



**BINARY IMAGE**

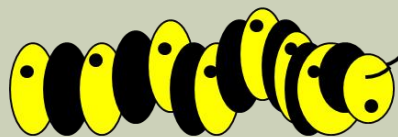
---

**MORPHOLOGICAL  
FILTERING**

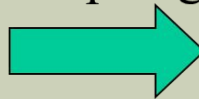
# MORPHOLOGICAL IMAGE PROCESSING

## Introduction

- The word *morphology* commonly denotes a branch of biology that deals with the **form and structure** of animals and plants.
- “morphing” in Biology which means “**changing a shape**”.



Morphing

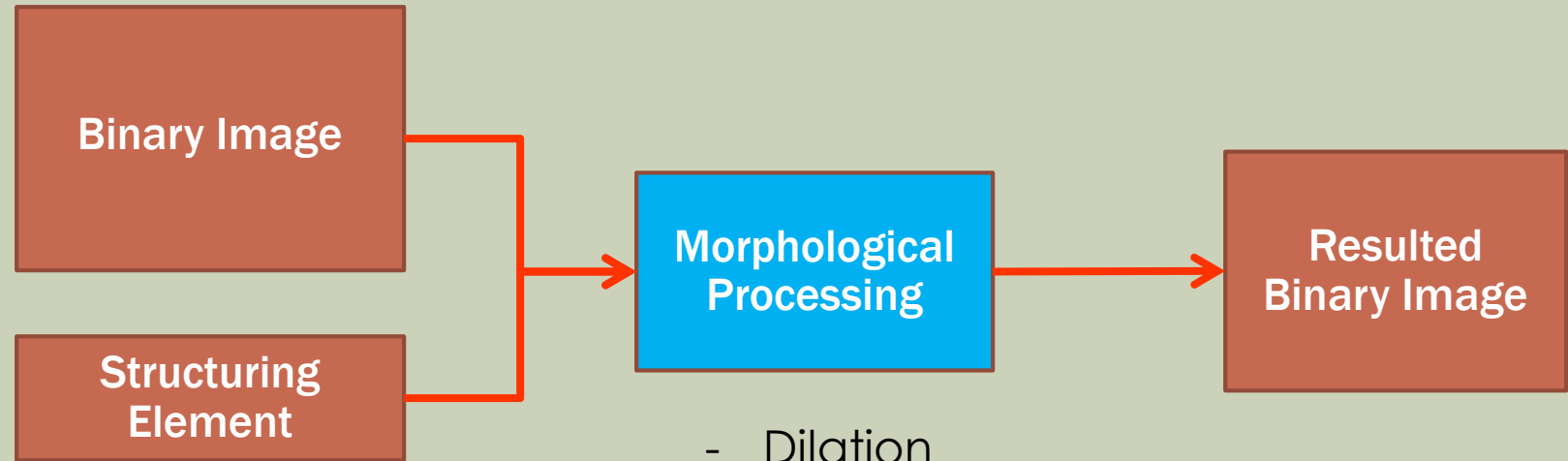


- Therefore, morphological operations are intended to affect the **shape of the object**

# BINARY MORPHOLOGICAL FILTERING

- **pre-processing** used to prepare binary (thresholded) images for object segmentation/recognition
  - Noise filtering, Shape simplification, ...
- **extracting image components** that are useful in the representation and description of region shape, such as
  - boundaries extraction
  - skeletons
  - thinning
  - pruning

# BASIC ELEMENTS



A shape mask with any shapes or sizes

- Square (Box)
- Circle (Disk)
- Cross
- Hexagon
- Any shape

- Dilation
- Erosion
- Opening
- Closing
- Hit-Miss
- Thinning



box



hexagon



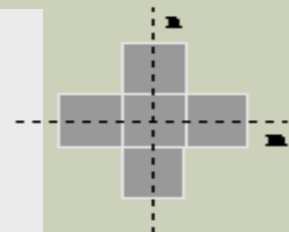
disk



any shape

box(length,width)

disk(diameter)



# BINARY IMAGE

- **white pixels**
  - normally represent foreground regions
  - Binary representation: '1'
- **black pixels**
  - denote background
  - Binary representation: '0'

# STRUCTURING ELEMENT (KERNEL)


- have varying shapes and sizes
- have an origin
- Usually, element values are 0,1 and
  - Other values are also permitted
  - Empty spots (none(!)) are *don't care's!*

**Box**

**Disc**



|   |   |   |
|---|---|---|
| 1 | 1 | 1 |
| 1 | ① | 1 |
| 1 | 1 | 1 |



|   |   |   |
|---|---|---|
|   | 1 |   |
| 1 | ① | 1 |
|   | 1 |   |

|   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|
|   |   | 1 | 1 | 1 |   |   |
|   | 1 | 1 | 1 | 1 | 1 |   |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 1 | 1 | ① | 1 | 1 | 1 |
| 1 | 1 | 1 | 1 | 1 | 1 | 1 |
|   | 1 | 1 | 1 | 1 | 1 |   |
|   |   | 1 | 1 | 1 |   |   |

|   |   |   |
|---|---|---|
| 1 | 1 |   |
| 1 | ① |   |
| 1 |   | 0 |

|   |   |   |
|---|---|---|
| 1 | 1 | 1 |
| 1 | ① | 1 |
| 1 | 1 | 1 |

# MORPHOLOGICAL OPERATIONS

- Basic Operations

- Erosion

- shrinks foreground, enlarges Background

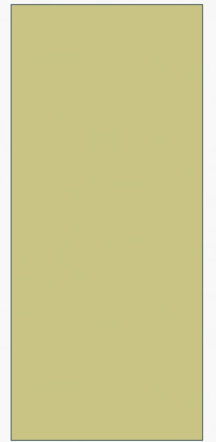


- Dilation

- enlarges foreground, shrinks background
    - filling holes and gaps



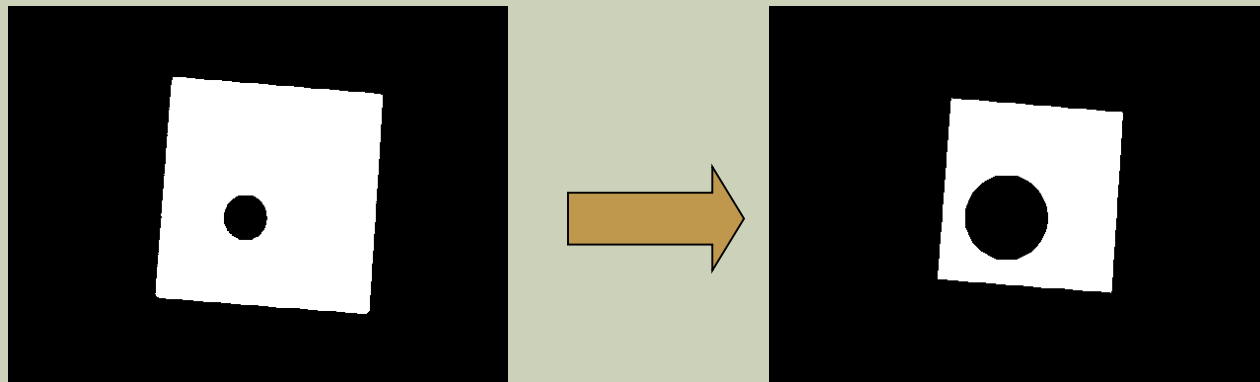
# EROSION OPERATION





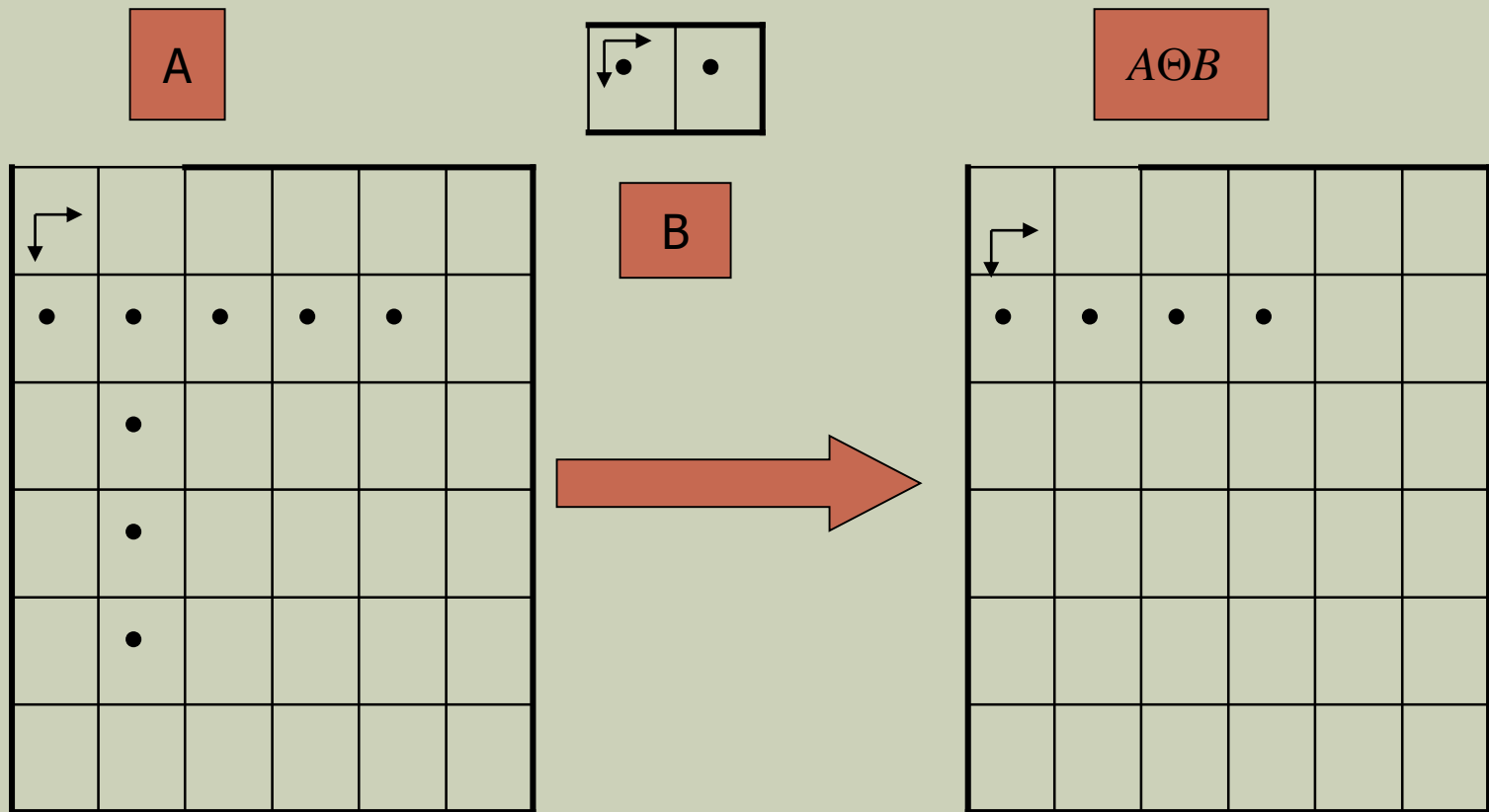
# EROSION OPERATION

- consider each of the *foreground* pixels
- superimpose the structuring element on top
- Consider each foreground pixel in the input image
  - If all the structuring element fits in foreground pixels,
    - write a “1” at the origin of the structuring element!

