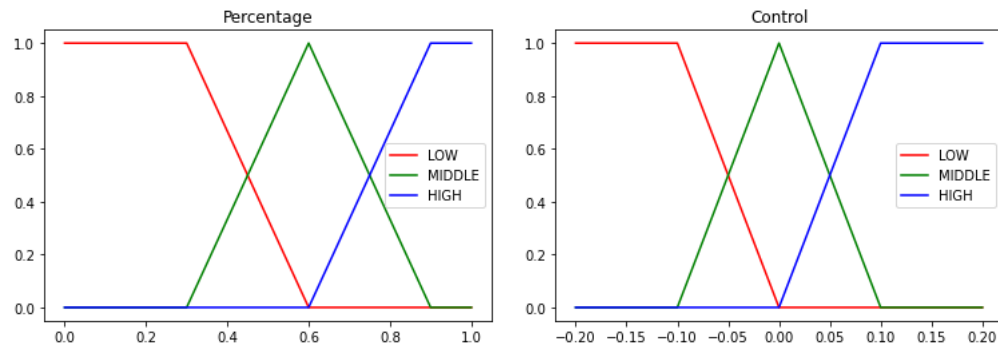


V1

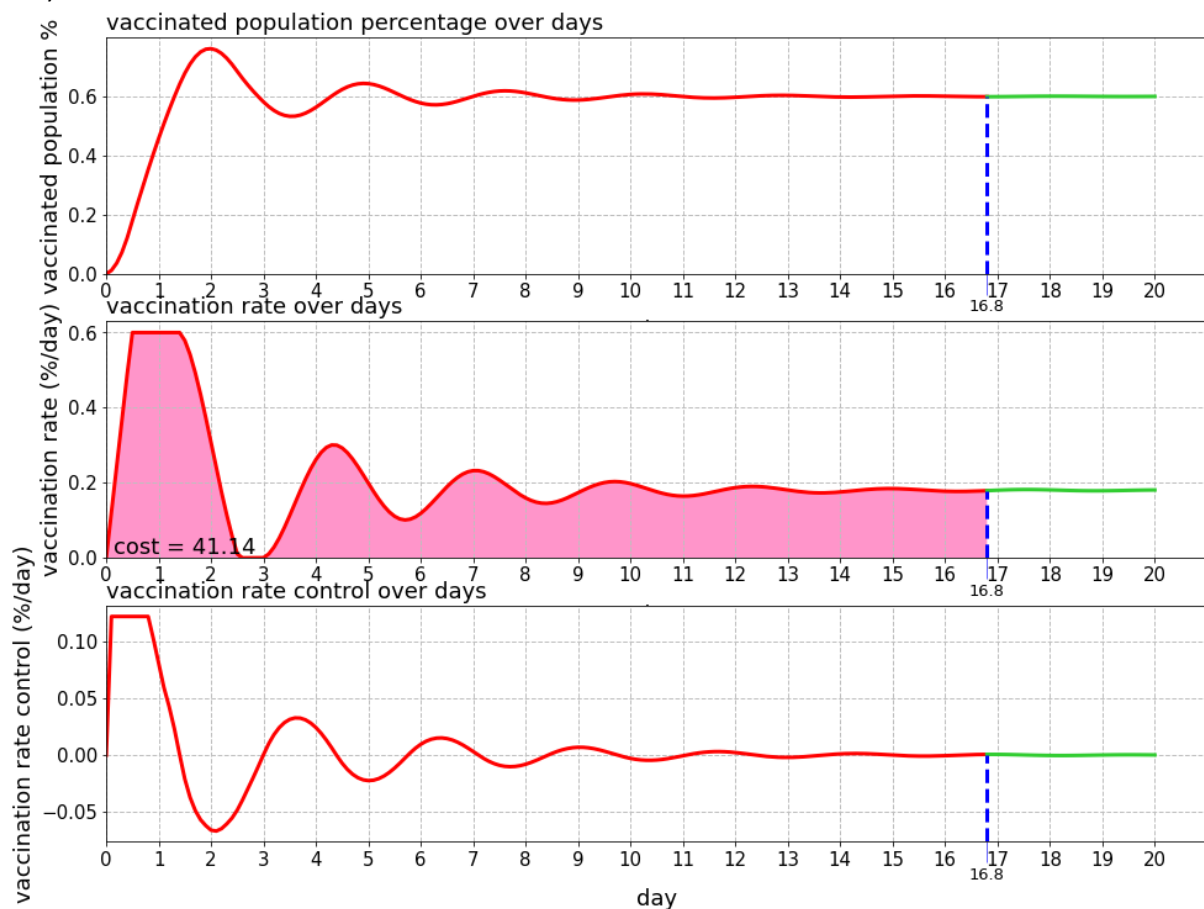
1.1) I created 3 partition for percentage and control.



