

16-350

Planning Techniques for Robotics

Planning Representations:

Symbolic Representation for Task Planning

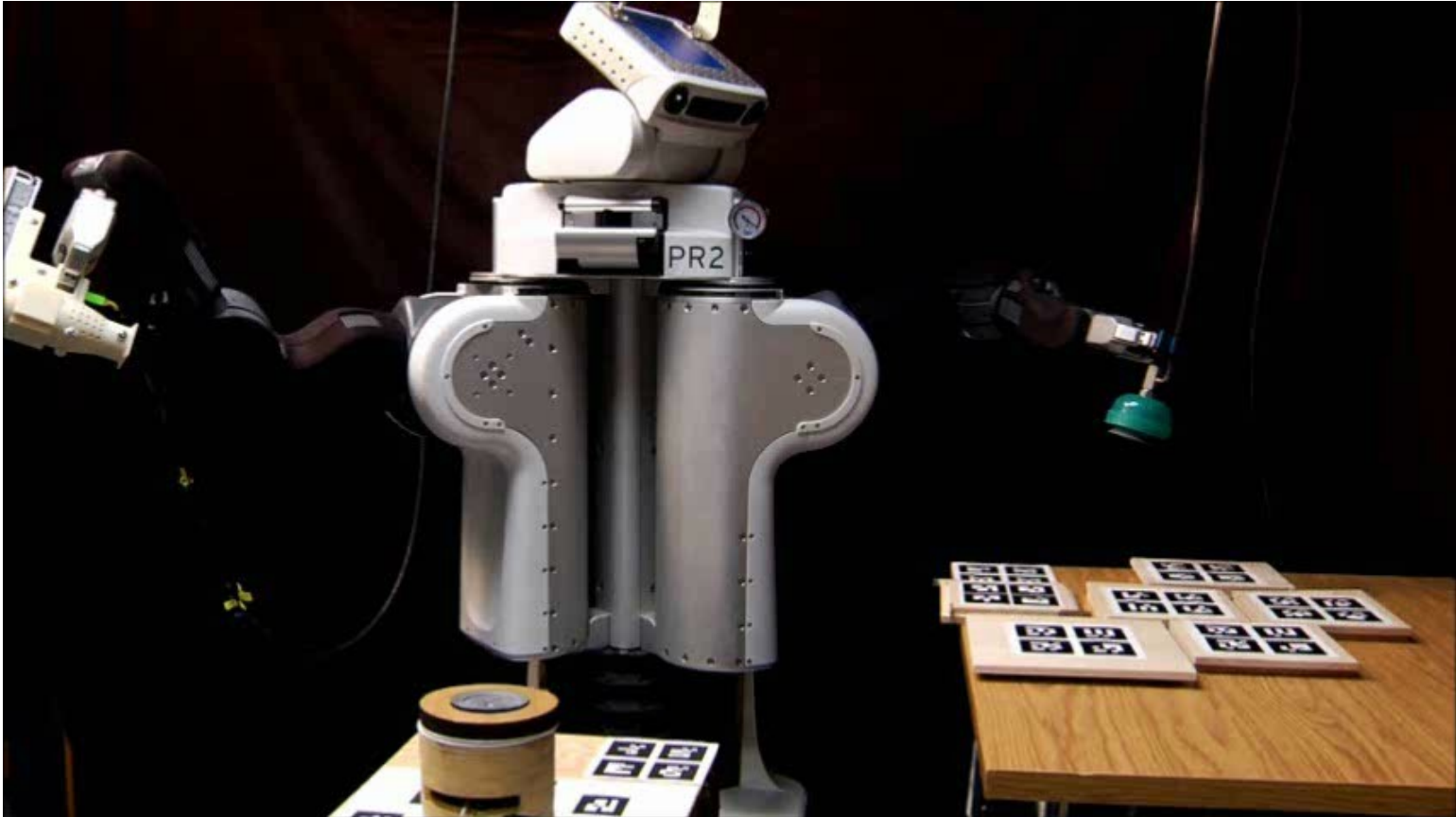
Maxim Likhachev

Robotics Institute

Carnegie Mellon University

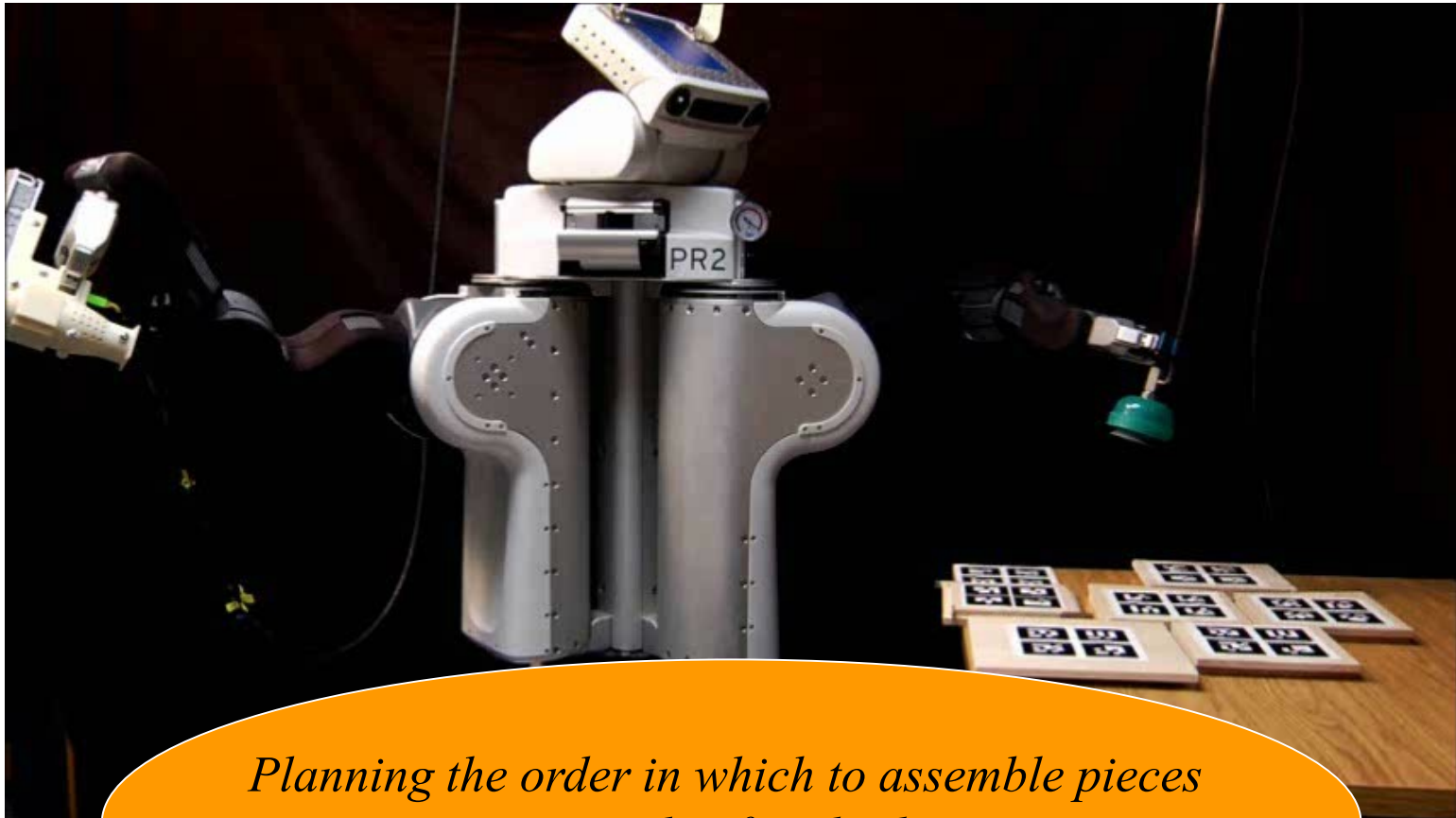
Planning to Construct a Birdcage

- Robot takes in a 3D model of a birdcage it needs to build



Planning to Construct a Birdcage

- Robot takes in a 3D model of a birdcage it needs to build



