

Assignment

Factorisation

Exercise 22(I)

1. Factorise:

a) $xy + yz$

→ Soln

$$xy + yz = y(x + z)$$

b) $3ax + 4a$

→ Soln

$$3ax + 4a = a(3x + 4)$$

c) $2x + 6y$

→ Soln

$$2x + 6y = 2(x + 3y)$$

→

d) $2x^2 + 4x$

→ Soln

$$2x^2 + 4x = 2x(x + 2)$$

e) $4ax^2 - 6ax$

→ Soln

Here,

$$4ax^2 - 6ax = 2ax(2x - 3)$$

f) $10ab^2 - 15a^2b$

→ Soln

$$10ab^2 - 15a^2b = 5ab(2b - 3a)$$

g) $2a^2x^2 - 6abx + 4ab^2x^3$

→ Soln

$$2a^2x^2 - 6abx + 4ab^2x^3 = 2ax(ax - 3b + 2b^2x^2)$$

h) $12p^3x^2 - 15p^2x^3 + 9p^2x^2$

→ Soln

$$12p^3x^2 - 15p^2x^3 + 9p^2x^2 =$$

$$3p^2x^2(4p - 5x + 3)$$

$$3p^2x^2(4p - 5x + 3)$$

2. Resolve into factors:

a) $a(x+a) + b(x+a)$

$\rightarrow (x+a)(a+b)$

b) $p(x-y) - q(x-y) - q(x-y)$

$\rightarrow (x-y)(p-q)$

c) $x(y+3) - 4(y+3)$

$\rightarrow (y+3)(x-4)$

d) $2y(x-5) + 3(x-5)$

$\rightarrow (x-5)(2y+3)$

e) $3x(2x+3) - 5(2x+3)$

$\rightarrow (2x+3)(3x-5)$

f) $2x(x+y-z) - y(x+y-z) + 3z(x+y-z)$

$\rightarrow (x+y-z)(2x-y+3z)$

\rightarrow

3) Factorise;

a) $amtbn + antbm$

$$\rightarrow \cancel{(am+bn)(an+bm)} - m(a-b)$$

$$\rightarrow (am+an)(bm+bn)$$

$$\rightarrow a(m+n) + b(m+n)$$

$$\rightarrow (m+n)(a+b)$$

b) $x^2 + 2x + 3x + 6$

$$\rightarrow (x^2 + 2x) + (3x + 6)$$

$$\rightarrow x(x+2) + 3(x+2)$$

$$\rightarrow \underline{(x+2)(x+3)}$$

c) $xy - 3x + y^2 - 3y$

$$\rightarrow (xy - 3x) + (y^2 - 3y)$$

$$\rightarrow x(y-3) + y(y-3)$$

$$\rightarrow \cancel{(x+y)} (y-3)(x+y)$$

d) $mn + 5m + 6n + 30$

$$\rightarrow (mn + 5m) + (6n + 30)$$

$$\rightarrow m(n+5) + 6(n+5)$$

$$\rightarrow \underline{(n+5)(m+6)}$$

$$e) pq - 3p + 4q - 12$$

$$\rightarrow (pq - 3p) + (4q - 12) = p(q - 3) + 4(q - 3)$$

$$= (q - 3)(p + 4)$$

$$f) 2p^2 - 3pq + 2pr - 3qr$$

$$\rightarrow (2p^2 - 3pq) + (2pr - 3qr)$$

$$\rightarrow p(2p - 3q) + r(2p - 3q)$$

$$\rightarrow (2p - 3q)(p + r)$$

$$g) xy - x + y - 1$$

$$\rightarrow (xy - x) + (y - 1)$$

$$\rightarrow x(y - 1) + 1(y - 1)$$

$$\rightarrow (y - 1)(x + 1)$$

$$h) x^3 + 2x^2y - 2xy - 4y^2$$

$$\rightarrow (x^3 + 2x^2y) - (2xy + 4y^2)$$

$$\rightarrow x^2(x + 2y) - 2y(x + 2y)$$

$$\rightarrow x^2(x + 2y) - 2y(x + 2y)$$

$$\rightarrow (x + 2y)(x^2 - 2y)$$

→

i) $a^2 - (b-1)a - b$

$\rightarrow \cancel{a^2 - b + 1a - b} = a(a-b) + 1(a-b)$

$\rightarrow a(a-b) + 1(a-b)$

$\rightarrow (a-b)(a+1)$

j) $x^2 - (a+b)x + ab$

$\rightarrow (x^2 - ax)(bx + ab)$

$\rightarrow x(x-a) - b(x-a)$

$\rightarrow (x-a)(x-b)$

k) $x^2 - (a+2b)x + 2ab$

$\rightarrow (x^2 - ax)(-2bx + 2ab)$

$\rightarrow x(x-a) - 2b(x-a)$

$\rightarrow (x-a)(x-2b)$

l) $ab(x^2 + y^2) - xy(a^2 + b^2)$

$\rightarrow \cancel{(abx^2 + aby^2)} - \cancel{a^2xy - b^2xy}$

$\rightarrow ab(x^2 + y^2)$

$\rightarrow abx^2 + aby^2 - a^2xy - b^2xy$

$\rightarrow (abx^2 - a^2xy) - (b^2xy - aby^2)$

$\rightarrow ax(bx - ay) - by(bx - ay)$

$\rightarrow (bx - ay)(ax - by)$