

Height 0 → 0 Swaps =  $n/2 * 0 = 0$

Height 1 → 2 Swaps =  $n/2 * 1/2 = n/4$

Height 2 → 1 Swaps =  $(n/2 * 1/2) * 1/2 = n/8$

Sumation =  $0 * n/2 + n/2 * 1/2 + n/4 * 1/2$   
 $= 0 + 7/4 + 7/8$   
 $= 2 + 1 = 3 \text{ swaps}$

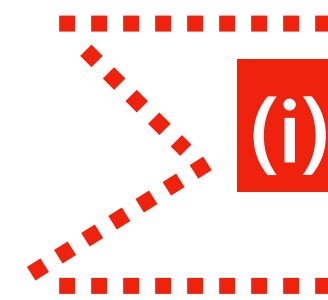
Logn

$$\sum_{l=0}^{l=\log n} (i) * (n/2^{l+1})$$

$l = 0$

$$\begin{aligned}\text{Sumation} &= 0 * n/2 + n/2 * 1/2 + n/4 * 1/2 \\ &= 0 + 7/4 + 7/8 \\ &= 2 + 1 = 3\text{swaps}\end{aligned}$$

(logn)



$$(i) * (n/ 2^{l+1})$$

$$(i) = 0$$

$$\begin{aligned}0 * n/2 + n/2 * 1/2 + n/2 * 1/4 + \dots \\ \Rightarrow n/2(0+1/2+1/4+\dots)\end{aligned}$$

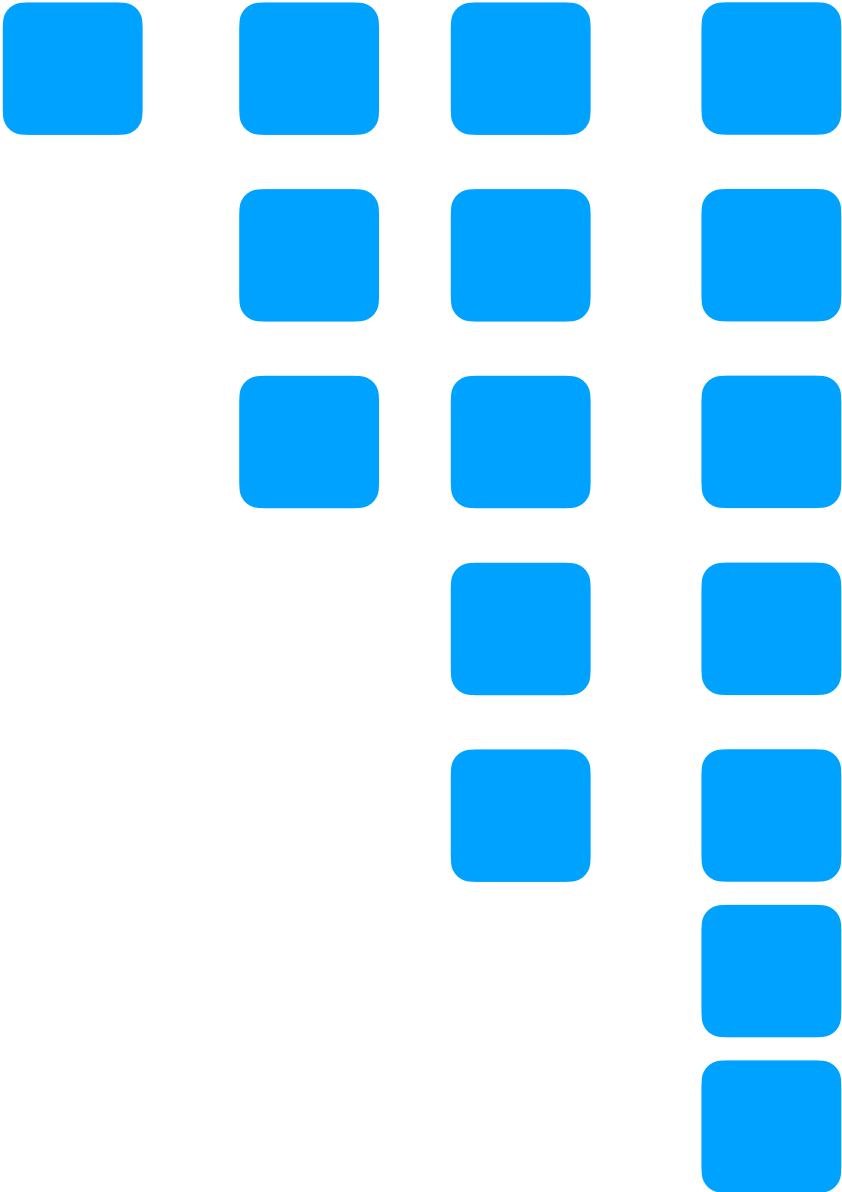
$$\begin{aligned}\text{Arithmetic Series} \\ (-4, 3, 10, 17) \\ (1, 3, 5, 7)\end{aligned}$$

