

2019



Data Science and AI

Module 4

Introduction to Machine Learning/Regression



Agenda: Module 4

- Introduction to Machine Learning
- The **Predictive** Modelling Process
- Feature Selection
- Measuring the Accuracy of Regression Models
- Overfitting



Introduction to Machine Learning

- Supervised Learning
- Unsupervised Learning
- Regression
- Classification



"All models are wrong; some are useful!"

George Edward Pelham Box (1919-2013)





Supervised Learning

• The main characteristic of **Supervised Learning** is to have previously known results

- Consider data collected from cases with known input and output
 - Cases can also be called observations, experiments, results, etc.
 - Input can also be called variables; input, explanatory or independent variables; features; predictors
 - Output can also be called output or dependent variable; label; result; outcome; response
- Supervised learning relies on induction:
 - the inference of a general law from particular instances.



Supervised Learning

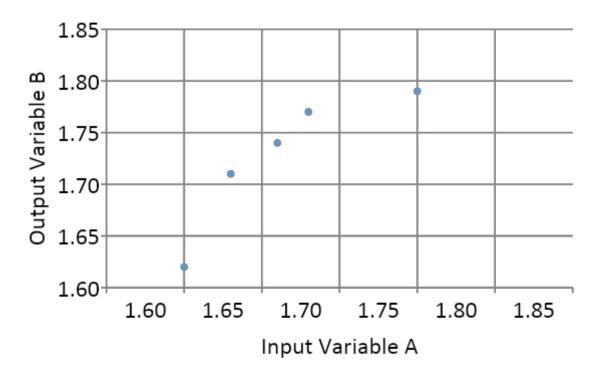
- The majority of practical Machine Learning uses Supervised Learning.
- Knowing the values of an input variable A and an output variable B can be the source of a model to predict future outcomes of B given a new input of A
- Definition:
 - Supervised learning is where you have input variables (x) and an output variable
 (Y) and you use an algorithm to learn the mapping function from the input to
 the output Y = f(X)



Supervised Learning

• The computer will find a function by the analysis of input-output pairs, so it can be used to predict future results in similar conditions

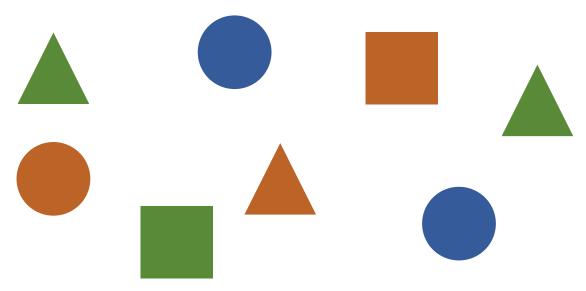
А	В
1.71	1.74
1.65	1.62
1.80	1.79
1.68	1.71
1.73	1.77





Unsupervised Learning

- The main characteristic of Unsupervised Learning is to have unknown prior outcomes
- Consider data collected from **observations** of which **only** the **input** is **known**. For example the collection of customers or transactions





Unsupervised Learning

 The computer will infer a function by the analysis of similar characteristics or proximity of the input examples, so it can be used to predict future results in the same conditions









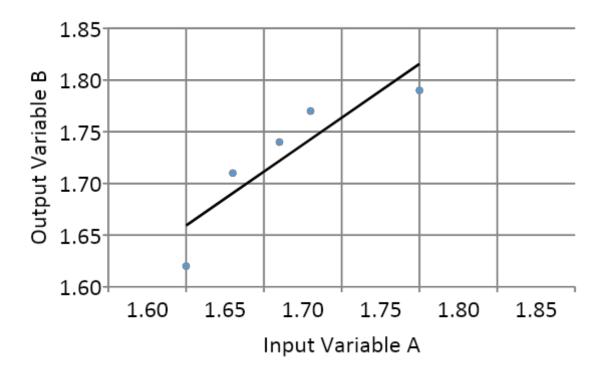
Regression

- What characterises **Regression** is to obtain a **scalar result**, a number
 - Regression results can have a value range from -∞ to ∞
- Tries to answer questions like: How Much / How Many?
 - What will the temperature be tomorrow?
 - How many new followers will be in the next week?
- Set of statistical processes for estimating the relationships among variables
 - One independent variable: univariate analysis
 - More than one independent variable: multivariate analysis



