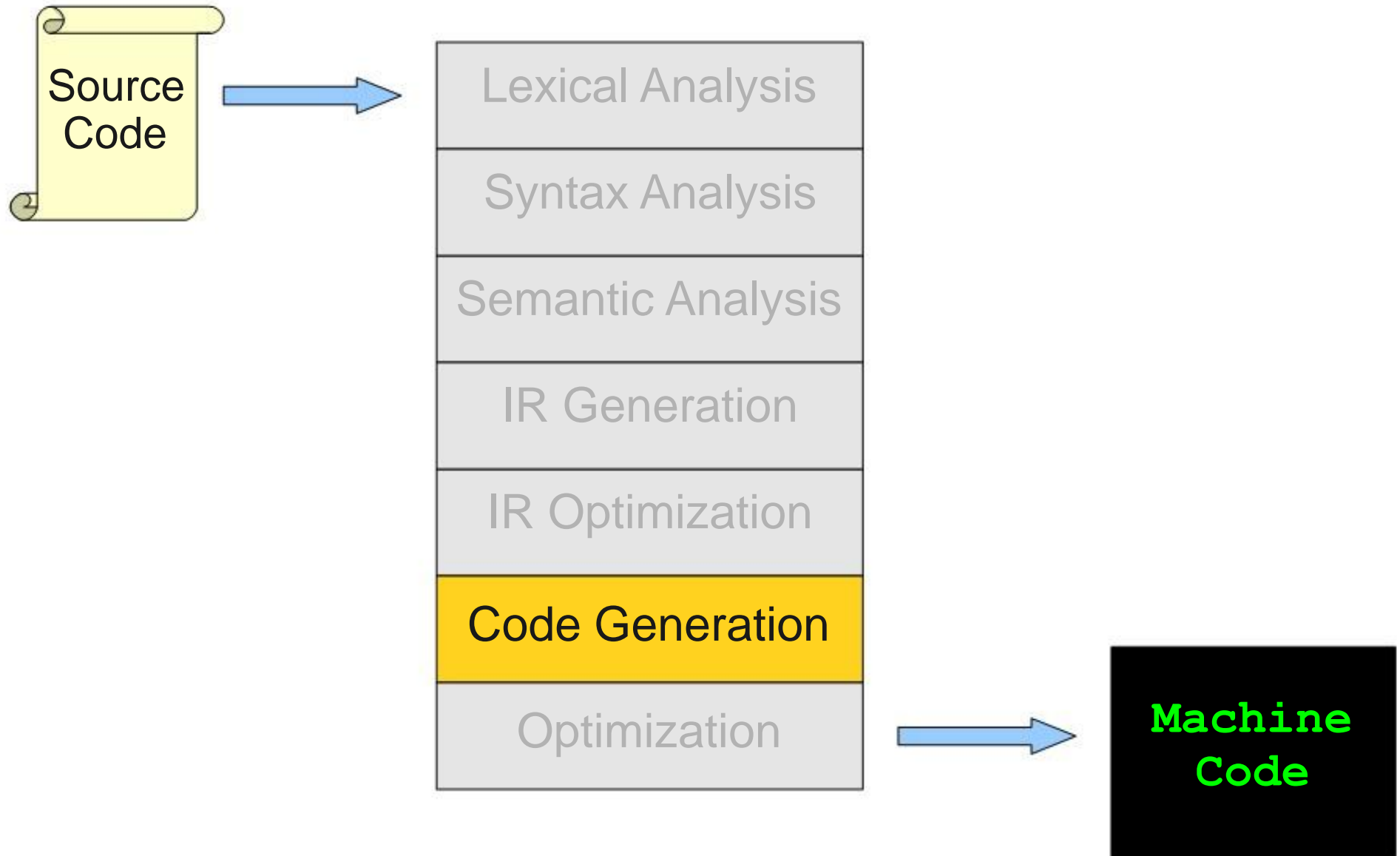


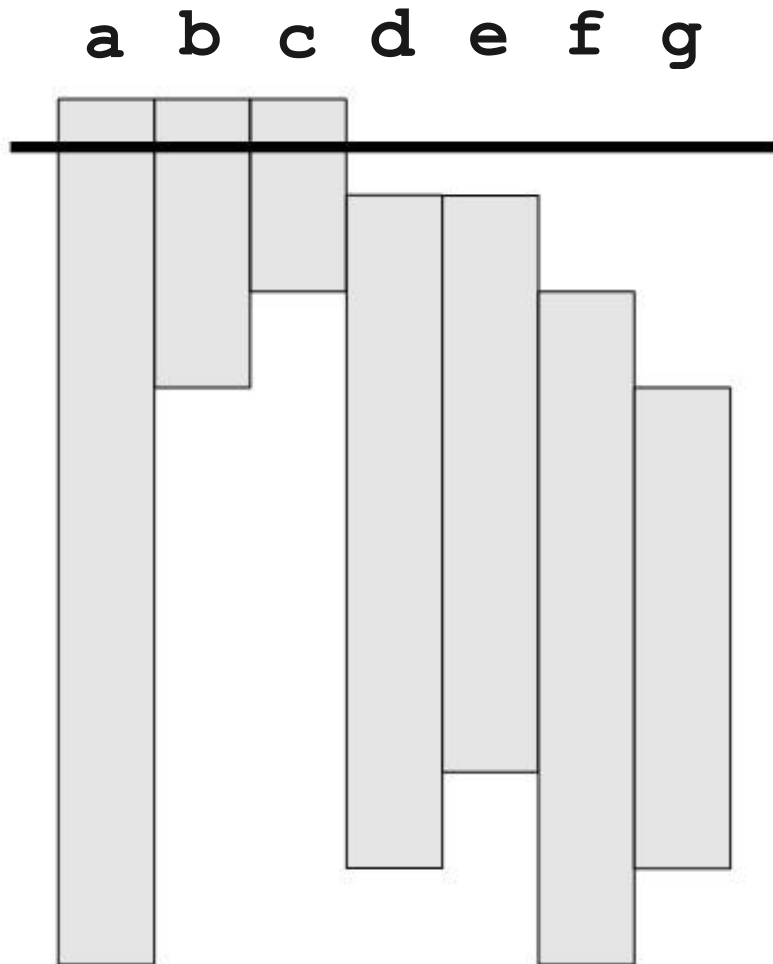
Where We Are



Register Spilling (Continue)

- If a register cannot be found for a variable v , we may need to **spill a variable into memory**.
- When we **need a register for the spilled variable**, temporarily **evict a register to memory**.
- When done with that register, write its value to the memory (if necessary) and load the old value back.
- Note: Some register allocation algorithms can handle spilling much more intelligently than this.
- Spilling is slow, but sometimes necessary.

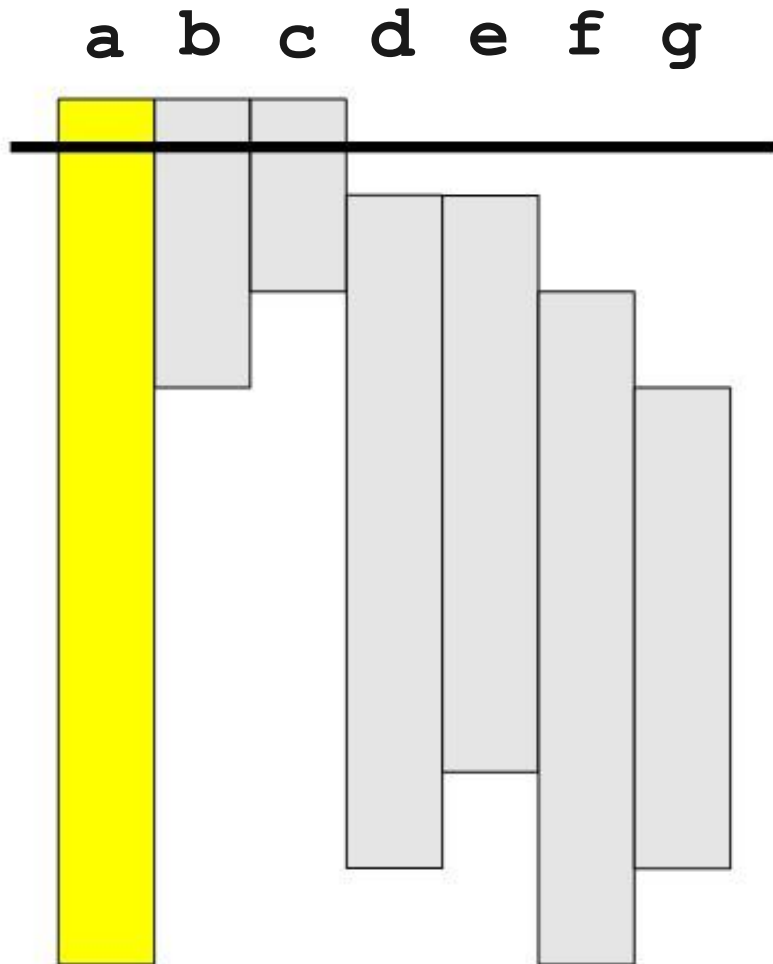
Another Example



Free Registers



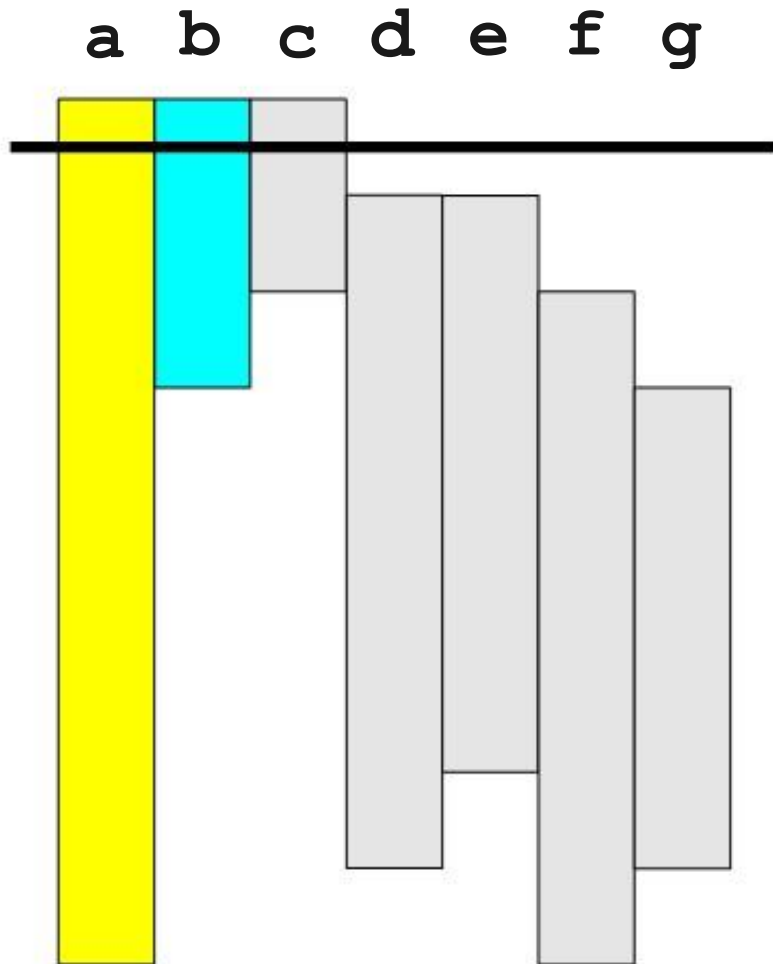
Another Example



Free Registers



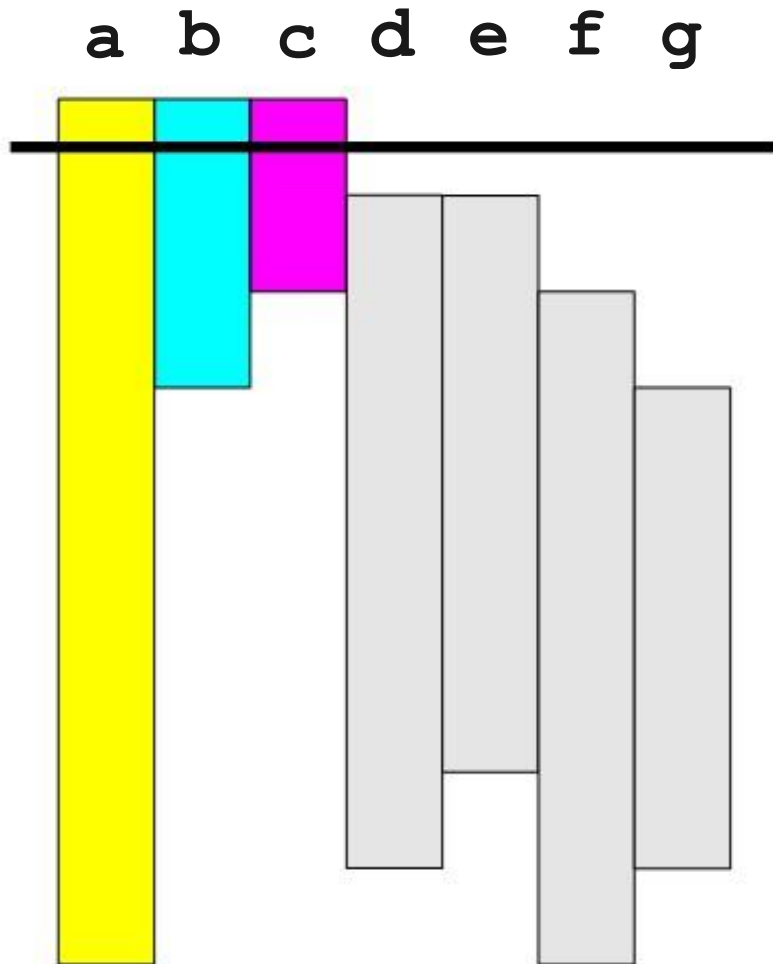
Another Example



Free Registers



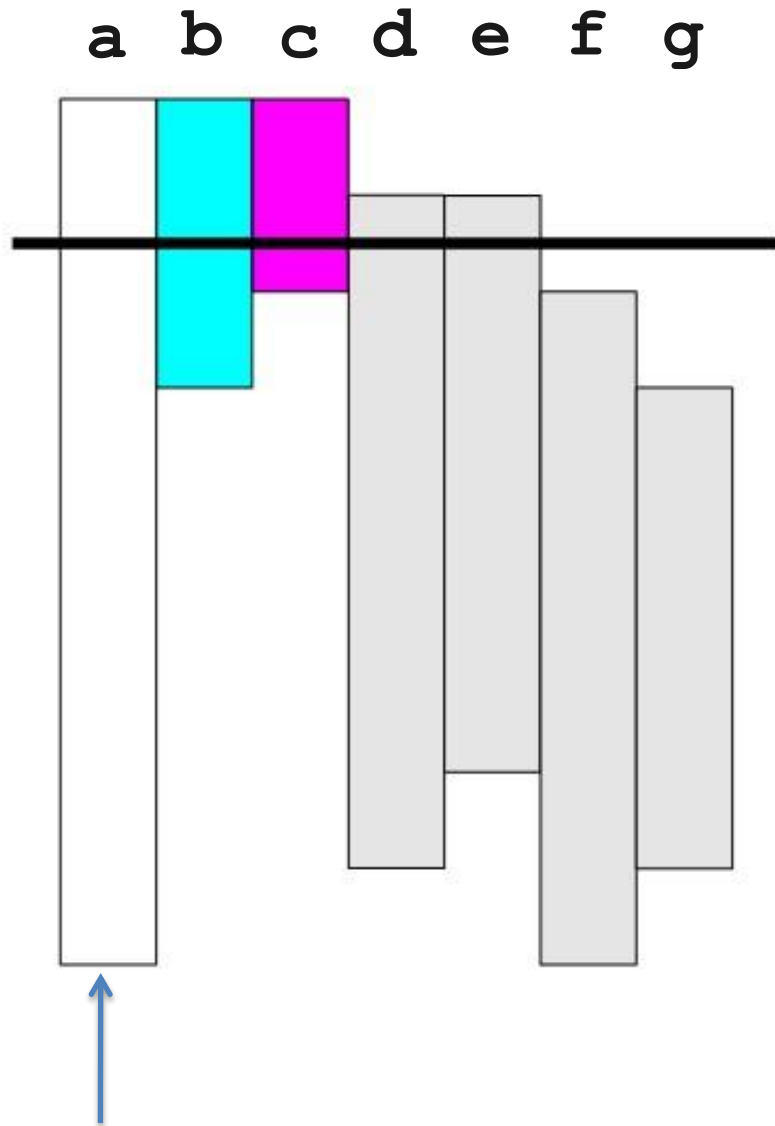
Another Example



Free Registers

R ₀	R ₁	R ₂
----------------	----------------	----------------

Another Example

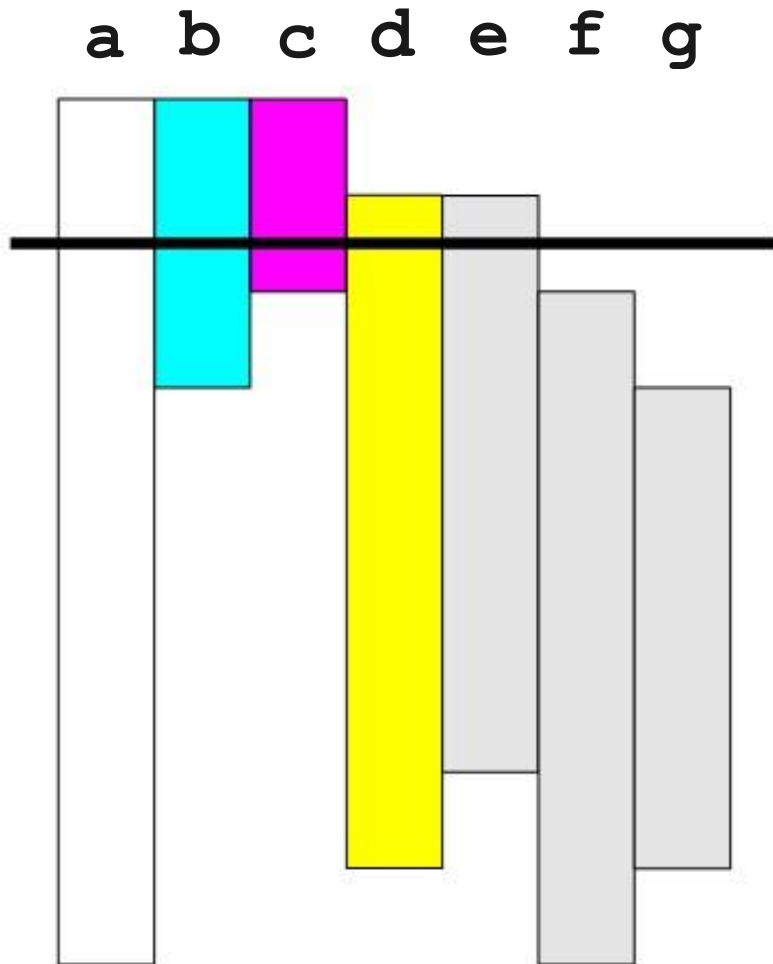


Free Registers



Spill the variable 'a' because it stays latest.

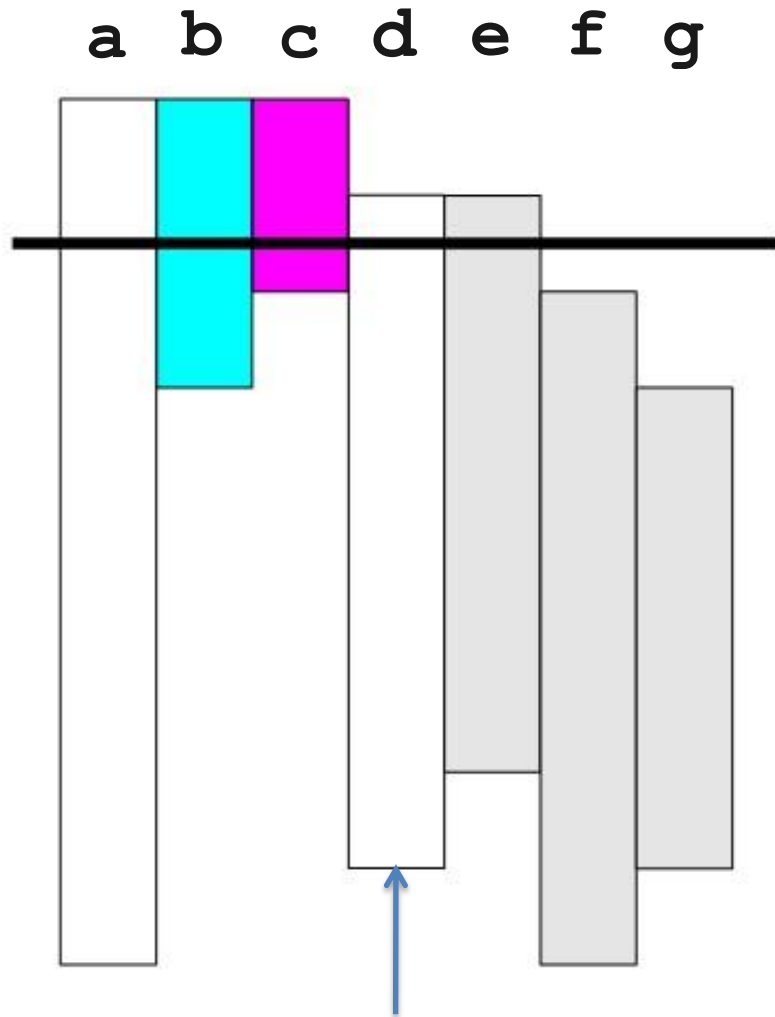
Another Example



Free Registers

R ₀	R ₁	R ₂
----------------	----------------	----------------

Another Example

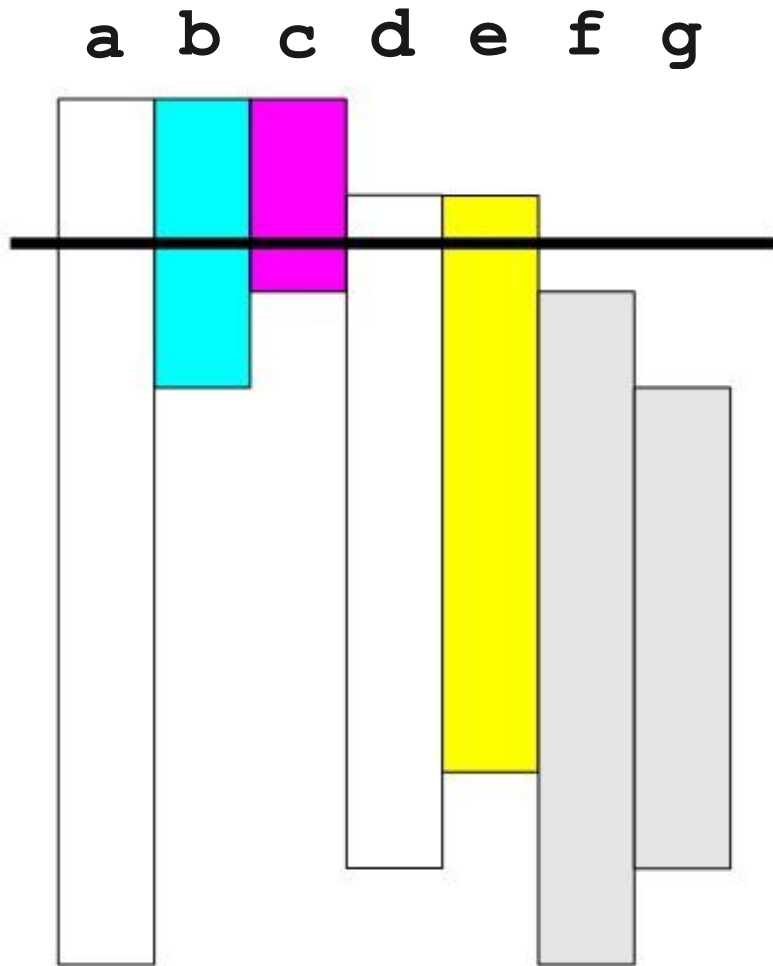


Free Registers



Spill the variable 'd'.