*Planning the order in which to assemble pieces
is an example of Task Planning*

Famous “Blocksworld” Example

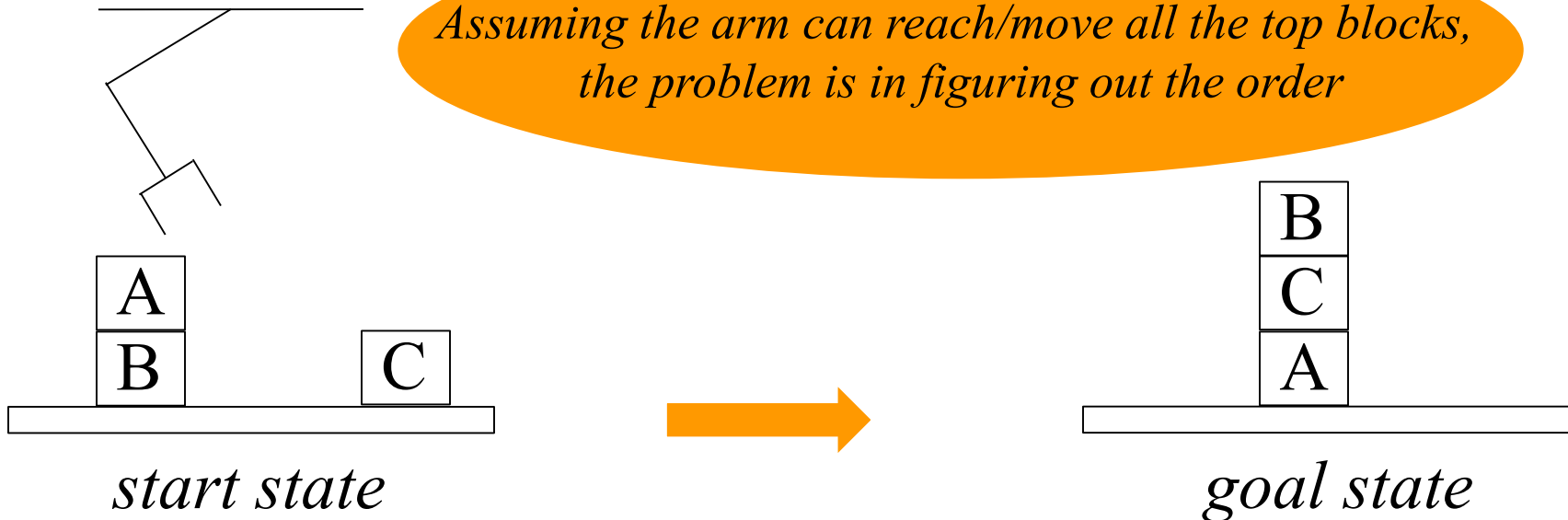
- Planning to re-order the blocks



Famous “Blockworld” Example

- Planning to re-order the blocks

Assuming the arm can reach/move all the top blocks, the problem is in figuring out the order



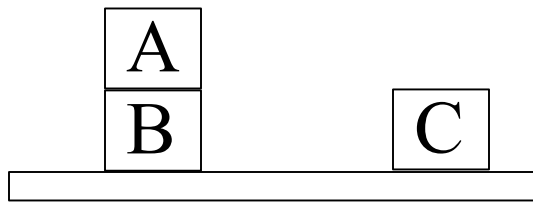
Famous “Blocksworld” Example

- Planning to re-order the blocks

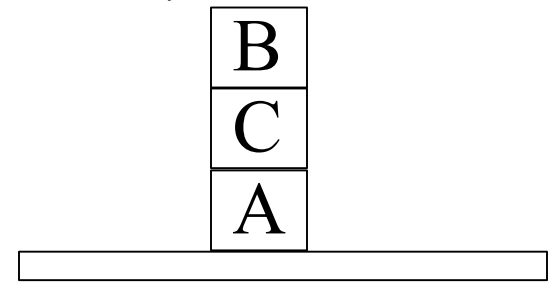
