

# Design considerations for subgroup analyses in cluster- randomized trials

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17 July, 2024

<https://bdwilliamson.github.io/#talks>

# Acknowledgments

This work was done in collaboration with:



**Yates Coley**

 **KAISER PERMANENTE®**  
Kaiser Permanente Washington  
Health Research Institute



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Health Research Institute



**Courtney McCracken**

 **KAISER PERMANENTE®**  
**CRE** Center for  
Research and Evaluation



**Andrea Cook**

 **KAISER PERMANENTE®**  
Kaiser Permanente Washington  
Health Research Institute

and was funded by the Patient-Centered Outcomes Research Institute (COVID-2021C2-1368)

# Heterogeneity of treatment effects: what and why

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If HTE is present:

- resources can be prioritized to maximize benefit and reduce risks [Knol and VanderWeele (2012)]
- can determine whether intervention remediates or exacerbates health disparities [Petkovic et al. (2020)]

# Case study: ENSPIRE trial

**ENSPIRE:** Engaging Staff to Improve COVID-19 Vaccination Response at Long-term Care Facilities

Background:

- Rates of COVID-19 disease and death higher in long-term care than general population [Chidambaram (2022)]
- Lag in COVID-19 vaccinations among long-term care workers
- Long-term care (LTC) workers often low-wage, represent diverse social, cultural, racial, and ethnic backgrounds

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Design:

- Enrolled 40 LTC centers, encompassing approximately 4000 staff members
- Recruited from 2 US states (Georgia and Washington)
- Recruited from urban (Atlanta or Seattle) and suburban/rural locations

# Case study: ENSPIRE trial

## Primary outcomes:

1. LTC center COVID-19 booster rate (**cluster-level**)
  - chosen due to concerns about data capture
2. LTC care staff net promoter score (**individual-level**)

**Intervention:** booster promotion materials co-designed with LTC staff

"Usual care"  
(Standard materials)



VS.

"Co-design"  
(Materials designed by teams of staff)



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HTE analysis natural for interventions, particularly co-designed:

- Planned analyses based on state, urban vs suburban/rural, baseline booster uptake
- Self-reported race and ethnicity both interesting and important, however:
  - neither sites nor other entity had comprehensive and accurate race and ethnicity data for staff
  - staff survey would only capture a portion of staff members
  - also, didn't know what this would look like with a cluster-level outcome!

# Individual-level data structure

Data on  $n_c$  staff members in each cluster  $c = 1, \dots, K$ :

- $A_{ci}$ : indicator of intervention assignment (cluster-level)
- $Z_{ci} \in \mathbb{R}^q$ : cluster-level subgroup variables
- $W_{ci} \in \mathbb{R}^p$ : baseline covariates
- $Y_{ci}$ : binary outcome

# HTE with individual-level outcomes

Suppose we are interested in HTE by a single binary variable  $W_{ci}$ .

Target estimand: the **difference in the risk difference** based on levels of  $W_{ci}$ .

Estimate using linear regression:

$$E(Y_{ci} \mid A_{ci} = a, Z_{ci} = z, W_{ci} = w) = \beta_0 + \beta_1 a + \beta_2 z + \beta_3 w + \beta_4 aw.$$

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Under standard assumptions,  $\beta_4$  quantifies HTE.

# Cluster-level data structure

In many settings, we observe cluster-level data:

- $\bar{Y}_c := \frac{1}{n_c} \sum_{i=1}^{n_c} Y_{ci}$ : cluster-level outcome proportion
- $A_c$ : indicator of intervention assignment
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Possible options for aggregating an individual-level covariate  $W_{cj}$ :

- $X_{cj} = V_{cj} - \frac{1}{K} \sum_{c=1}^K V_{cj}$ , where  $V_{cj} = \frac{1}{n_c} \sum_{i=1}^{n_c} W_{cji}$
- $X_{cj} = I(V_{cj} > t)$  for threshold  $t$

# Aggregated data: complications

Individual-level effects **may not be identifiable** based on aggregate data

- Often referred to as **ecological bias** [Wakefield (2008)]
- Exposure–outcome association can be biased: [Greenland & Morgenstern (1989)]
  - by aggregated confounders
  - by aggregated HTE variables

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Compositional data cause challenges in **interpretation**:

- Arise when aggregating mutually-exclusive binary variables
- Changing the value of one proportion **necessarily changes** at least one other



# HTE with cluster-level outcomes

Now, outcome  $\bar{Y}_c$  is a proportion; interest in HTE by single variable  $X_c$ .

