



2019

Data Science and AI

Module 3 Part 2:

Data Science Practice 1/2



Agenda: Module 3 Part 2

- Defining **Data Science**
- **Hypothesising**
- Statistical **Evidence**
- Statistical **Proof**
- **Causation**
- Statistical **Inferences**

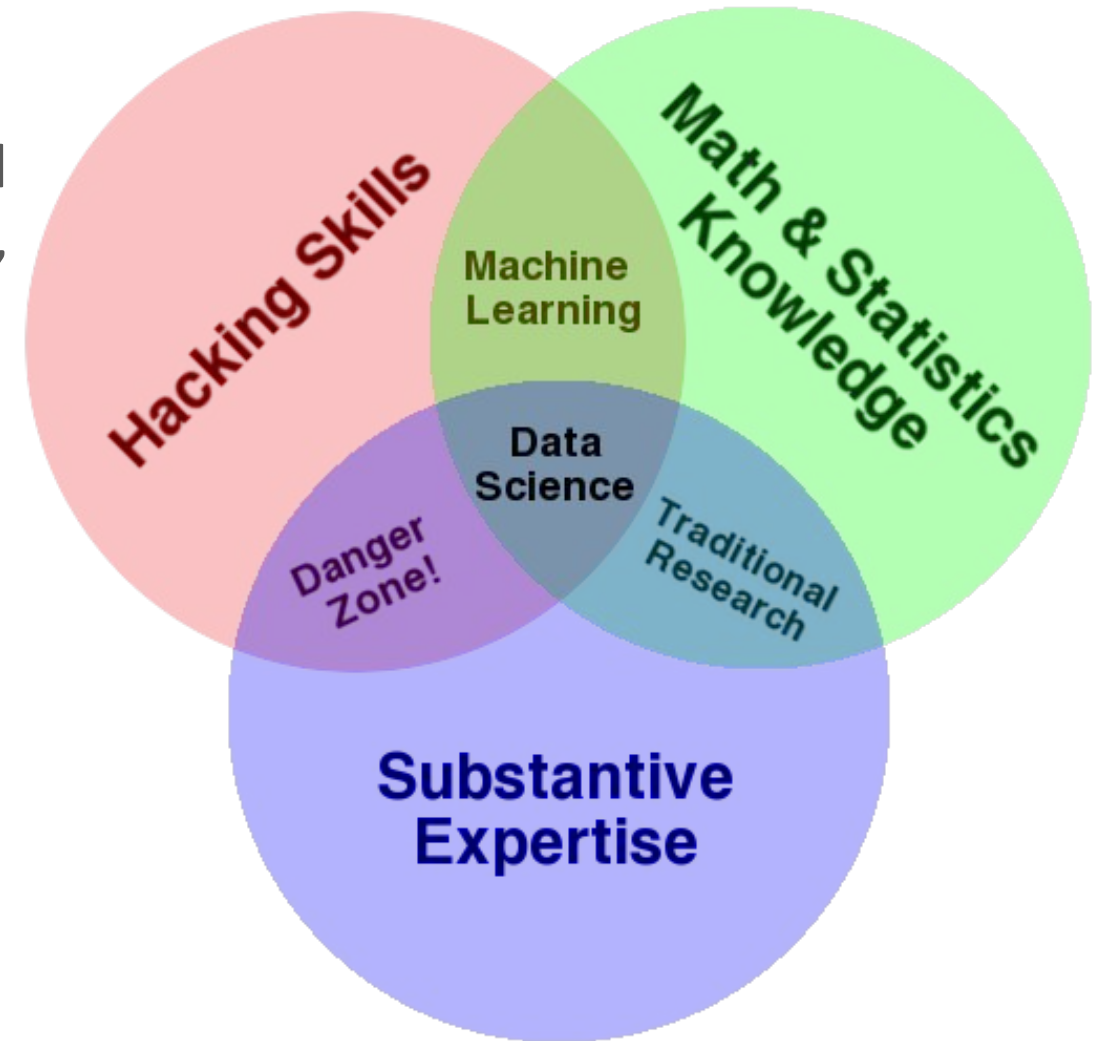


Defining Data Science

- What is **Data Science**?
- Users and **use cases**
- What makes a **Data Scientist**?
- The Data Science **pipeline**
- **Testable** hypotheses

What is Data Science?

- Data Science is a **multi-disciplinary** field that uses **scientific methods**, processes, algorithms and systems to extract **knowledge** and insights from structured and unstructured data
- business analysis on steroids
- the application of scientific method to practical problems

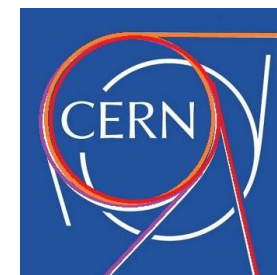


Drew Conway

Who Uses Data Science?

