

EE 120 Midterm 1 Review Session

Presented by <NAMES >(HKN)

Disclaimer

This is an unofficial review session and HKN is not affiliated with this course. Although some of the presenters may be course staff, the material covered in the review session may not be an accurate representation of the topics covered in and difficulty of the exam.

If you want to follow along: head to <Slides location and/or link >

Slides are also posted at @# on Piazza.

This is licensed under the Creative Commons CC BY-SA: feel free to share and edit, as long as you credit us and keep the license. For more information, visit <https://creativecommons.org/licenses/by-sa/4.0/>

HKN Drop-In Tutoring

- HKN has office hours every weekday from **11 AM - 3 PM** and **8 PM - 10 PM** on hkn.mu/ohqueue
- The schedule of tutors can be found at hkn.mu/tutor
<Itemize the presenter hours here >

Basic Signals

Complex Signals

- A complex-valued signal can be represented as

$$x(t) = x_r(t) + jx_i(t) = a(t)e^{j\Theta(t)}$$

- With amplitude and phase

$$a(t) = \sqrt{x_r(t)^2 + x_i(t)^2}$$

$$\cos(\Theta(t)) = \frac{x_r(t)}{a(t)}; \sin(\Theta(t)) = \frac{x_i(t)}{a(t)}$$

$$\Theta(t) = \arctan\left(\frac{\sin(\Theta(t))}{\cos(\Theta(t))}\right)$$

Euler's Formula and Complex Exponentials

- Euler's Formula is

$$e^{j\omega t} = \cos(\omega t) + j \sin(\omega t)$$

- A complex exponential has magnitude 1.

$$|e^{4+3j}| = |e^4 e^{3j}| = e^4$$

Signal Transformations

- Signal shifting: shifts signal to the right if $T > 0$, left if $T < 0$

$$x(t) \rightarrow x(t - T), x[n] \rightarrow x[n - T]$$

- Signal reversal: reflects signal

$$x(t) \rightarrow x(-t), x[n] \rightarrow x[-n]$$

- Even function

$$x(t) = x(-t), x_{\text{even}}(t) = \frac{x(t) + x(-t)}{2}$$

- Odd function

$$x(t) = -x(-t), x_{\text{odd}}(t) = \frac{x(t) - x(-t)}{2}$$

Signal Periodicity

- Continuous time signal is periodic if there exists a nonzero $T \in \mathbb{R}$ such that

$$x(t + T) = x(t)$$

- The smallest positive choice of T is the fundamental period of $x(t)$
- Discrete time signal is periodic if there exists a nonzero $N \in \mathbb{Z}$ such that

$$x[n] = x[n + N]$$

- The smallest positive choice of the integer N is the fundamental period of $x[n]$

Delta Function

- Dirac delta function: continuous time

$$\delta(t) = \begin{cases} \infty, & t = 0 \\ 0, & t \neq 0 \end{cases}$$

$$\delta(t - \tau) = 0, t \neq \tau$$

$$\int_{-\infty}^{\infty} \delta(t - \tau) dt = 1$$

- Delta scaling and sifting properties

$$\delta(at) = \frac{\delta(t)}{|a|}, \int_{-\infty}^{\infty} \delta(t - \tau) f(t) dt = f(\tau)$$

- Kronecker delta function: discrete time

$$\delta[n] = \begin{cases} 1, & n = 0 \\ 0, & n \neq 0 \end{cases}$$

System Properties

System Property Definitions

Linearity

- **Scaling** an input by some amount scales the output by the same amount
- **Superposition** of two inputs generates a superposition of two outputs

Time-Invariance

- A time invariant system means that a shift in time in the input results in the same shift in time in the output

System Property Definitions

Memoryless

- A memoryless system is one where the present output only depends on the present input

$$y(t) = 5x(t)✓$$

$$y[n] = x[n] + x[n - 2] + x[n + 1]✗$$

Causality

- A system is causal if the present output depends on only the current and past inputs.