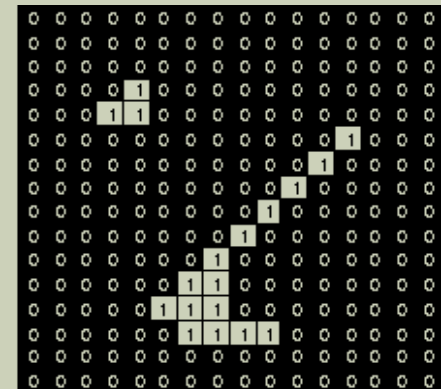
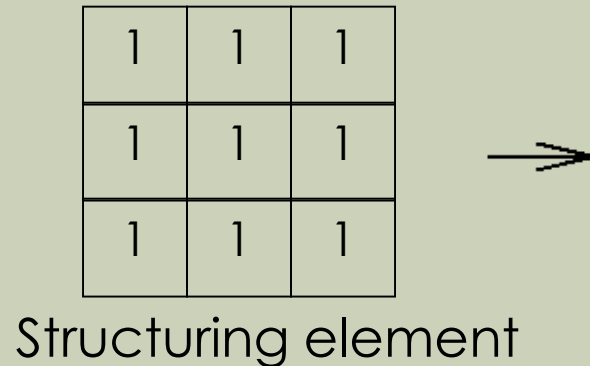
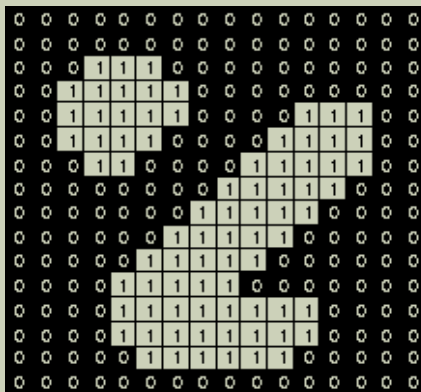
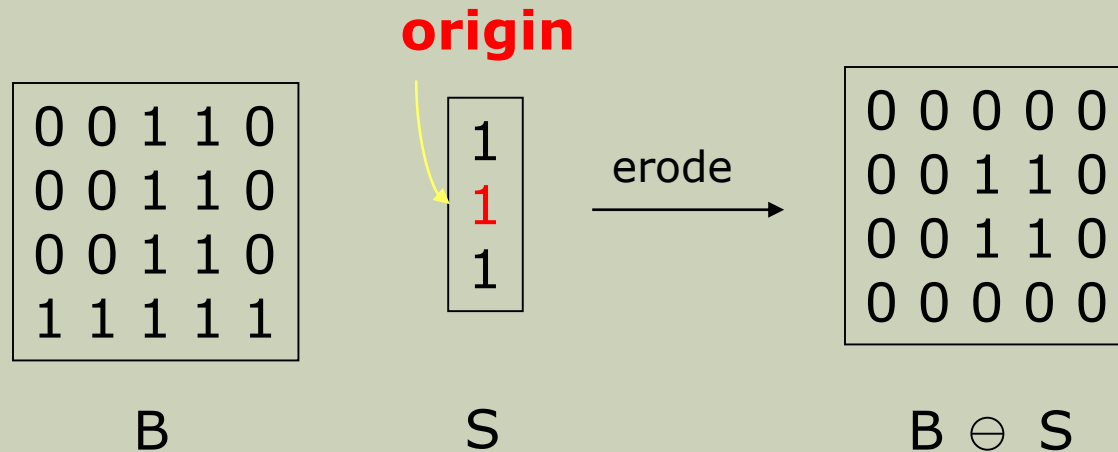


Pixels beyond the boundary of the image are assigned to maximum value -> '1'

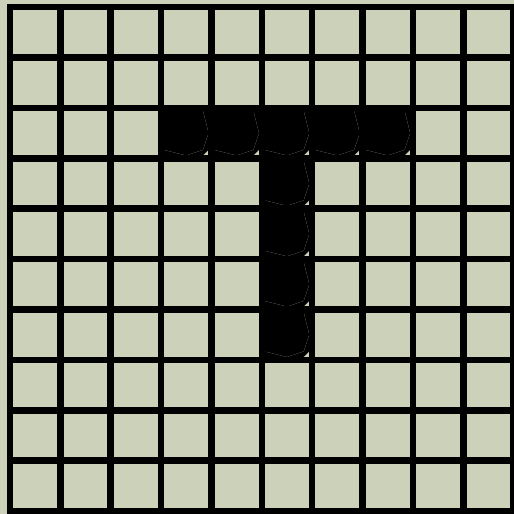
# EXAMPLES OF EROSION OPERATION



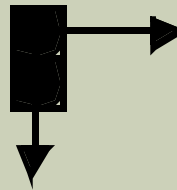
# EXAMPLES OF EROSION OPERATION



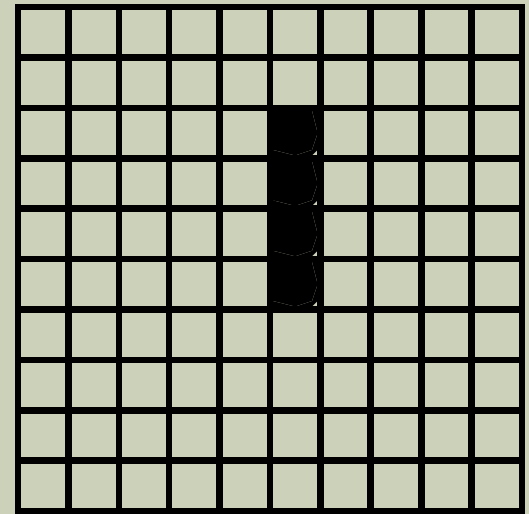
# STRUCTURING ELEMENT IN EROSION EXAMPLE



Image

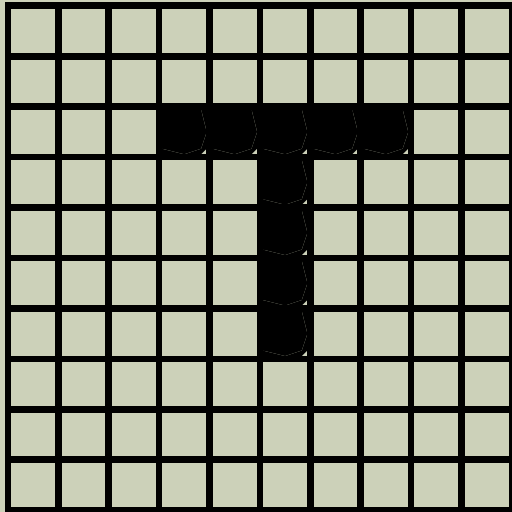


Structuring Element

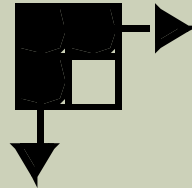


Result

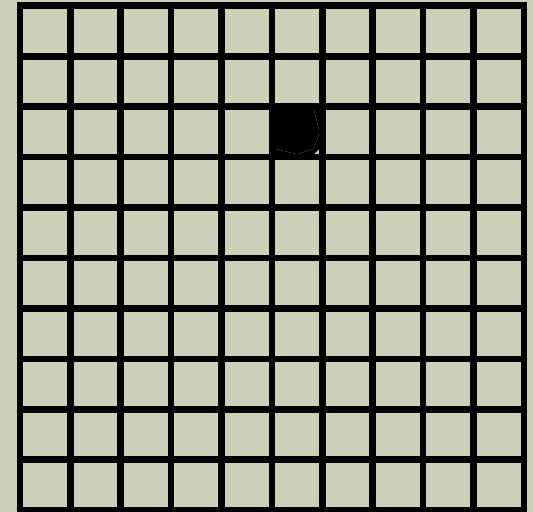
# STRUCTURING ELEMENT IN EROSION EXAMPLE



Image

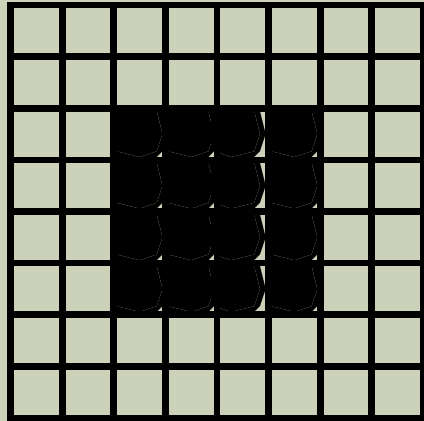


Structuring Element

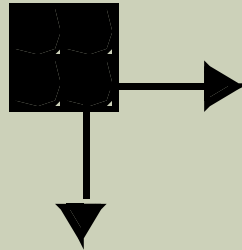


Result

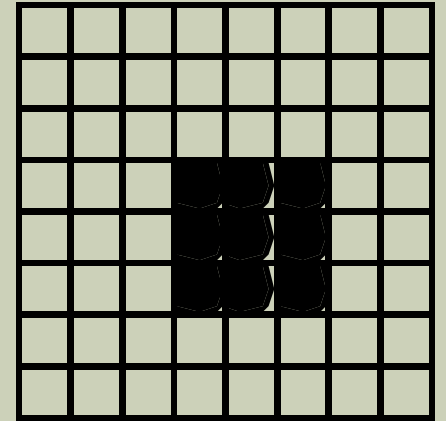
# STRUCTURING ELEMENT IN EROSION EXAMPLE



