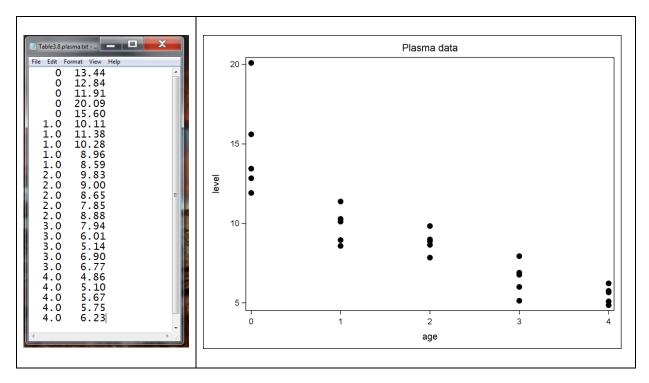
#### 2.2.2: SAS - Linear Regression Remedial Measures

Dr. Bean – Stat 5100

<u>Example</u>: Age and plasma level for 25 healthy children in a study are reported. Of interest is how plasma level depends on age. (Text Table 3.8 – first column is age; second column is plasma level)



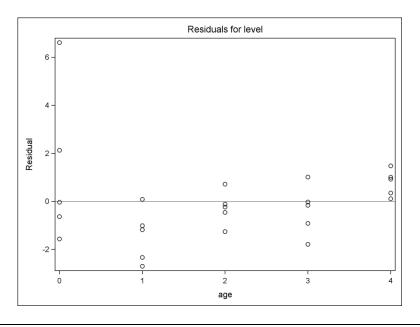
```
/*
data plasma;
   infile "[File Path]/Table3.8.plasma.txt";
   input age level;
run;
*/
data plasma; input age level @@; cards;
                                11.91
                                                           15.60
      13.44
                0
                   12.84
                             0
                                          0
                                              20.09
      10.11
                                                            8.59
 1.0
              1.0
                   11.38
                           1.0
                                10.28
                                        1.0
                                               8.96
                                                     1.0
 2.0
       9.83
              2.0
                    9.00
                           2.0
                                  8.65
                                               7.85
                                                     2.0
                                                            8.88
                                        2.0
 3.0
       7.94
              3.0
                     6.01
                           3.0
                                  5.14
                                        3.0
                                               6.90
                                                     3.0
                                                            6.77
 4.0
       4.86
              4.0
                    5.10
                          4.0
                                  5.67
                                        4.0
                                               5.75
                                                     4.0
                                                            6.23
  ;
/* Fit regression model and check assumptions */
proc reg data=plasma;
  model level = age;
  output out=out1 r=resid p=pred;
  title1 'Simple model for plasma data';
run;
```

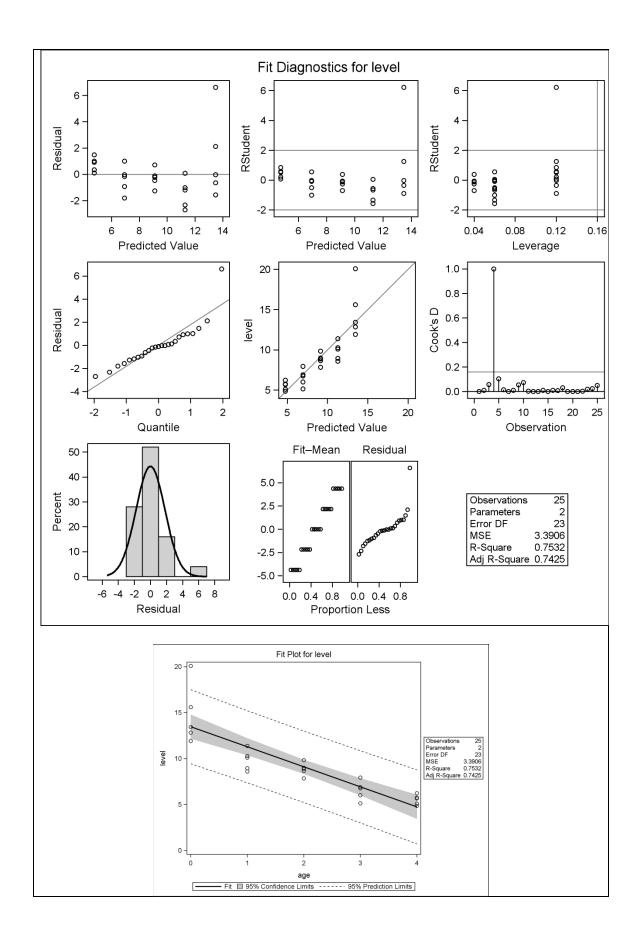
### Simple model for plasma data

Analysis of Variance					
Source	DF	Sum of Squares	Mean Square	F Value	<b>Pr</b> > <b>F</b>
Model	1	238.05620	238.05620	70.21	<.0001
Error	23	77.98306	3.39057		
<b>Corrected Total</b>	24	316.03926			