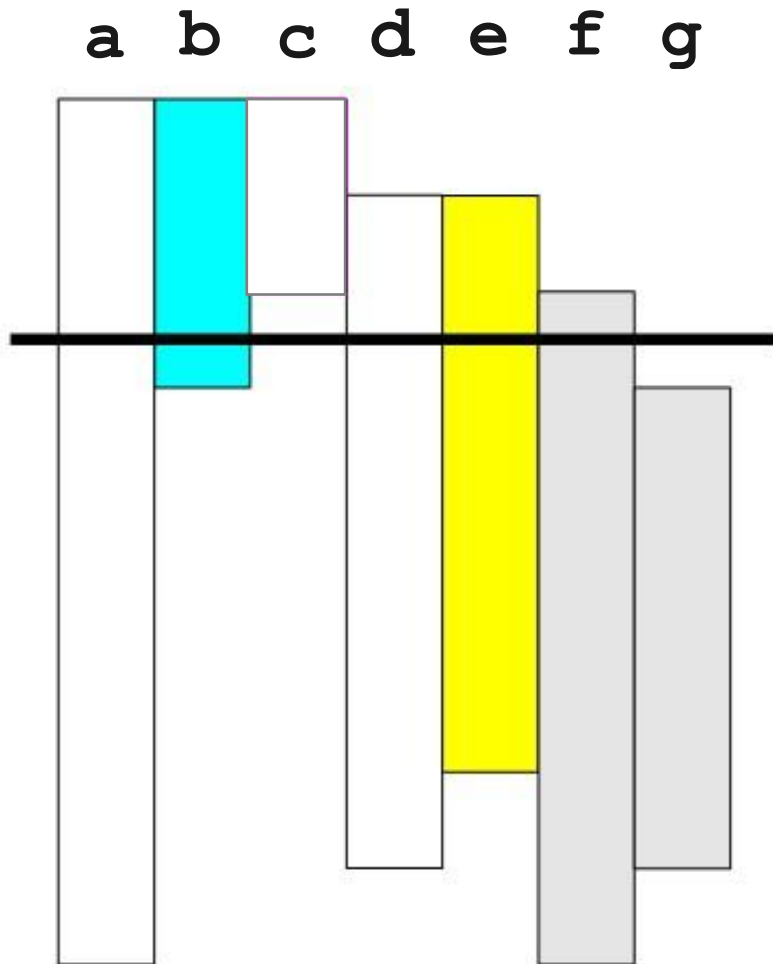
Another Example



Free Registers

R ₀	R ₁	R ₂
----------------	----------------	----------------

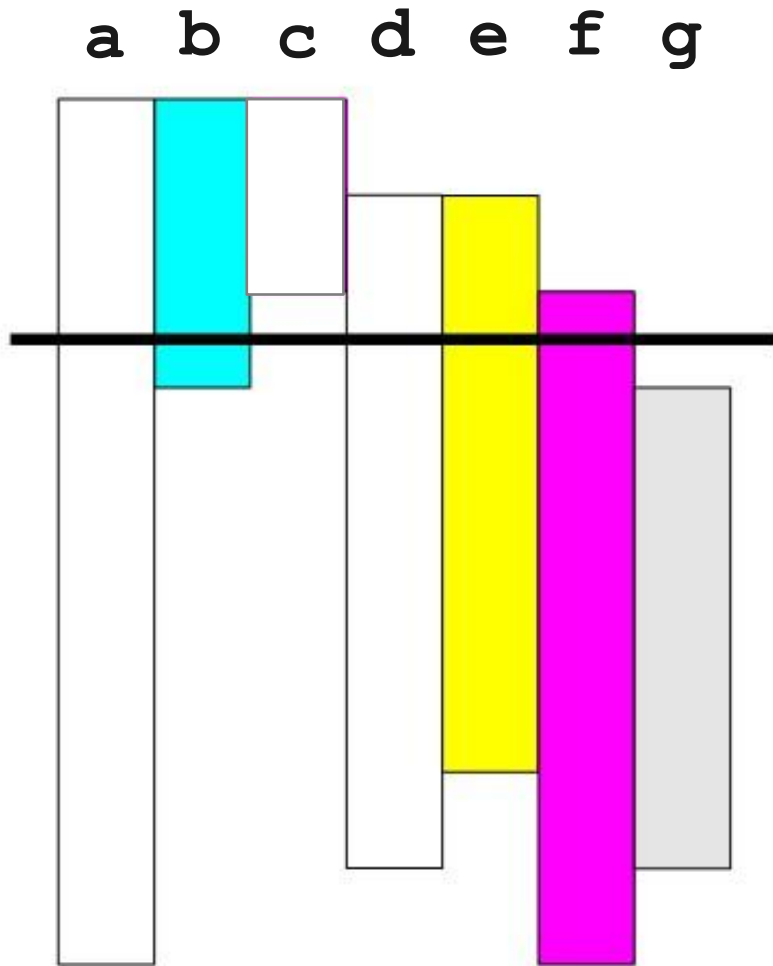
Another Example



Free Registers



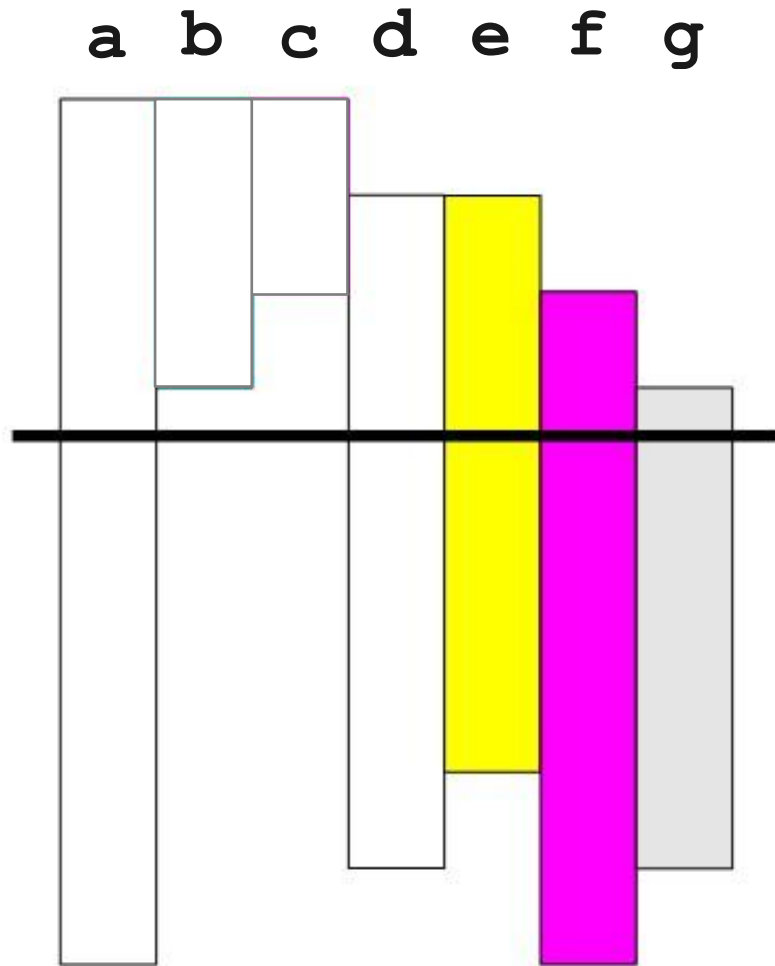
Another Example



Free Registers

R ₀	R ₁	R ₂
----------------	----------------	----------------

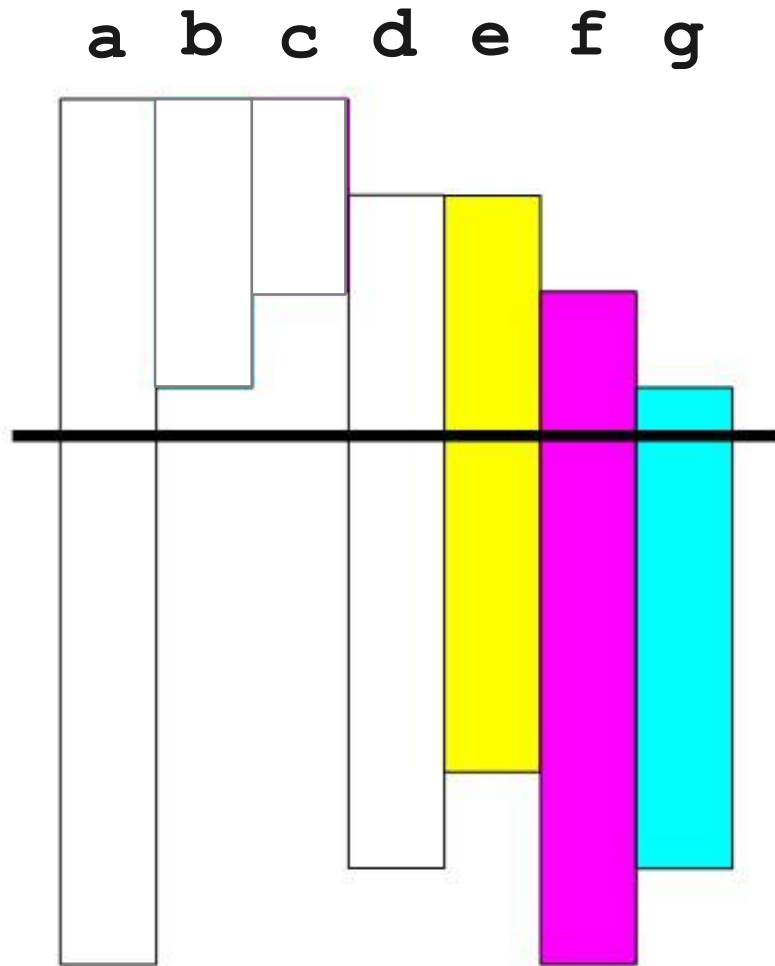
Another Example



Free Registers



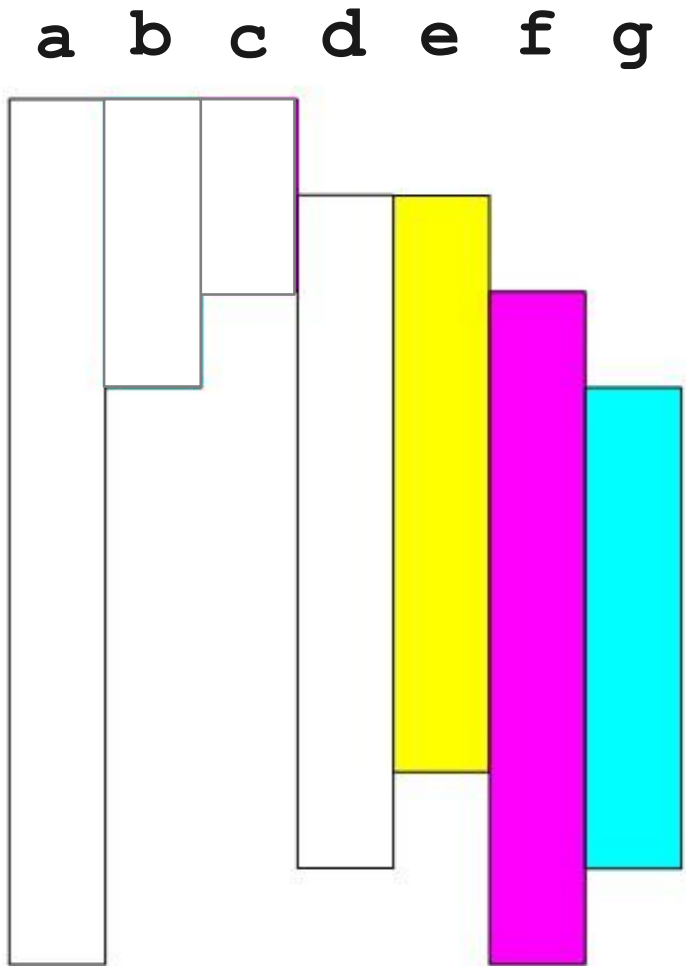
Another Example



Free Registers

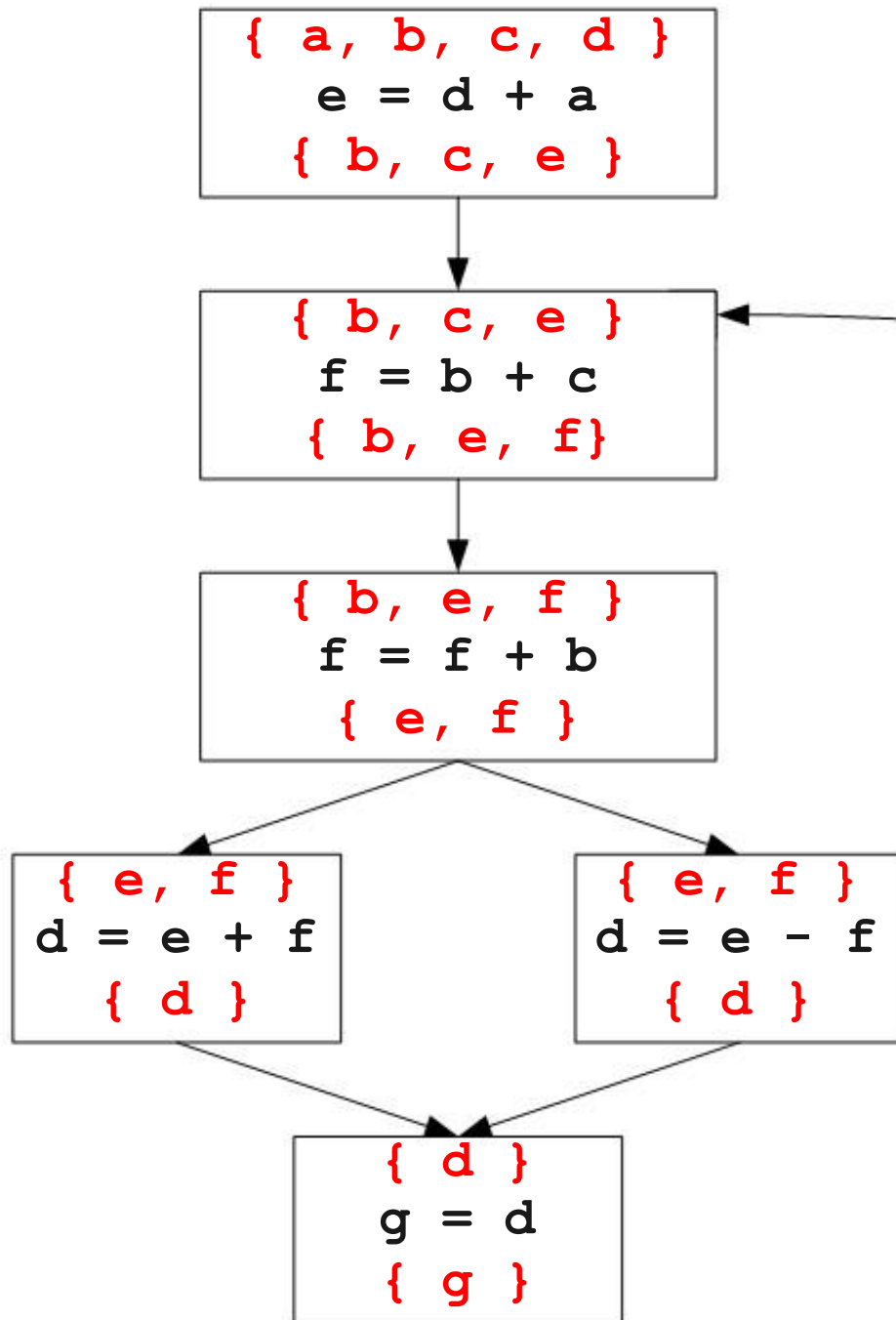


Another Example



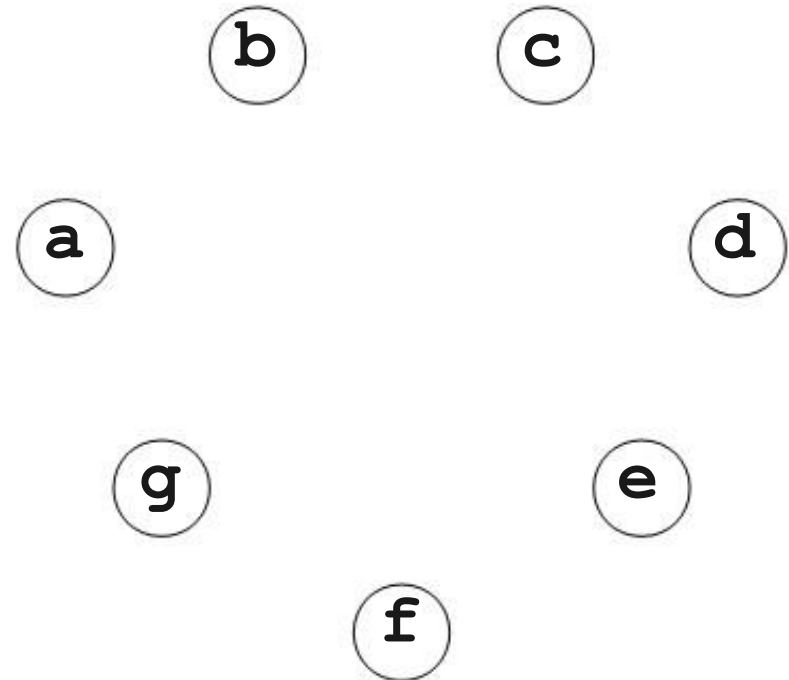
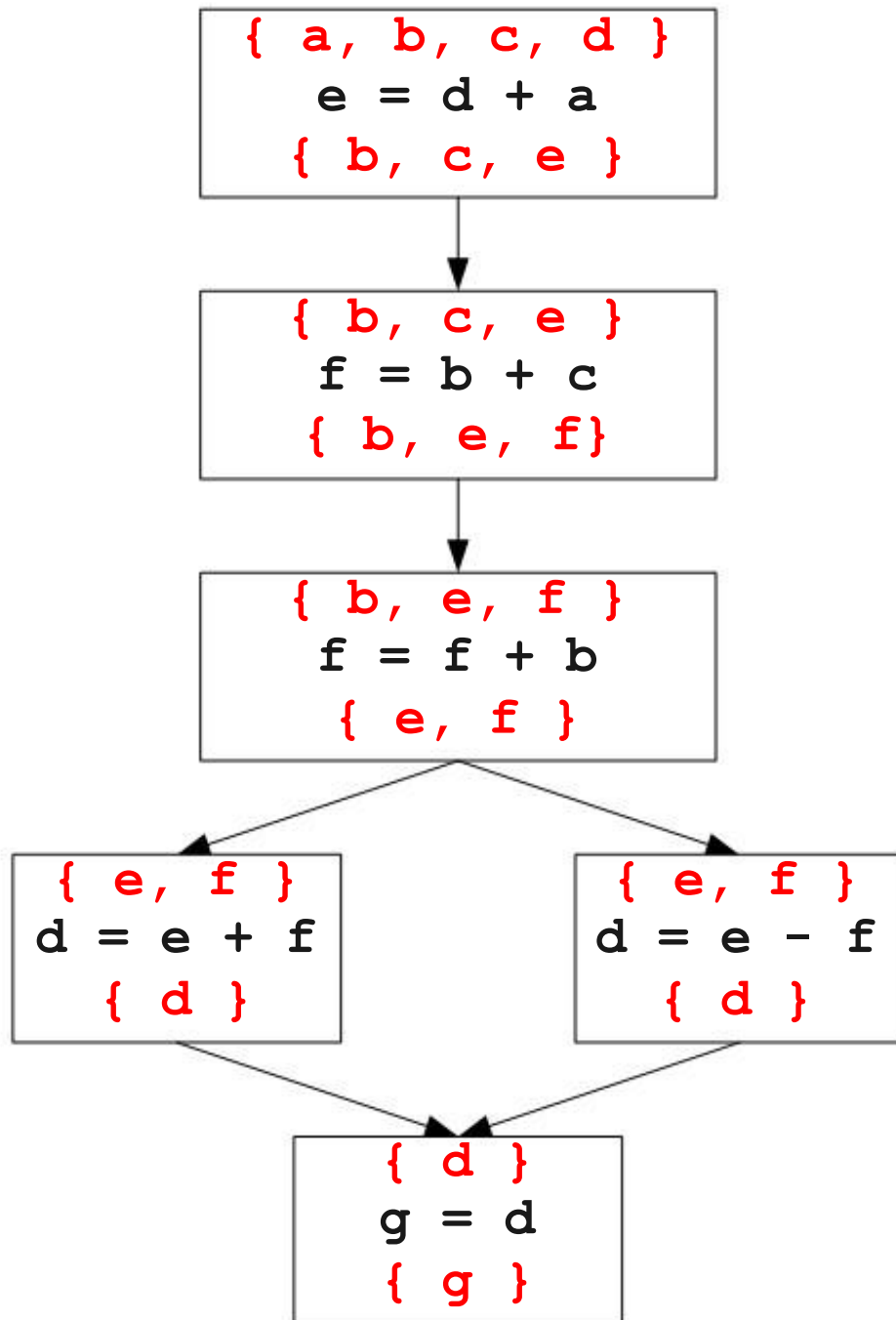
There is a smarter approach.

Smarter Approach

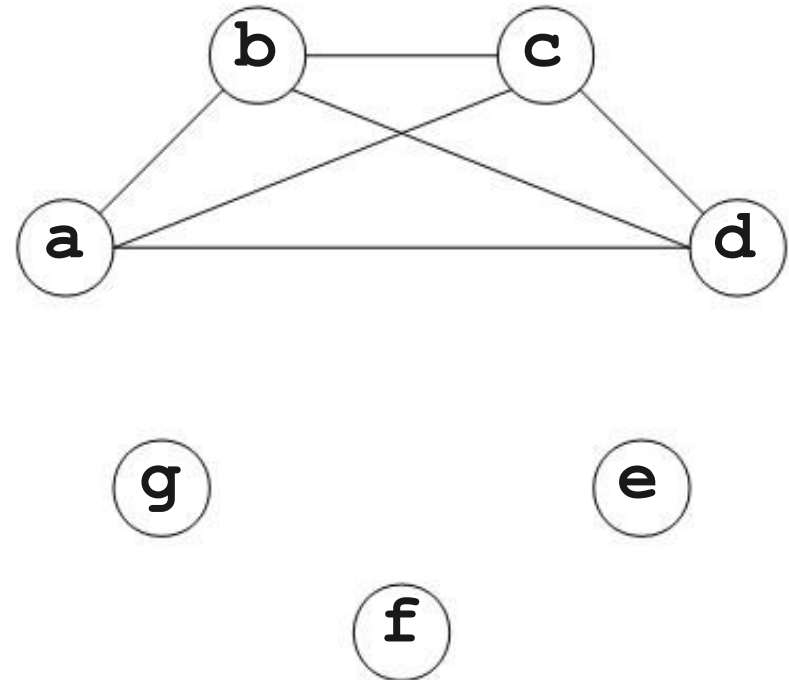
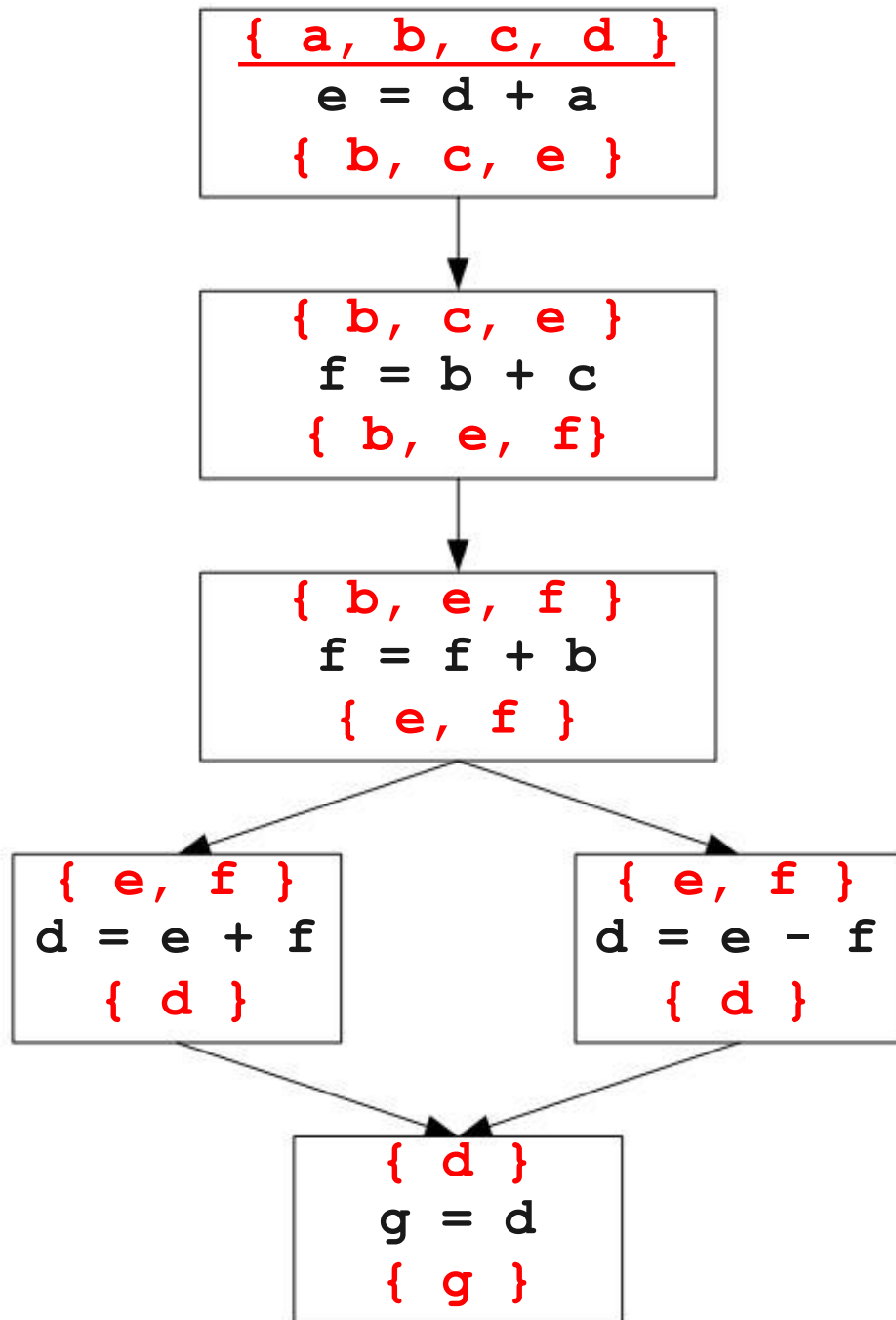


What can we infer from
all these variables being
live at each point?