1.2) Control rules decided on the idea of that if you are giving one of them as high then the other will be low which means if percentage is high then control is low.

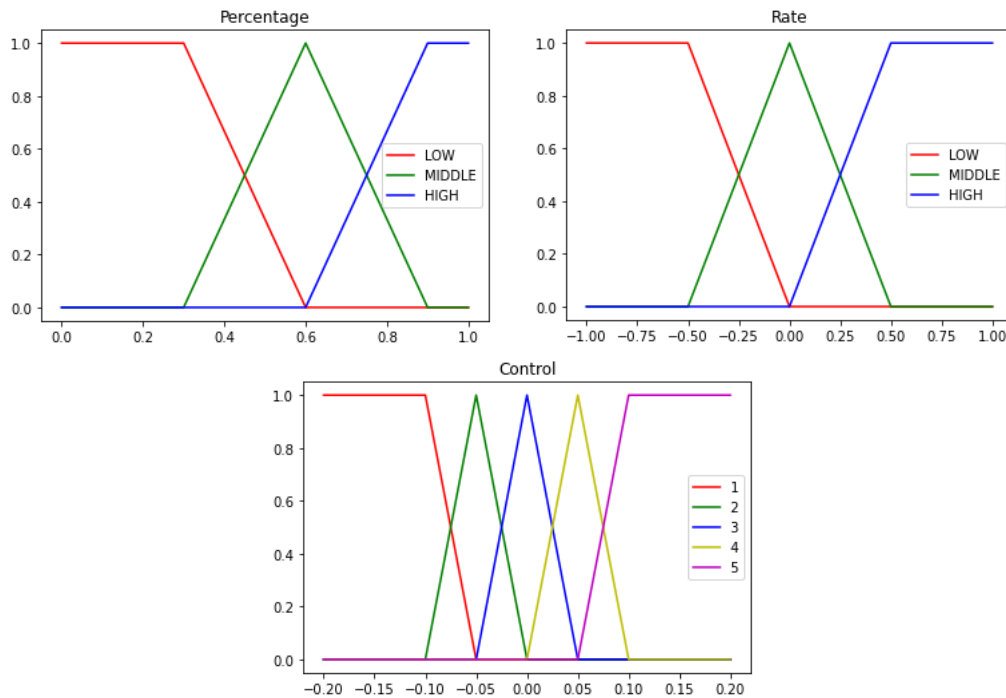
1.3) Fuzzification can be explained as precise data is converted into imprecise data, whereas defuzzification is the conversion of imprecise data to precise data. Defuzzification is the inverse of fuzzification.

1.4)