$$y(t) = x(t) - 2x(t - 0.5)✓$$

$$y[n] = x[n] - x[n + 2]✗$$

- An LTI system is causal iff

$$h(t) = 0, \forall t < 0, h[n] = 0, \forall n < 0$$

System Property Definitions

BIBO Stability

- A system is BIBO stable if every bounded input produces a bounded output
- A bounded input is one such that

$$\max_t |x(t)| < \infty, \max_n |x[n]| < \infty$$

- An **LTI** system is BIBO stable iff its impulse response is absolutely integrable/summable

$$\int_{-\infty}^{\infty} |h(t)| dt < \infty$$

$$\sum_{n=-\infty}^{\infty} |h[n]| < \infty$$

DT LTI Systems

Discrete Signals and Systems

- A discrete signal is described by a function

$$x : \mathbb{Z} \rightarrow \mathbb{R}$$

- A delta function is the unit impulse and any signal can be decomposed into a sum of deltas

$$\delta[n] = \begin{cases} 1 & n = 0 \\ 0 & n \neq 0 \end{cases}$$

$$x[n] = \sum_{k=-\infty}^{\infty} x[k] \delta[n - k] \forall x$$

- A discrete system, H , takes an input signal, x , and yields an output signal, y

Linear and Time-Invariant Systems

Linearity

- **Scaling** an input by some amount scales the output by the same amount

$$\alpha x_1[n] \xrightarrow{H} \alpha y_1[n]$$

- **Superposition** of two inputs generates a superposition of two outputs

$$x_1[n] + x_2[n] \xrightarrow{H} y_1[n] + y_2[n]$$

Time-Invariance

- A time invariant system means that a shift in time in the input results in the same shift in time in the output

$$x_1[n - N] \xrightarrow{H} y_1[n - N] \quad \forall N \in \mathbb{Z}$$

Impulse Response

- The impulse response is the output of a system for a $\delta[n]$ input

$$x[n] = \delta[n] \xrightarrow{H} y[n] = h[n]$$

Verify that knowing $h[n]$ allows you to determine the output $y[n]$ for any input in an LTI system. *Hint: decompose $x[n]$*

Proof and the Convolutional Sum

Proof Decompose $x[n]$

$$x[n] = \sum_k x[k] \delta[n - k]$$

Recall the definition of the impulse response

$$\delta[n] \xrightarrow{H} h[n]$$

Apply linearity and time-invariance to the definition of the impulse response

$$\sum_k x[k] \delta[n - k] \xrightarrow{H} \sum_k x[k] h[n - k]$$

Convolution

- This is the convolutional sum, and denoted by $(x * h)[n]$
- Note: $(x * h)[n] = (h * x)[n]$

Determine if the system described by the input-output relationship is 1) linear and 2) time-invariant. *Credit: Discussion #1 EE120 Sp21*

1. $y[n] = 7x[n + 1]$

2. $y[n] = x[n]x[n - 1]$

3. $y[n] = e^{x[n]}$

4. $y[n] = x[-n]$

5. $y[n] = v[n]x[n]$, where v is some fixed signal

LTI Example Solutions

1. $y[n] = 7x[n + 1]$
 - Linear: **Yes**
 - Time-invariant: **Yes**
2. $y[n] = x[n]x[n - 1]$
 - Linear: **No**, any scaling factor becomes squared at the output
 - Time-invariant: **Yes**
3. $y[n] = e^{x[n]}$
 - Linear: **No**, exponentials are non-linear (verify at $n = 0$)
 - Time-invariant: **Yes**
4. $y[n] = x[-n]$
 - Linear: **Yes**
 - Time-invariant: **No**, $\delta[n - 1]$ input results in $\delta[-n - 1]$
5. $y[n] = v[n]x[n]$, where v is some fixed signal
 - Linear: **Yes**
 - Time-invariant: **No**, consider when $v[n] = \delta[n]$ for $x[n]$ and $\tilde{x}[n] = x[n - 1]$; $y[0] = x[0]$ and $y[0] = x[-1]$

DT System Example Problem

Consider the *linear* DT system H

$$\delta[n - k] \xrightarrow{H} h_k[n] = \alpha^{|k|} u[n - k] \quad \forall |\alpha| < 1$$

Show that the output, $y[n]$, to a general input, $x[n]$ is

$$y[n] = \sum_{k=-\infty}^{+\infty} x[k] h_k[n]$$

Credit: Midterm #1 EE120 Sp20

DT System Example Solution

Decompose $x[n]$

$$x[n] = \sum_{m=-\infty}^{+\infty} x[m]\delta[n-m]$$

Recall the definition of the system H

$$\delta[n-m] \xrightarrow{H} h_m[n]$$

Apply linearity

$$x[n] = \sum_{m=-\infty}^{+\infty} x[m]\delta[n-m] \xrightarrow{H} \sum_{m=-\infty}^{+\infty} x[m]h_m[n] = y[n]$$

Notice the differences in this sum from the usual convolutional sum.