NETFLIX

amazon.com[®]



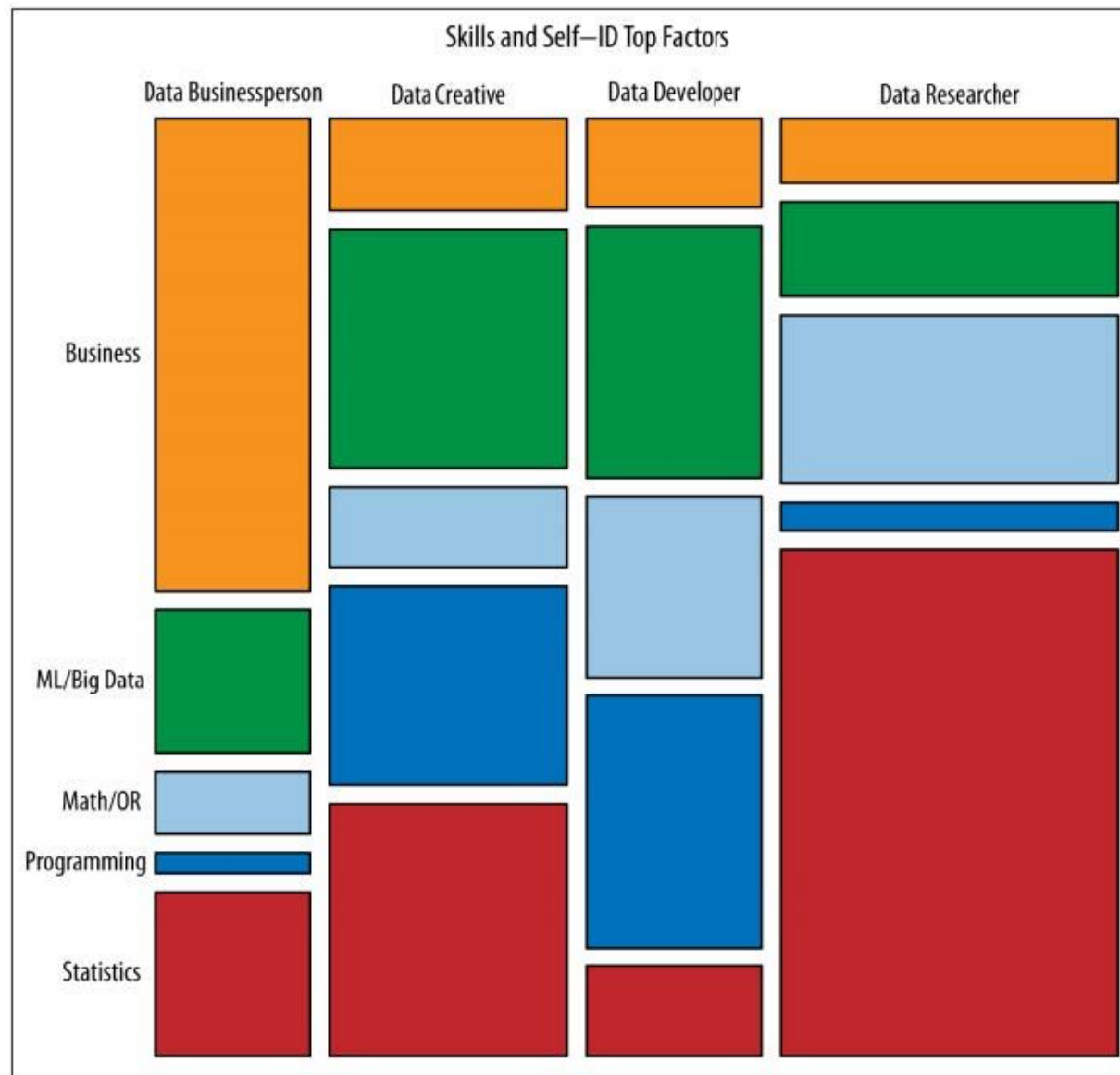
Where do Data Scientists come from?

What are their typical strengths?

