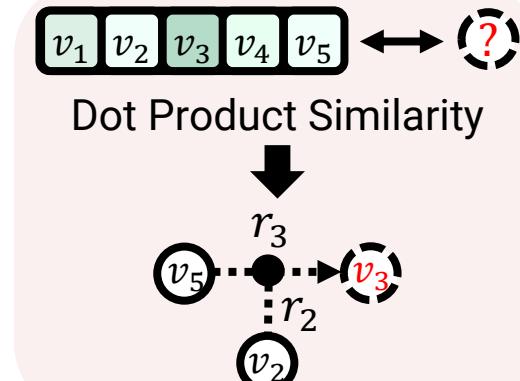
### Message Computation



### Updating Relations



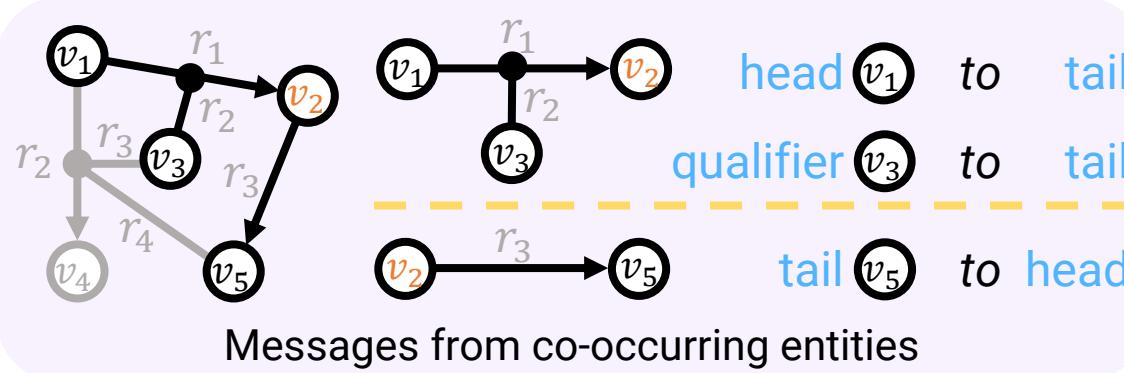
## III. Link Prediction



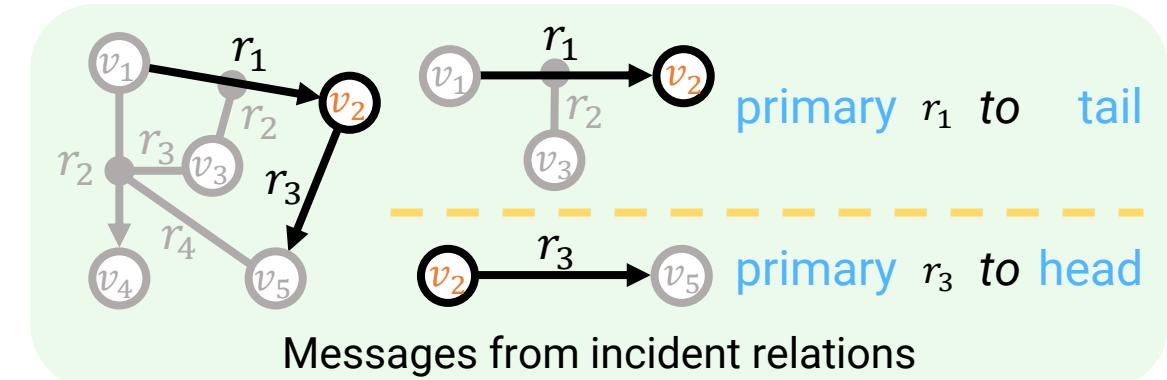
# Structure-driven Initializer

- Exploits the **interconnections**, **co-occurrence**, and **positions** of entities and relations
- Entity: Aggregate the messages of the **co-occurring entities** and **incident relations**

$$\tilde{\mathbf{v}}^{(\tilde{l})} = \frac{1}{\sum_{u \in \mathcal{V}_v} |\mathcal{H}_u \cap \mathcal{H}_v|} \sum_{u \in \mathcal{V}_v} \sum_{h \in \mathcal{H}_u \cap \mathcal{H}_v} \tilde{U}_{\lambda_h(v)}^{(\tilde{l})} \tilde{W}_{\lambda_h(u)}^{(\tilde{l})} \tilde{\mathbf{u}}^{(l-1)} + \frac{1}{|\mathcal{R}_v|} \sum_{r \in \mathcal{R}_v} \tilde{A}_{\tau_r(v)}^{(\tilde{l})} \tilde{\mathbf{r}}^{(l-1)}$$