Image

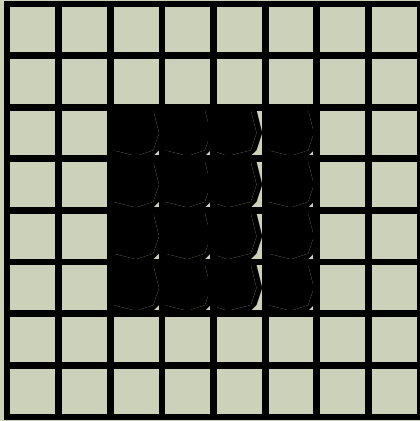


Structuring Element

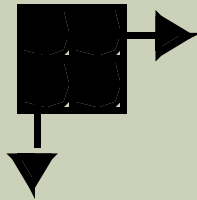


Result

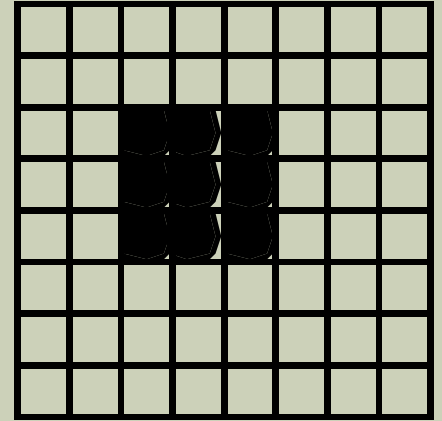
# STRUCTURING ELEMENT IN EROSION EXAMPLE



Image

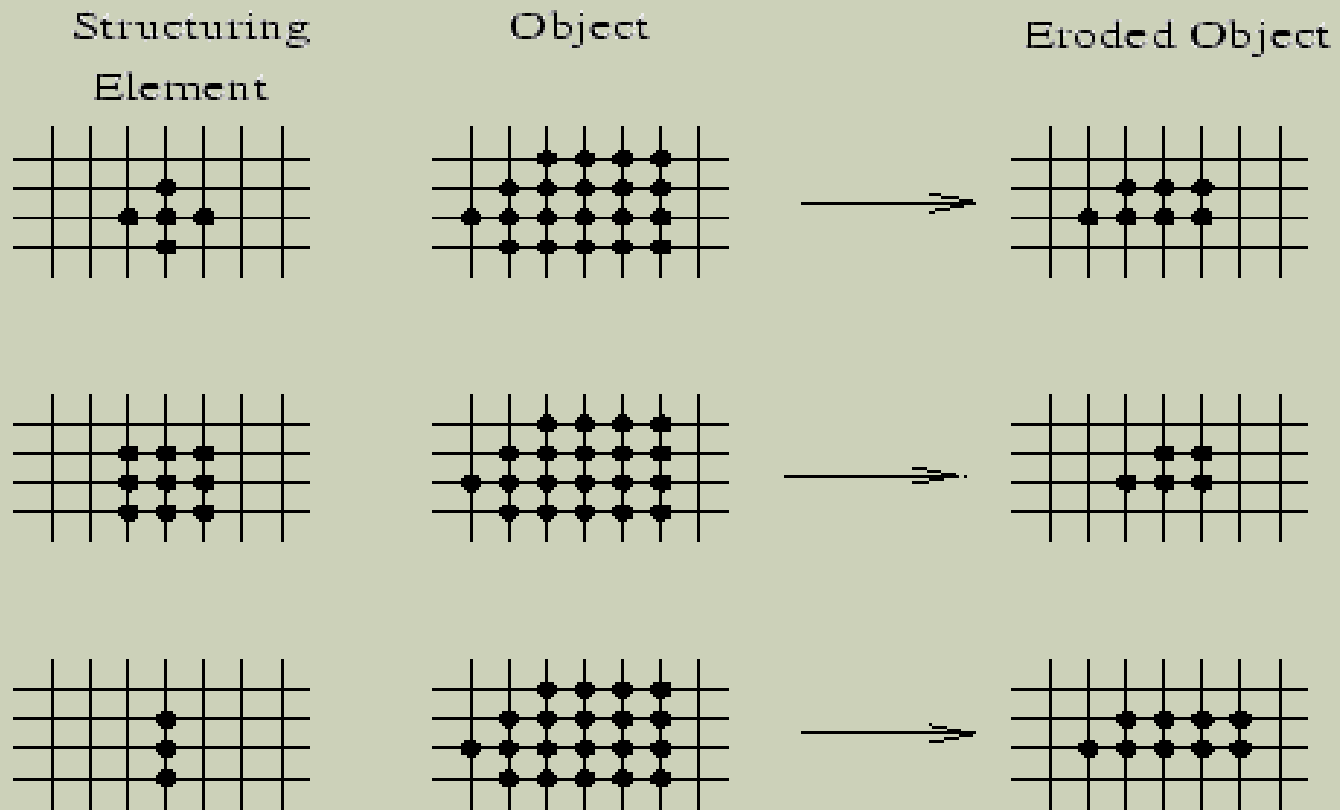


Structuring Element



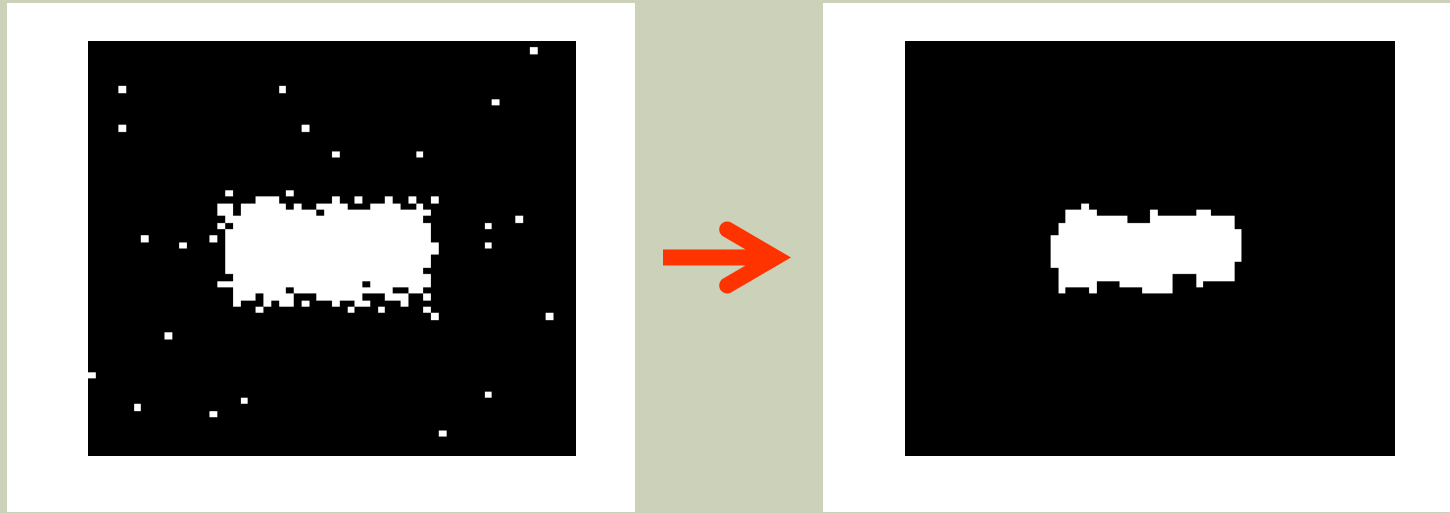
Result

# STRUCTURING ELEMENT IN EROSION EXAMPLE





# EXAMPLE OF EROSION APPLICATIONS

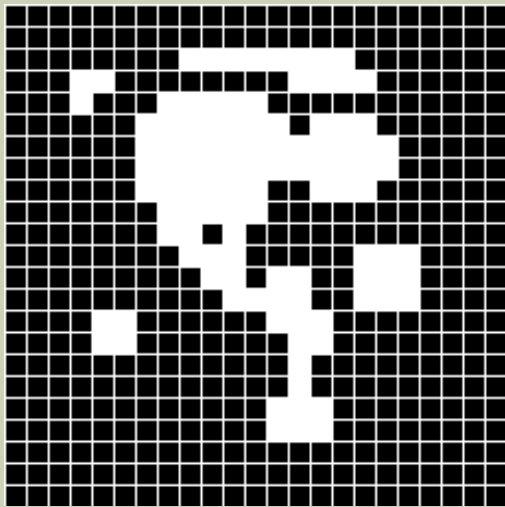


- Removing noise
- Removes the outer layer of object pixels

# EXAMPLE OF EROSION APPLICATIONS

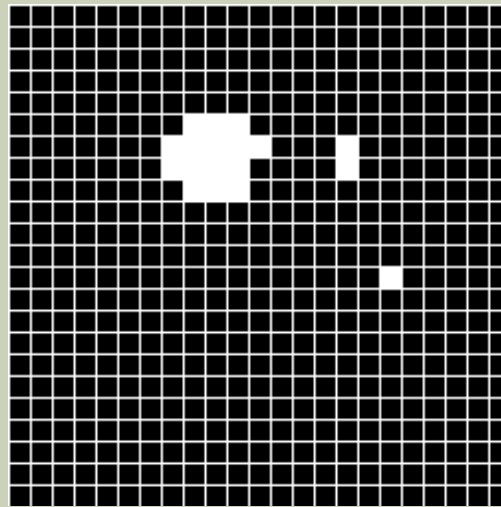
## ■ Edge Detection

- Erosion of an image and then subtracting it away from the original



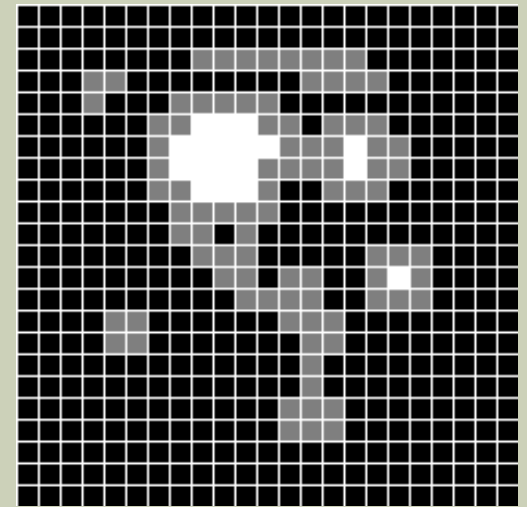
Segmented Image

-



Erosion Result

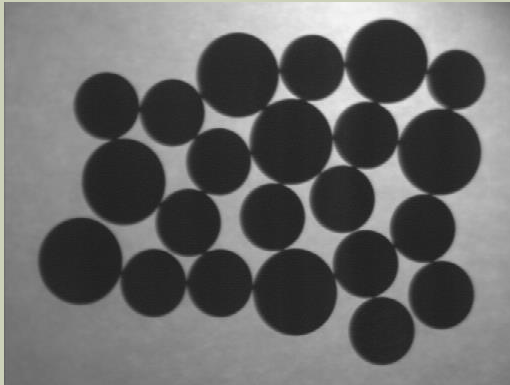
=



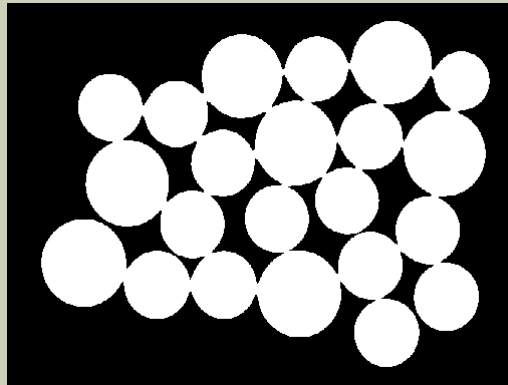
Edge Result

# EXAMPLE OF EROSION APPLICATIONS

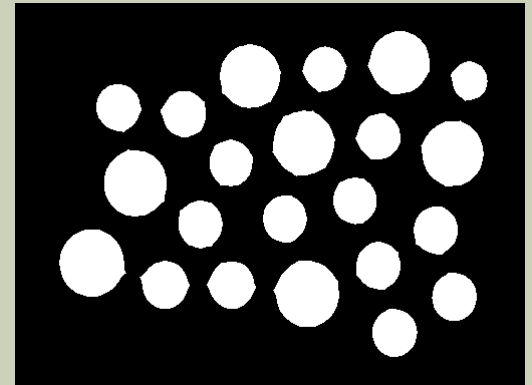
- Simple application of **pattern matching**