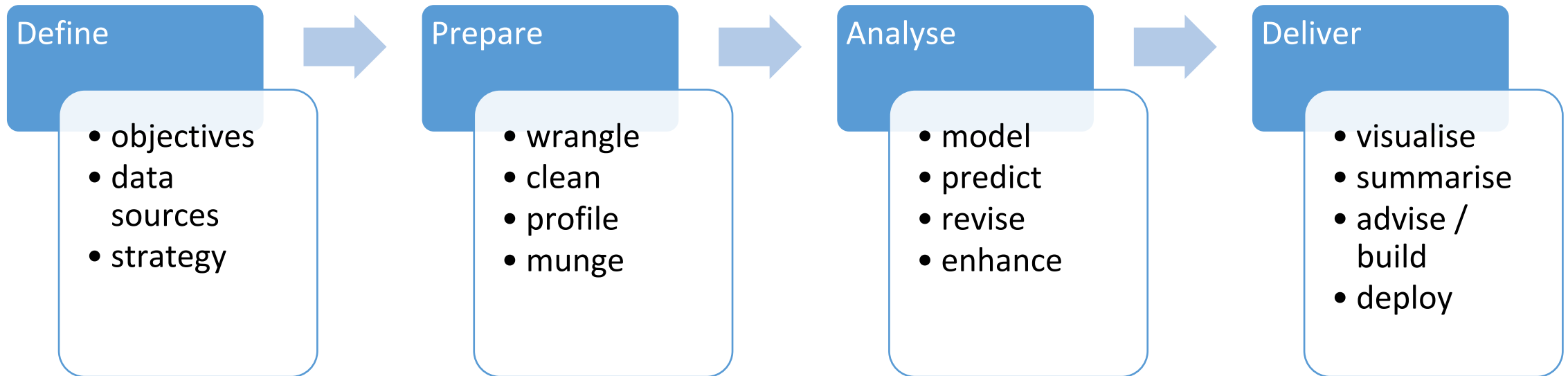
	Programming Skills	Math & Stats	Substantive Expertise	Methodology	Abstraction	Communication
Data Science program graduates						
Scientists (especially physics)						
Statisticians						
Developers						
Business Analysts						

Relative Strengths

- These roles prioritize different skill sets.
- All roles involve some part of each skillset.
- *Where are your ambitions?*
- *Where are your strengths and weaknesses?*



The Data Science Pipeline



Defining the Problem

Every Solution Begins with a **Question**

- any business problem, decision-support tool, or clever data product begins life with a well-defined **need**:
 - a set of **questions** that frame an analysis
- sets up for a successful **process**
- establishes the basis for **reproducibility**
- creates scope for future **expansion**



“A problem **well stated** is half solved.”

— Charles Kettering



“Judge a man by his **questions** rather than by his answers.”

— Voltaire

How to specify the question

A business challenge may be vague:

- “**How** can we grow our online market share?”

Data science questions need to be focused and ideally **quantitative** :

- “**What** is the conversion rate of our website (visitors->subscribers)?”
- “**How much** was our profit over the last 12 months?”
- “**When** did the stock price start to go below \$5.00?”

The Elements of a Good Question

Specific

The dataset and key variables are clearly defined.

Measurable

The type of analysis and major assumptions are articulated.

Attainable

The available data are amenable to the question and unlikely to be biased.

Reproducible

The analysis can be repeated by another person or at another time.

Time-bound

The time period and population to which the analysis pertains is clearly stated.

Knowledge check

Does this question follow the SMART framework:

“Is there an association between number of passengers with carry-on luggage and delayed take-off time?”

Knowledge check

How about this (revised) question:

“Is there an association between the number of passengers (on JetBlue, Delta, and United domestic flights) with carry-on luggage and delayed take-off time in the data from flightstats.com between January 2015 and December 2015?”

Dataset Characteristics

- What would we look for if we wanted to be able to describe a dataset?
 - size, completeness
 - periodicity, stationarity
 - bias
 - missing variables
 - correlated variables
 - due to causation or covariation
 - correlated samples
 - time series / Markov series
 - contaminated or prejudiced sampling
 - study design

Data Temporality

Cross-sectional

- 'static'
- treated as a **snapshot** in time
- causality is simultaneous

Longitudinal

- **'time series'**
- treated as a series of snapshots with a temporal or serial dependence

Dynamic

- **'streaming'**
- continuously accumulated or refreshed

Variables in Data Science

Features
Predictors

Independent variables
Inputs

A ***predictor*** is a ***feature*** that is useful in modelling the *response*. Specifically, its inclusion enables a *model* to account for more of the *variance* in the response.

Responses
Outcomes

Dependent variables
Outputs

A **covariate** is a variable that is possibly predictive of the response. It could also represent an interacting variable.

A **confounding** variable is one which influences the response but has not been measured (i.e. it introduces bias).

Data Preparation

def: Tidy data: the end goal of data cleaning and munging

- each **variable** should be in **one column**
 - each **observation** should comprise **one row**
 - each **type of observational** unit should form **one table**
 - key columns for **linking** multiple tables
 - top row contains (sensible) **variable names**
 - in general, save data as one file per table
-
- search: “Hadley Wickham's tidy data paper”

Lab 3.2.1: Hypothesising

- Purpose:
 - To create a testable hypothesis
- Resources:
 - 'titanic.csv'
- Instructions:
 1. You should already be familiar with the 'titanic' dataset from the last module's homework. Now, think about what stories the data might tell, and devise a hypothesis that could be tested.
 2. Provide some data profiling results to support your assertion that this hypothesis is testable.