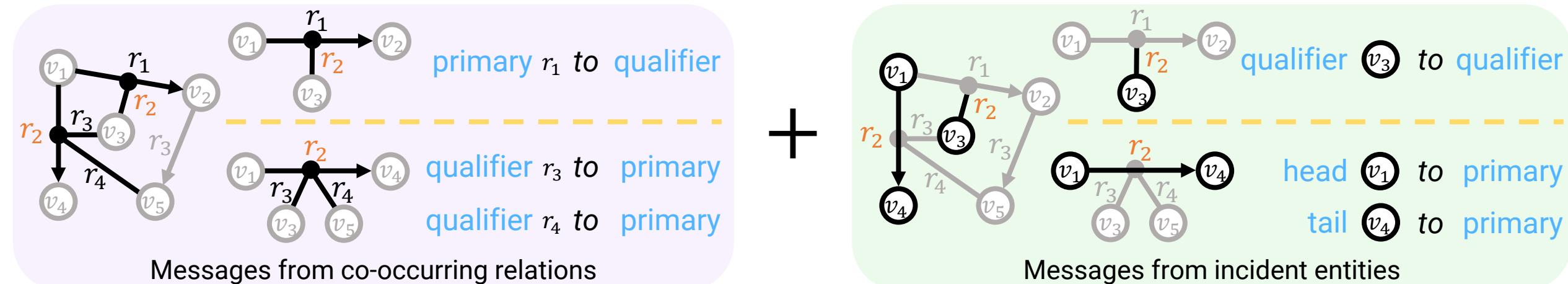
+



# Structure-driven Initializer

- Exploits the **interconnections**, **co-occurrence**, and **positions** of entities and relations
- Relation: Aggregate the messages of the **co-occurring relations** and **incident entities**

$$\tilde{\mathbf{r}}^{(\tilde{l})} = \frac{1}{\sum_{y \in \mathcal{R}_r} |\mathcal{H}_y \cap \mathcal{H}_r|} \sum_{y \in \mathcal{R}_r} \sum_{h \in \mathcal{H}_y \cap \mathcal{H}_r} \hat{U}_{\lambda_h(r)}^{(\tilde{l})} \hat{W}_{\lambda_h(y)}^{(\tilde{l})} \tilde{\mathbf{y}}^{(l-1)} + \frac{1}{|\mathcal{V}_r|} \sum_{v \in \mathcal{V}_r} \hat{A}_{\tau_r(v)}^{(\tilde{l})} \tilde{\mathbf{v}}^{(l-1)}$$



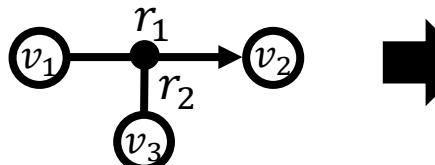
# Attentive Neural Message Passing

- Updates entity and relation representations by attentively aggregating facts' messages
- Computes a fact's message by considering which entities and relations comprise the fact
  - Decompose each fact as a set of its relation-entity pairs
  - compute a pair's message by considering the **entities** and **relations** and their **positions** within the fact

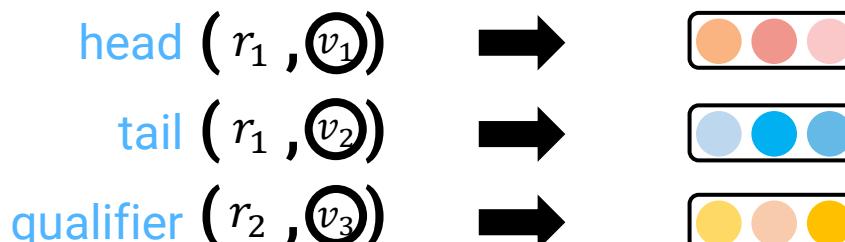
$$\mathbf{p}^{(l)} = \mathbf{P}_{\lambda_h(v)}^{(l)} \left( \left( \mathbf{W}_{\lambda_h(v)}^{(l)} \mathbf{v}^{(l-1)} \right) \odot \left( \mathbf{U}_{\lambda_h(v)}^{(l)} \mathbf{r}^{(l-1)} \right) \right)$$

- Compute a fact's message by aggregating messages of its relation-entity pairs

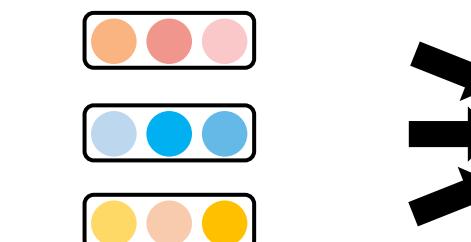
$$\mathbf{h}^{(l)} = \frac{1}{|(\mathcal{R} \times \mathcal{V})_h|} \sum_{p \in (\mathcal{R} \times \mathcal{V})_h} \mathbf{p}^{(l)}$$



