

Practice Problems

- 1) When will the Quicksort perform poorly (worst case)?
- 2) We have a system running insertion sort and we find that it's completing faster than expected. What could we conclude about the input to the sorting algorithm?
- 3) Explain which sorting algorithm you would use to sort the input array the fastest and why you chose this sorting algorithm. An array of n Comparable objects that is sorted except for k randomly located elements that are out of place (that is, the list without these k elements would be completely sorted)
- 4) Which sorting algorithm will have the best time complexity for sorting this array?
Select one of them: Bubble | Selection | Insertion

a. 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | -3 | -4

b. 1 | 15 | 3 | 4 | 5 | 8 | 10 | 12 | 13 | 2

c. 32 | 27 | 25 | 5 | 9 | 10 | 15 | 18 | 22 | 24

5)

Given an array, apply Shell Sort on it:

| | | | | | | | |
|---|---|---|---|---|---|---|---|
| 9 | 8 | 3 | 7 | 5 | 6 | 4 | 1 |
|---|---|---|---|---|---|---|---|

```
void shellSort(int array[], int n)
{
    for (int interval = n / 2; interval > 0; interval /= 2)
    {
        for (int i = interval; i < n; i += 1)
        {
            int temp = array[i];
            int j;
            for (j = i; j >= interval && array[j - interval] > temp; j -= interval)
            {
                array[j] = array[j - interval];
            }
            array[j] = temp;
        }
    }
}
```

1. Perform Dry run of the code and show array at each step. [10 marks]
2. Indicate the best and worst case of given algorithm in terms of Big -Oh [5 marks]

Solutions

- 1) Quicksort has a worst case runtime of $\Theta(N^2)$, if the array is partitioned very unevenly at each iteration.
- 2) Input already sorted.
- 3) Sort: Insertion sort
Runtime: $O(nk)$
Explanation: For the $n - k$ sorted elements, insertion sort only needs 1 comparison to check that it is in the correct location (larger than the last element in the sorted section). The re-maining k out-of-place elements could be located anywhere in the sorted section. In the worst case, they would be inserted at the beginning of the sorted section, which means there are $O(n)$ comparisons in the worst-case for these k elements. This leads to an overall runtime of $O(nk + n)$, which simplifies to $O(nk)$.
- 4)
 - a. Insertion sort
 - b. -
 - c. --