**Original Image**

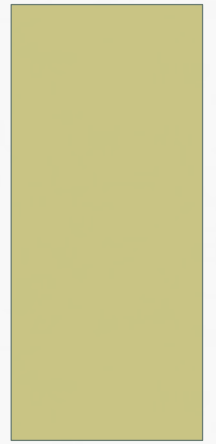


**Segmented Image**



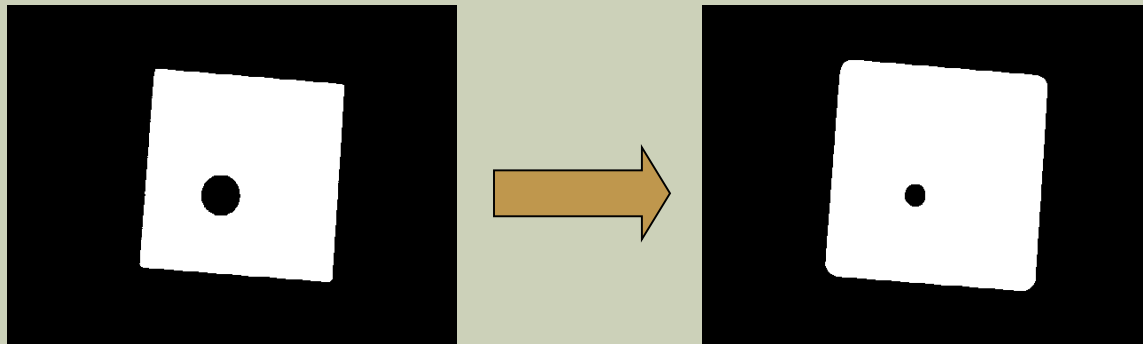
**Erosion Result**

# DILATION OPERATION

A solid dark grey horizontal bar spanning the width of the slide's main content area.

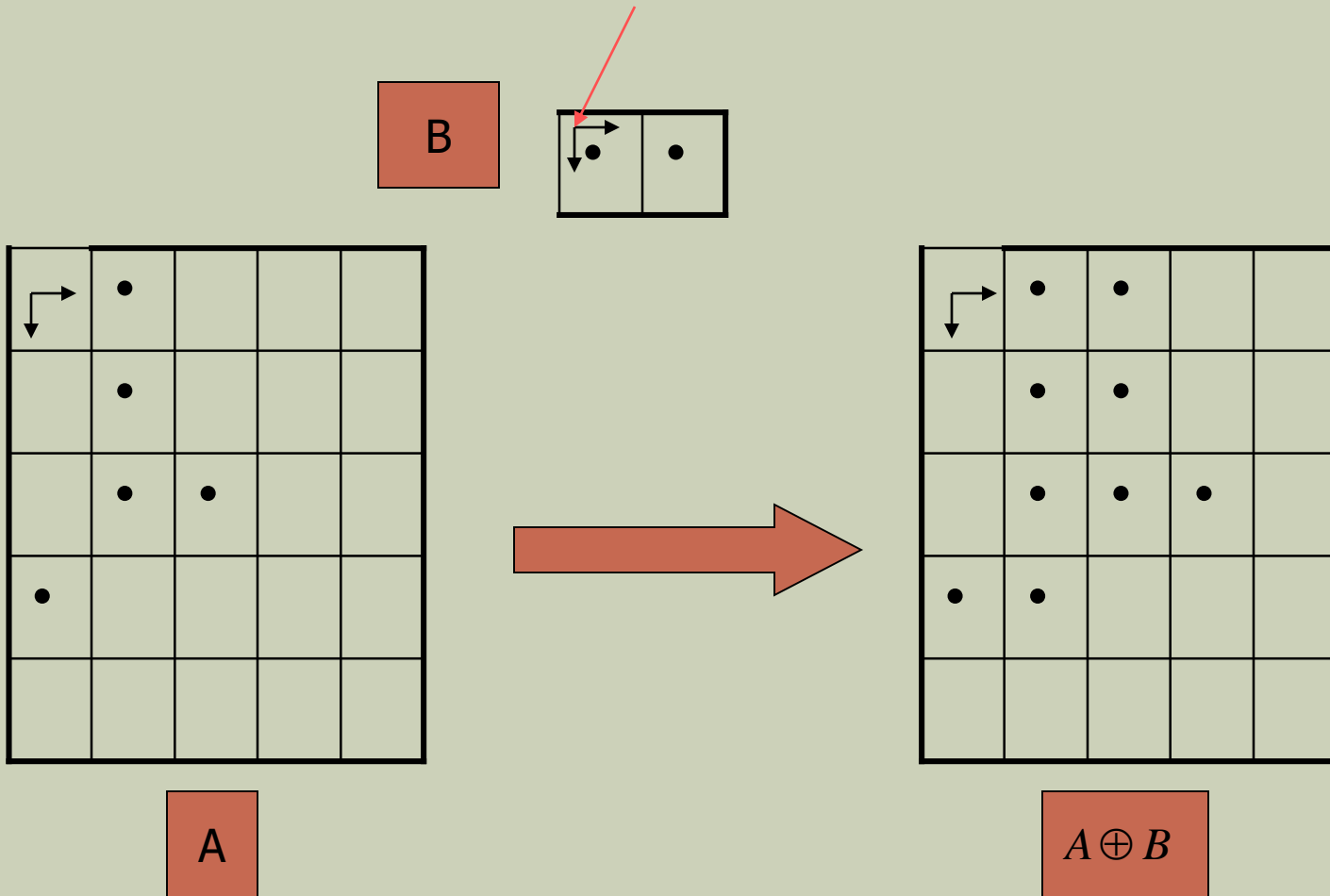
# DILATION OPERATION

- consider each of the *foreground* pixels
- superimpose the structuring element on top
- Consider each foreground pixel in the input image
  - If any the structuring element touches in foreground pixels,
    - write a “1” at the origin of the structuring element!

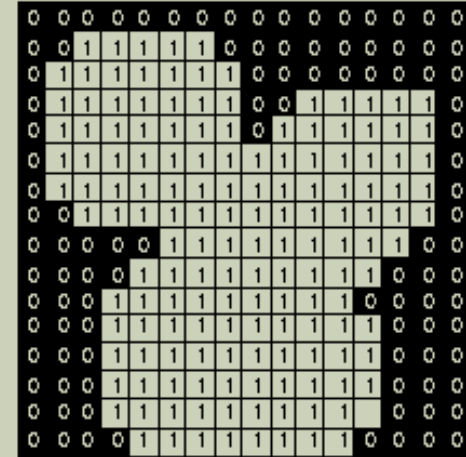
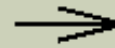
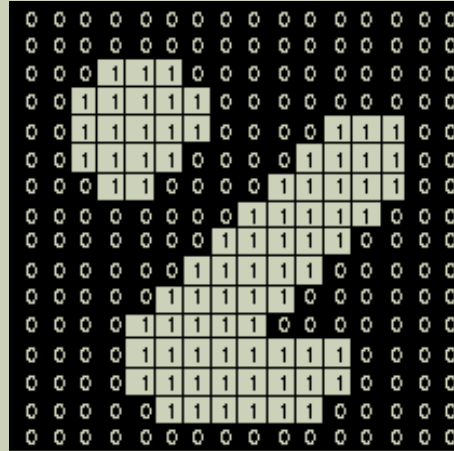
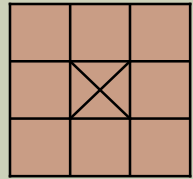


Pixels beyond the boundary of the image are assigned to minimum value -> '0'

