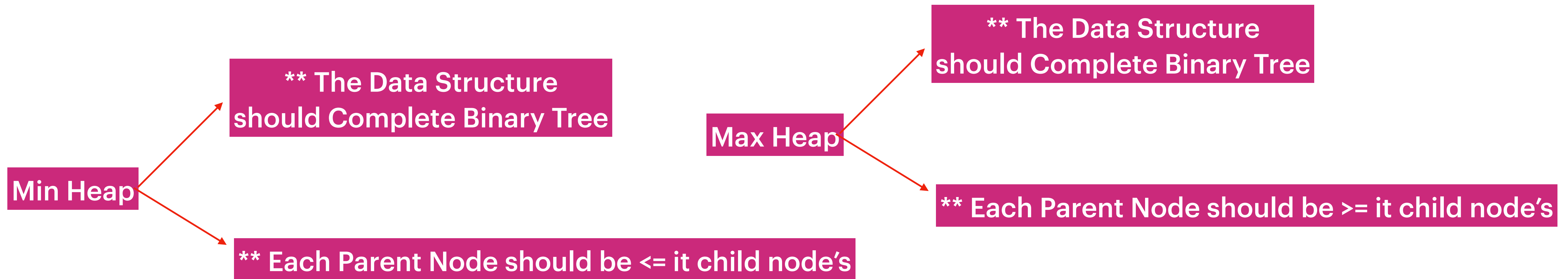
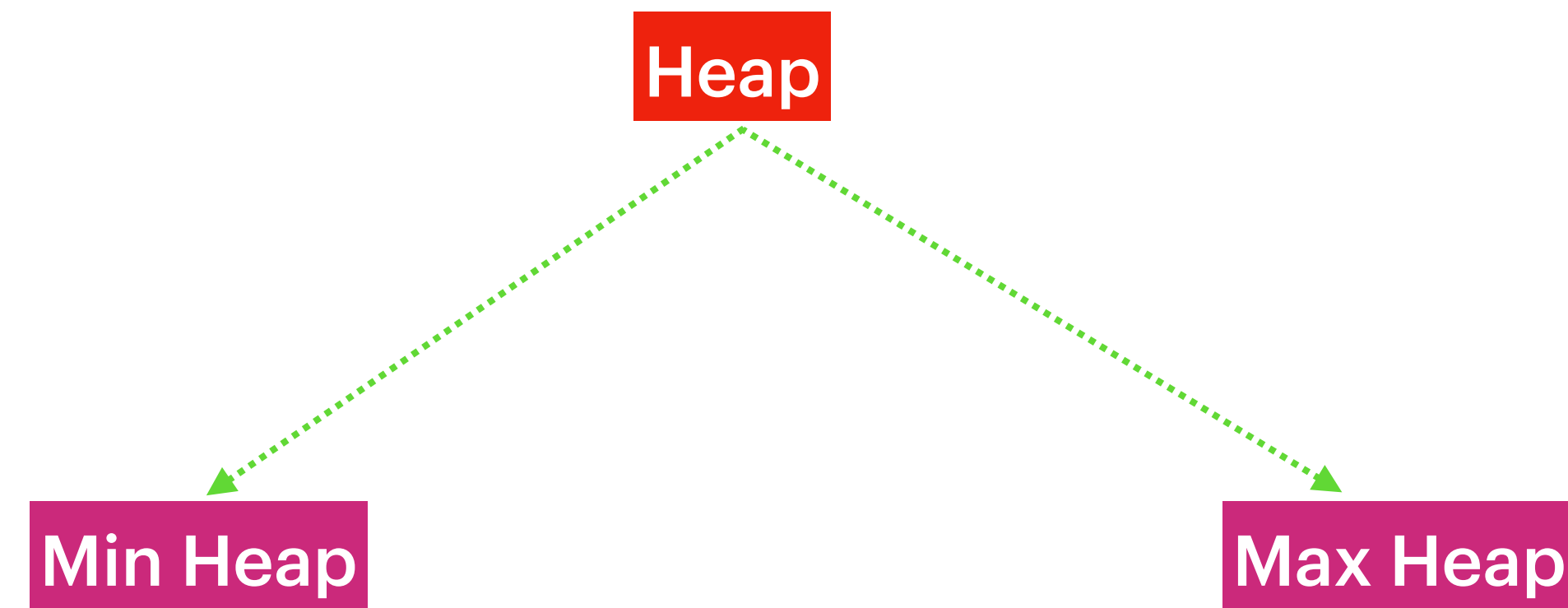


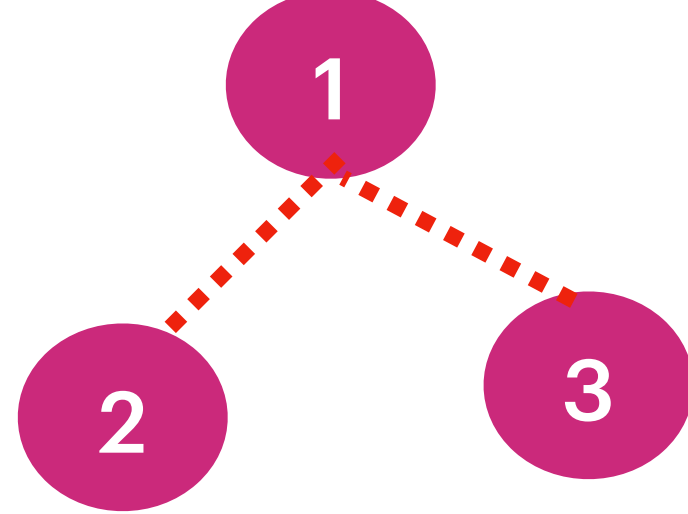
# Let's Understand Heap Before moving on to weighted Graphs



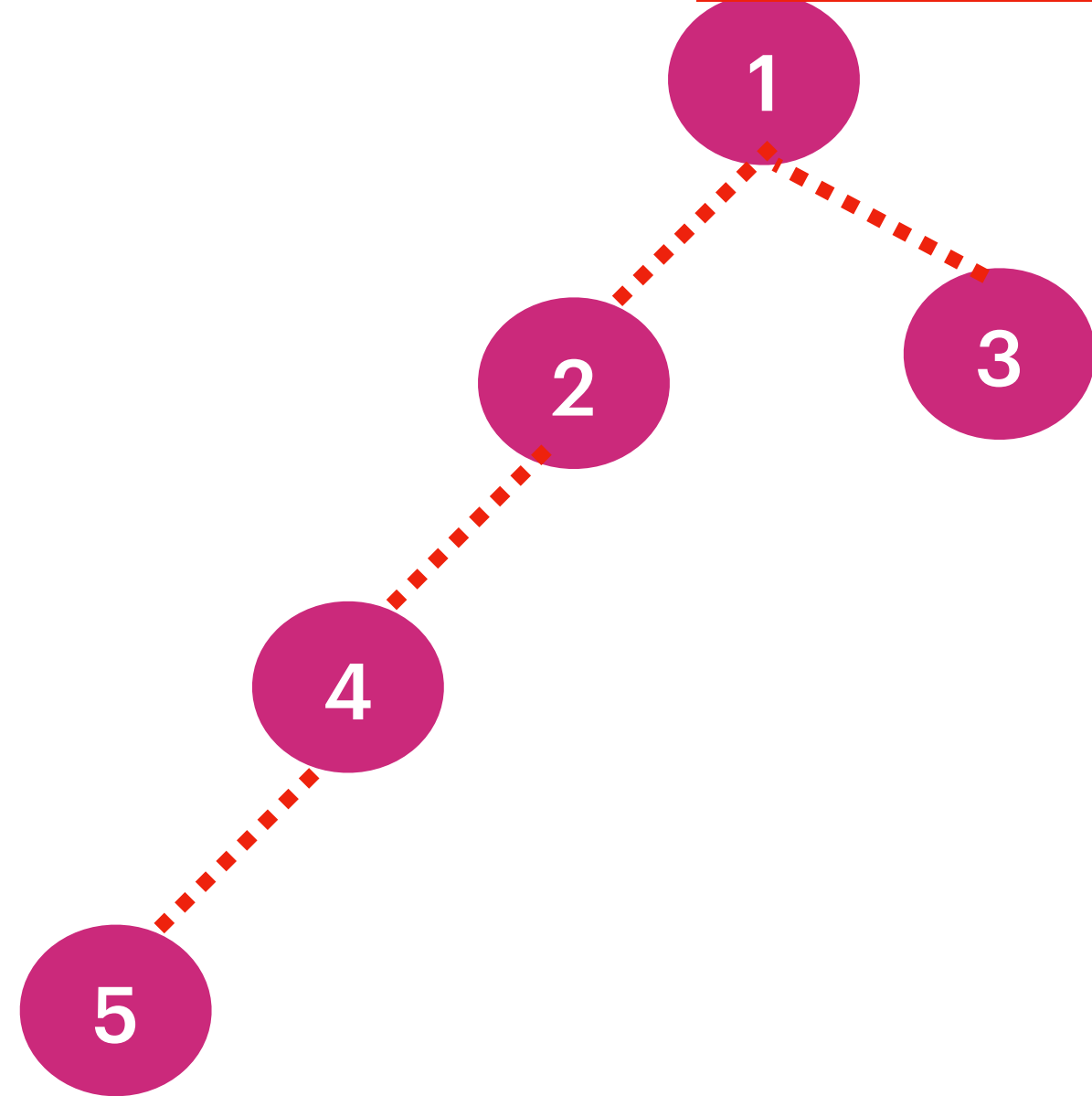
# What is Binary Tree ?