DT System Example Problem Continued

Derive a closed-form expression (no summations) for the output $y[n]$ when the input $x[n] = u[n]$, the unit step

Recall:

$$h_k[n] = \alpha^{|k|} u[n - k] \quad \forall |\alpha| < 1$$

$$y[n] = \sum_{k=-\infty}^{+\infty} x[k] h_k[n]$$

$$\sum_{k=M}^N \alpha^k = \begin{cases} \frac{\alpha^{N+1} - \alpha^M}{\alpha - 1} & \alpha \neq 1 \\ N - M + 1 & \alpha = 1 \end{cases}$$

DT System Example Solution

$$y[n] = \sum_{k=-\infty}^{+\infty} x[k]h_k[n]$$

Change the bounds and plug in for $x[k]$ and $h_k[n]$

$$y[n] = \sum_{k=0}^{+\infty} 1 \cdot \alpha^{|k|} u[n-k]$$

$$y[n] = u[n] + \alpha u[n-1] + \alpha^2 u[n-2] + \dots$$

$$y[0] = 1$$

$$y[1] = 1 + \alpha$$

$$y[2] = 1 + \alpha + \alpha^2$$

$$y[n] = \sum_{p=0}^n \alpha^p = \frac{\alpha^{n+1} - 1}{\alpha - 1}$$

Convolution and Cross-Correlation

Convolution

- Convolution is a mathematical operation that takes in two signals, and outputs a third signal as the result of flipping one function and "shifting" it over the other.
- Convolution is important because it allows us to determine the output of an LTI system given its provided input and its impulse response.

$$f[n] * g[n] = \sum_{k=-\infty}^{\infty} f[k] \cdot g[n - k]$$

$$f(t) * g(t) = \int_{-\infty}^{\infty} f(\tau) \cdot g(t - \tau) d\tau$$

Useful Things to Know About Convolution

- It is commutative in both DT and CT; $x * y = y * x$
- $x[n] * \alpha \delta[n - N] = \alpha x[n - N]$ (and likewise for CT)
- Convolution between two same-size rectangles gives a triangle
- Convolution between two different size rectangles gives a trapezoid

Graphical Interpretation of Convolution (CT)

- In the formula, the function with the $t - \tau$ input is being flipped and shifted over the other one.

$$f(t) * g(t) = \int_{-\infty}^{\infty} f(\tau) \cdot g(t - \tau) d\tau$$

- In CT, when drawing the signals being convolved, make sure to remember to graph them on the **tau** (τ) axis, not on the time axis – we are integrating with respect to $d\tau$ here! The output signal will be drawn on the standard time axis.
- With DT, draw the operands on the k axis, and the output on the n axis.

Convolution Practice

Determine the length of $x * y$ if:

- They are DT, with $x[n]$ of length 4 and $y[n]$ of length 5
- They are CT, with $x(t)$ of length 4 and $y(t)$ of length 5

Determine the length of $x * y$ if:

- They are DT, with $x[n]$ of length 4 and $y[n]$ of length 5
 - 8. For DT signals, convolution of a length N and M signal results in a length $N+M-1$ signal.
- They are CT, with $x(t)$ of length 4 and $y(t)$ of length 5
 - 9. For CT signals, convolution of a length N and M signal just results in a length $N+M$ signal.

Convolution Practice

Convolve $x * y$ if:

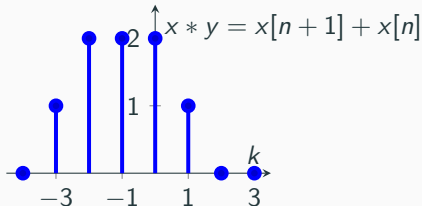
- $x[n] = u[n + 2] - u[n - 2]$ and $y[n] = u[n + 1] - u[n - 1]$.
- $x(t) = 1$ and $y[t] = 2(u(t + 2) - u(t - 2))$

Try doing these with as little math as possible.