Root MSE	1.84135	R-Square	0.7532
Dependent Mean	9.11120	Adj R-Sq	0.7425
Coeff Var	20.20974		

Parameter Estimates					
Variable	DF	Parameter Estimate	Standard Error	t Value	Pr >  t
Intercept	1	13.47520	0.63786	21.13	<.0001
age	1	-2.18200	0.26041	-8.38	<.0001





```
/* Define shortcut macro, using line copied from
    [File Path]/resid_num_diag_lline.sas
    */
%macro resid_num_diag(dataset,...
/* Call shortcut macro */
%resid_num_diag(dataset=out1, datavar=resid, label='Residual',
    predvar=pred, predlabel='Predicted Value');
```

### P-value for Brown-Forsythe test of constant variance in Residual vs. Predicted Value

Obs	t_BF	BF_pvalue
1	1.50583	0.14572

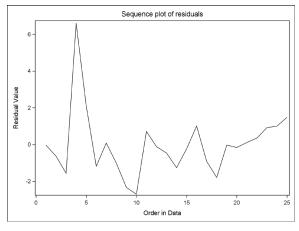
# Output for correlation test of normality of Residual (Check text Table B.6 for threshold)

Pearson Correlation Coefficients, N = 25 Prob >  r  under H0: Rho=0					
	resid	expectNorm			
resid Residual	1.00000	0.90360 <.0001			
expectNorm	0.90360 <.0001	1.00000			

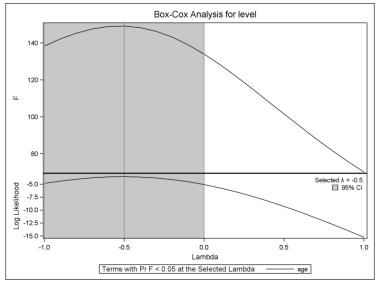
```
/* F-test for lack of fit */
proc rsreg data=plasma;
  model level = age / lackfit covar=1 noopt;
  title1 'F-test for lack of fit';
run;
```

Residual	DF	Sum of Squares	Mean Square	F Value	<b>Pr</b> > <b>F</b>
Lack of Fit	3	22.748784	7.582928	2.75	0.0699
Pure Error	20	55.234280	2.761714		
Total Error	23	77.983064	3.390568		

```
/* Look at sequence plot */
data temp; set out1;
  order = _n_;
proc sgplot data=temp;
  series x=order y=resid / lineattrs=(pattern=solid);
  xaxis label='Order in Data';
  yaxis label='Residual Value';
  title1 'Sequence plot of residuals';
run;
```

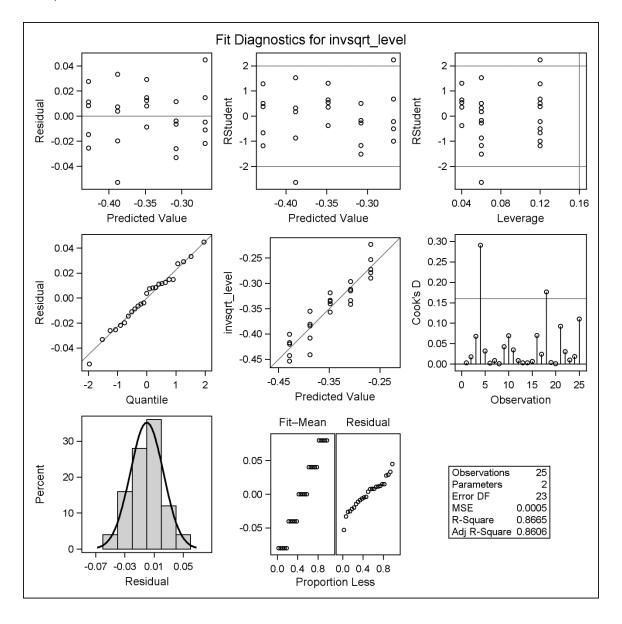


/\*\*\*\*\*\* Consider Transformations \*\*\*\*\*\*\*\*\*\*/



```
data plasma; set plasma;
  log_level = log(level);
  invsqrt_level = -1/sqrt(level);
run;
```

```
/* Inverse square root */
proc reg data=plasma;
  model invsqrt_level = age;
  output out=out2 r=resid p=pred;
  title1 'Simple model for negative inverse root plasma data';
run;
```



```
%resid_num_diag(dataset=out2, datavar=resid,
    label='Residual (neg. inverse root)',
    predvar=pred, predlabel='Predicted Value (neg. inverse
root)');
```