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If  $W$  is compositional, this is further complicated:

- how are the categories transformed to enable model fitting?
- what does a one-unit change imply?

# Simulation setup

Data mimic ENSPIRE trial:

- Sample  $K \in \{30, 40, 80\}$  clusters within two regions
- Clusters are urban or suburban/rural
- Randomization constrained to balance on region, urban vs suburban/rural
- Each center has 100 staff members, who each:
  - have record of receiving COVID-19 booster vaccine
  - have self-reported race (recorded as single binary variable)
- Define cluster-level booster rate  $\bar{Y}_c$
- Define two aggregations of self-reported race:
  - center-level proportion
  - indicator of whether proportion  $> 0.5$

# Simulation setup

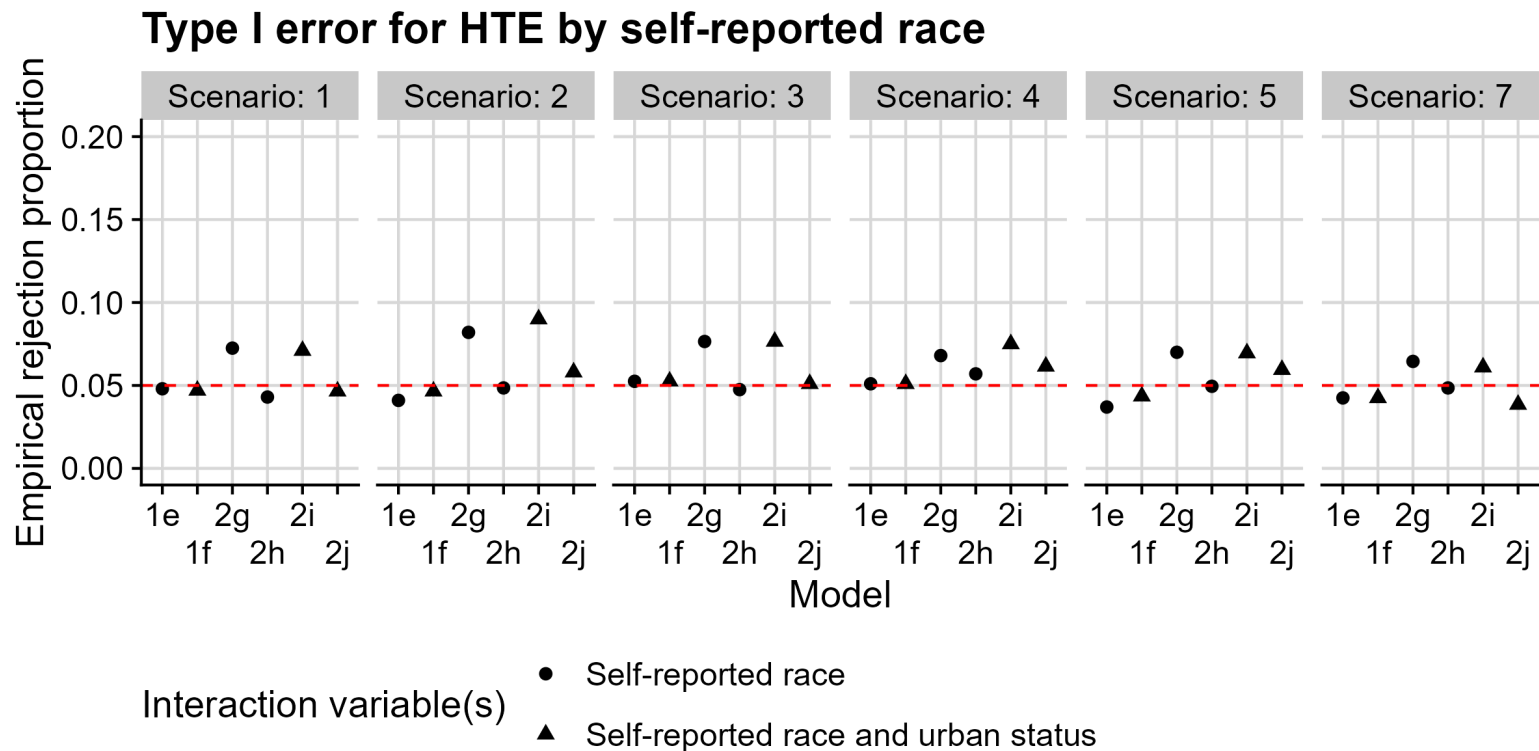
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Fit both **individual-level** and **cluster-level** regression models

