

Recurso - 15/02/21

$$1) \quad \phi_p = \phi_p^o$$

$$\Leftrightarrow \{ \text{S. 20} \}$$

$$\phi_p \subseteq \phi_p^o$$

$$\Leftrightarrow \{ \text{S. 13} - 2x \}$$

$$\phi_p \subseteq id \cdot \phi_p^o \cdot id$$

$$\Leftrightarrow \{ \phi_p \subseteq id, \text{lowering upper side} \}$$

$$\phi_p \subseteq \phi_p \cdot \phi_p^o \cdot \phi_p$$

$$\Leftrightarrow \{ \text{E' bijectiva; S. 13} \}$$

$$\phi_p \subseteq \phi_p$$

$$\Leftrightarrow \{ \text{trivial} \}$$

true

$$2) \quad (R \times S) \cdot \langle id, id \rangle = \langle R, S \rangle$$

$$(R \times S) \cdot \langle id, id \rangle$$

$$\Leftrightarrow \{ \text{S. 107} \}$$

$$\langle R \cdot \pi_1, S \cdot \pi_2 \rangle \cdot \langle id, id \rangle$$

$$\Leftrightarrow \{ \text{S. 104, since } R \cdot \pi_1 \cdot \langle id, id \rangle \subseteq R \}$$

$$\langle R \cdot \pi_1 \cdot \langle id, id \rangle, S \cdot \pi_2 \cdot \langle id, id \rangle \rangle$$

$$\Leftrightarrow \{ \text{Cancelamento - X; S. 13; 2x} \}$$

$$\langle R, S \rangle$$

$$3) \quad S = R \cdot \langle id, t_0 \rangle^o$$

Temos que $\langle id, t_0 \rangle^o$ é simples, porque $\langle id, t_0 \rangle$ é injetiva (regras 5.11a e 5.43). Logo, S também será simples. Se t_0 for substituído por

T continua simples pela mesma razão

$$S = R \cdot \langle id, T \rangle^o$$

$$\Leftrightarrow \{ \text{Shunting} \}$$

$$S \cdot \langle id, T \rangle = R$$

$$\Leftrightarrow \{ \text{Variáveis} \}$$

$$p(S \cdot \langle id, T \rangle)u = pRu$$

$$\Leftrightarrow \{ \text{S. 11} \}$$

$$\langle \exists u, t: pS(u, t): (u, t) \cdot \langle id, T \rangle u \rangle = pRu$$

$$\Leftrightarrow \{ \text{S. 101} \}$$

$$\langle \exists u, t: pS(u, t): u' = u \wedge tTu \rangle = pRu$$

$$\Leftrightarrow \{ \text{A. 2; A. 6; } \neg T = \text{True} \}$$

$$\langle \exists t: pS(u, t) \rangle = pRu$$

4) $\perp \cdot \text{id} \in R \Rightarrow \text{reflexiva}$

$\therefore \{$

$$\text{id} \in (\text{id} \cap \text{id}) \cdot T \cdot (\text{id} \cap \text{id})$$

$\Rightarrow \{ \text{trivial} \}$

$$\text{id} \in \text{id} \cdot T \cdot \text{id}$$

$\Rightarrow \{ 5, 13, 2x \}$

$$\text{id} \in T$$

$\Rightarrow \{ \text{trivial} \}$

true

$$2. \text{Ker}(A) \subseteq (\text{Ker}(A) \cap \text{id}) \cdot T \cdot (\text{id} \cap \text{Ker}(A))$$

\Rightarrow

$$\text{id} \cdot (R^0 \cdot R) \cdot \text{id} \in (R^0 \cdot R \cap \text{id}) \cdot T \cdot (\text{id} \cap (R^0 \cdot R))$$