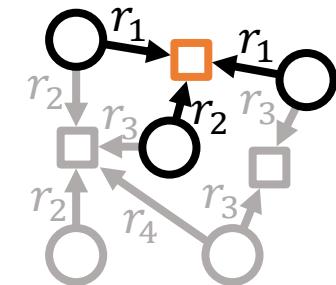
Hyper-relational Fact



Fact Decomposition



Compute Pairs'  
Messages



Compute Fact's  
Message

# Attentive Neural Message Passing

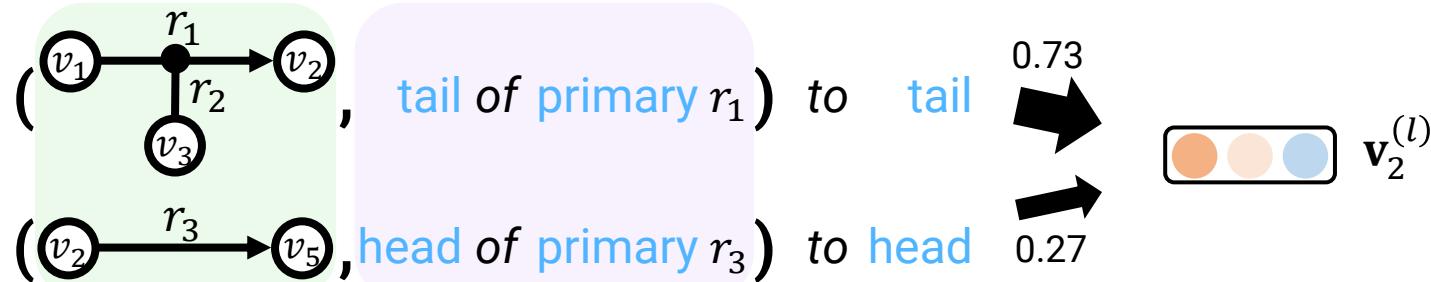
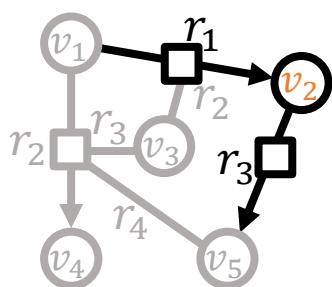
- Updates an entity representation by considering which fact the entity belongs to

- Considers pairs of **incident relations** and the **corresponding facts**

$$\mathbf{q}^{(l)} = \mathbf{Q}_{\lambda_h(v)}^{(l)} \left( \mathbf{h}^{(l)} \odot \left( \mathbf{A}_{\lambda_h(v)}^{(l)} \mathbf{r}^{(l-1)} \right) \right)$$

- Attentively aggregate relation-fact pairs

$$\mathbf{v}^{(l)} = \sum_{q \in (\mathcal{R} \times \mathcal{H})_v} \alpha_{q,v}^{(l)} \mathbf{B}^{(l)} \mathbf{q}^{(l)}, \text{ where } \alpha_{q,v}^{(l)} = \frac{\exp(\mathbf{a}^{(l)} \cdot \sigma(\mathbf{Q}^{(l)} \mathbf{v}^{(l-1)} + \mathbf{K}^{(l)} \mathbf{q}^{(l)}))}{\sum_{k \in (\mathcal{R} \times \mathcal{H})_v} \exp(\mathbf{a}^{(l)} \cdot \sigma(\mathbf{Q}^{(l)} \mathbf{v}^{(l-1)} + \mathbf{K}^{(l)} \mathbf{k}^{(l)}))}$$