(Univariate) Regression

• A function of changes in any one independent variable (holding others fixed)





Classification

- What characterises Classification is to identify a class or group
 - Classification results can be a value within the domain set

• Set of statistical processes to determine membership or similarity



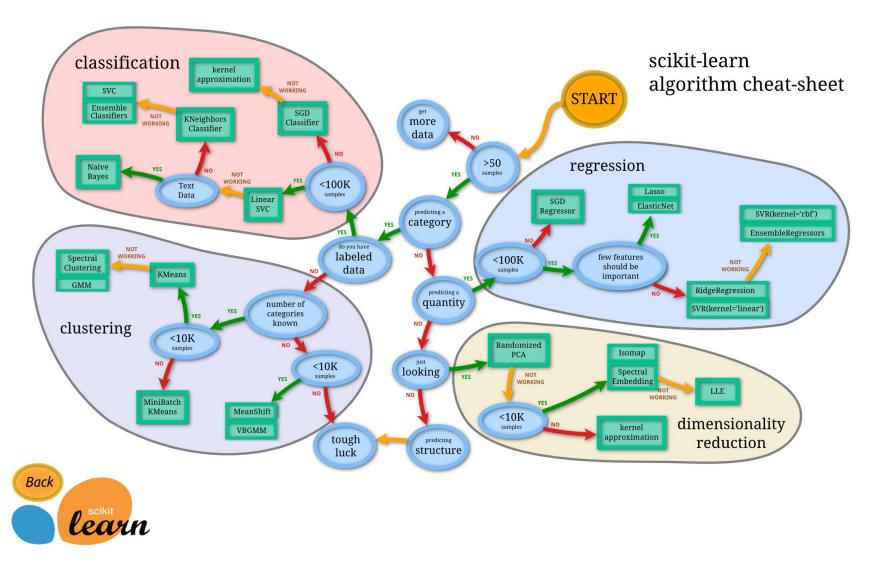
Classification

- Two classes (Binary classification): (Yes, No), (Positive, Negative)
 - Answer questions like:
 - Will the customer renew their subscription?
 - Will the website visitor click the submit button?

- More than two classes: A set of possible categories, classes or groups
 - Answer questions like:
 - Which animal is in this image?
 - What is the genre of this movie?



Scikit-Learn Cheat-Sheet





All together

	Supervised	Unsupervised
Discrete	Classification	Clustering
Continuous	Regression	Dimensionality Reduction



The Predictive Modelling Process

- Outline
- Data Science Process
- Defining the Response Variable
- Defining the Cost Function
- A Familiar Example: Univariate Linear Regression
- Multivariate Linear Regression
- Partitioning Data
- Model Training
- Model Testing



Outline

- data | 'deItə |, noun
 - facts and statistics collected together for reference or analysis
 - (Philosophy) things known or assumed as facts, making the basis of reasoning or calculation
 - ORIGIN: mid 17th century; from Latin, the plural of datum
- science | 'sAIƏns |, noun
 - the intellectual and practical activity encompassing the **systematic study** of the structure and behaviour of the physical and natural world through observation and experiment
 - ORIGIN: Middle English (denoting knowledge): from Old French, from Latin *scientia*, from *scire* 'know'



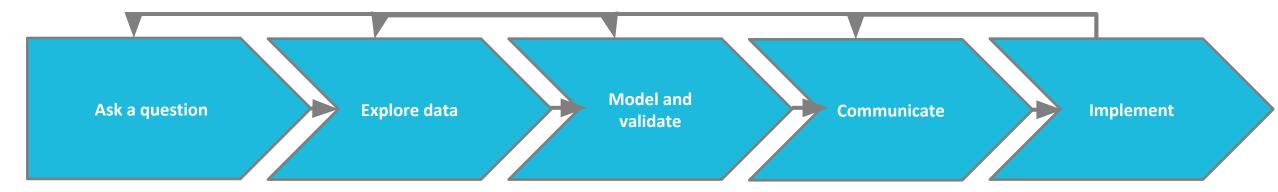
Outline

- Data Science: Systematic use of data to identify insights and inform decisions
- Data science is an interdisciplinary field that uses scientific methods, processes, algorithms and systems to extract *information*, *knowledge* and *insights* from both structured and unstructured data.
- Data science is a "concept to unify statistics, data analysis, machine learning and their related methods" to "understand and analyse actual phenomena" with data. It employs techniques and theories drawn from many fields within the context of mathematics, statistics, information science and computer science.