Actions:

Move(b,x,y) – moves block b from x to y

MoveToTable(b,x) – moves block b from x to table y



start state



goal state

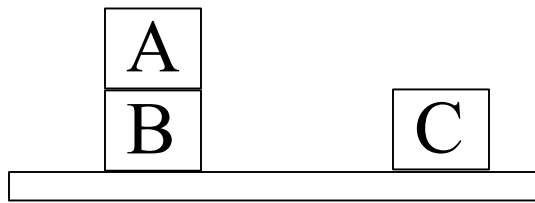
Famous “Blocksworld” Example

- Planning to re-order the blocks

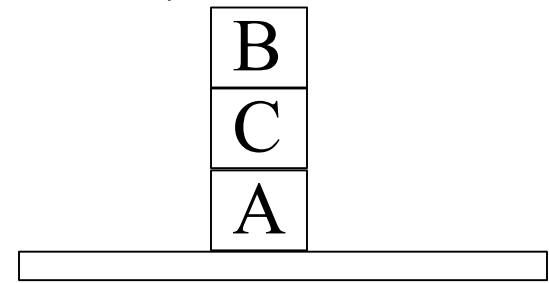
Actions:

Move(b,x,y) – moves block b from x to y

MoveToTable(b,x) – moves block b from x to table y



start state



goal state

What is a plan that achieves the goal?