$$\begin{aligned}(-4, 3, 10, 17) &= 26 \\ n/2(a+l) &= 4/2(-4+17) \\ &= 2(13) = 26\end{aligned}$$

$$(1, 3, 5, 7) = 16$$

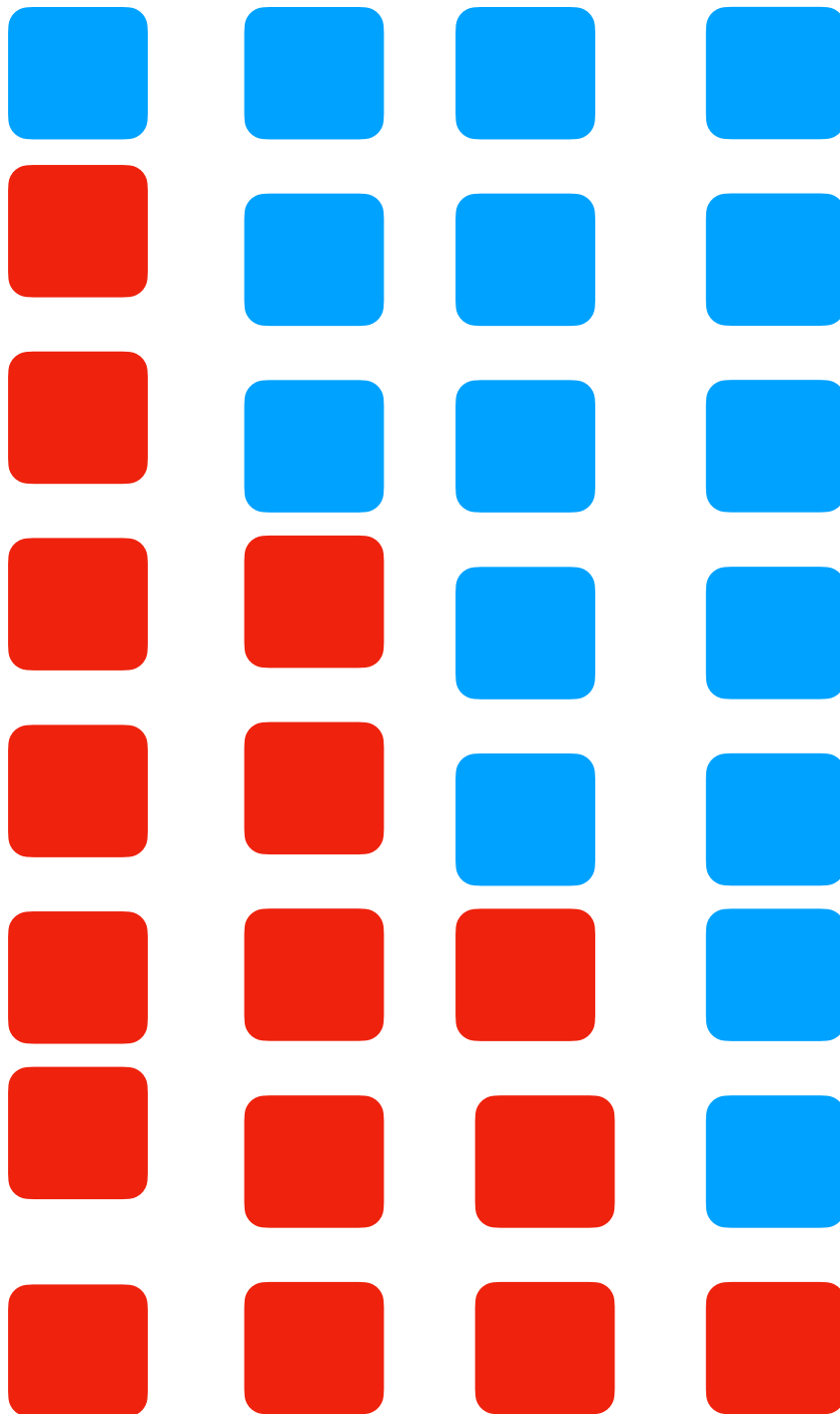
$$\begin{aligned}(1, 3, 5, 7, 9, 11) &= 36 \\ N/2(a+l) &= 6/2(1+11) = 36\end{aligned}$$