Convolution Practice

Convolve $x * y$ if:

- $x[n] = u[n + 2] - u[n - 2]$ and $y[n] = u[n + 1] - u[n - 1]$.
 - $x[n] * y[n] = x[n] * (\delta[n + 1] + \delta[n]) = x[n + 1] + x[n]$



- $x(t) = 1$ and $y[t] = 2(u(t + 2) - u(t - 2))$
 - This is convolving a horizontal line of height 1 with a rectangle of height 2 and width 4. The "overlap" is always going to have area 8 $\Rightarrow x(t) * y(t) = 8$

Cross-Correlation

- Cross-correlation is a similar operation to convolution, that also involved a shift and sum of two signals.
- It's not *exactly* convolution!
 - Not commutative
 - Signal is not flipped before shifting! Is directly shifted.

$$R_{f,g}[n] = \sum_{k=-\infty}^{\infty} f[k] \cdot g[n+k]$$

$$R_{f,g}(t) = \int_{-\infty}^{\infty} f(\tau) \cdot g(t+\tau) d\tau$$

Cross-Correlation Practice

Prove that cross-correlation is not commutative. More specifically, prove that $R_{x,y}[n] = R_{y,x}[-n]$, where

$$R_{x,y}[n] = \sum_{k=-\infty}^{\infty} x[k] \cdot y[n+k].$$

Cross-Correlation Practice

Prove that cross-correlation is not commutative. More specifically, prove that $R_{x,y}[n] = R_{y,x}[-n]$, where

$$R_{x,y}[n] = \sum_{k=-\infty}^{\infty} x[k] \cdot y[n+k].$$

$$\begin{aligned} R_{x,y}[n] &= \sum_{k=-\infty}^{\infty} x[k] \cdot y[n+k] = \sum_{w=-\infty}^{\infty} x[w-n] \cdot y[w] = \\ &= \sum_{w=-\infty}^{\infty} y[w] \cdot x[w-n] = R_{y,x}[-n] \end{aligned}$$

LCCDE

Linear Constant-Coefficient Difference Equations

- Discrete LTI systems can be described by LCCDEs in the following form

$$\sum_{k=0}^N a_k y[n-k] = \sum_{L=0}^M b_L x[n-L]$$

- Taking the frequency response of both sides and applying linearity and time-shifting properties results in

$$Y(\omega) \sum_{k=0}^N a_k e^{-j\omega k} = X(\omega) \sum_{L=0}^M b_L e^{-j\omega L}$$

$$H(\omega) = \frac{Y(\omega)}{X(\omega)} = \frac{\sum_{L=0}^M b_L e^{-j\omega L}}{\sum_{k=0}^N a_k e^{-j\omega k}}$$

Linear Constant-Coefficient Differential Equations

- LCCDEs for CT LTI systems have the following equations

$$\sum_{n=0}^N a_n \frac{d^n}{dt^n} y(t) = \sum_{m=0}^M b_m \frac{d^m}{dt^m} x(t)$$

$$H(\omega) = \frac{\sum_{m=0}^M b_m (j\omega)^m}{\sum_{n=0}^N a_n (j\omega)^n}$$

Linear Constant-Coefficient Differential Equations

- The homogeneous solution is found for input $x(t) = 0$

$$\sum_{n=0}^N a_n \frac{d^n}{dt^n} y(t) = 0$$

- The particular solution is found for the given input $x(t)$
- The overall solution is the sum of the homogeneous and particular solutions

$$y(t) = y_p(t) + y_n(t)$$

Practice: First-order RC circuit

- The continuous-time LCCDE for an RC circuit with input $x(t) = u(t)$, initially at rest is

$$\frac{dy(t)}{dt} + ay(t) = kx(t) = ku(t)$$

Find the homogenous, particular, and general solutions to this equation

Practice: First-order RC circuit

- Homogenous solution

$$\frac{dy_h(t)}{dt} + ay_h(t) = 0$$

$$\frac{dy_h(t)}{dt} = -ay_h(t)$$

- Integrate both sides:

$$\int \frac{dy_h(t)}{y_h(t)} = \int -a dt$$

$$\ln(y_h(t)) = -at + c$$

$$y_h(t) = e^{-at+c} = e^c e^{-at} = Ae^{-at}$$

- Review Lecture 03 notes for walkthrough of Particular and General solutions

Frequency Response

Frequency Response

- The frequency response, α , can be defined as

$$H(e^{j\omega n}) = \sum_n h[n]e^{-j\omega n}$$

- The magnitude response can be written in polar form in terms of the magnitude and phase

$$H(e^{j\omega n}) = |H(e^{j\omega n})|e^{\angle H(e^{j\omega n})}$$

- The frequency response is 2π periodic (Can you show this?)