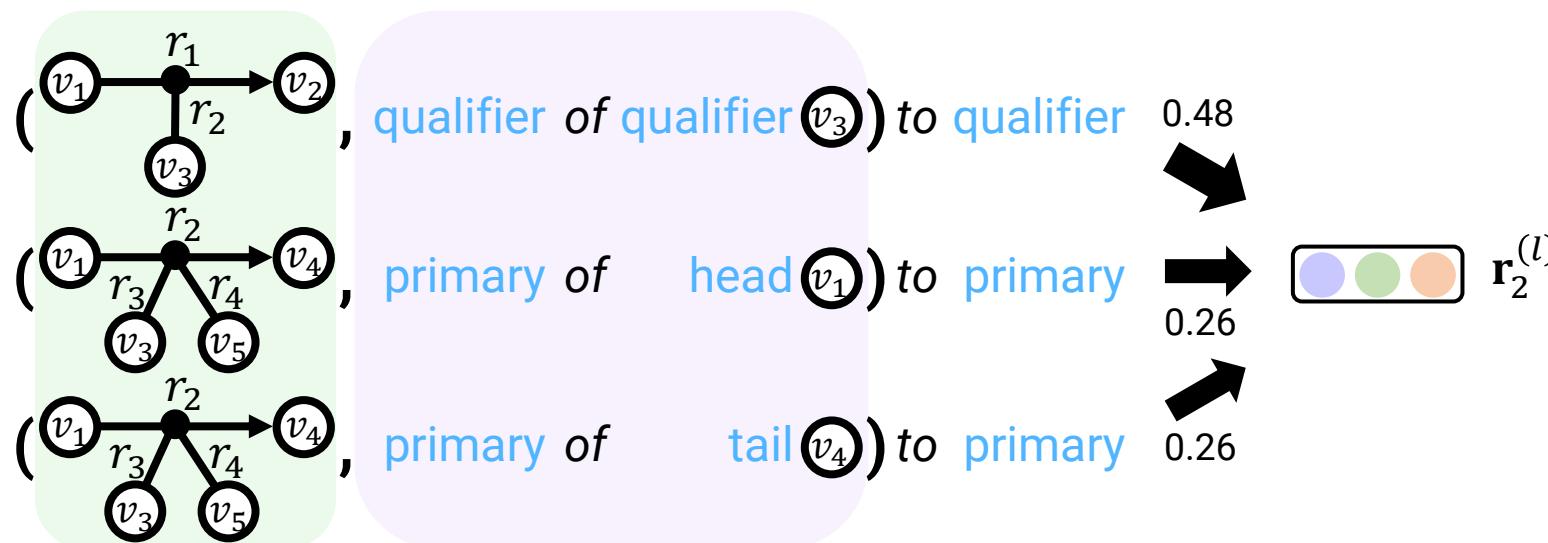
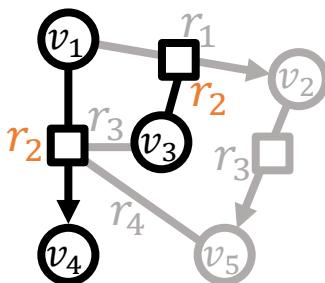
# Attentive Neural Message Passing

- Updates an relation representation by considering which fact the relation belongs to
  - Considers pairs of **incident entities** and the **corresponding facts**

$$\bar{\mathbf{q}}^{(l)} = \bar{\mathbf{Q}}_{\lambda_h(r)}^{(l)} \left( \mathbf{h}^{(l)} \odot \left( \bar{\mathbf{A}}_{\lambda_h(v)}^{(l)} \mathbf{v}^{(l-1)} \right) \right)$$

- Attentively aggregate relation-fact pairs

$$\mathbf{r}^{(l)} = \sum_{\bar{q} \in (\mathcal{V} \times \mathcal{H})_r} \bar{\alpha}_{\bar{q}, r}^{(l)} \bar{\mathbf{B}}^{(l)} \bar{\mathbf{q}}^{(l)}, \text{ where } \bar{\alpha}_{\bar{q}, r}^{(l)} = \frac{\exp(\bar{\mathbf{a}}^{(l)} \cdot \sigma(\bar{\mathbf{Q}}^{(l)} \mathbf{r}^{(l-1)} + \bar{\mathbf{K}}^{(l)} \bar{\mathbf{q}}^{(l)}))}{\sum_{\bar{k} \in (\mathcal{V} \times \mathcal{H})_r} \exp(\bar{\mathbf{a}}^{(l)} \cdot \sigma(\bar{\mathbf{Q}}^{(l)} \mathbf{r}^{(l-1)} + \bar{\mathbf{K}}^{(l)} \bar{\mathbf{k}}^{(l)}))}$$



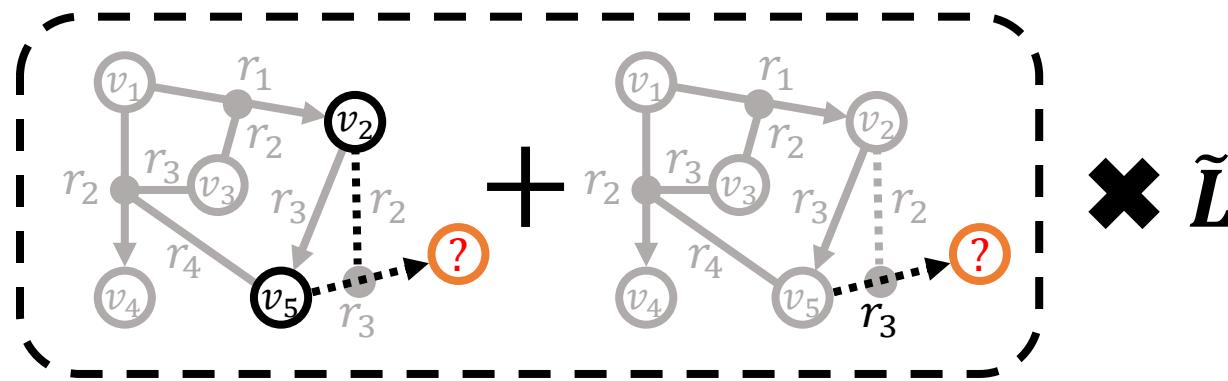
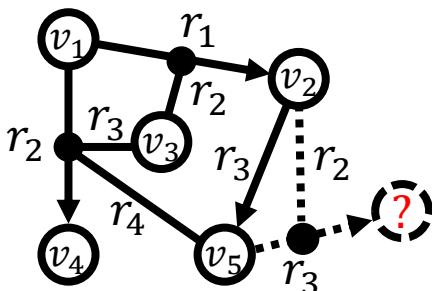
- Structure-driven initializer

