SOLVING WORD PROBLEMS

Where is she going with this?

- Units
- Steps for solving word problems
- Example
- Lots of exercises!

Using Units

$$\frac{2}{3} \times \frac{2}{5} = \frac{4}{15}$$

$$\frac{2\ \cancel{seek\ care}}{3\ diseased} \times \frac{2\ hospitalized}{5\ \cancel{seek\ care}} = \frac{4\ hospitalized}{15\ diseased}$$

Using Units

$$\frac{\frac{14\ diseased}{100\ at\ risk}}{\frac{3\ diseased}{200\ at\ risk}}$$

$$= \frac{14\ \cancel{diseased}}{100\ \cancel{at\ risk}} \times \frac{200\ \cancel{at\ risk}}{3\ \cancel{diseased}}$$

$$= \frac{2800}{300}$$

$$= 7$$

Using Units

$$\frac{38\ dead}{216\ ill} = \frac{x}{1{,}000\ ill}$$

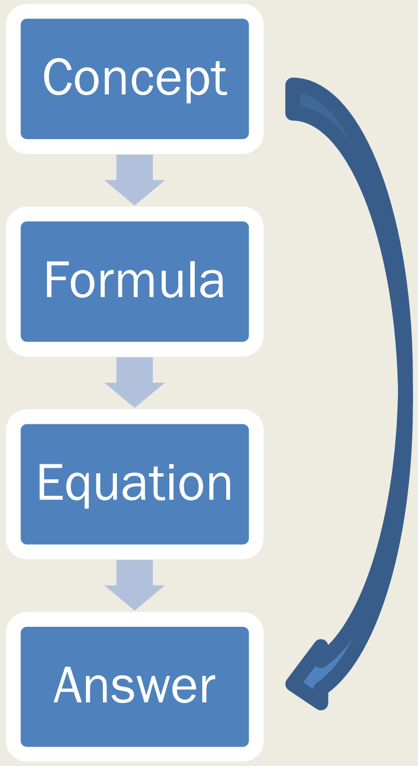
$$\frac{38\ dead}{216\ \cancel{ill}} \times 1{,}000\ \cancel{ill} = \frac{x}{1{,}000\ \cancel{ill}} \times 1{,}000\ \cancel{ill}$$

$$\frac{38{,}000}{216} dead = x$$

$$x = 176\ dead$$

Problem Solving

1. Read the whole problem
2. Identify the question
3. Break down the quantity being asked for
4. Identify useful information
5. Review remaining information
6. Calculate
7. Reflect on your answer



Example: Word Problem

Age (years)	Persons (in 1000's)	Deaths (in 1000's)
Under 5	198	1
5 - 19	580	4
20 - 44	601	1.3
45 - 64	396	4.6
65 and over	185	11.4
All ages	1,960	18.7

Average annual deaths in a population

- In a population of 500,000 how many deaths would you expect in a year?

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Average annual deaths in a population

1. Read the whole problem
2. Identify the question
3. Break down the quantity being asked for
   - *Expected deaths in a year*
4. Identify useful information
5. Review remaining information
6. Calculate
   - *(18.7/1,960)*500,000*
7. Reflect on your answer

Example: Word Problem

- A manufacturer sells products for \$5 per unit. Some retailers add \$1 per unit to the price for consumers. Fixed costs are constant at \$3,000 regardless of the number of units of product involved. Total cost is equal to the sum of fixed costs and variable costs. In this company, variable costs are estimated to be \$2 per unit. What is the breakeven point (i.e. how many units must be sold so that the total costs equal total revenues)?

1. Read the whole problem
2. Identify the question
3. Break down the quantity being asked for
   - $Costs = Revenue$
   - $Costs = Fixed + Variable * Units$
   - $Revenue = Price * Units$
   - $F + V * U = P * U$
4. Identify useful information
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1. Read the whole problem
2. Identify the question
3. Break down the quantity being asked for
   - $F + V * U = P * U$
4. Identify useful information
   - $F = \$3{,}000$
   - $V = \$2$
   - $P = \$5$
5. Review remaining information
6. Calculate
   - $\$3{,}000 + \$2U = \$5U$
7. Reflect on your answer

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1. Read the whole problem
2. Identify the question
3. Break down the quantity being asked for
4. Identify useful information
5. Review remaining information
6. Calculate
   - $\$3{,}000 + \$2U = \$5U$
   - $\$3{,}000 + \$2U - \$2U = \$5U - \$2U$
   - $\$3{,}000 = \$3U$
   - $\frac{\$3{,}000}{\$3} = \frac{\$3U}{\$3}$
   - $1{,}000 = U$
7. Reflect on your answer

EXERCISE

- The following data were obtained for children 6 months through 4 years from the Second NHANES survey, conducted February 1976-February 1980, among 27,801 persons in the United States.