Statistical Evidence

- What is **statistical proof**?
- Revisiting the **null hypothesis**
- The Student's **t-test**

Statistical Proof

Can a hypothesis be proved?

- in science, **no theory (or hypothesis) can actually be proved**
 - must explain known phenomenon
 - must make **testable predictions**
 - will gain acceptance if it **survives** rigorous testing

How can a hypothesis be tested?

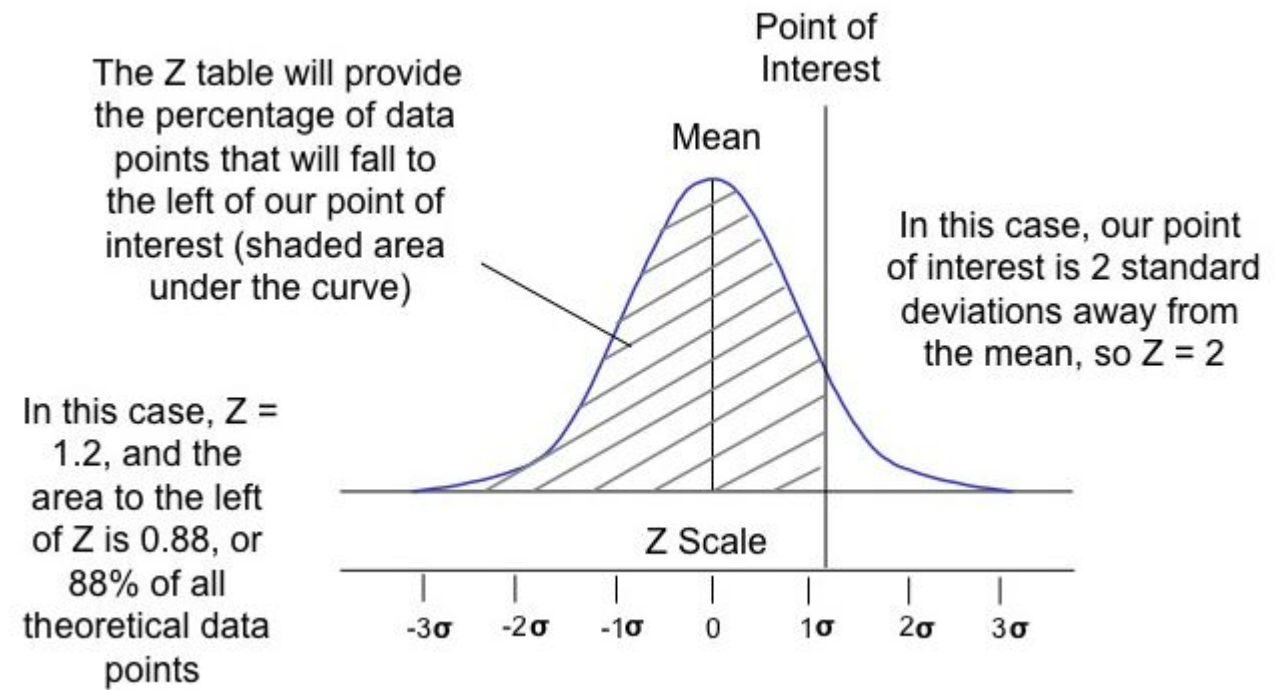
- by formulating it in a way that makes **its claims amenable to statistical analysis**
 - must **explain** the data
 - must have a corresponding **null hypothesis** that can be rejected at a predefined level of confidence

Statistical Proof – cont'd

• Z-statistic

$$Z = \frac{\bar{X} - \mu}{\sigma}$$

- Provides a measure of the **likelihood** that a data point belongs to a given population