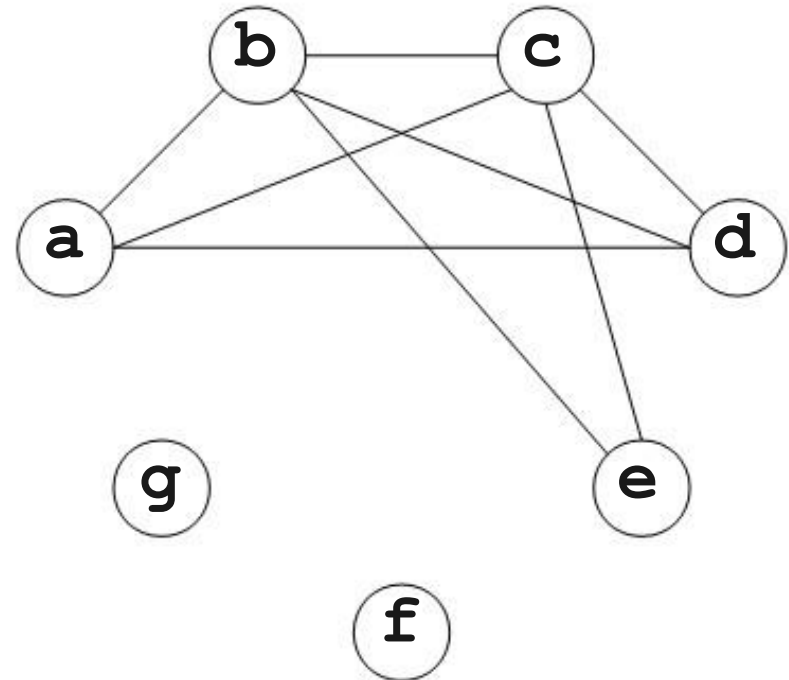
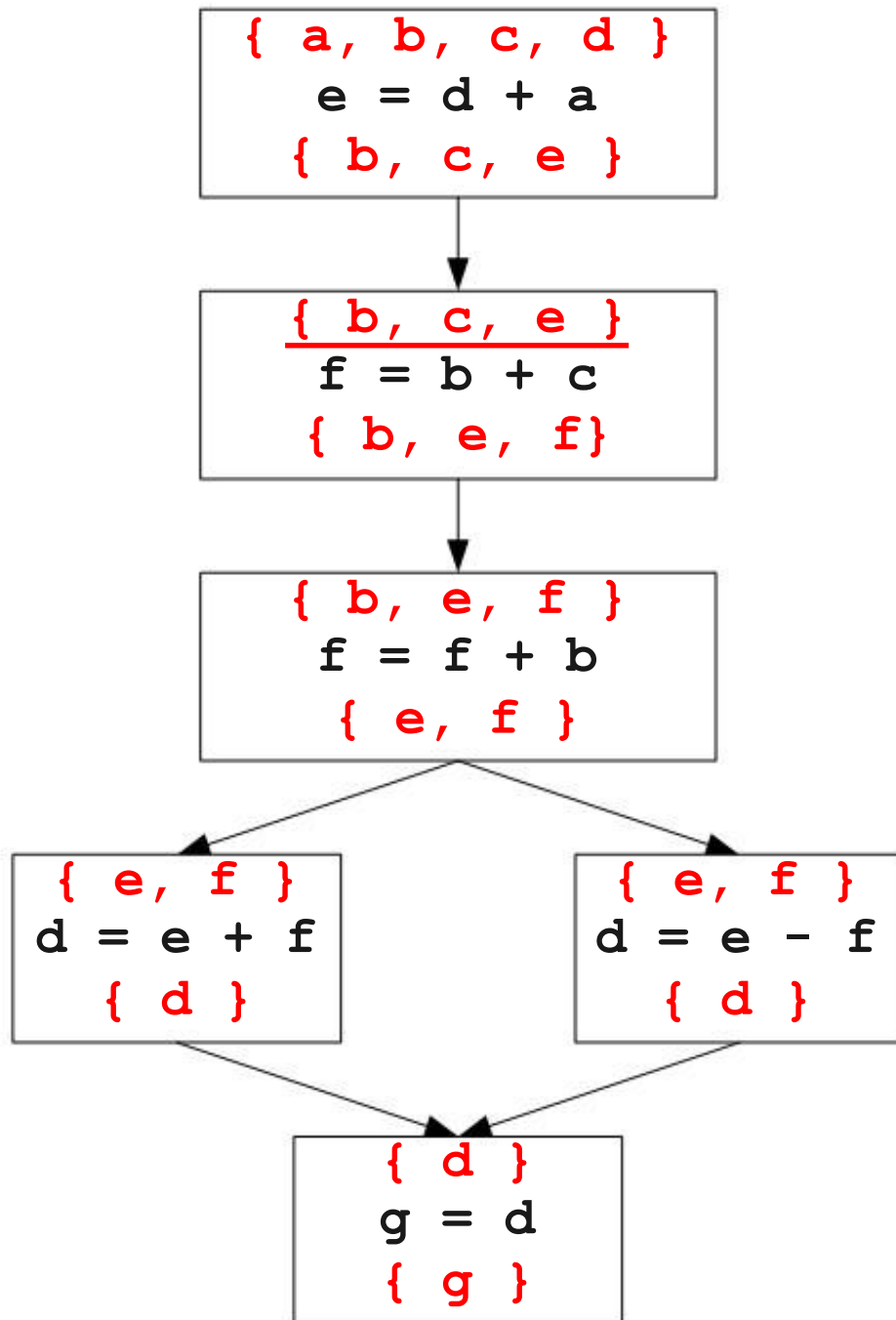
Smarter Approach



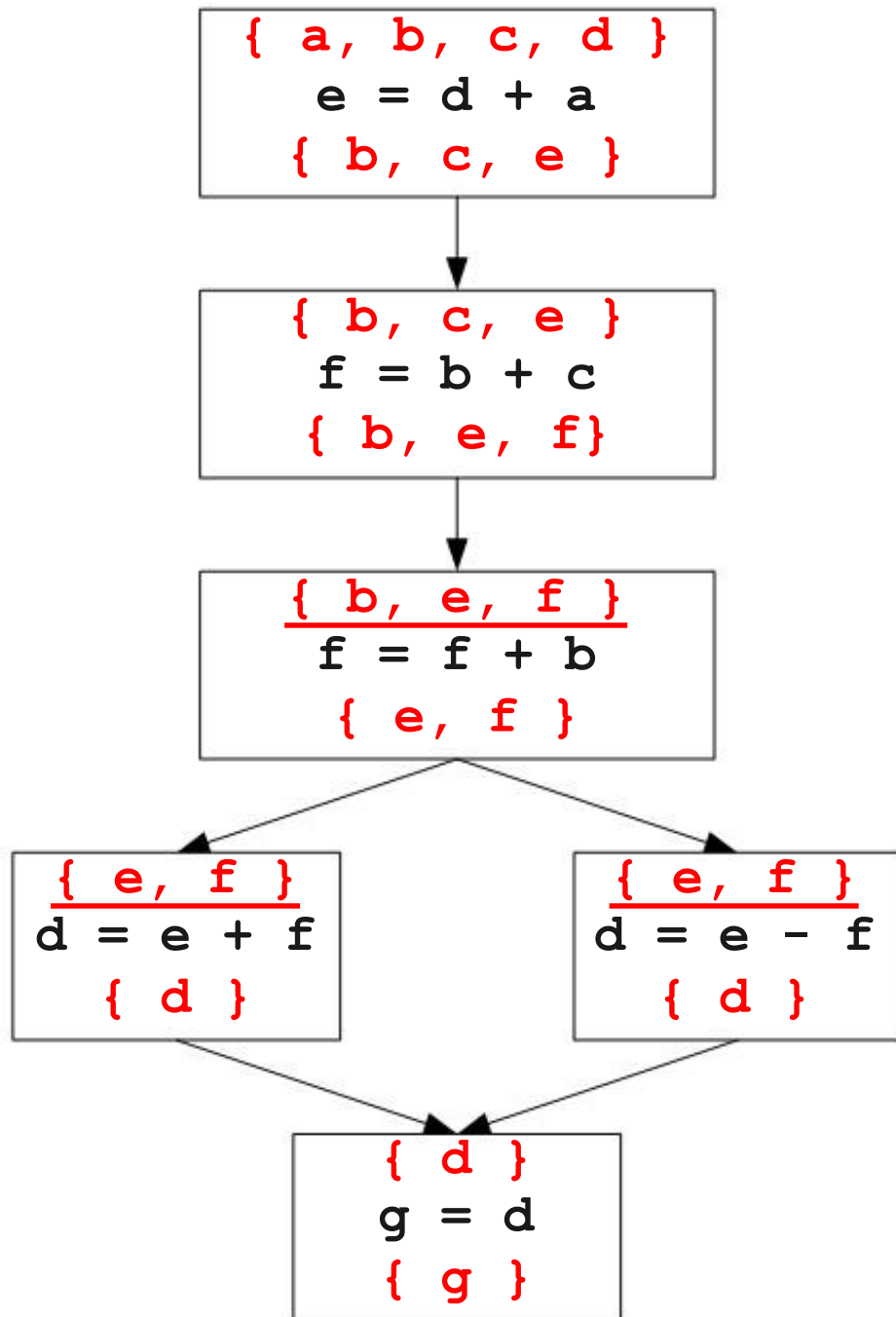
Smarter Approach



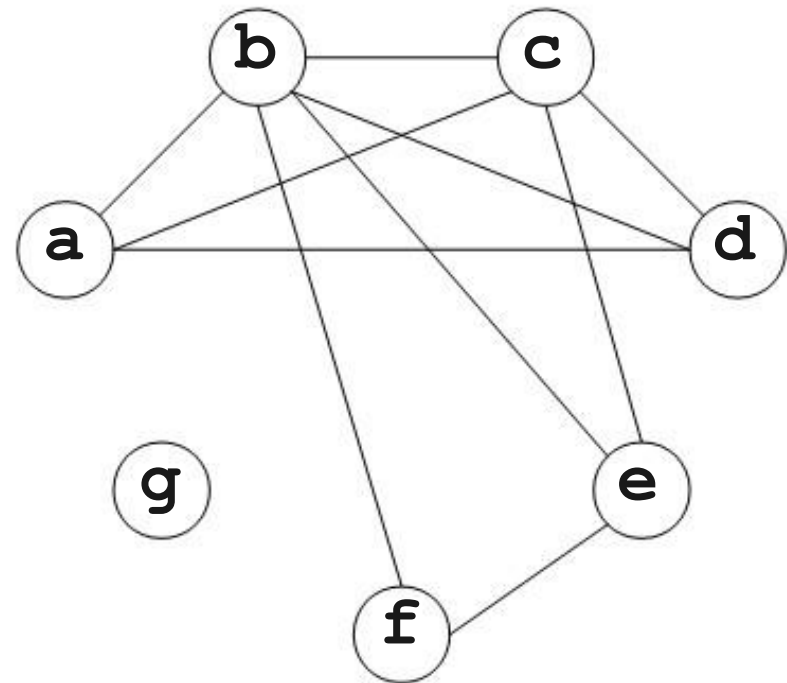
Smarter Approach



Smarter Approach

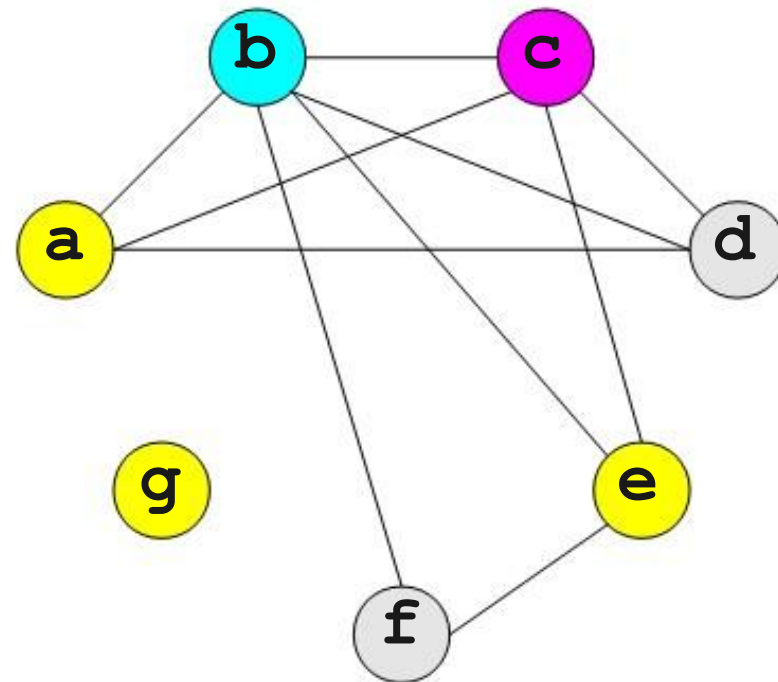
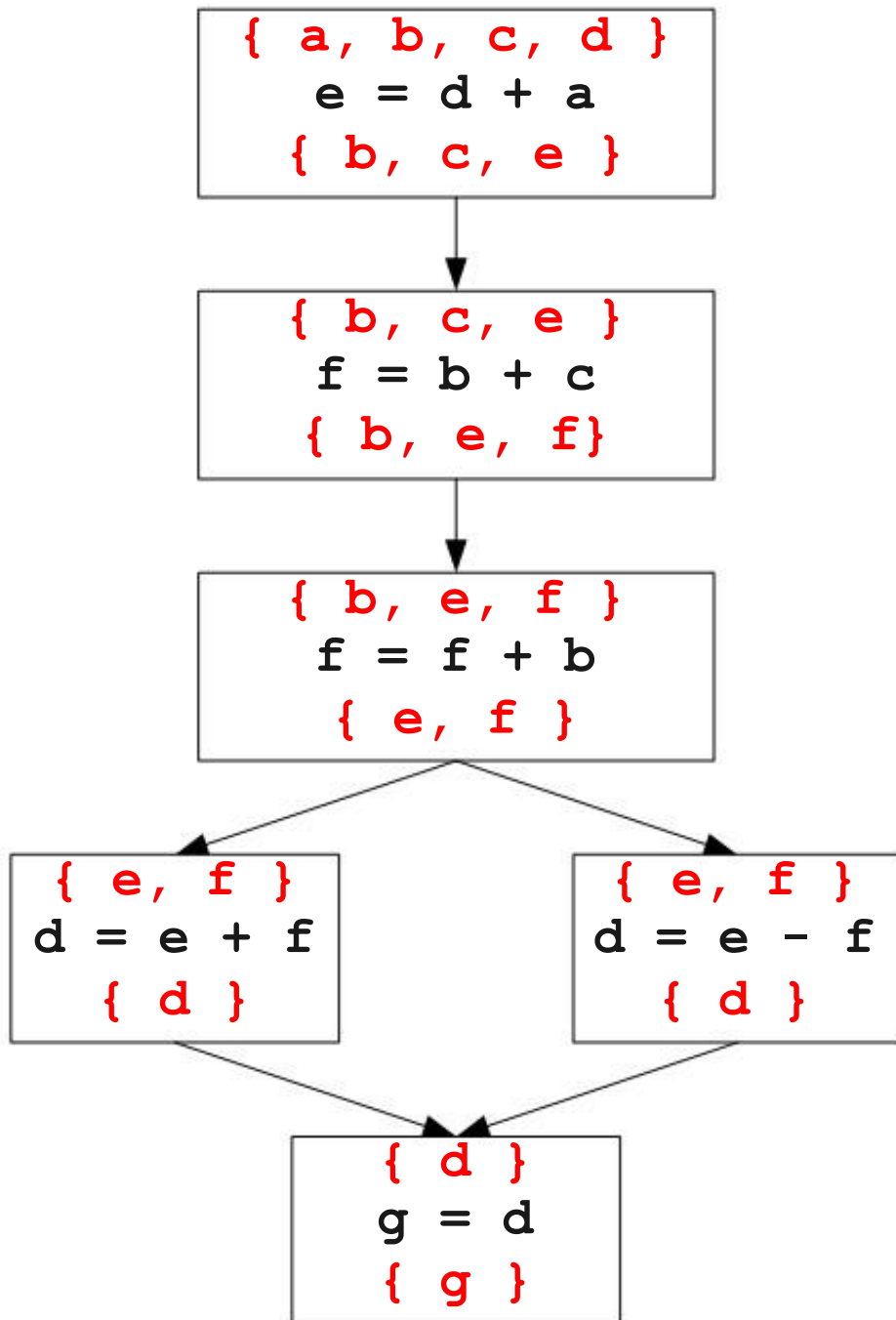


Register Interference Graph (RIG)



- Each node is a variable.
- An edge between two variables means they are live at the same program point.

Smarter Approach



Nodes which are adjacent cannot be assigned to the same register.

RIG & Graph-Coloring

- This problem is equivalent to **graph-coloring** (NP hard problem).
- No good polynomial-time algorithms are known for this problem.
- We have to use a heuristic* that is good enough in practice.

*A **heuristic** is a mental shortcut that allows people to solve problems and make judgments quickly and efficiently.

Chaitin's Algorithm

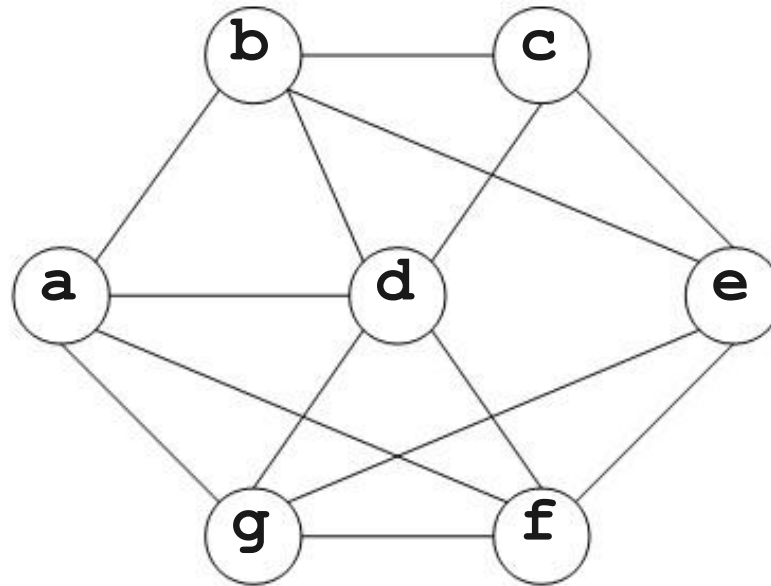
Intuition:

- Suppose we are trying to **k-color** a graph.
- Find a node with fewer than **k** edges.
- If we delete this node from the graph and color what remains, we can find a color for this node if we add it back in.

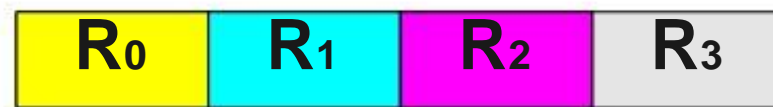
Algorithm:

- Find a node with fewer than k edges.
- Remove it from the graph.
- Recursively color the rest of the graph.
- Add the node back in.
- Assign it a valid color.