$\Rightarrow \{ 5, 7, 8 \}$

$$\int \text{id} \in R^0 \cdot R \cap \text{id}$$

$$\leftarrow R^0 \cdot R \in T \Rightarrow \text{true}$$

\Rightarrow

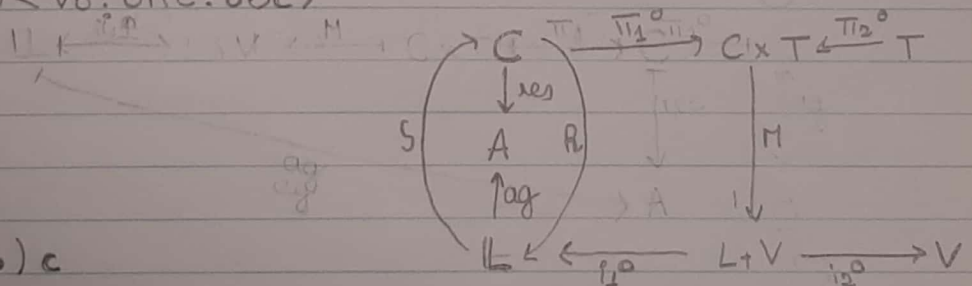
$$\text{id} \in R^0 \cdot R \wedge \text{id} \in \text{id}$$

$\Rightarrow R$ é interno

se é verdade se R for interna.

$$5) \text{id} \cap (c_1^0 \cdot M \cdot \pi_1^0) \setminus (res^0 \cdot ag)$$

$$c(A|S)c \Leftrightarrow \langle \forall b: bRc: bSc \rangle$$



$$b(\text{id} \cap R|S)c$$

\Leftrightarrow

$$\langle \forall c: cRa: cSa \rangle \text{ (res}^0 \cdot ag|c)$$

\Leftrightarrow

$$\langle \forall c: \langle \exists i: i=i_1c: \langle \exists j: iMj: a=\pi_1j \rangle \rangle: agc=resa \rangle: agc \rangle$$

\Rightarrow

$$\langle \forall c, t: (c|c)M(c, t): agc=resc \rangle \vee M(c, t): (c|c)M(c, t): agc \rangle$$

$$\langle \forall c, t: (c|c)M(c, t): agc=resc \rangle \vee M(c, t): (c|c)M(c, t): agc \rangle$$

$$\langle \forall c, t: (c|c)M(c, t): agc=resc \rangle \vee M(c, t): (c|c)M(c, t): agc \rangle$$

$$6) \text{ maybe}(S \leftarrow id + R \leftarrow (S \leftarrow R) \leftarrow S) \text{ maybe}$$

(\Rightarrow)

$$\text{maybe} \cdot S \subseteq (S \leftarrow id + R \leftarrow (S \leftarrow R)) \cdot \text{maybe}$$

(\Leftarrow)

$$aSb \Rightarrow (\text{maybe } a)(S \leftarrow id + R \leftarrow (S \leftarrow R))(\text{maybe } b)$$

(\Rightarrow)

$$aSb \Rightarrow (\text{maybe } a) \cdot (S \leftarrow R) \subseteq (S \leftarrow id + R) \cdot (\text{maybe } b)$$

(\Leftarrow)

$$aSb \wedge \beta(S \leftarrow R)g \Rightarrow (\text{maybe } a \beta)(S \leftarrow id + R)(\text{maybe } b g)$$

(\Rightarrow)

$$aSb \wedge \beta \cdot R \subseteq S \cdot g \Rightarrow (\text{maybe } a \beta) \cdot (id + R) \subseteq S \cdot (\text{maybe } b g)$$

$$R, S := id, s$$

$$a = sb \wedge \beta = s \cdot g \Rightarrow (\text{maybe}(sb))(s \cdot g) = s \cdot \text{maybe } b g$$

$$8) \in \cdot \Delta R = R$$

$$(\Rightarrow) \{F9, f = \Delta R\}$$

$$\Delta R = \Delta R$$

$$(\Rightarrow) \{\text{trivial}\}$$

True

$$\Delta R \cdot \beta = \Delta(R \cdot \beta)$$

$$(\Rightarrow) \{F9\}$$

$$\in \cdot \Delta R \cdot \beta = R \cdot \beta$$

$$(\Rightarrow) \{F10\}$$

$$R \cdot \beta = R \cdot \beta$$

$$(\Rightarrow) \{\text{trivial}\}$$

true