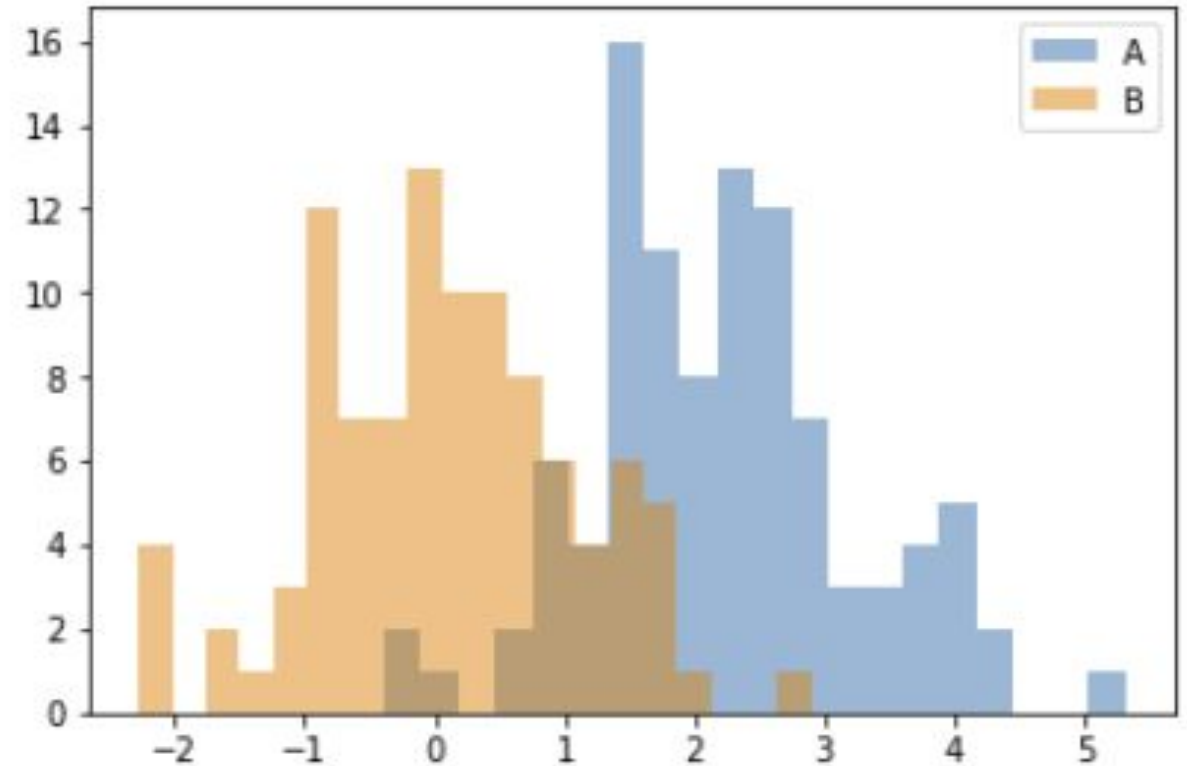
The Null Hypothesis

Example:

- dataset comprised of patients' responses to two different therapies:
 - **drug A** (the old drug, or 'control' treatment)
 - **drug B** (the new drug, or 'test' treatment).
- we are interested in testing the *alternative hypothesis H_a* :
 - A & B deliver significantly different outcomes
- but we do this by assuming (and then trying to reject) the *null hypothesis H_0* :
 - there is **no** significant difference between A & B
 - the distributions we get from the 'A' data and the 'B' data represent two sample sets from the same 'population'

Testing the Null Hypothesis for Two Samples

- Given two samples, A and B
 - compute the means X_A, X_B
 - compute the variances σ^2_A, σ^2_B
 - calculate how close X_A is to X_B given the uncertainty implied by their variances
 - calculate the likelihood that this value of our closeness parameter could be obtained at random



The Student's t -Test

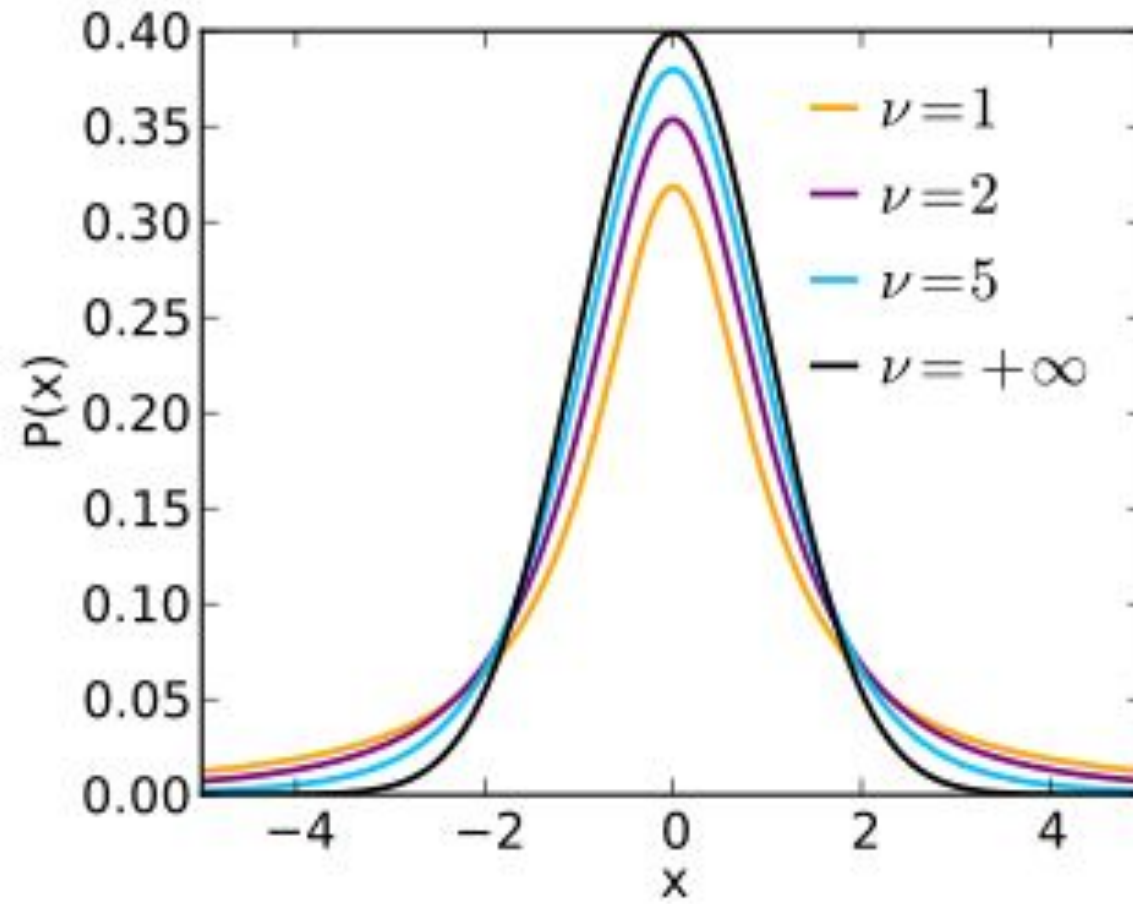
The t -statistic for comparing two samples is:

$$t = \frac{\overline{X}_1 - \overline{X}_2}{s_{1,2} \sqrt{2/N}}$$

where the *mutual* or *joint* standard deviation is given by:

$$s_{1,2} = \sqrt{\frac{\text{var}(X_1) + \text{var}(X_2)}{2}}$$

The t -Distribution



- ν is the number of degrees of freedom
- the distribution narrows (approaches normal distribution) as ν gets larger

Lab 3.2.2: Statistical Proof

- Purpose:
 - To learn how to use the Student's t -test for comparing two samples and accept or reject hypotheses.
- Materials:
 - 'Lab 3.2.2.ipynb'

Statistical Errors

Type I errors

- **false positives (FP)**
- we erroneously **rejected** the null hypothesis

Type II errors

- **false negatives (FN)**
 - we erroneously **upheld** the null hypothesis
-
- predicted positives $PP = TP + FP$
 - predicted negatives $PN = TN + FN$
 - actual positives $P = TP + FN$
 - actual negatives $N = TN + FP$

Statistical Errors – cont'd

sensitivity, recall

- true positive rate (FPR)

$$= TP / P$$

$$= TP / (TP + FN)$$

$$= 1 - FNR$$

specificity, precision

- true negative rate (TNR)

$$= TN / N$$

$$= TN / (TN + FP)$$

$$= 1 - FPR$$

confusion matrix

		True condition	
		Condition positive	Condition negative
Predicted condition	Predicted condition positive	True positive, Power	False positive, Type I error
	Predicted condition negative	False negative, Type II error	True negative

Discussion

- Is it sufficient to declare statistical significance at $p < 0.05$?
 - how much confidence is enough?
- Is it okay to mine for significance by testing each variable in turn?
 - how would we control the error estimate in multivariate testing?
- Resources:
 - Statistical Thinking for Managerial Decisions
<https://home.ubalt.edu/ntsbarsh/Business-stat/opre504.htm>
 - Statistics: The Art & Science of Learning from Data
<http://www.artofstat.com/webapps.html>

ANOVA

Analysis of variance

- generalises t -test to >2 samples (groups)
 - more conservative
 - reduces Type I errors
- decomposes data additively
 - compares mean squares, F -statistic
 - can test a nested sequence of models
- comprises a suite of methods
 - one-way, two-way, multiple

ANOVA – cont'd

One-way ANOVA

- F -statistic:

$$F = \frac{(\text{variance between groups})}{(\text{variance within groups})} = \frac{SS_T / (I - 1)}{SS_E / (n_T - I)}$$

I = number of groups

n_T = number of subjects

- compare this statistic to F -distribution for $I - 1, n_T - I$ degrees of freedom
- reject H_0 for $F \geq F_{\text{critical}}$

<https://www.marsja.se/four-ways-to-conduct-one-way-anovas-using-python/>

Statistical Power

def: the probability that the test correctly rejects the null hypothesis (H_0) when a specific alternative hypothesis (H_1) is true

example

- let A, B be the control & test cohorts:

$$D(N) = \frac{1}{N} \sum_{i=1}^N B_i - A_i$$

- define test statistic:

$$T(N) = \frac{D(N) - \mu_D}{\sigma_D / N}, \quad \mu_D = 0 \quad (H_0)$$

Statistical Power – cont'd

- specify $p < 0.05$ for significance
- from the t -distribution, $p = 0.05$ corresponds to $t = 1.64$
- therefore, to reject H_0 we require:

$$T(N) > 1.64$$

- specify power > 0.9 to detect $\mu_D > 1$
- after a few more steps, we obtain this requirement:

$$N > 8.56 \sigma_D$$

Statistical Power – cont'd

Errors and Power in Significance Testing

Select null hypothesis value p_0 :