(1,3,5,7)



+

(7,5,3,1)



=

$n/2(a+l)$

$$1 + 1/2 + 1/4 + 1/8 + \dots = 1 * 1/2^0 + 1 * (1/2^1) + 1 * 1/2^2 + 1 * 1/2^3 + \dots$$

Geometric Series

$$r = 1/2$$

$$S_n = a r^0 + a r^1 + a r^2 + \dots + a r^{n-3} + a r^{n-2} + a r^{n-1}$$

$$r S_n = a r^1 + a r^2 + a r^3 + \dots + a r^{n-2} + a r^{n-1} + a r^n$$

$$S_n - r S_n = a - a r^n$$

$$S_n(1-r) = a(1-r^n)$$

$$S_n = a(1-r^n) / (1-r)$$

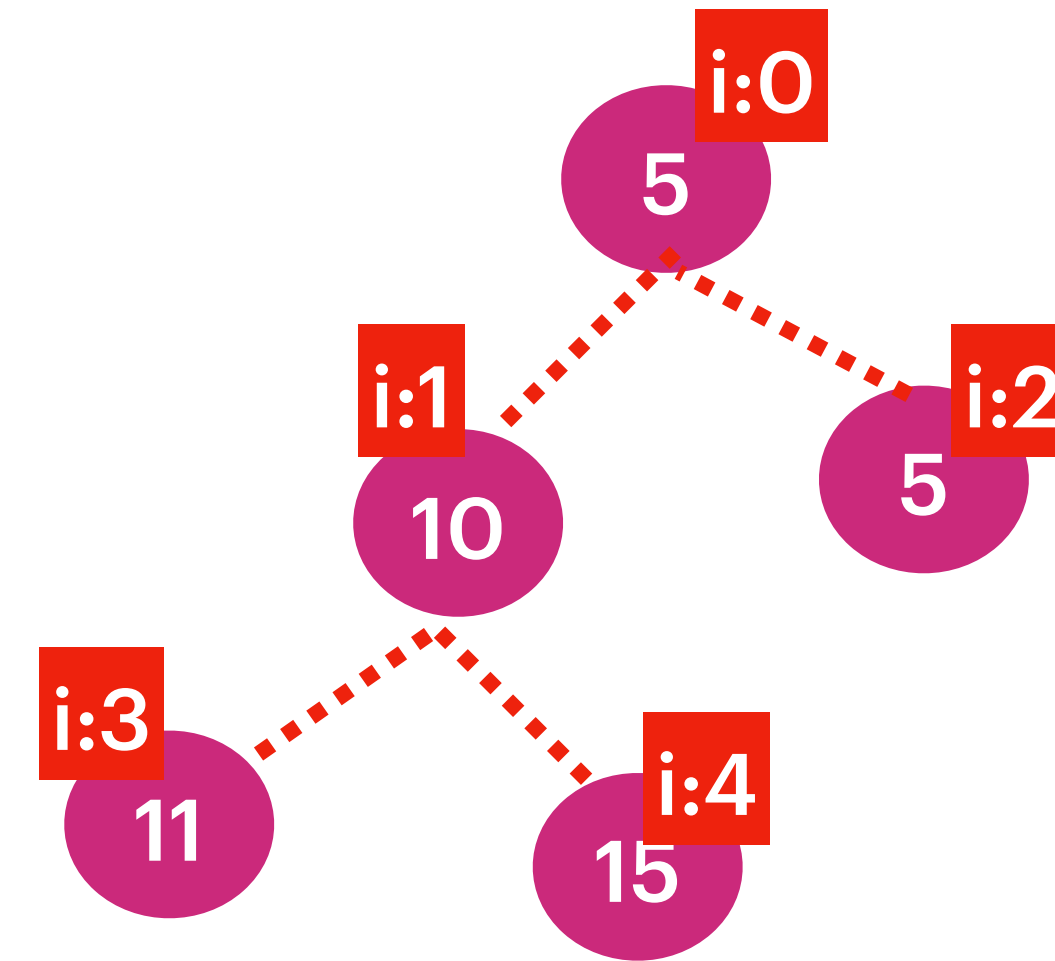
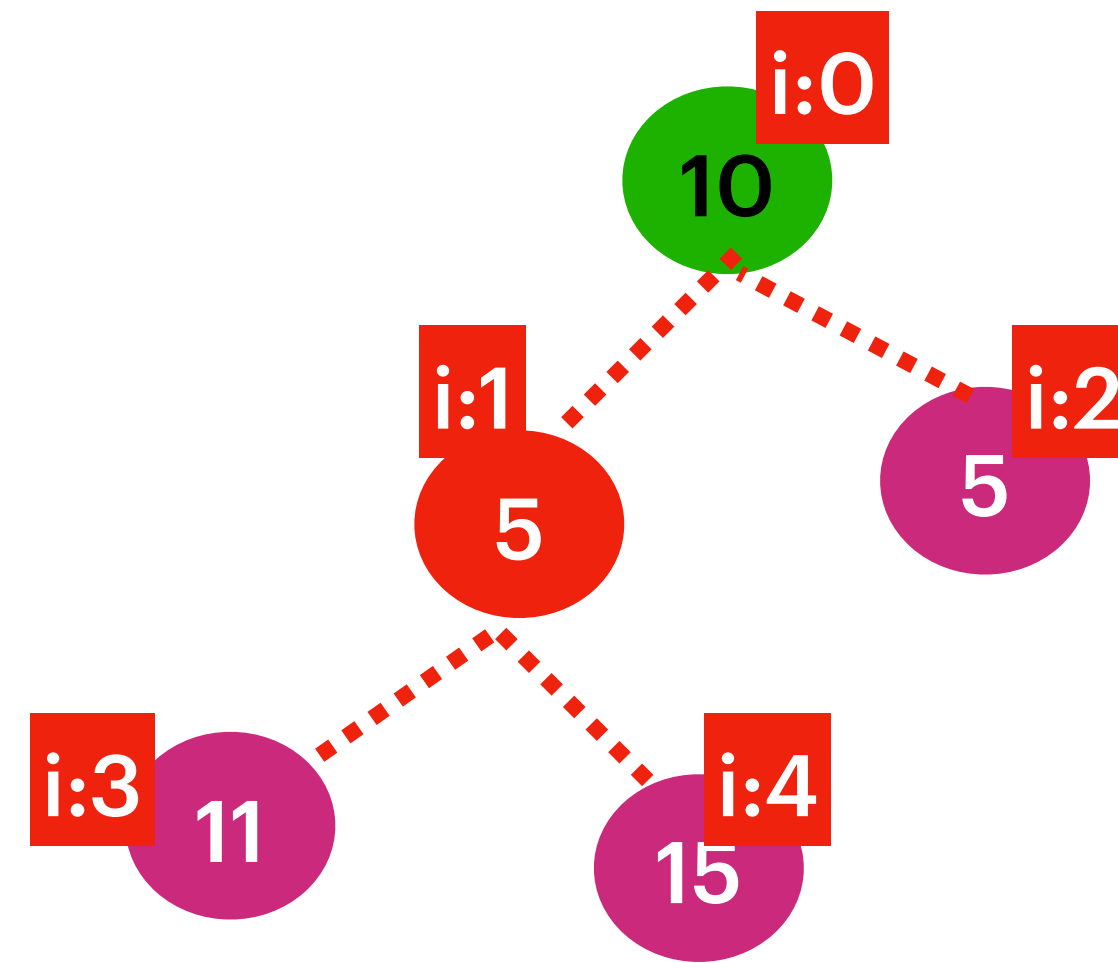
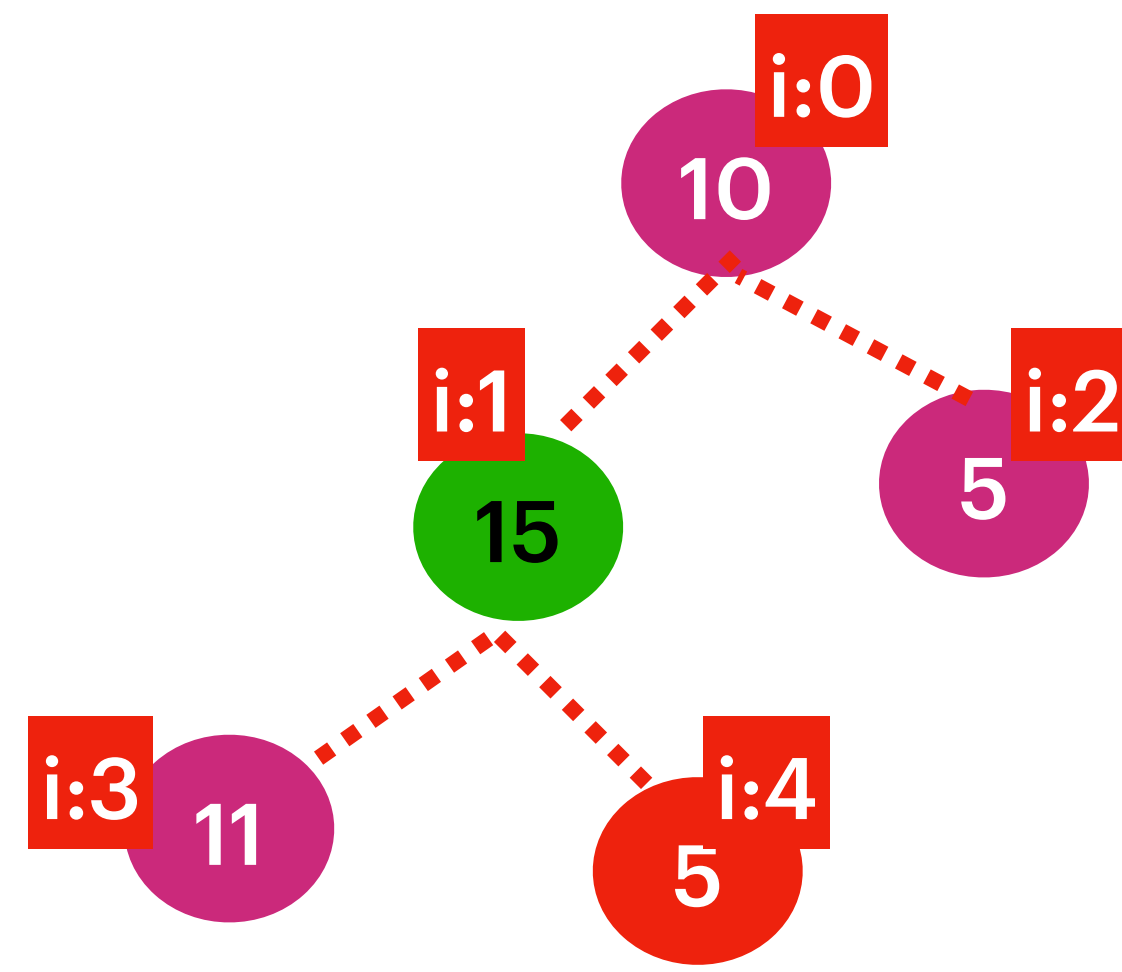
$$0 * n/2 + n/2 * 1/2 + n/2 * 1/4 + \dots$$

$$\Rightarrow n/2(0 + 1/2 + 1/4 + \dots)$$

$$\Rightarrow n/2(a(1-r^n) / (1-r))$$

$$\Rightarrow n/2 * 2 = n$$

$$O(n)$$



$\text{heapifyStartIndex} = N/2 - 1;$   
 $\text{leftIndex} = 2 * \text{index} + 1$   
 $\text{rightIndex} = 2 * \text{index} + 2$