Each Parent node at max have two Childs

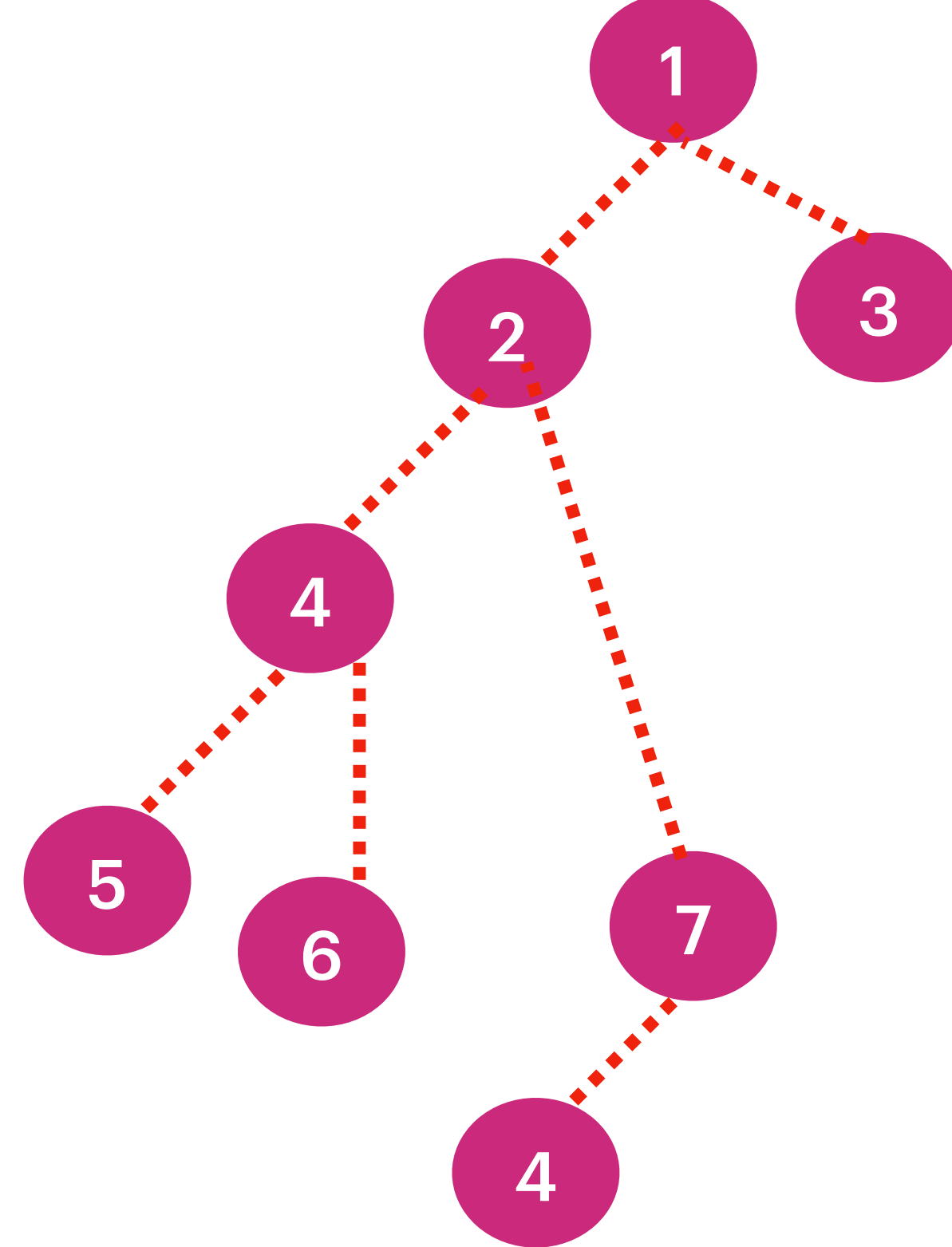
Binary Tree



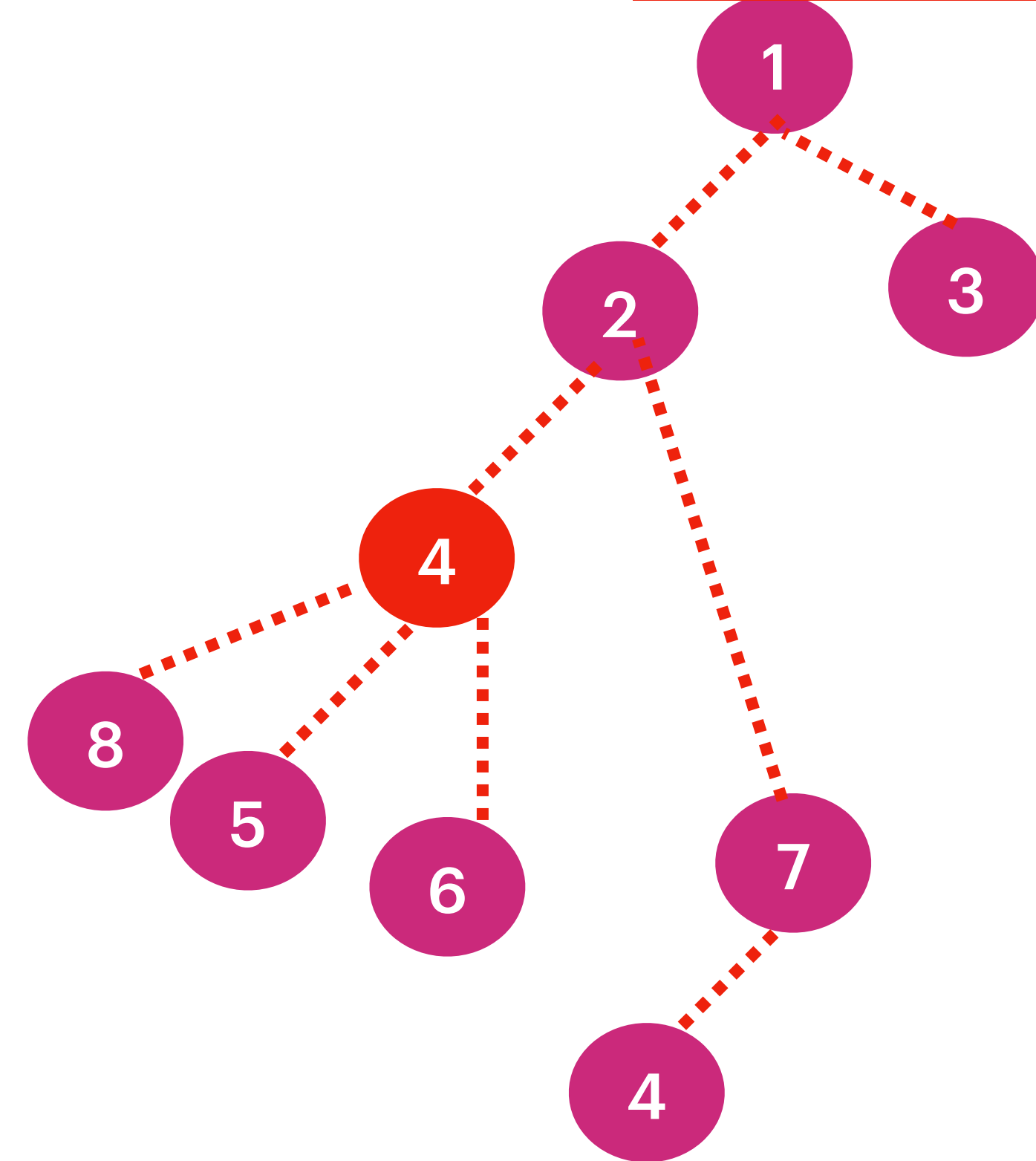
Binary Tree



Binary Tree



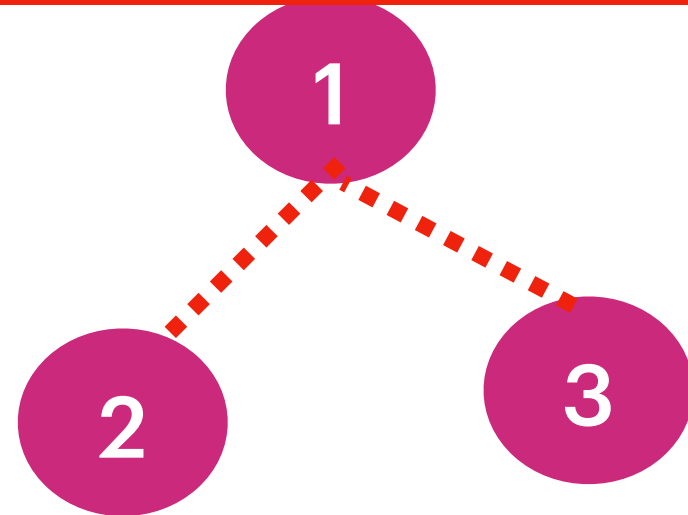
Not a Binary Tree



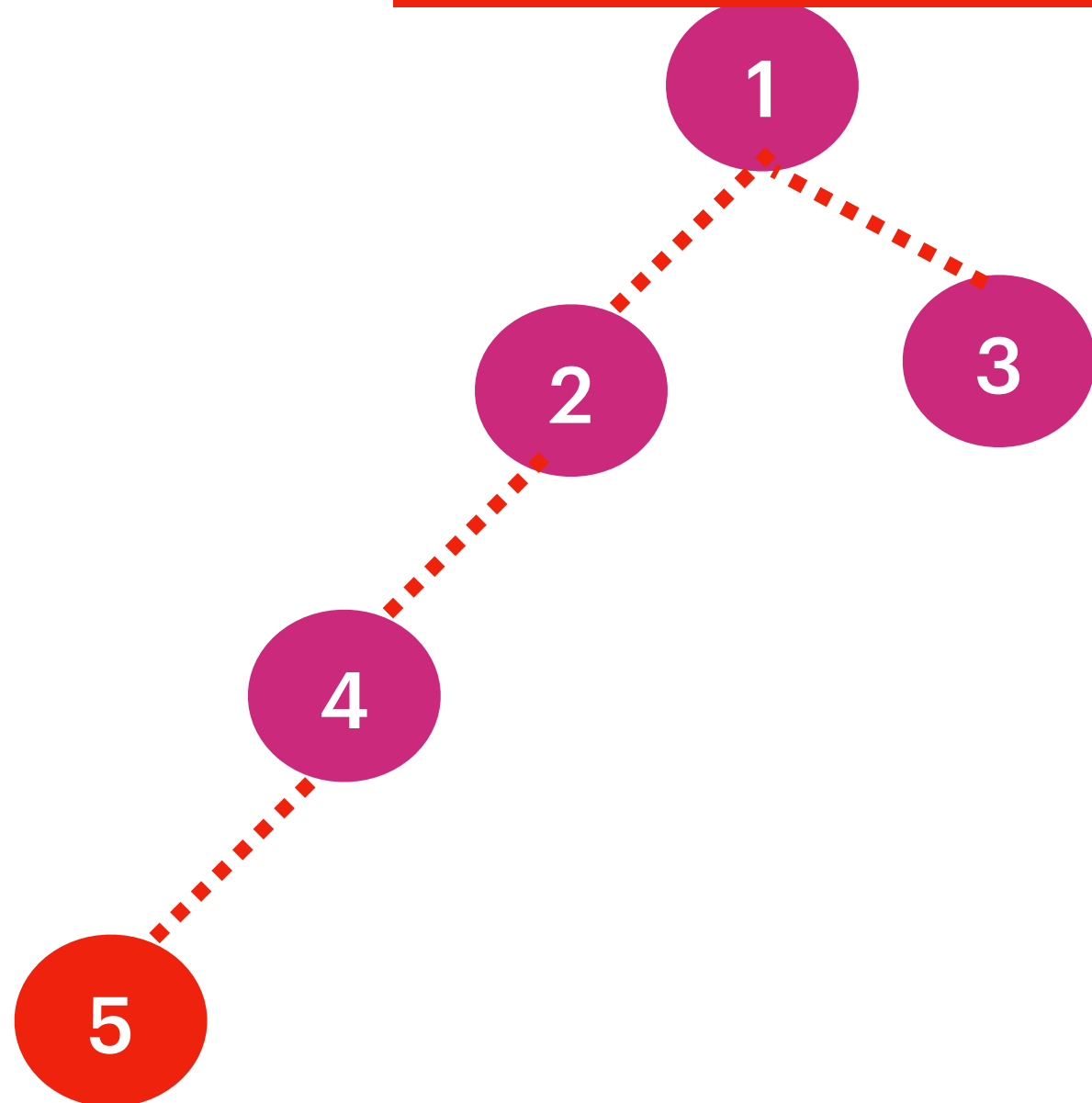
## What is Complete Binary Tree ?

Each Parent node at max have two Childs,  
At Each level order of elements should  
Be filled from left -> right.  
Once the the current level complete we can  
Move on to next level.