- $\tilde{\mathbf{x}}^{(\tilde{l})} = \sum_{v \in \mathcal{V}_x} \tilde{\mathbf{U}}_{\lambda_h(x)}^{(\tilde{l})} \tilde{\mathbf{W}}_{\lambda_h(v)}^{(\tilde{l})} \tilde{\mathbf{v}}^{(\tilde{l}-1)} + \tilde{\mathbf{A}}_{\tau_r(v)}^{(\tilde{l})} \tilde{\mathbf{r}}^{(\tilde{l}-1)}$

- Attentive Neural Message Passing

- $\mathbf{x}^{(l)} = \mathbf{B}^{(l)} \left( \mathbf{Q}_{\lambda_h(x)}^{(l)} \left( \mathbf{h}^{(l)} \odot \left( \mathbf{A}_{\lambda_h(x)}^{(l)} \mathbf{r}^{(l-1)} \right) \right) \right)$

- Compute the dot product similarity between  $\mathbf{x}^{(L)}$  and each entity representation
  - MAYPL predicts the missing entity as the entity with the highest similarity



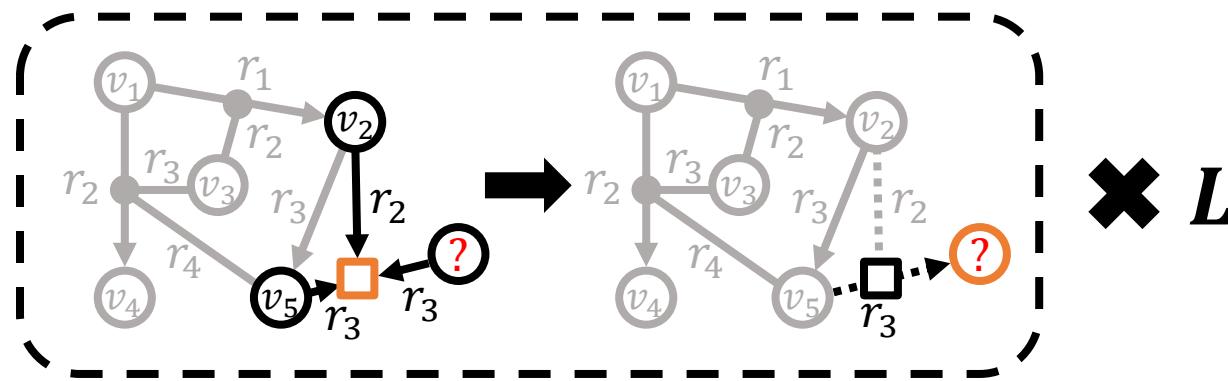
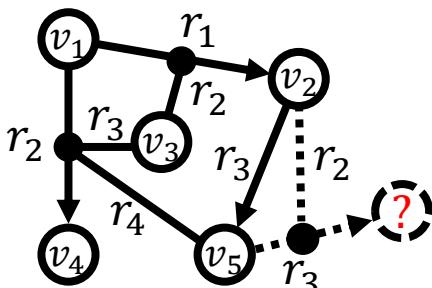
- Structure-driven initializer

- $\tilde{\mathbf{x}}^{(\tilde{l})} = \sum_{v \in \mathcal{V}_x} \tilde{\mathbf{U}}_{\lambda_h(x)}^{(\tilde{l})} \tilde{\mathbf{W}}_{\lambda_h(v)}^{(\tilde{l})} \tilde{\mathbf{v}}^{(l-1)} + \tilde{\mathbf{A}}_{\tau_r(v)}^{(\tilde{l})} \tilde{\mathbf{r}}^{(\tilde{l}-1)}$