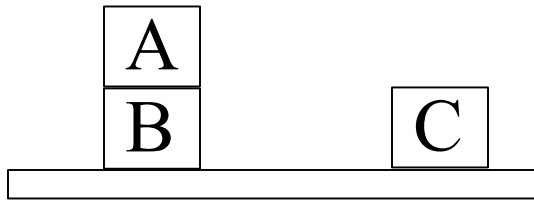
Defining it as a Graph Search (State-space Search)

- Planning to re-order the blocks

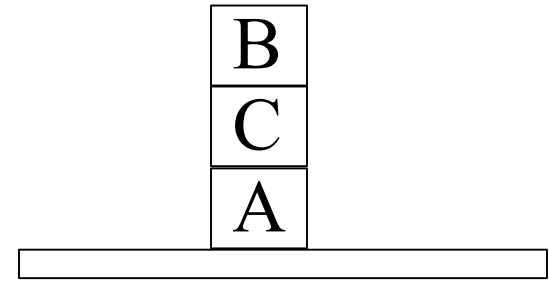
Actions:

Move(b,x,y) – moves block b from x to y

MoveToTable(b,x) – moves block b from x to table y



start state



goal state

Any ideas for how to represent a state in a graph?

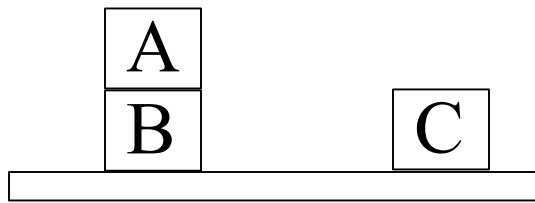
Defining it as a Graph Search (State-space Search)

- Planning to re-order the blocks

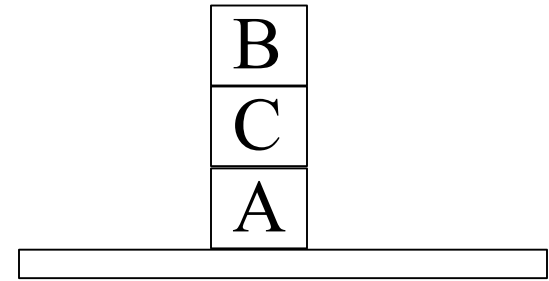
Actions:

Move(b,x,y) – moves block b from x to y

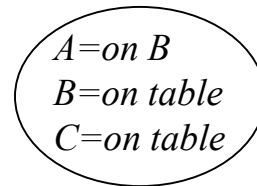
MoveToTable(b,x) – moves block b from x to table y



start state



goal state



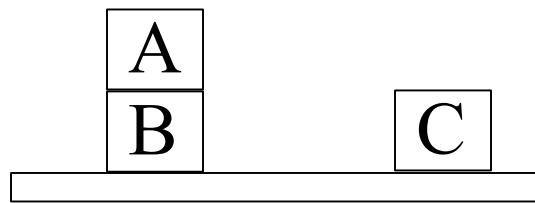
Defining it as a Graph Search (State-space Search)

- Planning to re-order the blocks

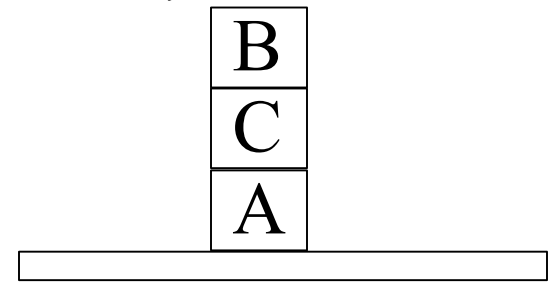
Actions:

Move(b,x,y) – moves block b from x to y

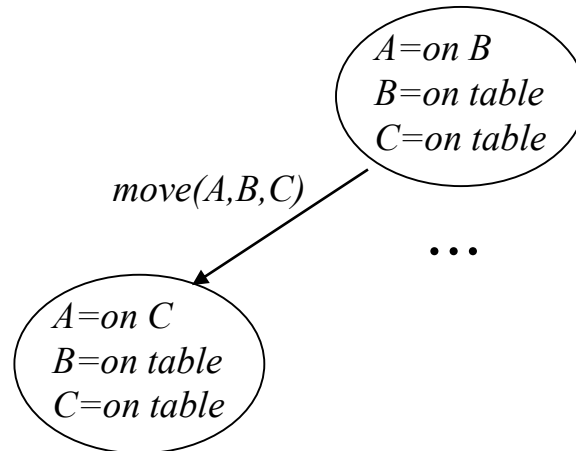
MoveToTable(b,x) – moves block b from x to table y



start state



goal state



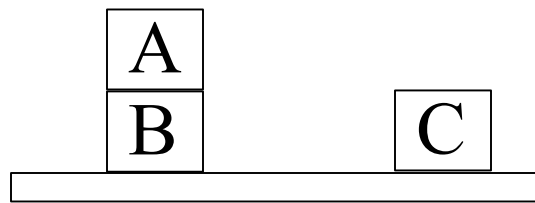
Defining it as a Graph Search (State-space Search)