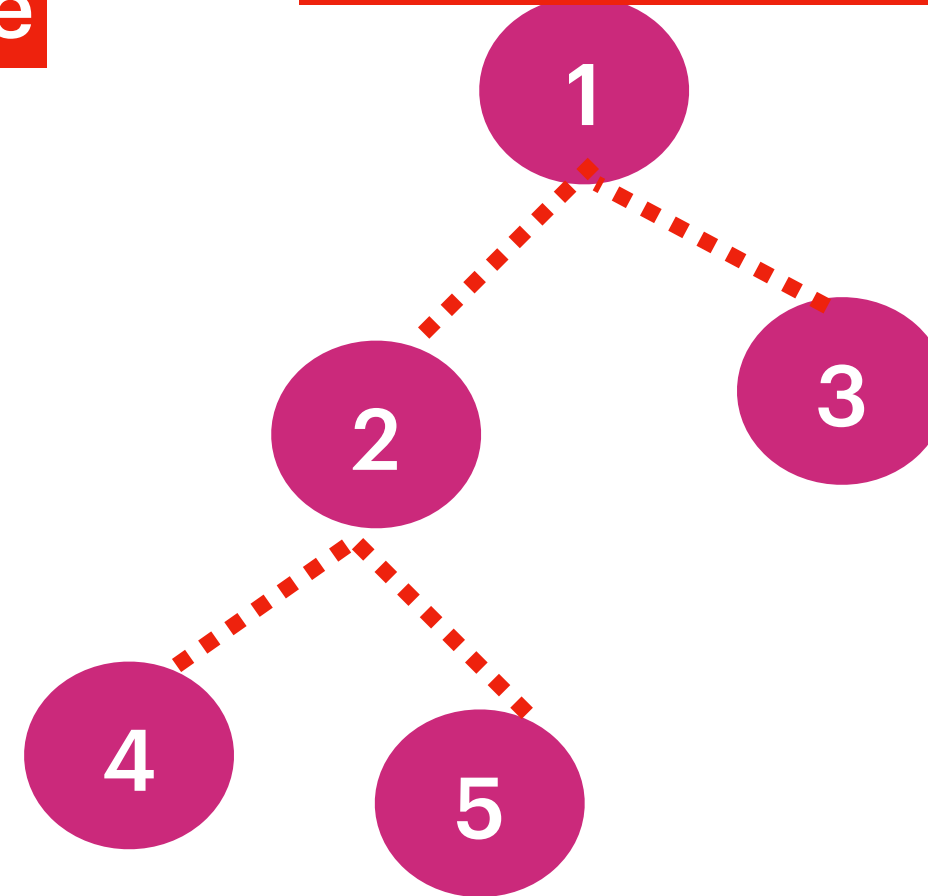
Complete Binary Tree



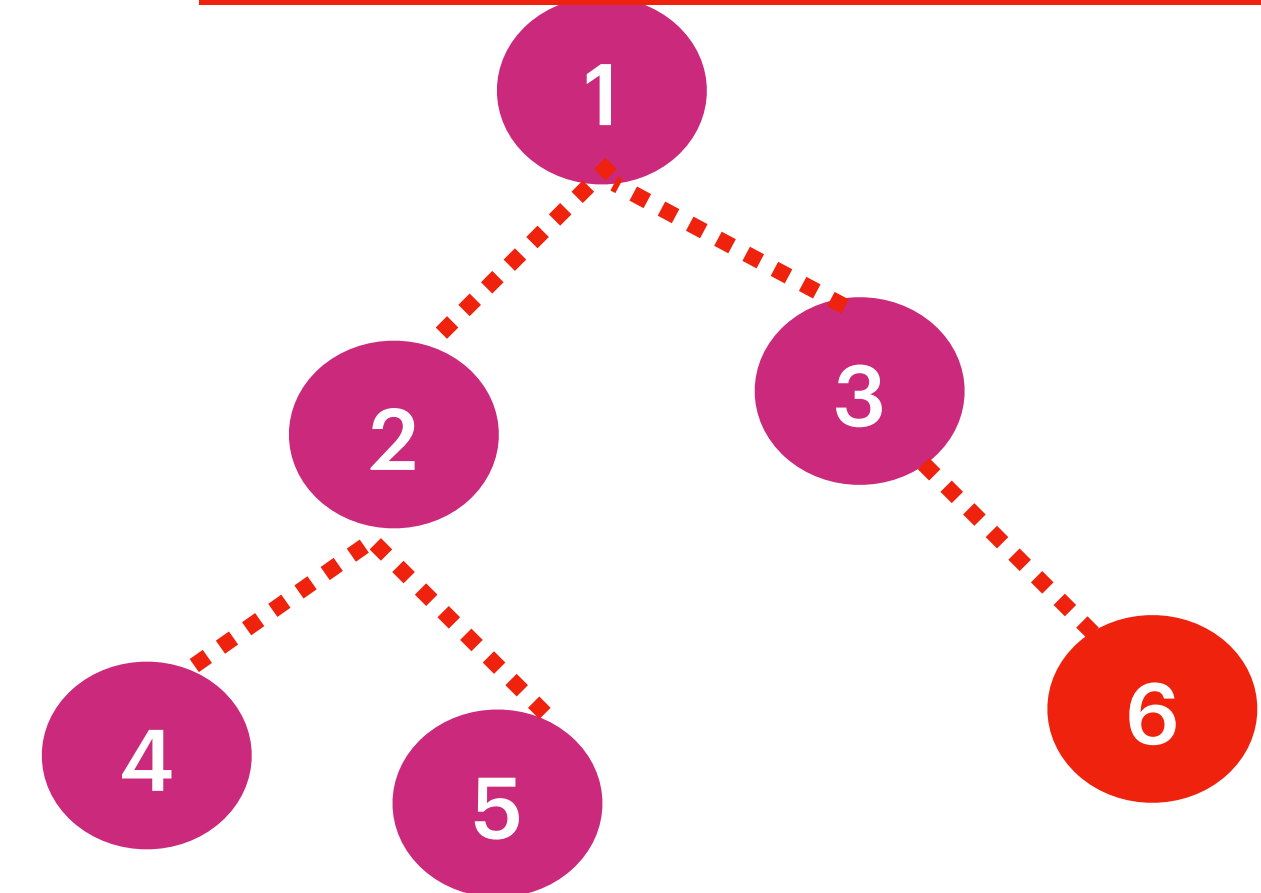
Not a Complete Binary Tree



Complete Binary Tree



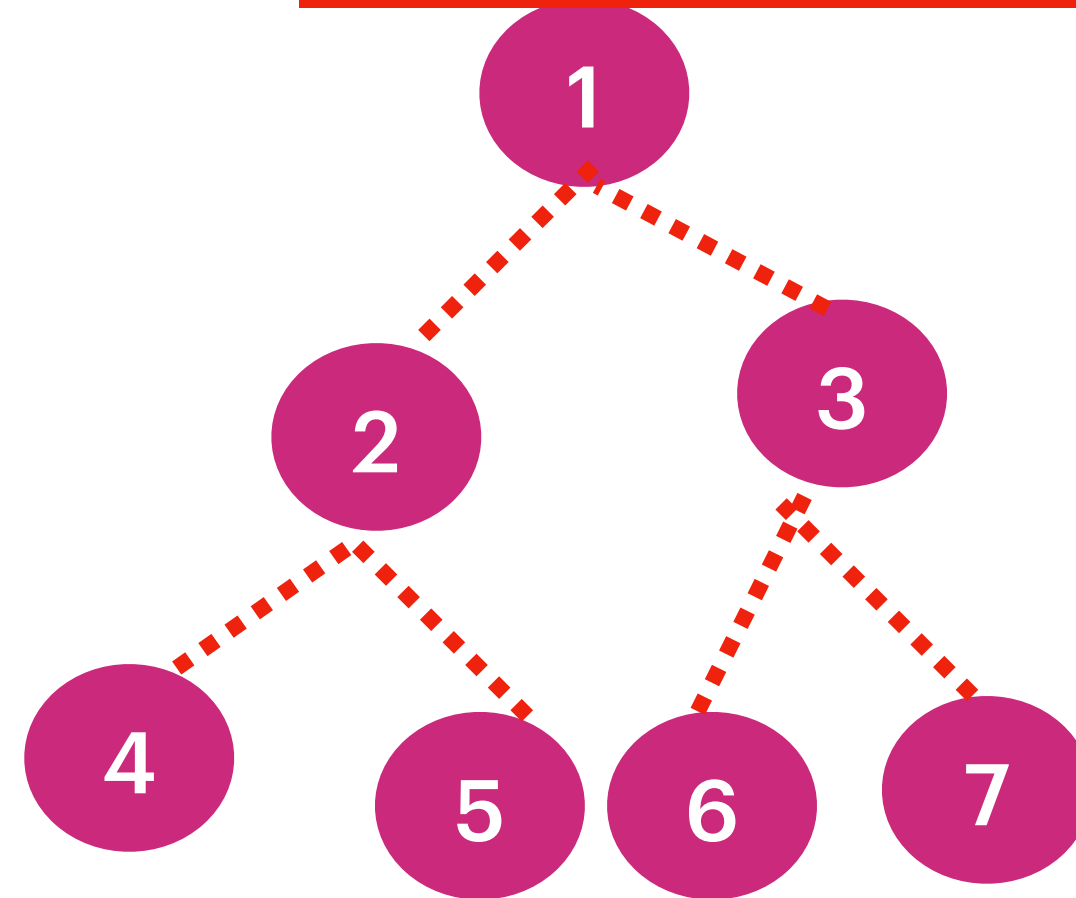
Not a Complete Binary Tree



## What is Complete Binary Tree ?

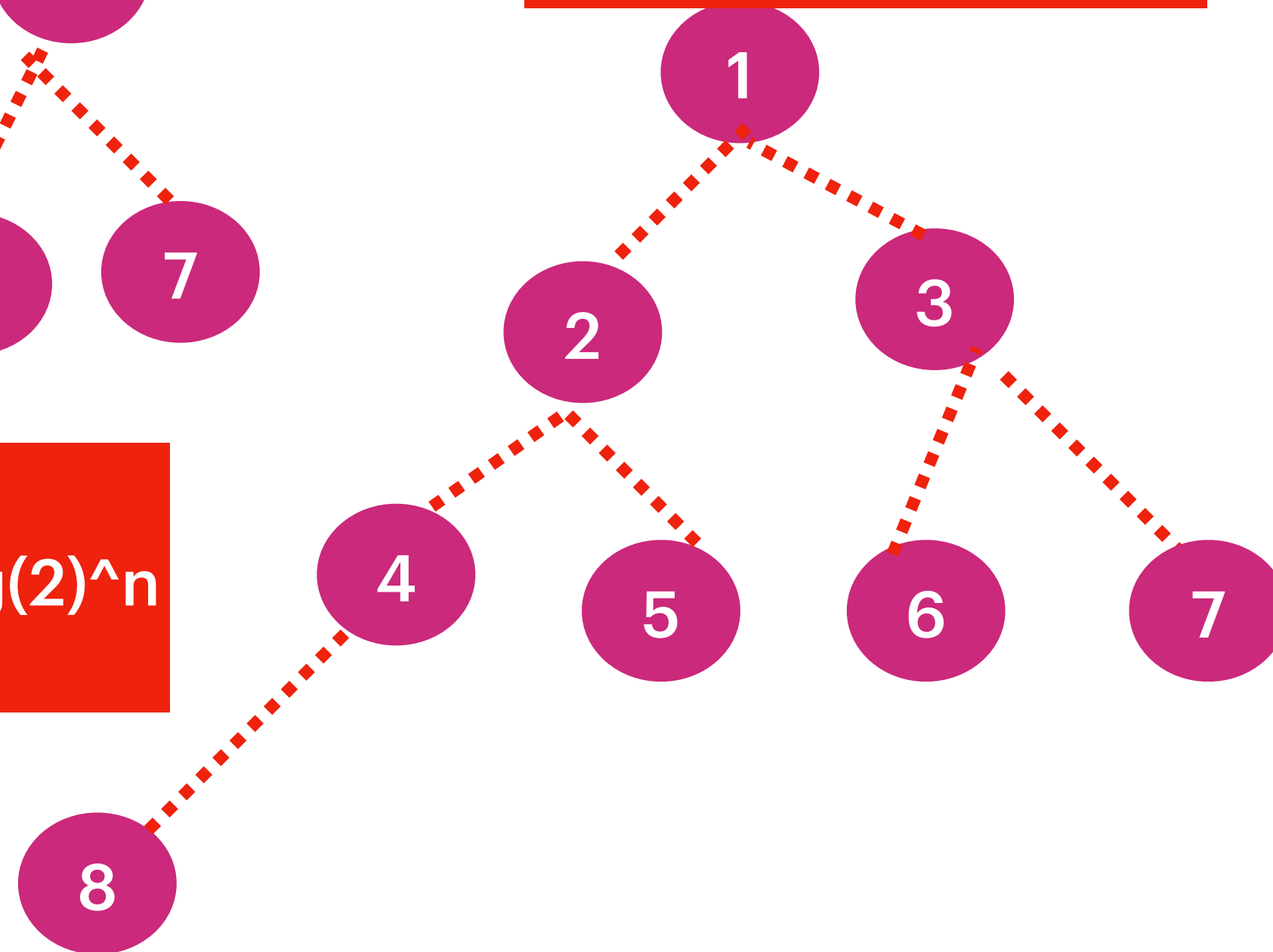
Each Parent node at max have two Childs,  
At Each level order of elements should  
Be filled from left -> right.  
Once the the current level complete we can  
Move on to next level.