Type of alternative hypothesis:
☒ greater ☐ not equal ☐ less

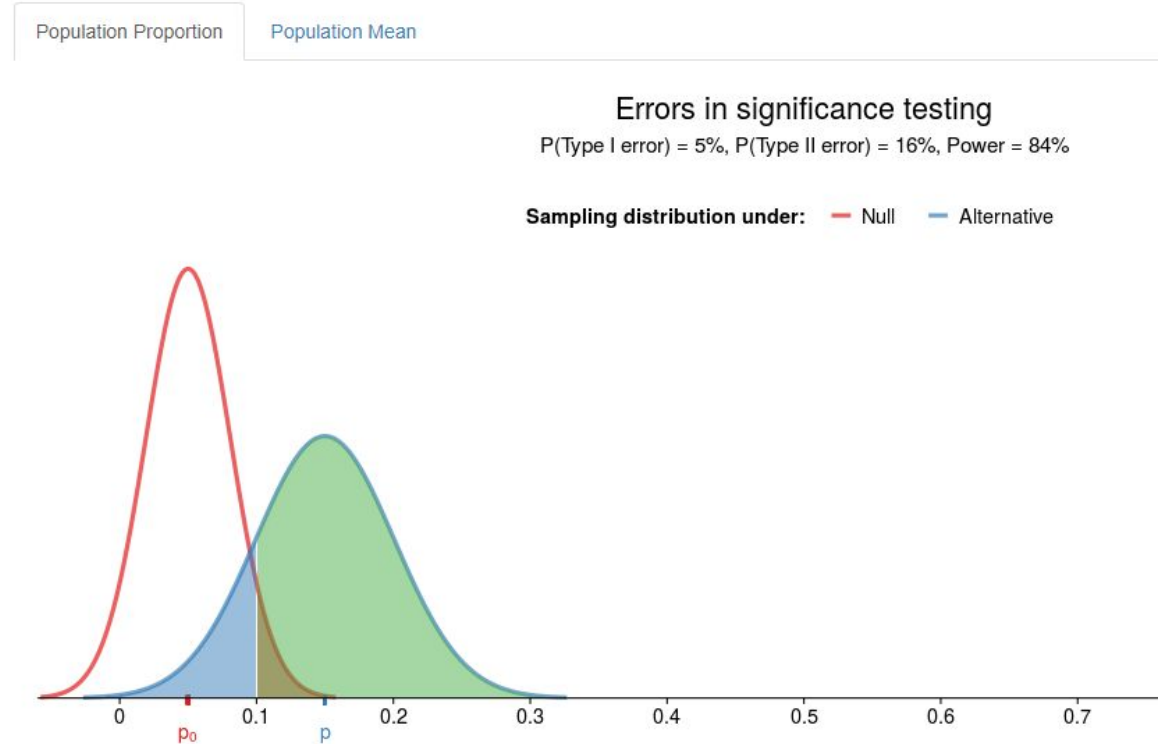
Show:
☒ Type I error ☒ Type II error ☒ Power

True value of p :

Sample size n :

Type I Error α :

Download Graph



<https://istats.shinyapps.io/power/>

Controlled Trials

objectives:

- to evaluate an experimental cohort (**test group**) against a baseline (**control group**)
- to measure every **factor** that has the potential to **influence** the response variable



challenges / considerations:

- the control group must be **representative** of the test group in **every way except** for the influence of the effect that is under test
- if we have limited understanding of the phenomenon, we may neglect important variables

Randomised Controlled Trials

objective:

- to **minimise experimental bias** by evenly distributing uncontrolled variables between the study cohorts

challenges / considerations:

- different **classes** of subjects should be **evenly distributed** between cohorts
 - e.g. age range, weight range, sex, medical status
 - requires data profiling of subjects prior to commencing experiment
- others?

Blind Randomised Controlled Trials

blind

- subjects do not know if they have been allocated to the test group or the control group



double blind

- experimenters do not know which individuals are test subjects or control subjects
- only the analysts know!

A/B Testing

def: a **randomised experiment** with two variants

examples

- evaluate / compare options for improving performance
 - marketing campaigns
 - website engagement
 - product variants
- conversion rate
 - proportion of sales resulting from all visits
- funnel
 - stages from visit through to conversion

Experimental Design for Big Data

- processing **time** (**cost**)
 - **sample** small subsets of the data
 - design the experiment, validate analytic methods before progressing to full dataset
 - for time-dependent data, need to sample many epochs so that periodicity is captured
- the **curse of high-dimensionality**
 - special methods required when number of features $\sim 10^3$
 - $O(n^2)$ algorithms too slow
 - exploit **sparseness** where possible
 - large number of features \rightarrow many **spurious correlations**



Causation

- Causation vs correlation
- Domain knowledge

Causation vs Correlation

example:

- a study finds that homicide correlates with ice cream consumption
 - what does this mean?

