



UNIVERSITY OF SWANSEA

MASTERS DISSERTATION

BL1: Interfaces in the 2D Potts model

Author:
Robert JAMES

Supervisor:
Professor Biagio LUCINI

February 22, 2015

Abstract

Contents

Contents	1
1 Introduction	3
2 Theory	5
3 Code	7
4 Results	9
5 Discussion of Results	11
Bibliography	13

Chapter 1

Introduction

In the field of Computational Physics, there is a large interest in lattice simulation. One of the most simple models that still exhibits non trivial behaviour is the q-state Potts Model. By Restricting the Potts model to 2 or 1 dimension(s) and the constraining the number of independent states, $q = 2$ you can determine the behaviour at high, low and critical temperatures analytically[1] this is known as the Ising Model.

This dissertation will be looking at directly determining the interface free energy as a ratio of the partition functions.

$$F_I(L) = -\log \frac{\tilde{Z}(L)}{Z(L)} + \log(L) \quad (1.1)$$

From the interface free energy above we can calculate the interface tension σ .

$$\sigma = \lim_{L \rightarrow \infty} \frac{F_I(L)}{L^{D-1}} \quad (1.2)$$

Chapter 2

Theory

The Potts Model

Chapter 3

Code

Chapter 4

Results

Chapter 5

Discussion of Results

Bibliography

- [1] Elliott W. Montroll, Renfrey B. Potts, and John C. Ward. Correlations and spontaneous magnetization of the two dimensional ising model. *Journal of Mathematical Physics*, 4(2):308–322, 1963.