Complete Binary Tree

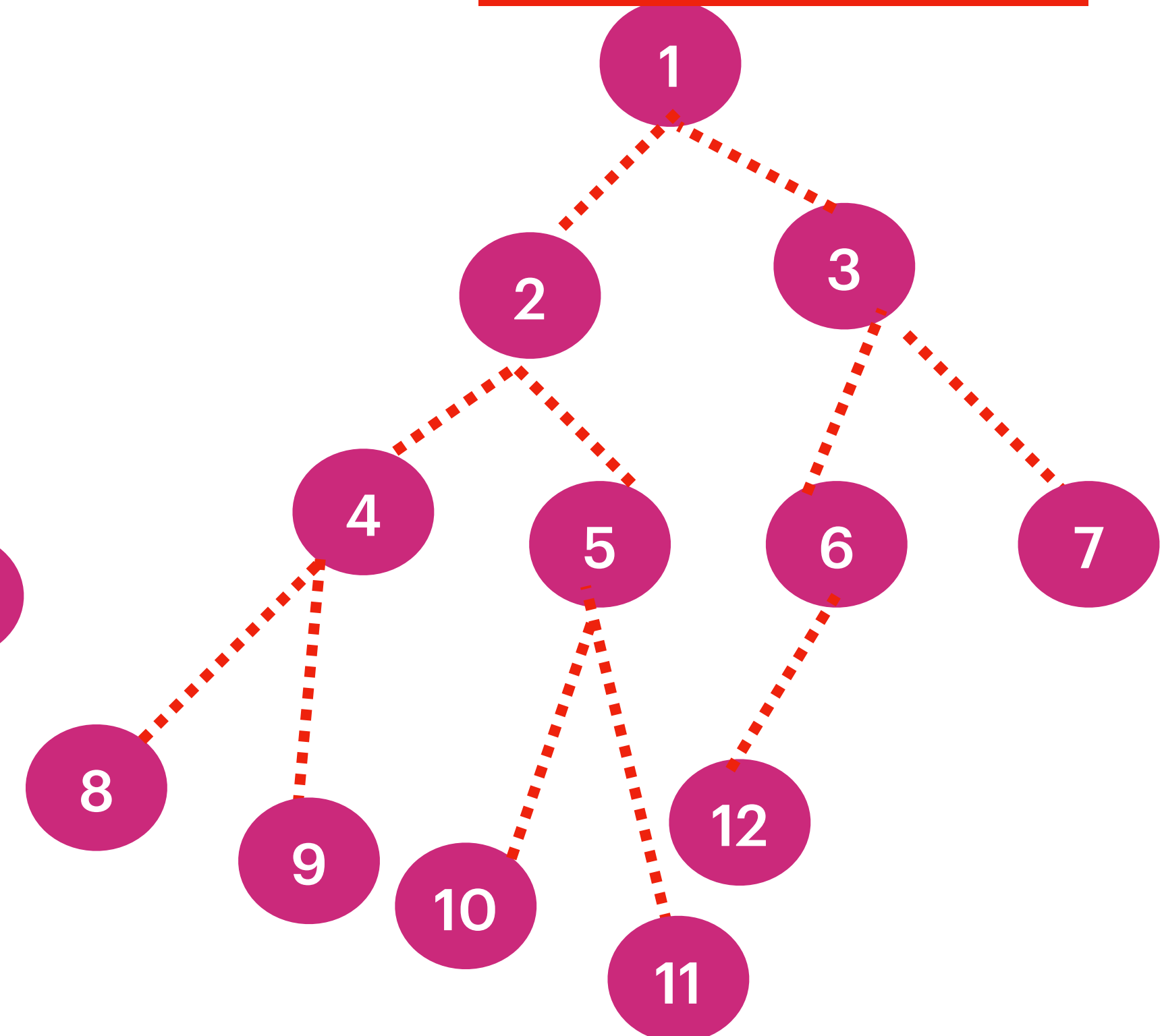


Height  
Of Complete Binary Tree :  $\log(2)^n$

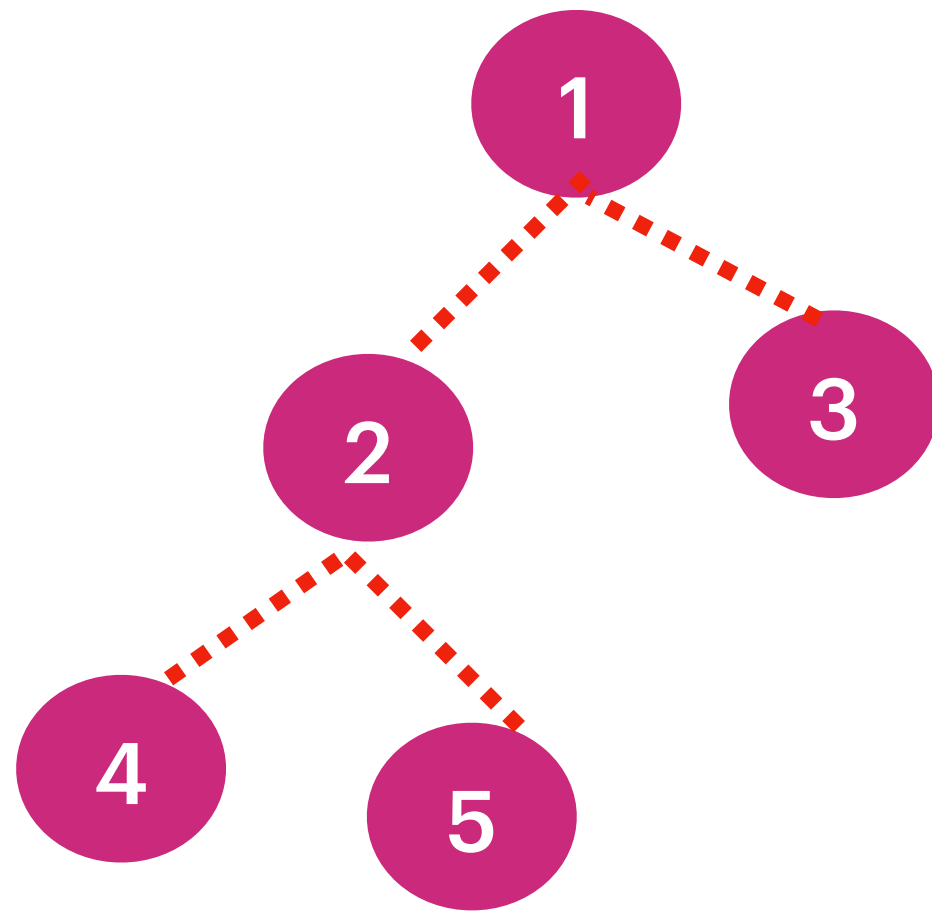
Complete Binary Tree



Complete Binary Tree



## Complete Binary Tree



Root :

1

Leaf Nodes :

3

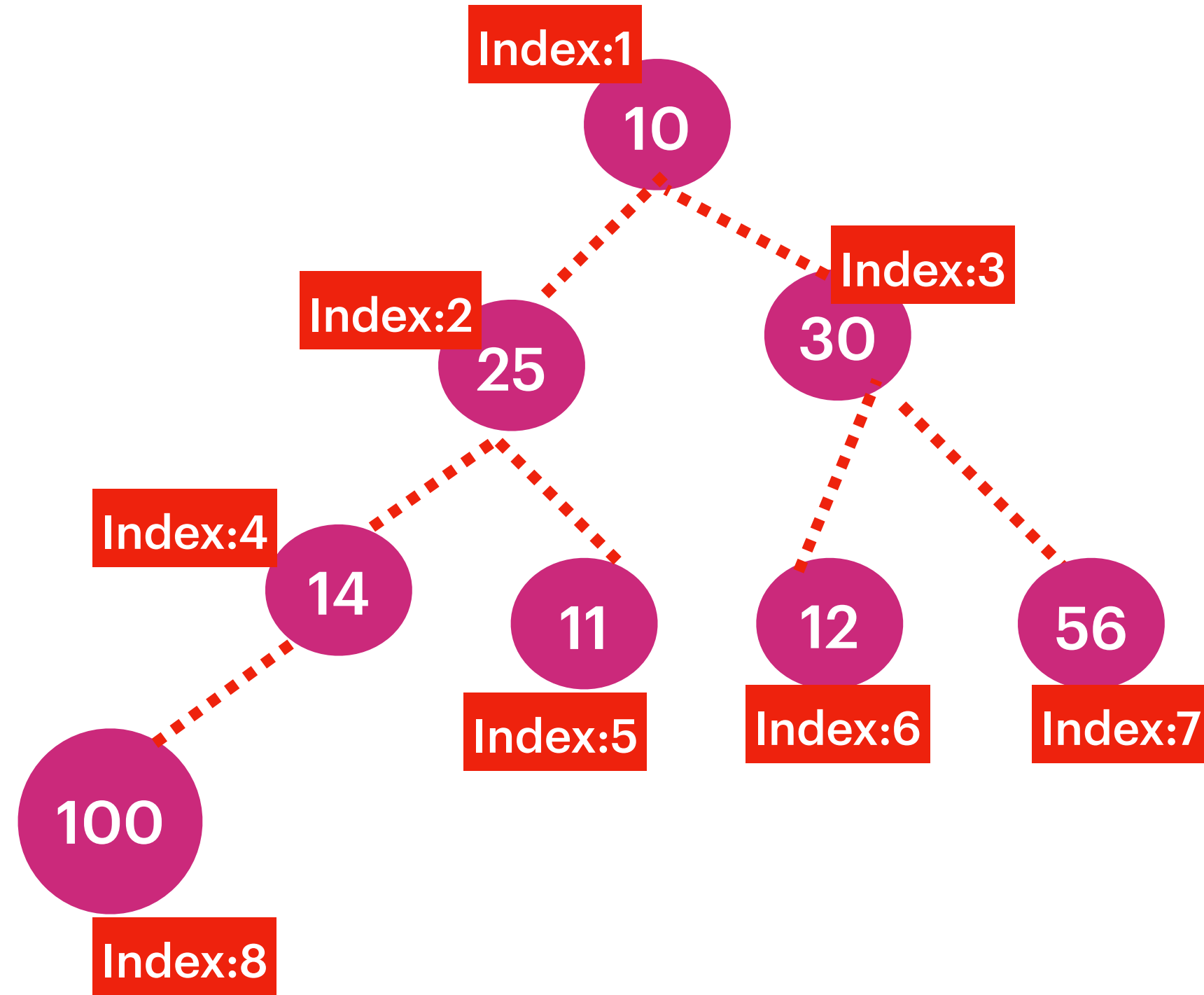
4

5

A Node which does not have Childs is a leafNode

Height : 3 ~  $\log_2 n$

## Complete Binary Tree



Parent =  $\text{index}/2$ ;

Ex: Parent Of 25 =  $2/2 = \text{index:1} = 10$

## Transform Complete Binary Tree to the Hash/Array

How to you find parent ?

How do you find left & right child ?

How do you know that current element is a leaf Node ?

Left Child =  $\text{index} * 2$

Right Child =  $\text{index} * 2 + 1$

Ex: Left Child of Element 30 =  $2 * \text{index:3} = \text{index:6} = 12$

Right Child of Element 30 =  $2 * \text{index:3} + 1 = \text{index:7} = 56$

How do you know that current element is a leaf Node ?

LeafNode:  $\text{index} > \text{size}/2$

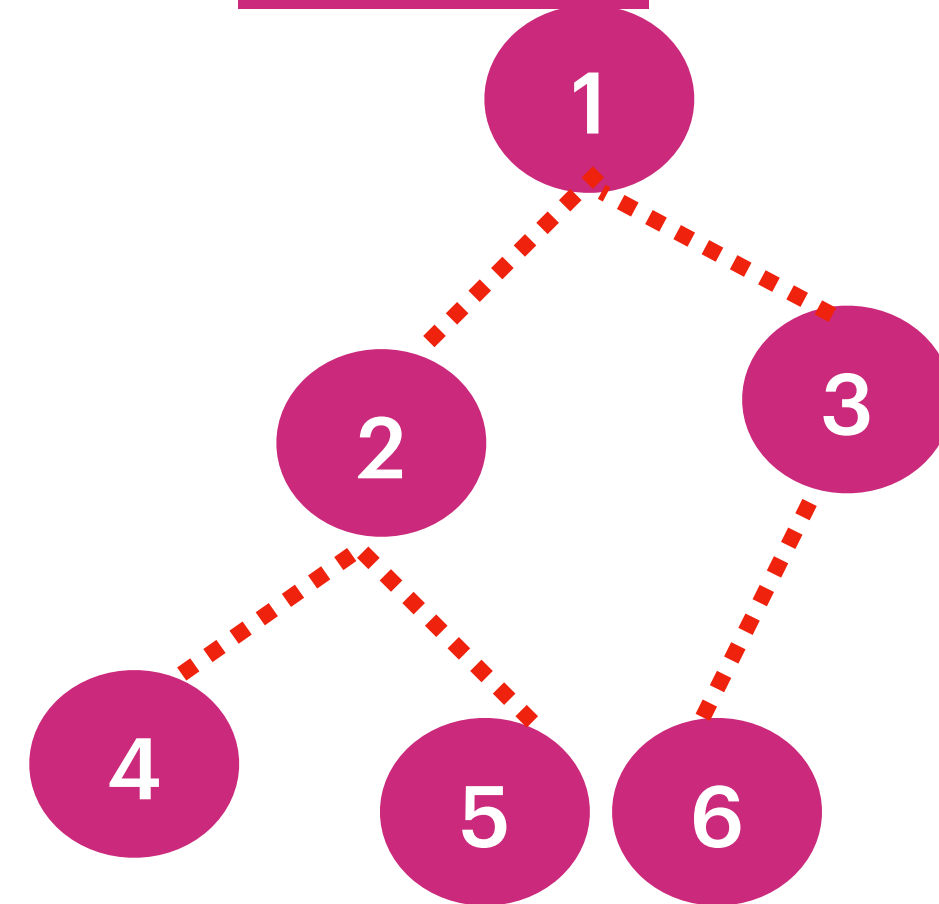


Min Heap

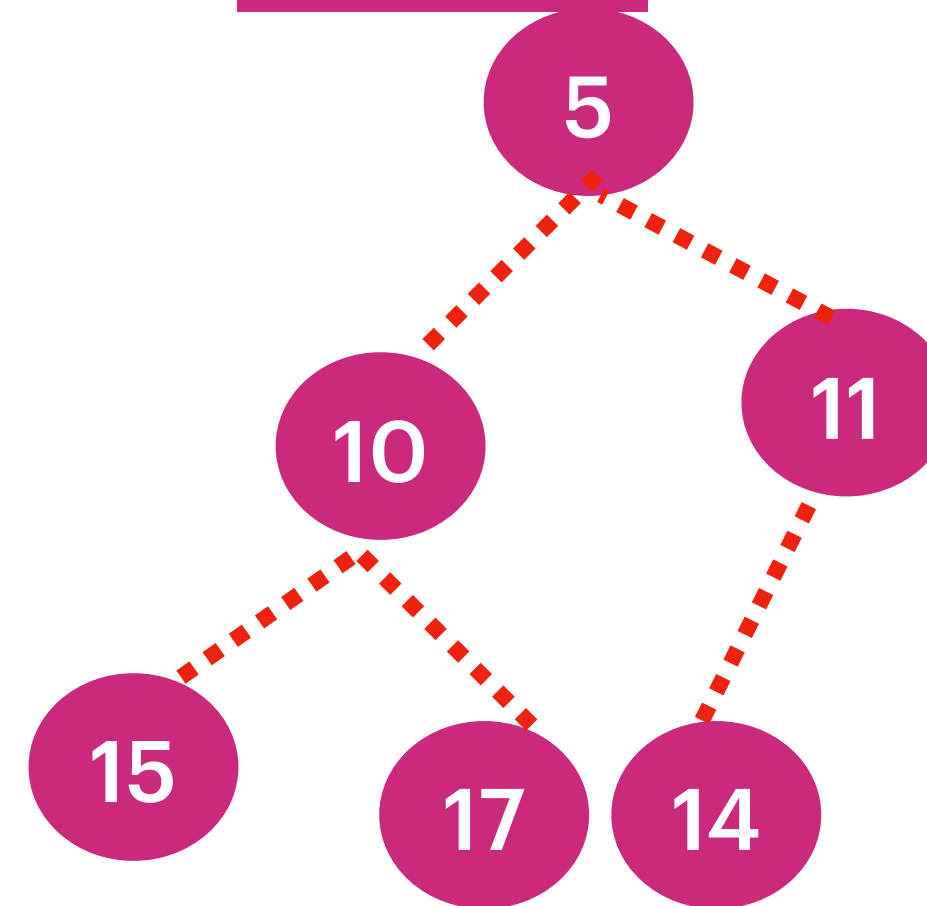
**\*\* The Data Structure  
should Complete Binary Tree**