Headline #1: *'Ice Cream Linked to Murder'*

- scientists are desperately trying to discover which brands or flavours of ice cream are driving the murder rate

Headline #2: *'Heat Wave Pushes Murder Rate Up'*

- scientists suspect elevated brain temperatures increase mental instability
- meanwhile, ice cream sales are soaring

Causation vs Correlation – cont'd

A few cups of coffee may lower colon cancer risk

Posted: 01 August 2007 17:08 hrs

TOKYO : Drinking a few cups of coffee a day may lower the risk of advanced colon cancer, at least for women, Japanese researchers said Wednesday.

The study, supported by Japan's health ministry, showed women who drink more than three cups of coffee a day were 56 percent less likely to develop advanced colon cancer than those who drink no coffee at all.

"Drinking coffee sustains the secretion of bile acid and keeps down cholesterol levels, the mechanisms thought to prevent colon cancer," the report said.

But unfortunately the effect was not seen in men, the medical research team said.

Many men smoke and drink alcohol more than women, and those habits probably offset the effect of coffee, the study said.

The research team tracked down about 96,000 people in Japan aged from 40 to 69 between the early 1990s and 2002, of whom 726 men suffered colon cancer.



Photos

CancerConsultants.com
oncology resource center

Start CME

Critical Choices for Improving Outcomes in Renal Cell Carcinoma

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Cancer News: Rectal Cancer Article

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Rectal Cancer News

Coffee Does Not Decrease Risk of Colorectal Cancer

Researchers from the Harvard School of Public Health have reported that, contrary to the results of several previous studies, coffee consumption does not appear to reduce the risk of colorectal cancer. The details of this study were reported in the April 1, 2009 issue of the *International Journal of Cancer*.^[1]

Habitual coffee drinking has been associated with a reduced risk of mortality and chronic diseases, including cancer. Current evidence suggests that coffee consumption is associated with a reduced risk of liver, kidney, and to a lesser extent, premenopausal breast cancer and colorectal cancer; coffee consumption has no association with prostate, pancreas, and ovarian cancers.

Some studies have indicated that coffee may have a protective effect against colon cancer; however, researchers continue to evaluate this link in an effort to establish more direct evidence. In order to examine the relationship between coffee consumption and colorectal cancer, researchers from Harvard conducted a review of 12 studies that included 646,846 participants and 5,403 cases of colorectal cancer.

They evaluated high versus low coffee consumption and found no significant effect of coffee consumption on colorectal cancer risk. The review

Causation vs Correlation – cont'd

Simpson's paradox

- a trend appears in different groups of data but disappears or reverses when these groups are combined
 - common in social-science and medical-science statistics
https://en.wikipedia.org/wiki/Simpson%27s_paradox
- caused by **experimental bias**
- results in H_0 rejected despite insufficient statistical power
 - difference in means is too small
 - variances are too large
 - number of samples is too small

Can't we just use 'common sense'?

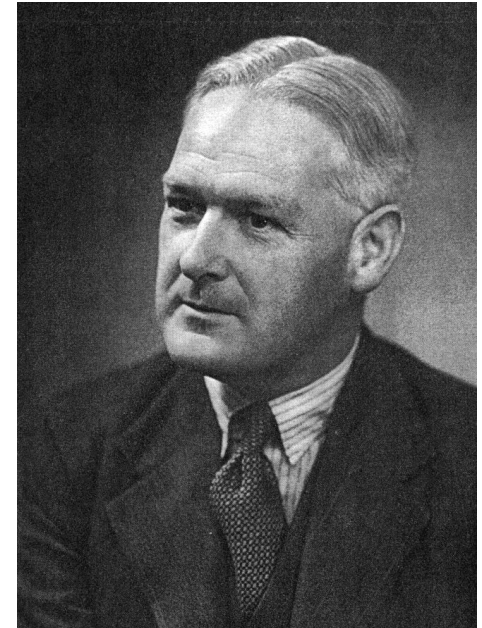
Common sense is the collection of
prejudices acquired by age eighteen.

Albert Einstein

Criteria for Evaluating Causation

- **Strength of association**
- Consistency
- Specificity
- Temporality
- Biological gradient
- Plausibility
- Coherence
- **Experiment**
- Analogy
- *Reversibility (not the original list)*

> subject matter expertise + statistics + reasoning



Bradford Hill

Lab 3.2.3: Statistical Inference

- Purpose:
 - To consolidate the basic concepts of sampling and distributions.
- Materials:
 - 'Lab 3.2.3.ipynb'