02/03/15 - 17/03/15

1 Dissertation

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2 Code

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param.cfg

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M potts.h
M template.cfg
M utilityfunctions.cpp
M utilityfunctions.h

3 Data and Results

3.1 Metropolis Thermodynamic Quantities

The Specific Heat Capacity was calculated using

$$C_V = \frac{1}{T^2} \left[\langle E^2 \rangle - \langle E \rangle^2 \right]$$
 (1)

The Magnetic Susceptibility was calculated using

$$\chi = \frac{1}{T} \left[\langle M^2 \rangle - \langle M \rangle^2 \right] \tag{2}$$

3.2 q=2

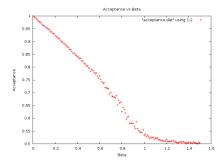
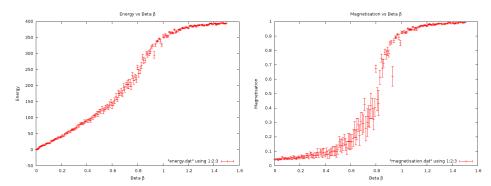
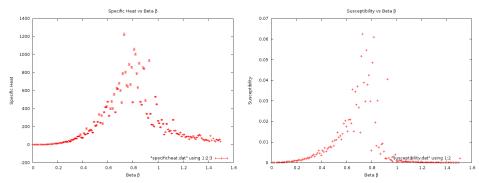


Figure 1: Acceptance for q = 2 on a 20 * 20 grid



(a) Energy per Lattice Site with Er- (b) Magnetisation per Lattice Site rors with Errors



(a) Specific Heat of the System with (b) Magnetic Susceptibility without Errors $\,\,$ errors

3.3 q=4

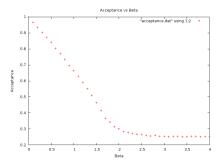
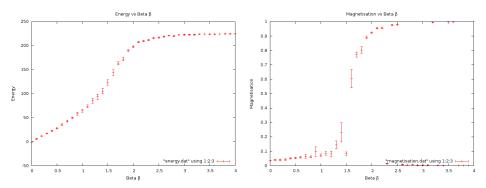
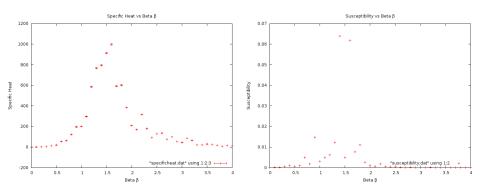


Figure 4: Acceptance for q=2 on a 20*20 grid



(a) Energy per Lattice Site with Er- (b) Magnetisation per Lattice Site rors with Errors



(a) Specific Heat of the System with (b) Magnetic Susceptibility without Errors errors

3.4 q=10

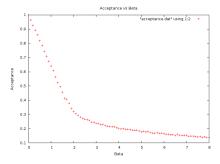
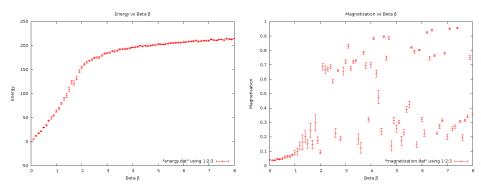
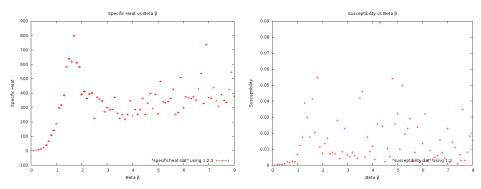


Figure 7: Acceptance for q=2 on a 20*20 grid



(a) Energy per Lattice Site with Er- (b) Magnetisation per Lattice Site rors with Errors



(a) Specific Heat of the System with (b) Magnetic Susceptibility without Errors errors

At higher and higher q we get some interesting artefacts after the phase transition, behaviours that look like energy level splitting and multiple minor phase transitions.

Because the Error of the Magnetic Susceptibility becomes significantly larger than the data itself around β_c it was not shown in this plot as to show the behaviour.

Behaviour is as expected when coupling is J=1/2 to match the Ising Model. However when changing to the Antiferromagnetic case J=-0.5 the simulation becomes erratic. Further investigation will be required to identify the source of the problem.

3.5 an Convergence

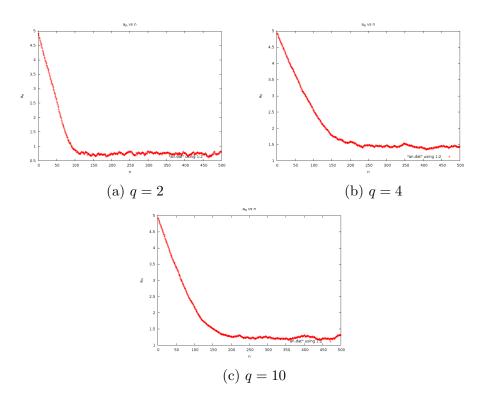


Figure 10: Target Energy: -100.0, Energy Band Width: 15.0

Taking the energies calculated from the Metropolis at various β and using those as a target to drive the configuration into to calculate a_n . I intend to prove that the two different values are indeed compatible.