Data Science Process

Iterate



- Ask a (business) question
- Define objective and strategy

- Identify and collect, clean and transform data
- Explore data
- Ascertain quality and ability to answer questions

- Determine target and feature variables
- Select model, apply and validate
- c Communicate to stakeholders and obtain buy in

- Develop end-to-end solution
- Build, test, deploy and monitor

Most important step!

May consume large proportion of the total effort

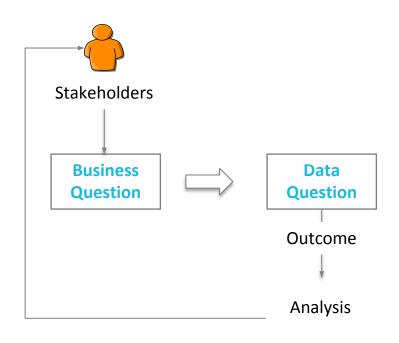
Feature engineering requires deep domain knowledge

Perform as early and as often as possible

Consider the total cost of implementation earlier in the process



Defining the Outcome/ Response Variable



- Your question leads to the selection of the outcome/ response variable:
 - To answer the question
 - You could frame it as a hypothesis that can be statistically tested
- The initial step to answer the question is to define which is the Response Variable and its characteristics, such as type and range
- Some modelling techniques that are only relevant to a particular type of variable, so knowing the nature of the response variable can reduce the number of approaches to consider



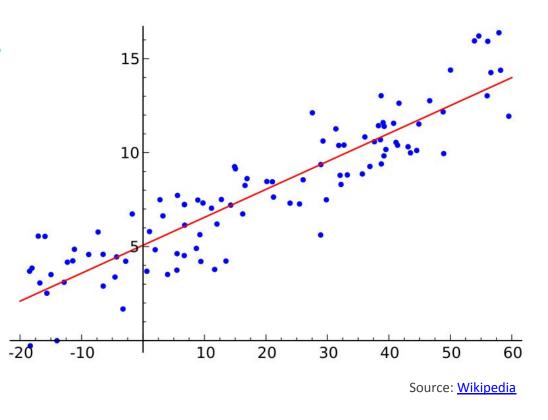
Defining the Cost Function

- A cost function calculates how close the model can estimate the relationship between the input variables (X) and output variable (y)
- In other words, it describes how wrong the model is by how far off its predictions are in comparison to reality
- Some traditional statistical methods such Linear Regression have error metrics associated with it, like MSE (Mean Squared Error)



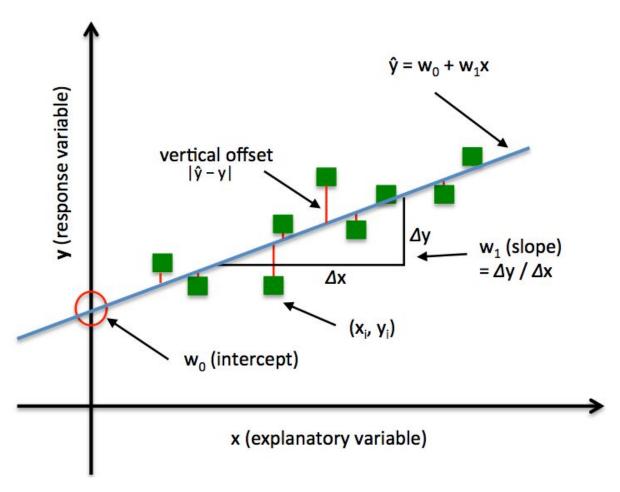
A Familiar Example: Univariate Linear Regression