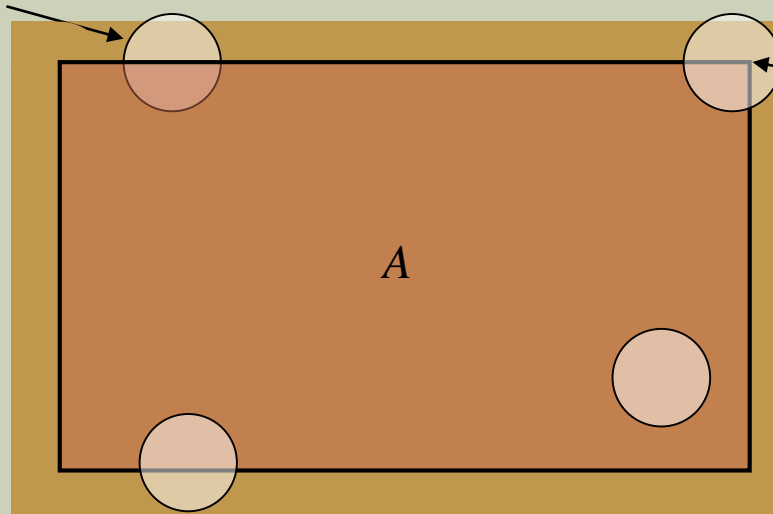
# EXAMPLES OF DILATION OPERATION



# EXAMPLES OF DILATION OPERATION



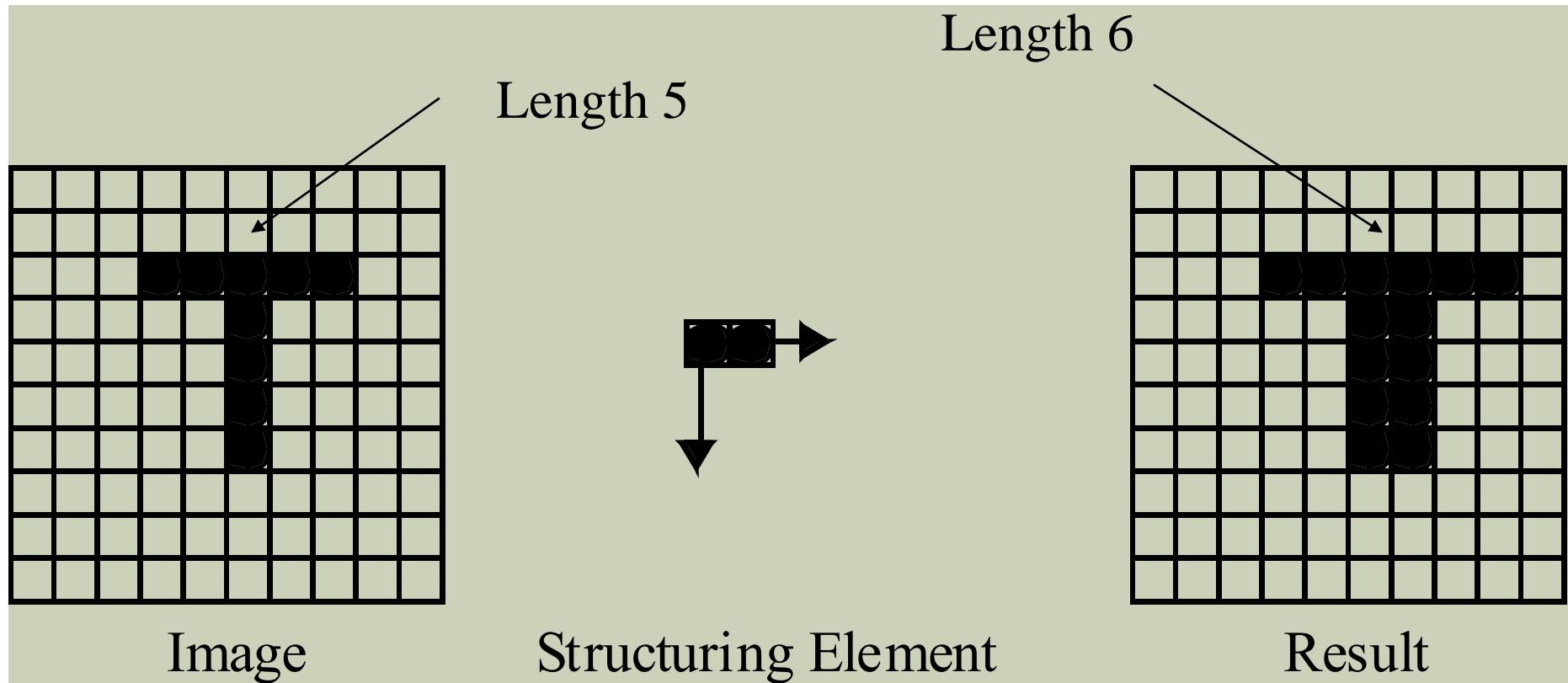
$(B)_x$



Center of  
the circle

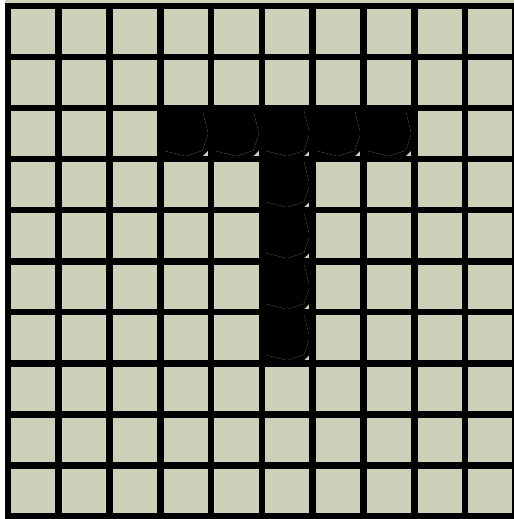
$A \oplus B$

# EXAMPLES OF DILATION OPERATION

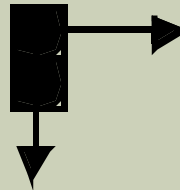




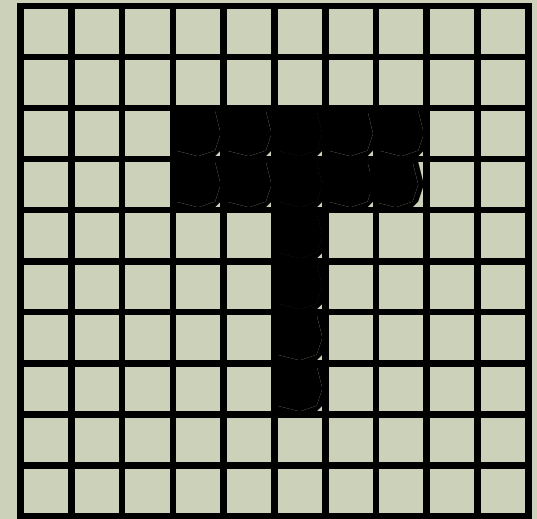
# EXAMPLES OF DILATION OPERATION



Image

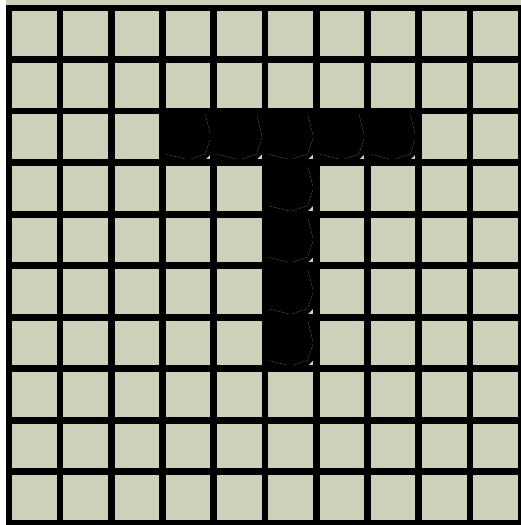


Structuring Element

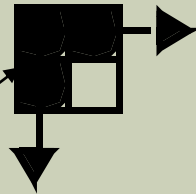


Result

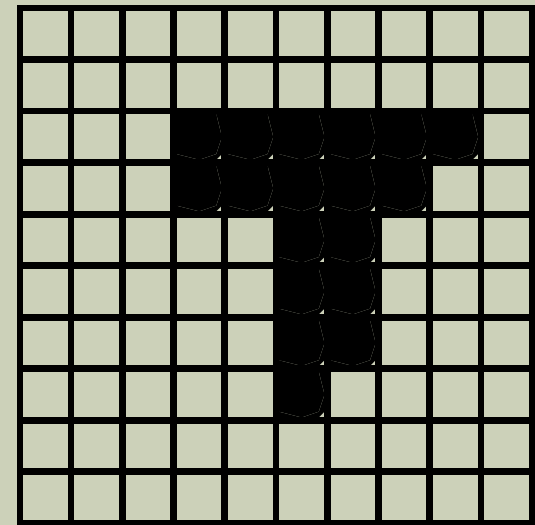
# EXAMPLES OF DILATION OPERATION



Image



Structuring Element



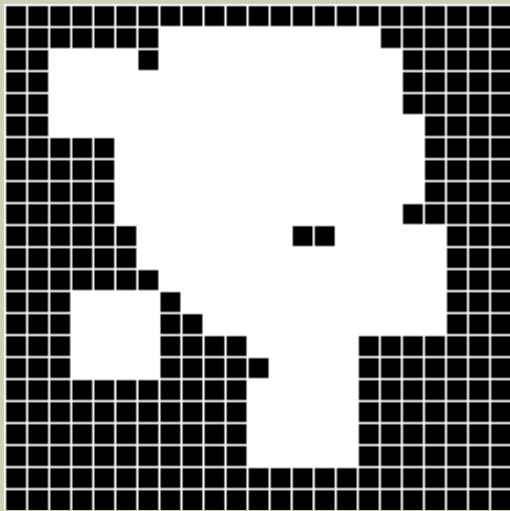
Result

Single point in Image replaced with  
this in the Result

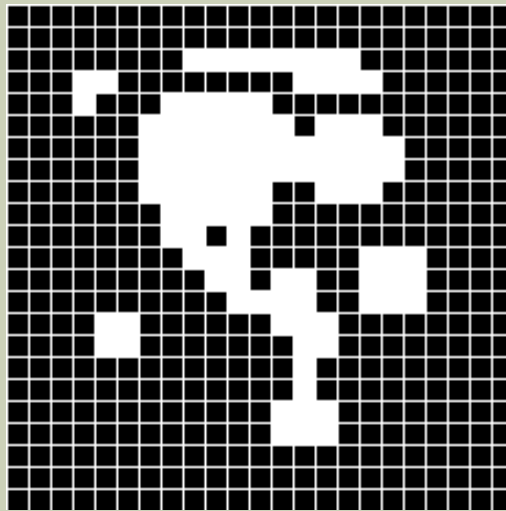
# EXAMPLE OF DILATION APPLICATIONS

- Edge Detection

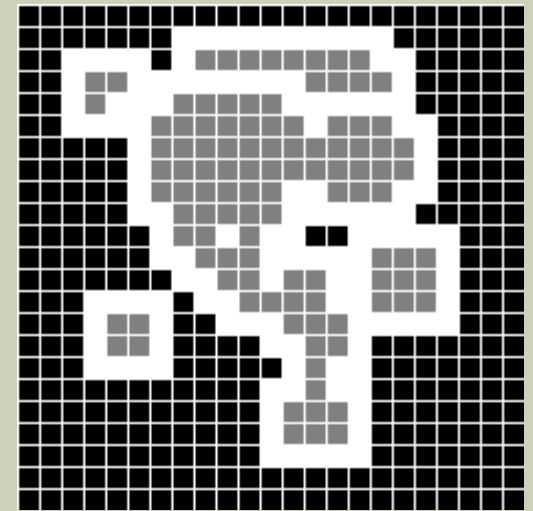
- Dilation of an image and then subtracting it away from the original