Tested for HTE by self-reported race, investigated **type I error and power**

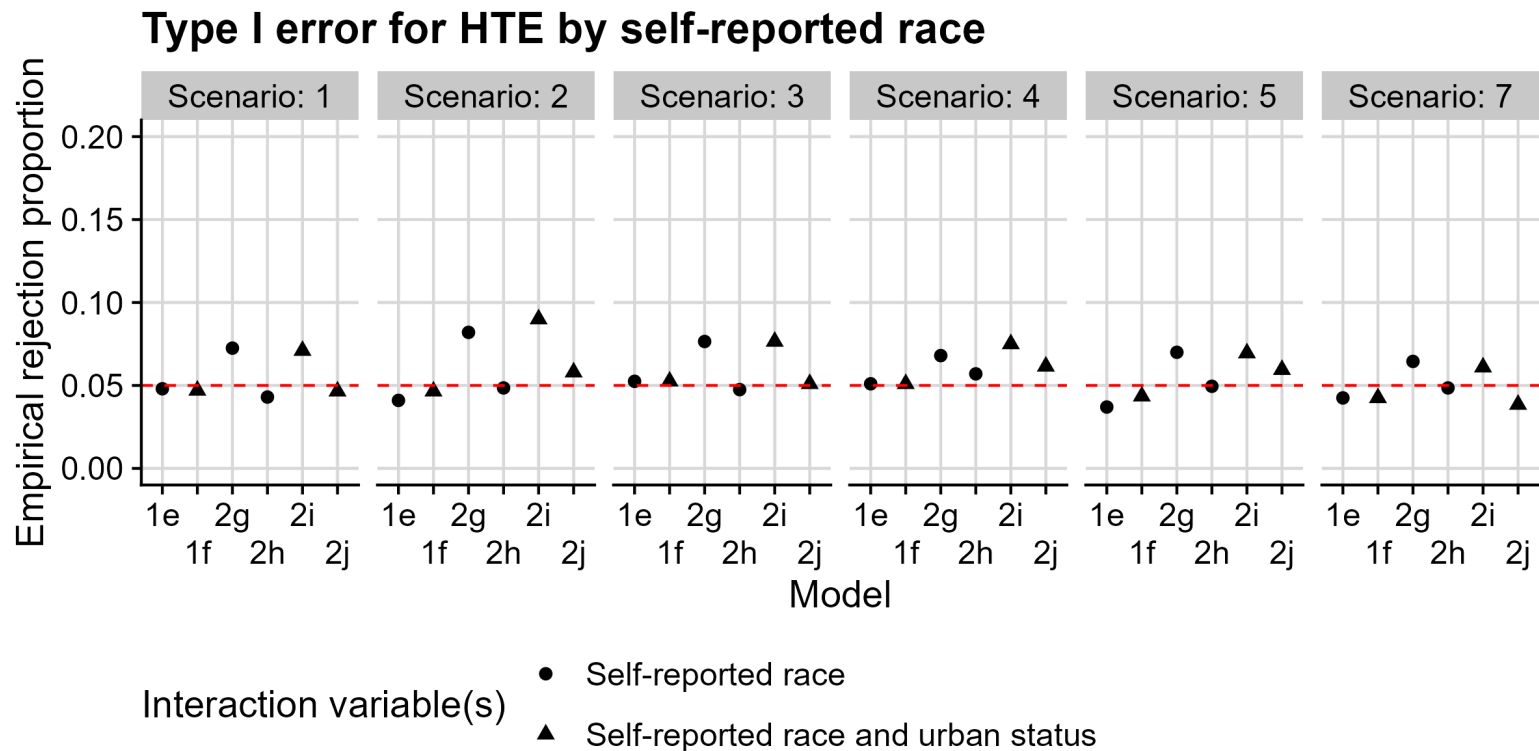
# Results: type I error



Scenarios encode presence of true differences in booster rate or HTE:

- 1, 2, 5: no difference in booster rate by self-reported race, no HTE
- 3, 4, 7: difference in booster rate by self-reported race, no HTE