Chaitin's Algorithm

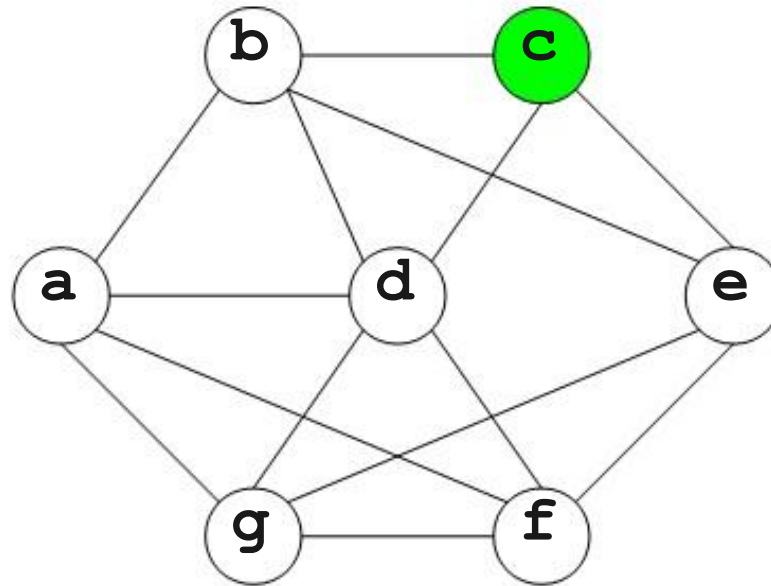


Registers

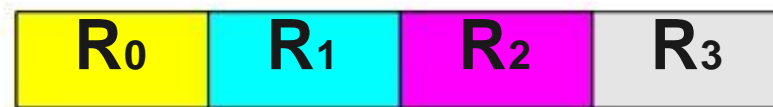


4-color

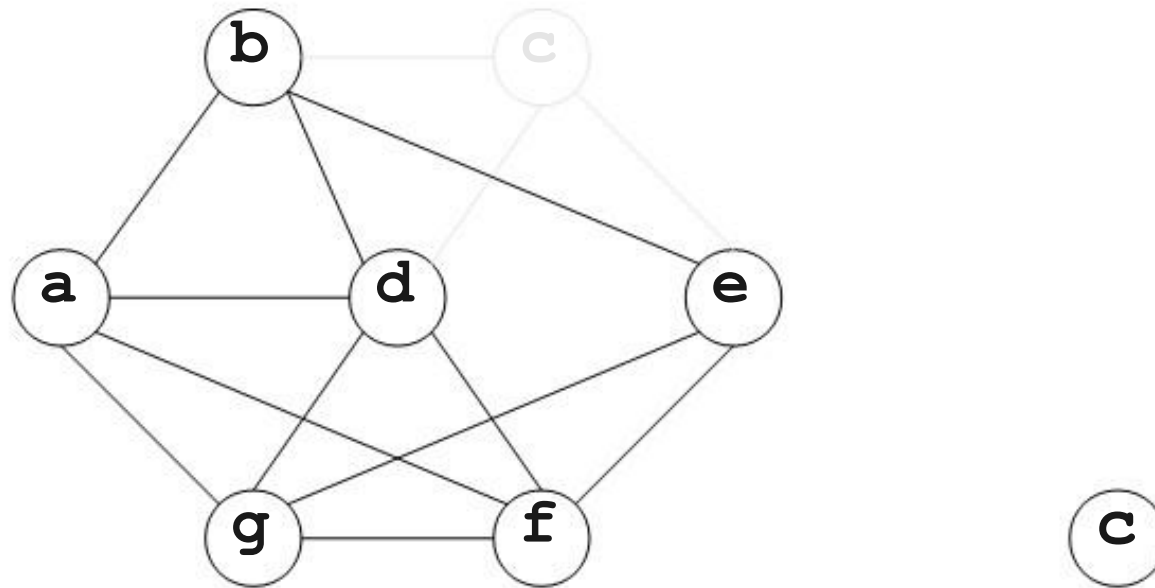
Chaitin's Algorithm



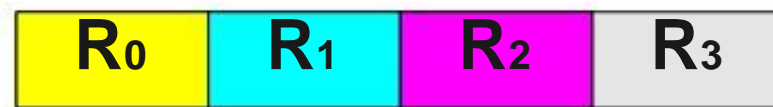
Registers



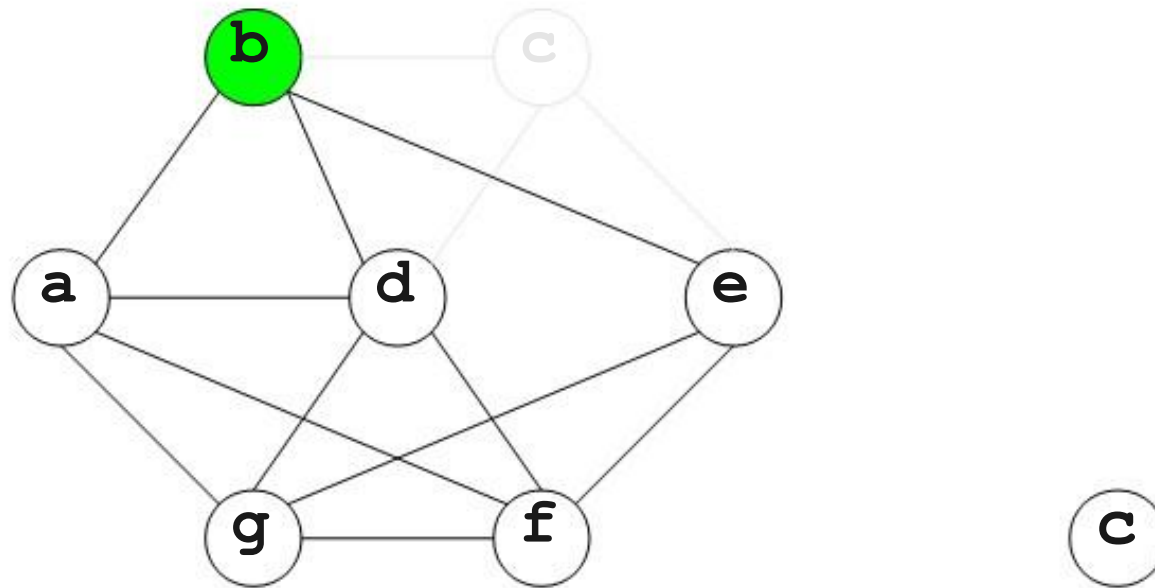
Chaitin's Algorithm



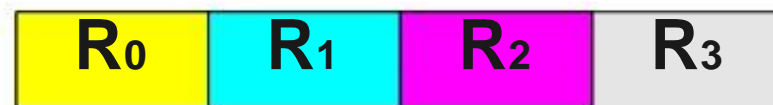
Registers



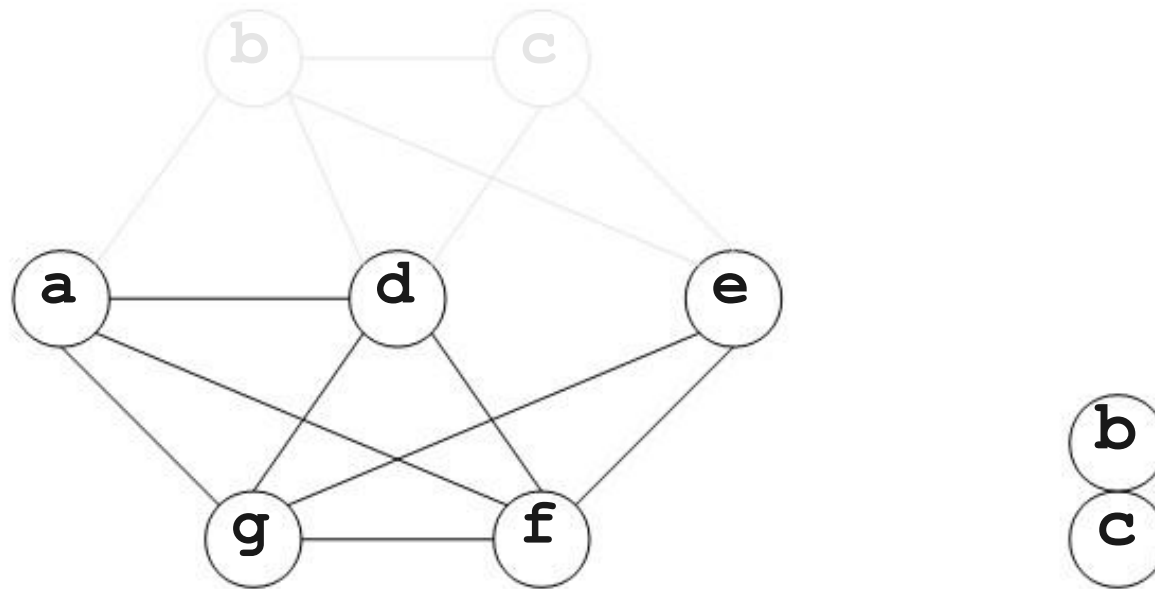
Chaitin's Algorithm



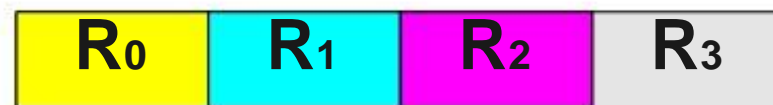
Registers



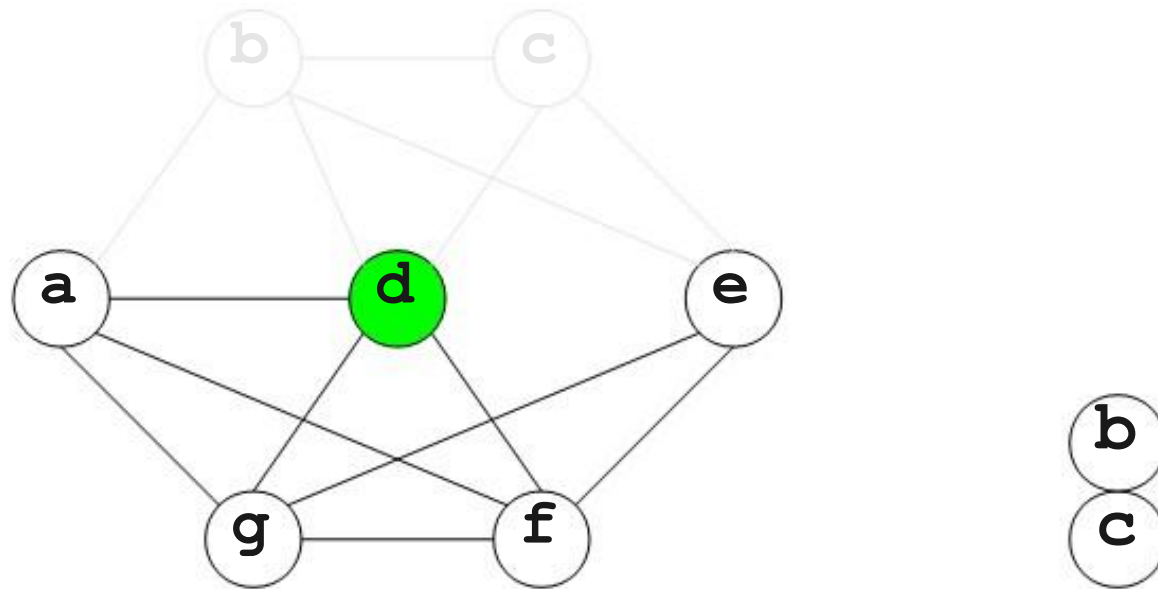
Chaitin's Algorithm



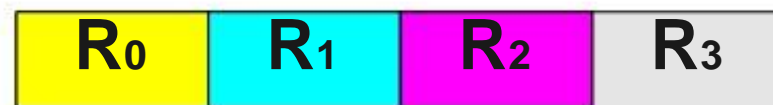
Registers



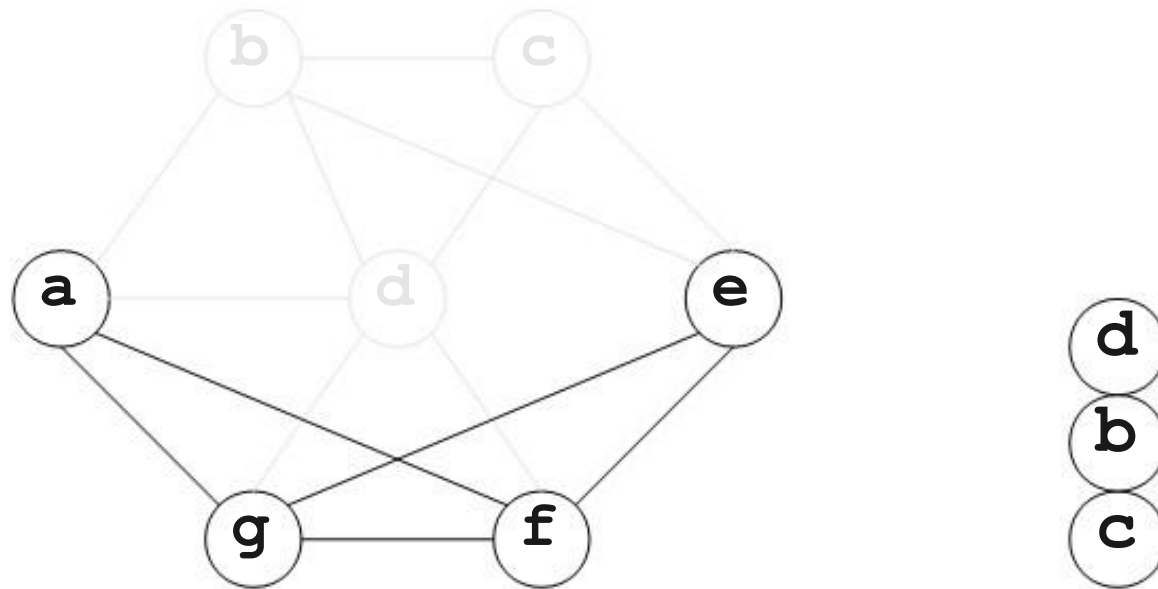
Chaitin's Algorithm



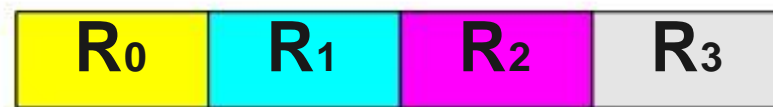
Registers



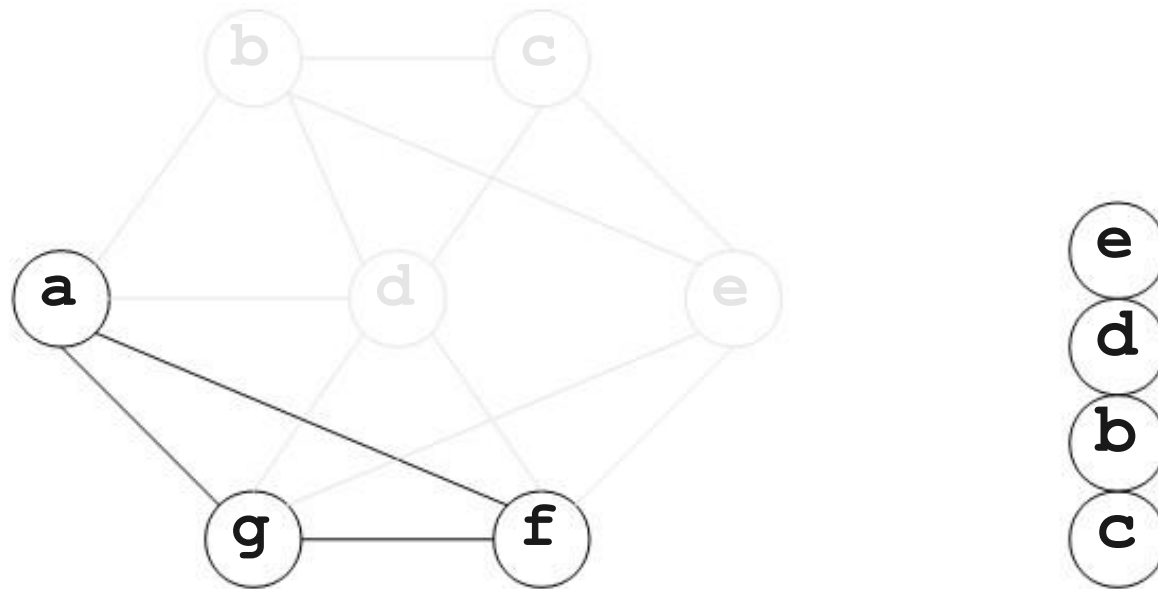
Chaitin's Algorithm



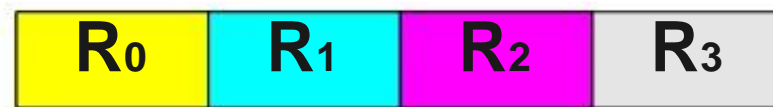
Registers



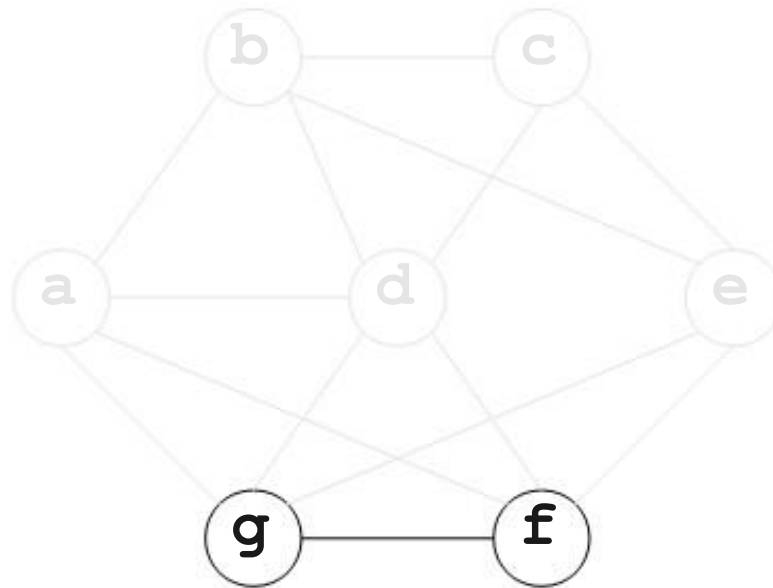
Chaitin's Algorithm



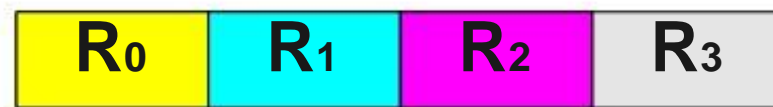
Registers



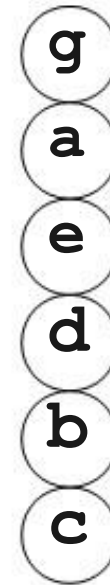
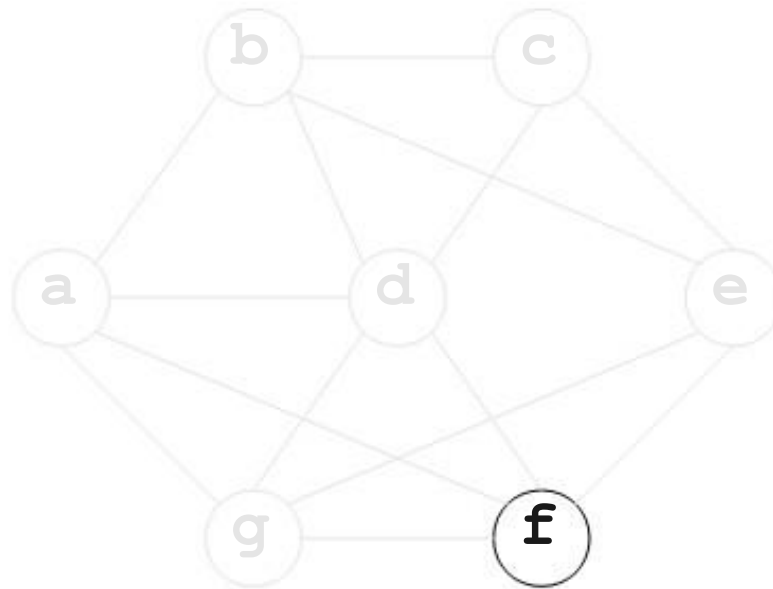
Chaitin's Algorithm



Registers



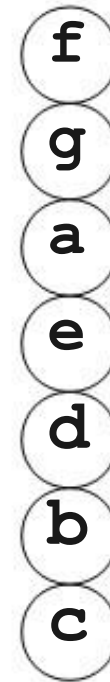
Chaitin's Algorithm



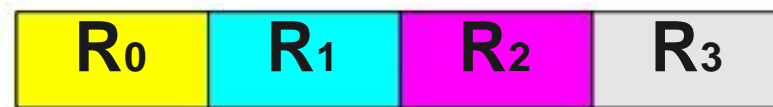
Registers



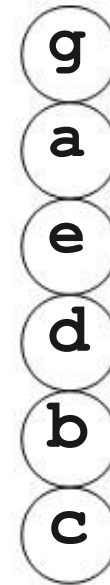
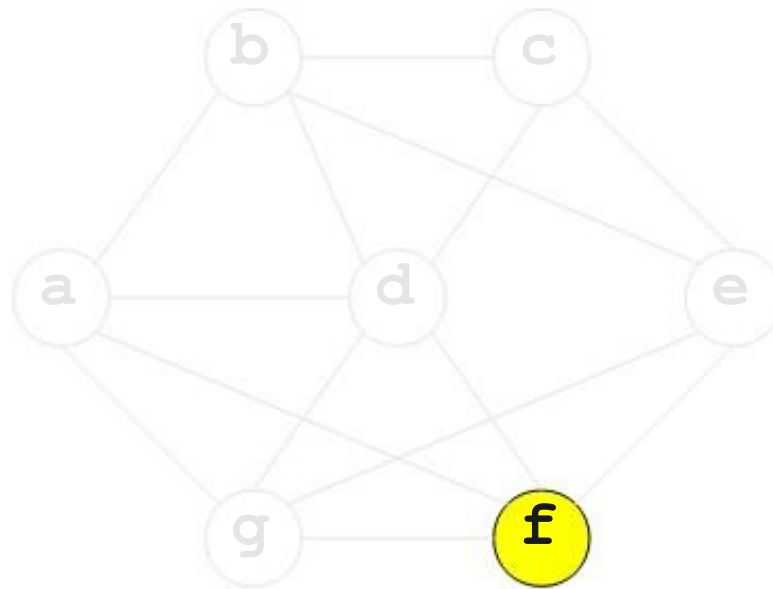
Chaitin's Algorithm



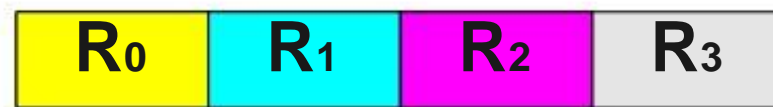
Registers



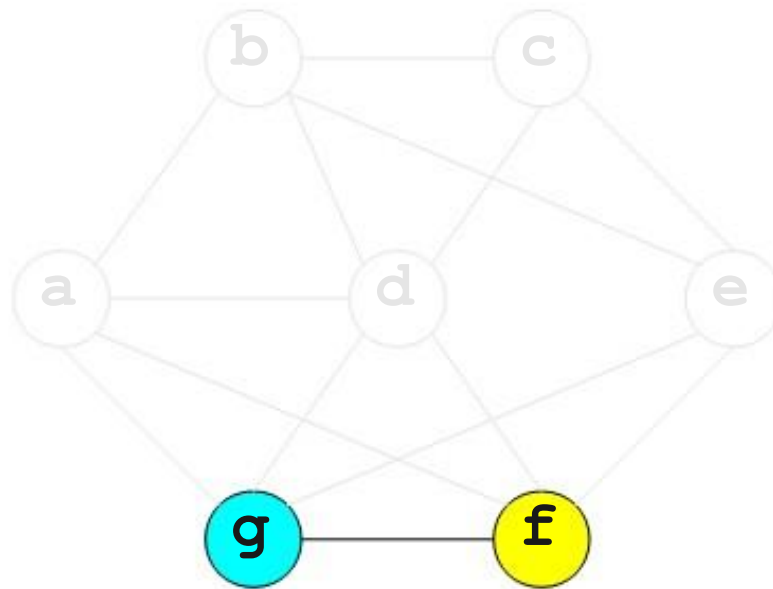
Chaitin's Algorithm



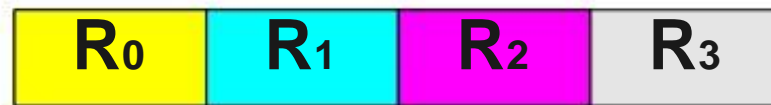
Registers



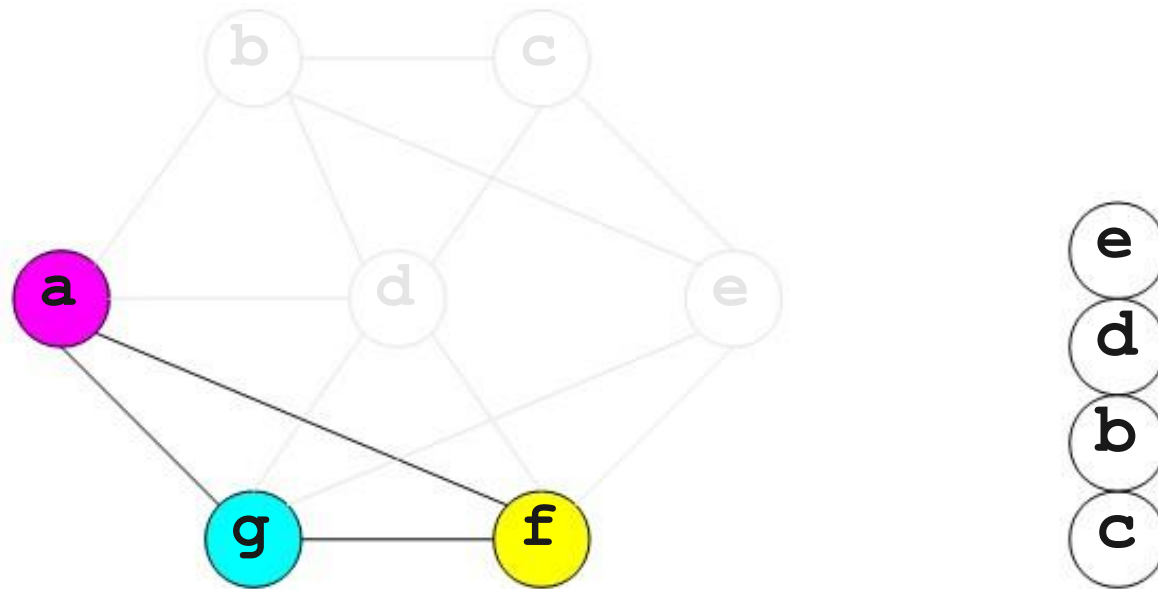
Chaitin's Algorithm



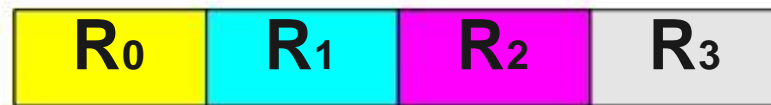
Registers



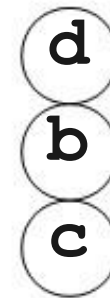
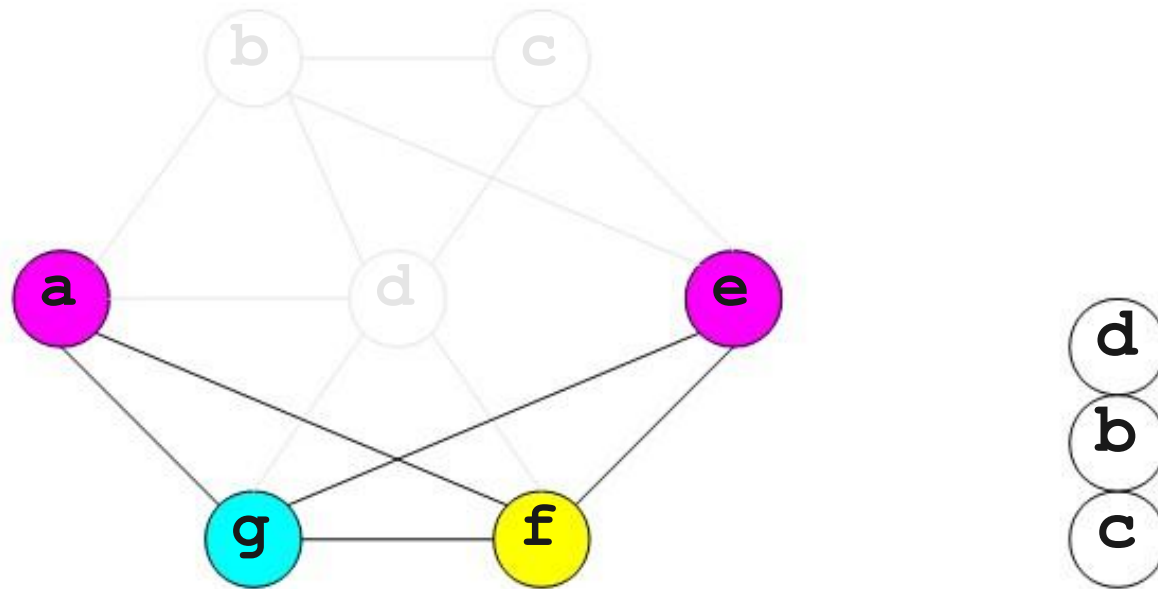
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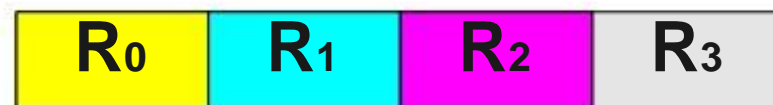
Registers



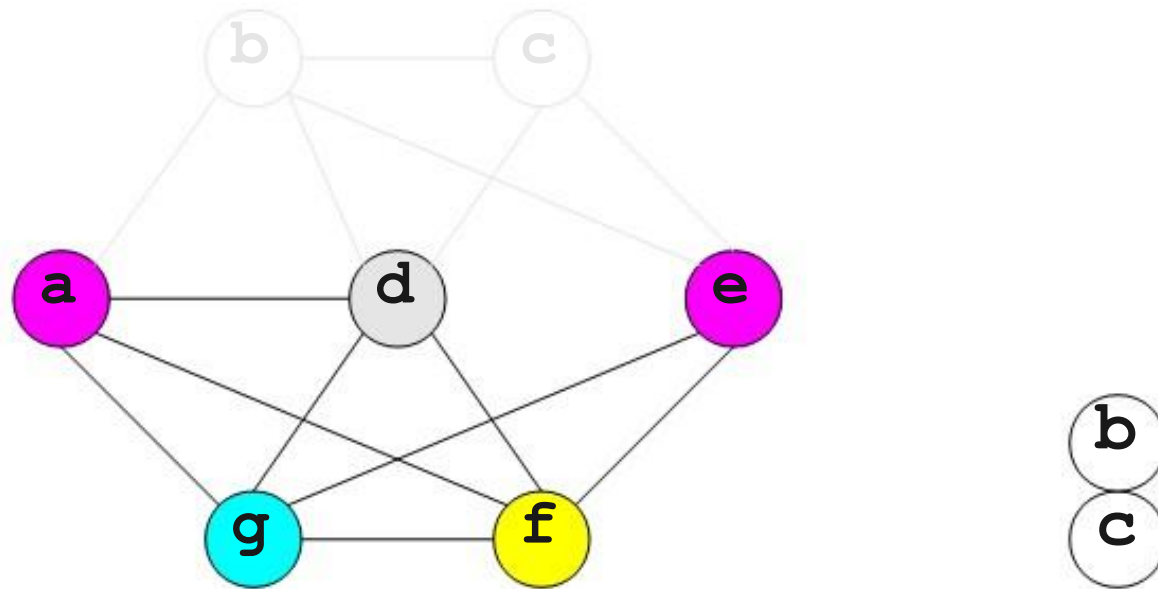
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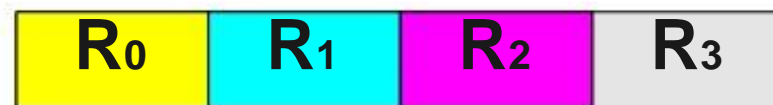
Registers