Dilation Result

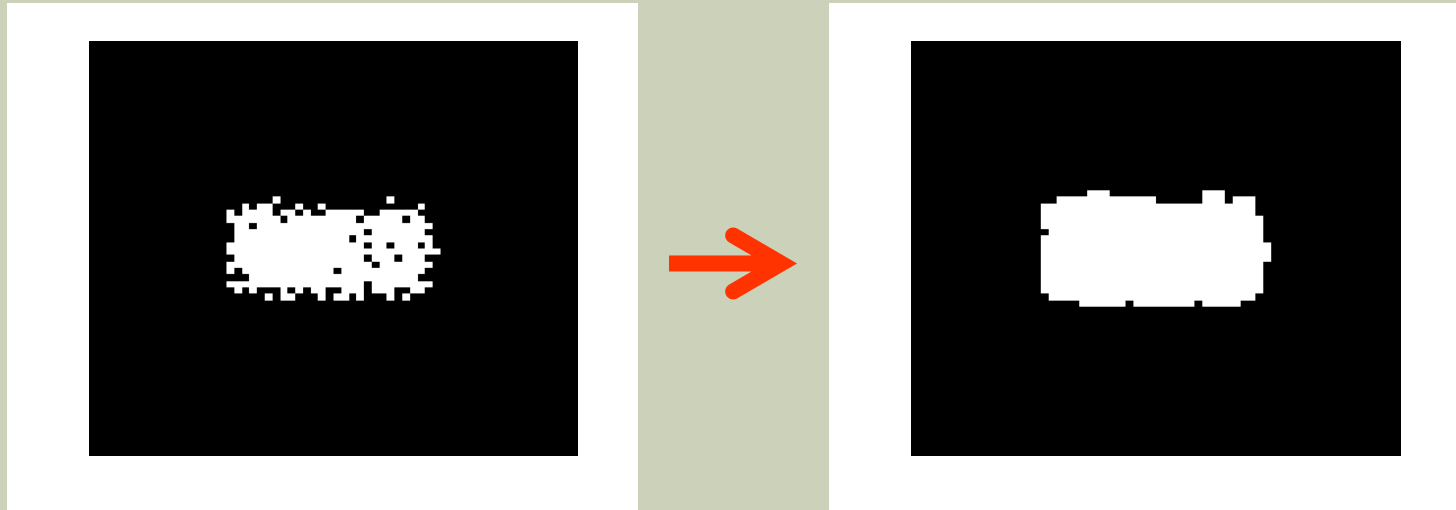


Segmented Image



Edge Result

# EXAMPLE OF DILATION APPLICATIONS



- Fill holes in objects
- Smooth object boundaries.
- Adds an extra outer ring of pixels onto object boundary, ie, object becomes slightly larger

# BOUNDARY HANDLING

- Outside an image
  - It would be either all zeros or ones
  - Sometimes depend on tools
- In Matlab
  - Erosion operation
    - Set outside pixels as zero padding
  - Dilation operation
    - Set outside pixels as one padding

# EXERCISE

**SE =**

|   |   |   |
|---|---|---|
|   | 1 |   |
| 1 | 1 | 1 |
|   | 1 |   |

## ■ Exercise#1

■ Erosion -> Dilation

## ■ Exercise#2

■ Dilation -> Erosion

|   |   |   |   |   |   |   |   |
|---|---|---|---|---|---|---|---|
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 |
| 0 | 1 | 1 | 1 | 1 | 0 | 0 | 1 |
| 0 | 1 | 1 | 1 | 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 | 1 | 0 | 0 | 0 |
| 0 | 1 | 0 | 0 | 1 | 0 | 1 | 1 |
| 0 | 1 | 1 | 1 | 0 | 0 | 1 | 1 |
| 0 | 1 | 1 | 1 | 0 | 0 | 0 | 0 |
| 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

# OPENING OPERATION

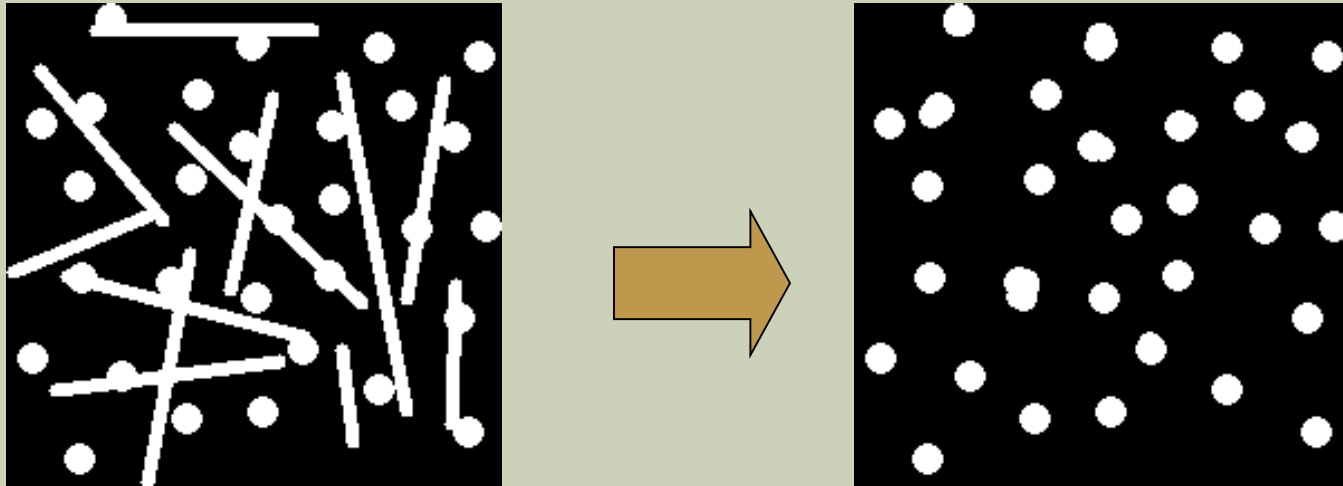


# OPENING OPERATION

- An erosion followed by a dilation
- the same structuring element for both operations.
- Take the structuring element (SE) and slide it around *inside* each foreground region.
  - All pixels which can be covered by the SE with the SE being entirely within the foreground region will be preserved.
  - All foreground pixels which can *not* be reached by the structuring element without lapping over the edge of the foreground object will be eroded away!
- Opening is idempotent: Repeated application has no further effects

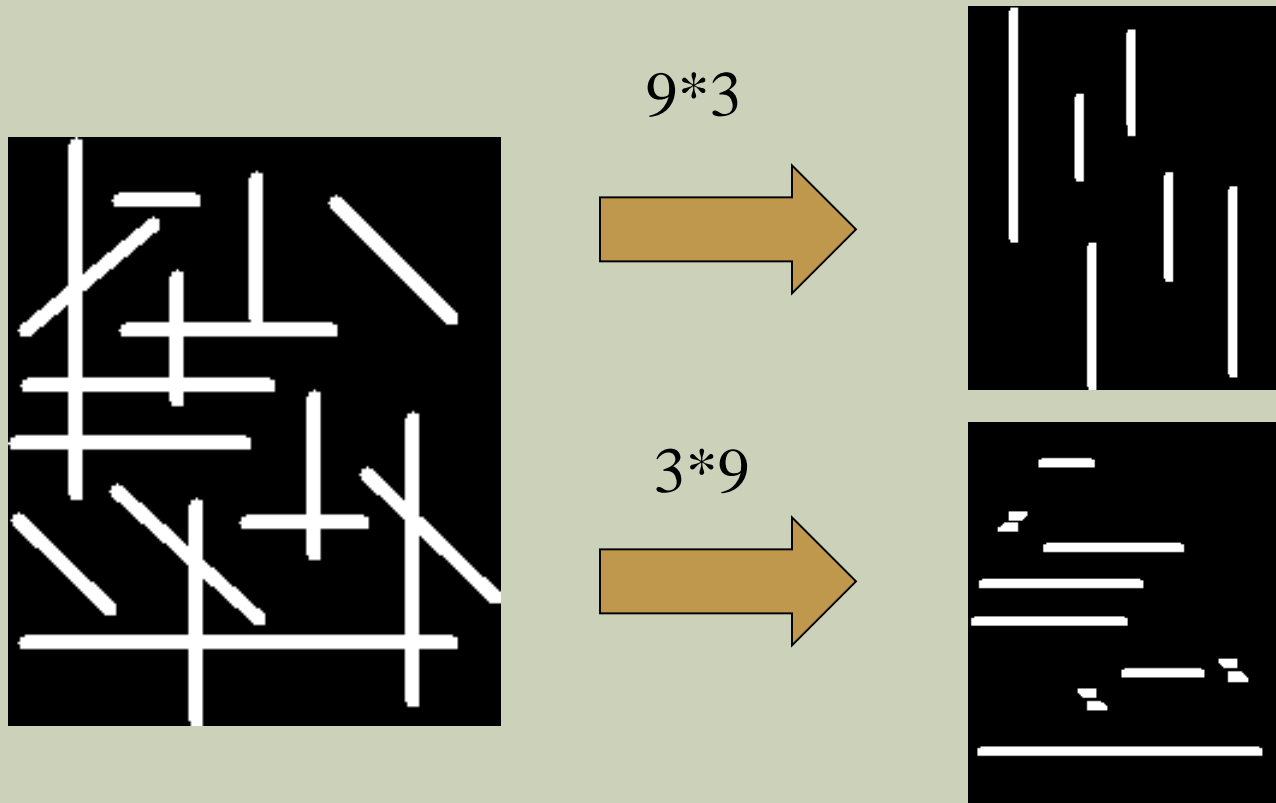


# EXAMPLE OF OPENING APPLICATIONS



- Opening with a 11 pixel diameter disc
- Preserve circle objects
  - diameter equal or greater than 11 pixels

# EXAMPLE OF OPENING APPLICATIONS



- 9x3 and 3x9 Structuring Element

# CLOSING OPERATION



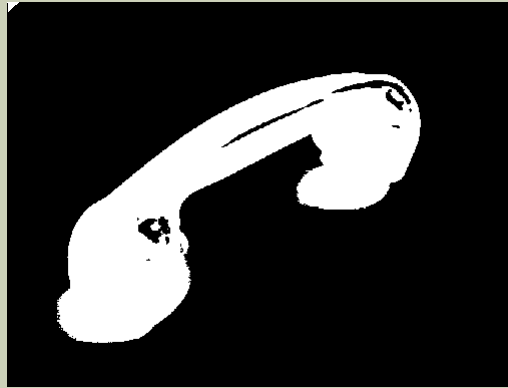
# CLOSING OPERATION

- **Dilation followed by erosion**
- *the same structuring element for both operations.*
- Take the structuring element (**SE**) and **slide it around** *outside* each foreground region.
  - All background pixels which can be **covered by the SE** with the SE being entirely within the background region will be **preserved**.
  - All background pixels which can *not* be reached by the structuring element without lapping over the edge of the foreground object will be turned into a foreground.
- Closing is idempotent: **Repeated** application has **no further effects**

