

3.1 Alternate Variable Types and Interactions

Dr. Bean - Stat 5100

Describe the difference between multicollinearity and interactions.

Multicollinearity only deals with relationships among the X variables and has NOTHING to do with Y. Interactions have EVERYTHING to do with Y and the way that X_k 's relationship with Y is influenced by the other X variables.

Identify whether each of the following variables are qualitative or quantitative:

- hours worked **quantitative**
- shirt color **qualitative**
- a person's shoe size **quantitative**
- systolic blood pressure **quantitative**
- blood type **qualitative**
- college major **qualitative**

Ignoring the significance of the model coefficients and assuming that assumptions regarding residuals are satisfied, please write the estimated regression equation corresponding to the following SAS output (not that Y represents Oxygen Intake Rate).

Parameter Estimates						
Variable	Label	DF	Parameter Estimate	Standard Error	t Value	Pr > t
Intercept	Intercept	1	107.29565	43.38302	2.47	0.0202
Age	Age (in years)	1	-0.46161	0.87289	-0.53	0.6014
Weight	Weight (in kilograms)	1	-0.23470	0.54681	-0.43	0.6713
RunTime	Time to Run 1.5 Miles (in minutes)	1	-3.15204	0.37523	-8.40	<.0001
ageWeight	Age*Weight	1	0.00370	0.01115	0.33	0.7427

$$\hat{Y} = 107.296 - 0.461 * Age - 0.235 * Weight - 3.152 * RunTime + 0.004 * Age * Weight$$

What is the expected change in the average of Y when a person ages by one year?

$$-0.461 + 0.004 * Weight$$

Suppose you are trying to predict a person's happiness and you suspect that country of origin is a significant predictor of happiness. You take a sample of 100 people to test your hypothesis. In this scenario, what issue will you run into trying to use country of origin as a predictor variable?

We need $q - 1$ dummy variables to represent q countries. There are more than 100 countries in the world, so our model would require more degrees of freedom than is feasible with our sample size.