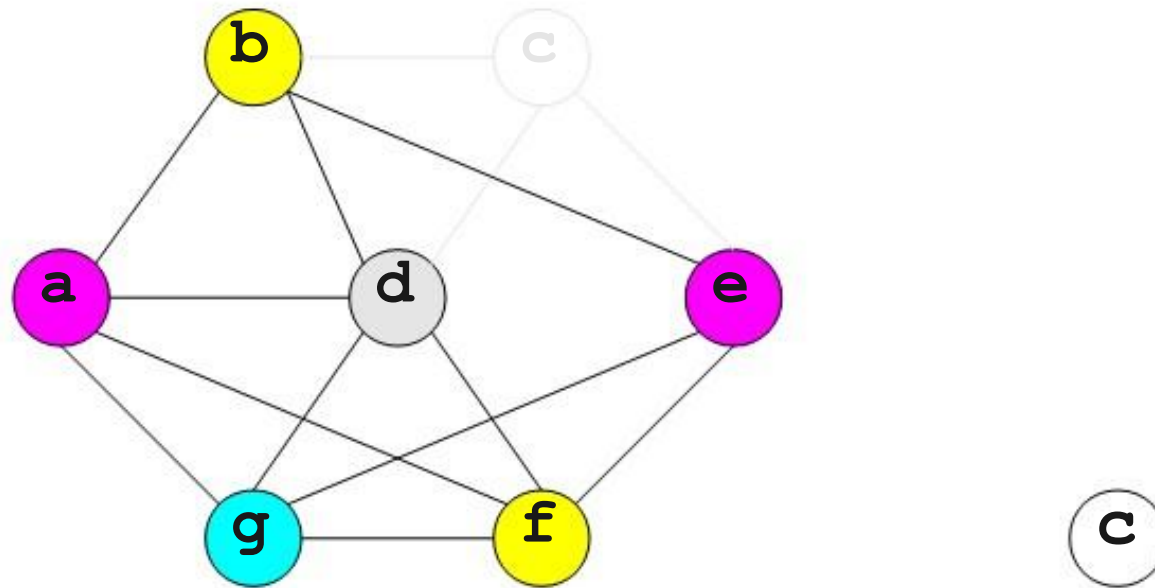
Chaitin's Algorithm



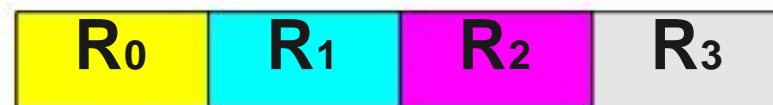
Registers



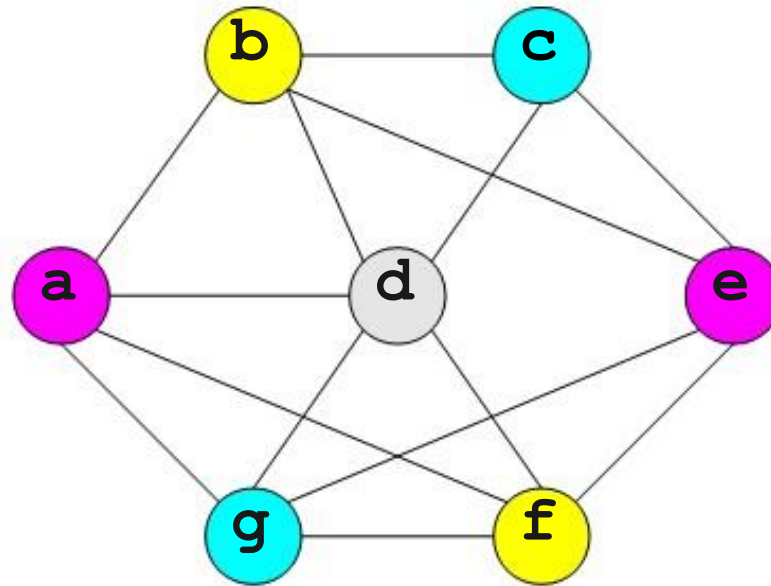
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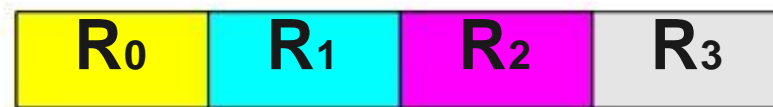
Registers



Chaitin's Algorithm



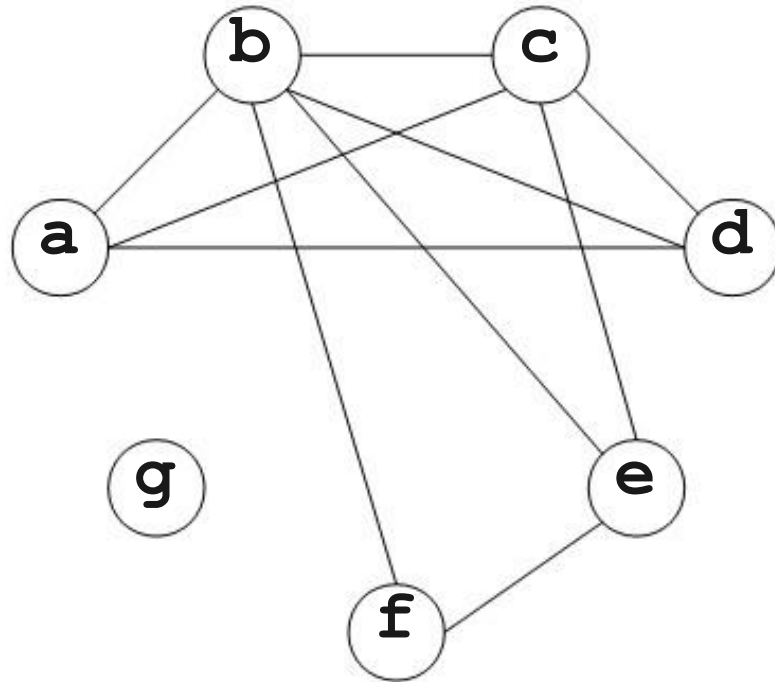
Registers



One Problem

- What if we can't find a node with $< k$ neighbors?
- Choose and remove an arbitrary node
- When adding node back in, it may be possible to find a valid color.
- Otherwise, we have to spill that node.

