

3. Express the following angles into Sexagesimal seconds;

i) 20°

→ Soln

Here,

$$20^\circ = (20^\circ \times 60' \times 60'')''$$

$$= (1200' \times 60'')''$$

$$\therefore 20^\circ = 72000''$$

$$\begin{array}{r} 60 \\ \times 20 \\ \hline 00 \\ 1200 \\ \hline 1200 \end{array}$$

ii) 65°

→ Solⁿ

Here,

$$65^{\circ} = (65 \times 60 \times 60)''$$

$$\therefore 65^{\circ} = 234000''$$

iii) 70°

→ Solⁿ

Here,

$$70^{\circ} = (70 \times 60 \times 60)''$$

$$\therefore 70^{\circ} = 252000''$$

iv) $10^{\circ}40'$
→ Solⁿ

Here,

$$\begin{aligned} 10^{\circ}40' &= (10 \times 60 + 40)' \\ &= (600 + 40)' \\ &= 640' \end{aligned}$$

Now,

$$\begin{aligned} \cancel{600}640' &= [640 \times 60]'' \\ &= 38400'' \end{aligned}$$

$$\therefore 10^{\circ}40' = 38400''$$

4) Express the following angles into centesimal seconds;

i) 16^g
→ Solⁿ

Here,

$$\begin{aligned} 16^g &= [16 \times 100 \times 100]'' \\ \therefore 16^g &= 160000'' \end{aligned}$$

ii) 42^9

→ Solⁿ

Here,

$$42^9 = [42 \times 100 \times 100]^9$$

$$\therefore 42^9 = 420000^9$$

iii) 50^9

→ Solⁿ

Here,

$$50^9 = [50 \times 100 \times 100]^9$$

$$\therefore 50^9 = 500000^9$$

iv) $80^9 80^1$

→ Solⁿ

Here,

$$80^9 80^1 = [80 \times 100 + 80]^1$$

$$= [8000 + 80]^1$$

$$= 8080^1$$

Now,

$$8080^1 = [8080 \times 100]^9 = 808000^9$$

$$\therefore 80^9 80^1 = 808000^9$$

5) Express the following sexagesimal seconds into degree:

i) $43200''$

→ Soln

Here,

$$43200'' = \left[\frac{43200}{60 \times 60} \right]^\circ$$

$$\therefore 43200'' = 12^\circ$$

ii) $126000''$

→ Soln

Here,

$$126000'' = \left[\frac{126000}{60 \times 60} \right]^\circ$$

$$\therefore 126000'' = 35^\circ$$

iii) $201600''$

→ Soln

Here,

$$201600'' = \left[\frac{201600}{60 \times 60} \right]^\circ$$

$$\therefore 201600'' = 56^\circ$$

iv) $91800''$

→ Soln,

Here,

$$91800'' = \left[\frac{91800}{60 \times 60} \right]^\circ$$

$$\therefore 91800'' = 25.5^\circ$$

6) Express the following centesimal seconds into grade:

a) $180000''$

→ Soln,

Here,

$$180000'' = \left[\frac{180000}{100 \times 100} \right]^g$$

$$\therefore 180000'' = 18^g$$

ii) $460000''$

→ Soln,

Here, $460000'' = \left[\frac{460000}{100 \times 100} \right]^{\circ}$

$\therefore 460000'' = 46^{\circ}$

iii) $720000''$

→ Soln

Here,

$720000'' = \left[\frac{720000}{100 \times 100} \right]^{\circ}$

$\therefore 720000'' = 72^{\circ}$

iv) $335600''$

→ Soln

Here,

$335600'' = \left[\frac{335600}{100 \times 100} \right]^{\circ}$

$\therefore 335600'' = 33.56^{\circ}$

7(i) Express an angle of a square

into grade.

→ Soln

Here,

Angle of a square = 90°

We have,

$$1^\circ = \left[\frac{10}{9} \right]^g$$

$$\text{or, } 90^\circ = \left[\frac{10 \times 90}{9} \right]^g$$

$$\therefore 90^\circ = [100]^g$$

\therefore Angle of square in grade = 100^g

7(ii) Express an angle of an equilateral triangle into grade.

→ Soln

Here,

Angle of an equilateral triangle = 60°

We have,

$$1^\circ = \left[\frac{10}{9} \right]^9$$

$$\text{or, } 60^\circ = \left[\frac{10}{9} \times \frac{20}{60} \right]^9$$

$$\therefore 60^\circ = \left[\frac{200}{3} \right]^9$$

\therefore Angle of an equilateral triangle = $\left[\frac{200}{3} \right]^9$.