- Attentive Neural Message Passing

- $\mathbf{x}^{(l)} = \mathbf{B}^{(l)} \left( \mathbf{Q}_{\lambda_h(x)}^{(l)} \left( \mathbf{h}^{(l)} \odot \left( \mathbf{A}_{\lambda_h(x)}^{(l)} \mathbf{r}^{(l-1)} \right) \right) \right)$

- Compute the dot product similarity between  $\mathbf{x}^{(L)}$  and each entity representation
  - MAYPL predicts the missing entity as the entity with the highest similarity



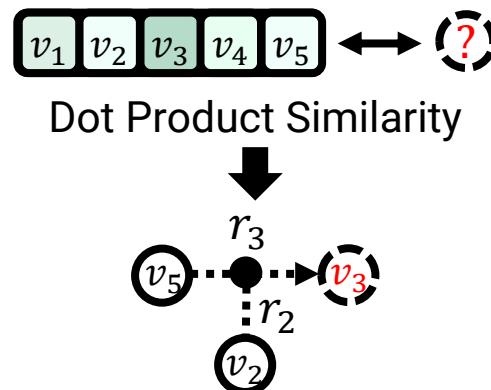
- Structure-driven initializer

- $\tilde{\mathbf{x}}^{(\tilde{l})} = \sum_{v \in \mathcal{V}_x} \tilde{\mathbf{U}}_{\lambda_h(x)}^{(\tilde{l})} \tilde{\mathbf{W}}_{\lambda_h(v)}^{(\tilde{l})} \tilde{\mathbf{v}}^{(l-1)} + \tilde{\mathbf{A}}_{\tau_r(v)}^{(\tilde{l})} \tilde{\mathbf{r}}^{(\tilde{l}-1)}$

- Attentive Neural Message Passing

- $\mathbf{x}^{(l)} = \mathbf{B}^{(l)} \left( \mathbf{Q}_{\lambda_h(x)}^{(l)} \left( \mathbf{h}^{(l)} \odot \left( \mathbf{A}_{\lambda_h(x)}^{(l)} \mathbf{r}^{(l-1)} \right) \right) \right)$

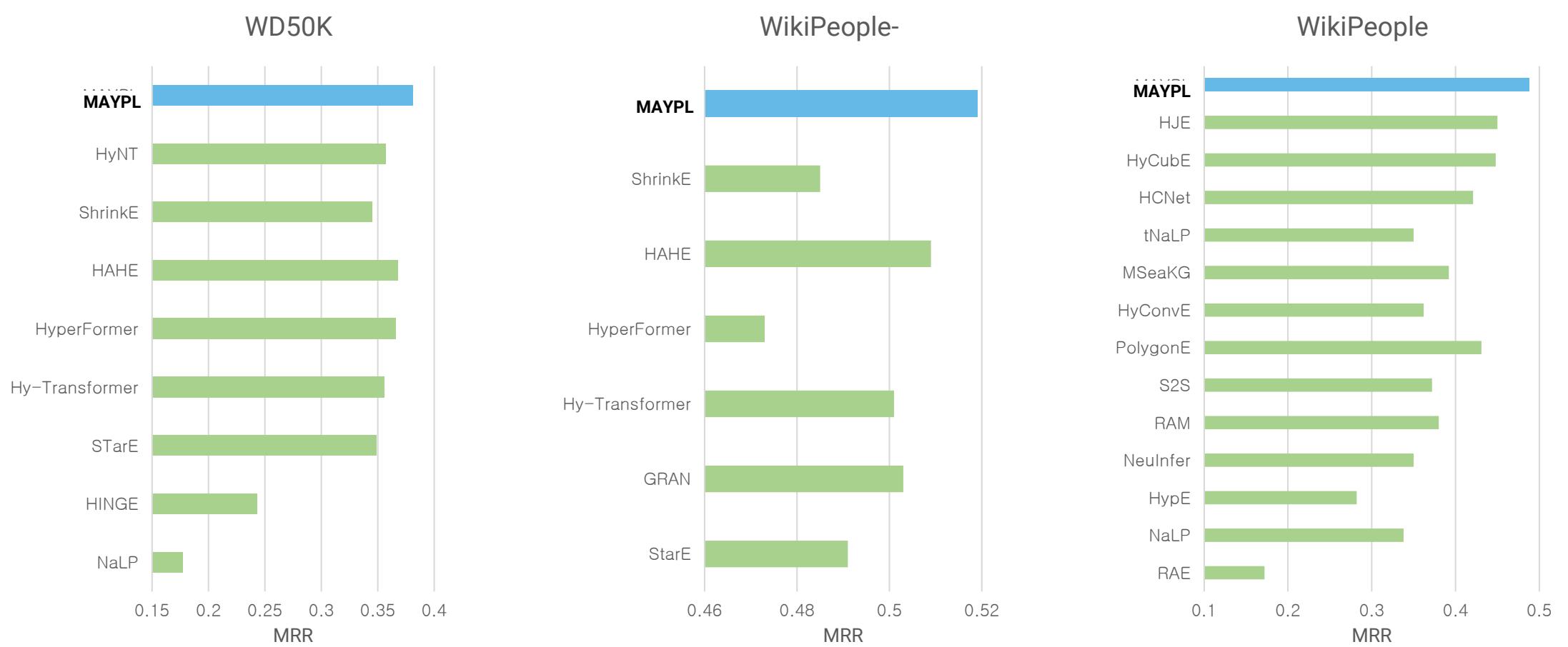
- Compute the dot product similarity between  $\mathbf{x}^{(L)}$  and each entity representation
  - MAYPL predicts the missing entity as the entity with the highest similarity