Chaitin's Algorithm Reloaded

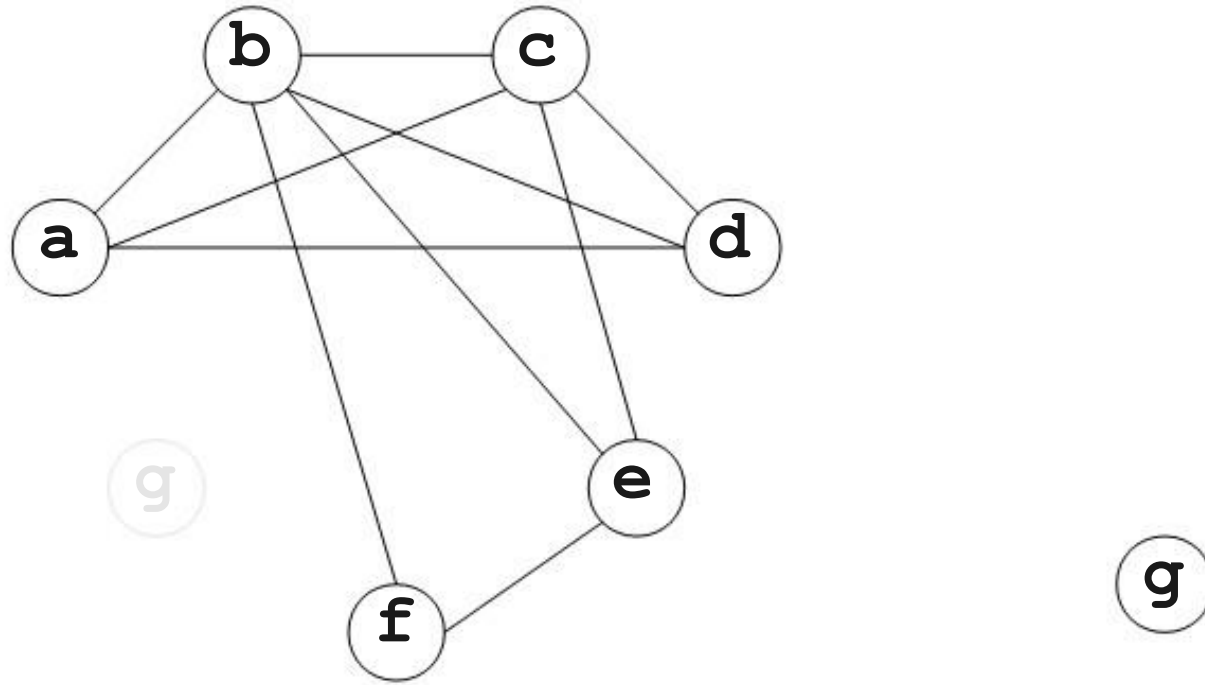


Registers



3-color

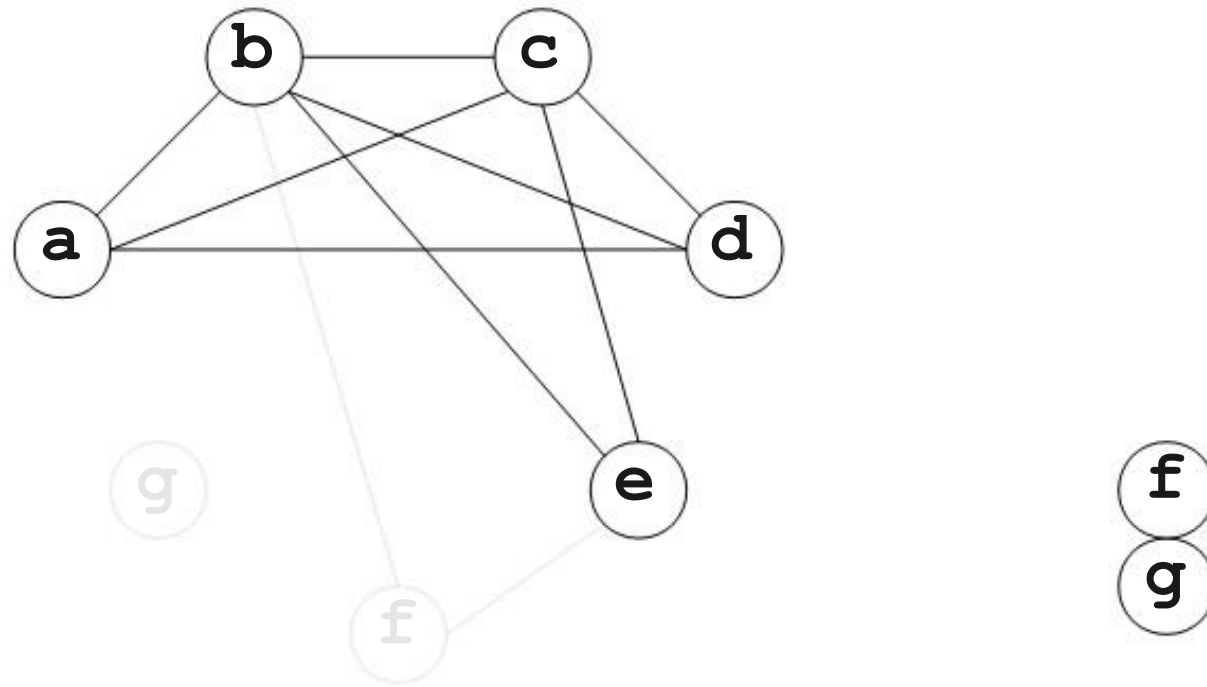
Chaitin's Algorithm Reloaded



Registers



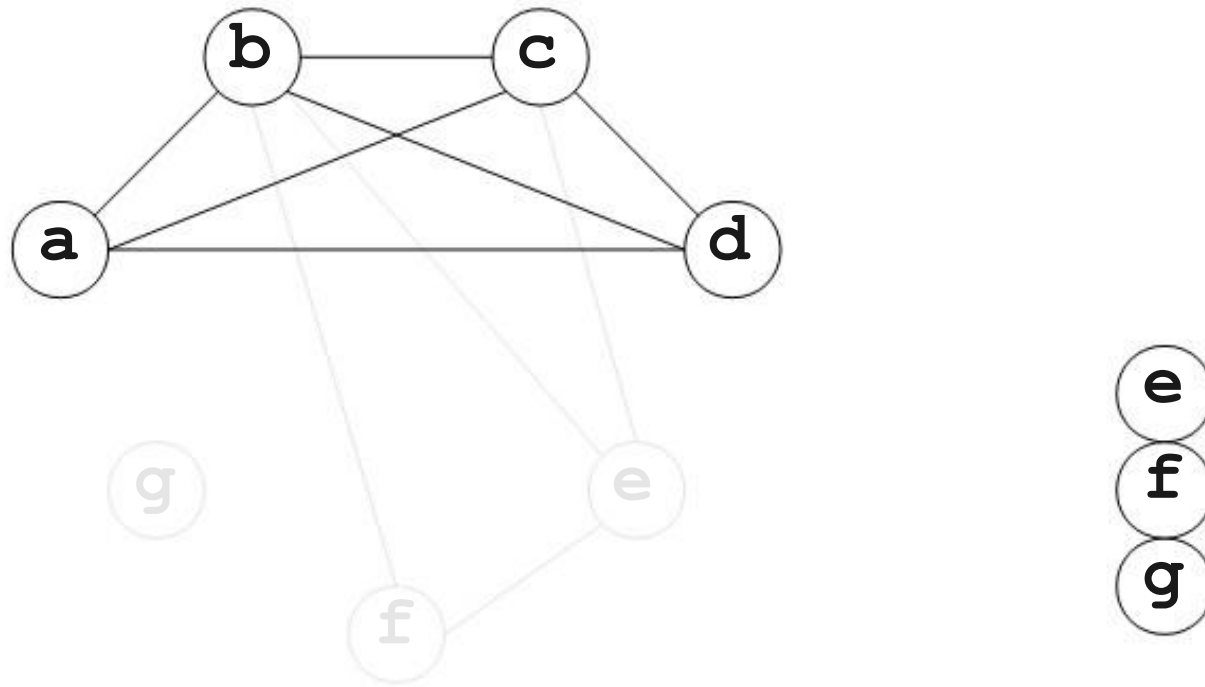
Chaitin's Algorithm Reloaded



Registers



Chaitin's Algorithm Reloaded

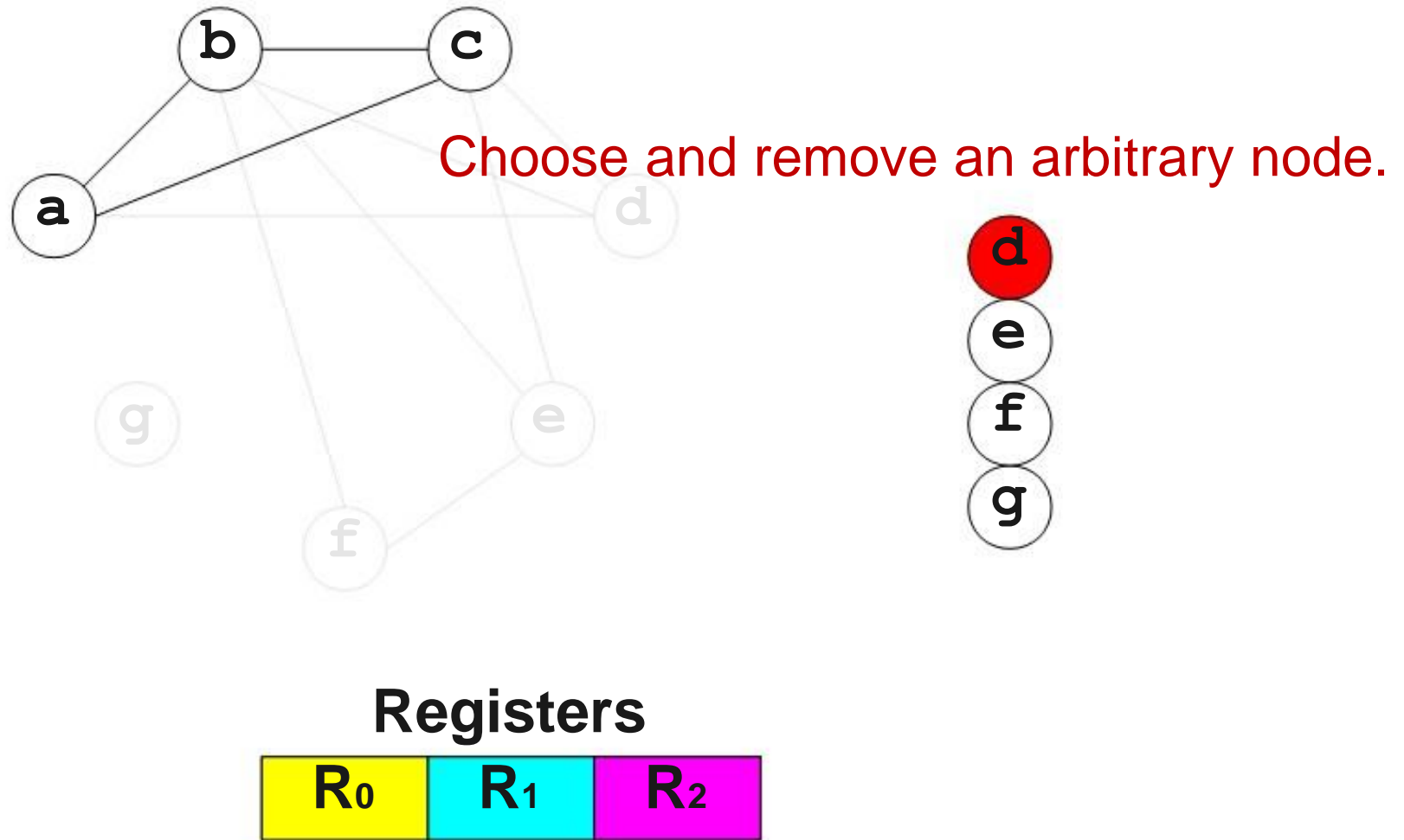


Registers

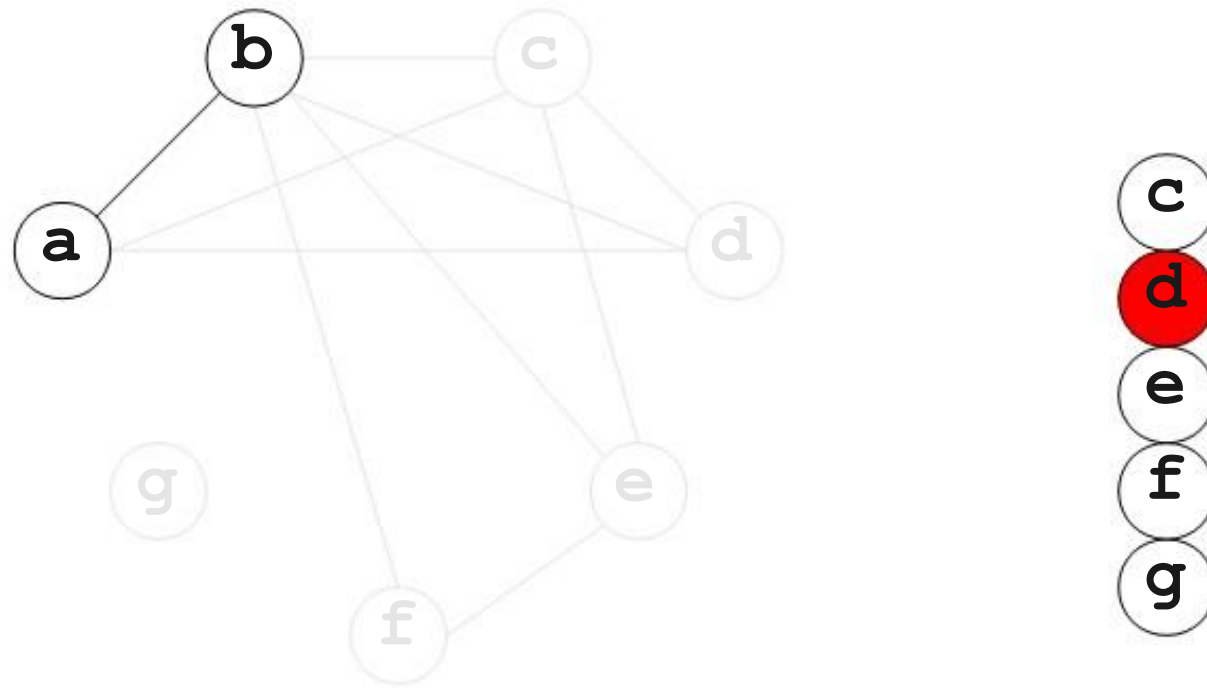


3-color

Chaitin's Algorithm Reloaded



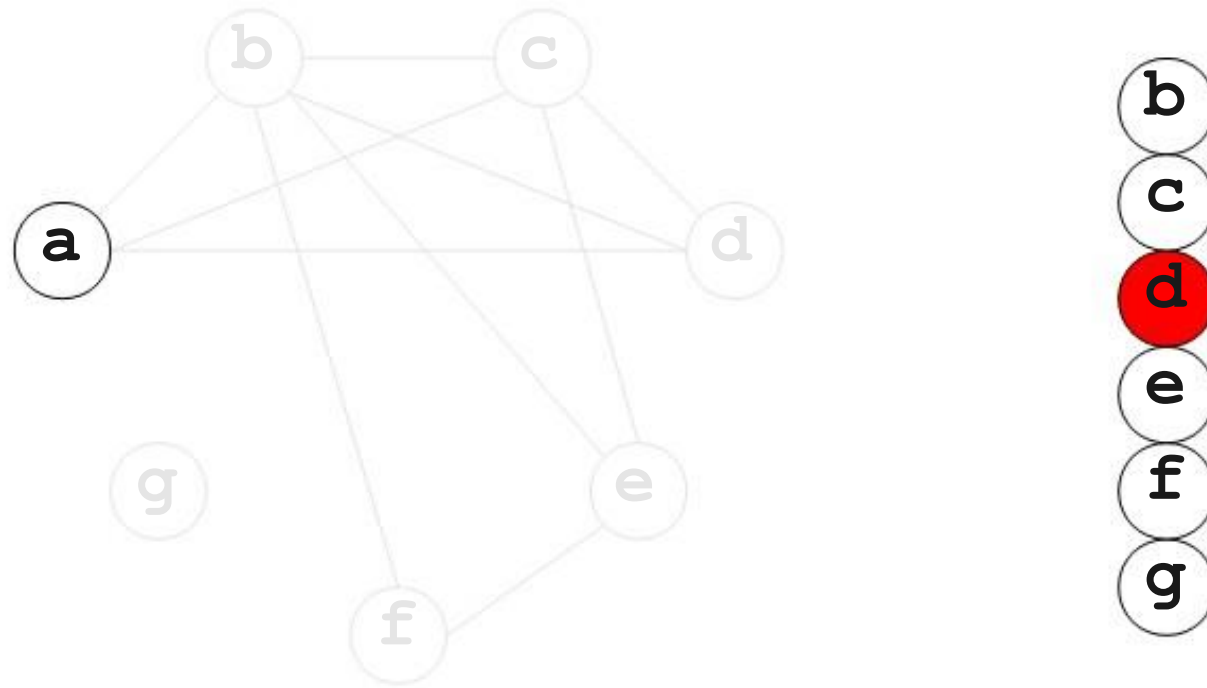
Chaitin's Algorithm Reloaded



Registers



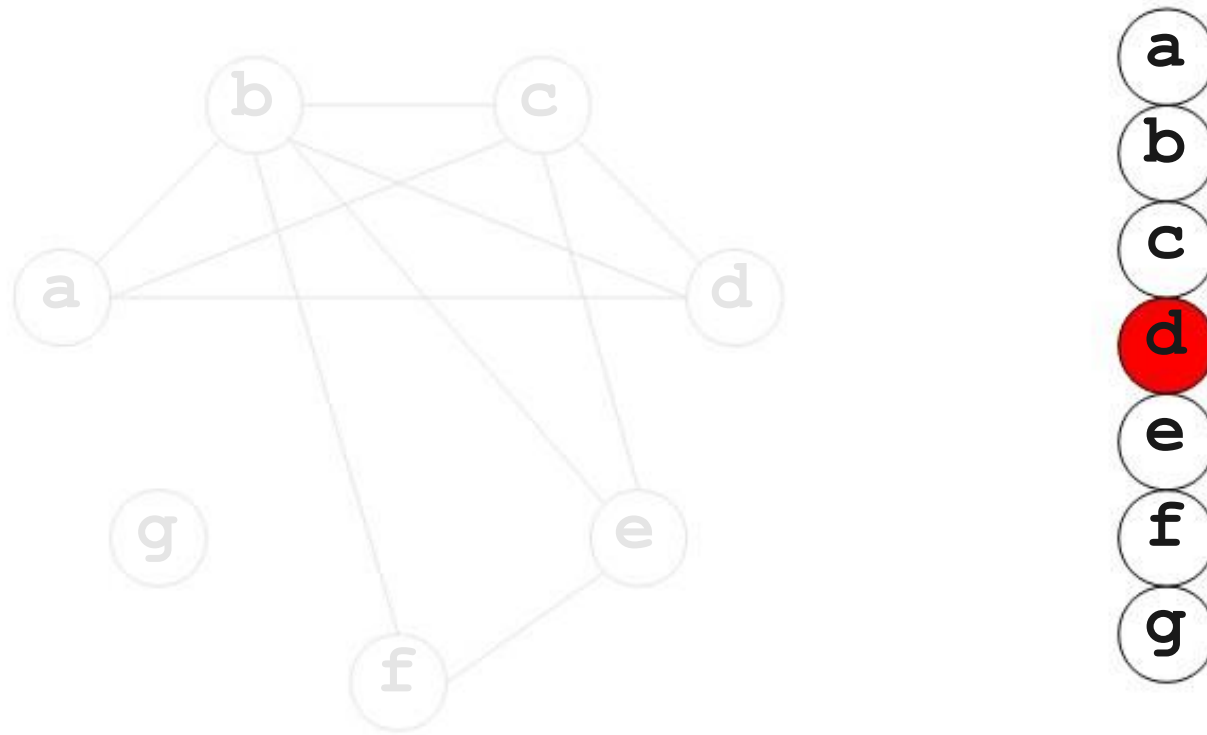
Chaitin's Algorithm Reloaded



Registers



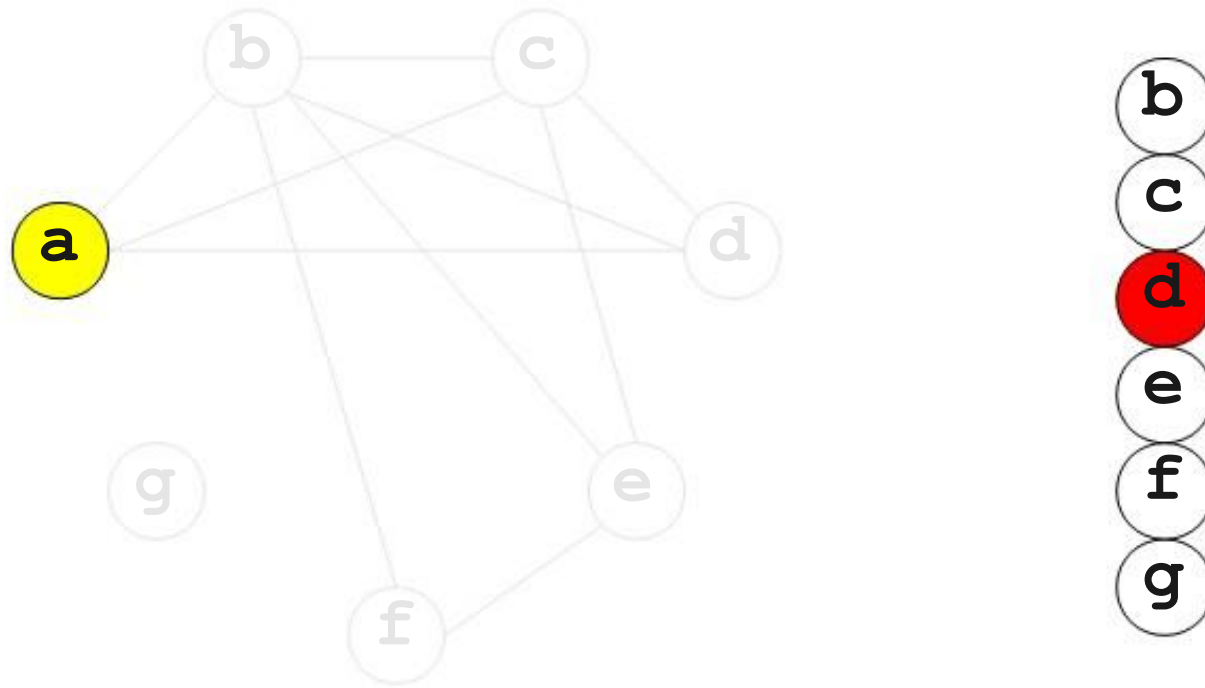
Chaitin's Algorithm Reloaded



Registers



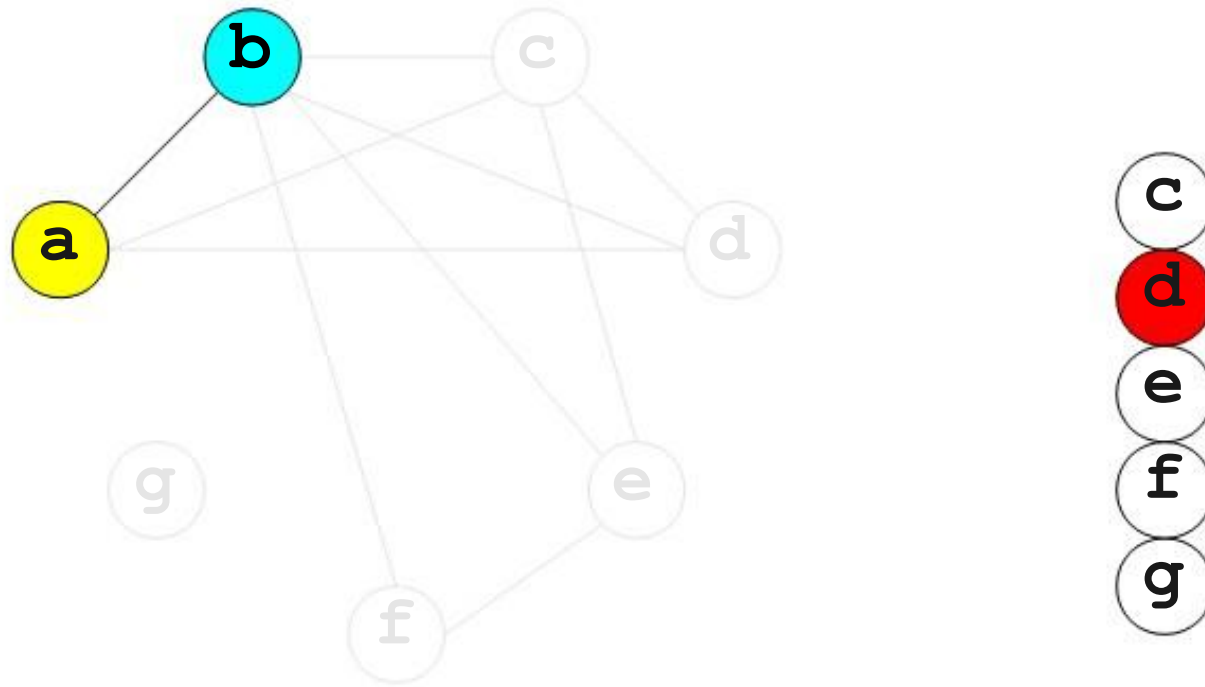
Chaitin's Algorithm Reloaded



Registers



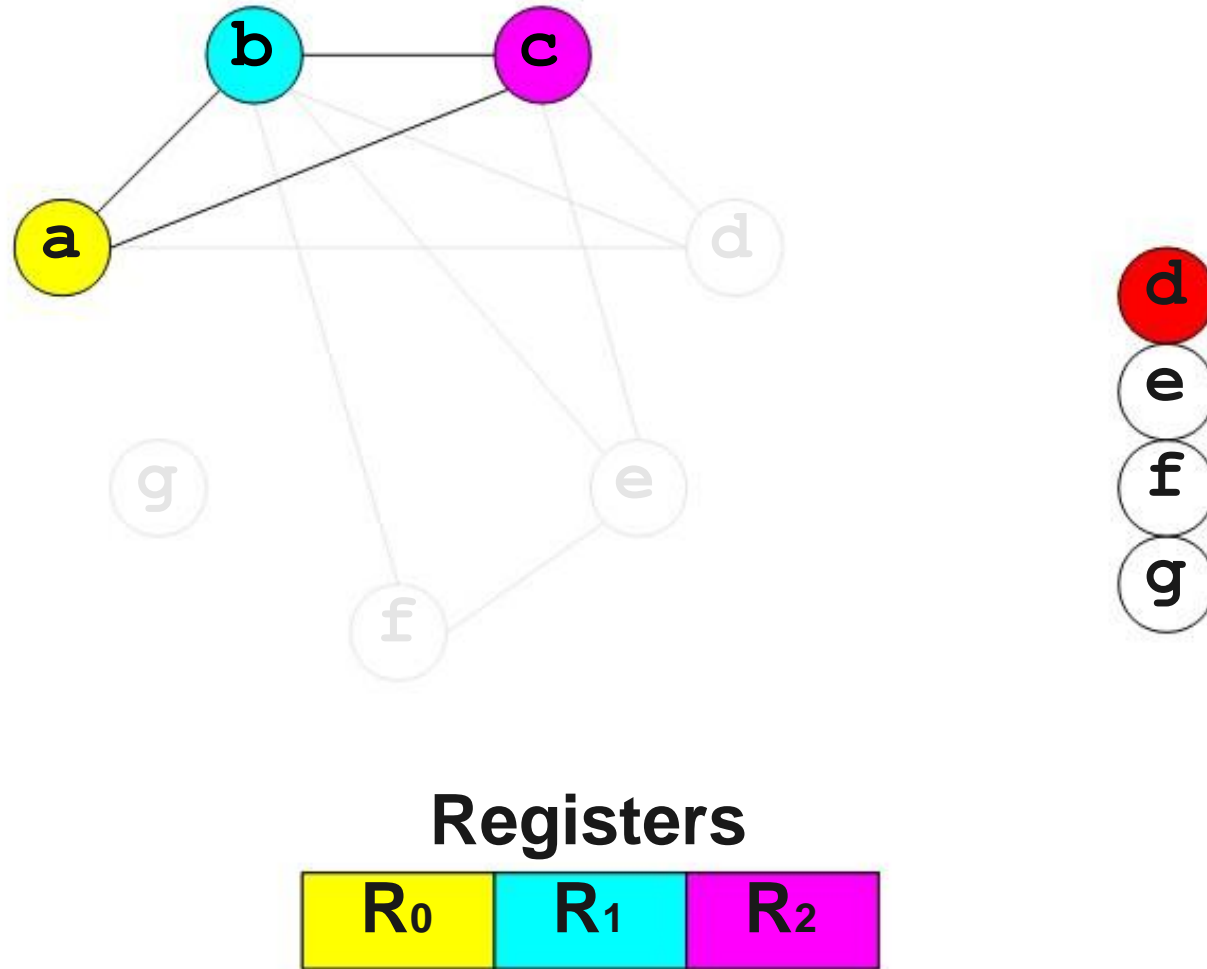
Chaitin's Algorithm Reloaded



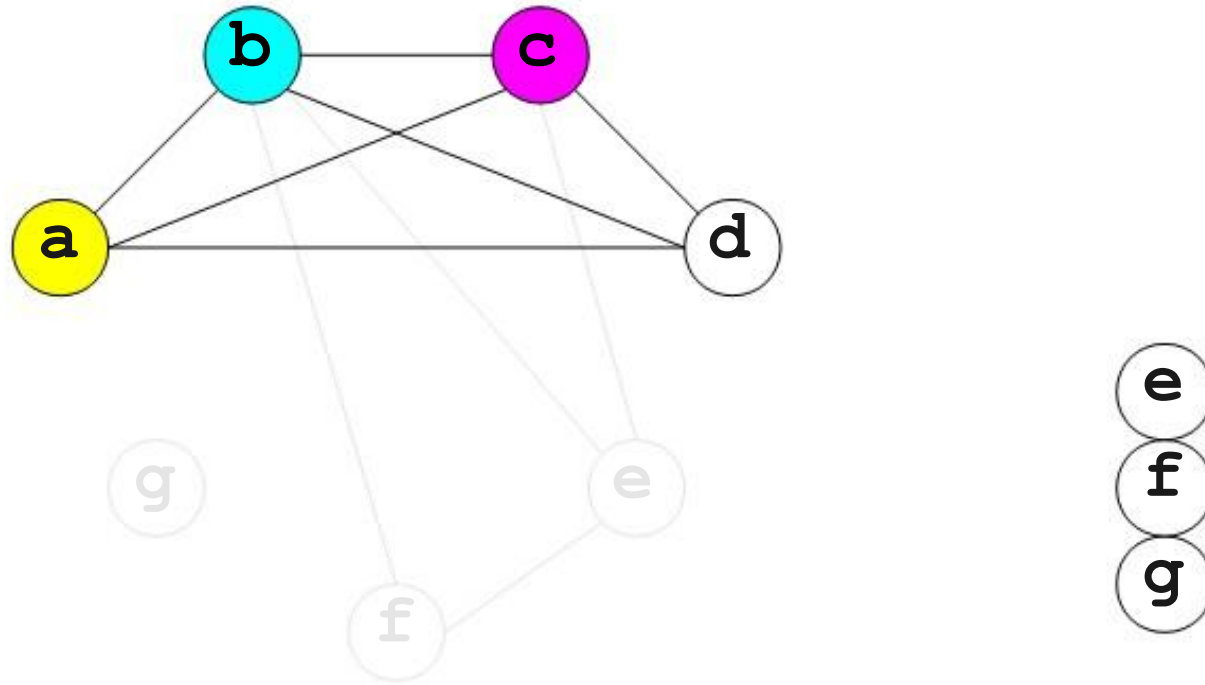
Registers



Chaitin's Algorithm Reloaded



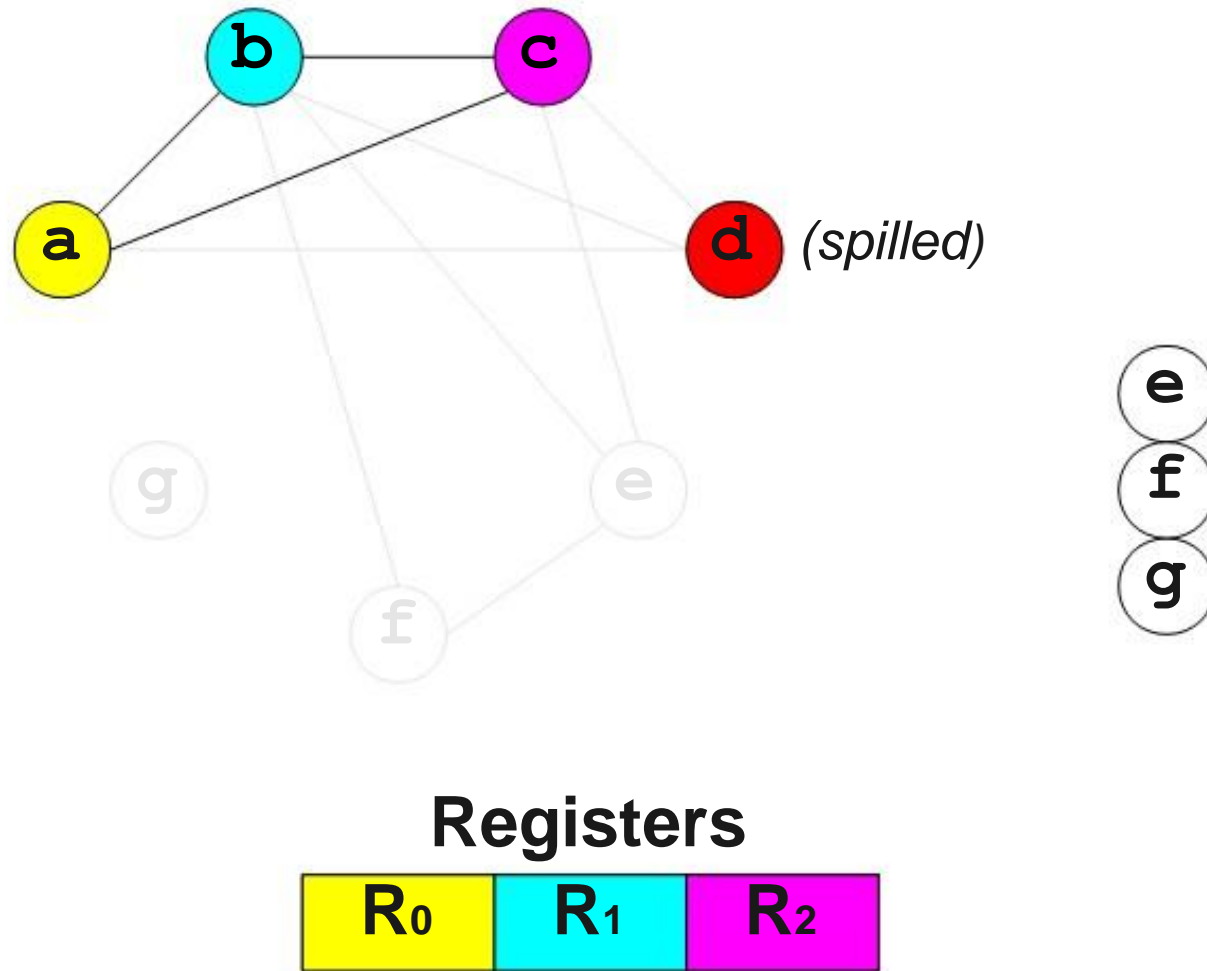
Chaitin's Algorithm Reloaded



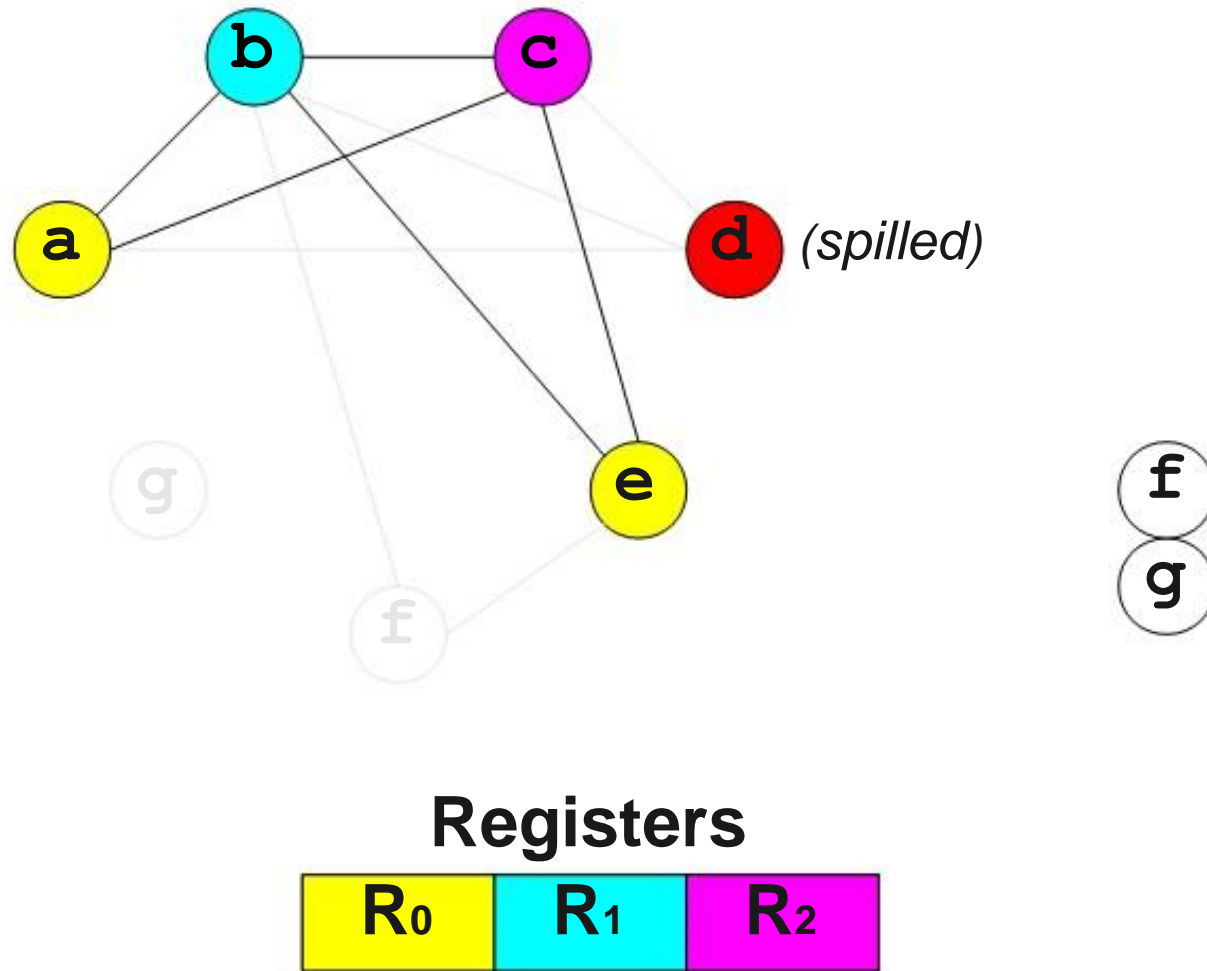
Registers



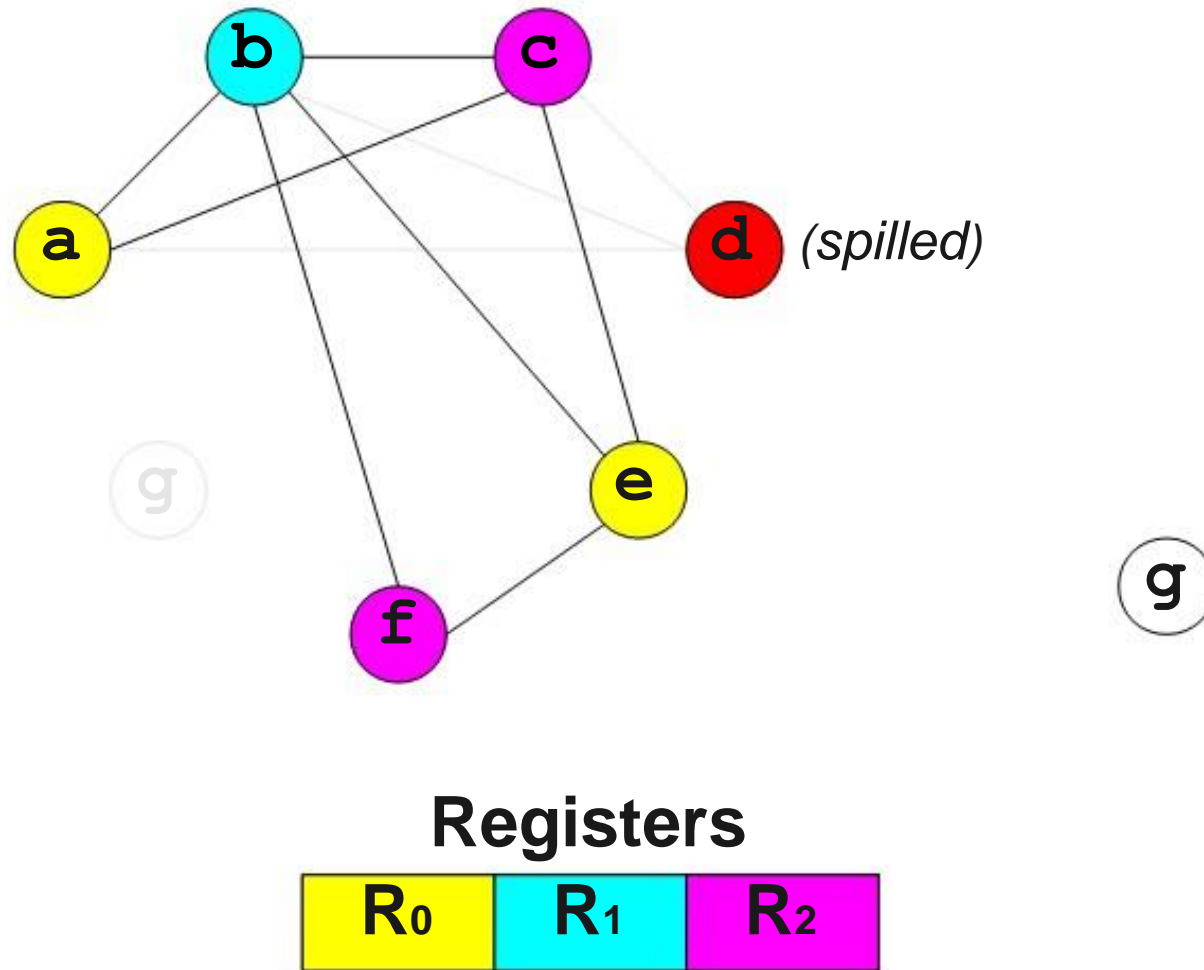
Chaitin's Algorithm Reloaded



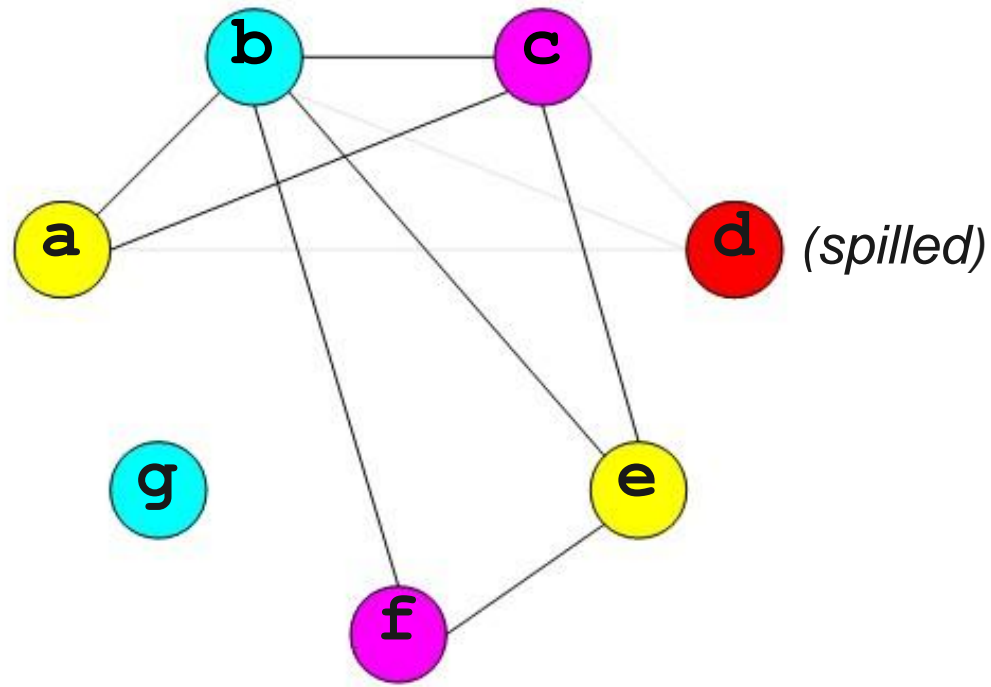
Chaitin's Algorithm Reloaded



Chaitin's Algorithm Reloaded



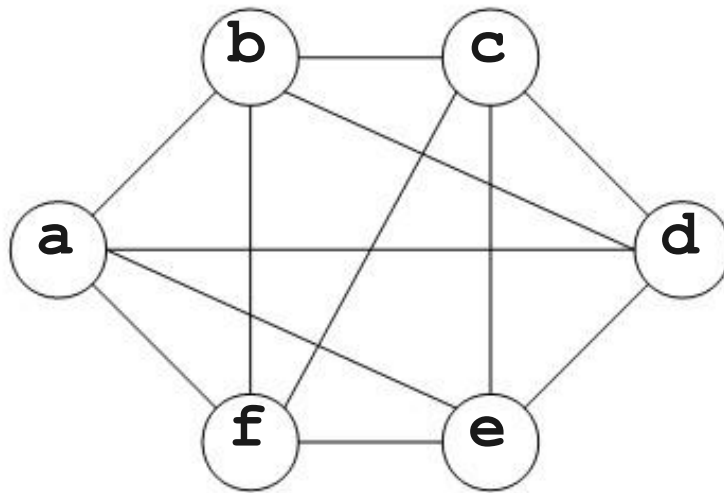
Chaitin's Algorithm Reloaded



Registers



Another Example

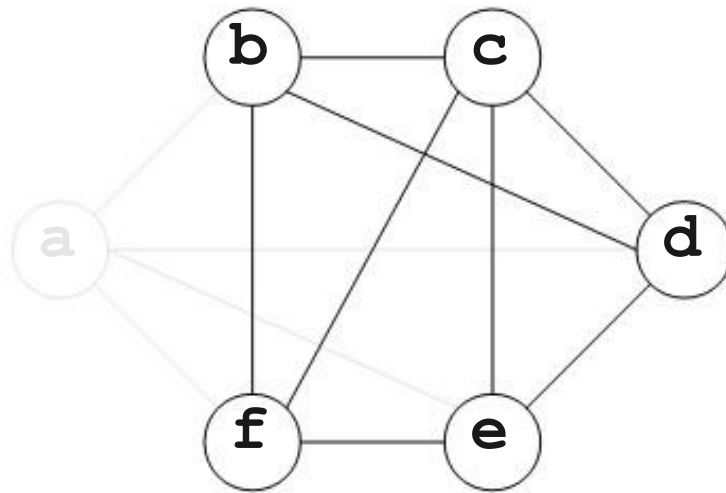


Registers



3-color

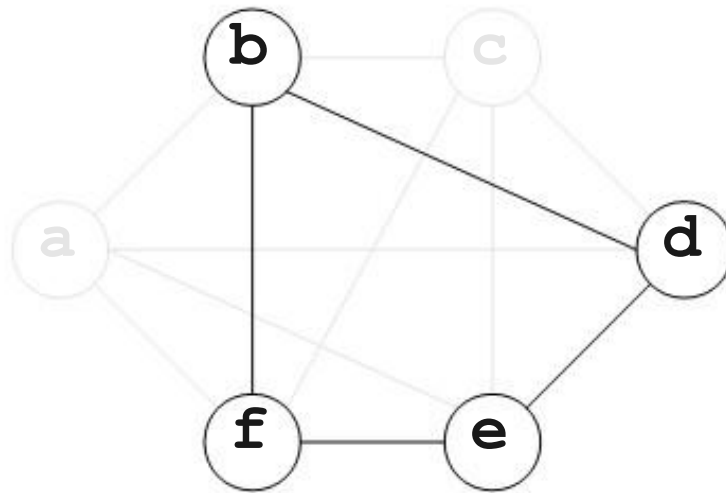
Another Example



Registers



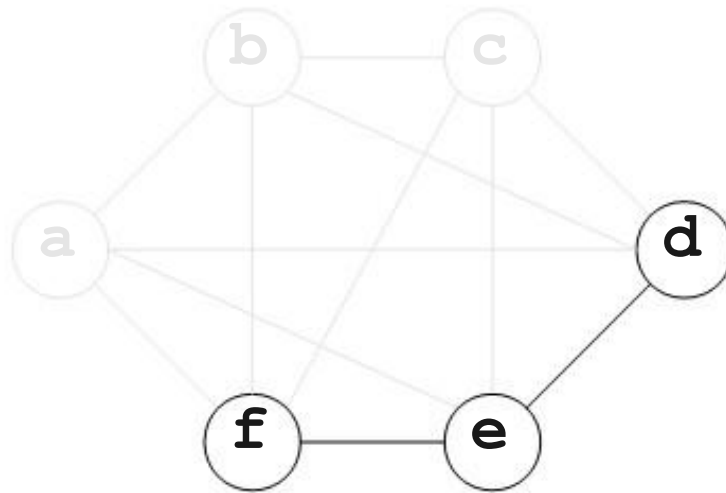
Another Example



Registers



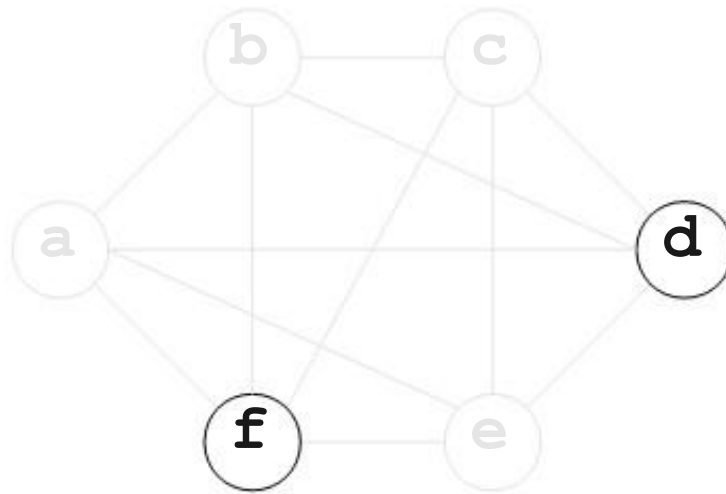
Another Example



Registers



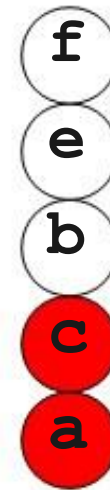
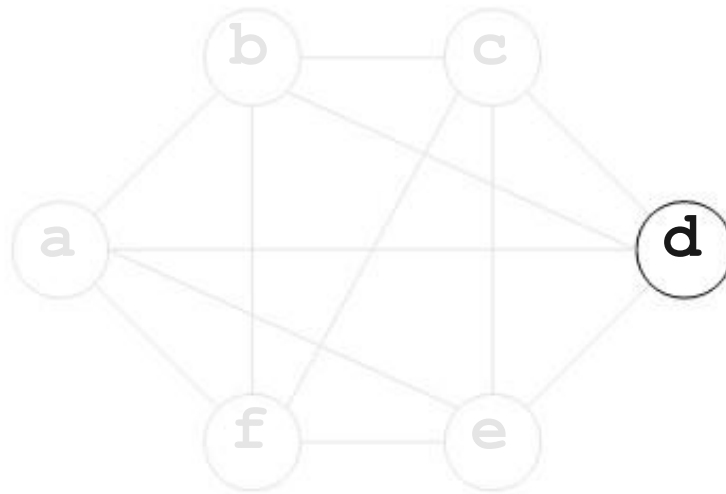
Another Example



Registers



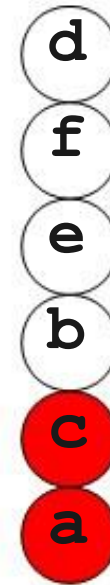
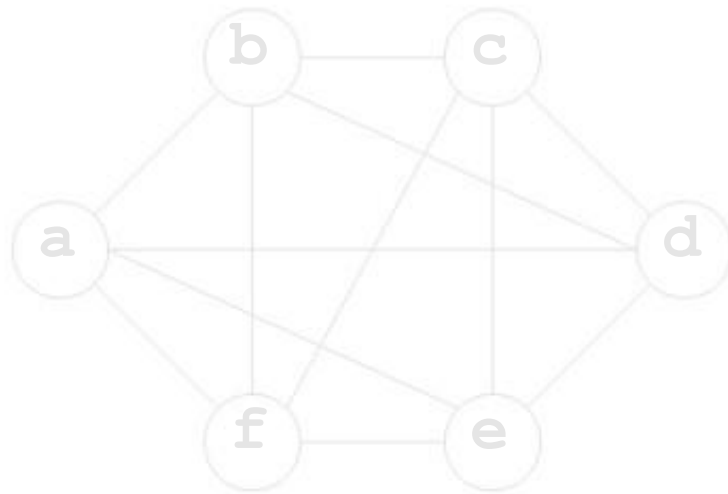
Another Example



Registers



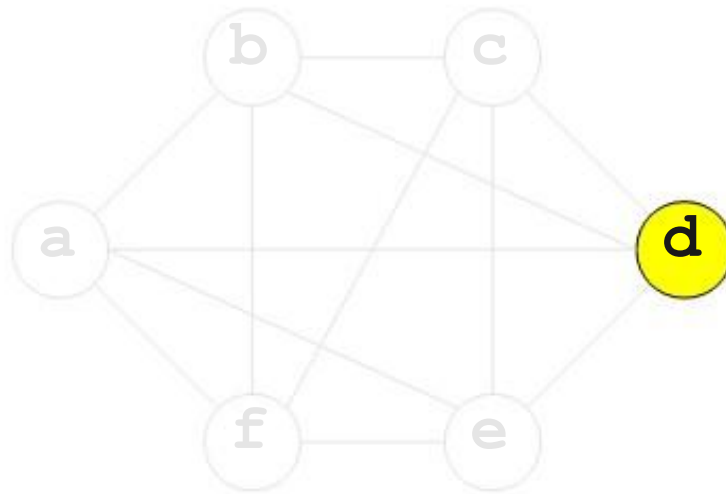
Another Example



Registers



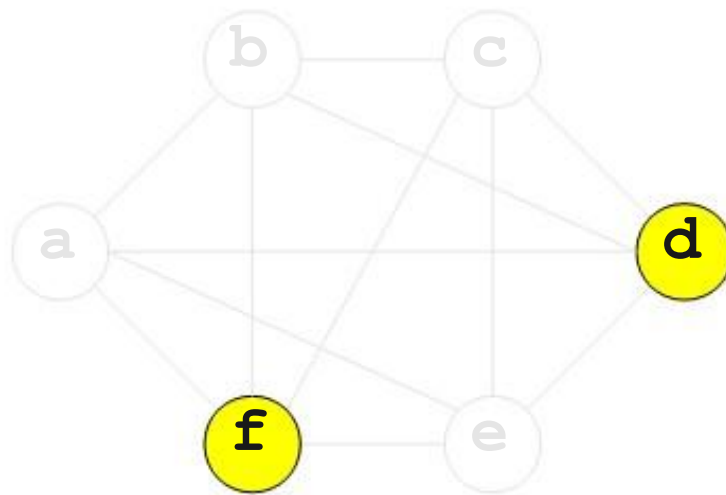
Another Example



Registers



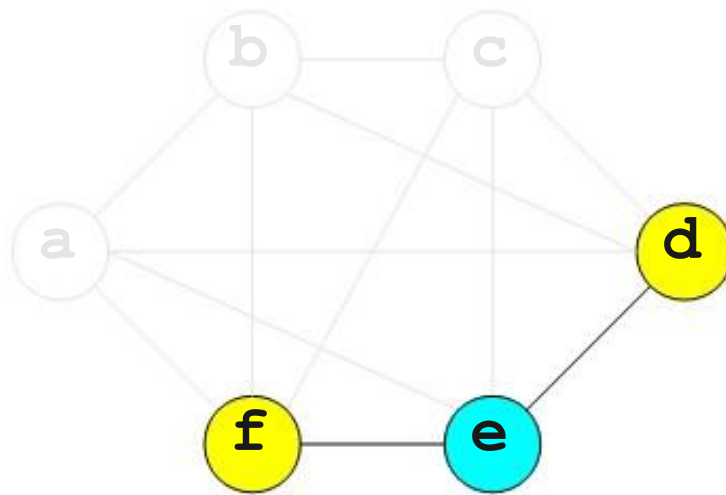
Another Example



Registers



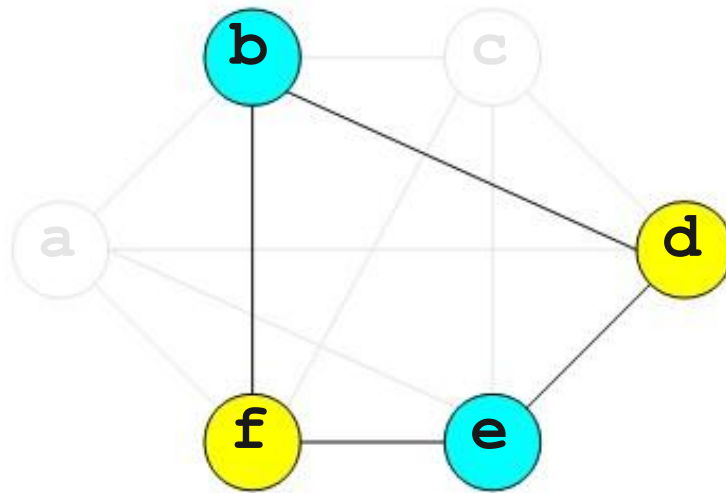
Another Example



Registers



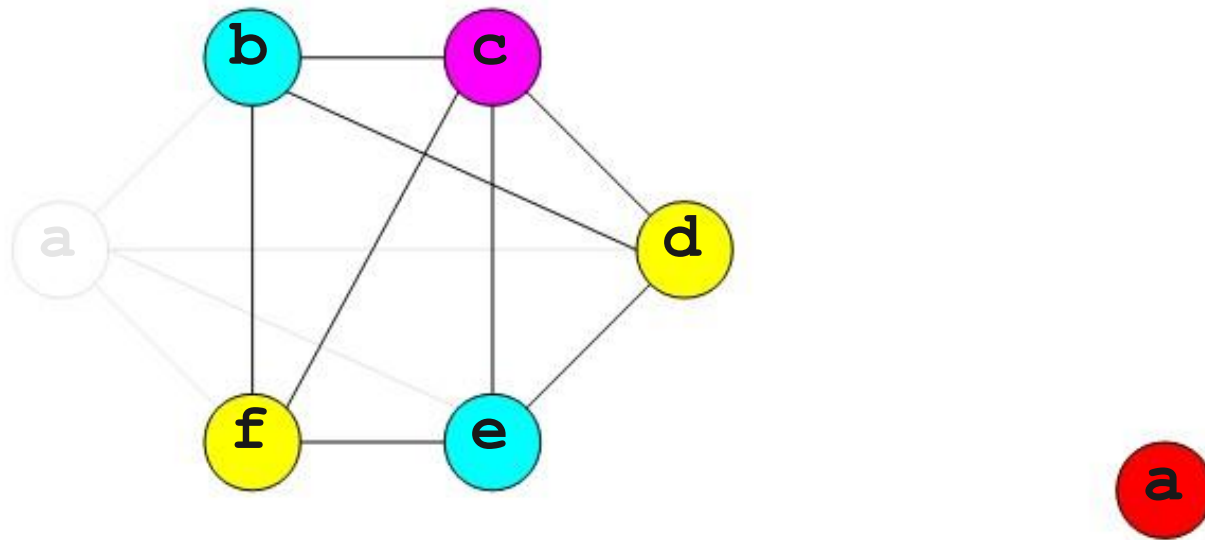
Another Example



Registers