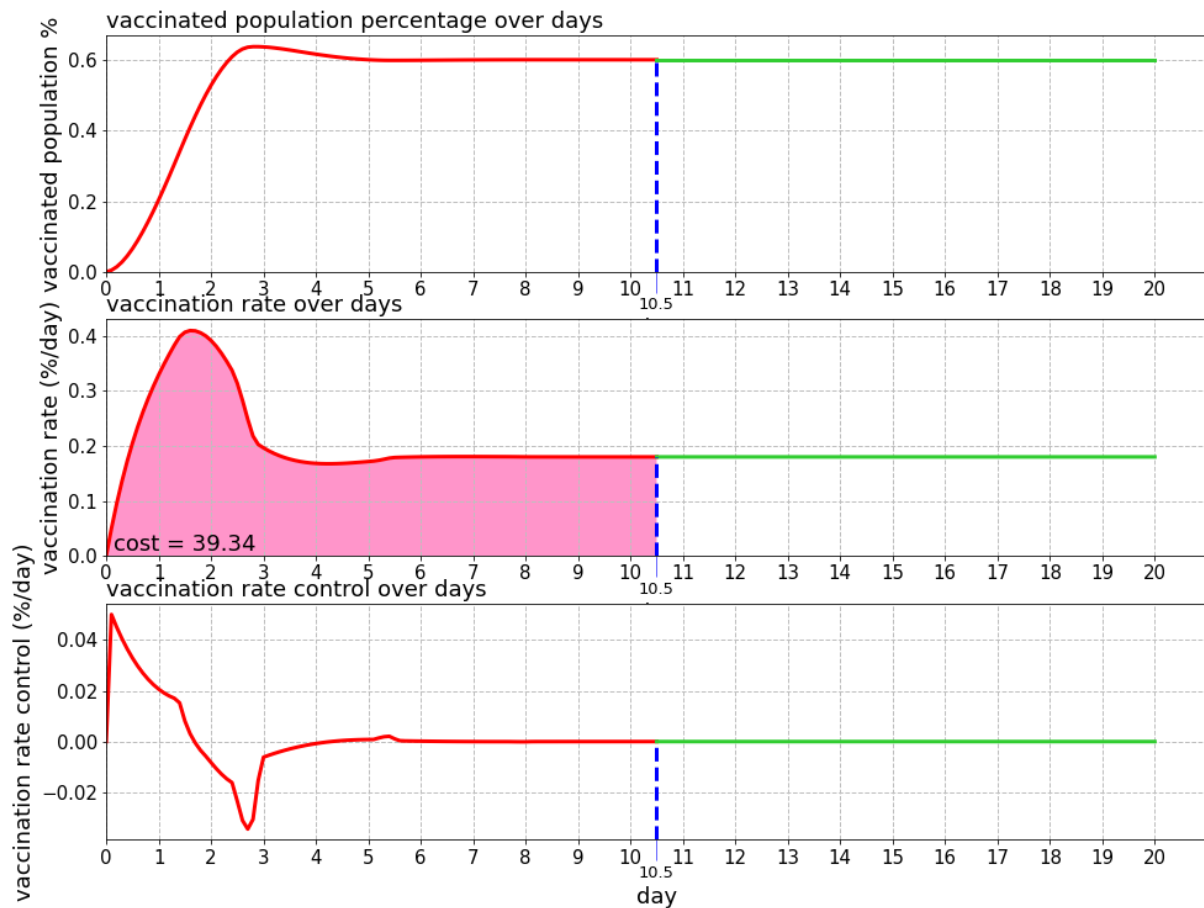
V2

2.1) The percentage and rate partitions are set as in v1. Partition of the output set into 5 fuzzy sets between $[-0.2, 0.2]$ as in the graph.



2.2) Rules are created as to give highest control to the lowest percentage and lowest rate whereas lowest control is given to the highest percentage and highest rate.

2.3)



2.4) Comparing the v_1 and v_2 , in v_2 case of vaccination we have earlier convergence and lower cost. In that sense v_2 is greater choice instead of v_1 . Vaccination rate and vaccination rate control are also more stable in v_2 .

```

1 #!/usr/bin/env python3
2 # -*- coding: utf-8 -*-
3 """
4 Created on Tue Jun  7 20:59:44 2022
5
6 @author: bahadir
7 """
8
9 #%% VACCINATION V1
10 from vaccination import Vaccination
11 import os
12 import numpy as np
13 import matplotlib.pyplot as plt
14 import skfuzzy as fuzzy
15 import skfuzzy.membership as skfm
16
17 def Fuzzy_Model1(current_percent_vacc_people, plot):
18     #set partitioning
19     #creating percentages and control variables
20     #giving 1.1 to see clearly in graph
21     percent_vacc_people = np.arange( 0 , 1.1 , 0.1 )
22     control_variable = np.arange(-0.2,0.21,0.05)
23     #percent low is 1 from 0 and after 0.3-0.6 interval it becomes 0
24     percent_vacc_low = skfm.trapmf(percent_vacc_people, [0, 0, 0.3, 0.6])
25     percent_vacc_mid = skfm.trimf(percent_vacc_people, [0.3, 0.6, 0.9])
26     percent_vacc_high = skfm.trapmf(percent_vacc_people, [0.6, 0.9, 1, 1])
27
28     control_low = skfm.trapmf(control_variable, [-0.20, -0.20, -0.1, 0])
29     control_mid = skfm.trimf(control_variable, [-0.1, 0, 0.1])
30     control_high = skfm.trapmf(control_variable, [0, 0.1, 0.25, 0.25])
31
32     if plot == 199:
33         #plotting
34         plt.plot(percent_vacc_people, percent_vacc_low , 'r')
35         plt.plot(percent_vacc_people, percent_vacc_mid , 'g')
36         plt.plot(percent_vacc_people, percent_vacc_high, 'b')
37         plt.legend(["LOW", "MIDDLE" , "HIGH"])
38         plt.title("Percentage")
39         plt.show()
40         plt.savefig("percetage1.png")
41
42         plt.plot(control_variable, control_low , 'r')
43         plt.plot(control_variable, control_mid , 'g')
44         plt.plot(control_variable, control_high, 'b')
45         plt.legend(["LOW", "MIDDLE" , "HIGH"])
46         plt.title("Control")
47         plt.show()
48         plt.savefig("control1.png")
49
50     #Fuzzyfying
51     percent_fit1 = fuzzy.interp_membership(percent_vacc_people,
52     percent_vacc_low , current_percent_vacc_people)
53     percent_fit2 = fuzzy.interp_membership(percent_vacc_people,
54     percent_vacc_mid , current_percent_vacc_people)
55     percent_fit3 = fuzzy.interp_membership(percent_vacc_people,
56     percent_vacc_high, current_percent_vacc_people)
57
58     #Fuzzy Control Rules--- with low percentage we have higher control or
59     vice versa