- The relationship between a continuous variable and other independent variables
- Explain the relationship between x and y using the starting point a and the power in explanation b
- The simplest version is just a line of best fit





Example: Univariate Linear Regression



Source: MLxtend



Multivariate Linear Regression

However, linear regression uses linear algebra to explain the relationship between y
and multiple x

- Explains the relationship
 - Between a Matrix X and a Dependent Vector y
 - By using a y-intercept alpha and the relative coefficients beta



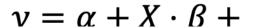
Multivariate Linear Regression

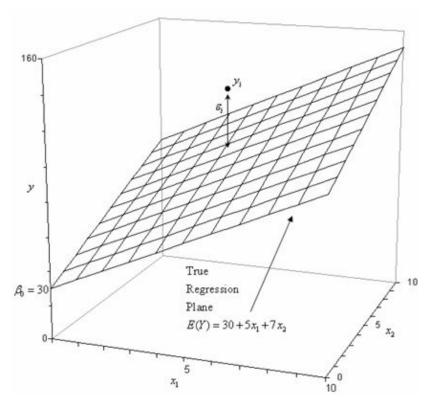
$$\nu = \alpha + X \cdot \beta +$$

$$\begin{bmatrix} y_1 \\ y_2 \\ y_3 \\ \cdots \\ y_n \end{bmatrix} = \begin{bmatrix} 1 & x_{1,1} & x_{1,2} & x_{1,3} & \cdots & x_{1,m} \\ 1 & x_{2,1} & x_{2,2} & x_{2,3} & \cdots & x_{2,m} \\ 1 & x_{3,1} & x_{3,2} & x_{3,3} & \cdots & x_{3,m} \\ \cdots & \cdots & \cdots & \cdots & \cdots \\ 1 & x_{n,1} & x_{n,2} & x_{n,3} & \cdots & x_{n,m} \end{bmatrix} \cdot \begin{bmatrix} \alpha \\ \beta_1 \\ \beta_2 \\ \beta_3 \\ \cdots \\ \beta_m \end{bmatrix} + \begin{bmatrix} \epsilon_1 \\ \epsilon_2 \\ \epsilon_3 \\ \cdots \\ \epsilon_n \end{bmatrix}$$



Multivariate Linear Regression





Source: Reliawiki

Source: MathWorks



Linear Regression

- Linear Regression works best when
 - The data is normally distributed (but does not have to be)
 - Xs significantly explain y (have low p-values)
 - Xs are **independent** from one another (low multicollinearity/ correlation)



Model Training, evaluation and testing

- Application of one or more modelling techniques on the training data aiming for a model with either or both better performance and lower cost
- Collect evaluation results for each technique, each set of variables
- Refine and select the best model for testing
- Optionally explore a combination of techniques
- Test and compare metrics with previous results



Discussion

What do you think about the terms "Data Science" and "Machine Learning"?

What do they mean?

Are they meaningful/ practical term?

Any Questions?



Partitioning Data

 Models are simplified representations of reality created from data that can be used to estimate future outcomes better

 To validate the models, it is necessary to simulate existing data and future data, hence the need to use existing data to play those roles

- The Quality of data is more critical than the Quantity of data
 - Data must be representative
 - Large quantities may incur in higher storage and computation costs without improving the model's performance



Partitioning Data

- Existing data can be **split** into (percentages shown are common, not a rule):
 - Training (70%) and Testing (30%), or
 - Training (65%), Validation (20%) and Testing (15%)
- Training (Learning) Data is used during the development of the model
- Validation Data can be used to improve the performance of the model
- Test Data is used to check the performance of the model with unseen data
- Data split must be random



Lab 4.1.1: Linear Regression from scratch

- Purpose
 - To develop familiarity with the Data Science Process
- Resources
 - Sample data
- Materials
 - Jupyter Notebook (Lab-4.1.1)



Lab 4.1.2: Splitting Data

- Purpose
 - To develop familiarity with the Data Science Process
 - Split data for model development and evaluation
- Resources
 - Sample data from SciKit-Learn
- Materials
 - Jupyter Notebook (Lab-4.1.2)