# Results: type I error

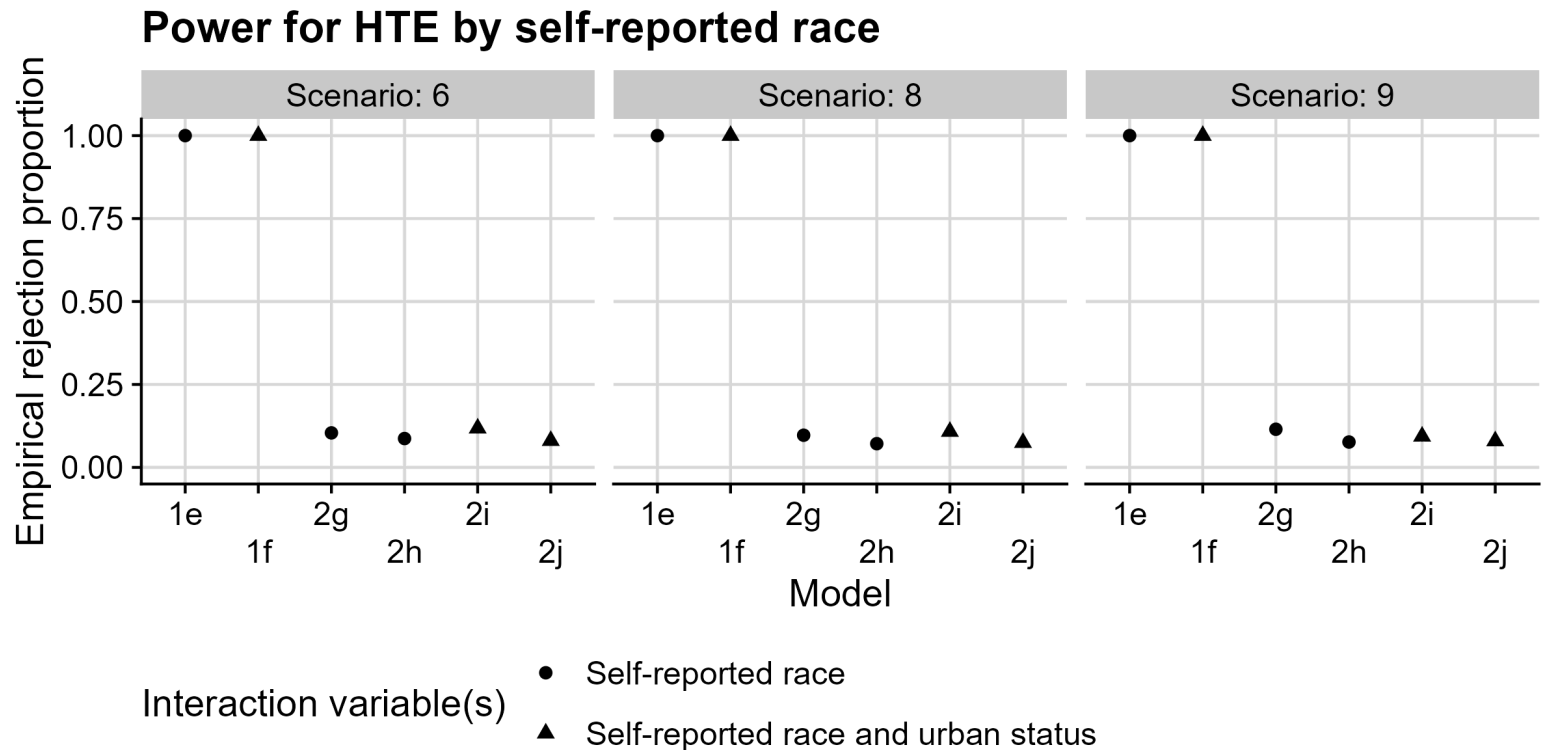


Models encode individual- (1) vs cluster-level (2), adjustment and interaction variables:

- 1e, 1f: adjust for self-reported race, allow HTE by self-reported race (1f also by urban)
- 2g, 2i: adjust for center-level race proportion, allow HTE by self-reported race (2i also by urban)
- 2h, 2j: adjust for proportion > 0.5, allow HTE by self-reported race (2j also by urban)



