Bryan Ngo

Differentia Equations

RC Circuits

ransistors

EECS 16B CSM Drop-In Session

Bryan Ngo

Computer Science Mentors

2021-02-01



Who am I?

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Differentia Equations

RC Circuit

Transistor



- 2nd year majoring in EECS
- took EECS 16B Spring 2020
- How I spent break
 - lots of vidya (Civ VI, Valorant, etc.)
 - built mechanical keyboard

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Differential Equations

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Concept check!

Differential Equations

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Concept check!

$$\frac{d}{dt}x(t) = f(x,t) \tag{1}$$

- Focusing on first-order ODEs
- Relates the derivative in other terms
- 3Blue1Brown video

Exponential Differential Equation

Homogeneous

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$$\frac{d}{dt}x(t) = \lambda x(t) \implies x(t) = x_0 e^{\lambda t}$$
 (2)

Exponential Differential Equation

Non-Homogeneous

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$$\frac{d}{dt}x(t) = \alpha x(t) + \beta \tag{3}$$

$$\frac{d}{dt}x(t) = \alpha \left(x(t) + \frac{\beta}{\alpha}\right) \tag{4}$$

$$\int \frac{1}{x(t) + \frac{\beta}{\alpha}} dx(t) = \int \alpha dt$$
 (5)

$$\ln\left|x(t) + \frac{\beta}{\alpha}\right| = \alpha t + C \tag{6}$$

$$\Rightarrow x(t) = -\frac{\beta}{\alpha} + Ce^{\alpha t} \tag{7}$$

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Undamped Response

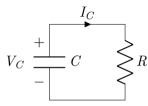
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Undamped Response

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$$V_C \stackrel{+}{=} C \stackrel{I_C}{=} I$$

$$C\frac{d}{dt}V_C = -\frac{V_C}{R}$$

$$\frac{d}{dt}V_C = -\frac{V_C}{R} \tag{8}$$

$$\frac{d}{dt}V_C = \underbrace{-\frac{1}{RC}}_{\lambda}V_C$$

$$\Rightarrow V_C(t) = V_0 e^{-\frac{1}{RC}t} = V_0 e^{-\frac{1}{\tau}t}$$
 (10)



(9)

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Transistors

NMOS & PMOS

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