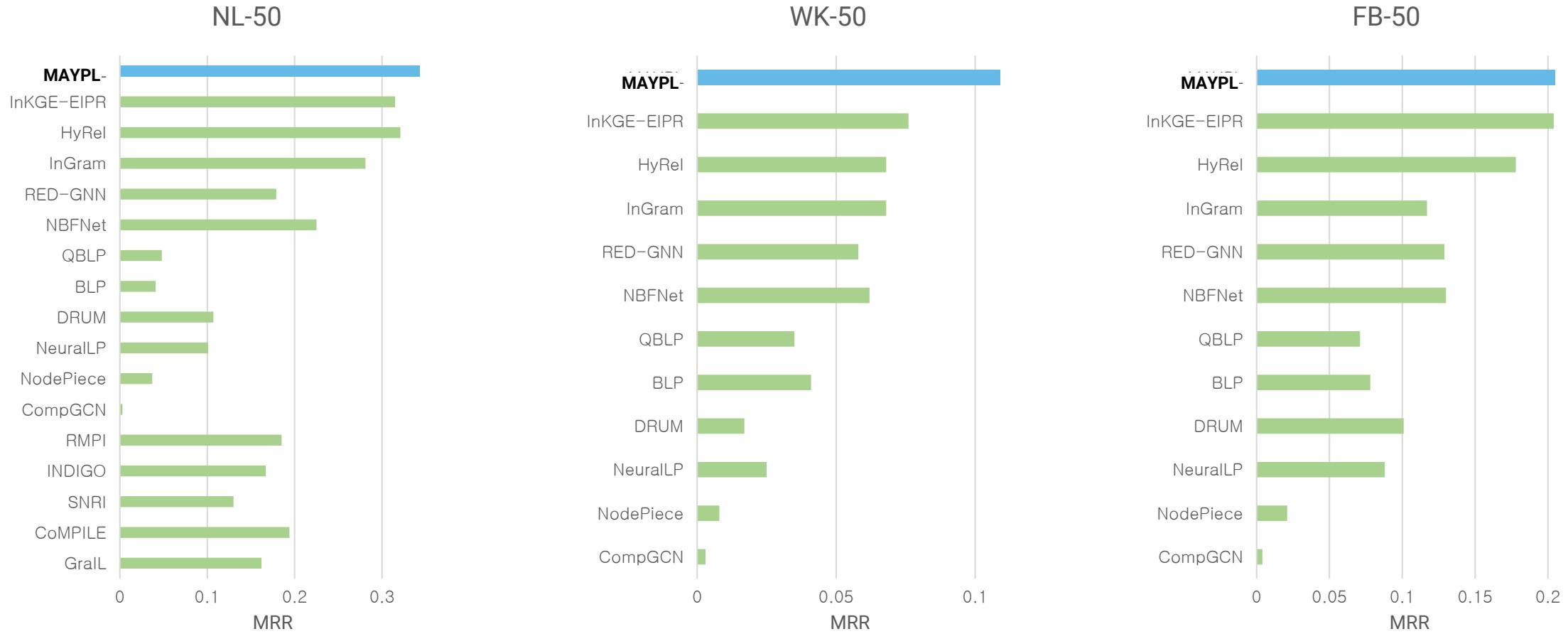
# Experimental Results

- Datasets
  - **3 Transductive HKG** datasets: WD50K, WikiPeople<sup>-</sup>, WikiPeople
  - **12 Inductive KG** datasets from InGram (e.g., NL-100, WK-100, FB-100)
  - **4 Inductive HKG** datasets: WD20K(100)v1, WD20K(100)v2, WP-IND, MFB-IND
- Baselines
  - **41 knowledge graph completion methods**, compared with different baseline methods on different datasets