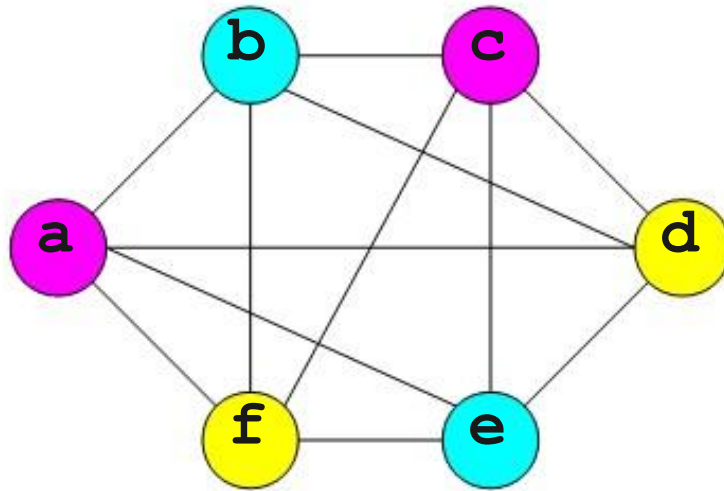
Another Example



Registers



Another Example



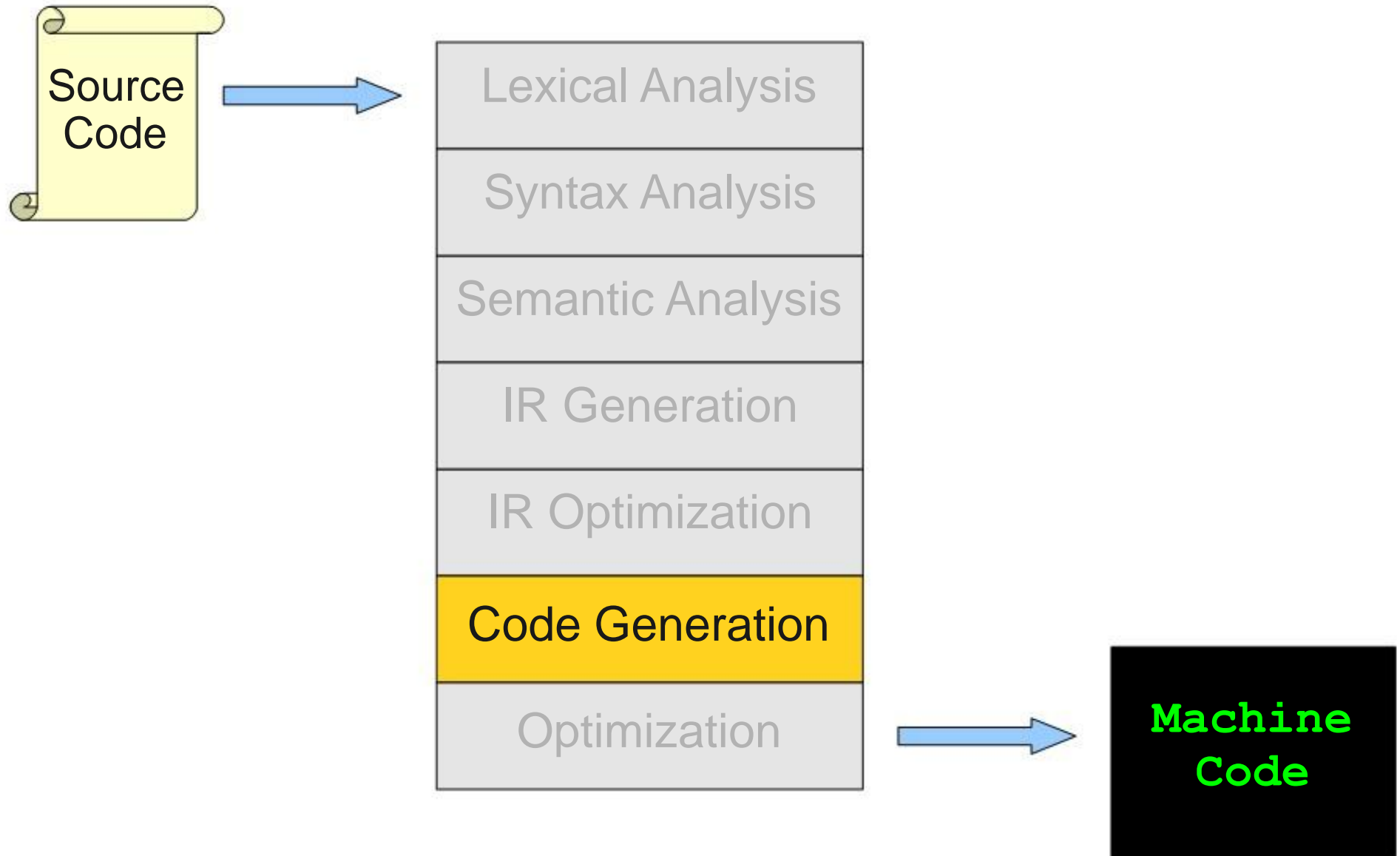
Registers



Note: Chaitin's algorithm often used in production compilers like GCC.

Garbage Collection

Where We Are



Memory Management So Far

- Some memory is preallocated and persists throughout the program:
 - Global variables, virtual function tables, executable code, etc.
- Some memory is allocated on the runtime stack:
 - Local variables, parameters, temporaries.
- **Some memory is allocated in the heap:**
 - Variables or Objects whose size don't know at compile time.
- Memory management for the first two is trivial.
- How do we **manage heap-allocated memory**?

Manual Memory Management

Option One: The programmer handles allocation and deallocation of dynamic memory.

- Approach used in C, C++, e.g. `malloc()`, `free()`
- Advantages:
 - Programmer can exercise precise control over memory usage.
- Disadvantages: (programmer's mistake)
 - **Memory leaks** where resources are never freed.
 - **Double frees** where a resource is freed twice
 - **Use-after-frees** where a deallocated resource is still used.

Automatic Memory Management

- **Idea:** Have the runtime environment automatically reclaim memory.
- Objects that won't be used again are called **garbage**.
- Reclaiming garbage objects automatically is called **garbage collection**.

Types of Garbage Collectors

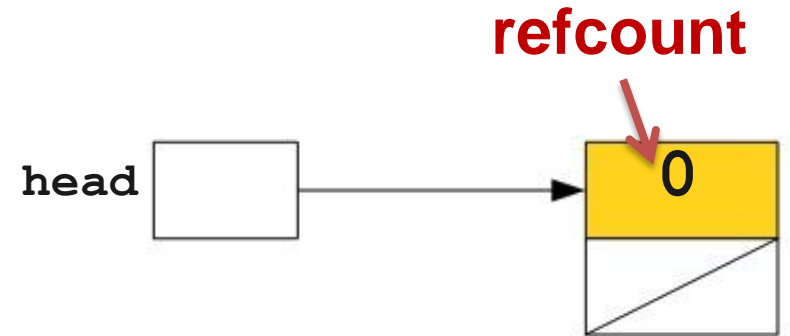
- **Incremental** vs **stop-the-world**:
 - An **incremental** collector is one that runs concurrently with the program.
 - A **stop-the-world** collector pauses program execution to look for garbage.
- **Compacting** vs **non-compacting**:
 - A **compacting** collector is one that moves objects around in memory.
 - A **non-compacting** collector is one that leaves all objects where they originated.
- **Garbage Collection Techniques**
 - Reference Counting, Mark-and-Sweep, Stop-and-Copy, Generational Garbage Collection

Reference Counting

- A simple framework for garbage collection.
- Idea: Store in each object a **reference count** (**refcount**) tracking **how many references exist to the object**.
- When an object has zero **refcount**, it is unreachable and can be reclaimed.