Feature Selection

- Forward and Backward Stepwise Feature Selection
- Feature Engineering



Forward and Backward Stepwise Feature Selection

- Occam's razor (also Ockham's razor or Ocham's razor; Latin: lex parsimoniae
 "law of parsimony") is the problem-solving principle that the simplest solution
 tends to be the right one.
 - When presented with competing hypotheses to solve a problem, one should select the solution with the fewest assumptions
 - The idea is attributed to William of Ockham (c. 1287–1347), who was an English Franciscan friar, scholastic philosopher, and theologian

<u>Wikipedia</u>



Forward and Backward Stepwise Feature Selection

- Forward Feature Selection
 - Take **each** of the predictors **individually** and select the variable from the model that explains the output variable the best
 - Repeat the process by adding the remaining predictors individually until there is no significant improvement
- Backward Feature Selection
 - Take all of the predictors and create a model
 - Remove each of the predictors individually and keep the model that explains the output variable the best
 - Repeat the process by removing the remaining predictors individually until there is a significant reduction in performance



Feature Engineering

- Feature Engineering can be described as the process of transforming the variables into forms or domains suitable both to the underlying problem and to computation
- Modelling techniques manipulate numbers to optimise parameters and coefficients used in functions
- Not all techniques can manipulate nominal and ordinal variables (classes, categories)



Feature Engineering

• There are no specific rules in cases when the data manipulation relates to particular problems, industries or businesses

- Some data manipulations are mode specific to the chosen modelling approaches, such:
 - Variables transformation from nominal/ordinal to numeric
 - A common practice is to use one hot encoding
 - Change of scale or range for numeric variables
 - Variables with different orders of magnitude (A:0-10, B:300-9000) can be normalised to be closer to each other (A:0-1, B:0-1)



Lab 4.2: Feature Selection

- Purpose
 - To understand Forward Feature Selection
- Resources
 - Sample data from SciKit-Learn
- Materials
 - Jupyter Notebook (Lab-4_2_1, Lab-4_2_2)



Measuring the Accuracy of Regression Models

- Introduction
- R-Squared
- Mean Squared Error (MSE)



Introduction

- It is possible to compare the known results with the ones predicted by the model when using **Supervised modelling**
- When comparing known and predict results it is possible to make calculations and create metrics on how close or similar there outcomes are
- Such metrics can both tell how "good" or how "efficient" a model is and how it compares to other models as most metrics have standard results



R-Squared

- Is the central metric introduced for Linear Regression
- It determines how much of the variation in y is explained by the change in X
 - But does it tell the magnitude or scale of error?
- The value range is between:
 - 0: the model does not model explain any variability in y
 - 1: the model explains full variability in the target variable
- Exploring cost or loss functions can be used to refine the models



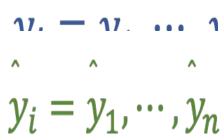
R-Square and Residuals

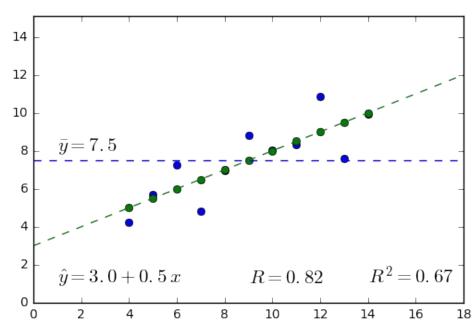
- In a data set with n cases where the outputs are:
- And the predicted values are (note the *y-hat*):
- SS: Sum of Squares
- The mean of y is (note the y-bar):

$$\overline{y} = \frac{1}{n} \sum_{i=1}^{n} y_i$$

$$SS_{tot} = SS_{reg} + SS$$

$$R^2 = \frac{SS_{reg}}{SS_{tot}}$$







R-Square and Sum of Squares (SS)

Total SS

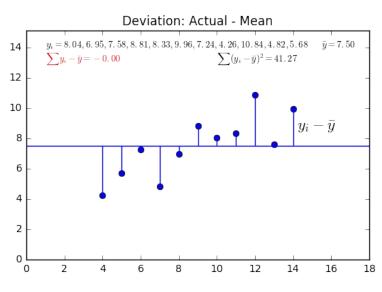
$$SS_{tot} = \sum_{i=1}^{n} (y_1 - \overline{y})$$