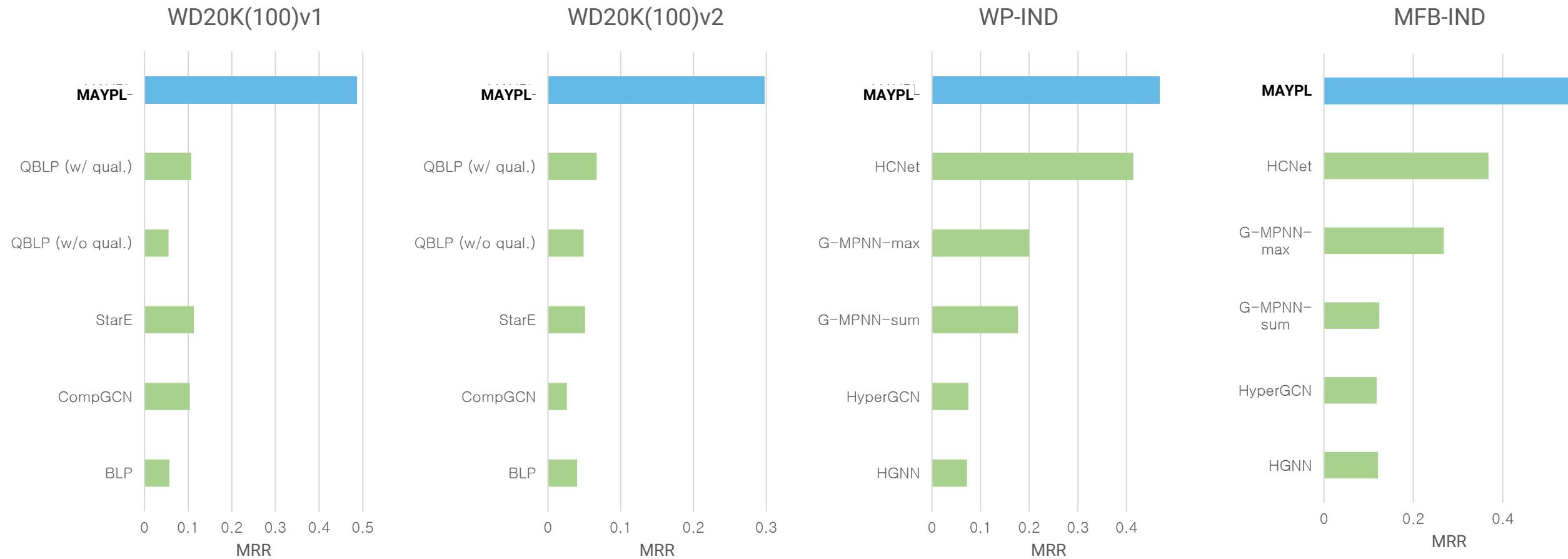
# Transductive Link Prediction on HKGs



# Inductive Link Prediction on KGs



# Inductive Link Prediction on HKGs



- Employing an **HKG's structure is crucial** for HKG reasoning
  - Thoroughly learning and exploiting the structure of an HKG is necessary and sufficient for learning representations on HKGs
- Propose **MAYPL**, the first structure-oriented representation learning method for HKGs
  - Can be applied in both transductive and inductive settings
- MAYPL can make inductive inferences with new entities and relations by **learning how to compute representations based solely on the structure** of a given HKG
- MAYPL outperforms **41 different methods on 19 benchmark datasets** in varied settings
  - Transductive link prediction on HKGs, inductive link prediction on KGs, and inductive link prediction on HKGs

- Some slides are made based on the following references.
  - P. Rosso et al., "Beyond Triplets: Hyper-Relational Knowledge Graph Embedding for Link Prediction", TheWebConf, 2020.
  - M. Galkin et al., "Message Passing for Hyper-Relational Knowledge Graphs", EMNLP, 2020.
  - Q. Wang et al., "Link Prediction on N-ary Relational Facts: A Graph-based Approach", ACL Findings, 2020.
  - M. Ali et al., "Improving Inductive Link Prediction Using Hyper-relational Facts", ISWC, 2021.
  - H. Luo et al., "HAHE: Hierarchical Attention for Hyper-Relational Knowledge Graphs in Global and Local Level", ACL, 2023.
  - B. Xiong et al., "Shrinking Embeddings for Hyper-Relational Knowledge Graphs", ACL, 2023.
  - C. Chung et al., "Representation Learning on Hyper-Relational and Numeric Knowledge Graphs with Transformers", KDD, 2023.
  - Z. Hu et al., "HyperFormer: Enhancing Entity and Relation Interaction for Hyper-Relational Knowledge Graph Completion", CIKM, 2023.
  - J. Lee and J. J. Whang, "Structure Is All You Need: Structural Representation Learning on Hyper-Relational Knowledge Graphs", ICML, 2025.