Fourier Transforms

Continuous Time Fourier Transform

- Given a continuous-time signal $x(t)$, you can apply the **Continuous Time Fourier Transform (CTFT)** to find its **spectrum**, $X(\omega)$.
- $X(\omega)$ is also known as the **frequency domain representation** of $x(t)$.
- The CTFT (sometimes known as the **CTFT analysis equation**) can be written as follows:

$$X(\omega) = \int_{-\infty}^{\infty} x(t)e^{-i\omega t} dt.$$

CTFT (Continued)

- Given the spectrum of a signal, you can find the time-domain representation using the inverse CTFT (also known as the **CTFT synthesis equation**):

$$x(t) = \frac{1}{2\pi} \int_{-\infty}^{\infty} X(\omega) e^{i\omega t} d\omega.$$

- If $h(t)$ is the impulse response of LTI system \mathcal{H} , the CTFT of $h(t)$, $H(\omega)$ is known as the **frequency response** of \mathcal{H} .
 - For any input signal of the form $x(t) = e^{i\omega t}$, the output of the system will be $y(t) = H(\omega)x(t)$.
 - We sometimes call such an $x(t)$ an **eigenfunction** of \mathcal{H} .

CTFT (Continued)

- You can only use the CTFT analysis equation if $x(t)$ is absolutely integrable, i.e.

$$\int_{-\infty}^{\infty} |x(t)| dt < \infty.$$

- For signals that are not absolutely integrable but have a CTFT representation, you can find the spectrum using other methods.
 - For periodic signals, you can calculate the CTFS and convert from the CTFS to the CTFT.
 - Later on, you will learn about properties of Fourier Transforms you can utilize.

Practice: CTFT

1. Find the CTFT of the signal $x(t) = e^t(u(t+3) - u(t-3))$.
2. Given that the CTFT of $y(t)$ is $Y(\omega) = \delta(\omega - \pi)$, find $y(t)$.

Practice: CTFT (Solutions)

1. $X(\omega) = \frac{2i}{1-i\omega} \sin(3-3i\omega).$

$$\begin{aligned} X(\omega) &= \int_{-\infty}^{\infty} x(t) e^{-i\omega t} dt &&= \int_{-3}^3 e^t e^{-i\omega t} dt \\ &= \int_{-3}^3 e^{(1-i\omega)t} dt &&= \frac{1}{1-i\omega} e^{1-i\omega t} \Big|_{-3}^3 \\ &= \frac{1}{1-i\omega} (e^{3-3i\omega} - e^{-(3-3i\omega)}) = \frac{2i}{1-i\omega} \sin(3-3i\omega). \end{aligned}$$

2. $y(t) = e^{i\pi t}.$

Practice: CTFT (Solutions)

1. $X(\omega) = \frac{2i}{1-i\omega} \sin(3 - 3i\omega)$.
2. $y(t) = e^{i\pi t}$.

$$\begin{aligned} y(t) &= \frac{1}{2\pi} \int_{-\infty}^{\infty} Y(\omega) e^{i\omega t} d\omega = \frac{1}{2\pi} \int_{-\infty}^{\infty} \delta(\omega - \pi) e^{i\omega t} d\omega \\ &= \frac{1}{2\pi} \int_{-\infty}^{\infty} \delta(\omega - \pi) e^{i\pi t} d\omega = \frac{1}{2\pi} e^{i\pi t}. \end{aligned}$$

Continuous Time Fourier Series

- For periodic continuous-time signals (where $x(t) = x(t + T), \forall t$), we can represent $x(t)$ as a sum of complex exponentials at multiples of the fundamental frequency $\omega_0 = \frac{2\pi}{T}$.
- The CTFS synthesis equation is as follows:

$$x(t) = \sum_{k=-\infty}^{\infty} X_k e^{i\frac{2\pi}{T}kt},$$

where X_k is the k^{th} **Fourier coefficient** of $x(t)$.

- X_k is can be calculated as follows (CTFS analysis equation):

$$X_k = \frac{1}{T} \int_{\langle T \rangle} x(t) e^{-i \frac{2\pi}{T} kt} dt.$$

Note that $\int_{\langle T \rangle}$ denotes an integral over any interval of length T (for instance, 0 to T or $-T/2$ to $T/2$).