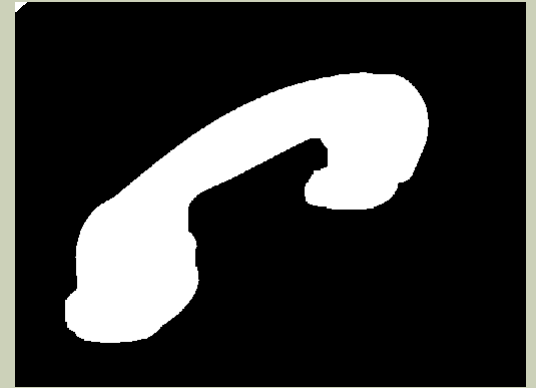
# EXAMPLE OF CLOSING APPLICATIONS



**Original Image**



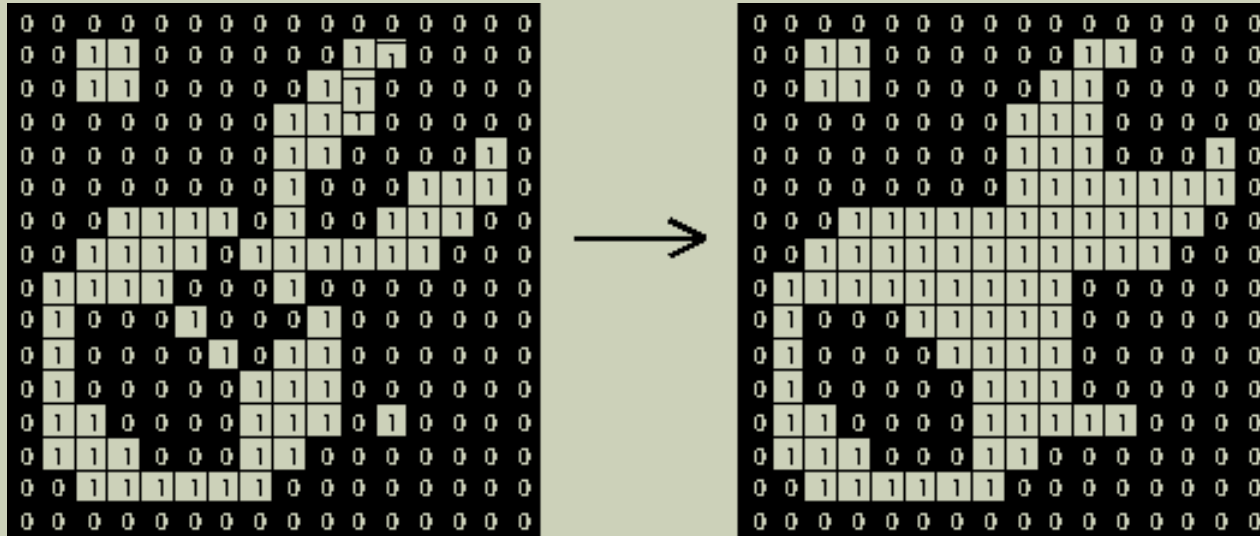
**Segmented Image**



**Closing Result**

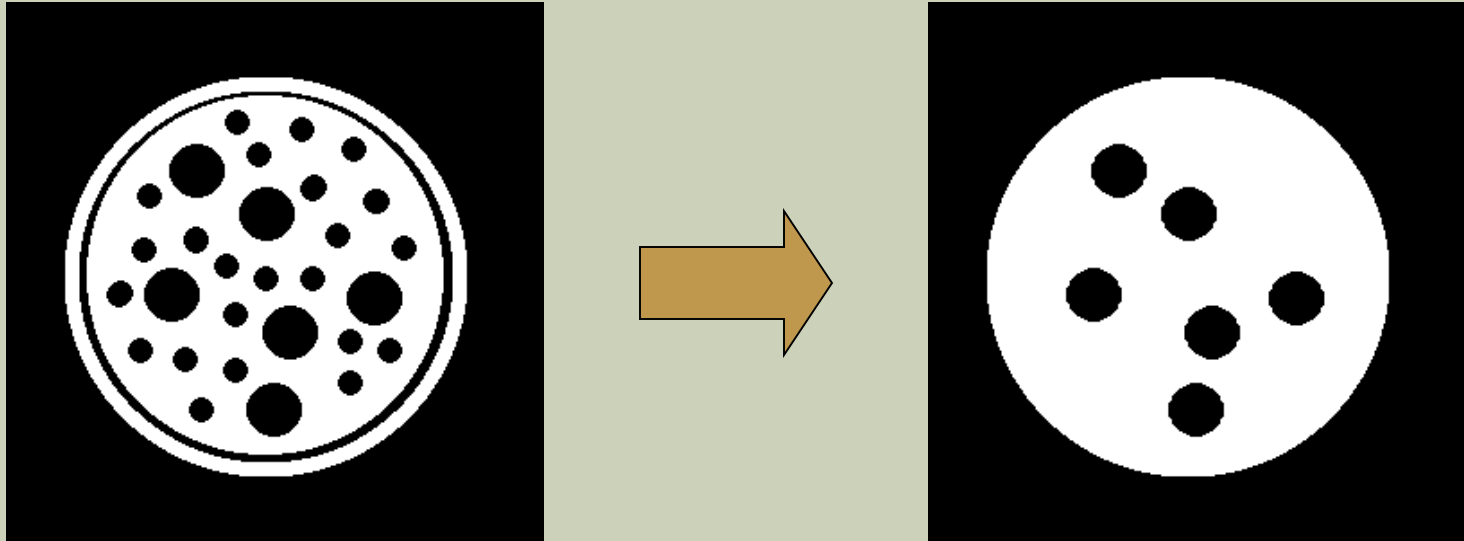
- Closing with disc of size 20

# EXAMPLE OF CLOSING APPLICATIONS



- Structuring element: 3x3 square

# EXAMPLE OF CLOSING APPLICATIONS



- Closing operation with a 22 pixel disc
- Closes small holes in the foreground

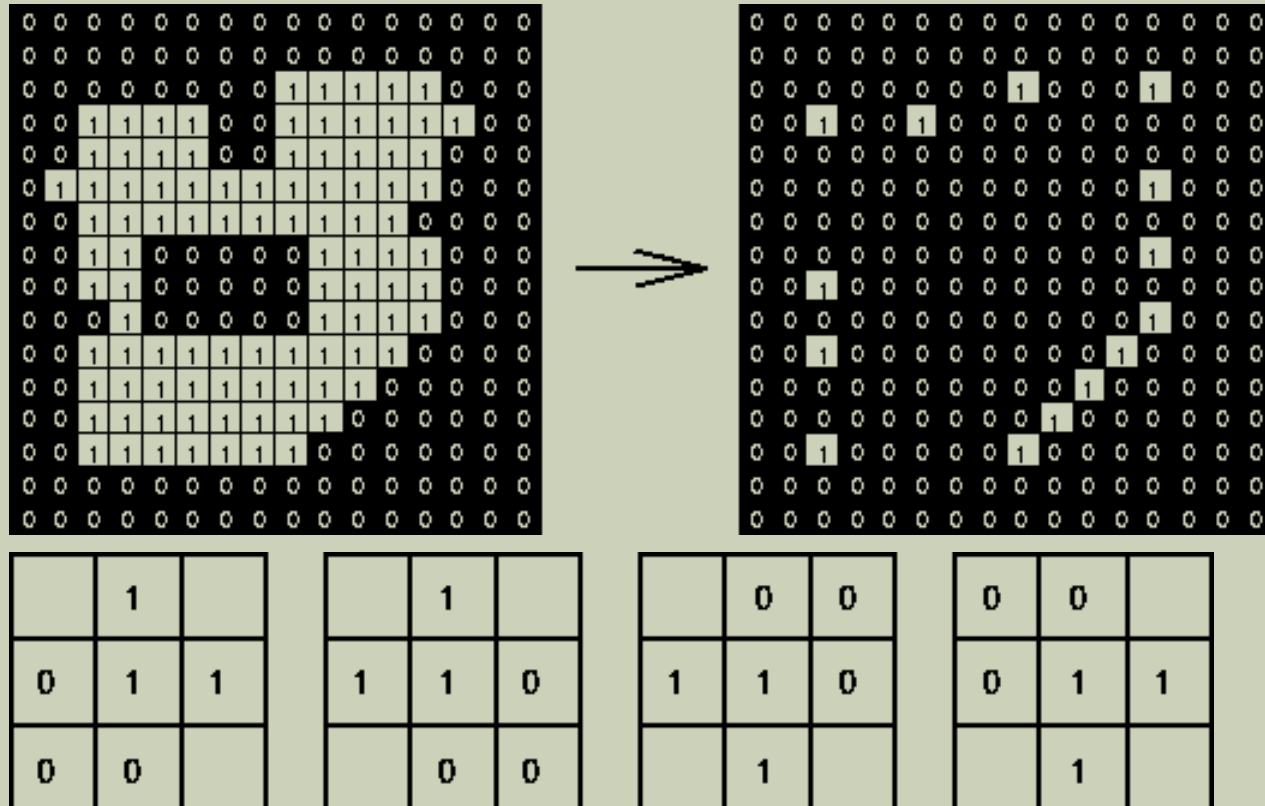
# HIT-MISS OPERATION



# HIT-MISS OPERATION

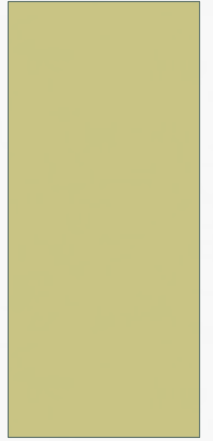
- look for particular patterns of foreground and background pixels
- Very simple object recognition
- Similar to Pattern Matching:
  - If foreground and background pixels in the structuring element *exactly match* foreground and background pixels in the image, then
    - the pixel underneath the origin of the structuring element is set to the foreground color.

# EXAMPLE OF HIT-MISS APPLICATIONS



- **Corner detection with**
  - **Structuring Elements representing four corners**

# THINNING OPERATION

A thick, solid dark grey horizontal bar spanning the width of the text box.

# THINNING OPERATION

- **remove** selected **foreground pixels** from binary images
- After edge detection, lines are often **thicker than one pixel**.
  - **Thinning** can be used to thin those line to **one pixel width**.