### P-value for Brown-Forsythe test of constant variance in Residual (neg. inverse root) vs. Predicted Value (neg. inverse root)

Obs	t_BF	BF_pvalue
1	0.16654	0.86918

## Output for correlation test of normality of Residual (neg. inverse root) (Check text Table B.6 for threshold)

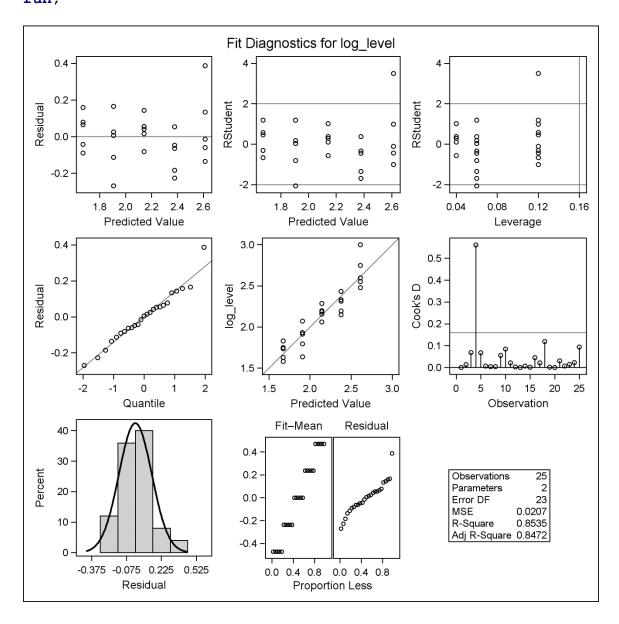
Pearson Correlation Coefficients, N = 25 Prob >  r  under H0: Rho=0					
resid expectNorm					
resid	1.00000	0.99188			
Residual (neg. inverse root)		<.0001			
expectNorm	0.99188	1.00000			
	<.0001				

```
proc rsreg data=plasma;
  model invsqrt_level = age / lackfit covar=1 noopt;
  title1 'F-test for lack of fit (neg. inverse root)';
run;
```

#### F-test for lack of fit (neg. inverse root)

Residual	DF	Sum of Squares	Mean Square	F Value	Pr > F
Lack of Fit	3	0.001556	0.000519	0.96	0.4312
Pure Error	20	0.010813	0.000541		
Total Error	23	0.012369	0.000538		

```
/* Log */
proc reg data=plasma;
  model log_level = age;
  output out=out3 r=resid p=pred;
  title1 'Simple model for log plasma data';
run;
```



```
%resid_num_diag(dataset=out3, datavar=resid,
label='Residual (log)',
    predvar=pred, predlabel='Predicted Value (log)');
```

# P-value for Brown-Forsythe test of constant variance in Residual (log) vs. Predicted Value (log)

Obs	t_BF	BF_pvalue
1	0.95179	0.35110

## Output for correlation test of normality of Residual (log) (Check text Table B.6 for threshold)

Pearson Correlation Coefficients, N = 25 Prob >  r  under H0: Rho=0					
	resid	expectNorm			
resid Residual (log)	1.00000	0.98071 <.0001			
expectNorm	0.98071 <.0001	1.00000			

```
proc rsreg data=plasma;
  model log_level = age / lackfit covar=1 noopt;
  title1 'F-test for lack of fit (log)';
run;
```

#### F-test for lack of fit (log)

Residual	DF	Sum of Squares	Mean Square	F Value	Pr > F
Lack of Fit	3	0.081944	0.027315	1.39	0.2758
Pure Error	20	0.394004	0.019700		
Total Error	23	0.475948	0.020693		

```
/* Probably go with inverse square root */
proc reg data=plasma;
  model invsqrt_level = age;
  title1 'Negative inverse root plasma data';
run;
```

### Negative inverse root plasma data

Analysis of Variance								
Source	DF	Sum of Squares	Mean Square	F Value	Pr > F			
Model	1	0.08025	0.08025	149.22	<.0001			
Error	23	0.01237	0.00053778					
<b>Corrected Total</b>	24	0.09262						

Root MSE	0.02319	R-Square	0.8665
----------	---------	----------	--------

Parameter Estimates								
Variable	DF	Parameter Estimate	Standard Error	t Value	Pr >  t			
Intercept	1	-0.26803	0.00803	-33.36	<.0001			
age	1	-0.04006	0.00328	-12.22	<.0001			