**\*\* Each Parent Node should be  $\leq$  it child node's**

Min Heap



Min Heap



## Insert Operation On MinHeap

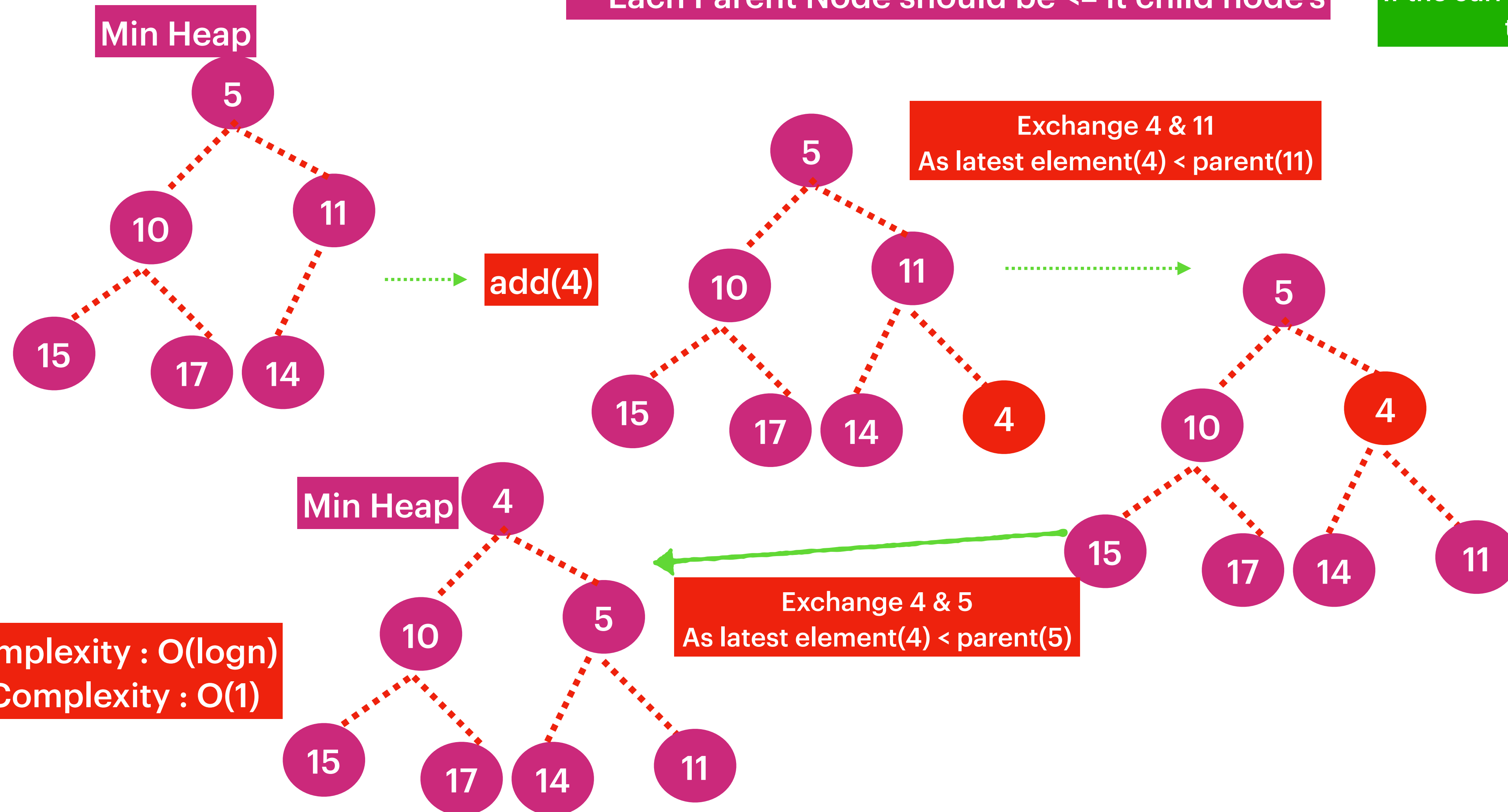
Min Heap

**\*\* The Data Structure  
should Complete Binary Tree**

**\*\* Each Parent Node should be  $\leq$  it child node's**

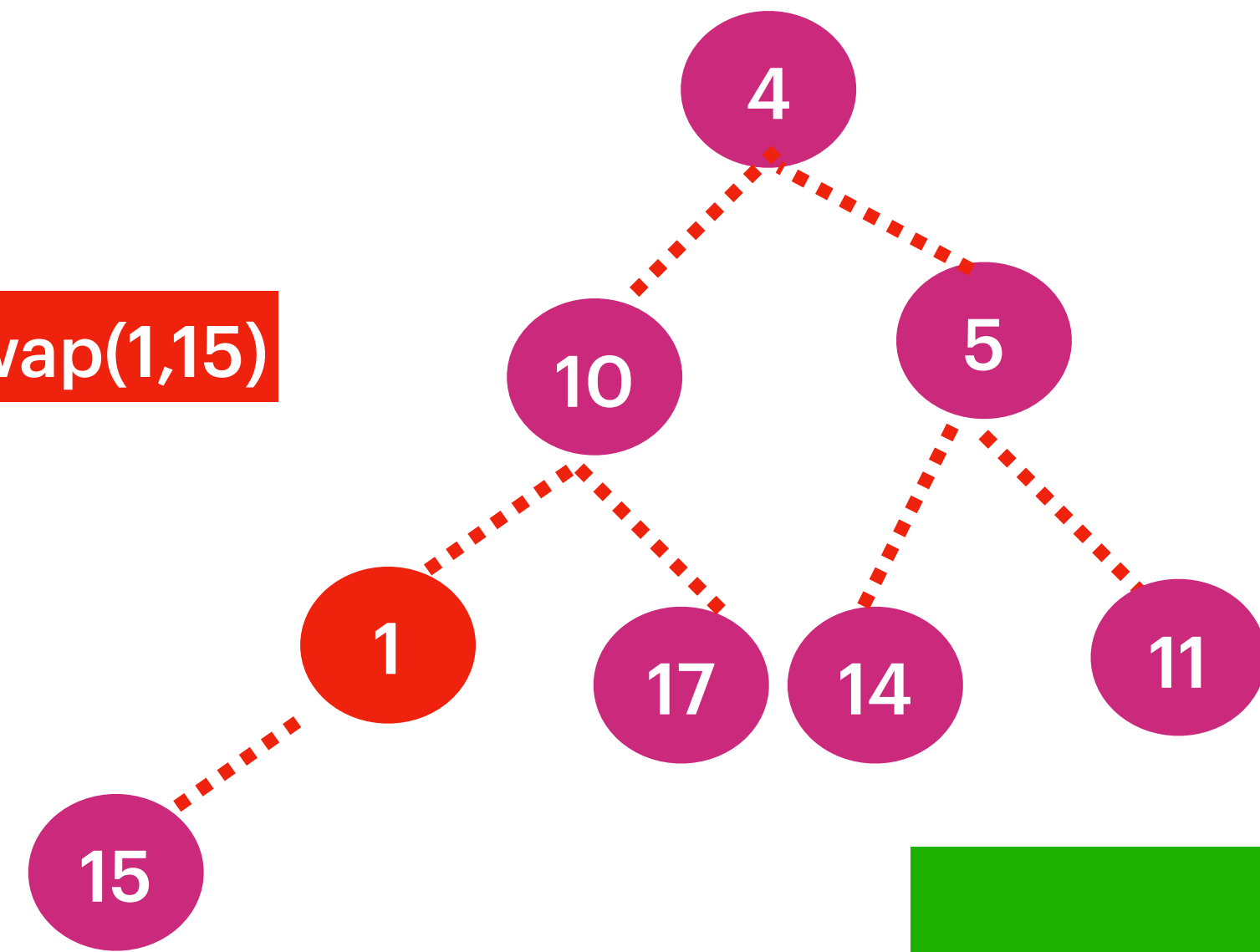
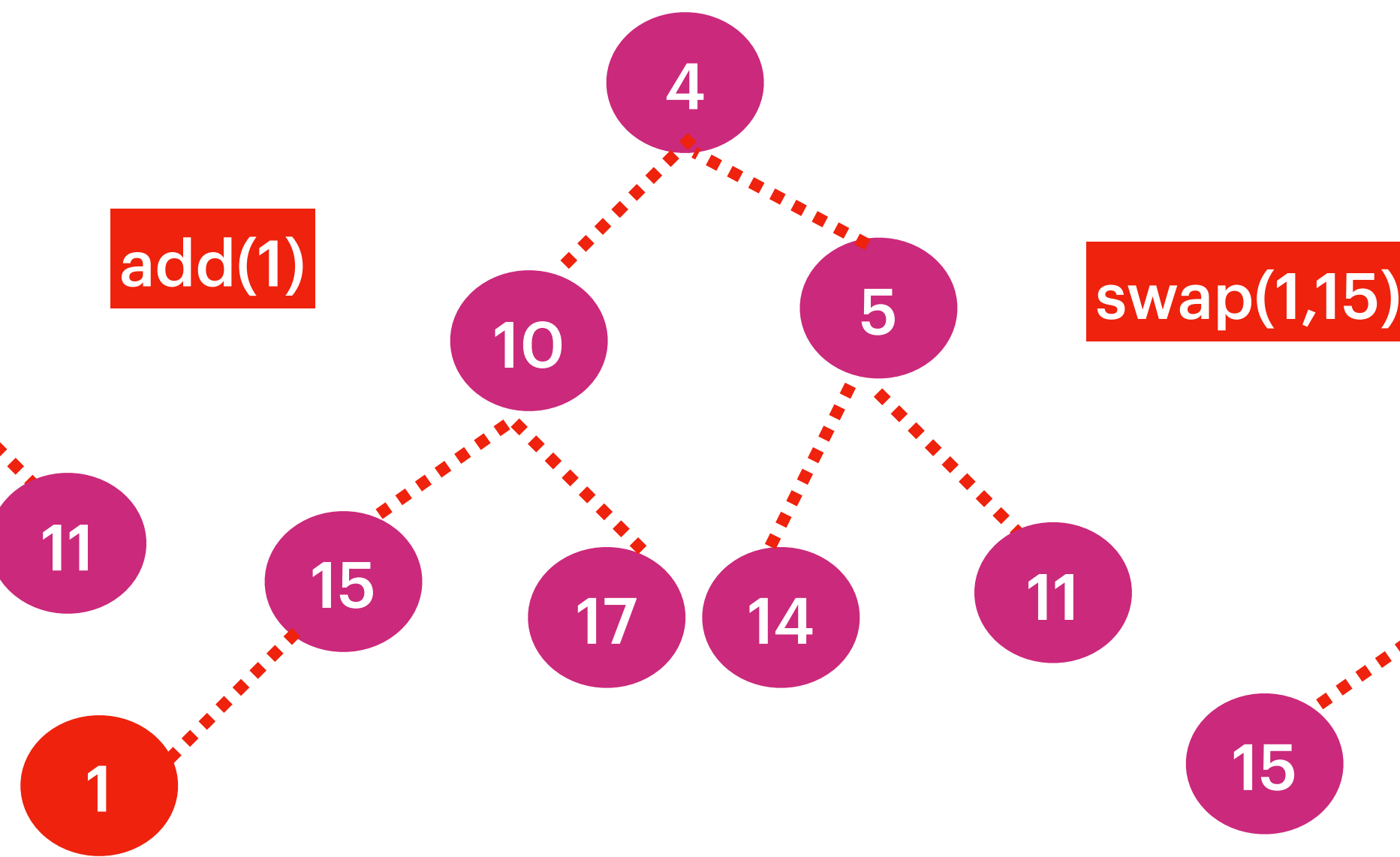
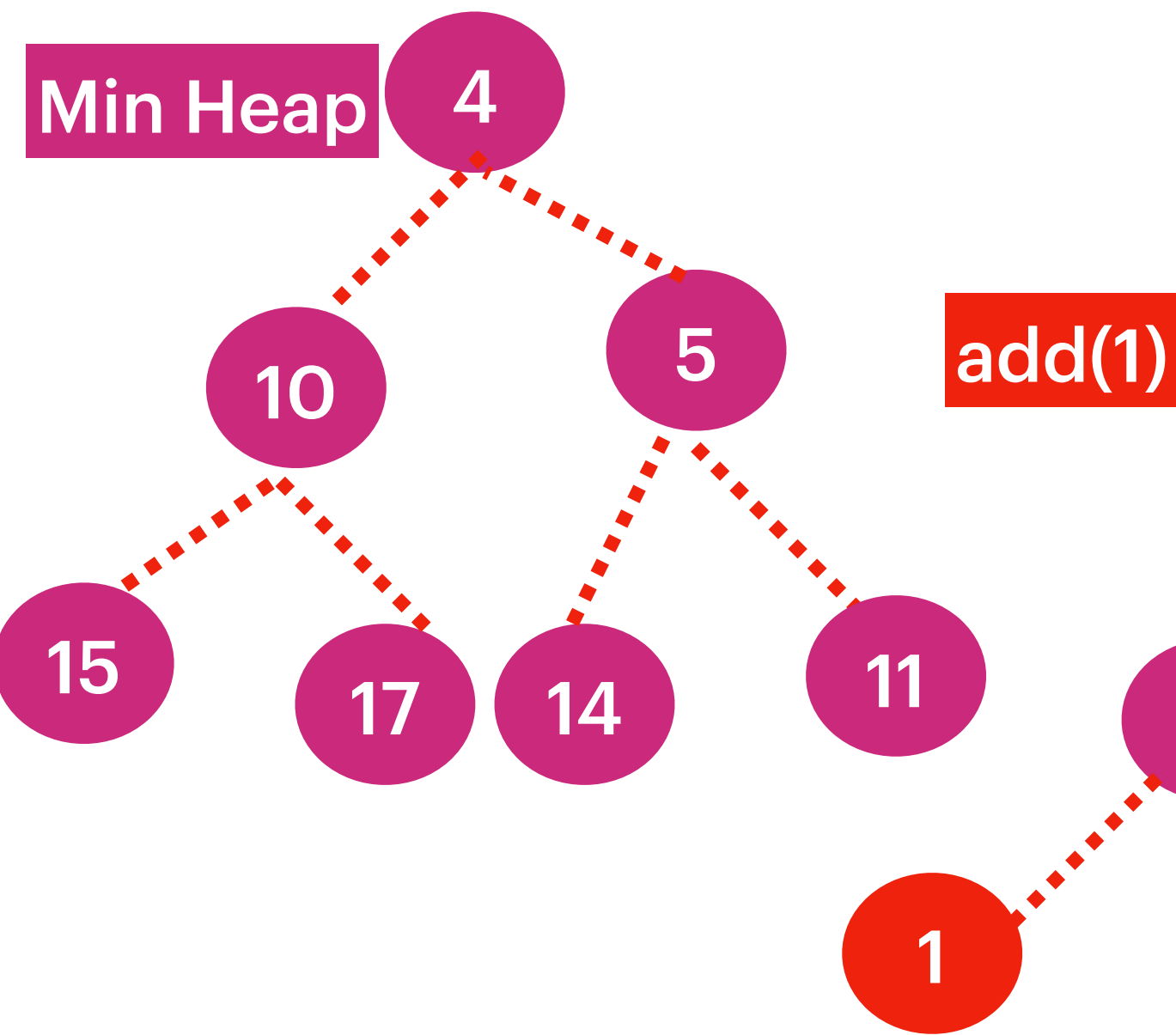
Algorithm :