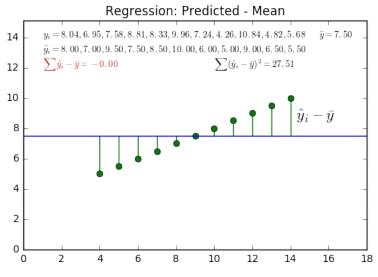
Regression

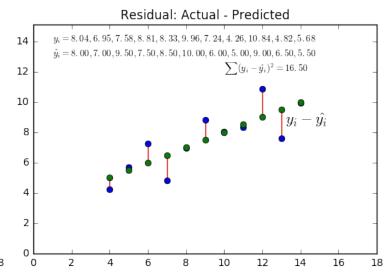
$$SS_{reg} = \sum_{i=1}^{ss} (\hat{y}_1 - \overline{y})$$

Residual

$$SS_{tot} = \sum_{i=1}^{n} (y_1 - \overline{y})$$
 $SS_{reg} = \sum_{i=1}^{ss} (y_1 - \overline{y})$ $SS_{res} = \sum_{i=1}^{n} (y_1 - y_1)$









Adjusted R-Squared

- The Adjusted R-Square is the R-Square adjusted for the **number of predictors** in the model
- It incorporates a model's degree of freedom
- Adjusted R-Square only increases if the new term improves the model accuracy

$$AdjustedR^{2} = 1 - \frac{(1 - R^{2})(N - N)}{N - N}$$

- where
 - R² = Sample R-Square
 - N = total sample size
 - p = Number of predictors



Residual Error

- In linear models, the residual error must be normal with a median close to zero
- Individual residuals are useful to see the error of specific points, but it does not provide an overall picture for optimisation
- It is necessary a metric to summarise the error in the model into one value
 - Mean Square Error: the mean residual error in our model



Mean Square Error (MSE)

- Calculate the difference between each target y and the model's predicted value y-hat (i.e. the residual)
- Take the mean of the squared residual errors

$$MSE = \frac{1}{n} \sum_{i=1}^{n} (y_i - y_i)^2$$

- The MSE is always greater or equal to zero, with smaller errors being better
- An MSE of 0 means that actual and predicted results are identical



Minimising the Error, MSE as Cost Function

- The linear regression method with MSE is also known as:
 - Ordinary Least Squares

- Meaning that given a matrix X
 - Solve for the least amount of square error for y

- Assuming that X is unbiased
 - Saying it is representative of the population



Lab 4.3: Measurements

- Purpose
 - To compare model complexity
- Resources
 - Sample data from SciKit-Learn
- Materials
 - Jupyter Notebook (Lab-4_3)



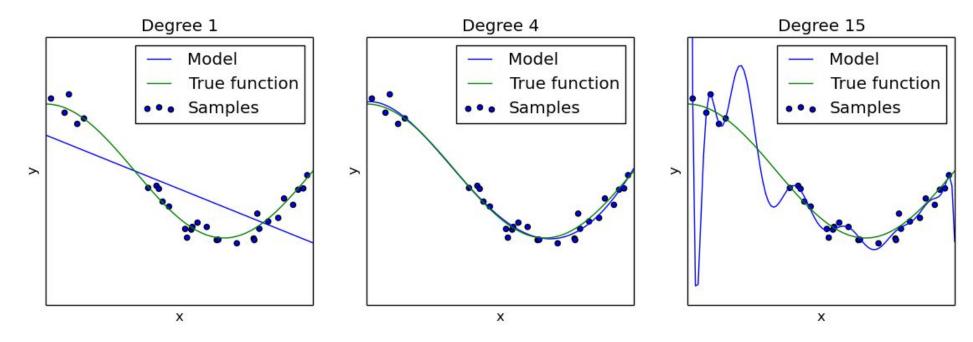
Overfitting

- Detecting Overfitting
- Avoiding Overfitting
- Cross-Validation
- Regularisation