- Planning to re-order the blocks

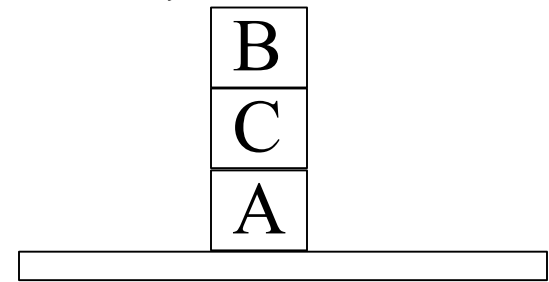
Actions:

Move(b,x,y) – moves block b from x to y

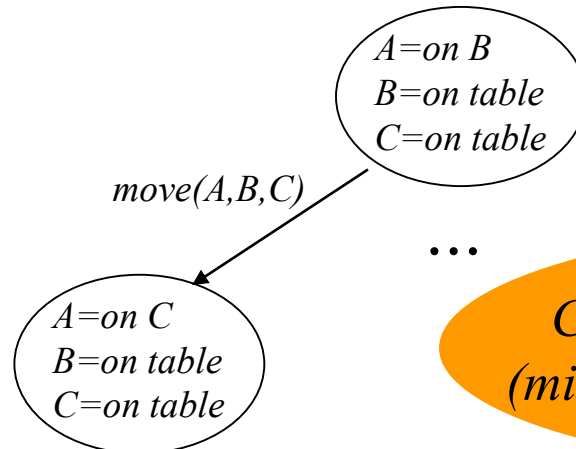
MoveToTable(b,x) – moves block b from x to table y



start state



goal state



*Cost of each edge is often set to 1
(minimization of the total # of actions)*

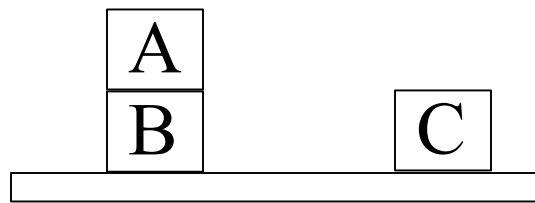
Defining it as a Graph Search (State-space Search)

- Planning to re-order the blocks

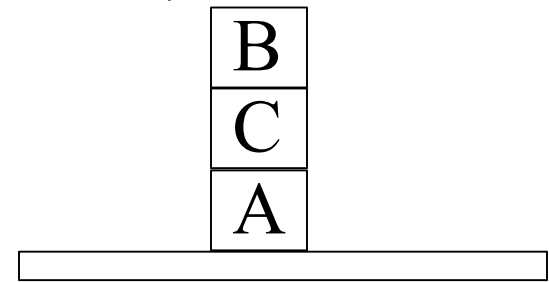
Actions:

Move(b,x,y) – moves block *b* from *x* to *y*

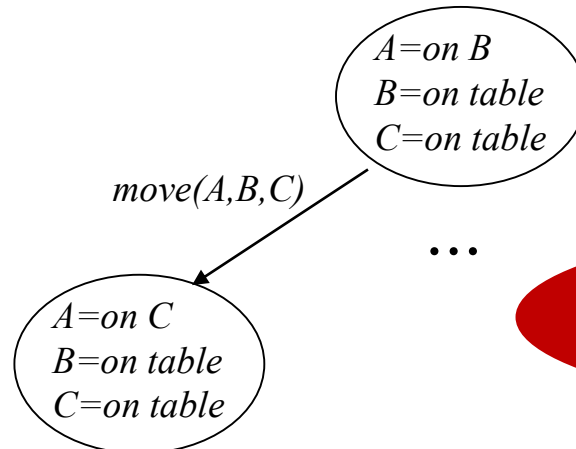
MoveToTable(b,x) – moves block *b* from *x* to table *y*



start state



goal state



Any ideas for heuristics?

Generic Representation of Symbolic Planning Problems

*We would like to be able to represent ANY planning problem
with a single representational language that allows for the definition of:
STATES, ACTIONS, GOAL*

Generic Representation of Symbolic Planning Problems

- STRIPS (=Stanford Research Institute Problem Solver)

State Representation:

Goal Representation:

Action Representation:

Generic Representation of Symbolic Planning Problems

- STRIPS (=Stanford Research Institute Problem Solver)

State Representation:

conjunction of positive(true) literals

(e.g, $\text{On}(A,B) \wedge \text{On}(B, \text{Table}) \wedge \text{On}(C, \text{Table}) \wedge \text{Block}(A) \wedge \text{Block}(B) \wedge \text{Block}(C) \wedge \text{Clear}(A) \wedge \text{Clear}(C)$)