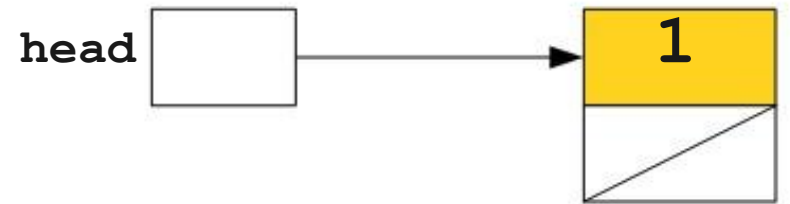
Reference Counting in Action

```
class LinkedList {  
    LinkedList next;  
}  
  
int main() {  
    LinkedList head = new LinkedList;  
    LinkedList mid = new LinkedList;  
    LinkedList tail = new LinkedList;  
  
    head.next = mid;  
    mid.next = tail;  
  
    mid = tail = null;  
  
    head.next.next = null;  
  
    head = null;  
}
```



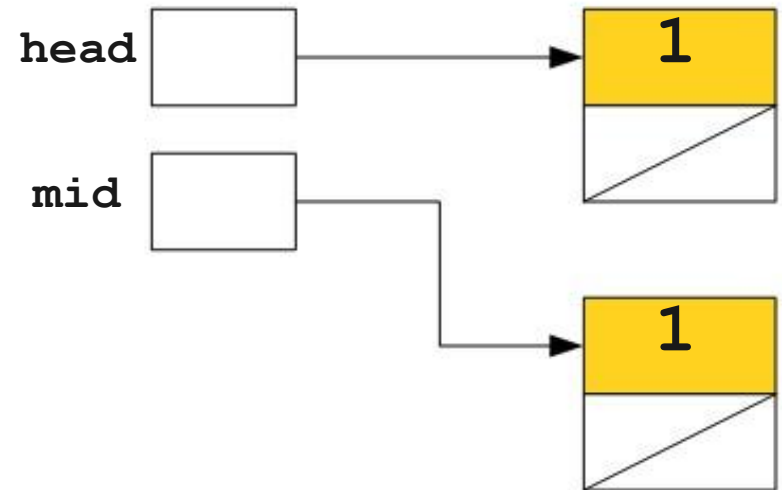
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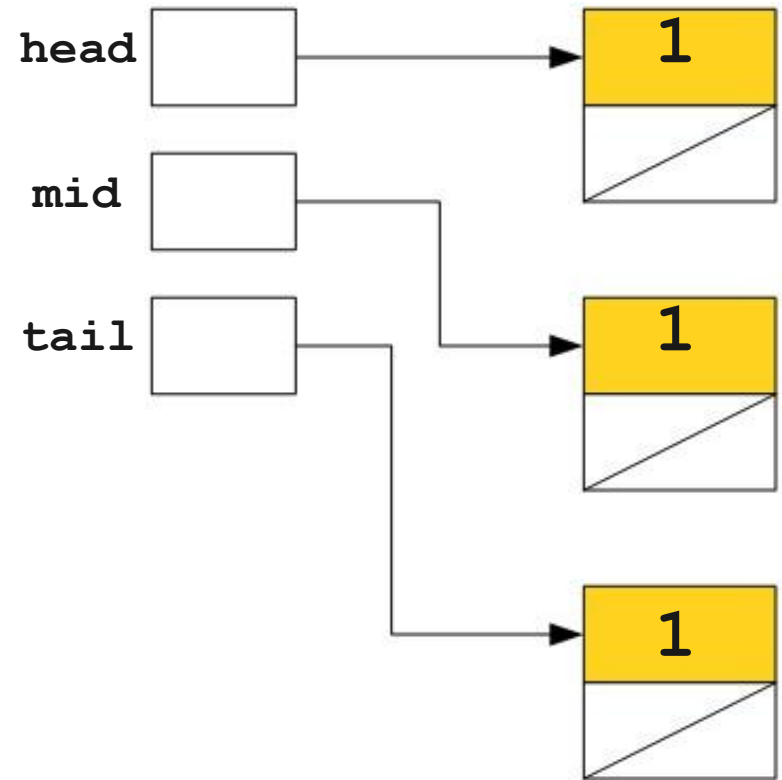
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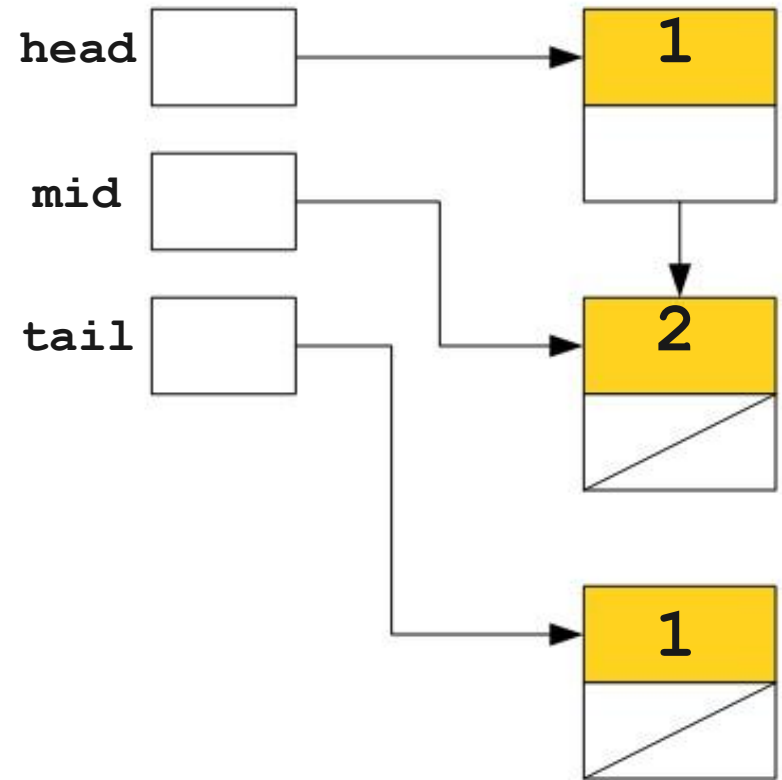
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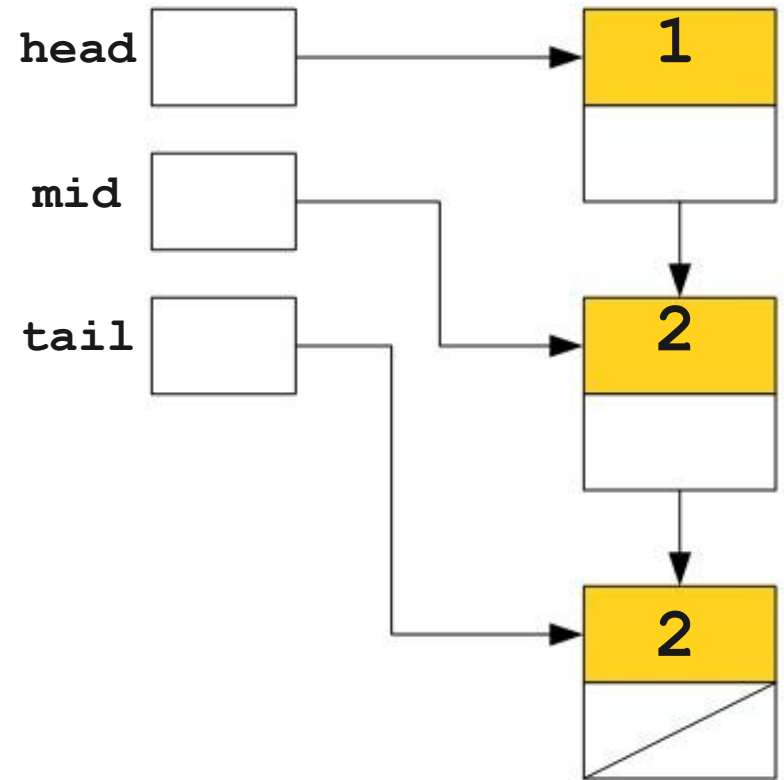
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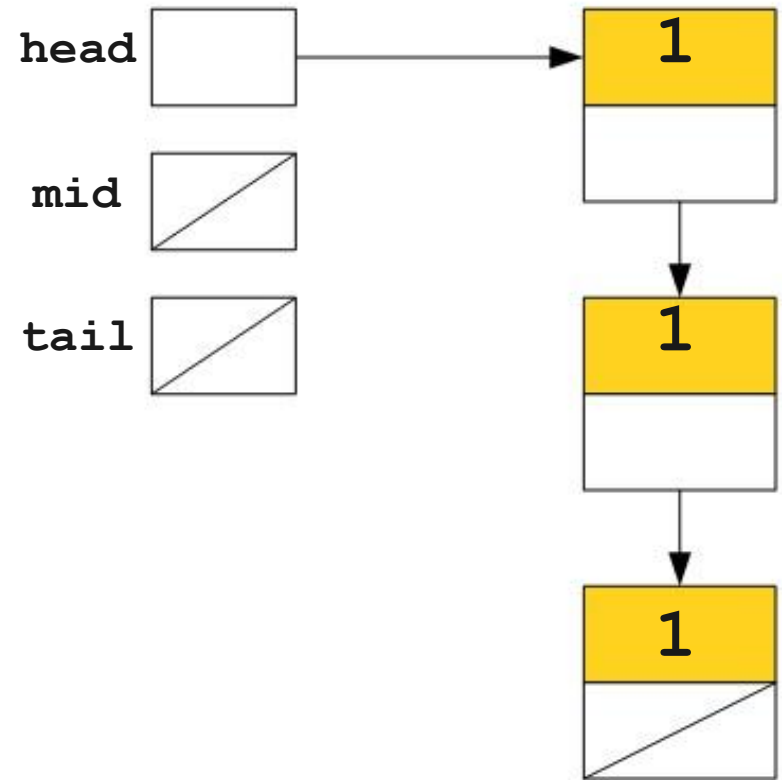
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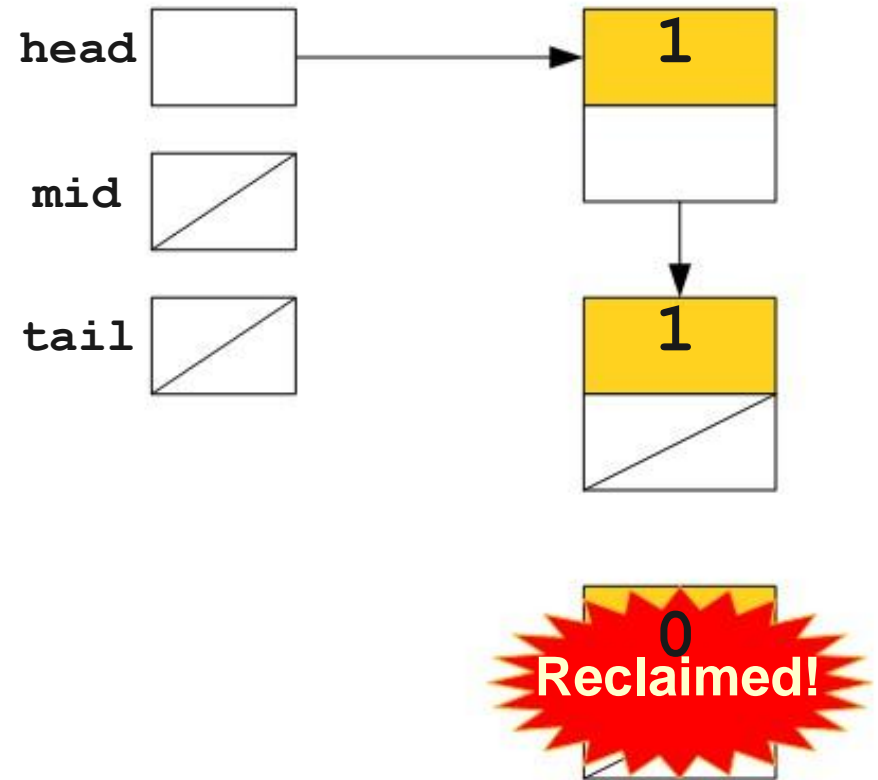
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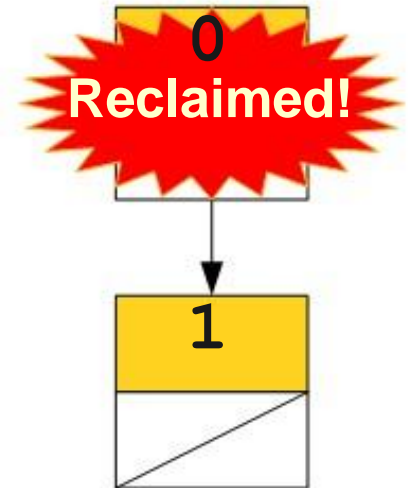
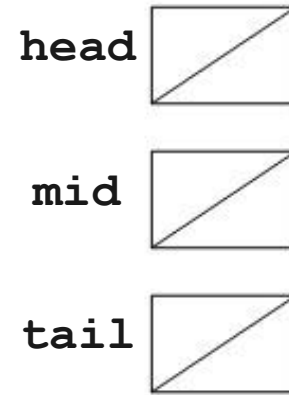
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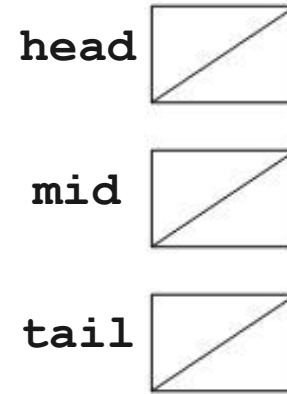
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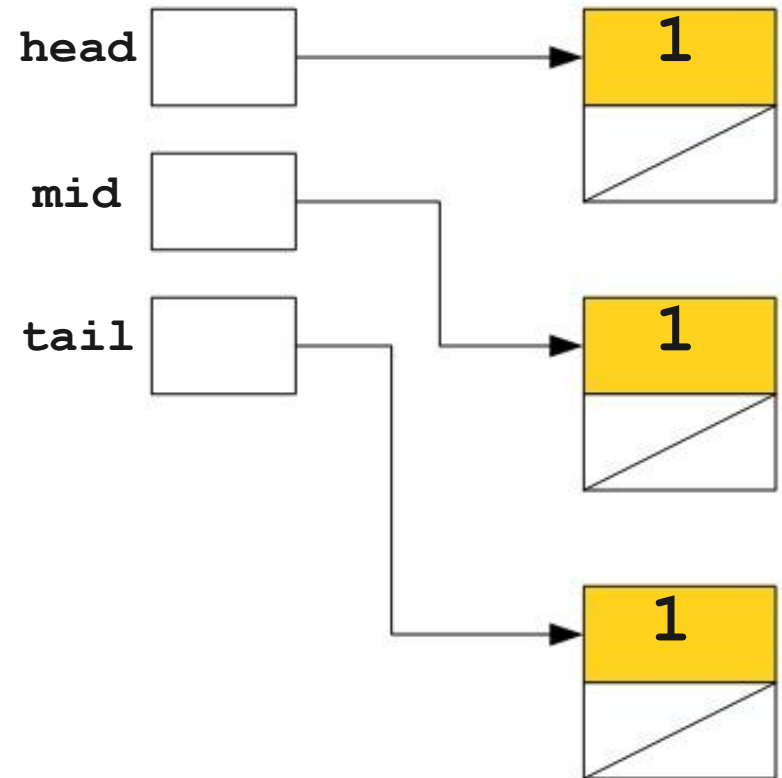
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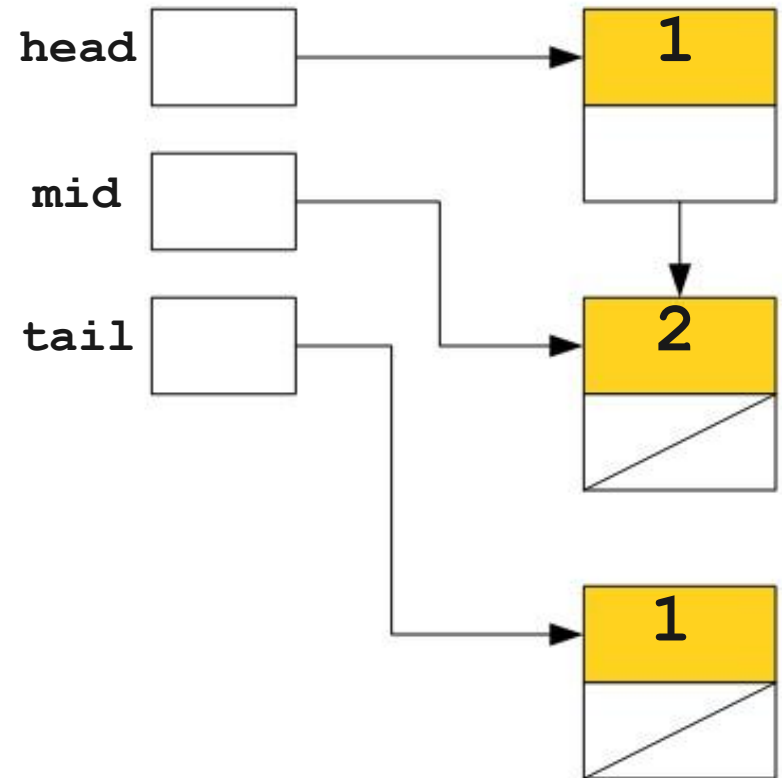
One Major Problem

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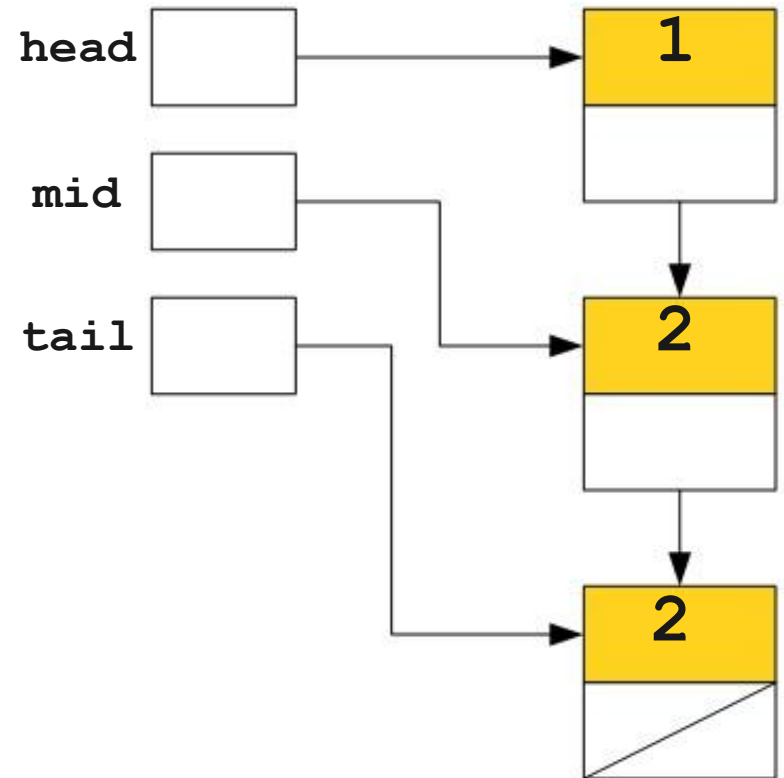
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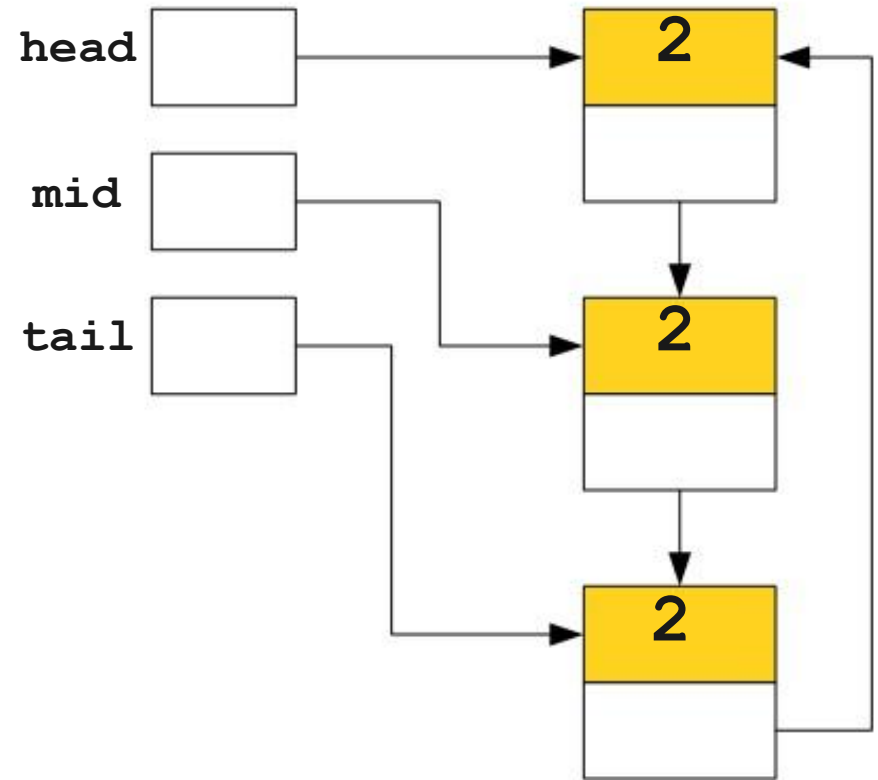
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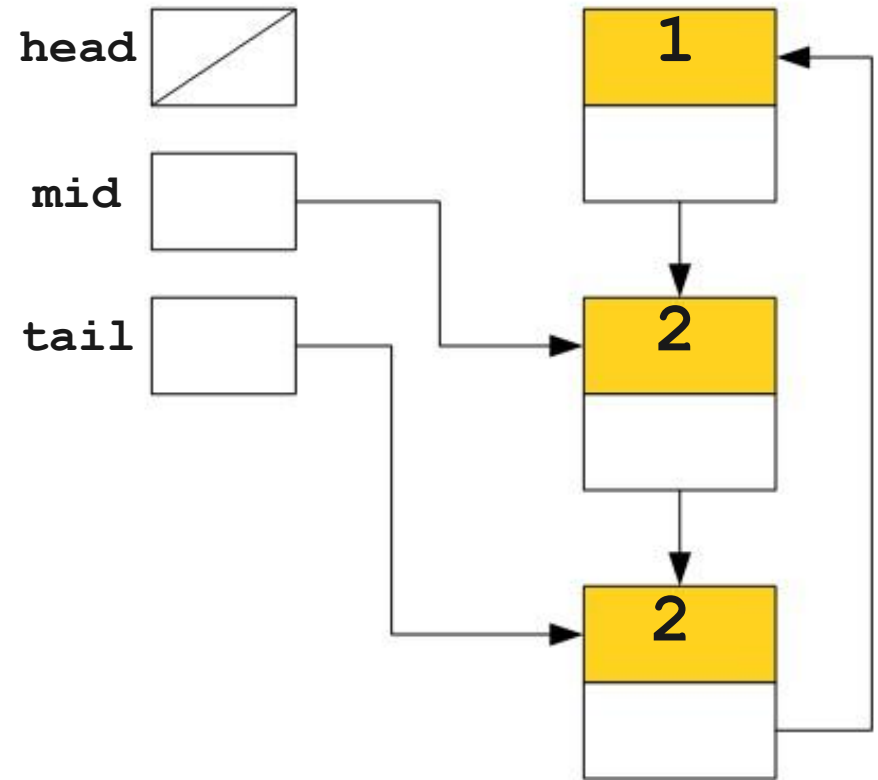
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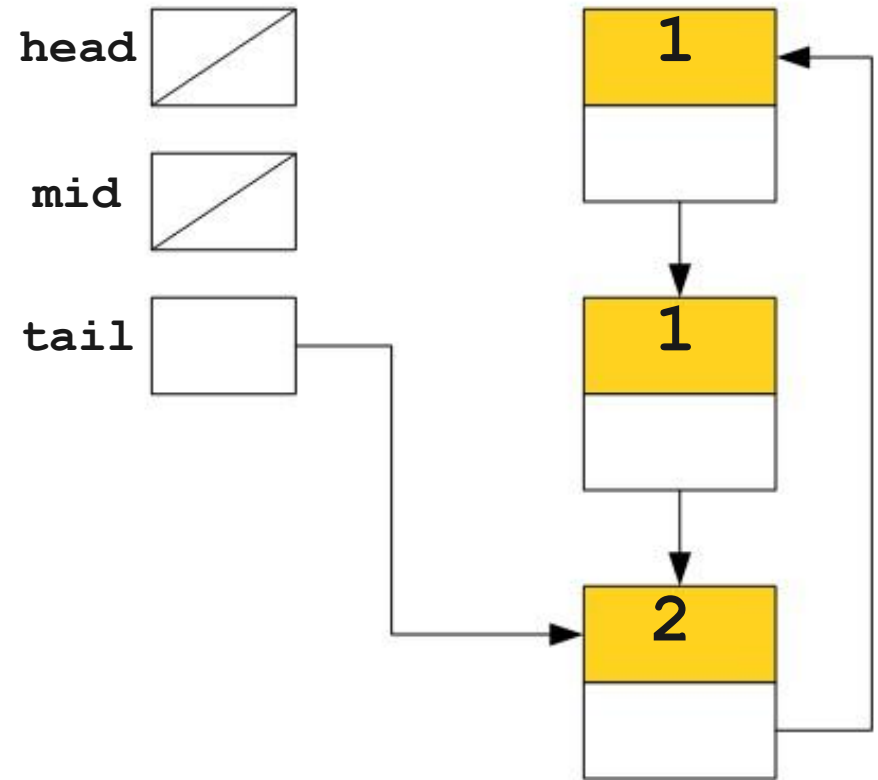
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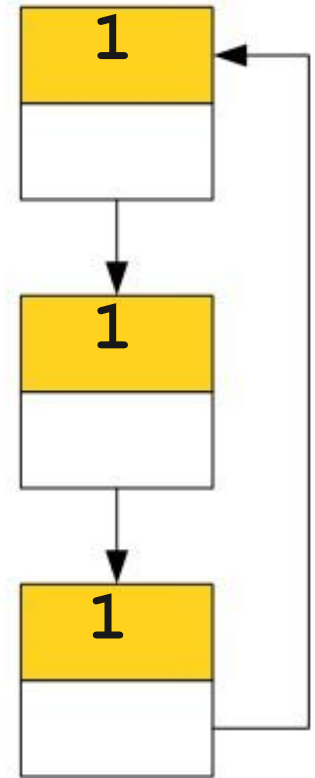
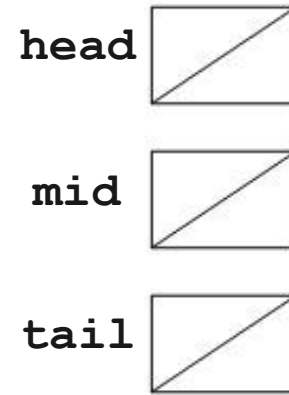
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}
```



Cannot clear the circular garbage !

- Issue: Refcount tracks number of references, not number of *reachable* references.
- Major problems in languages/systems that use reference counting, e.g. Perl, Firefox 2.