Overfitting

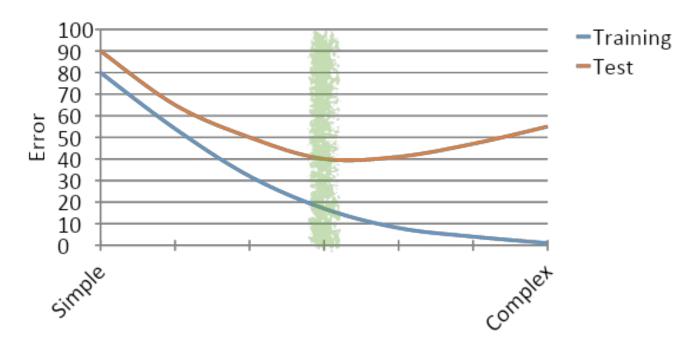
- The first model poorly explains the data (underfitting)
- The second model describes the general curve of the data
- The third model drastically overfits the model, bending to every point





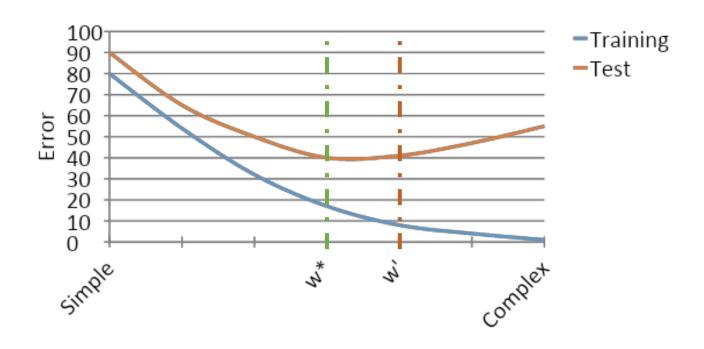
Detecting Overfitting

Mathematically modelling is to fit a curve to a set of known data points, so
overfitting is to find a curve that fits the known data points very closely but does
not generalise well to unknown data points





Detecting Overfitting



- Overfitting:
 - Training Error(w*) > Training Error(w')
 - Test Error(w*) < Test Error(w')



Avoiding Overfitting

- Have the data split into a training set and a test set
 - Works well only with the availability of large datasets
- To find out the best model (training error) the residual sum of squares is used
- Varies model complexity
 - Includes varying the set of variables and data manipulation
- Continuously updated the parameters/coefficients/weights
- Use techniques such as Cross-Validation and Regularisation



Cross-Validation

- The goal of cross-validation is to test a model's ability to predict new data that was not used in estimating it
 - Used to flag problems like overfitting and to give an insight on how the model will generalise to an independent dataset
- General Process
 - Generate several models on different cross-sections of the data
 - Partition the data in separate data sets alternating their roles as Training and Test
 - Measure the performance of each iteration
 - Take the overall performance
 - Usually the mean of the collected results



Common types of Cross-Validation Exhaustive cross-validation

All distinct ways to divide the original sample are used to learn and test

- Leave-p-out
 - Use p observations as the test set and the remaining as the training set
 - This is repeated in all ways to cut the original sample on a validation set of p
 observations and a training set



Common types of Cross-Validation Non-exhaustive cross-validation

- •Do not compute all ways of splitting the original sample; these methods are approximations of leave-p-out cross-validation
- •k-fold
 - The original sample is randomly partitioned into k equal sized subsamples
 - •In stratified k-fold cross-validation, the folds are selected so that the mean response value is approximately equal in all the folds
- Holdout method
 - Randomly assign data points to two sets do and d1, usually called the training and the test sets, respectively
 - •The size of each of the sets is arbitrary although typically the test set is smaller than the training set