Goal Representation:

Action Representation:

Generic Representation of Symbolic Planning Problems

- STRIPS (=Stanford Research Institute Problem Solver)

State Representation:

conjunction of positive(true) literals

(e.g, $\text{On}(A,B) \wedge \text{On}(B, \text{Table}) \wedge \text{On}(C, \text{Table}) \wedge \text{Block}(A) \wedge \text{Block}(B) \wedge \text{Block}(C) \wedge \text{Clear}(A) \wedge \text{Clear}(C)$)



Goal Representation:

Closed-world assumption:

any conditions not mentioned in the state are assumed to be false

Action Representation:

Generic Representation of Symbolic Planning Problems

- STRIPS (=Stanford Research Institute Problem Solver)

State Representation:

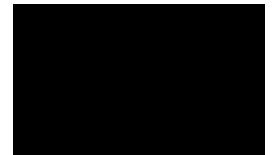
conjunction of positive(true) literals

(e.g, $\text{On}(A,B) \wedge \text{On}(B, \text{Table}) \wedge \text{On}(C, \text{Table}) \wedge \text{Block}(A) \wedge \text{Block}(B) \wedge \text{Block}(C) \wedge \text{Clear}(A) \wedge \text{Clear}(C)$)



Goal Representation:

desired conjunction of positive(true) literals



Action Representation:

Generic Representation of Symbolic Planning Problems

- STRIPS (=Stanford Research Institute Problem Solver)

State Representation:

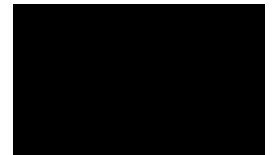
conjunction of positive(true) literals

(e.g, $\text{On}(A,B) \wedge \text{On}(B, \text{Table}) \wedge \text{On}(C, \text{Table}) \wedge \text{Block}(A) \wedge \text{Block}(B) \wedge \text{Block}(C) \wedge \text{Clear}(A) \wedge \text{Clear}(C)$)



Goal Representation:

desired conjunction of positive(true) literals



Action Representation:

What is it for this goal?



Generic Representation of Symbolic Planning Problems

- STRIPS (=Stanford Research Institute Problem Solver)

State Representation:

conjunction of positive(true) literals

(e.g, $\text{On}(A,B) \wedge \text{On}(B, \text{Table}) \wedge \text{On}(C, \text{Table}) \wedge \text{Block}(A) \wedge \text{Block}(B) \wedge \text{Block}(C) \wedge \text{Clear}(A) \wedge \text{Clear}(C)$)



Goal Representation:

desired conjunction of positive(true) literals

Could be partially-specified

Action Representation:



*Goal: any state where A
is directly on the table*

Generic Representation of Symbolic Planning Problems

- STRIPS (=Stanford Research Institute Problem Solver)

State Representation:

conjunction of positive(true) literals

(e.g, $\text{On}(A,B) \wedge \text{On}(B, \text{Table}) \wedge \text{On}(C, \text{Table}) \wedge \text{Block}(A) \wedge \text{Block}(B) \wedge \text{Block}(C) \wedge \text{Clear}(A) \wedge \text{Clear}(C)$)



Goal Representation:

desired conjunction of positive(true) literals

Could be partially-specified

Action Representation:

*Goal: any state where A
is directly on the table*



What is it for this goal?



Generic Representation of Symbolic Planning Problems

- STRIPS (=Stanford Research Institute Problem Solver)

State Representation:

conjunction of positive(true) literals

(e.g, $On(A,B) \wedge On(B,Table) \wedge On(C,Table) \wedge Block(A) \wedge Block(B) \wedge Block(C) \wedge Clear(A) \wedge Clear(C)$)



Goal Representation:

desired conjunction of positive(true) literals

Action Representation:

Preconditions: *conjunction of positive(true) literals that must held true in order for the action to be applicable*

Effect: *conjunction of positive(true) literals showing how the state will change (what should be deleted and added)*

Generic Representation of Symbolic Planning Problems

- STRIPS (=Stanford Research Institute Problem Solver)

State Representation:

conjunction of positive(true) literals

(e.g, $On(A,B) \wedge On(B,Table) \wedge On(C,Table) \wedge Block(A) \wedge Block(B) \wedge Block(C) \wedge Clear(A) \wedge Clear(C)$)



Goal Representation:

desired conjunction of positive(true) literals

What are preconditions & effect for MoveToTable(b,x) action?

