5.1.1 - R: Logistic Regression Stat 5100: Dr. Bean

Example: (Text Table 14.3) Individuals were randomly sampled within two sectors of a city, and checked for presence of disease (here, spread by mosquitoes). Subjects' age (in years), socioeconomic status (low, medium, high), and city sector are to be used to predict the probability of contracting the disease.

In R, we can create logistic regression models with the glm function. "GLM" stands for generalized linear model, and can be used to fit a variety of linear models. To specify logistic regression, we set an option in side the glm function that specifies a binomial (two classes) response.

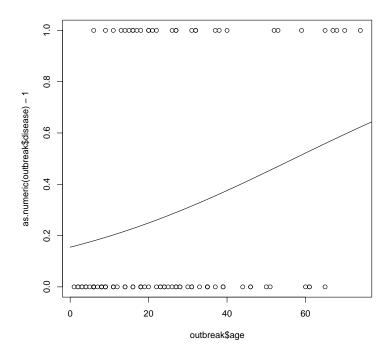
Fit a logistic regression model

```
# Input the data
library(stat5100)
data(outbreak)
# Some of the things we do below in the document work better when these
# variables are treated numerically.
outbreak$SES_mid <- as.numeric(as.character(outbreak$SES_mid))</pre>
outbreak$SES_low <- as.numeric(as.character(outbreak$SES_low))</pre>
outbreak$sector <- as.numeric(as.character(outbreak$sector))</pre>
# To do logistic regression, we use the qlm function.
outbreak_logreg <- glm(disease ~ age + SES_mid + SES_low + sector,
                    data = outbreak, family = "binomial")
summary(outbreak_logreg)
##
## Call:
## glm(formula = disease ~ age + SES_mid + SES_low + sector, family = "binomial",
      data = outbreak)
##
##
## Deviance Residuals:
##
    Min 1Q Median
                            3Q
                                     Max
## -1.6552 -0.7529 -0.4788 0.8558
                                   2.0977
##
## Coefficients:
            Estimate Std. Error z value Pr(>|z|)
##
## age
            ## SES_mid
             0.40879 0.59900 0.682 0.494954
## SES_low
            1.57475
                       0.50162 3.139 0.001693 **
## sector
## ---
## Signif. codes: 0 '***' 0.001 '**' 0.05 '.' 0.1 ' ' 1
##
## (Dispersion parameter for binomial family taken to be 1)
```

```
## Null deviance: 122.32 on 97 degrees of freedom
## Residual deviance: 101.05 on 93 degrees of freedom
## AIC: 111.05
##
## Number of Fisher Scoring iterations: 4
```

Plot a graph of observed values and predicted probabilities

Because we have multiple predictor variables, we have to choose one variable to put on the x-axis, and the rest of the variables will have to be fixed at some value. We will use Age for our x-axis variable. We will set $SES_mid = 0.245$, $SES_low = 0.367$, and Sector = 0.398.



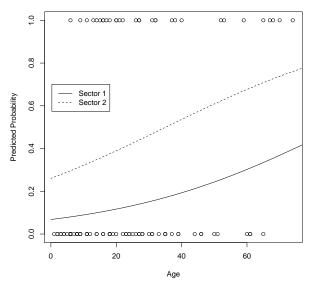
Goodness of fit tests

```
# Conduct a Hosmer and Lemeshow Goodness-of-Fit Test
# To do the test, we first need a vector of the predicted probabilities
# from the logistic regression model.
```

Create a conditional effects plot

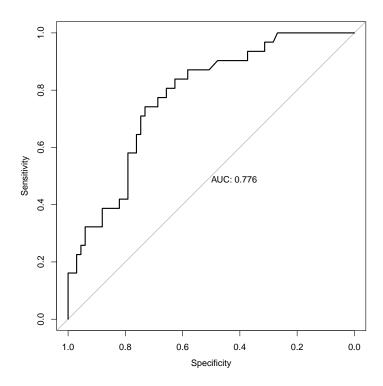
Compare the predicted disease probabilities for sector 1 (displayed as sector=0) vs sector 2 (displayed as sector=1) at low socioeconomic status (SES_mid=0, SES_low=1) as a function of age. Note that the numbers plugged in below come from the summary of the fitted logistic regression model.

Conditional Effect Plot at Low SES



Plot an ROC curve

```
# ROC Curve
prob <- fitted(outbreak_logreg)
pROC::roc(outbreak$disease ~ prob, plot = TRUE, print.auc = TRUE)
## Setting levels: control = 0, case = 1
## Setting direction: controls < cases</pre>
```



```
##
## Call:
## roc.formula(formula = outbreak$disease ~ prob, plot = TRUE, print.auc = TRUE)
##
## Data: prob in 67 controls (outbreak$disease 0) < 31 cases (outbreak$disease 1).
## Area under the curve: 0.7764</pre>
```

Check for multicollinearity

We can get the variance inflation factors for the logistic model with the vif() function inside the car package:

```
car::vif(outbreak_logreg)

## age SES_mid SES_low sector
## 1.023343 1.221073 1.255794 1.047822
```

Variable selection

In R, we can perform variable selection for logistic regression by using the stepAIC() function available in the MASS package.

```
MASS::stepAIC(outbreak_logreg, trace = FALSE)
##
## Call: glm(formula = disease ~ age + sector, family = "binomial", data = outbreak)
##
## Coefficients:
## (Intercept)
                                  sector
                        age
      -2.33515
                                 1.67345
                    0.02929
##
##
## Degrees of Freedom: 97 Total (i.e. Null); 95 Residual
## Null Deviance:
                      122.3
## Residual Deviance: 102.3 AIC: 108.3
```

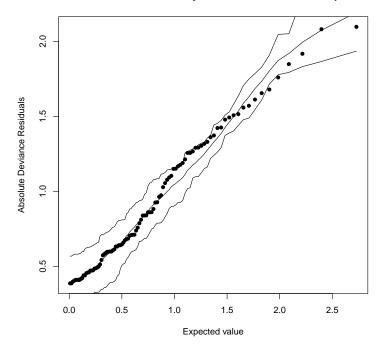
Based upon the above, the so-called "best model" would be the model that includes age and sector as predictor variables.

Simulated envelope

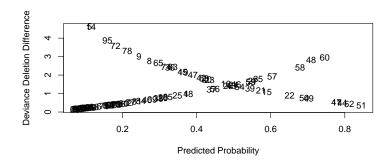
Check for outliers using the half-normal probability plot with simulated envelope.

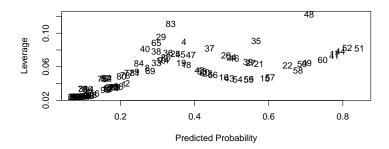
```
# Set a seed first because this does use some randomization
set.seed(1741)
stat5100::simulated_envelope_logreg(outbreak_logreg)
```

Half-Normal Probability Plot with Simulated Envelope



Check for influential observations





Look at a suspect observation

```
outbreak[outbreak$case == 48, ]

## case age SES_mid SES_low sector disease
## 48 48 65 0 1 1 0
```