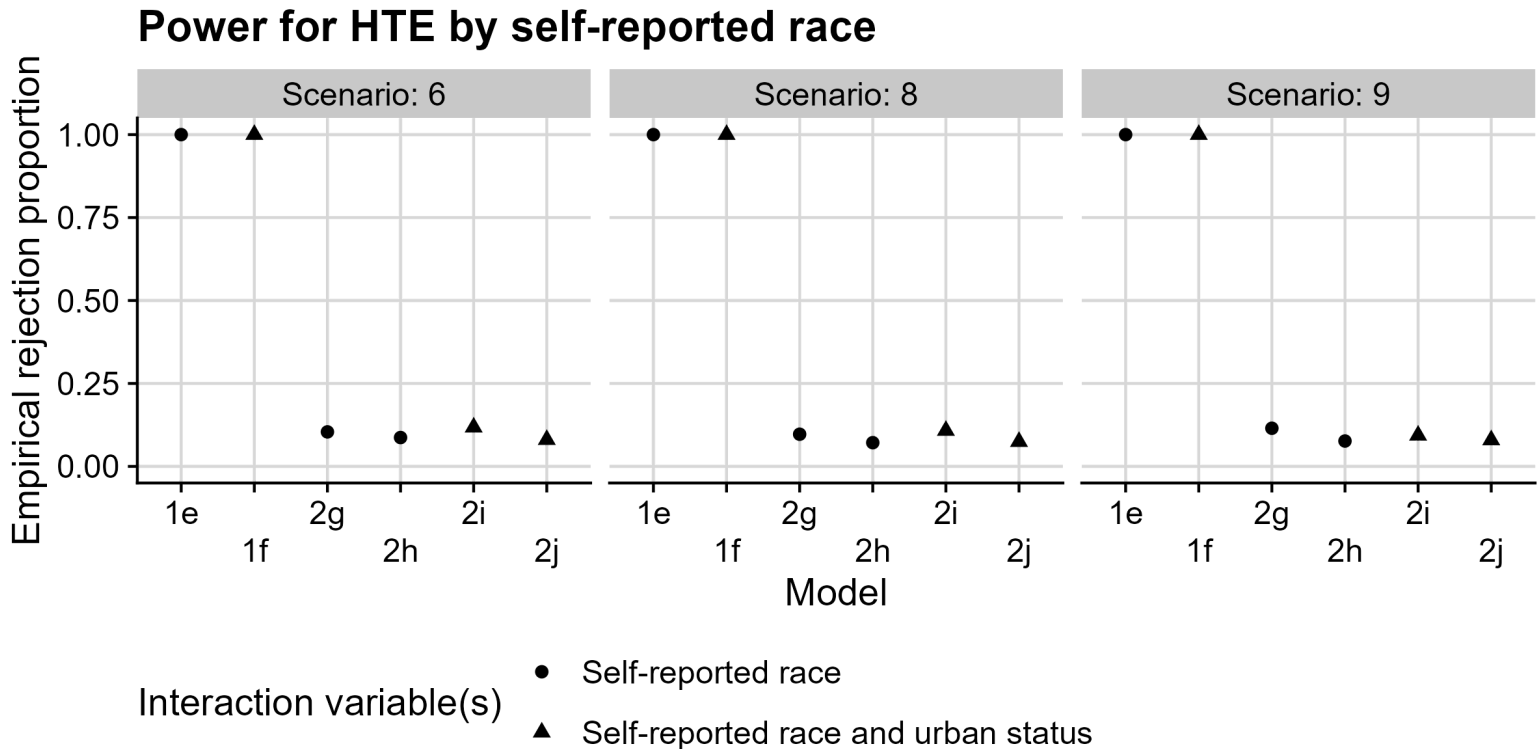
# Results: power



Scenarios encode presence of true differences in booster rate or HTE:

- 6: difference in booster rate by self-reported race, HTE by self-reported race
- 8: difference in booster rate by urban and self-reported race, HTE by self-reported race
- 9: difference in booster rate by urban and self-reported race, HTE by urban and self-reported race

# Results: power



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# Closing thoughts

High power, controlled type I error to detect HTE in the individual-level analysis

- where possible, this approach is key for identifying and remedying disparities

Low power to detect HTE by an aggregated individual-level predictor

- even in simple setting with only two possible categories!
- likely exacerbated in more realistic settings
- elevated type I error when using proportion in some settings

However, meaningful estimated differences across groups can still be acted upon

Power calculations should aggregate simulated individual-level data, rather than simulating cluster-level data directly.

For more details, including more realistic simulation settings:

Williamson BD, Coley RY, Hsu C, McCracken CE, Cook AJ (2023). Considerations for subgroup analyses in cluster-randomized trials based on individual-level predictors. *Prevention Science*.

# References

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