Add to the RightMost position.  
If the current element  $>$  parent  
then swap.



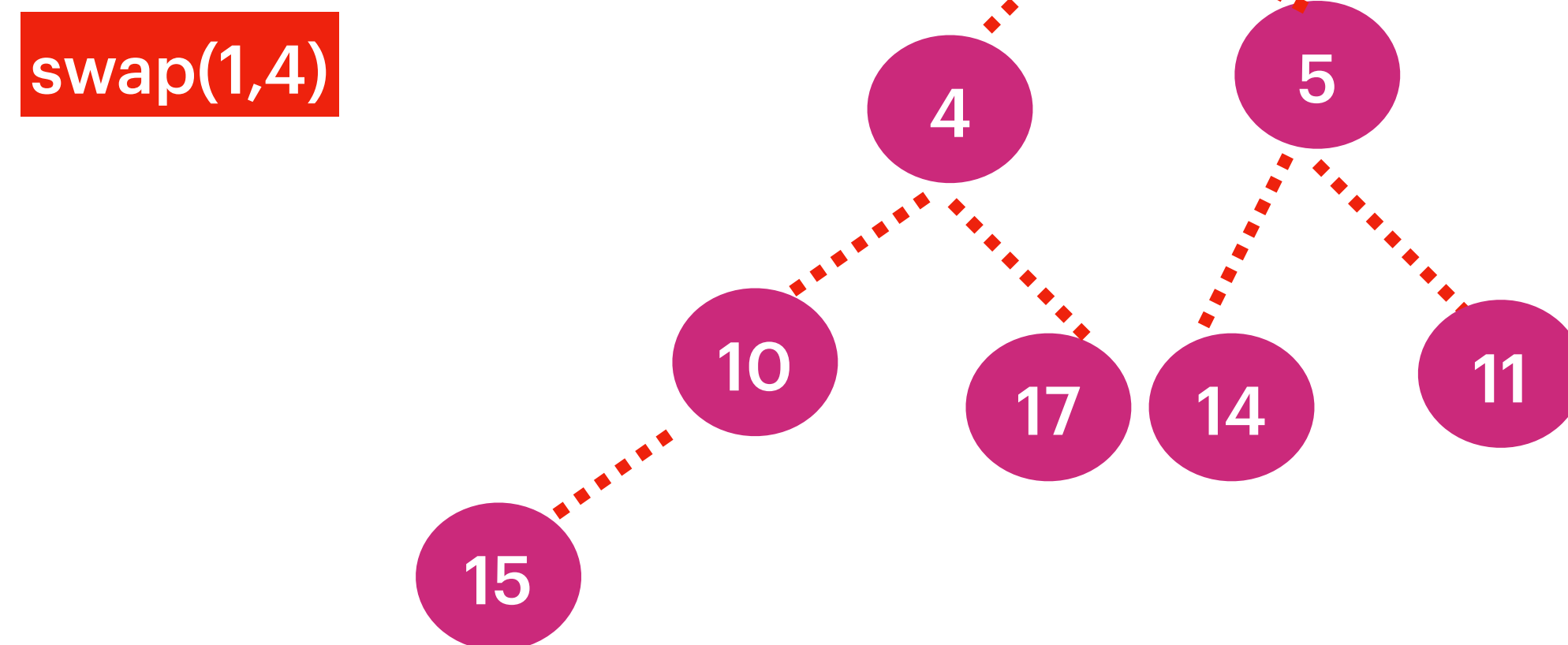
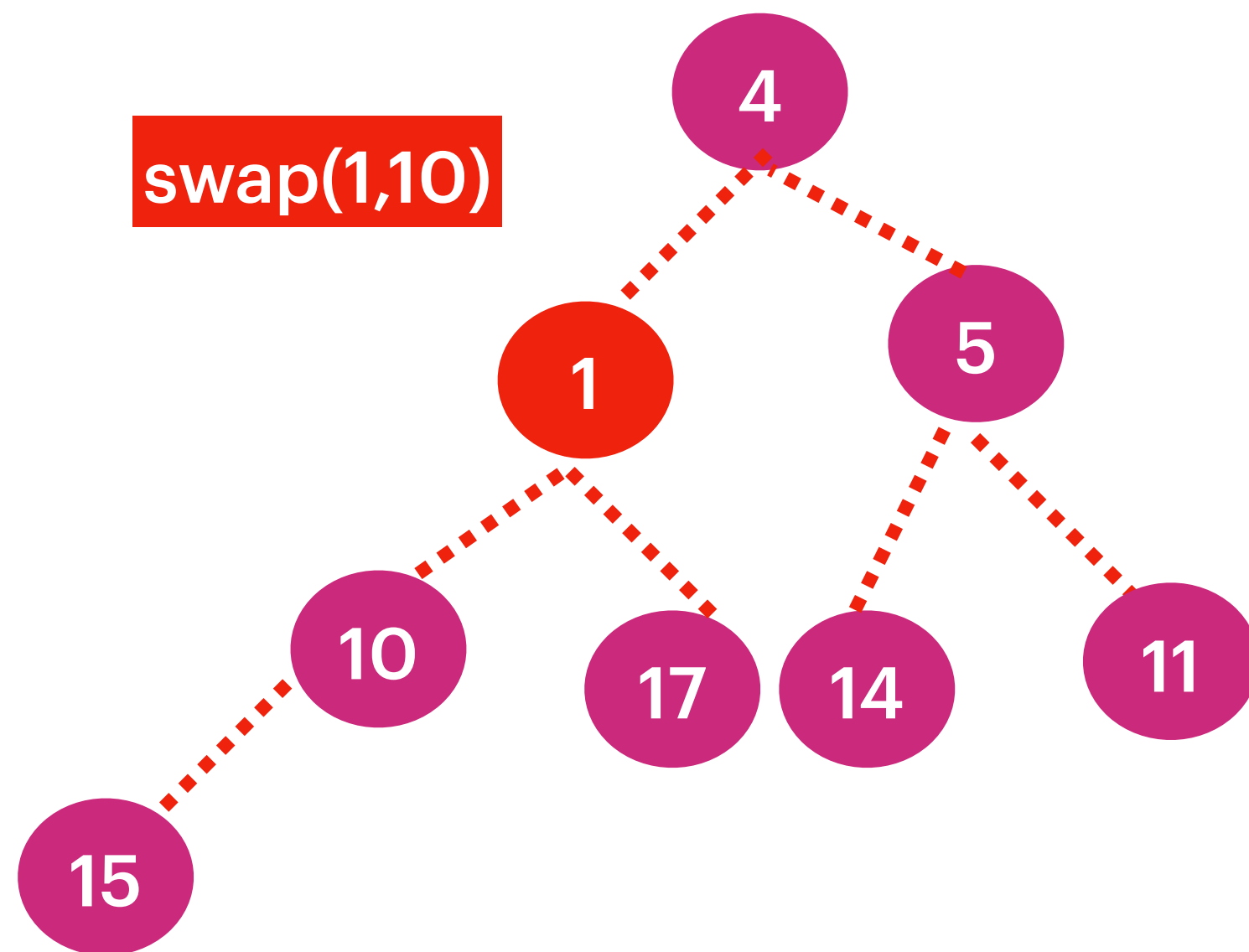
Time Complexity :  $O(\log n)$   
Space Complexity :  $O(1)$



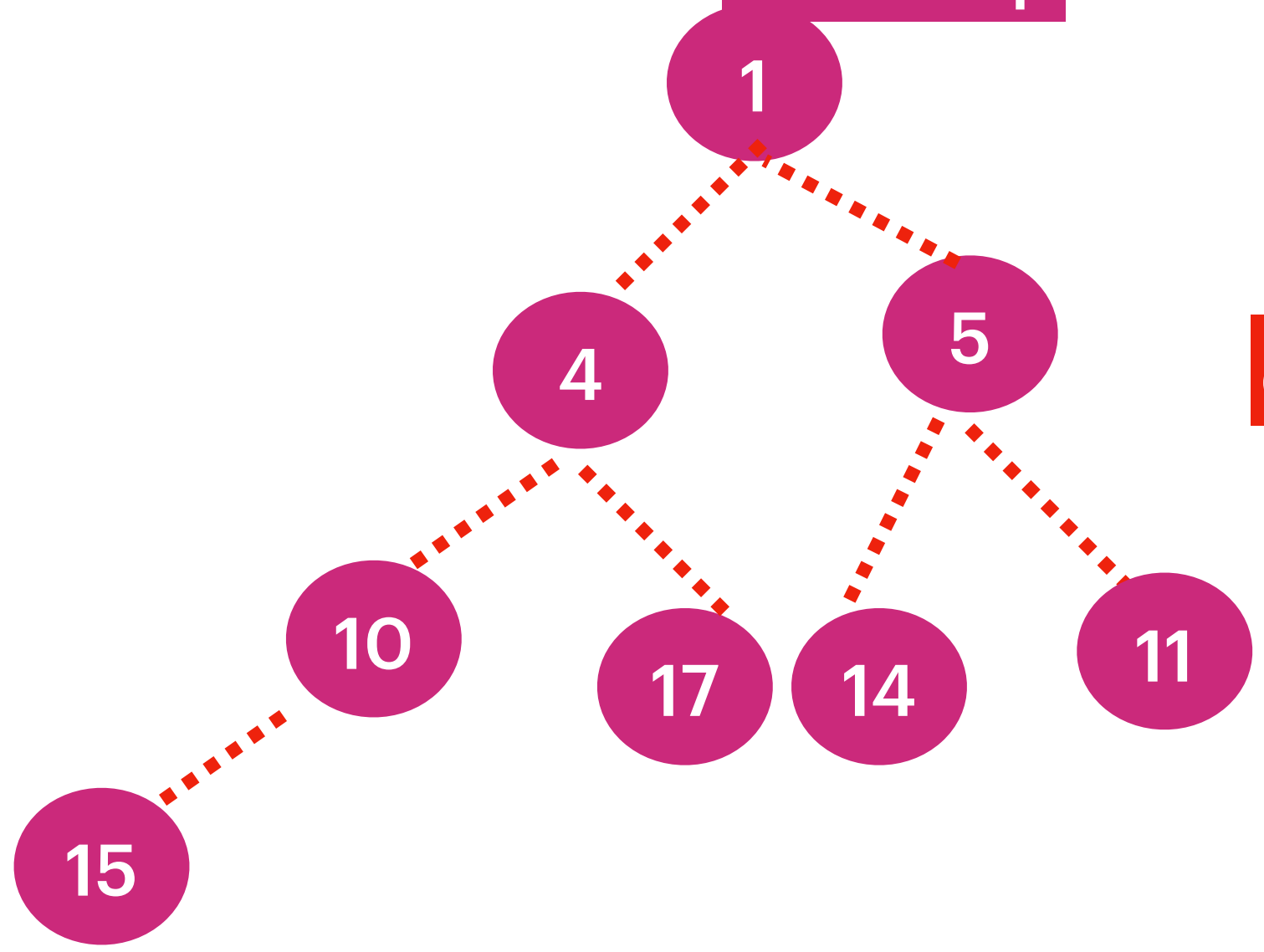


Algorithm :

Add to the RightMost position.  
If the current element > parent  
then swap.