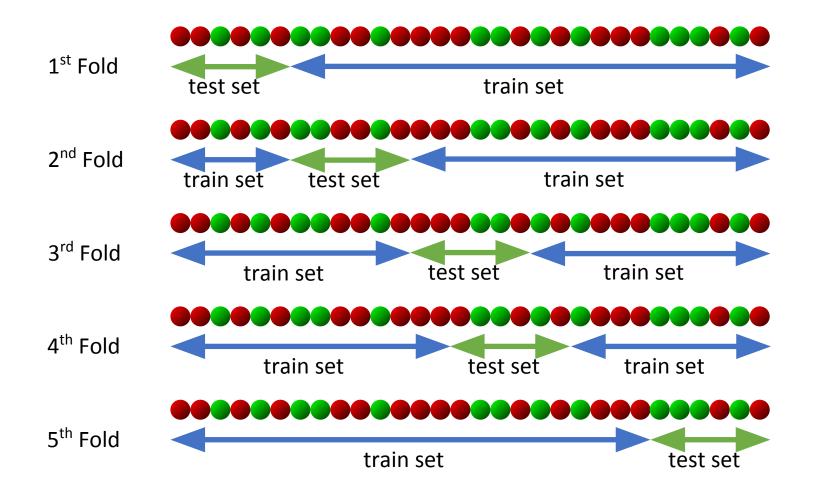
k-Fold Cross-Validation

- k-fold cross-validation
 - Split the data into k group
 - Train the model in all segments except one
 - Test model performance on the remaining set

• If k = 5, split the data into five segments and generate five models



Cross-Validation





Cross-Validation

- Computational issues
 - Straightforward to implement if the prediction method being studied is available
 - If the prediction method is **expensive** to train, cross-validation can be very slow since the training must be carried out repeatedly
- Limitations
 - Cross-validation only yields meaningful results if the validation set and training set are drawn from the same population and only if human biases are controlled
- Cross validation for time-series models
 - •Since the order of the data is important, cross-validation might be problematic for time-series models
 - A more appropriate approach might be to use forward chaining



Regularisation

- Form of regression, that constrains or shrinks the coefficient estimates towards zero
 - This technique discourages a more complex model to avoid the risk of overfitting

- Given a set of p coefficient (β_p) , the fitting procedure involves a loss function (RSS or SS_{res})
 - The coefficients are chosen, such that they minimise the loss function by adding an "extra cost"

 The estimated coefficients do not generalise well with unseen data if there is noise in the training data



Regularisation

- The are multiple forms or regularisation, the most common being:
 - Ridge Regression
 - Adds cost by the inclusion of a new parameter called lambda (
 - Lasso Regression
 - Adds cost by the addition of a new parameter called lambda (
 - Can force coefficients to be zero, hence effectively removing them from the model



Regularisation - Ridge Regression

The RSS is added a shrinkage quantity

$$RSS + \lambda \sum_{j=1}^{p} \beta_j^2$$

The coefficients are estimated by minimising the new function

• The coefficient λ is the parameter that controls how much to penalise the model

The Ridge Regression force coefficients to stay low



Regularisation - Ridge Regression

• When $\lambda=0$, the penalty term has no effect and the estimates produced by Ridge regression will be equal to Least Squares

• It is necessary to standardise the predictors or bring the predictors to the same scale before performing Ridge regression



Regularisation - Lasso Regression

ullet It penalises the high coefficients by using $|oldsymbol{eta}_j|$

$$RSS + \lambda \sum_{j=1}^{p} |\beta_j|$$

- Ridge regression will shrink the coefficients for least important predictors, very close to zero, but never make them precisely zero
 - The final model will include all predictors
- Lasso regression can force some of the coefficient estimates to be equal to zero when the tuning parameter λ is sufficiently large
 - The lasso method also performs variable selection and is said to yield sparse models



Lab 4.4: Regularisation

- Purpose
 - To compare some regularisation approaches
- Resources
 - Sample data from SciKit-Learn
- Materials
 - Jupyter Notebook (Lab-4_4)



Discussion: Lasso or Ridge

When to use Lasso or Ridge regressions?



Project II

- Purpose
 - Apply the **Data Science Process** on an area of your choice
- 1. Choose a dataset from Google Public Datasets, scikit-Learn or anywhere else; or select a question and identify and gather the data you need
- 2. Constraint it to the prediction of a continuous value
- 3. Follow the steps presented in the course so far,
 - a) Perform **EDA** on the data
 - b) Select the outcome/ response variable
 - c) Select **features**
 - d) Select approach/ model
 - e) Apply the model and evaluate it
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Questions?





End of presentation