```

```

56     control_rule1 = np.fmin(percent_fit1 , control_high)
57     control_rule2 = np.fmin(percent_fit2 , control_mid )
58     control_rule3 = np.fmin(percent_fit3, control_low )
59
60     final_control = np.fmax(control_rule1,control_rule2)
61     final_control = np.fmax(final_control,control_rule3)
62
63     #Defuzzify the control variable and final variable
64     defuzzed = fuzzy.defuzz(control_variable, final_control, 'centroid')
65     return defuzzed
66
67     #start vaccination
68     vaccination = Vaccination()
69     equilibrium_day = 0
70     cost = 0
71     final_cost = 0
72     percent_temp_previous = -5
73     percent_temp_current = 0
74     s=0
75     for i in range (200):
76         percentage , rate = vaccination.checkVaccinationStatus()
77         #Vaccinate people according to the control variable comes from the Fuzzy
78         vaccination.vaccinatePeople(Fuzzy_Model1(percentage,i))
79         cost = cost + vaccination.vaccination_rate_curve[-1]
80
81         if abs(percent_temp_previous -
vaccination.vaccinated_percentage_curve[-1]) < 0.000001 and s==0 :
82             equilibrium_day = i
83             final_cost = cost
84             s=1
85
86         percent_temp_previous = percent_temp_current
87         percent_temp_current = vaccination.vaccinated_percentage_curve[-1]
88
89     vaccination.viewVaccination(equilibrium_day,cost)
90
91     #%% VACCINATION V2
92     from vaccination import Vaccination
93     import os
94     import numpy as np
95     import matplotlib.pyplot as plt
96     import skfuzzy as fuzzy
97     import skfuzzy.membership as skfm
98
99     def Fuzzy_Model2(current_percent_vacc_people,current_rate, plot):
100         #set partitioning
101         #creating percentages and control variables
102         #giving 1.1 to see clearly in graph
103         percent_vacc_people = np.arange( 0 , 1.1 , 0.1 )
104         rate = np.arange(-1, 1.1, 0.1)
105         control_variable = np.arange(-0.2,0.21,0.05)
106         #percent low is 1 from 0 and after 0.3-0.6 interval it becomes 0
107         percent_vacc_low = skfm.trapmf(percent_vacc_people, [0, 0, 0.3, 0.6])
108         percent_vacc_mid = skfm.trimf(percent_vacc_people, [0.3, 0.6, 0.9])
109         percent_vacc_high = skfm.trapmf(percent_vacc_people, [0.6, 0.9, 1, 1])
110
111         rate_low = skfm.trapmf(rate, [-1, -1, -0.5, 0])
112         rate_mid = skfm.trimf(rate, [-0.5, 0, 0.5])
113         rate_high = skfm.trapmf(rate, [0, 0.5, 1, 1])
114