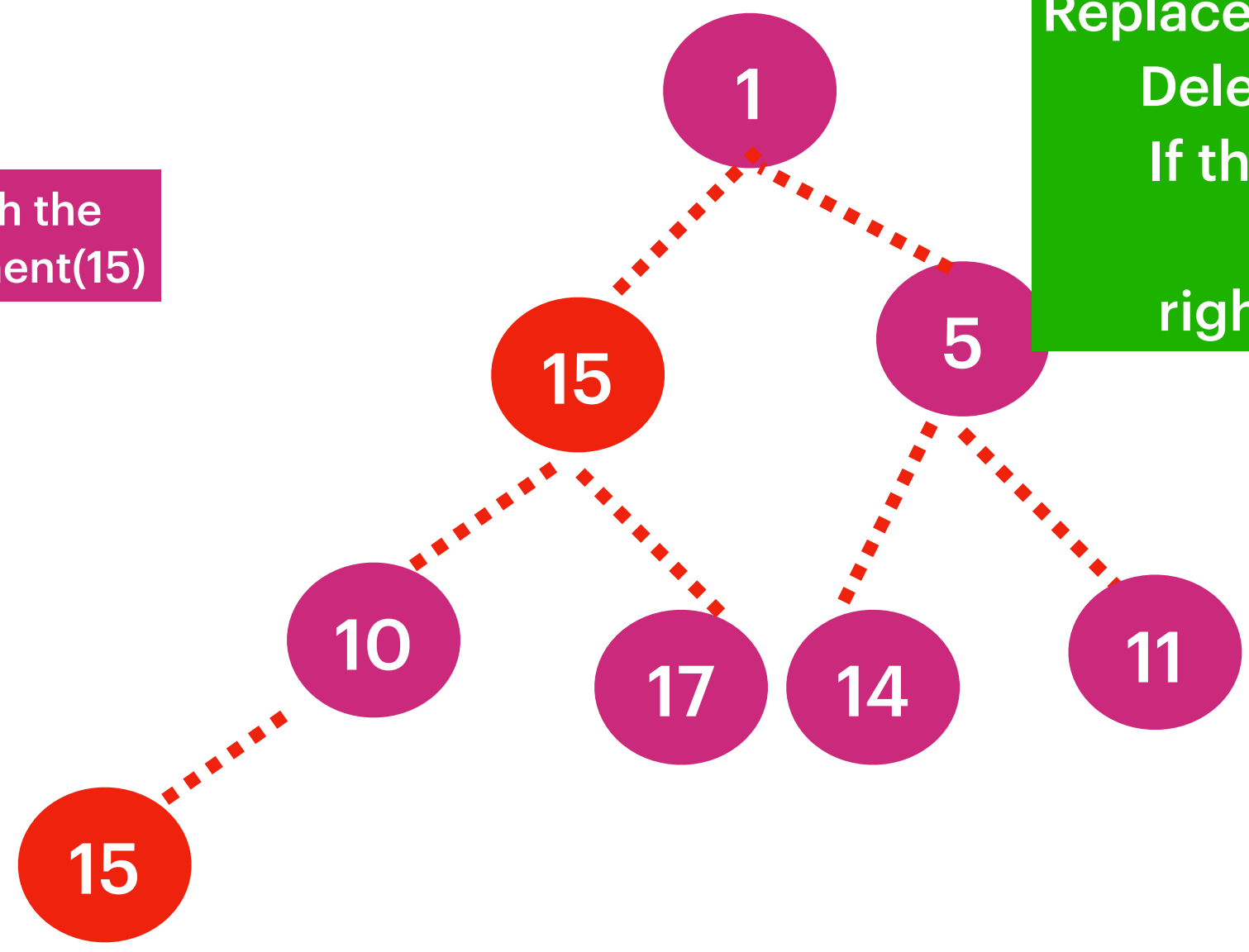


Min Heap



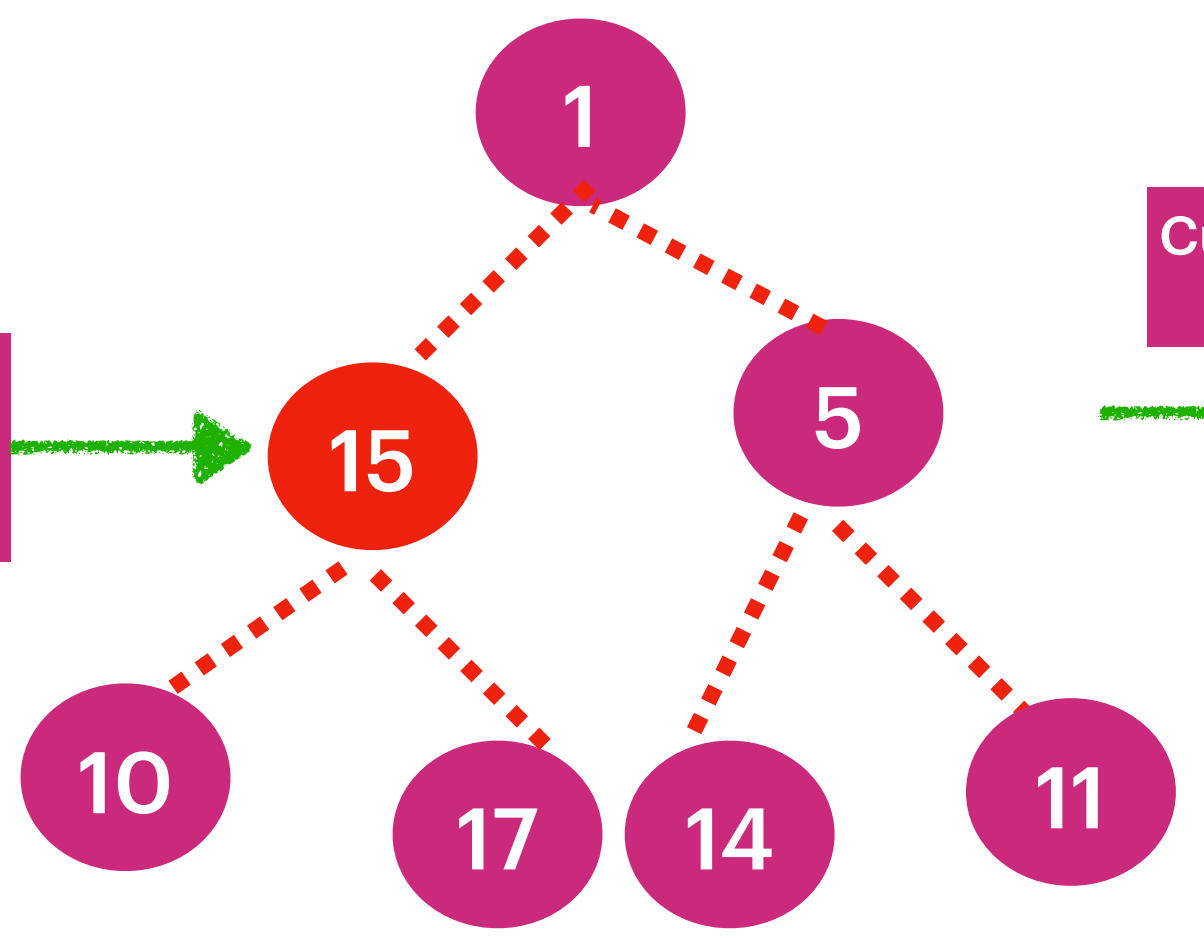
Delete Operation On MinHeap

delete(4) → replace(4) with the Right Most Element(15)

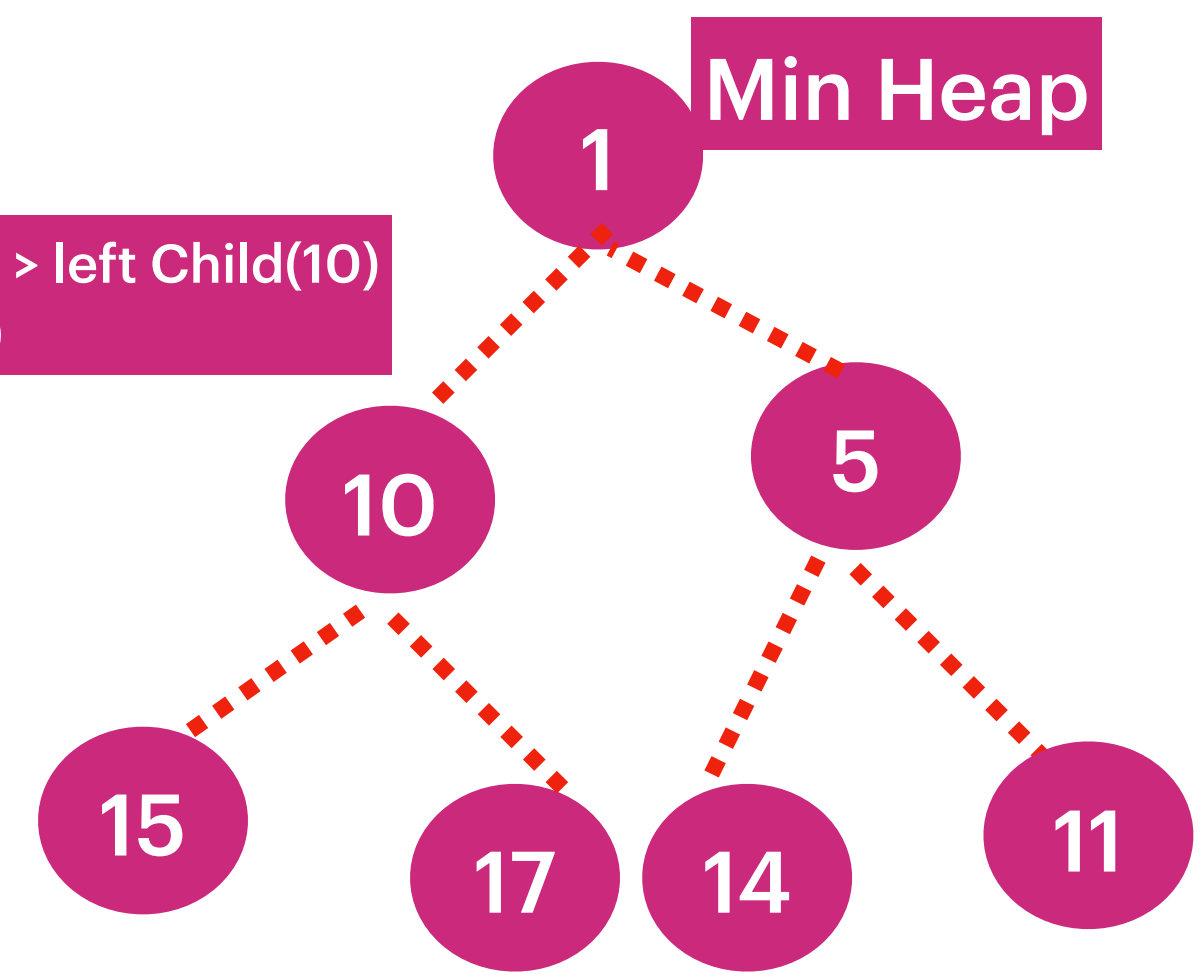


Algorithm :  
Replace with the right most element ,  
Delete the right most element.  
If the current Element either > (leftNode || rightNode) swap accordingly

Delete the Right Most Element(15) in the max level of MinHeap

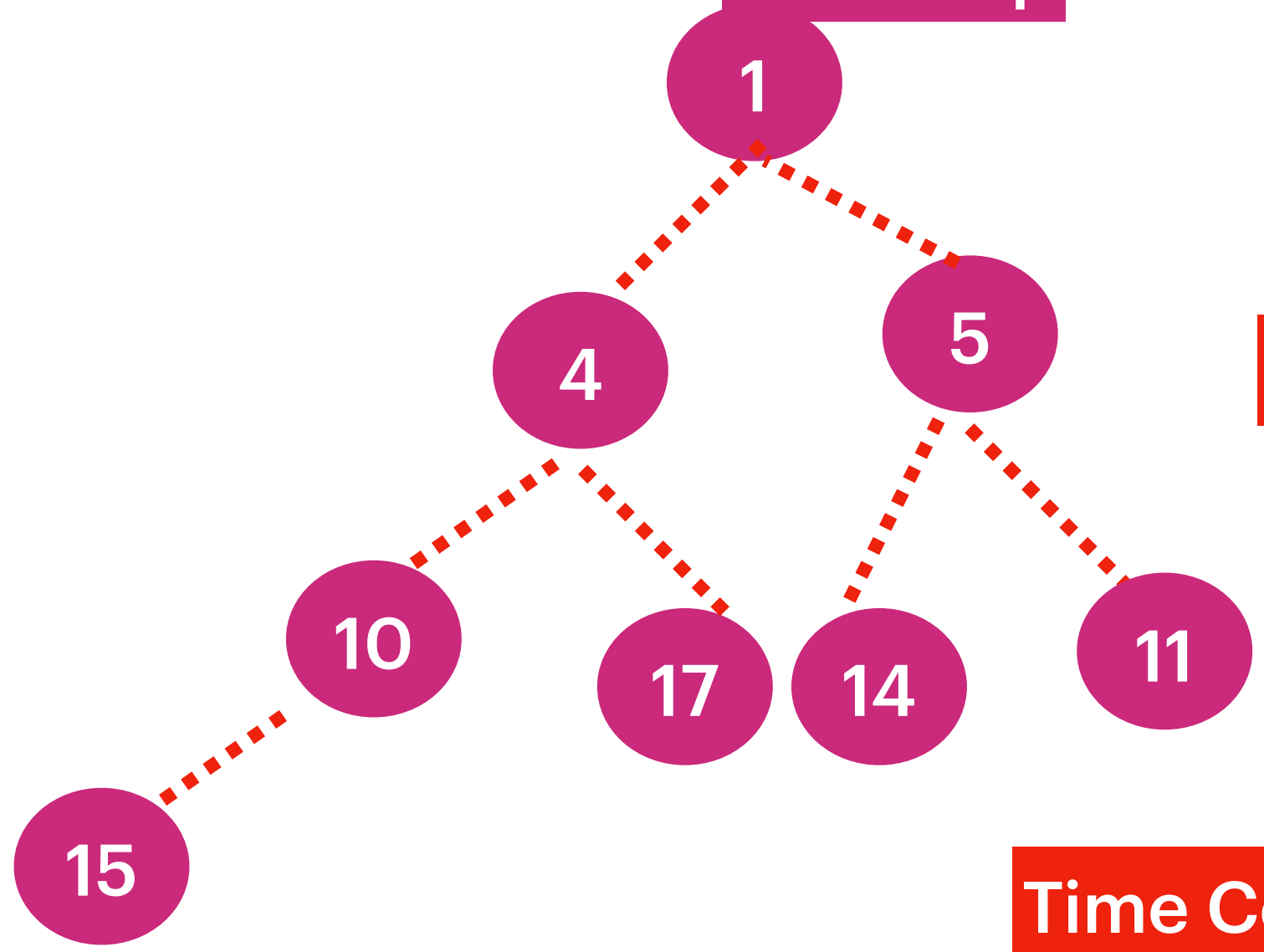


Current Parent(15) which is > left Child(10)  
Swap (10,15)