Action Rep

Preconditions: conjunction of positive(true) literals that must held true in order for the action to be applicable

Effect: conjunction of positive(true) literals showing how the state will change (what should be deleted and added)

Generic Representation of Symbolic Planning Problems

- STRIPS (=Stanford Research Institute Problem Solver)

State Representation:

conjunction of positive(true) literals

(e.g, $On(A,B) \wedge On(B,Table) \wedge On(C,Table) \wedge Block(A) \wedge Block(B) \wedge Block(C) \wedge Clear(A) \wedge Clear(C)$)



Goal Representation:

desired conjunction of positive(true) literals

What are preconditions & effect for MoveToTable(b,x) action?

Action Rep

Precondition: *conjunction of positive(true) literals that must*

hold before the action is executed
MoveToTable(b,x)

Precond: $On(b,x) \wedge Clear(b) \wedge Block(b)$

Effect: *showing how the*

state will change (literals to be deleted and added)
Effect: $On(b,Table) \wedge Clear(x) \wedge \sim On(b,x)$

Generic Representation of Symbolic Planning Problems

- STRIPS (=Stanford Research Institute Problem Solver)

State Representation:

conjunction of positive(true) literals

(e.g, $\text{On}(A,B) \wedge \text{On}(B,\text{Table}) \wedge \text{On}(C,\text{Table}) \wedge \text{Block}(A) \wedge \text{Block}(B) \wedge \text{Block}(C) \wedge \text{Clear}(A) \wedge \text{Clear}(C)$)



Goal Representation:

desired conjunction of positive(true) literals

What are preconditions & effect for for Move(b,x,y) action?

Action Rep

Preconditions: conjunction of positive(true) literals that must held true in order for the action to be applicable

Effect: conjunction of positive(true) literals showing how the state will change (what should be deleted and added)

Back to the Example

- Representing it with STRIPS



Start state:

$On(A,B) \wedge On(B,Table) \wedge On(C,Table) \wedge Block(A) \wedge Block(B) \wedge Block(C) \wedge Clear(A) \wedge Clear(C)$

Goal state:

$On(B,C) \wedge On(C,A) \wedge On(A,Table)$

Actions:

$MoveToTable(b,x)$

Precond: $On(b,x) \wedge Clear(b) \wedge Block(b)$

Effect: $On(b,Table) \wedge Clear(x) \wedge \sim On(b,x)$

$Move(b,x,y)$

Precond: $On(b,x) \wedge Clear(b) \wedge Clear(y) \wedge Block(b) \wedge Block(y) \wedge (b \neq y)$

Effect: $On(b,y) \wedge Clear(x) \wedge \sim On(b,x) \wedge \sim Clear(y)$

Back to the Example

- Representing it with STRIPS



Start state:

$On(A,B) \wedge On(B,Table) \wedge On(C,Table) \wedge Block(A) \wedge Block(B) \wedge Block(C) \wedge Clear(A) \wedge Clear(C)$

Goal state:

$On(B,C) \wedge On(C,A) \wedge On(A,Table)$

Actions:

$MoveToTable(b,x)$

Precond: $On(b,x) \wedge Clear(b) \wedge Block(b)$

Effect: $On(b,Table) \wedge Clear(x) \wedge \sim On(b,x)$

$Move(b,x,y)$

Precond: $On(b,x) \wedge Clear(b) \wedge Clear(y) \wedge Block(b) \wedge Block(y) \wedge (b \neq y)$

Effect: $On(b,y) \wedge Clear(x) \wedge \sim On(b,x) \wedge \sim Clear(y)$

Problem (domain) specification

Back to the Example

- Representing it with STRIPS

B

We can now write a (domain-independent) program that takes in such specifications and automatically provides a function $\text{GetSuccessors}(\text{state } S, \text{action } A)$ required for implicit graph construction

Start state:

$\text{On}(A,B) \wedge \text{On}(B, \text{Table}) \wedge \text{On}(C, \text{Table}) \wedge \text{Block}(A) \wedge \text{Block}(B) \wedge \text{Block}(C) \wedge \text{Clear}(A) \wedge \text{Clear}(C)$

Goal state:

$\text{On}(B,C) \wedge \text{On}(C,A) \wedge \text{On}(A, \text{Table})$

Actions:

$\text{MoveToTable}(b,x)$

Precond: $\text{On}(b,x) \wedge \text{Clear}(b) \wedge \text{Block}(b)$

Effect: $\text{On}(b, \text{Table}) \wedge \text{Clear}(x) \wedge \sim \text{On}(b,x)$