- You can convert from the CTFS to the CTFT as follows:

$$X(\omega) = 2\pi \sum_{k=-\infty}^{\infty} X_k \delta(\omega - \frac{2\pi k}{T}).$$

Finding CTFS Coefficients

- Determine the period, T , and fundamental frequency $\omega_0 = \frac{2\pi}{T}$ of the signal.
- If you can write the signal as a sum of complex exponentials (for example, if it's a cos or a sin), pattern-match the sum with the CTFS synthesis equation.
- Otherwise, use the CTFS analysis equation to find expressions for the Fourier coefficients.

Practice: CTFS

1. Find the fundamental frequency and nonzero CTFS coefficients of $x(t) = \sin(\frac{\pi}{2}t) + \cos(2\pi t)$.
2. Find the fundamental frequency and nonzero CTFS coefficients of $y(t) = \sum_{n=-\infty}^{\infty} \delta(t - n)$.

Practice: CTFS (Solutions)

1. $\omega_0 = \pi/2$, $X_{-4} = \frac{1}{2}$, $X_{-1} = \frac{-1}{2i}$, $X_1 = \frac{1}{2i}$, $X_4 = \frac{1}{2}$.

First find the period of $x(t)$:

$$x(t + T) = \sin\left(\frac{\pi}{2}(t + T)\right) + \cos(2\pi(t + T)) = x(t).$$

The fundamental period of $x(t)$ is the smallest T such that both $\frac{\pi}{2}T$ and $2\pi T$ are integer multiples of 2π , so $T = 4$.

$$\omega_0 = \frac{2\pi}{T} = \frac{\pi}{2}.$$

Practice: CTFS (Solutions)

1. $\omega_0 = \pi/2$, $X_{-4} = \frac{1}{2}$, $X_{-1} = \frac{-1}{2i}$, $X_1 = \frac{1}{2i}$, $X_4 = \frac{1}{2}$.

Now, we can write out $x(t)$ using Euler's formula and pattern-match with the CTFS synthesis equation.

$$\begin{aligned}x(t) &= \frac{1}{2i}(e^{\frac{\pi}{2}t} - e^{-\frac{\pi}{2}t}) + \frac{1}{2}(e^{2\pi t} + e^{-2\pi t}) \\&= \frac{1}{2i}(e^{\frac{\pi}{2}t} - e^{-\frac{\pi}{2}t}) + \frac{1}{2}(e^{\frac{\pi}{2}4t} + e^{-\frac{\pi}{2}4t})\end{aligned}$$

Pattern-matching with

$$x(t) = \sum_{k=-\infty}^{\infty} X_k e^{i\frac{\pi}{2}kT},$$

we can see that $X_{-4} = \frac{1}{2}$, $X_{-1} = \frac{-1}{2i}$, $X_1 = \frac{1}{2i}$, $X_4 = \frac{1}{2}$, and the rest of the CTFS coefficients are 0.

2. $\omega_0 = 2\pi$, $X_k = 1$, $\forall k$.

Practice: CTFS (Solutions)

- $\omega_0 = \pi/2$, $X_{-4} = \frac{1}{2}$, $X_{-1} = \frac{-1}{2i}$, $X_1 = \frac{1}{2i}$, $X_4 = \frac{1}{2}$.
- $\omega_0 = 2\pi$, $Y_k = 1$, $\forall k$.

$y(t)$ repeats itself every 1 timestep, so it has a period $T = 1$ and fundamental frequency $\omega_0 = 2\pi$.

$y(t)$ cannot be easily written as a sum of sinusoids, so let's plug $y(t)$ into the CTFS analysis equation. Note that only one Dirac delta appears every period of the signal.

$$\begin{aligned} Y_k &= \frac{1}{T} \int_{-T/2}^{T/2} y(t) e^{-i\frac{2\pi}{T}t} dt \\ &= \int_{-1/2}^{1/2} \delta(t) e^{-i2\pi t} dt = e^{-i2\pi(0)} = 1. \end{aligned}$$

Frequency Domain and Convolution

- **Convolution** in the time domain corresponds to **multiplication** in the frequency domain.
- If $y(t) = x(t) * h(t)$ in the time domain, then $Y(\omega) = X(\omega)H(\omega)$ in the CTFT domain.
- Likewise, multiplication in the time domain corresponds to convolution in the frequency domain.
- If $y(t) = x(t)h(t)$, then $Y(\omega) = X(\omega) * H(\omega)$.