Blood lead level (micrograms/deciliter)	No. examined	% with history of eating unusual substances
≥30	117	16.2
20-29	503	14.1
<20	1,752	5.2

- How many children examined with blood lead levels greater than or equal to 20 micrograms/deciliter had a history of eating unusual substances?

Adapted from Exercises in Epidemiology *by Noel Weiss, 2012.*

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$$\#Eating = \#Examined * \%Eating$$

$$\#Eat_{\geq 20} = \#Eat_{20-29} + \#Eat_{\geq 30}$$

$$\#Eat_{20-29} = \#Ex_{20-29} * \%Eat_{20-29}$$

$$\#Eat_{\geq 30} = \#Ex_{\geq 30} * \%Eat_{\geq 30}$$

$$\#Eat_{\geq 20} = 503 * 0.141 + 117 * 0.162$$

$$\#Eat_{\geq 20} = 90$$

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$$\%Eat_{tot} = \frac{\#Eat_{tot}}{\#Ex_{tot}}$$

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$$\%Eat_{tot} = \frac{\#Eat_{tot}}{\#Ex_{tot}}$$

$$\#Ex_{tot} = \#Ex_{\geq 30} + \#Ex_{20-29} + \#Ex_{<20} = 117 + 503 + 1752 = 2372$$

$$\%Eat_{tot} = \frac{\#Ex_{\geq 30}}{\#Ex_{tot}}(\%Eat_{\geq 30}) + \frac{\#Ex_{20-29}}{\#Ex_{tot}}(\%Eat_{20-29}) + \frac{\#Ex_{<20}}{\#Ex_{tot}}(\%Eat_{<20})$$

$$\%Eat_{tot} = \frac{117}{2372}(0.162) + \frac{503}{2372}(0.141) + \frac{1752}{2372}(0.052) = 0.076 = 7.6\%$$

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$$\%Eat_{\geq 30} = \frac{\#Eat_{\geq 30}}{\#Eat_{tot}}$$

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$$\%Eat_{\geq 30} = \frac{\#Eat_{\geq 30}}{\#Eat_{tot}}$$

$$\%Eat_{\geq 30} = \frac{\#Eat_{\geq 30}}{\#Eat_{\geq 30} + \#Eat_{\geq 30} + \#Eat_{\geq 30}}$$

$$= \frac{\#Ex_{\geq 30}(\%Eat_{\geq 30})}{\#Ex_{\geq 30}(\%Eat_{\geq 30}) + \#Ex_{20-29}(\%Eat_{20-29}) + \#Ex_{<20}(\%Eat_{<20})}$$

$$= \frac{117(0.162)}{117(0.162) + 503(0.141) + 1752(0.052)} = 0.105 = 10.5\%$$

Adapted from Exercises in Epidemiology *by Noel Weiss, 2012.*

EXERCISE

- The following is from a newspaper article on seat belts:

Of the 649 people who died in traffic accidents in Washington last year, 55 percent were not wearing seat belts. In those same fatal crashes, 73 percent of people who were belted in survived without serious injury.

- Can you identify the percent of people who survived these crashes without serious injury and were *not* belted in? If so, calculate it. If not, what quantity would you need to calculate this number?

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$$\frac{Survived_{not\ belted}}{Survived_{tot}}$$

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$$\frac{Survived_{not\ belted}}{Survived_{tot}}$$

- 649 died- 55% not belted, 45% belted

$$\frac{Died_{not\ belted}}{Died_{tot}} = \frac{Died_{not\ belted}}{649} = 0.55$$

- X belted- 73% survived, 27% died

$$\frac{Belted_{surv}}{Belted_{tot}} = \frac{Surv_{belted}}{Belted_{tot}} = 0.73$$

NOT ENOUGH INFORMATION

Adapted from Exercises in Epidemiology *by Noel Weiss, 2012.*

EXERCISE

- The rate of suicide among American physicians, relative to the corresponding rate in the population as a whole, varies by gender. Among men, the rate in physicians is 1.5 times higher, whereas among women the corresponding relative rate is 3.0. It turns out that the rate of suicide in American male and female physicians is identical. For American men and women in general, what is the relative rate of suicide in men compared to women?

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$$\frac{Suicide\ Rate_{American\ men}}{Suicide\ Rate_{American\ women}}$$

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$$\frac{Suicide\ Rate_{American\ men}}{Suicide\ Rate_{American\ women}}$$

$$S_{P.M.} = S_{P.F.} = S_P$$

$$\frac{S_P}{S_{A.M.}} = 1.5 \rightarrow S_{A.M.} = \frac{S_P}{1.5}$$

$$\frac{S_P}{S_{A.F.}} = 3.0 \rightarrow S_{A.F.} = \frac{S_P}{3.0}$$

$$\frac{S_{A.M.}}{S_{A.F.}} = \frac{\frac{S_P}{1.5}}{\frac{S_P}{3.0}} = \frac{S_P}{1.5} \times \frac{3.0}{S_P} = 2$$

Taken from Exercises in Epidemiology *by Noel Weiss, 2012.*