```

```

115 control1 = skfm.trapmf(control_variable, [-0.20, -0.20, -0.1, -0.05])
116 control2 = skfm.trimf(control_variable, [-0.1, -0.05, 0])
117 control3 = skfm.trimf(control_variable, [-0.05, 0, 0.05])
118 control4 = skfm.trimf(control_variable, [0, 0.05, 0.1])
119 control5 = skfm.trapmf(control_variable, [0.05, 0.1, 0.25, 0.25])
120
121
122 if plot == 199:
123     #plotting
124     plt.plot(percent_vacc_people, percent_vacc_low, 'r')
125     plt.plot(percent_vacc_people, percent_vacc_mid, 'g')
126     plt.plot(percent_vacc_people, percent_vacc_high, 'b')
127     plt.legend(["LOW", "MIDDLE", "HIGH"])
128     plt.title("Percentage")
129     plt.show()
130     plt.savefig("percentage2.png")
131
132     plt.plot(rate, rate_low, 'r')
133     plt.plot(rate, rate_mid, 'g')
134     plt.plot(rate, rate_high, 'b')
135     plt.legend(["LOW", "MIDDLE", "HIGH"])
136     plt.title("Rate")
137     plt.show()
138     plt.savefig("rate2.png")
139
140     plt.plot(control_variable, control1, 'r')
141     plt.plot(control_variable, control2, 'g')
142     plt.plot(control_variable, control3, 'b')
143     plt.plot(control_variable, control4, 'y')
144     plt.plot(control_variable, control5, 'm')
145     plt.legend(["1", "2", "3", "4", "5"])
146     plt.title("Control")
147     plt.show()
148     plt.savefig("control2.png")
149
150     #Fuzzyfying
151     percent_fit1 = fuzzy.interp_membership(percent_vacc_people,
percent_vacc_low, current_percent_vacc_people)
152     percent_fit2 = fuzzy.interp_membership(percent_vacc_people,
percent_vacc_mid, current_percent_vacc_people)
153     percent_fit3 = fuzzy.interp_membership(percent_vacc_people,
percent_vacc_high, current_percent_vacc_people)
154
155     rate_fit1 = fuzzy.interp_membership(rate, rate_low, current_rate)
156     rate_fit2 = fuzzy.interp_membership(rate, rate_mid, current_rate)
157     rate_fit3 = fuzzy.interp_membership(rate, rate_high, current_rate)
158
159     #Fuzzy Control Rules--- with low percentage we have higher control or
vice versa
160     control_rule1 = np.fmin(np.fmin(percent_fit1, rate_fit1), control5)
161     control_rule2 =
np.fmin(np.fmax(np.fmin(percent_fit2, rate_fit1), np.fmin(percent_fit1, rate_fit
2))), control4)
162     control_rule3 = np.fmin(np.fmax(np.fmax(np.fmin(percent_fit1, rate_fit3),
np.fmin(percent_fit3, rate_fit1)), np.fmin(percent_fit2,
rate_fit2))), control3)
163     control_rule4 =
np.fmin(np.fmax(np.fmin(percent_fit3, rate_fit2), np.fmin(percent_fit2, rate_fit
3))), control2)
164     control_rule5 = np.fmin(np.fmin(percent_fit3, rate_fit3), control1)

```

```
165
166     final_control =
np.fmax(np.fmax(np.fmax(control_rule1,control_rule2),np.fmax(control_rule3,co
ntrol_rule4)),control_rule5)
167
168     #Defuzzify the control variable and final variable
169     defuzzed = fuzzy.defuzz(control_variable, final_control, 'centroid')
170     return defuzzed
171
172     #start vaccination
173     vaccination = Vaccination()
174     equilibrium_day = -1
175     cost = 0
176     final_cost = 0
177     percent_temp_previous = -5
178     percent_temp_current = 0
179     s=0
180     for i in range (200):
181         percentage , rate = vaccination.checkVaccinationStatus()
182         #Vaccinate people according to the control variable comes from the Fuzzy
183         vaccination.vaccinatePeople(Fuzzy_Model2(percentage,rate,i))
184         cost = cost + vaccination.vaccination_rate_curve_[-1]
185
186         if abs(percent_temp_previous -
vaccination.vaccinated_percentage_curve_[-1]) < 0.000001 and s==0 :
187             equilibrium_day = i
188             final_cost = cost
189             s=1
190
191         percent_temp_previous = percent_temp_current
192         percent_temp_current = vaccination.vaccinated_percentage_curve_[-1]
193
194     vaccination.viewVaccination(equilibrium_day,cost)
195
196
```