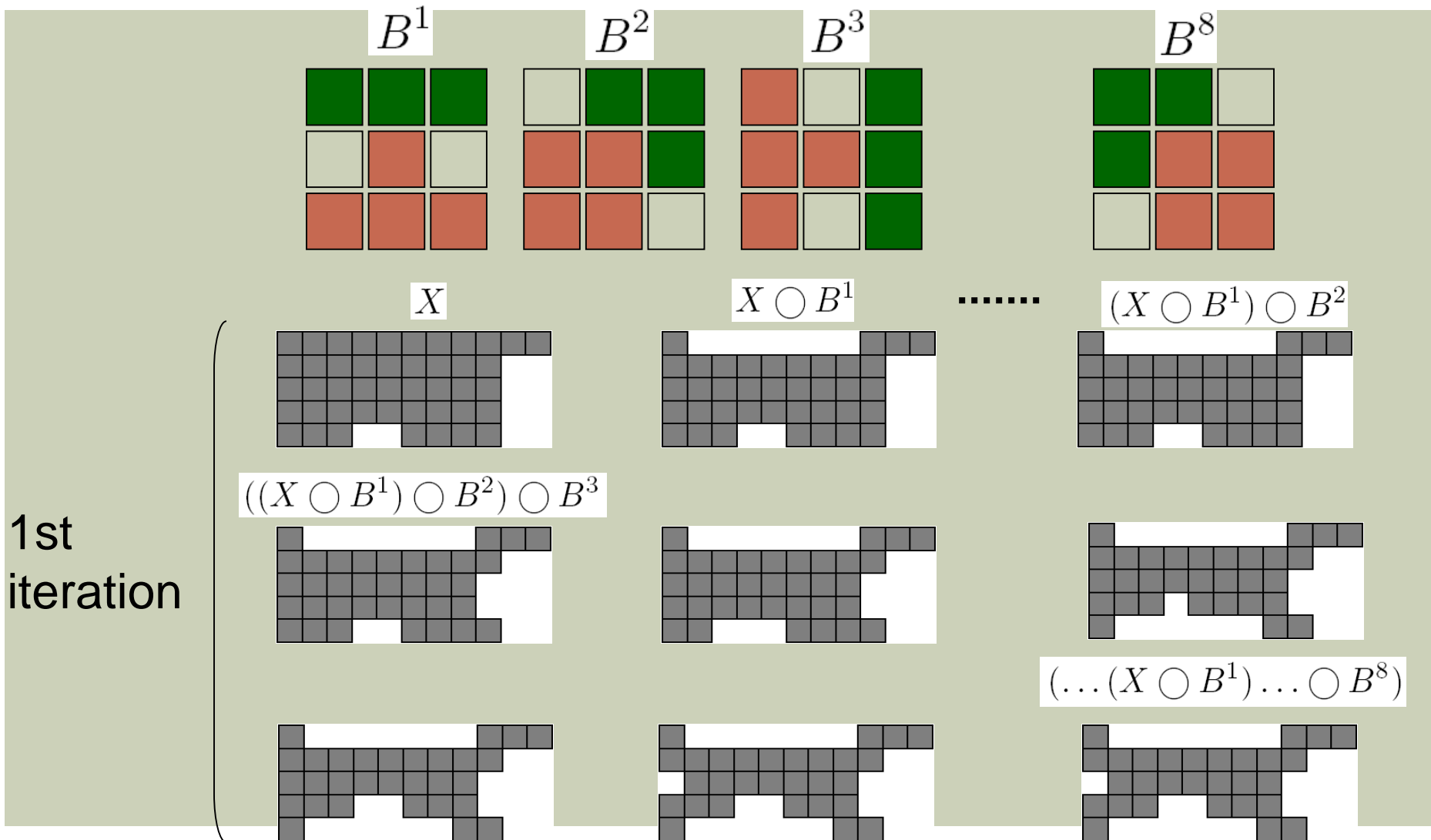
- Let  $K$  be a kernel and  $I$  be an image

$$\text{thin} (I, K) = I - \text{HitAndMiss} (I, K)$$

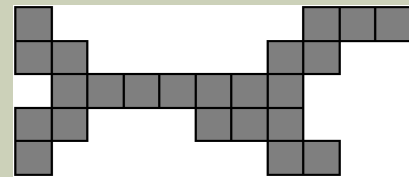
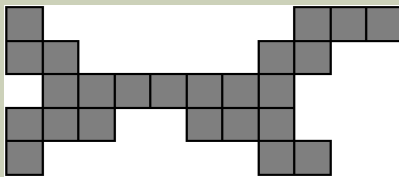
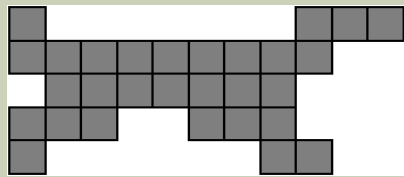
with  $0-1=0!!$

- **If** foreground and background **fit** the structuring element exactly, **then** the pixel at the origin of the SE is set to 0
- Note that the value of the SE at the origin is 1 or *don't care*!

# THINNING OPERATION

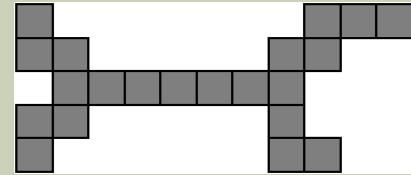
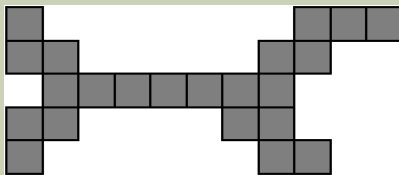


# THINNING OPERATION



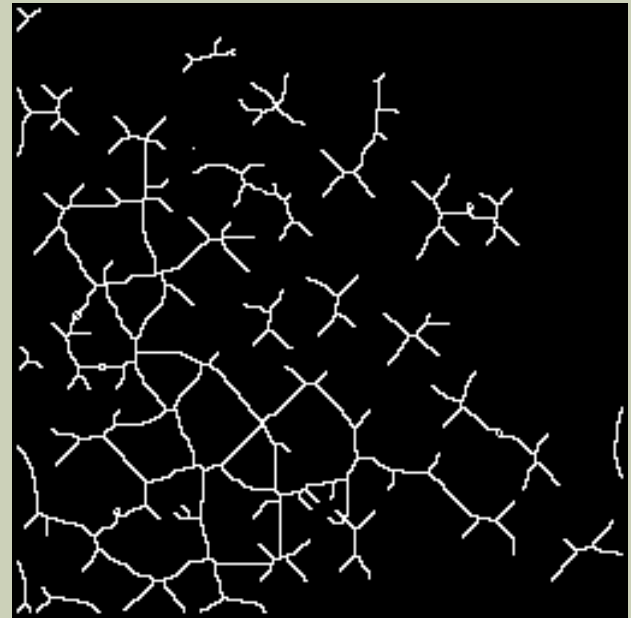
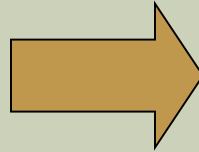
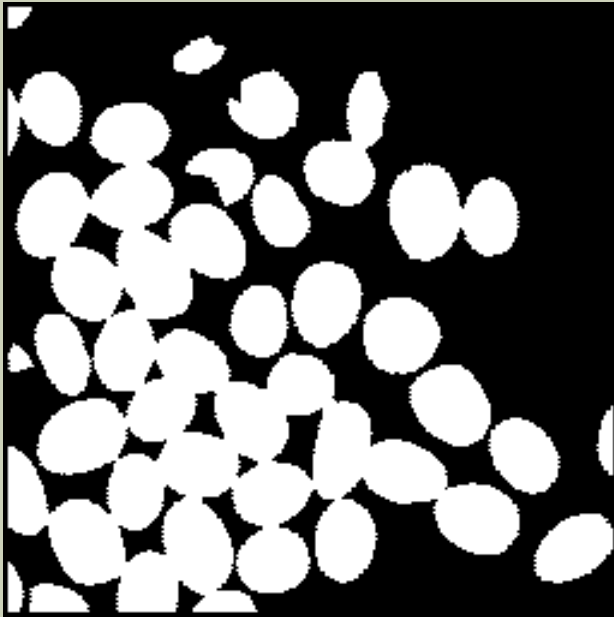
.....

result of  
1st iteration

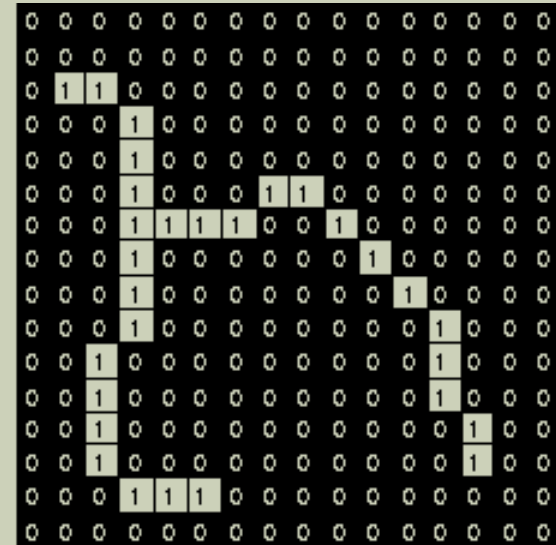
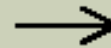
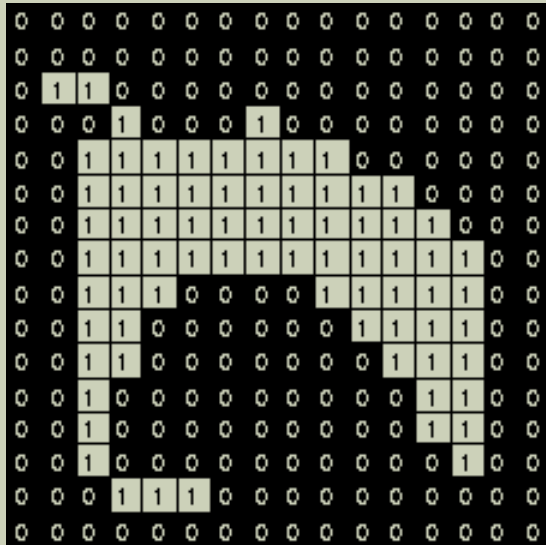


2nd iteration reaches  
idempotence

# THINNING OPERATION



- 20 iterations of thinning color white



|   |   |   |
|---|---|---|
| 0 | 0 | 0 |
|   | 1 |   |
| 1 | 1 | 1 |

|   |   |   |
|---|---|---|
|   | 0 | 0 |
| 1 | 1 | 0 |
|   | 1 |   |

- Corner detection with
  - Structuring Elements representing two corners