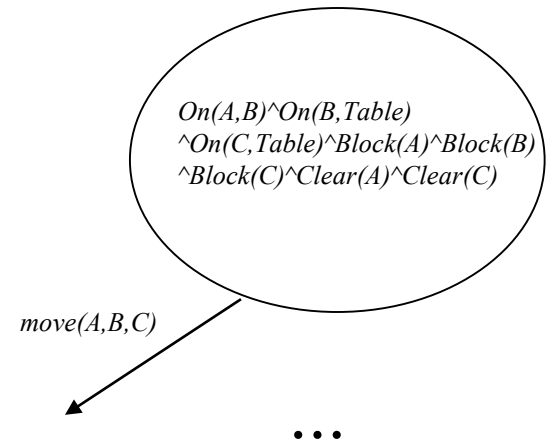
$\text{Move}(b,x,y)$

Precond: $\text{On}(b,x) \wedge \text{Clear}(b) \wedge \text{Clear}(y) \wedge \text{Block}(b) \wedge \text{Block}(y) \wedge (b \neq y)$

Effect: $\text{On}(b,y) \wedge \text{Clear}(x) \wedge \sim \text{On}(b,x) \wedge \sim \text{Clear}(y)$

This graph can be

searched with A^ or any other search*



Back to the Example

- Representing it with STRIPS

B

We can now write a (domain-independent) program that takes in such specifications and automatically provides a function $\text{GetSuccessors}(\text{state } S, \text{action } A)$ required for implicit graph construction

Start state:

$\text{On}(A,B) \wedge \text{On}(B, \text{Table}) \wedge \text{On}(C, \text{Table}) \wedge \text{Clear}(A) \wedge \text{Clear}(B) \wedge \text{Clear}(C)$

This graph can be

searched with A^ or any other search*

Goal state:

$\text{On}(B,C) \wedge \text{On}(C,A) \wedge \text{On}(A,B)$

*This is often referred to as **domain-independent planning***

Actions:

$\text{MoveToTable}(b,x)$

Precond: $\text{On}(b,x) \wedge \text{Clear}(b) \wedge \text{Block}(b)$

Effect: $\text{On}(b, \text{Table}) \wedge \text{Clear}(x) \wedge \sim \text{On}(b,x)$

$\text{Move}(b,x,y)$

Precond: $\text{On}(b,x) \wedge \text{Clear}(b) \wedge \text{Clear}(y) \wedge \text{Block}(b) \wedge \text{Block}(y) \wedge (b \neq y)$

Effect: $\text{On}(b,y) \wedge \text{Clear}(x) \wedge \sim \text{On}(b,x) \wedge \sim \text{Clear}(y)$

$\text{move}(A,B,C)$

$\text{On}(C, \text{Table}) \wedge \text{Block}(A) \wedge \text{Block}(B) \wedge \text{Block}(C) \wedge \text{Clear}(A) \wedge \text{Clear}(C)$

...

Back to the Example

- Representing it with STRIPS



Start state: *Any ideas for domain-independent heuristics?*

$On(A,B) \wedge On(B,Table) \wedge On(C,Table) \wedge Block(A) \wedge Block(B) \wedge Block(C) \wedge Clear(A) \wedge Clear(C)$

Goal state:

$On(B,C) \wedge On(C,A) \wedge On(A,Table)$

Actions:

MoveToTable(b,x)

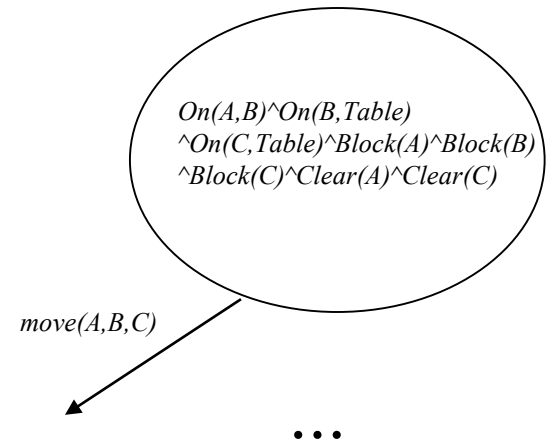
Precond: $On(b,x) \wedge Clear(b) \wedge Block(b)$

Effect: $On(b,Table) \wedge Clear(x) \wedge \sim On(b,x)$

Move(b,x,y)

Precond: $On(b,x) \wedge Clear(b) \wedge Clear(y) \wedge Block(b) \wedge Block(y) \wedge (b \neq y)$

Effect: $On(b,y) \wedge Clear(x) \wedge \sim On(b,x) \wedge \sim Clear(y)$



Summary

- Task planning typically abstracts away lower-level planning (continuous motion/path planning) and focuses on finding a sequence of higher level actions required to achieve a task
- STRIPS (and its latest extensions such as ADL and PDDL) allow for translating compact representations of domains/problems into implicit graphs
- A* (and its variants including weighted A*) can be used to search these implicit graphs