Min Heap

Min Heap

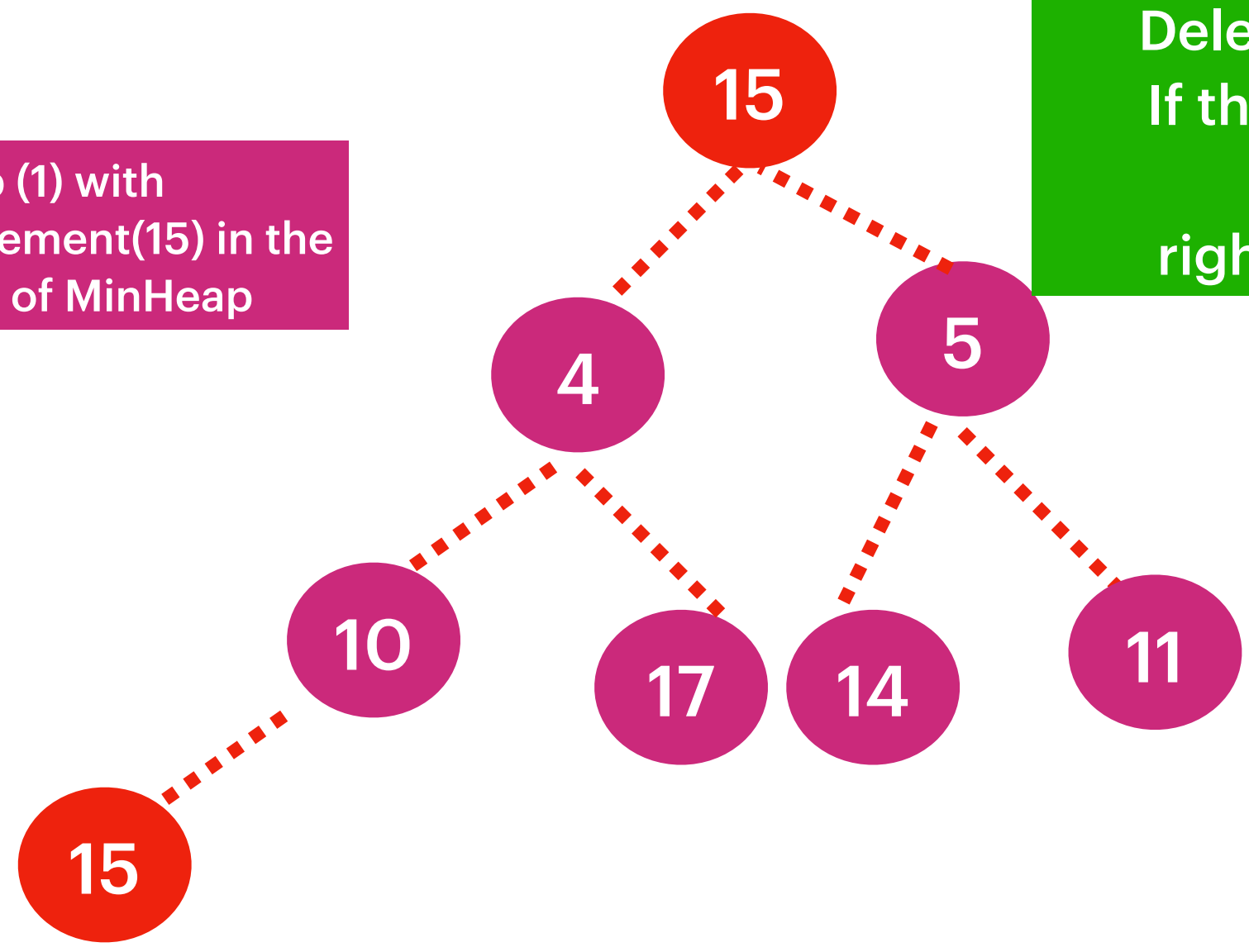


Delete Operation On MinHeap

delete(1)



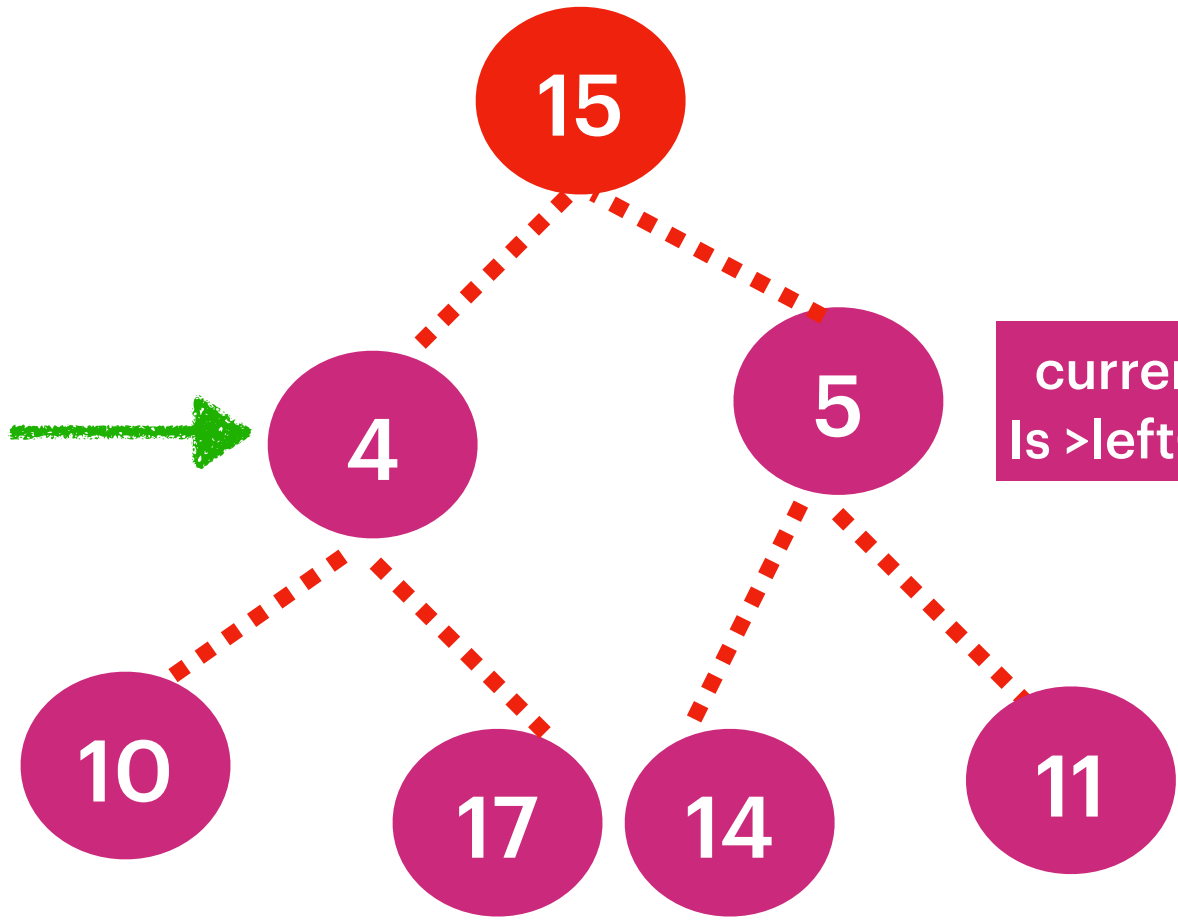
Swap (1) with  
Right Most Element(15) in the  
max level of MinHeap



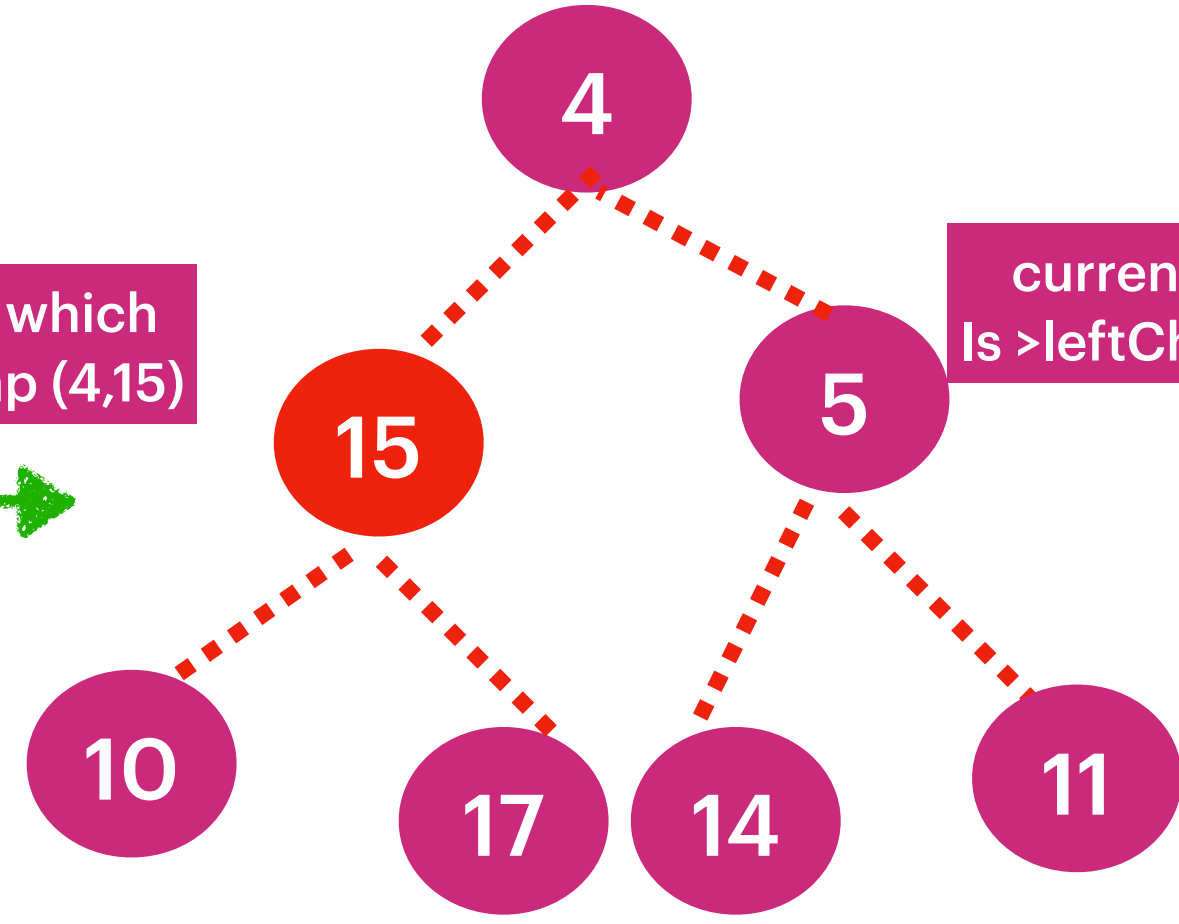
Algorithm :  
Replace with the right most element ,  
Delete the right most element.  
If the current Element either >  
(leftNode ||  
rightNode) swap accordingly

Time Complexity :  $O(\log n)$   
Space Complexity :  $O(1)$

Delete the  
Right Most Element(1) in the  
max level of MinHeap



currentParent(15) which  
Is > leftChild(4) swap (4,15)



currentParent(15) which  
Is > leftChild(10) swap (10,15)

