EECS 16A HW06

Bryan Ngo

2019-10-12

1 Elementary Matrices

1.a

1.a.i

$$\mathbf{E}_1 = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 1 & 0 & 0 \\ 1 & 0 & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \tag{1}$$

1.a.ii

$$\mathbf{E}_2 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -5 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \tag{2}$$

1.a.iii

$$\mathbf{E}_3 = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 3 & 0 & 1 \end{bmatrix} \tag{3}$$

1.a.iv

$$\mathbf{E}_4 = \begin{bmatrix} 1 & -1 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \tag{4}$$

The composite of the above matrix followed by the previous problem is

$$\mathbf{E}_{3}\mathbf{E}_{4} = \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 3 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & -1 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} = \begin{bmatrix} 1 & -1 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 3 & 0 & 1 \end{bmatrix}$$
 (5)

1.b

 \mathbf{E}_1 makes sense as the negative of r_1 is moved down to r_4 . \mathbf{E}_2 makes sense as r_2 is multiplied by 2 and its negative is moved down to r_3 . \mathbf{E}_3 makes sense as r_3 is moved up to r_4 and all of r_3 is multiplied by -1. Finally, \mathbf{E}_4 makes sense as r_4 is multiplied by 6 and its negative is moved up to r_3 , then $-5r_4$ is moved up to r_1 , before r_4 is multiplied by -1.

Verifying the matrix multiplication,

$$\mathbf{E}_{4}\mathbf{E}_{3}\mathbf{E}_{2}\mathbf{E}_{1} = \begin{pmatrix} \begin{bmatrix} 1 & 0 & 0 & -5 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & -6 \\ 0 & 0 & 0 & -1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & -1 & 0 \\ 0 & 0 & 1 & 1 \end{bmatrix} \end{pmatrix} \begin{pmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & -2 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ -1 & 0 & 0 & 1 \end{bmatrix} \end{pmatrix}$$

$$(6)$$

$$\begin{bmatrix}
1 & 0 & -5 & -5 \\
0 & 1 & 0 & 0 \\
0 & 0 & -7 & -6 \\
0 & 0 & -1 & -1
\end{bmatrix}
\begin{bmatrix}
1 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 \\
0 & -2 & 1 & 0 \\
-1 & 0 & 0 & 1
\end{bmatrix}$$

$$= \begin{bmatrix}
6 & 10 & -5 & -5 \\
0 & 1 & 0 & 0 \\
6 & 14 & -7 & -6 \\
1 & 2 & -1 & -1
\end{bmatrix}$$
(8)

$$= \begin{bmatrix} 6 & 10 & -5 & -5 \\ 0 & 1 & 0 & 0 \\ 6 & 14 & -7 & -6 \\ 1 & 2 & -1 & -1 \end{bmatrix}$$
 (8)

Multiplying **EA**,

$$\mathbf{EA} = \begin{bmatrix} 6 & 10 & -5 & -5 \\ 0 & 1 & 0 & 0 \\ 6 & 14 & -7 & -6 \\ 1 & 2 & -1 & -1 \end{bmatrix} \begin{bmatrix} 1 & 0 & 0 & -5 & | & 15 \\ 0 & 1 & 0 & 0 & | & -7 \\ 0 & 2 & -1 & 6 & | & 3 \\ 1 & 0 & 1 & -12 & | & -5 \end{bmatrix} = \begin{bmatrix} 1 & 0 & 0 & 0 & | & 30 \\ 0 & 1 & 0 & 0 & | & -7 \\ 0 & 0 & 1 & 0 & | & 1 \\ 0 & 0 & 0 & 1 & | & 3 \end{bmatrix}$$

$$(9)$$

Homework Process and Study Group $\mathbf{2}$

I did this homework by myself.